FOCUS Semileptonic and Rare Decays (a retrospective)

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Fixed Target Semileptonics (a stepping stone process)

Typically, kinematics can not be closed (no energy constraint) and though statistics can be sizable, backgrounds can be large compared to e⁺e⁻ experiments, like CLEO-C (or BES-III)...



Fixed Target Semileptonics

• ...But factorizable if you can measure or estimate the backgrounds FOCUS $D^+ \rightarrow \rho \mu^+ \nu$ (All Phys.Lett. B:637,32-38)

the backgrounds

• And

$$D^{+} \rightarrow (K^{-}\pi^{+}) \mu^{+} \nu$$

Is the Key to it all
FOCUS $D^{+} \rightarrow (K^{-}\pi^{+}) \mu^{+} \nu$







- Cabibbo-favored
- Important background in other modes
- Very little excited mode feed-down
- FOCUS Cerenkov separates K/pi/e well
- Long lifetime = large vertex separation
- In principle, well understood decay but
 - FOCUS found a surprise...

FOCUS saw discrepancies in the data



 $\frac{d^2\Gamma}{d\cos\theta_V d\cos\theta_\ell} \propto \{(1+\cos\theta_\ell)^2\Gamma_+ + (1-\cos\theta_\ell)^2\Gamma_-\}\sin^2\theta_V + 4\sin^2\theta_\ell\cos^2\theta_V\Gamma_0$ Prefers W spin along muon,e
Prefer L_z=0



FOCUS BR Measurements



FOCUS Form Factors $D^+ \to \overline{K}^{*0} \mu^+ \nu$

$$H_{\pm}(q^{2}) = (M_{D} + m_{K\pi})A_{1}(q^{2}) \mp 2 \frac{M_{D}K}{M_{D} + m_{K\pi}}V(q^{2}) \qquad H_{t}(q^{2}) \text{ has } m_{\mu}^{2} \text{ factor, set} = 0$$

$$H_{0}(q^{2}) = \frac{1}{2m_{K\pi}\sqrt{q^{2}}} \left[(M_{D}^{2} - m_{K\pi}^{2} - q^{2})(M_{D} + m_{K\pi})A_{1}(q^{2}) - 4 \frac{M_{D}^{2}K^{2}}{M_{D} + m_{K\pi}}A_{2}(q^{2}) \right] \qquad \text{Tried in fit, no sensitivity}$$

$$A_{i}(q^{2}) = \frac{A_{i}(0)}{1 - q^{2}/M_{A}^{2}}, (M_{A} = 2.5 \text{ GeV}/c^{2}) \qquad V(q^{2}) = \frac{V(0)}{1 - q^{2}/M_{V}^{2}}, (M_{V} = 2.1 \text{ GeV}/c^{2})$$

Fit to
$$\boxed{r_{v} = \frac{V(0)}{A_{1}(0)}} \qquad r_{2} = \frac{A_{2}(0)}{A_{1}(0)} \qquad \text{and S-wave parameters, } A \text{ and } \delta$$

(common – vary generated parameters in Montecarlo
 by using agreement with reconstructed distributions and data)
 Pioneered by D.M. Schmidt for E691 K*ev analysis: NIM A 328 (1993)

1st find S-wave with PDG r's,

3 bins in $\cos\theta_{V}$, 3 in $\cos\theta_{\ell}$, 3 in χ and 4 in $m_{K\pi}$ **S-wave term Breaks symmetry** 5 bins in $\cos\theta_{V}$, 5 in $\cos\theta_{\ell}$, 3 in $|\chi|$ and 3 in q^{2}/q_{max}^{2}

FOCUS Form Factors



Cuts similar to previous, some change to get uniform acceptance, one extra

OoM – Charm vertex outside of target and silicon by $1\sigma_{\scriptscriptstyle Vertex}$

Cut on $q^2 < 0.2 \text{ GeV}^2/c^2$

Goodness of fit issue

2000 right sign 10 GeV/c² KR rong sign Systematic Checks 1500 S-wave – varied cuts 1000 events 35 fits – Sample Variance 500 $A = 0.330 \pm 0.022 \pm 0.015$ Form Factor (3 sources) Varied Cuts 1) $\delta = 0.68 \pm 0.07 \pm 0.05$ 1.20.8 1.0 2) Split sample M(Kπ), GeV/c² 1000 \pm (stat) \pm (sys) $P_D, DD, m_{K\pi} (0.9 \, GeV / c^2)$ £0.0 ₩ 3) Vary MC input 600 events Right sign – Wrong sign Charm Backgrounds $r_{V} = 1.504 \pm 0.057 \pm 0.039$ 400 $-2 < \frac{A_3(0)}{A_1(0)} < 2$ 200 $r2 = 0.875 \pm 0.049 \pm 0.064$ 0.0 0.2 0.4 0.6 0.8 1.0 q^2/q^2_{max} Charm Phys.Lett.B544:89-96, 2002 Background

r's are flat, feeling m_?

FOCUS Form Factors $D^+ \to \overline{K}^{*0} \mu^+ \nu$

Non-Parametric test to look at single pole dominance ansatz (esp choice for s-wave) - Build up bin-wise transform of form factors

- Transform back from data to get projections, then fit using SPD model

 $\int |A|^2 d\chi = \frac{q^2 - m_\ell^2}{8} \left(\left\{ (1 + \cos \theta_\ell)^2 |BW|^2 |H_+(q^2)|^2 + (1 - \cos \theta_\ell)^2 |BW|^2 |H_-(q^2)|^2 \right\} \sin^2 \theta_V$

+ $2\sin^2\theta_{\ell}\cos^2\theta_{V}|BW|^2H_0^2(q^2)$ + $8\sin^2\theta_{\ell}\cos\theta_{V}H_0(q^2)h_0(q^2)\operatorname{Re}\{A_{S}e^{-i\delta}BW\})$ Monte Carlo Data



Challenges at low q² persist even in the latest CLEO-c results

FOCUS Form Factors $D_S^+ \rightarrow \phi \mu^+ \nu$

Similar to K* (should be similar via SU(3)), but S-wave not apparent here (< 5% at least) -Data (Histogram) compared to fit + ccbar Bkgnd (dots) and just ccbar Bkgnd (dashed)

Phys.Lett.B586:183-190,2004



March towards $D^0 \rightarrow K^- \mu^+ v$

- With the K* analisysis done, we were ready to tackle the neutral D pseuoscalar decays
 - The dream was to compare to LQCD, E687
 - K* feed-down important to know
- Problem! We didn't agree with CLEO result:

Phys. Rev. Lett. 89, 222001, 2002

 $\frac{D^+ \to \overline{K}^{*0} e^+ v}{D^+ \to \overline{K}^0 e^+ v} = 0.99 \pm 0.16$

Previous (E687 muon) result compared D⁰ and D⁺: 0.62 ± 0.11 (Phys. Lett. B 364, 127, 1995)

- Problem! PDG results (incl. 2003 partial update) looked very interesting (diff at 99% CL) $\Gamma(D^+ \to \overline{K}^0 e^+ v) - \Gamma(D^0 \to \overline{K}^- e^+ v) = -25 \pm 9.7 \text{ ns}^{-1}$
- So we decided to measure $D^+ \rightarrow \overline{K}^{*0} \mu^+ \nu$

$$D^+ \to \overline{K}{}^0 \mu^+ \nu$$

March towards $D^0 \rightarrow K^- \mu^+ \nu$



And there is better agreement between D⁰ and D⁺

$$\Gamma(D^+ \to \overline{K}^0 \mu^+ \upsilon) - \Gamma(D^0 \to \overline{K}^- \mu^+ \upsilon) = 11 \pm 11 \, \text{ns}^{-1}$$

FOCUS Form Factors

- Use D* tag to get cleaner signal, help close kinematics
 - In $K\mu$ CM frame D, ν solutions on a cone D, $\nu_{\text{(cone)}}$
 - Boost cone to lab, compare D direction
 - Choose best χ^2 , cut on CL of agreement

- Two techniques for fitting
 - Non-parametric deconvolution (remember K*?)
 - Only for $D^0 \to K^- \mu^+ \nu$
 - Discrete transform
 - Fit only to parameterized function $D^0 \rightarrow K^- \mu^+ v \& \pi^- \mu^+ v$
 - Use for BR too

π

Κ

(picture from speakers thesis...very dusty)

FOCUS Form Factors $D^0 \rightarrow K^- \mu^+ \nu \& \pi^- \mu^+ \nu$

Backgrounds are more challenging for the pion mode, similar to B-> π lv in Babar/Belle



FOCUS Form Factors (&BR) $D^0 \rightarrow K^- \mu^+ \nu \& \pi^- \mu^+ \nu$



$$\frac{\Gamma(D^0 \to \pi^- \mu^+ \nu)}{\Gamma(D^0 \to K^- \mu^+ \nu)} = 0.074 \pm 0.008 \pm 0.007$$
$$\frac{\left|\frac{V_{cd}}{V_{cd}}\right|^2}{\left|\frac{f_{\pm}^{\pi}(0)}{e^{K_{c}(0)}}\right|^2} = 0.037 \pm 0.004 \pm 0.004$$

 $\frac{\Gamma(D^0 \to \pi^- e^+ \nu)}{\Gamma(D^0 \to K^- e^+ \nu)} = 0.082 \pm 0.003$ (My calculations from the CLEO – c Paper) $\frac{\left|\frac{V_{cd}}{V_{cs}}\right|^2 \left|\frac{f_+^{\pi}(0)}{f_+^{K}(0)}\right|^2}{\left|\frac{f_+^{\pi}(0)}{f_+^{K}(0)}\right|^2} = 0.041 \pm 0.002$





FOCUS last Semileptonic BR

Phys.Lett. B:637,32-38, 2005



$$\frac{D^+ \to \rho \mu^+ \nu}{D^+ \to \overline{K}^{*0} \mu^+ \nu} = 0.041 \pm 0.006 \pm 0.004$$

Tour de-force in the Background Est Did w/constraints and w/o (many)

 $\frac{D^+ \to \rho \mu^+}{D^+ \to \overline{K}^{*0} \mu^+}$

Decay Mode	Total Yield	Yield in signal region		
$D^+ \to \rho^0 \mu^+ \nu$	320 ± 44	282		
$D^+ \to K^- \pi^+ \mu^+ \nu$	68^{a}	44		
$D^+ \to K^0_S \mu^+ \nu$	7 ± 6	0		
D_s^+ modes total	179 ± 40	101		
$D^+ \to \omega \mu^+ \nu$	51 ± 22	10		
Muon Mis-Id	550 ± 44	263		
Combinatoric	233 ± 50	99		

Systematics : different event selections, alternative fit methods, consistency of results between split samples, varying input parameters

PDG fit to e mode: 0.039 +/- 0.007 My estimate from CLEO-c e modes from HQL2010 & PRD 81:112001, 2010 = 0.042 +/- 0.003

Rare Charm Decays

Potential FCNC Decays are Suppressed

Box Diagrams are Smallish for Charm



No Top Quuark in the loop

Short Distance





Rare Decay Results from FOCUS $D^+_{(S)} \rightarrow (\pi, K)^{\pm} \mu^{\mp} \mu^+$

Decay Mode	Dual Bootstrap	Sensitivity	Sys. Error	Result W/sys	Single Cut(w/sys)	Previous (E791)
D ⁺ ⇔K⁺µ⁺µ⁻	9.1x10 ⁻⁶	7.5x10 ⁻⁶	7.5%	9.2x10 ⁻⁶	12x10 ⁻⁶	44x10 ⁻⁶
D ⁺ ⇔K⁻μ⁺μ⁺	13x10 ⁻⁶	4.8x10 ⁻⁶	7.5%	13x10 ⁻⁶	12x10 ⁻⁶	120x10 ⁻⁶
D ⁺ ⇔π⁺μ⁺μ⁻	8.8x10 ⁻⁶	7.6x10 ⁻⁶	7.5%	8.8x10 ⁻⁶	7.4x10 ⁻⁶	15x10 ⁻⁶
D ⁺ ⇔π⁻μ⁺μ⁺	4.9x10 ⁻⁶	5.6x10 ⁻⁶	7.5%	4.8x10 ⁻⁶	5.2x10 ⁻⁶	17x10 ⁻⁶
D _s ⁺ ⇔K⁺μ⁺μ⁻	3.3x10 ⁻⁵	3.3x10 ⁻⁵	27.5%	3.6x10 ⁻⁵	3.8x10 ⁻⁵	1.4x10 ⁻⁴
D _s ⁺ ⇔K ⁻ μ ⁺ μ ⁺	1.3x10 ⁻⁵	2.1x10 ⁻⁵	27.5%	1.3x10 ⁻⁵	2.0x10 ⁻⁵	1.8x10 ⁻⁴
D _s ⁺ ⇔π ⁺ μ ⁺ μ ⁻	2.4x10 ⁻⁵	3.1x10⁻⁵	27.5%	2.6x10 ⁻⁵	1.8x10⁻⁵	1.4x10 ⁻⁴
D _s ⁺ ⇔π ⁻ μ ⁺ μ ⁺	2.6x10 ⁻⁵	2.3x10 ⁻⁵	27.5%	2.9x10 ⁻⁵	2.2x10 ⁻⁵	0.8x10 ⁻⁴

(E687)

Dominated by PDG rate to normalizing mode ²¹

Situation almost the same as in 2003



FOCUS Round-UP

- We had some pioneering results
 - S-wave in the K* mode
 - Running comparison to LQCD
 - Non-parametric and cone-closure techniques
 - Remember that our results built up over time as we learned more about the realities of the higher statistics environment
- Our results seem to have held up well
 - There's still an opportunity to improve many FOCUS results, 13 years after data taking ended
- Apologies to others experiments I left out
 - (And for not mentioning the K* width measurement)
 - And experiments that never got a chance to run...