

Charmonium and charm spectroscopy from Lattice QCD

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Outline

1. Advantages of lattice QCD
2. Lattice objectives
3. Lattice challenges
4. Lattice results
5. Conclusions

What is new and not new this year?

- ▶ Predictions of exotics and excited states.
 - ▶ Status unchanged. I will review briefly.
- ▶ Gold-plated masses: that is, ones with no complications from open charm. Examples: charmonium spectrum below the $\psi(2S)$.
 - ▶ Significant progress in methods.
 - ▶ The term “precision” is often used.
 - ▶ Points the way to improvements in all quantities.

Advantages of lattice QCD

- ▶ Nonperturbative *ab initio* method for solving QCD.
- ▶ Charm and bottom, heavy-light and heavy-heavy, all with the same basic tools.
- ▶ Now mature. Beginning to have an important impact on the analysis of experimental results.
- ▶ For some quantities, more precise than any other method. Some notable successes (Standard Model parameters)

$\alpha_{\overline{MS}}(M_Z, n_f = 5)$	0.1183(7)
$m_c(3\text{GeV}, n_f = 4)$	0.986(6) GeV
$m_b(10\text{GeV}, n_f = 5)$	3.617(25) GeV
$ V_{cb} $	$(39.7 \pm 0.7_{\text{exp}} \pm 0.7_{\text{theo}}) \times 10^{-3}$
$ V_{ub} $	$(3.38 \pm 0.36) \times 10^{-3}$

- ▶ **Predictions** confirmed later by experiment:
 - ▶ Shape of form factor for $D \rightarrow K\ell\nu$
 - ▶ $m(B_c)$, f_D , $m(\eta_b)$

[Kronfeld hep-lat/0607011, HPQCD arXiv:1004.4285]

Lattice objectives for charm physics

- ▶ Phenomenological
 - ▶ Spectroscopy
 - ★ Reproduce well-known results to verify methods.
 - ★ Help classify new levels: exotics, etc.
 - ▶ Decay constants (Simone and Na talks)
 - ▶ EM transitions
- ▶ Theoretical
 - ▶ Guidance for effective field theory

Lattice limitations

- ▶ Charmonium production (?)
- ▶ Inclusive processes (?)
- ▶ Multihadronic (> 2 -body) decays (?)

Lattice challenges

- ▶ Reducing lattice cutoff $1/a$ effects, especially for heavy quarks. $\mathcal{O}(Ma)$ errors are bad for charm and bottom when, typically $1/a \approx 1.8 - 3$ GeV.
 - ▶ Nonrelativistic QCD: expansion in p/M slow for charm, good for bottom.
 - ▶ Fermilab quarks good for both. Further improvements under study [Oktay, Kronfeld]
 - ▶ Highly Improved Staggered Quarks (HISQ) has $\mathcal{O}(\alpha_s^2(aM_c)^2)$: good for charm, not so good for bottom with today's lattices.
- ▶ Working with the correct sea quark masses. Most calculations are done with larger (m_u, m_d) and we extrapolate.
- ▶ Excited states. Ground state properties are easiest. Excited states more difficult.
- ▶ Multihadronic states, e.g., open charm are complicated. We are just beginning to learn how to treat them.

Toward precision lattice charmonium results

Through tackling the “gold-plated” quantities, we have learned what is required to do good lattice charm physics for all quantities:

- ▶ A heavy quark action with small discretization errors and an accurate tuning of the heavy quark masses.
- ▶ An accurate determination of the lattice scale.
- ▶ A full treatment of sea quarks. Simulate at the physical light quark masses or do a controlled extrapolation.
- ▶ A careful extrapolation to zero lattice spacing.
- ▶ Good interpolating operators and an adequate data sample.

Quarkonium spectroscopy

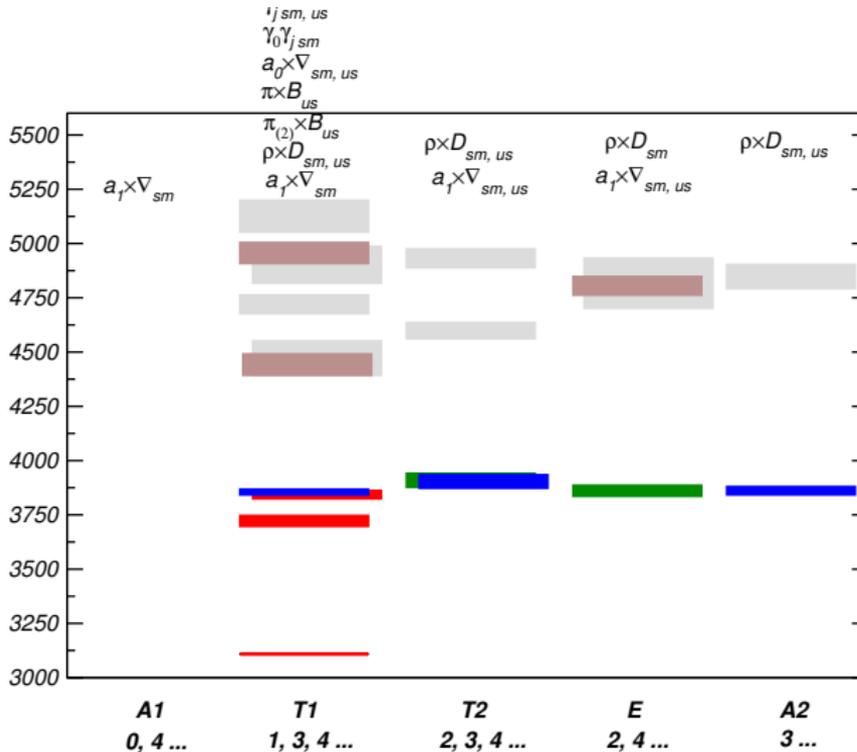
- ▶ Hadron masses are determined from propagators

$$C_{ij}(t) = \langle 0 | \mathcal{O}_i(t) \mathcal{O}_j(0) | 0 \rangle \rightarrow z_i^* z_j \exp(-mt) \text{ for large } t ,$$

where \mathcal{O}_i 's are suitable interpolating operators. For example, for the J/ψ we could use $\mathcal{O} = \bar{q}\gamma_\mu q$.

- ▶ Operators are classified according to lattice symmetries.
- ▶ The cubic group replaces the rotation group. A_1 replaces $J = 0$, T_1 replaces $J = 1$, etc.
- ▶ Ambiguities: A_1 sees $J = 0, 4, 6$; T_1 could be 1, 3, 4, etc. With a little effort we can often resolve them.
- ▶ If we use a large basis set \mathcal{O}_j for the same quantum numbers, we get a correlation matrix. The eigenvalues contain information about the ground and excited states. Several groups now use this method successfully.
- ▶ In the next slides I show a sample of results obtained by Dudek *et al.* (2007) using this method.

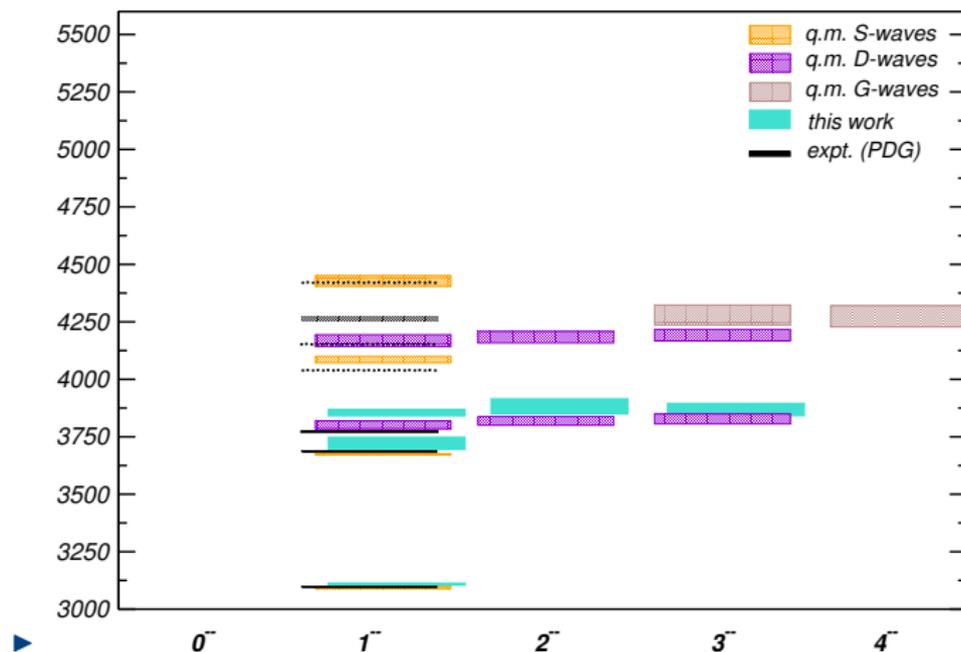
JLab quarkonium: J^{--} states



$J = 1$, $J = 2$, $J = 3$, Gray, brown: undetermined J .

[Dudek, Edwards, Mathur, and Richards, arXiv:0707.4162]

JLab quarkonium: J^{--} states



- ▶ Comparison with experimental masses and quark potential model masses. Tabulated masses in MeV.

[Dudek, Edwards, Mathur, and Richards, *op cit.*]

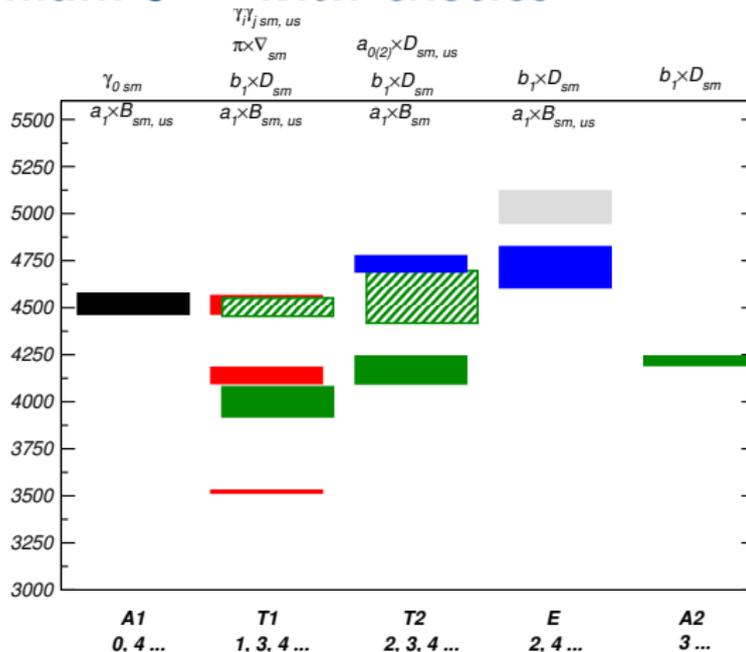
JLab quarkonium J^{--} with exotics

- ▶ How well does this work? Look at the T_1^{--} channel, where the ground state J/ψ has a very clean signal.

state	predict	PDG	difference
J/ψ	3109(2)	3097	12
$\psi(2S)$	3722(24)	3686	36
$\psi(3S)$	3855(12)	3773	82
$\psi(4040)$	3843(18)?	4039	-196
$\psi(4160)$	4472(79)?	4153	319
$\psi(4415)$	4442(48)?	4421	21

- ▶ Here ? means the authors did not make any assignment.
- ▶ Higher excitations: more difficult to assign J .
- ▶ Errors grow with excitation, as expected.
- ▶ When the ground state signal is not so clean, less can be extracted.

JLab quarkonium J^{+-} with exotics



$J = 0$, $J = 1$, $J = 2$, $J = 3$, Gray: undetermined J .

- ▶ Predict exotic 0^{+-} (4520), 2^{+-} (4600).
- ▶ Similarly, possibly exotic 1^{-+} (4700) [but could be a nonexotic 4^{-+}].

[Dudek, Edwards, Mathur, and Richards, *op cit.*]

Hadron Spectrum Collaboration quarkonium future

These results are pioneering and impressive, but ...

- ▶ No sea quarks (quenched approximation).
- ▶ Only one lattice spacing, so no continuum limit.
- ▶ No open charm states (none, anyway, in quenched approximation.)

The collaboration is currently remedying these shortcomings.

[Ryan, Lattice 2010]

Open charm mixing?

Causes level shifts. Is it significant?

- ▶ For static quarks, string breaking studies on the lattice suggest mixing is weak.
- ▶ For dynamical quarks, very little is known from lattice studies.
- ▶ Bali and Ehmman (Lattice 2009) studied mixing between S-wave charmonium and a $D\bar{D}$ “molecule” using a variational method.

state	$(c\bar{c})_l$	$(c\bar{c})_n$	$(c\bar{u}\bar{c}u)_l$	$(c\bar{u}\bar{c}u)_n$
η_c	0.54(3)	-0.02(1)	-0.1(1)	-0.31(5)
$D_1\bar{D}^*$	0.07(1)	0.01(1)	-0.46(8)	0.14(2)
J/ψ	0.51(4)	-0.03(1)	0.09(1)	0.21(6)
$D_1\bar{D}$	0.08(6)	0.04(1)	-0.18(1)	0.53(4)
χ_{c1}	0.39(5)	0.69(3)	-0.22(3)	-0.49(4)
$D\bar{D}^*$	0.63(4)	-0.23(3)	-0.73(4)	0.12(3)

- ▶ (“ l ” and “ n ” refer to different basis wave functions.)
- ▶ In some cases such as the χ_{c1} the mixing appears to be large, but a more thorough study is now needed.

[Bali, Ehmman, arXiv:0911.1238]

MILC Collaboration gauge field ensembles

- ▶ An example of the sort of resource needed.
- ▶ Parameters of a publicly available archive of gauge configurations based on u , d , and s sea quarks.

ensemble	a (approx) (fm)	sea quark ratio m_{ud}/m_s
Extra coarse	0.18	0.6, 0.4, 0.2, 0.1
Medium coarse	0.15	0.6, 0.4, 0.2, 0.1
Coarse	0.12	0.6, 0.4, 0.2, 0.15, 0.1
Fine	0.09	0.4, 0.2, 0.1, 0.05
Superfine	0.06	0.4, 0.2, 0.1
Ultrafine	0.045	0.2

- ▶ With these one can carry out an extrapolation to physical m_{ud} ($\approx 0.037m_s$) and $a = 0$ (continuum).

[MILC, Rev Mod Phys **82**, 1349 (2010)]

Progress in lattice actions and analysis campaigns

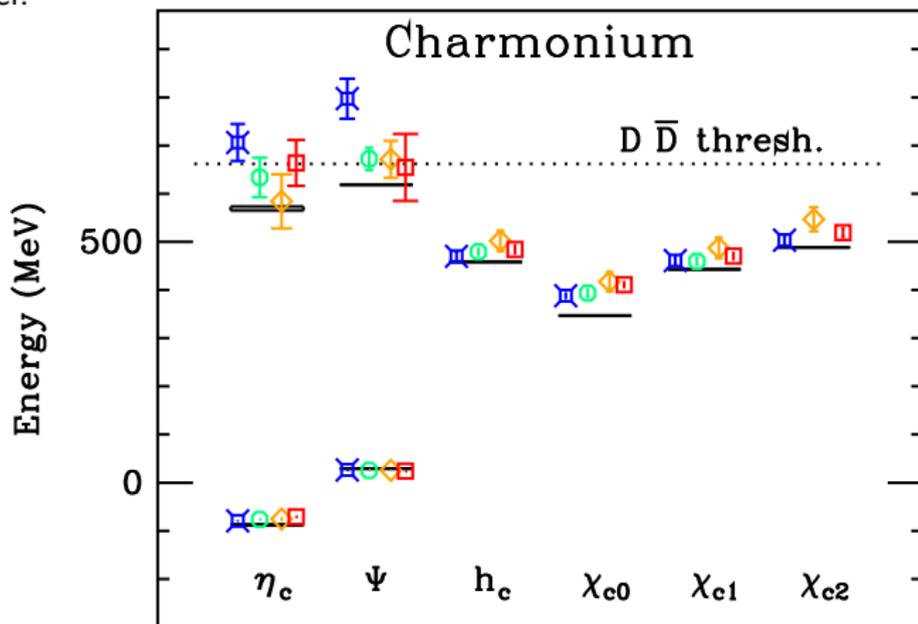
- ▶ Fermilab-Lattice/MILC collaboration
 - ▶ 2008/09 (old data) Fermilab charm and bottom-quark action (completed)
 - ▶ 2009/10 (new data - more statistics, smaller lattice spacing) Fermilab charm-quark action (in progress)
 - ▶ future (HISQ charm quark action, HISQ sea quarks, Fermilab bottom quark)
- ▶ HPQCD
 - ▶ 2006-2010 (HISQ charm-quark action, NRQCD bottom)
 - ▶ future (HISQ charm, sea, bottom quarks, and NRQCD bottom)

Fermilab-Lattice/MILC quarkonium 2008/09

- ▶ Fermilab action for heavy quarks: c and b
- ▶ MILC gauge ensembles.
- ▶ s , c , b quark masses tuned to physical values using light mesons and D_s and B_s .
- ▶ Measure only low-lying S and P wave states.
- ▶ Objective: Extrapolate to the physical point. Test methodology.

FNAL/MILC Overview

- ▶ Charmonium levels constructed from splittings from the spin-averaged $\overline{1S}$ level.

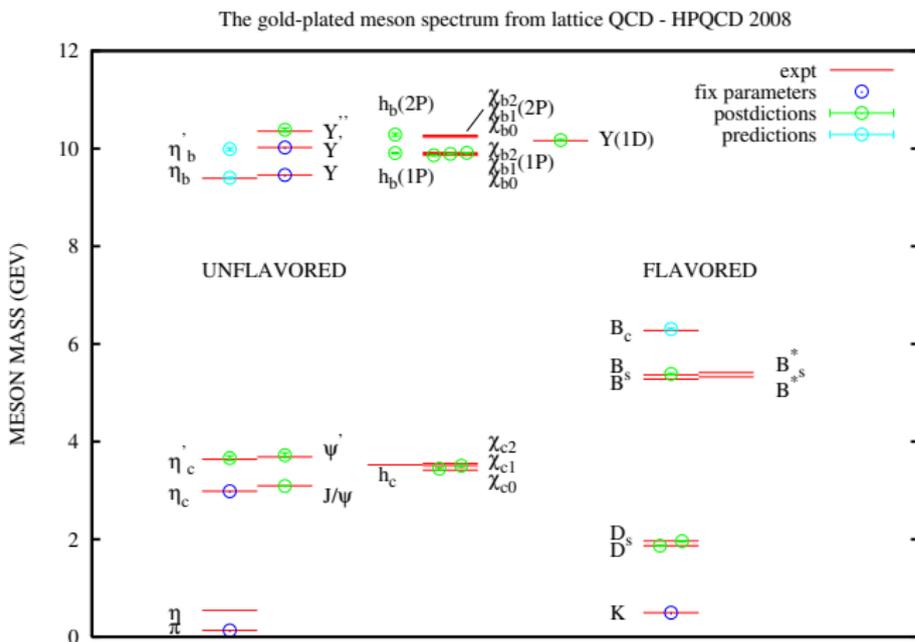


- ▶ Lattice spacings are 0.18 fm, 0.15 fm, 0.12 fm, 0.09 fm.

[MILC/FNAL, PRD 81, 034508 (2010)]

HPQCD Overview

- ▶ Gold-plated meson spectrum based on a subset of the MILC ensembles.



- ▶ Five states are used to get the four quark masses and lattice spacing.
- ▶ Three states were predictions.

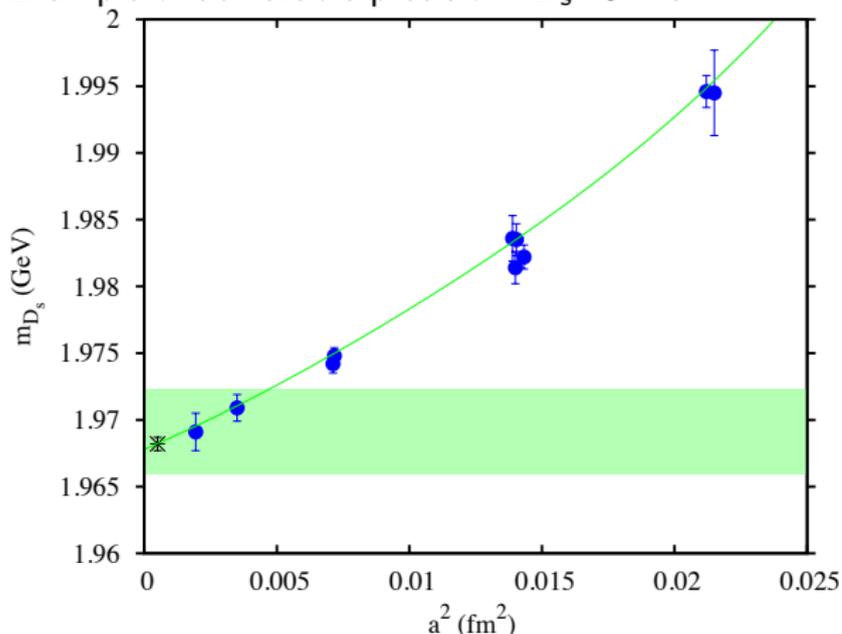
[HPQCD-PoS LATTICE2008, 118]

Overviews

- ▶ These pictures are nice but we don't appreciate the details on this scale.
- ▶ And we want more than just gold-plated states.

HPQCD D_s

Example of achievable precision: D_s : 3 MeV!

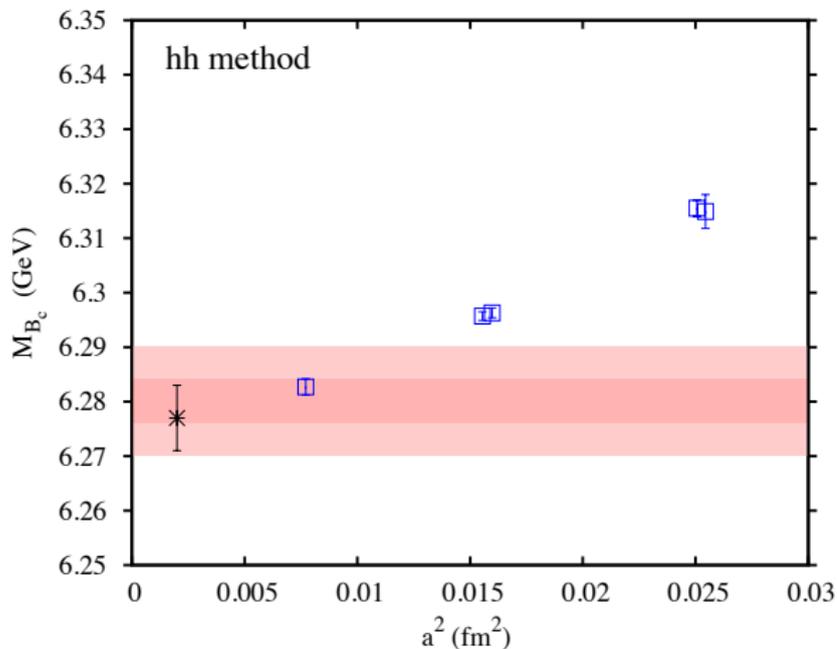


- ▶ Based on splitting $M(c\bar{s}) - \frac{1}{2}M(\eta_c)$
- ▶ PACS-CS Lattice 2009 result using their relativistic heavy quark action: 1.972(2) GeV vs expt 1.968. Error is statistical only.

[HPQCD, arXiv:1008.4018; PACS-CS arXiv:0911.5362]

HPQCD B_c

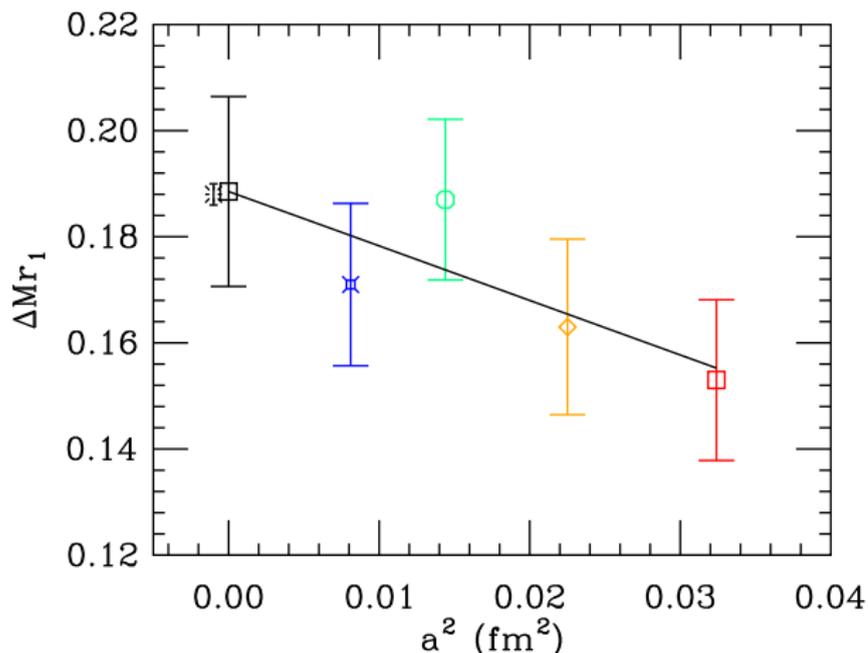
Example of achievable precision: B_c : 10 MeV!



- ▶ Based on splitting $M(B_c) - M(b\bar{b})/2 - M(\eta_c)/2$.
- ▶ Light shaded band includes all errors.

[HPQCD, arXiv:1010.3848]

MILC/FNAL 1S hyperfine splitting

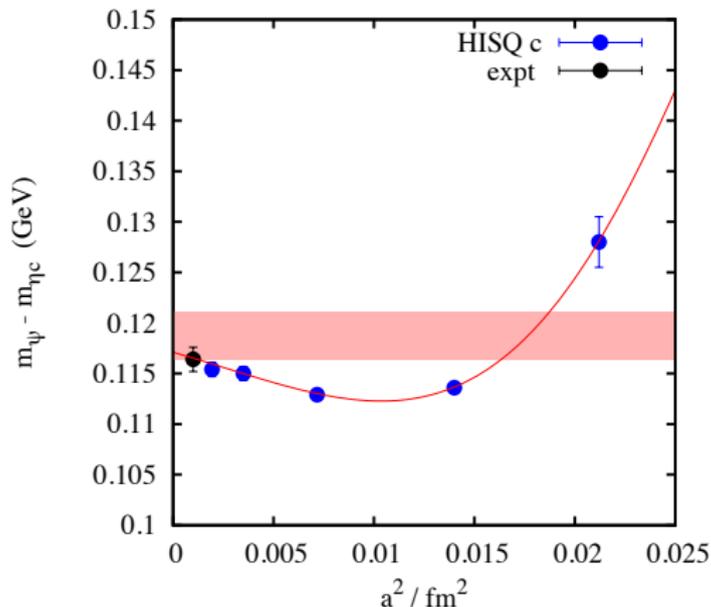


- ▶ Charm result 117(11) MeV.
- ▶ Annihilation effects are ignored here.

[FNAL/MILC PRD **81**, 034508 (2010)]

HPQCD 1S hyperfine splitting

HPQCD PRELIMINARY

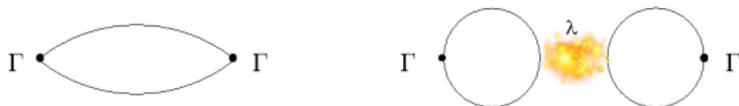


- ▶ Annihilation effects are estimated from perturbation theory. They and other corrections shift the result up to the pink band, which indicates all errors: 2 MeV

[HPQCD, private communication, 2010]

Annihilation contribution to charm HFS

Calculated from the lattice rather than perturbation theory.

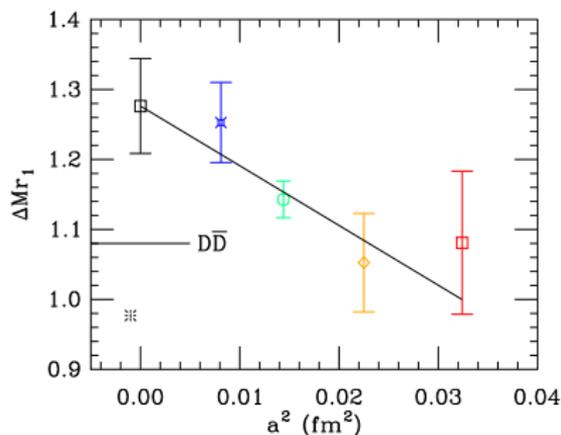


Connected and disconnected diagrams

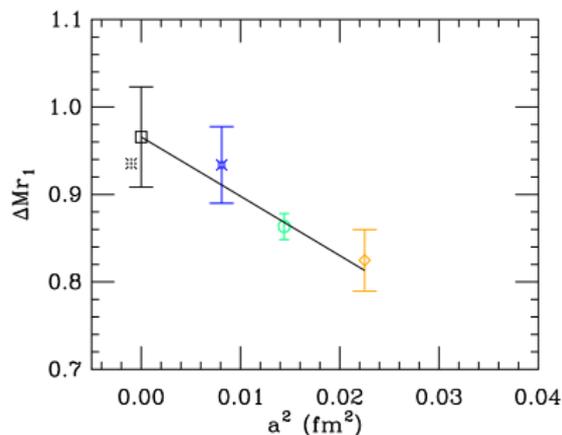
- ▶ Decreases the HFS splitting - by 1.6 to 7 MeV.
- ▶ Contrary to perturbation theory (partly due to axial anomaly).

[Levkova and DeTar, Lattice 2010]

MILC/FNAL $\overline{2S} - \overline{1S}$ splitting



Charmonium

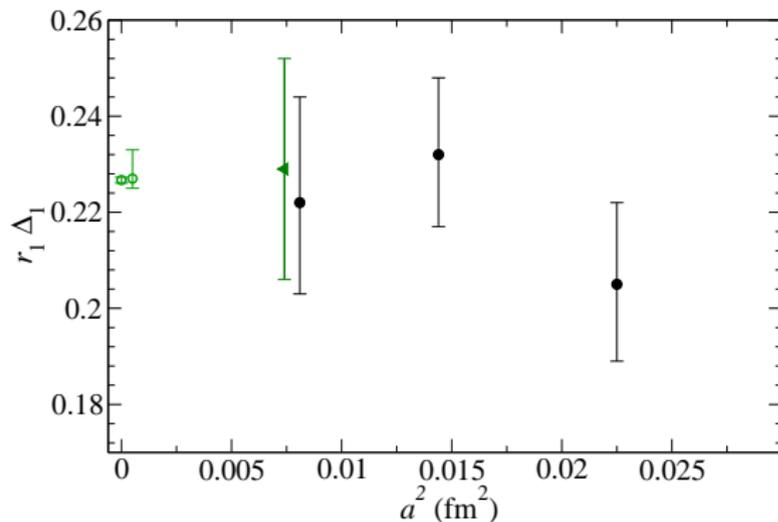


Bottomonium

- ▶ The calculation does not treat the open charm threshold.
- ▶ Note the open bottom threshold is safely off scale here.
- ▶ Is the disagreement in charmonium caused by open charm?

[FNAL/MILC PRD **81**, 034508 (2010)]

MILC/FNAL $D_S^* - D_S$



- ▶ Based on our “old” data.
- ▶ Splittings are in $r_1 = 0.311$ fm units here. ($1/r_1 = 635$ MeV).
- ▶ The green point includes discretization errors. Accuracy: 4 MeV.
- ▶ PACS-CS Lattice 2009 result with their relativistic heavy quark action: 135(3) MeV vs expt 144. (Statistical only.)

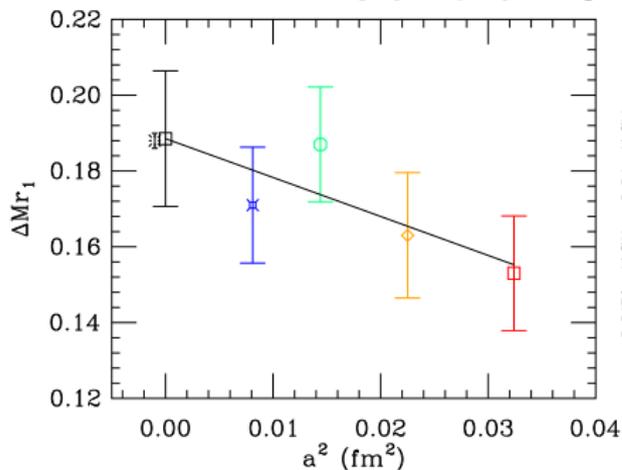
[FNAL/MILC arXiv:1003.1937, PACS-CS arXiv:0911.5362]

MILC/FNAL quarkonium future

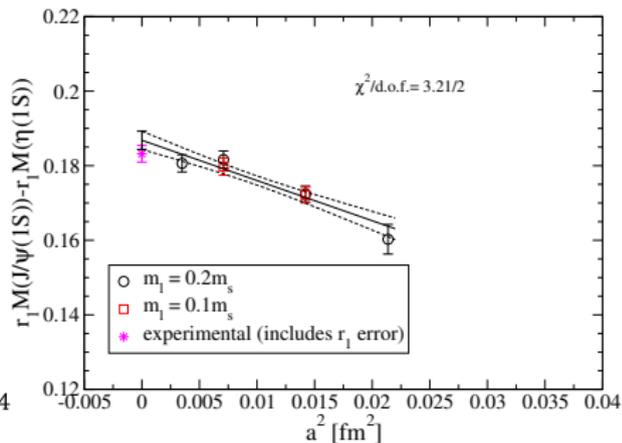
- ▶ Near term
 - ▶ New ongoing (2010) analysis with a JLab-style basis set to get higher states.
 - ▶ Finer lattices, more statistics.
- ▶ Longer term
 - ▶ HISQ charm with a large basis set.

Fermilab-Lattice/MILC quarkonium preview

Charmonium 1S hyperfine splitting



old data 2009



new data 2010

[FNAL/MILC 2010 PRELIMINARY]

Conclusions

- ▶ Improved lattice charm quark formulations yield high precision for gold-plated quantities.
- ▶ This experience is teaching us how to do good charm physics on the lattice.
- ▶ Gauge field ensembles at smaller lattice spacing enable significant reductions in errors for all quantities.
- ▶ Expect improvements in excited state and exotic predictions from the Hadron Spectrum and MILC/Fermilab Lattice collaborations.
- ▶ Treating two-hadron mixing (e.g. open charm) remains a challenge.