

Testing the light scalar meson as a non- $q\bar{q}$ state in semileptonic D decays

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Outline:

1. Introduction
2. Formalism
3. Results
4. Summary



Introduction

Light scalar meson (S_0)

- S_0 with masses below 1 GeV

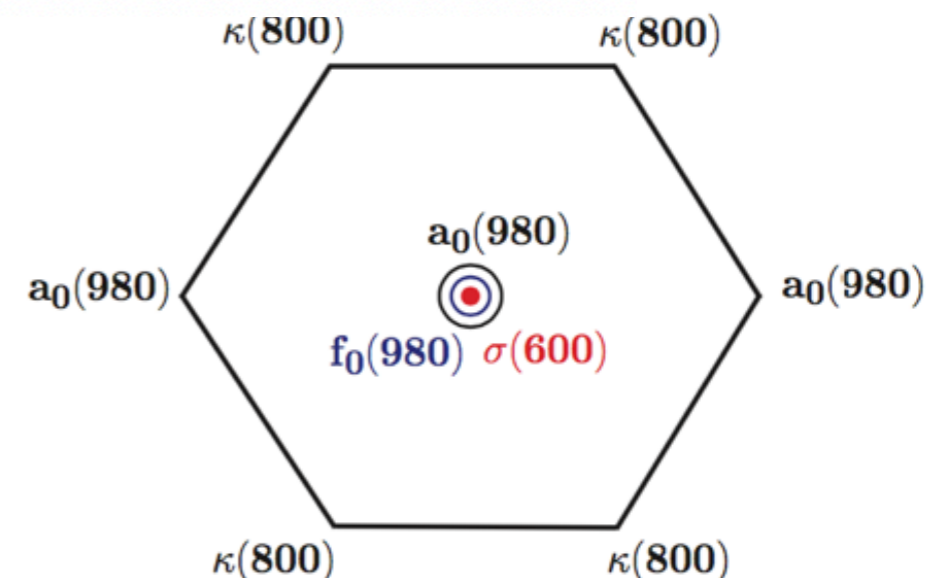
$$f_0 \equiv f_0(980), \sigma_0 \equiv f_0(500), a_0 \equiv a_0(980), \kappa \equiv K_0^*(700)$$

- Controversially, regarded as

the normal p-wave meson ($q\bar{q}$),

exotic tetraquark [compact $q^2\bar{q}^2$ bound state or

molecular M_1M_2 bound state.]

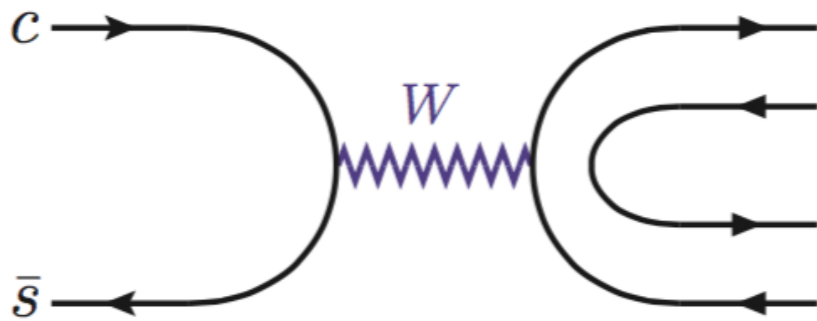


Introduction

- BESIII presented that

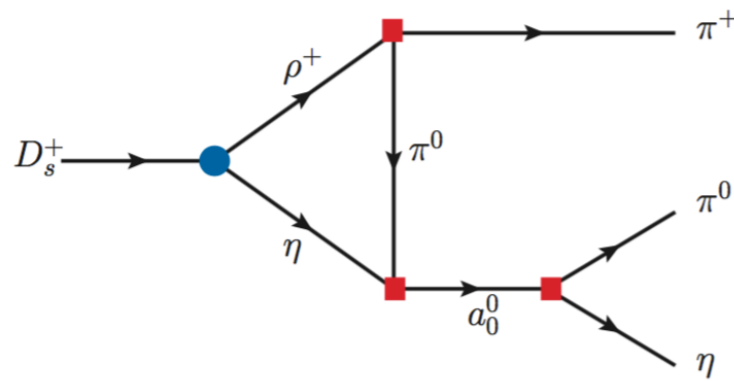
$$\mathcal{B}(D_s^+ \rightarrow \pi^{+(0)} a_0^{0(+)}, a_0^{0(+)} \rightarrow \pi^{0(+)} \eta) = (1.46 \pm 0.15 \pm 0.23) \times 10^{-2}$$

“Amplitude analysis of $D_s^+ \rightarrow \pi^+ \pi^0 \eta$ and first observation of the pure W -annihilation decays $D_s^+ \rightarrow a_0(980)^+ \pi^0$ and $D_s^+ \rightarrow a_0(980)^0 \pi^+$,” [PRL123,112001 (2019)]

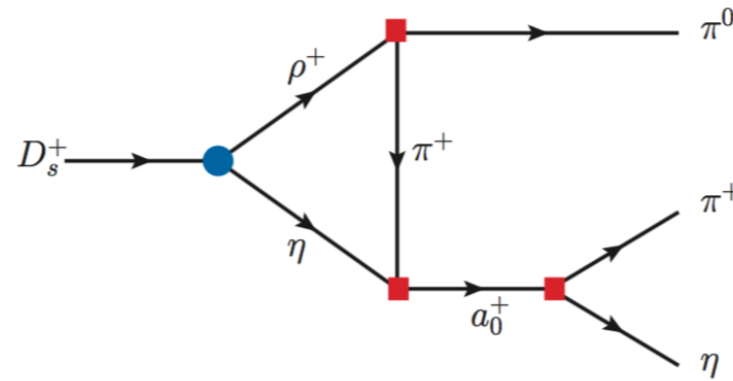


$$D_s^+ \rightarrow a_0^{0(+)} \pi^{+(0)}, a_0^{0(+)} \rightarrow \pi^{0(+)} \eta$$

Triangle rescattering as FSI [Hsiao, Yu, Ke, EPJC80, 895 (2020)].



(a)



(b)

$$\mathcal{B}(D_s^+ \rightarrow a_0^{0(+)} \pi^{+(0)}) = (1.7 \pm 0.2 \pm 0.1) \times 10^{-2},$$

$$\mathcal{B}(D_s^+ \rightarrow \pi^{+(0)} (a_0^{0(+)} \rightarrow) \pi^{0(+)} \eta) = (1.4 \pm 0.1 \pm 0.1) \times 10^{-2},$$

- $D_s^+ \rightarrow \pi^+(a_0^0 \rightarrow) \pi^0 \eta$ and $D_s^+ \rightarrow \pi^0(a_0^+ \rightarrow) \pi^+ \eta$

large interference with a relative phase of 180°

$$\rho^+(q_4) \rightarrow \pi^0(q_3) \pi^+(q_4 - q_3), \rho^+(q_4) \rightarrow \pi^+(q_3) \pi^0(q_4 - q_3)$$

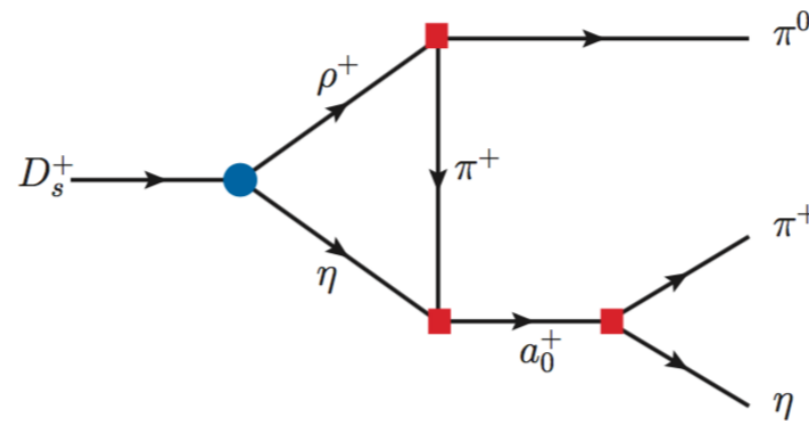
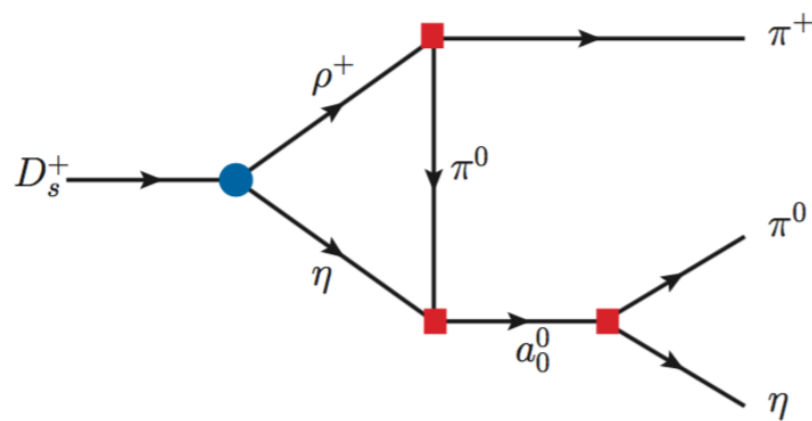
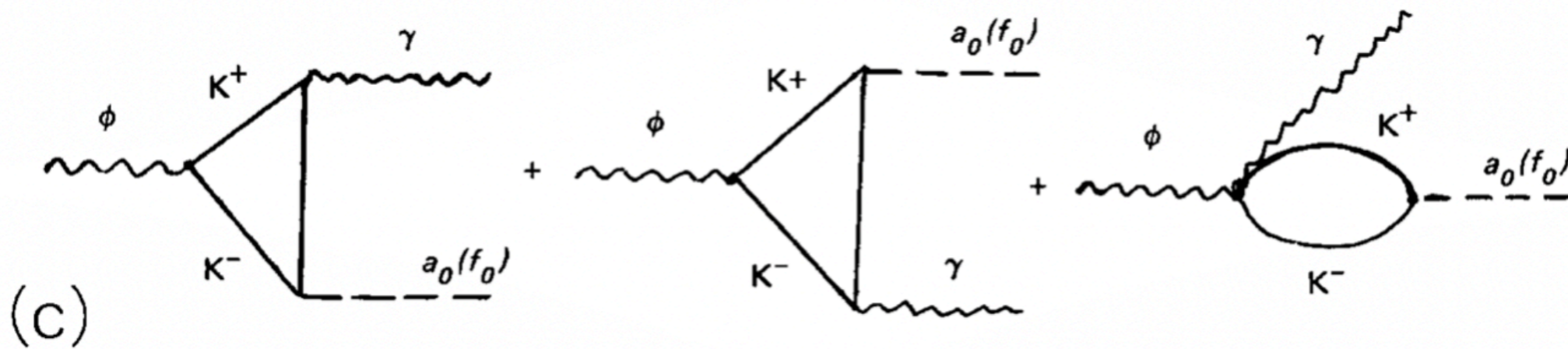
$$\mathcal{A}_a(\rho^+ \rightarrow \pi^+ \pi^0) = -\mathcal{A}_b(\rho^+ \rightarrow \pi^0 \pi^+)$$

30% cancellation to the total branching ratio.

$\mathcal{B}(\phi \rightarrow a_0 \gamma) \sim 10^{-4}$ from the kaon-loop calculation.

[Achasov, Ivanchenko, NPB315, 465 (1989)],

“On a Search for Four Quark States in Radiative Decays of ϕ Meson.”



• BESIII has recently measured that

1. PRD105, 3 (2022)

$$\mathcal{B}(D_s^+ \rightarrow f_0 e^+ \nu_e, f_0 \rightarrow \pi^0 \pi^0) = (7.9 \pm 1.4 \pm 0.3) \times 10^{-4},$$

$$\mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^0 \pi^0) < 6.4 \times 10^{-4} \text{ (90\% C.L.)}.$$

2. PRL132, 141901 (2024) [arXiv:2303.12927]

$$\mathcal{B}(D_s^+ \rightarrow f_0 e^+ \nu_e, f_0 \rightarrow \pi^+ \pi^-) = (1.72 \pm 0.13 \pm 0.10) \times 10^{-3}$$

$$\mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-) < 3.3 \times 10^{-4} \text{ (90\% C.L.)}.$$

Form factor (FF), extracted as

$$f^+(0)|V_{cs}| = 0.504 \pm 0.017 \pm 0.035, f^+(0) = f^+(p^2) \text{ at } p^2 = 0,$$

$|V_{cs}|$ the $c \rightarrow s$ CKM matrix element,

test the model calculations

TABLE I. Comparison of the FF at $q^2 = 0$ between our measurement and various theoretical predictions.

	This work	CLFD [6]	DR [6]	QCDSR [7]	QCDSR [8]	LCSR [9]	LFQM [11]	CCQM [12]
$f_+^{f_0}(0)$	$0.518 \pm 0.018_{\text{stat}} \pm 0.036_{\text{syst}}$	0.45	0.46	0.50 ± 0.13	0.48 ± 0.23	0.30 ± 0.03	0.24 ± 0.05	0.39 ± 0.02
Difference (σ)	—	—	—	0.1	0.2	4.3	4.3	2.8
ϕ in theory	—	$(32 \pm 4.8)^\circ$	$(41.3 \pm 5.5)^\circ$	35°	$(8_{-8}^{+21})^\circ$	—	$(56 \pm 7)^\circ$	31°

- a_0 , f_0 , and σ_0 in $q\bar{q}$ and $q^2\bar{q}^2$ pictures

$SU(3)$ relations, mixing scenarios

$|\theta| \simeq 20^\circ$ for $q\bar{q}$, $|\theta| < 10^\circ$ for $q^2\bar{q}^2$,

FFs for $q\bar{q}$ and $q^2\bar{q}^2$ can be very different

- extracting $f^+(0)$ from the data,

calculating $\mathcal{B}(D \rightarrow S_0 e^+ \nu, S_0 \rightarrow M_1 M_2)$

compared to the data

used to test the two quark contents

S_0 formation in weak decays, such as

- $D \rightarrow S_0 P$ [H. Y. Cheng, PRD67, 034024 (2003)],
“Hadronic D decays involving scalar mesons,”
- $D, B \rightarrow S_0 e^+ \nu$ [Wang, Lu, PRD82, 034016 (2010)],
“Distinguishing two kinds of scalar mesons from heavy meson decays,”
- $\bar{B}_{(s)}^0 \rightarrow J/\psi(f_0, \sigma_0)$ [Stone, Zhang, PRL (2013)], *“Use of $B \rightarrow J/\psi f_0$ decays to discern the $q\bar{q}$ or tetraquark nature of scalar mesons,”*

$D \rightarrow S_0 e^+ \nu_e$ and $D \rightarrow S_0 e^+ \nu_e, S_0 \rightarrow M_1 M_2$

• Used to investigate the quark constituents of the scalar meson:

1. Wang, Lu, PRD82, 034016 (2010), “*Distinguishing two kinds of scalar mesons from heavy meson decays.*”

2. Achasov, Kiselev, Shestakov, PRD102, 016022 (2020), “*Semileptonic decays $D \rightarrow \pi^+ \pi^- e^+ \nu_e$ and $D_s \rightarrow \pi^+ \pi^- e^+ \nu_e$ as the probe of constituent quark-antiquark pairs in the light scalar mesons*”

3. Achasov, Kiselev, Shestakov, PRD104, 016034 (2021), “*Semileptonic decays $D \rightarrow \eta \pi e \nu$ in the $a_0(980)$ region,*”
taking $a_0(980)$ as a tetraquark.

Amplitudes of $D \rightarrow S_0 e^+ \nu_e, S_0 \rightarrow M_1 M_2$

- $\mathcal{M}(D \rightarrow S_0 e^+ \nu_e) = \frac{G_F}{\sqrt{2}} V_{cq} \langle S_0 | \bar{q} \gamma_\mu (1 - \gamma_5) c | D \rangle \bar{u}_\nu \gamma_\mu (1 - \gamma_5) v_e,$
- $\langle S_0 | (\bar{q} c) | D \rangle = i(p_D + p_{S_0})_\mu f^+(p^2) + i \frac{m_D^2 - m_{S_0}^2}{p^2} p_\mu [f^0(p^2) - f^+(p^2)],$
- FFs with the double and single pole representations:

Becirevic, Kaidalov, PLB478, 417 (2000),

“Comment on the heavy \rightarrow light form-factors.”

$$f^+(p^2) = \frac{f(0)}{(1 - p^2/m_A^2)^2}, \quad f^0(p^2) = \frac{f(0)}{1 - p^2/m_B^2},$$

$f(0)$: $f(p^2)$ at $p^2 = 0$, pole masses: m_A and m_B .

FFs with 2 possible quark contents of S_0

- $q\bar{q}$:

$$|n\bar{n}\rangle \equiv |\sqrt{1/2}(u\bar{u} + d\bar{d})\rangle$$

$$|f_0\rangle = \cos\theta_I |s\bar{s}\rangle + \sin\theta_I |n\bar{n}\rangle,$$

$$|\sigma_0\rangle = -\sin\theta_I |s\bar{s}\rangle + \cos\theta_I |n\bar{n}\rangle,$$

$$|a_0^0\rangle = |\sqrt{1/2}(u\bar{u} - d\bar{d})\rangle, |a_0^-\rangle = |d\bar{u}\rangle,$$

- FFs with $q\bar{q}$: $D^+ \rightarrow d\bar{d} \rightarrow S_0$, $D_s^+ \rightarrow s\bar{s} \rightarrow S_0$,

$$f_n \equiv |n\bar{n}\rangle, f_s \equiv |s\bar{s}\rangle$$

$$\langle f_0, \sigma_0 | (\bar{d}c) | D^+ \rangle = (\sin\theta_I, \cos\theta_I) \times \langle f_n | (\bar{d}c) | D^+ \rangle,$$

$$\langle a_0^0 | (\bar{d}c) | D^+ \rangle = \sqrt{1/2} \langle a_0^- | (\bar{d}c) | D^0 \rangle = -\langle f_n | (\bar{d}c) | D^+ \rangle,$$

$$\langle f_0, \sigma_0, a_0^0 | (\bar{s}c) | D_s^+ \rangle = (\cos\theta_I, -\sin\theta_I, 0) \times \langle f_s | (\bar{s}c) | D_s^+ \rangle.$$

- $q^2\bar{q}^2$:

$$|n\bar{n}s\bar{s}\rangle \equiv |\sqrt{1/2}(u\bar{u} + d\bar{d})s\bar{s}\rangle,$$

$$|f_0\rangle = \cos\theta_{II}|n\bar{n}s\bar{s}\rangle + \sin\theta_{II}|u\bar{u}d\bar{d}\rangle,$$

$$|\sigma_0\rangle = -\sin\theta_{II}|n\bar{n}s\bar{s}\rangle + \cos\theta_{II}|u\bar{u}d\bar{d}\rangle,$$

$$|a_0^0\rangle = |\sqrt{1/2}(u\bar{u} - d\bar{d})s\bar{s}\rangle, \quad |a_0^-\rangle = |d\bar{u}s\bar{s}\rangle.$$

- FFs with $q^2\bar{q}^2$: need extra quark pair from $g \rightarrow q\bar{q}$

$$F_{ns} \equiv |n\bar{n}s\bar{s}\rangle, \quad F_{ud} \equiv |u\bar{u}d\bar{d}\rangle,$$

$$\langle f_0 | (\bar{d}c) | D^+ \rangle = \cos\theta_{II} \langle F_{ns} | (\bar{d}c) | D^+ \rangle + \sin\theta_{II} \langle F_{ud} | (\bar{d}c) | D^+ \rangle,$$

$$\langle \sigma_0 | (\bar{d}c) | D^+ \rangle = -\sin\theta_{II} \langle F_{ns} | (\bar{d}c) | D^+ \rangle + \cos\theta_{II} \langle F_{ud} | (\bar{d}c) | D^+ \rangle,$$

$$\langle a_0^0 | (\bar{d}c) | D^+ \rangle = \sqrt{1/2} \langle a_0^- | (\bar{d}c) | D^0 \rangle = -\langle F_{ns} | (\bar{d}c) | D^+ \rangle,$$

$$\langle f_0, \sigma_0, a_0^0 | (\bar{s}c) | D_s^+ \rangle = (\cos\theta_{II}, -\sin\theta_{II}, 0) \times \langle F_{ns} | (\bar{s}c) | D_s^+ \rangle.$$

• Calculating $D \rightarrow S_0 e^+ \nu$, $S_0 \rightarrow M_1 M_2$ as a four-body decay, instead of using $\mathcal{B} \simeq \mathcal{B}(D \rightarrow S_0 e^+ \nu) \mathcal{B}(S_0 \rightarrow M_1 M_2)$.

• Resonant amplitudes of $S_0 \rightarrow M_1 M_2$:

Flatté formula for f_0 and a_0 , Breit-Wigner model for σ_0 ,

$$1. \mathcal{R}_{f_0} \equiv \mathcal{R}(f_0 \rightarrow \pi\pi) = \frac{C_{f_0 \rightarrow \pi\pi}}{m_{f_0}^2 - t - im_{f_0}(g_{f_0 \pi\pi} \rho_{\pi\pi} + g_{f_0 KK} \rho_{KK})},$$

$$\rho_{M_1 M_2} \equiv [(1 - m_+^2/t)(1 - m_-^2/t)]^{1/2}, \quad m_{\pm} = m_{M_1} \pm m_{M_2},$$

$\langle M_1 M_2 | S_0 \rangle \equiv C_{S_0 \rightarrow M_1 M_2}$ for $S_0 \rightarrow M_1 M_2$ strong decay.

LHCb, PRD86, 052006 (2012),

“Analysis of the resonant components in $B_s \rightarrow J/\psi \pi^+ \pi^-$,”

LHCb, PRD92, 032002 (2015),

“Dalitz plot analysis of $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ decays.”

$$2. \mathcal{R}_{a_0} \equiv \mathcal{R}(a_0 \rightarrow \pi\eta) = \frac{C_{a_0 \rightarrow \pi\eta}}{m_{a_0}^2 - t - i(g_{a_0 \pi\eta}^2 \rho_{\pi\eta} + g_{a_0 KK}^2 \rho_{KK})},$$

BaBar, PRD72, 052008 (2005),

“Dalitz plot analysis of $D^0 \rightarrow \bar{K}^0 K^+ K^-$,”

BESIII, arXiv:2006.02800 [hep-ex],

“Analysis of the decay $D^0 \rightarrow K_S^0 K^+ K^-$,”

$$3. \mathcal{R}_{\sigma_0} \equiv \mathcal{R}(\sigma_0 \rightarrow \pi\pi) = \frac{C_{\sigma_0 \rightarrow \pi\pi}}{m_{\sigma_0}^2 - t - i m_{\sigma_0} \Gamma_{\sigma_0}},$$

$$\Gamma_{\sigma_0} \equiv (\rho_{\pi\pi} / \bar{\rho}_{\pi\pi}) \Gamma_{\sigma_0}^0, \quad \bar{\rho}_{\pi\pi} = \rho_{\pi\pi}(t) \text{ at } t = m_{\sigma_0}^2,$$

LHCb, PRD87, 052001 (2013),

“Analysis of the resonant components in $\bar{B}^0 \rightarrow J/\psi \pi^+ \pi^-$.”

• **Amplitude of $D \rightarrow S_0 e^+ \nu$, $S_0 \rightarrow M_1 M_2$:**

$$\mathcal{M} = \mathcal{R}_{S_0} \mathcal{M}(D \rightarrow S_0 e^+ \nu_e).$$

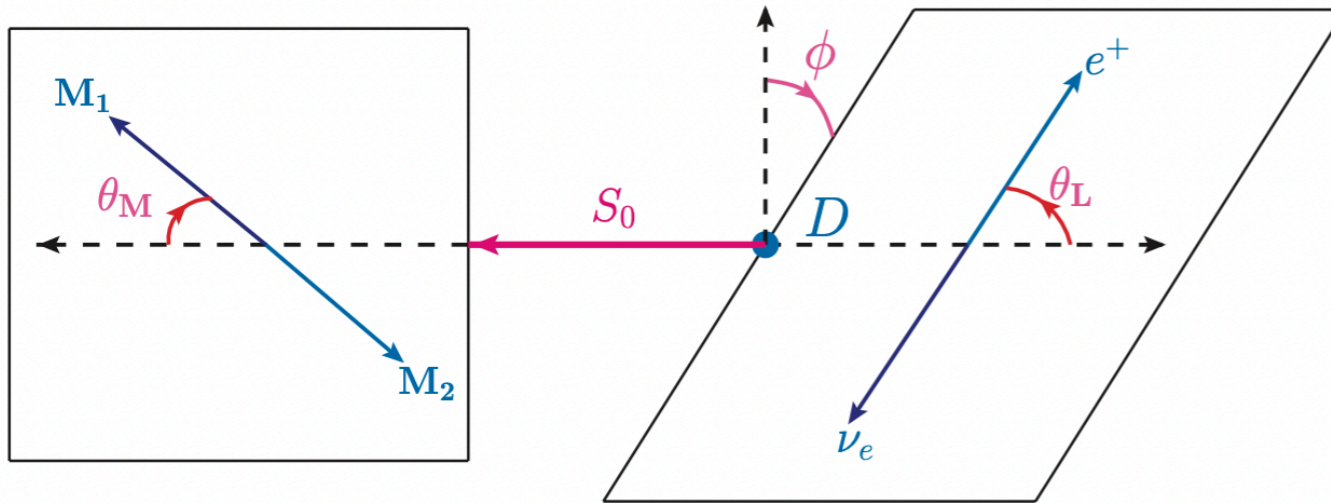
Phase space $D(p_D) \rightarrow S_0(p_{S_0})e^+(p_e)\nu(p_\nu), S_0(p_{S_0}) \rightarrow M_1(p_1)M_2(p_2)$

$$d\Gamma = \frac{|\bar{\mathcal{M}}|^2}{4(4\pi)^6 m_D^3} X \alpha_{\mathbf{M}} \alpha_{\mathbf{L}} ds dt d\cos\theta_{\mathbf{M}} d\cos\theta_{\mathbf{L}} d\phi$$

$$X = [(m_D^2 - s - t)^2/4 - st]^{1/2},$$

$$\alpha_{\mathbf{M}} = \lambda^{1/2}(t, m_1^2, m_2^2)/t, \quad \alpha_{\mathbf{L}} = \lambda^{1/2}(s, m_e^2, m_\nu^2)/s$$

$$\lambda(a, b, c) = a^2 + b^2 + c^2 - 2ab - 2bc - 2ca.$$



The allowed regions of the variables:

$$(m_e + m_\nu)^2 \leq s \leq (m_D - \sqrt{t})^2,$$

$$(m_1 + m_2)^2 \leq t \leq (m_D - m_e - m_\nu)^2,$$

$$0 \leq \theta_{\mathbf{M},\mathbf{L}} \leq \pi, \text{ and } 0 \leq \phi \leq 2\pi.$$

Theoretical inputs

- Mixing angle:

$$\theta_I = (158.7 \pm 4.0)^\circ, \text{ Klempt, PLB820, 136512 (2021),}$$

“Scalar mesons and the fragmented glueball.”

$$\theta_{II} = (174.6^{+3.4}_{-3.2})^\circ, \text{ Maiani, Piccinini, Polosa, Riquer,}$$

PRL93, 212002 (2004), *“A New look at scalar mesons.”*

- Parameters in the denominator of \mathcal{R}_{S_0}

$$(m_{f_0}, g_{f_0\pi\pi}) = (940, 199 \pm 30) \text{ MeV}, g_{f_0KK} = (3.0 \pm 0.3)g_{f_0\pi\pi},$$

$$(m_{a_0}, g_{a_0\pi\eta}) = (999, 324 \pm 15) \text{ MeV}, g_{a_0KK}^2 = (1.03 \pm 0.14)g_{a_0\pi\eta}^2,$$

$$(m_{\sigma_0}, \Gamma_{\sigma_0}^0) = (500, 500) \text{ MeV}.$$

- $C_{S_0 \rightarrow M_1 M_2}$

$$C_{f_0 \rightarrow \pi^+ \pi^-} = \sqrt{2}C_{f_0 \rightarrow \pi^0 \pi^0} = (1.5 \pm 0.1) \text{ GeV},$$

$$C_{a_0^{-(0)} \rightarrow \pi^{-(0)} \eta} = (2.5 \pm 0.2) \text{ GeV},$$

$$C_{\sigma_0 \rightarrow \pi^+ \pi^-} = \sqrt{2}C_{\sigma_0 \rightarrow \pi^0 \pi^0} = (3.9 \pm 0.1) \text{ GeV}.$$

Numerical results

We determine $F^{D \rightarrow S_0} \equiv f(0)$ for $D \rightarrow S_0$:

$$|F_{q\bar{q}, q^2\bar{q}^2}^{D_s^+ \rightarrow f_0}| = (0.52 \pm 0.02, 0.53 \pm 0.02),$$

agreeing with the experimental value of

0.52 ± 0.04 by BESIII,

justifying our determination.

decay channel	our work: $(q\bar{q}, q^2\bar{q}^2)$	experimental data
$10^4 \mathcal{B}(D_s^+ \rightarrow f_0 e^+ \nu_e, f_0 \rightarrow \pi^+ \pi^-)$	$(16.9 \pm 1.2 \pm 0.7, 17.2 \pm 1.3 \pm 0.7)$	17.1 ± 1.6 [48]
$10^4 \mathcal{B}(D_s^+ \rightarrow f_0 e^+ \nu_e, f_0 \rightarrow \pi^0 \pi^0)$	$(8.4 \pm 0.6 \pm 0.4, 8.6 \pm 0.7 \pm 0.4)$	7.9 ± 1.4 [49]
$10^4 \mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-)$	$(20.3 \pm 1.8 \pm 0.5, 0.58_{-0.57}^{+1.43} \pm 0.01)$	< 3.3 [48]
$10^4 \mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^0 \pi^0)$	$(10.7 \pm 1.0 \pm 0.3, 0.29_{-0.29}^{+0.72} \pm 0.01)$	< 7.3 [49] (< 1.7 [48]) [†]
$10^4 \mathcal{B}(D^0 \rightarrow a_0^- e^+ \nu_e, a_0^- \rightarrow \pi^- \eta)$	$(1.8 \pm 0.2 \pm 0.2, 0.8 \pm 0.1 \pm 0.1)$	1.3 ± 0.3 [8]
$10^4 \mathcal{B}(D^+ \rightarrow a_0^0 e^+ \nu_e, a_0^0 \rightarrow \pi^0 \eta)$	$(2.4 \pm 0.2 \pm 0.3, 1.0 \pm 0.1 \pm 0.1)$	1.7 ± 0.7 [8]
$10^5 \mathcal{B}(D^+ \rightarrow f_0 e^+ \nu_e, f_0 \rightarrow \pi^+ \pi^-)$	$(1.3 \pm 0.1 \pm 0.1, 2.9 \pm 0.7 \pm 0.2)$	< 2.8 [87]
$10^4 \mathcal{B}(D^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-)$	$(5.4 \pm 0.5 \pm 0.1, 6.2 \pm 0.9 \pm 0.1)$	6.3 ± 0.5 [87]

- From the mixing, we obtain

$$F_{(q\bar{q}, q^2\bar{q}^2)}^{D_s^+ \rightarrow \sigma_0} = -(\tan \theta_I, \tan \theta_{II}) \times F^{D_s^+ \rightarrow f_0}$$

$$= (0.22 \pm 0.01, 0.037 \pm 0.032), \text{ leading to}$$

$$\mathcal{B}_{(q\bar{q}, q^2\bar{q}^2)}^{D_s^+ \rightarrow \sigma_0 \rightarrow \pi^+ \pi^-} \equiv \mathcal{B}_{(q\bar{q}, q^2\bar{q}^2)}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-)$$

$$= (20.3 \pm 1.8 \pm 0.5, 0.58_{-0.57}^{+1.43} \pm 0.01) \times 10^{-4},$$

$$\mathcal{B}_{(q\bar{q}, q^2\bar{q}^2)}^{D_s^+ \rightarrow \sigma_0 \rightarrow \pi^0 \pi^0} \equiv \mathcal{B}_{(q\bar{q}, q^2\bar{q}^2)}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^0 \pi^0)$$

$$= (10.7 \pm 1.0 \pm 0.3, 0.29_{-0.29}^{+0.72} \pm 0.01) \times 10^{-4},$$

respecting isospin symmetry.

- Compared to the data:

$$\mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-) < 3.3 \times 10^{-4},$$

$$\mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^0 \pi^0) < 6.4 \times 10^{-4} \text{ or } 1.7 \times 10^{-4}.$$

- 9σ (10σ) deviations

Excluding the possibility that S_0 is a ordinary $q\bar{q}$ meson.

Semileptonic $D^{+(0)}$ decays

- Form factors: $F^{D_s^+ \rightarrow F_{ns}}$, $F^{D^+ \rightarrow F_{ns}}$, $F^{D^+ \rightarrow F_{ud}}$

$$(F_{q^2\bar{q}^2}^{D_s^+ \rightarrow f_0}, F_{q^2\bar{q}^2}^{D_s^+ \rightarrow \sigma_0}) = (\cos \theta_{II}, -\sin \theta_{II}) \times F^{D_s^+ \rightarrow F_{ns}}$$

$$F_{q^2\bar{q}^2}^{D^+ \rightarrow a_0^0} = -F^{D^+ \rightarrow F_{ns}}, \quad F_{q^2\bar{q}^2}^{D^0 \rightarrow a_0^-} = -\sqrt{2}F^{D^+ \rightarrow F_{ns}}$$

$$F_{q^2\bar{q}^2}^{D^+ \rightarrow f_0} = \cos \theta_{II} F^{D^+ \rightarrow F_{ns}} + \sin \theta_{II} F^{D^+ \rightarrow F_{ud}}$$

$$F_{q^2\bar{q}^2}^{D^+ \rightarrow \sigma_0} = -\sin \theta_{II} F^{D^+ \rightarrow F_{ns}} + \cos \theta_{II} F^{D^+ \rightarrow F_{ud}}$$

$$F^{D^+ \rightarrow F_{ud}} = \sqrt{2}F^{D^+ \rightarrow F_{ns}} \quad [SU(3)_f \text{ assumption}]$$

- Experimental data:

$$\mathcal{B}(D^0 \rightarrow a_0^- e^+ \nu_e, a_0^- \rightarrow \pi^- \eta) = (1.3 \pm 0.3) \times 10^{-4},$$

$$\mathcal{B}(D^+ \rightarrow a_0^0 e^+ \nu_e, a_0^0 \rightarrow \pi^0 \eta) = (1.7 \pm 0.7) \times 10^{-4},$$

$$\mathcal{B}(D^+ \rightarrow f_0 e^+ \nu_e, f_0 \rightarrow \pi^+ \pi^-) < 2.8 \times 10^{-5},$$

$$\mathcal{B}(D^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-) = (6.3 \pm 0.5) \times 10^{-4}.$$

- $\bar{B}_s^0 \rightarrow J/\psi(f_0, \sigma_0), \bar{B}^0 \rightarrow J/\psi(f_0, \sigma_0),$

through $\bar{B}_s^0 \rightarrow s\bar{s} \rightarrow (f_0, \sigma_0)$ and $\bar{B}^0 \rightarrow d\bar{d} \rightarrow (f_0, \sigma_0).$

- Proposed to distinguish between the quark content of S_0 being quark-antiquark or tetraquark [Stone, Zhang, PRL (2013)].

- The following measurement of $\bar{B}_s^0 \rightarrow J/\Psi f_0, f_0 \rightarrow \pi^+ \pi^-$

suggests the mixing angle to be less than $7.7^\circ,$

LHCb, PRD89, 092006 (2014), “*Measurement of resonant and*

CP components in $\bar{B}_s^0 \rightarrow J/\psi \pi^+ \pi^-$ decays,”

consistent with the tetraquark interpretation.

Summary

- We obtained

$$\mathcal{B}_{(q\bar{q})}^{D_s^+ \rightarrow \sigma_0 \rightarrow \pi^+ \pi^-} = (20.3 \pm 1.8 \pm 0.5) \times 10^{-4},$$

$$\mathcal{B}_{(q\bar{q})}^{D_s^+ \rightarrow \sigma_0 \rightarrow \pi^0 \pi^0} = (10.7 \pm 1.0 \pm 0.3) \times 10^{-4},$$

in comparison with the data:

$$\mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^+ \pi^-) < 3.3 \times 10^{-4},$$

$$\mathcal{B}(D_s^+ \rightarrow \sigma_0 e^+ \nu_e, \sigma_0 \rightarrow \pi^0 \pi^0) < 6.4 \times 10^{-4} \quad (1.7 \times 10^{-4}).$$

- It has led to the 9σ (10σ) deviations:

not favoring S_0 as an ordinary $q\bar{q}$ meson.

Thank You