



COEPP

ARC Centre of Excellence for
Particle Physics at the Terascale

RADIATIVE NEUTRINO MASS MODELS AT THE LHC

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Collaboration between theorists and ATLAS experimentalists at CoEPP

Theory: Paul Angel, Nick Rodd, RV

Experiment: Elisabetta Barberio, Kenji Hamano, Lucas Ong, Nick Rodd

Part of the “exotics” group within ATLAS

Goals:

- To search for the physics of neutrino mass generation at the LHC
- To construct new LHC-testable models that complement existing models, e.g. Zee-Babu
- To see if a systematic analysis of all such models is possible, under reasonable assumptions

Approach on the theory side:

- Use $\Delta L=2$ effective operators as starting point for models
- Rule out as many as possible using simple criteria, e.g. ν mass too small
- “Open up” the operators, i.e. construct all possible UV completions
- Filter using flavour and other constraints
- Examine LHC signatures

Project only partially done, so progress report.

Approach on experimental side:

- **Piggyback on generic exotica searches**
- **Initial focus on like-sign dilepton production (e.g. the doubly-charged Zee-Babu scalar) and testing type-III see-saw model**
- **Some ATLAS results presented at ICHEP 2012 (mass limits soon). CMS has approx. 400 GeV lower bound on doubly-charged scalars**

Contents:

1. $\Delta L=2$ effective operators
2. Topological analysis of opening-up of operators (P. Angel MSc thesis 2011)
3. Building specific models (P. Angel 2011 and N. Rodd MSc thesis 2012)
4. Conclusions

1. $\Delta L=2$ Effective Operators

Assumption: SM gauge group and multiplets

Babu & Leung, NPB619, 667 (2001)

de Gouvêa & Jenkins, PRD77, 013008 (2008)

W. Winter et al, recent papers

Classification criteria:

- mass dimension = d
- number of fermion fields = f

d=5, f=2:

LLHH, the famous Weinberg operator

Can be opened up at tree-level: **type I, II and III see-saw mechanisms**

$$m_\nu \sim v^2/M \rightarrow M \sim 10^{12} \text{ TeV}$$

unless some couplings are very small

The new physics is not forced to be at TeV scale

B=Babu J=Julio L=Leung Z=Zee

d=detailed, b=brief

d	f	operator(s)	scale from m_ν (TeV)	model(s)?	comments
7	4	$O_2 = LLLe^c H$	10^7	Z (1980, d)	pure-leptonic, 1-loop, ruled out
		$O_3 = LLQd^c H(2)$	$10^{5,8}$	BJ (2012, d) BL (2001,b)	2012 = 2-loop 2001 = 1-loop
		$O_4 = LL\bar{Q}\bar{u}^c H(2)$	$10^{7,9}$	BL (2001,b)	1-loop vector leptoquarks
		$O_8 = L\bar{e}^c \bar{u}^c d^c H$	10^4	BJ (2010, d)	2-loop
9	4	$O_5 = LLQd^c HH\bar{H}$	10^6	BL (2001,b)	1-loop
		$O_6 = LL\bar{Q}\bar{u}^c HH\bar{H}$	10^7		
		$O_7 = LQ\bar{e}^c \bar{Q}HHH$	10^2		
		$O_{61} = (LLHH)(Le^c \bar{H})$	10^5		purely leptonic
		$O_{66} = (LLHH)(Qd^c \bar{H})$	10^6		
		$O_{71} = (LLHH)(Qu^c H)$	10^7	BL (2001,b)	1-loop

d	f	operator(s)	scale from mv (TeV)	model(s)?	comments
9	6	$O_9 = LLLe^cLe^c$	10³	BZ (1988, d)	2-loop, purely leptonic
		$O_{10} = LLLe^cQd^c$	10⁴	BL (2001,b)	two 2-loop models
		$O_{11} = LLQd^cQd^c(2)$	30, 10⁴	BL (2001,b) A (2011, d)	three 2-loop models one 2-loop model
		$O_{12} = LL\bar{Q}\bar{u}^c\bar{Q}\bar{u}^c(2)$	10^{4,7}	BL (2001,b)	2-loop
		$O_{13} = LL\bar{Q}\bar{u}^cLe^c$	10⁴		
		$O_{14} = LL\bar{Q}\bar{u}^cQd^c(2)$	10^{3,6}		
		$O_{15} = LLLd^c\bar{L}\bar{u}^c$	10³		
		$O_{16} = LL\bar{e}^cd^c\bar{e}^c\bar{u}^c$	2		
		$O_{17} = LLd^cd^c\bar{d}^c\bar{u}^c$	2		
		$O_{18} = LLd^cu^c\bar{u}^c\bar{u}^c$	2		
		$O_{19} = LQd^cd^c\bar{e}^c\bar{u}^c$	1	dGJ (2008,b)	
		$O_{20} = Ld^c\bar{Q}\bar{u}^c\bar{e}^c\bar{u}^c$	40		

d=11, f=6:

40 operators + 12 which are (d=7,f=4)x(d=4,f=2)

A large number have $M < 10^3$ TeV.

Many already require $O(1)$ couplings or worse to get $m_\nu \sim 0.05\text{eV}$ with the new physics at $O(\text{TeV})$.

There are no models worked out in detail yet.

This largely unexplored class is of interest for LHC searches. Do any of them work?

Sketched models exist for:

$O_{21} = LLLe^c Qu^c HH(2)$ **BL (2001), three models**
 $M < 10^3 \text{ TeV}$

$O_{56} = LQd^c d^c \bar{e}^c \bar{d}^c HH$ **dGJ (2008), $M < 500 \text{ GeV}$**

2. Diagram topologies

P. Angel, MSc thesis (2011)
A. de Gouvêa & Jenkins (2008)
K. Babu & C.N. Leung (2001)

The Weinberg operator $O_1=LLHH$ is the only one that, when opened, produces tree-level neutrino mass models.

Our study is thus necessarily of radiative neutrino mass generation.

How many loops?

Three looks difficult.

You have to fight $\left(\frac{1}{16\pi^2}\right)^3 \simeq 10^{-7}$ to get $m_\nu \sim 0.05\text{eV}$.

This may not be completely ruled out – deG&J considered such cases – but we shall stop at two loops.

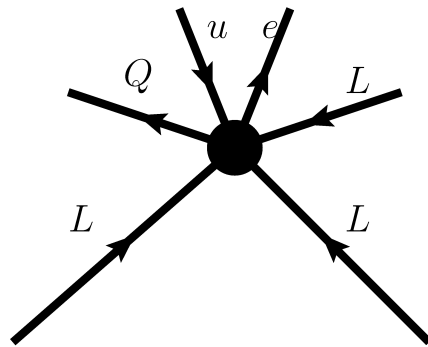
There are two places loops can arise:

- on external lines of the effective operator
- in the opening-up of the operator itself

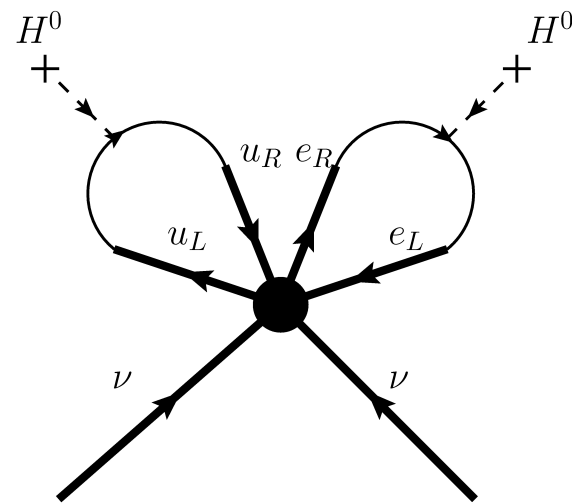
It is easy to examine the external lines to see how many can close into loops. Doing that, you find that **the following operators require >2 loops:**

O_{15-20} , O_{34-38} , O_{43} , O_{50} , O_{52-60} , O_{65} , O_{70} , O_{75} .

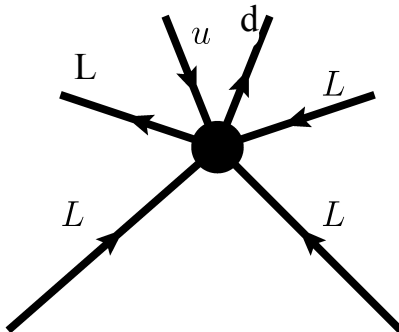
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9	6	$O_9 = LLLe^c Le^c$	10^3	BZ (1988, d)	2-loop, purely leptonic
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		$O_{14} = LL\bar{Q}\bar{u}^c Qd^c(2)$	$10^{3,6}$		
		$O_{15} = LL\bar{L}\bar{L}^c \bar{u}^c \bar{u}^c$	10^3		
		$O_{16} = LL\bar{L}\bar{L}^c \bar{u}^c \bar{u}^c$			
		$O_{17} = LLd^c d^c d^c \bar{u}^c$			
		$O_{18} = LLd^c u^c \bar{u}^c \bar{u}^c$			
		$O_{19} = LQ\bar{Q}\bar{u}^c$		dGJ	
		$O_{20} = Ld^c Q\bar{Q}\bar{u}^c$	40		



$$O_{13} = LL\bar{Q}\bar{u}^c Le^c$$



**2-loop external line
dressing to give m_ν**



No such dressing possible

$$O_{15} = LLLd^c \bar{L}\bar{u}^c$$

That leaves $75 - 1 - 25 = 49$ operators:

All four $d=7$, $f=4$ ops.

All six $d=9$, $f=4$ ops.

Six out of twelve $d=9$, $f=6$ ops.

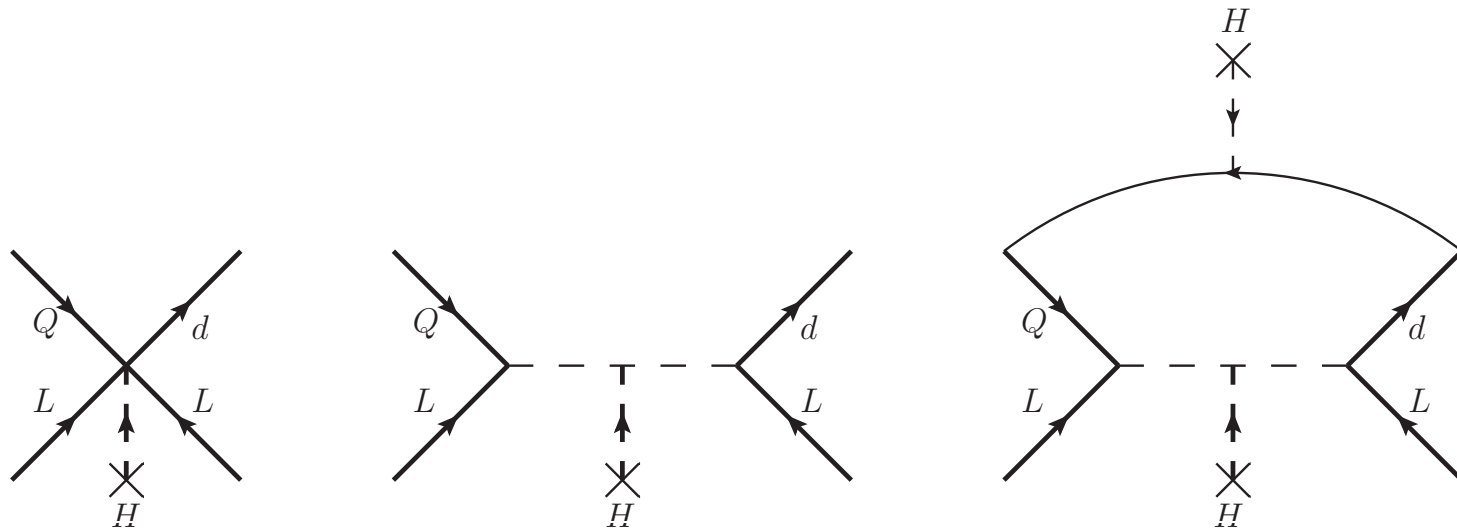
Thirty-three $d=11$, $f=6$ ops.

f = 4 operators leading to 1-loop models:

$$O_{2-6}, O_{61}, O_{66}, O_{71}$$

Examples:

Exotic scalar completion of $O_3 = LLQd^c H$

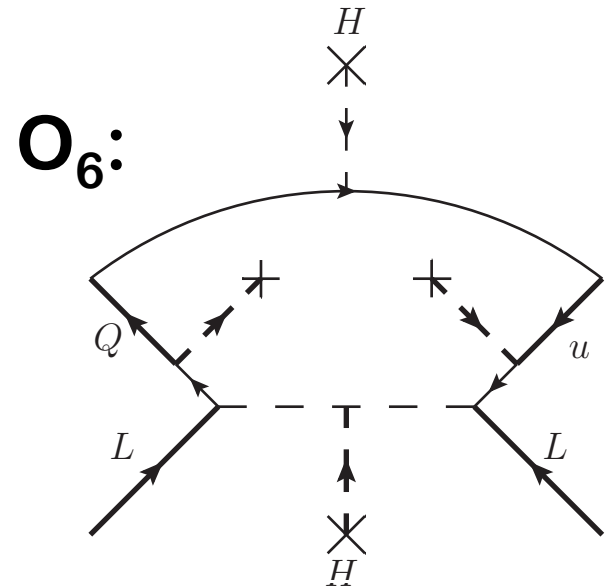


$$O_4 = LL\bar{Q}\bar{u}^c H(2) \quad O_6 = LL\bar{Q}\bar{u}^c HH\bar{H}$$

require exotic vector-like fermions
in addition to exotic scalars.

Scalars-only not allowed because you
get structures like $\bar{L}_L Q_L S$ which are
identically zero.

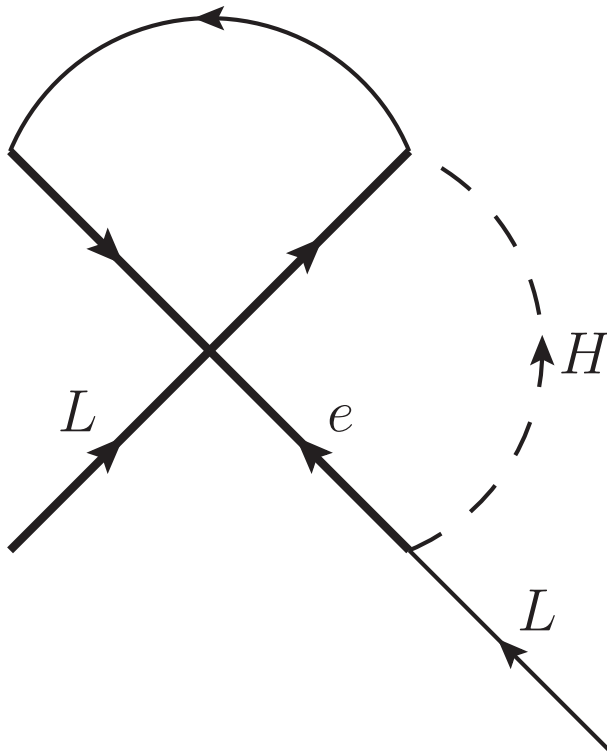
Models with exotic fermions
as well as exotic scalars
have not been looked at much.



f = 4 operators leading to 2-loop models

$$O_7 = LQ\bar{e}^c\bar{Q}HHH$$

$$O_8 = L\bar{e}^c\bar{u}^cd^cH$$



**plus 1 or 3 Higgs lines
heading in to effective
vertex**

d = 9, f = 6 operators (all models are 2-loop)

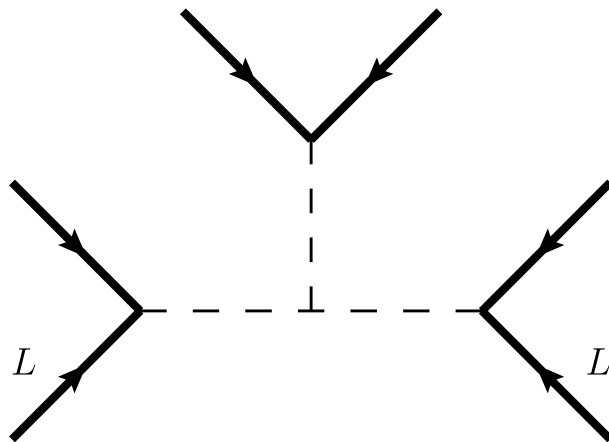
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		$O_{14} = LL\bar{Q}\bar{u}^c Qd^c(2)$	10^{3,6}		

BZ (1988) very well studied and used by ATLAS as exemplar 2-loop model. This whole class can be thoroughly analysed, but not done yet.

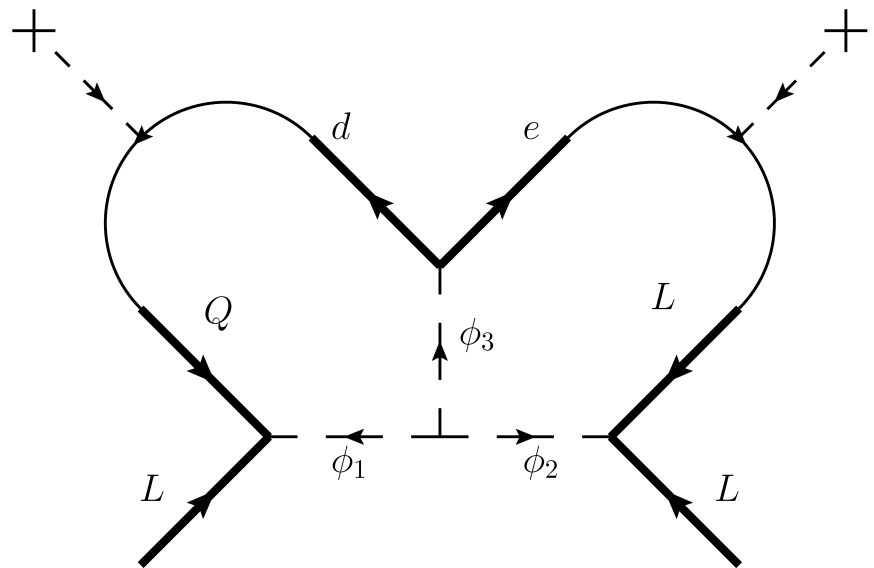
Each of the operators contains LL.

The other 4 fermions join to give 2 loops.

The effective operator completion must be tree-level.



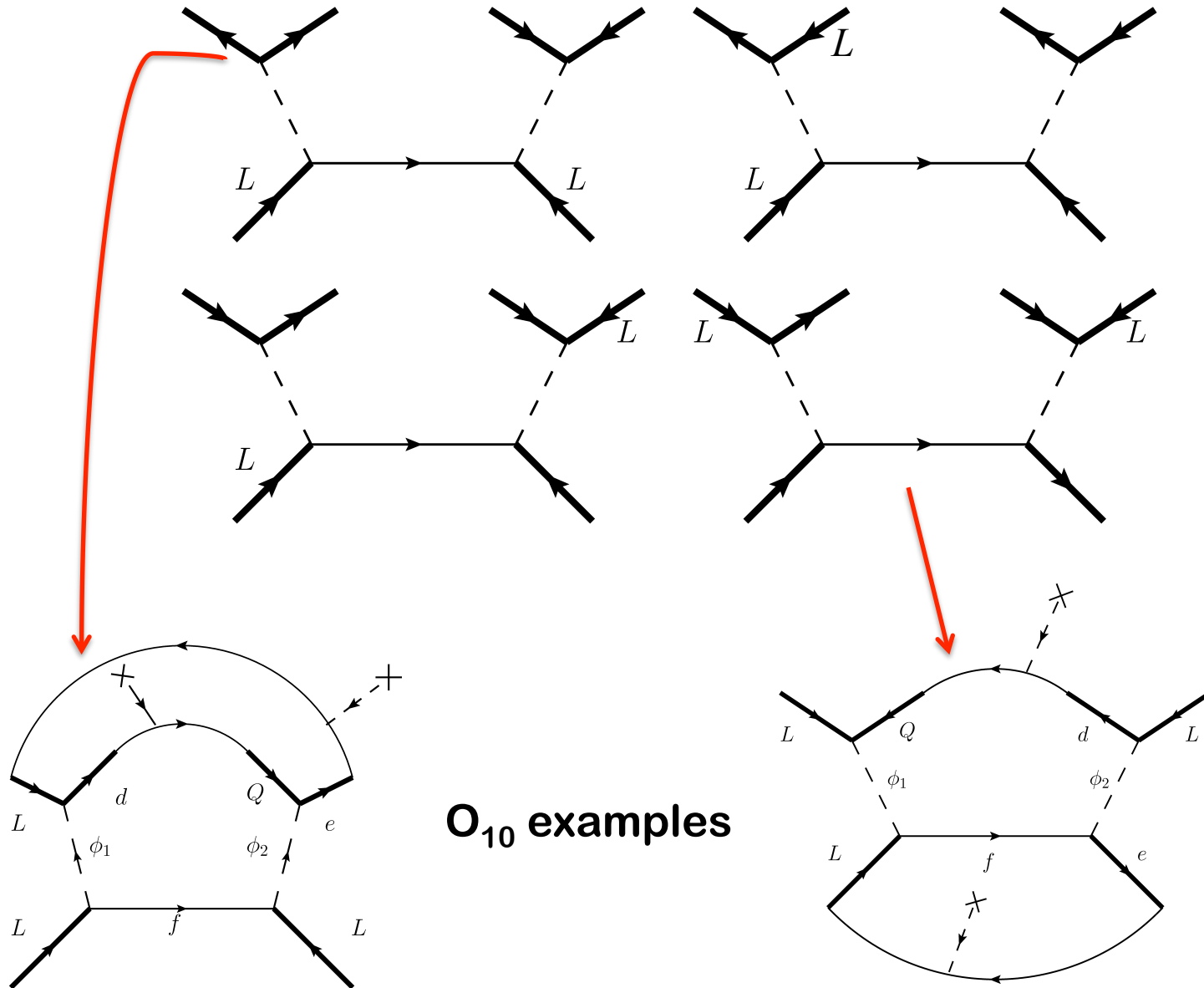
scalar-only completion



O_{10} example

Note: the two L's are separated to avoid a type-II see-saw triplet – not an absolute requirement

Including exotic fermions:



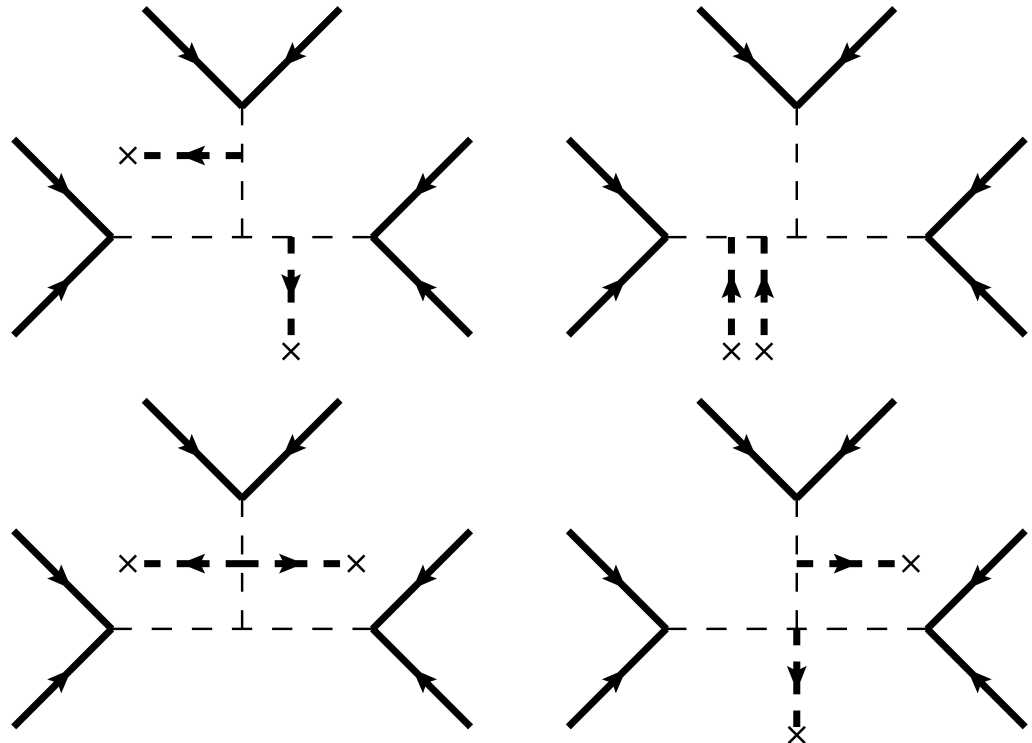
O_{10} examples

$d = 11$, $f = 6$ operators and 2-loop models

The 33 operators all contain LL and either HH or $H\bar{H}$.

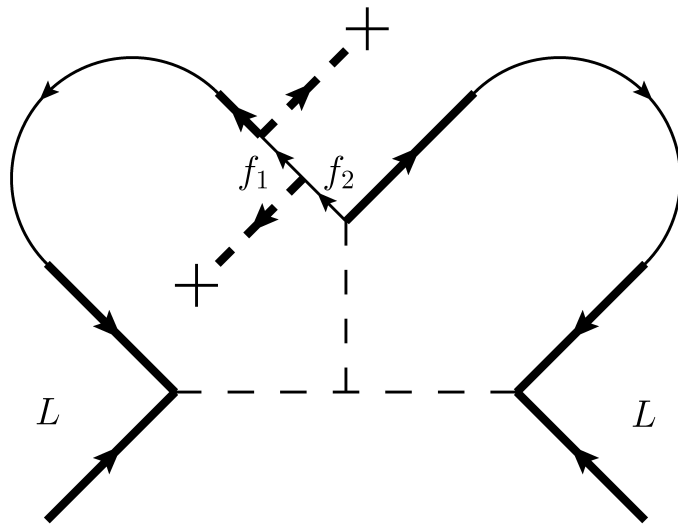
The previous $f = 6$ rules can be adapted to accommodate the two Higgs lines.

Exotic-scalar-only
completion case:

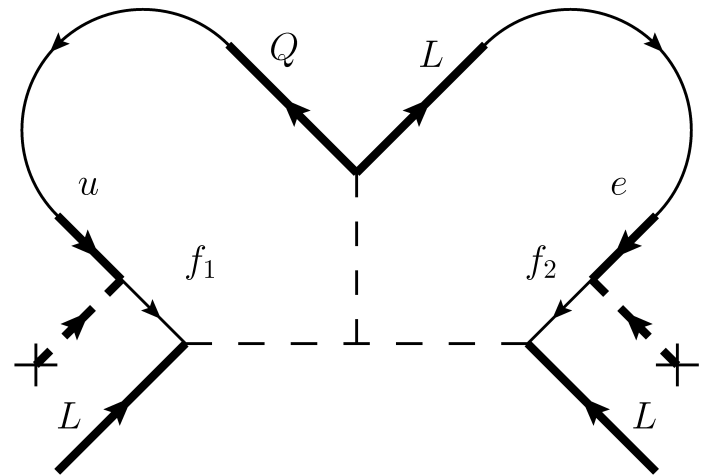


Including exotic fermions

An incomplete list:

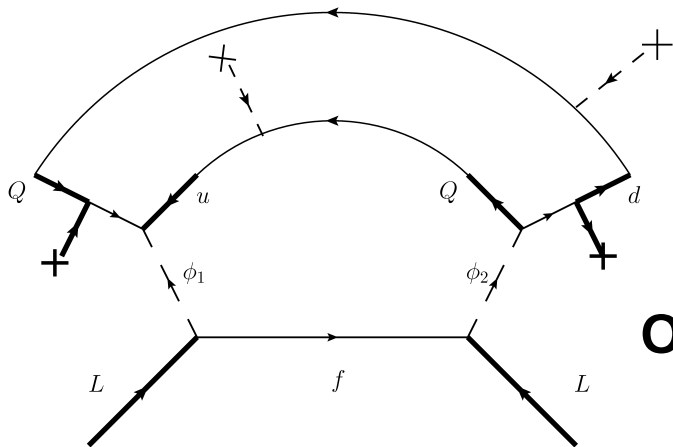
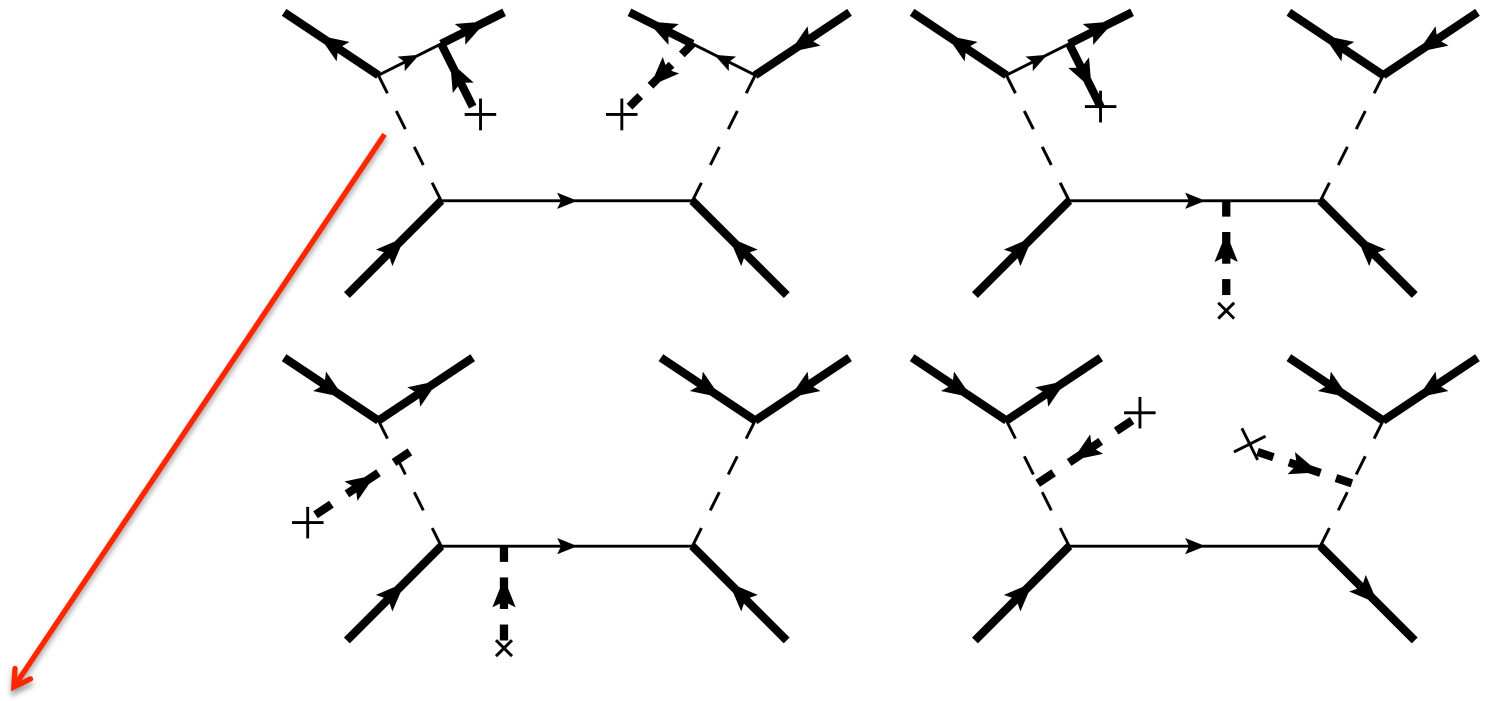


one generic topology



O_{12} example displaying another topology

More generic topologies:



O_{28} example

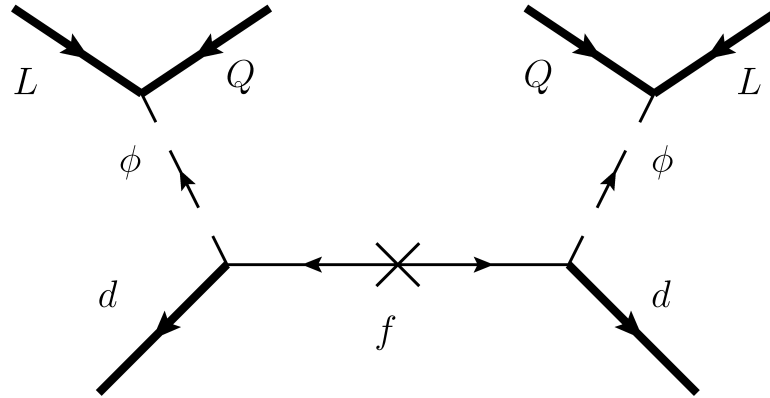
3. Models

Some general issues:

- Chirality – some diagrams vanish via $LR = 0$
- Divergent subdiagrams
- Generating lower-d operators

Angelic O_{11} model

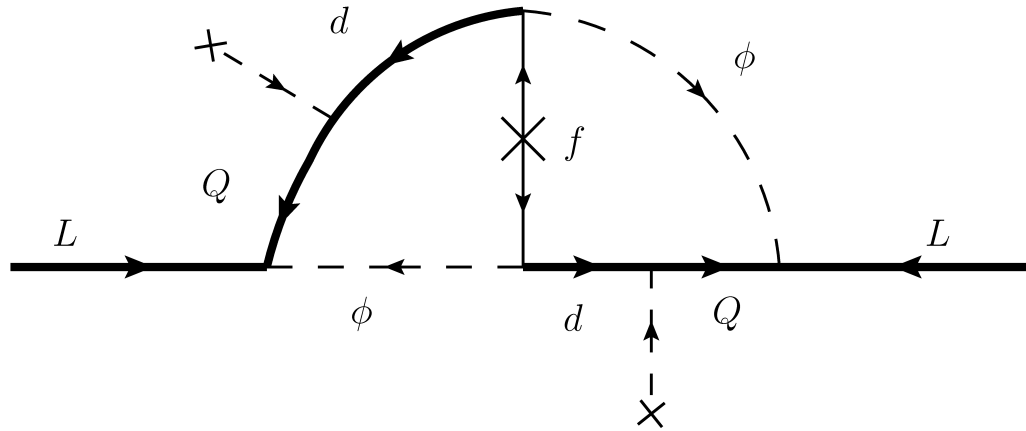
$$O_{11} = LLQd^c Qd^c (2)$$



$$\phi \sim (3^*, 1, 2/3) \quad f \sim (8, 1, 0)$$

$$\mathcal{L} = \lambda_{ab}^{LQ} \bar{L}_a^c Q_b \phi + \lambda_a^f \bar{d}_a f \phi^* + \frac{1}{2} m_f \bar{f}^c f + H.c.$$

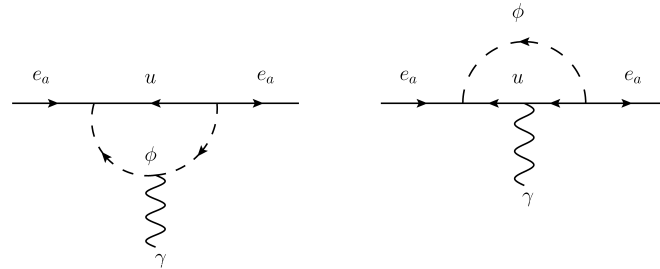
$\Delta L=2$ term



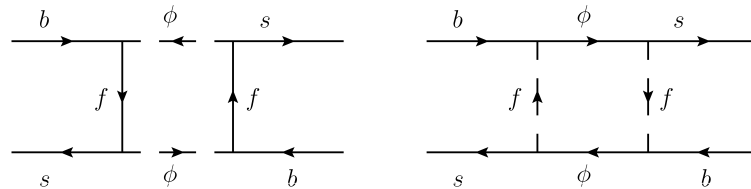
**Neutrino mass and mixing angles can be fitted
with $m_f, m_\phi \sim \text{TeV}$ and couplings $0.01-0.1$**

Constraints (under study):

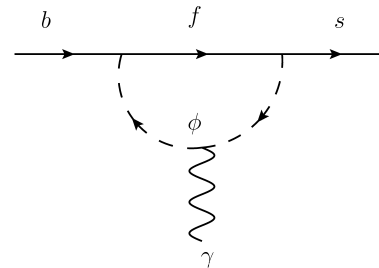
$g-2$ and $l_1 \rightarrow l_2 \gamma$:



meson mixing:



$b \rightarrow s \gamma$:



Rodd's investigation:

See if any viable models can arise from the $d=11$ operators.

Generic issue: it is not so easy to write a $d=11$ completion that does not also generate a lower d operator.

We have been looking at specific operators, and having noted this recurring problem are now trying to determine general rules for lower d operator generation.

4. Conclusions

1. Radiative ν mass models can be tested at the LHC.
2. Analysis of 2-loop diagram topologies exists.
3. New models can be generated.
4. All scalar+fermion models to $d=9$ can be constructed, but this has not yet been completed.
5. Are there any viable $d=11$ models?