

Interpreting the peak structures around 1800 MeV in the BES data on $J/\psi \rightarrow \phi\pi^+\pi^-$, $\rightarrow \gamma\omega\phi$

Kanchan Khemchandani
Institute of Physics-Univ. of São Paulo, Brazil

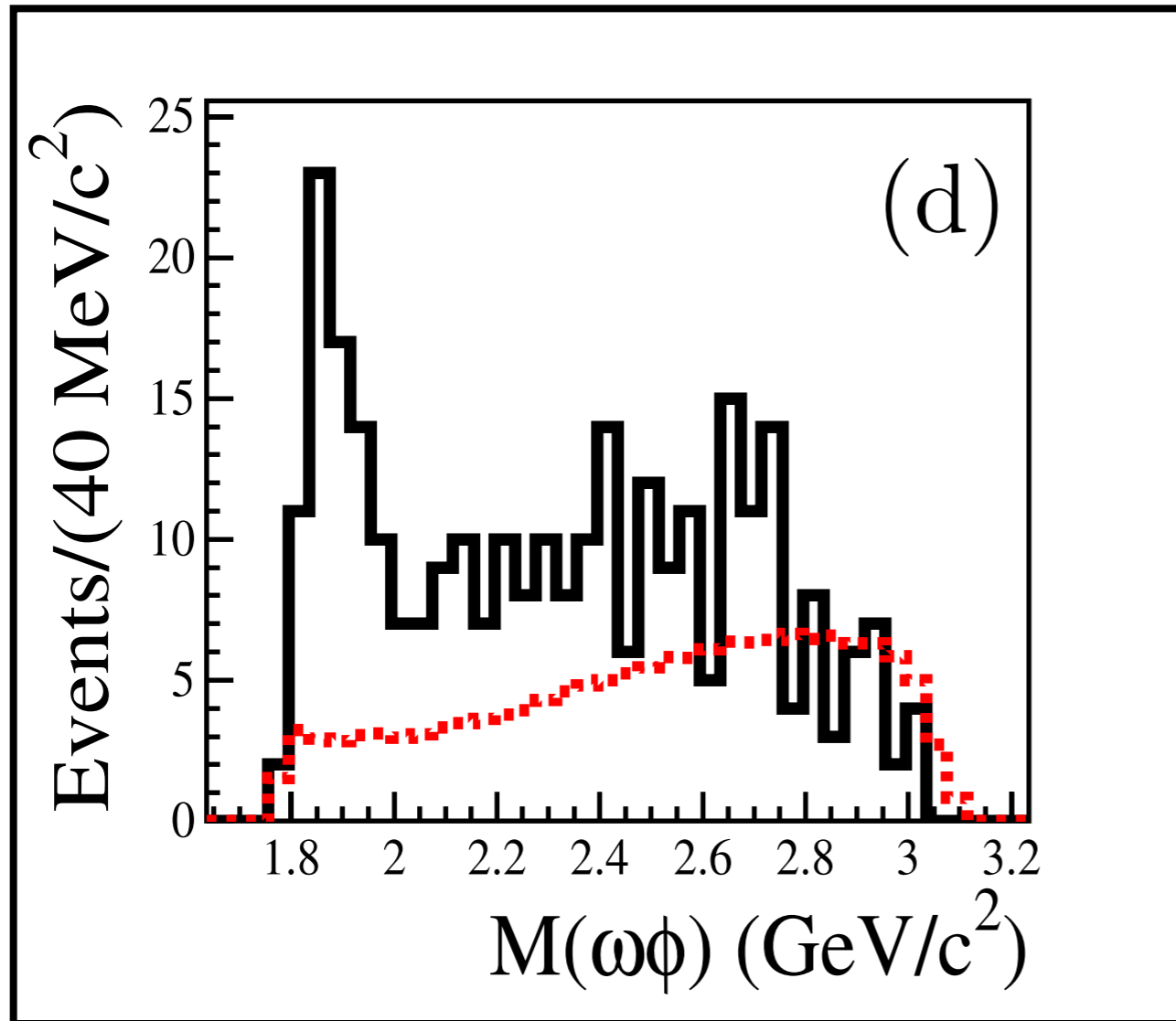
with

A. M. Torres, M. Nielsen, F. S. Navarra, E. Oset, A. Hosaka, D. Jido

**Based on: (1) Phys.Rev. D84 (2011) 074027
(2) Phys.Lett. B719 (2013) 388-393**

The 7th International Symposium on Chiral Symmetry in Hadrons and Nuclei
Oct.27-30, 2013, Beihang university, China

**OBSERVATION OF A NEAR-THRESHOLD ENHANCEMENT IN THE $\omega\phi$
MASS SPECTRUM FROM THE DOUBLY OZI-SUPPRESSED DECAY $J/\psi \rightarrow \gamma\omega\phi$**



PHYSICAL REVIEW LETTERS
PRL **96**, 162002 (2006)

0^{++} Resonance

$M = 1812 + 19 - 26 \pm 18$ MeV

$\Gamma = 105 \pm 20 \pm 28$ MeV

Known spectrum of (isoscalar) scalars

- $f_0(600)$
- $f_0(980)$
- $f_0(1370)$
- $f_0(1500)$
- $f_0(1710)$
- $f_0(2200)$
- $f_0(2330)$

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Q. Zhao and B. -S. Zou,
Phys. Rev. D **74**, 114025 (2006): enhancement found,
strength much smaller than the data,
 $f_0(1710) \omega\phi$ not known at that time

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More explanations:

tetraquark: B. A. Li, Phys. Rev. D 74, 054017 (2006).

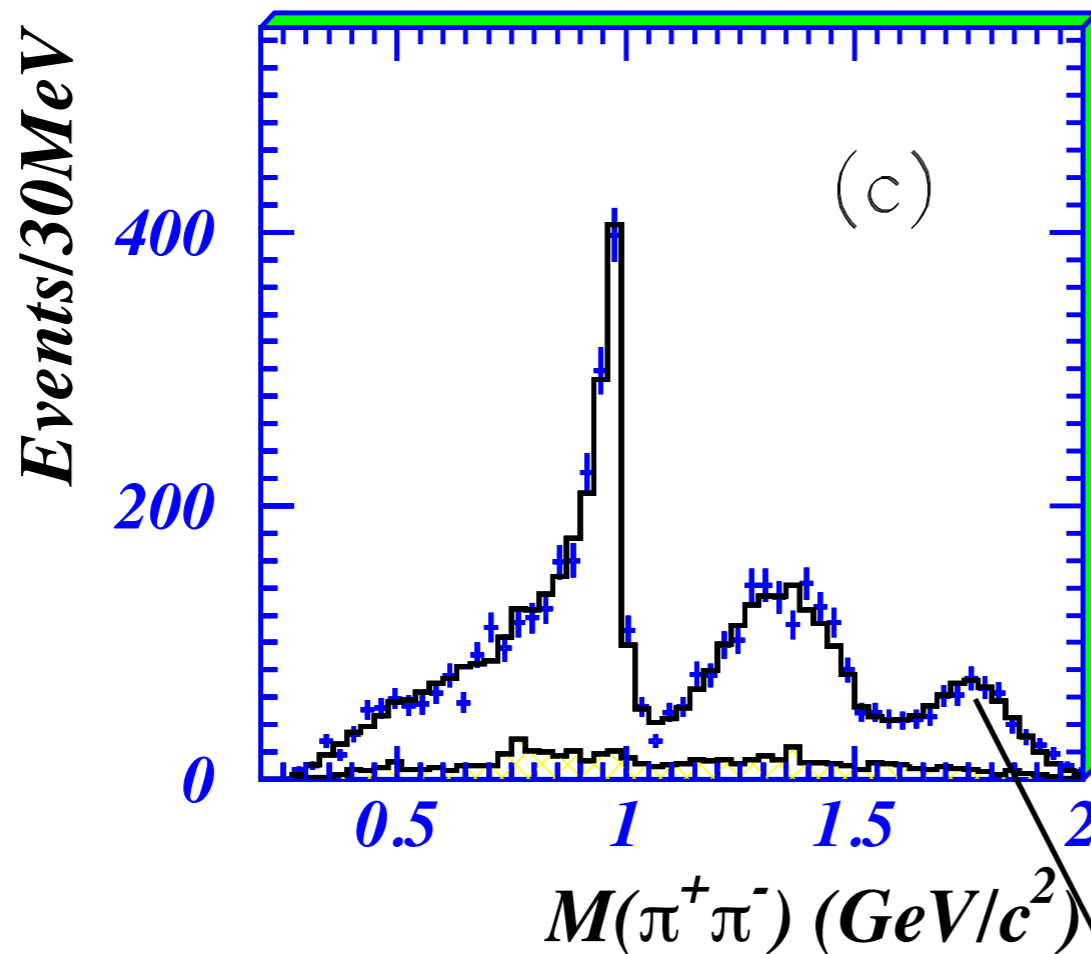
hybrid: K. -T. Chao, hep-ph/0602190.

Glueball: P. Bicudo, S. R. Cotanch, F. J. Llanes-Estrada and D. G. Robertson, Eur. Phys. J. C 52, 363 (2007).

Q. Zhao and B. -S. Zou,
Phys. Rev. D **74**, 114025 (2006): **enhancement found,**
strength much smaller than the data,
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Sometime ago.

OBSERVATION OF A PEAK STRUCTURE IN THE $\pi^+\pi^-$ MASS SPECTRUM WAS REPORTED IN $J/\psi \rightarrow \pi^+\pi^-\phi$ (ALSO DOUBLY OZI-SUPPRESSED) DECAY



Ref: BES Collaboration, Phys. Lett. B
607 (2005) 243-253.

$f_0(1790)$

Peculiarity: Its decay to K anti-K is suppressed.
Thus, it can't be the known $f_0(1710)$ (known to decay with a large branching ratio to K anti-K, decay to pions is suppressed).

- ✦ **THE QUANTUM NUMBERS ($J^{\pi C}=0^{++}, I=0$) OF THE STATES FOUND IN $J/\psi \rightarrow \pi^+\pi^-\phi$ AND $J/\psi \rightarrow \gamma\omega\phi$ ARE SAME.**
- ✦ **THERE MASSES ARE VERY SIMILAR.**
- ✦ **IS IT THE SAME STATE SHOWING UP IN THE TWO CASES?**
- ✦ **THE ANSWER IS A “No” (AS ALSO ANALYZED BY BES).**

- ✦ **It seems from BES' work that there are 3 scalar resonances: $f_0(1710)$, $f_0(1790)$, $f_0(1800)$.**
- ✦ **We show that there are only two states. That the enhancement seen in the $J/\psi \rightarrow \gamma \omega \phi$ decay is the manifestation of the known $f_0(1710)$.**
- ✦ **And the scalar resonance found in two pion spectrum is indeed a new state “ $f_0(1790)$ ”, distinct to the $f_0(1710)$.**
- ✦ **We explain, why the decay of the latter one ($f_0(1790)$) to K-anti-K is suppressed.**

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Supporting the existence of $f_0(1790)$ distinct to $f_0(1710)$

✦ WE FIND A “ $\pi\text{-}\pi\text{-}f_0(980)$ ” MOLECULAR INTERPRETATION FOR THE $f_0(1790)$.

FORMALISM OF THE STUDY IN A NUTSHELL:

✦ OBTAINING POTENTIALS FROM LOWEST ORDER CHIRAL LAGRANGIANS.

✦ SOLVING COUPLED CHANNEL BETHE SALPETER EQUATIONS TO GET TWO-BODY T-MATRICES.

✦ SOLVING FADDEEV EQUATIONS $T = T^1 + T^2 + T^3$ FOR THE $\pi K \bar{K}$ SYSTEM

$$T^1 = \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} + \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} + \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} + \\ \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} + \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} + \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \end{array} + \dots$$

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$f_0(980)$

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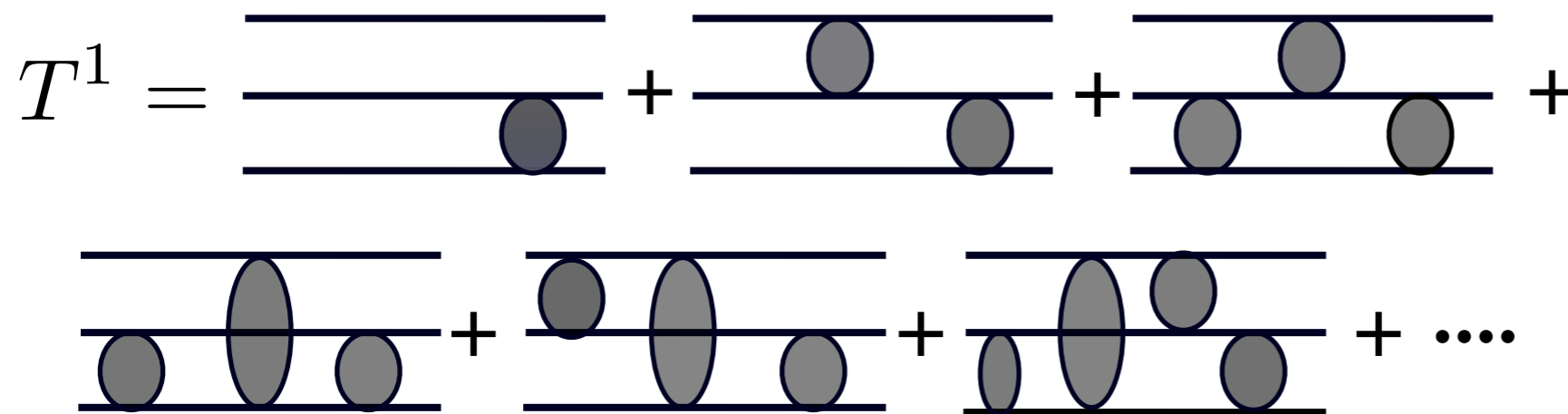
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$\pi f_0(980)$



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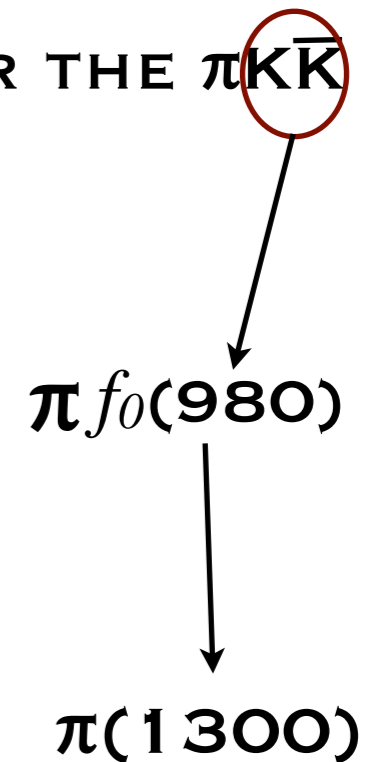
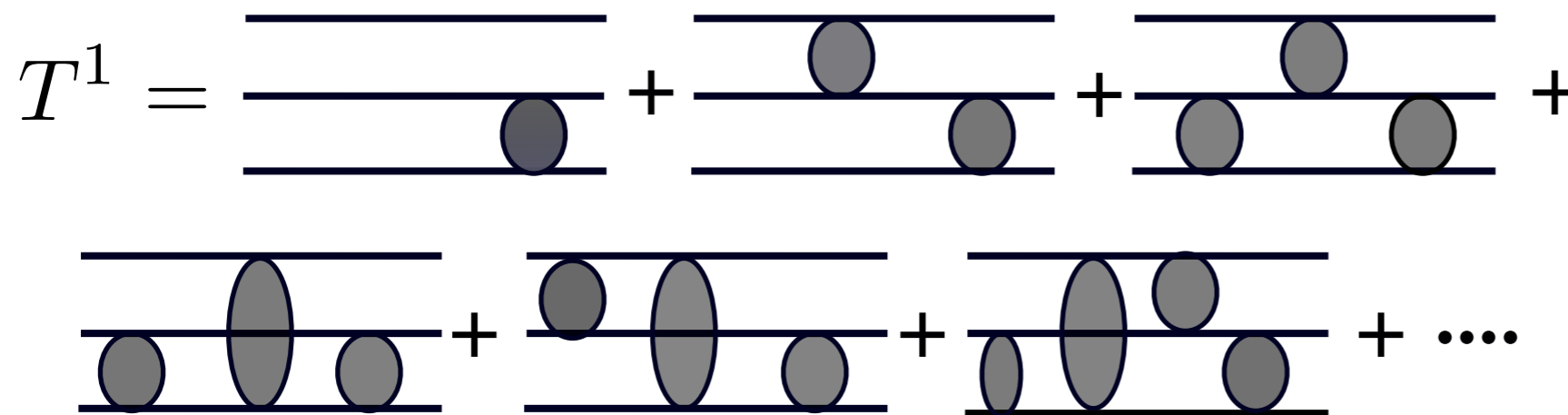
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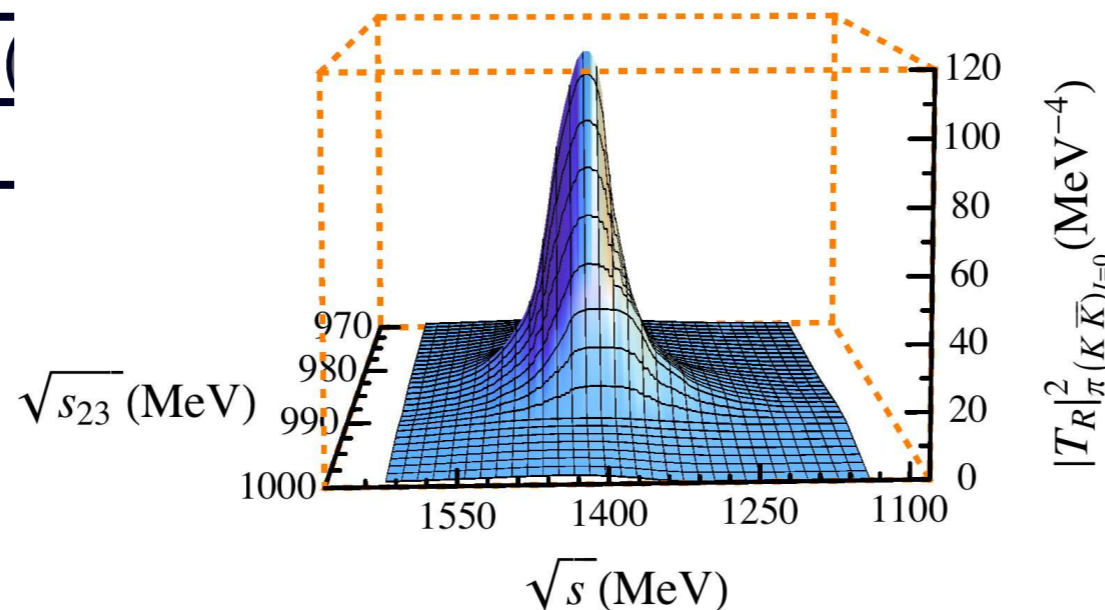
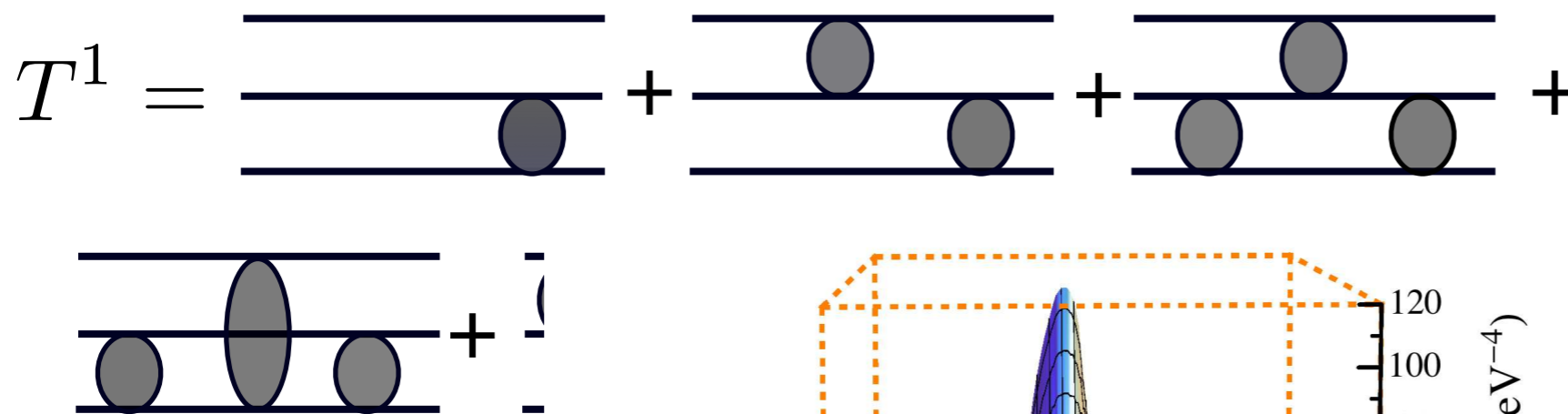
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$\pi f_0(980)$
 \downarrow
 $\pi(1300)$

Supporting the existence of $f_0(1790)$ distinct to $f_0(1710)$

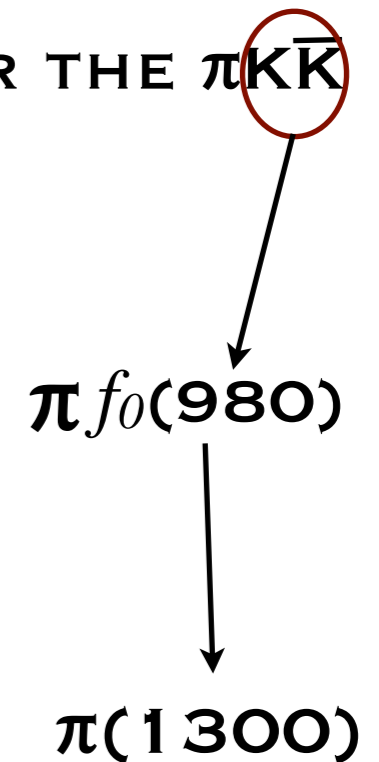
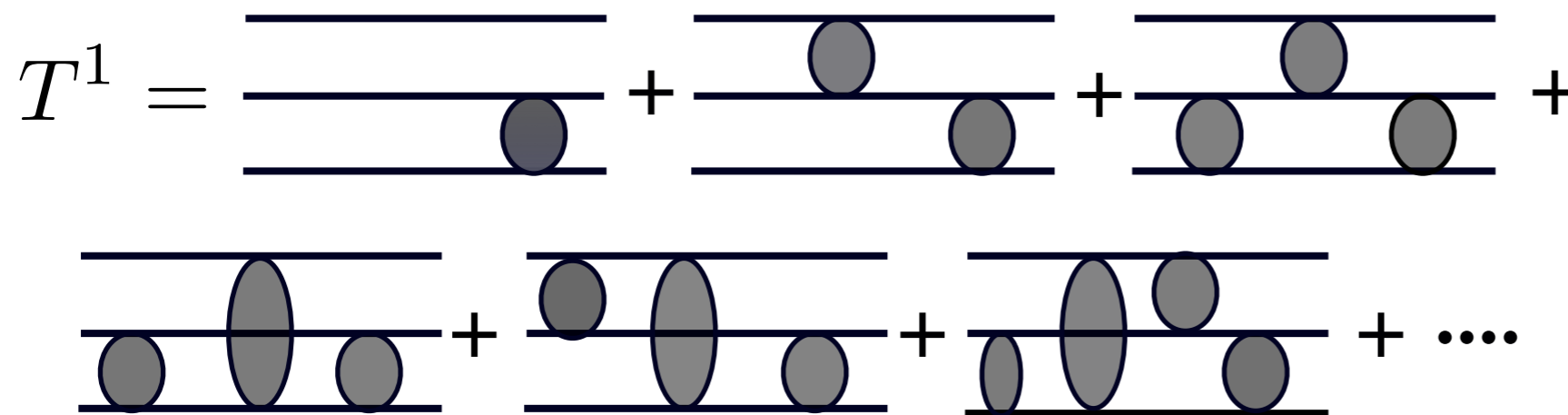
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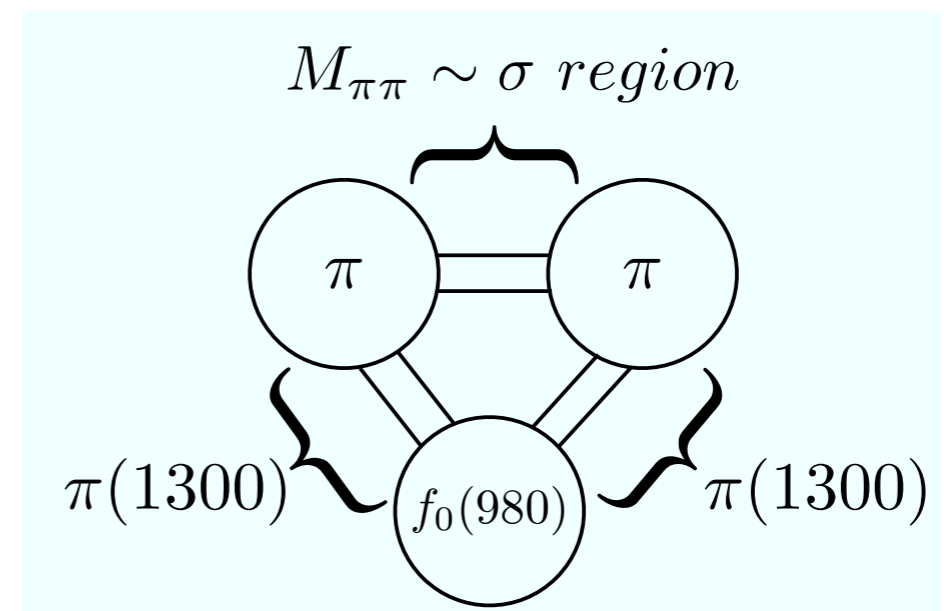
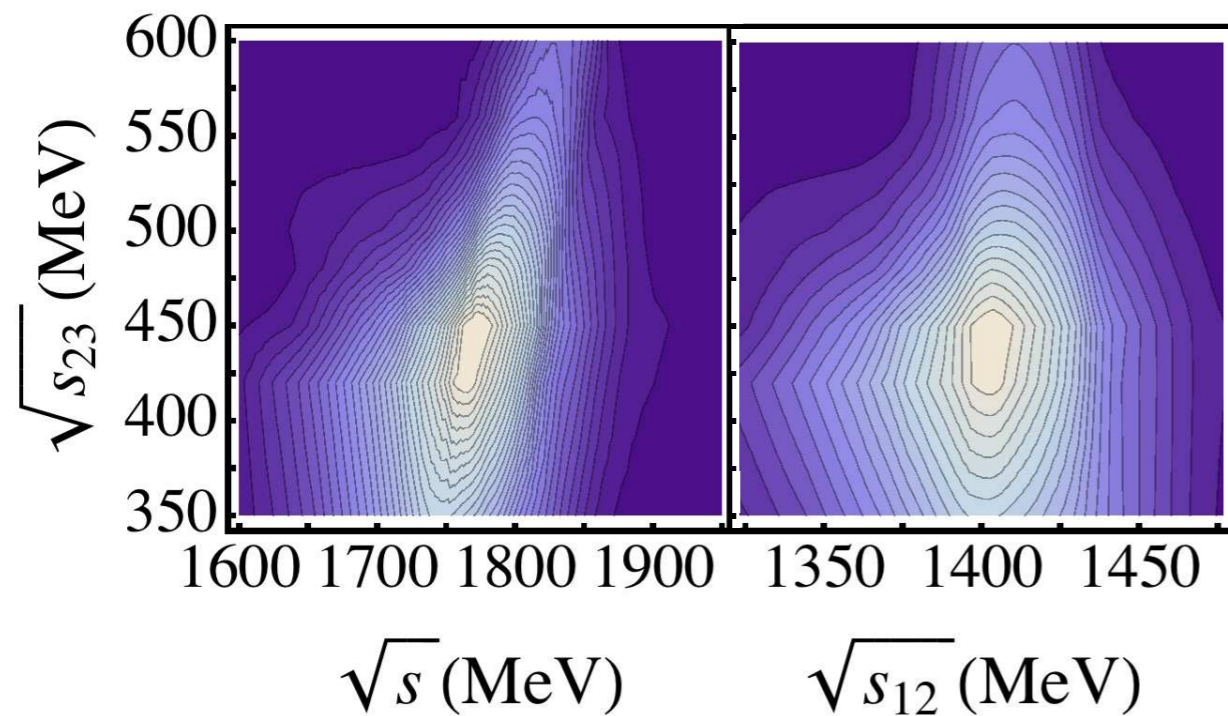
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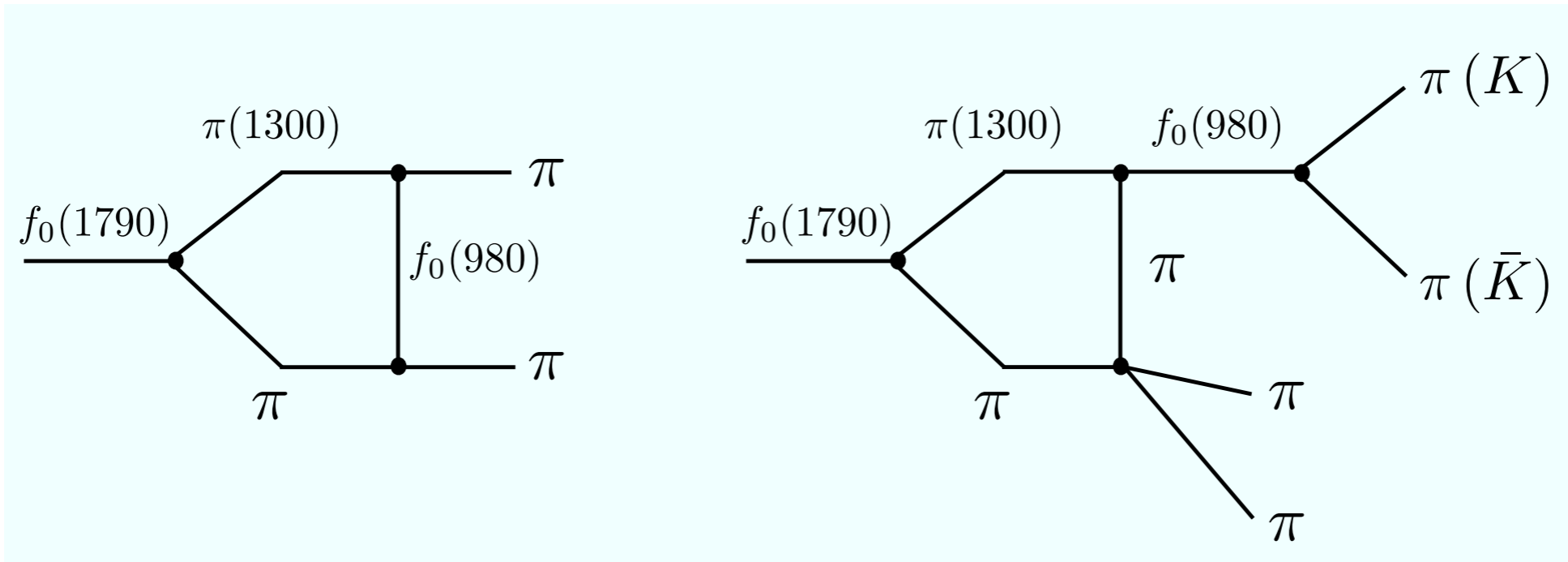


Supporting the existence of $f_0(1790)$ distinct to $f_0(1710)$

- ★ SOLVE FADDEEV EQUATIONS AGAIN FOR $\pi\pi f_0(980)$ SYSTEM.

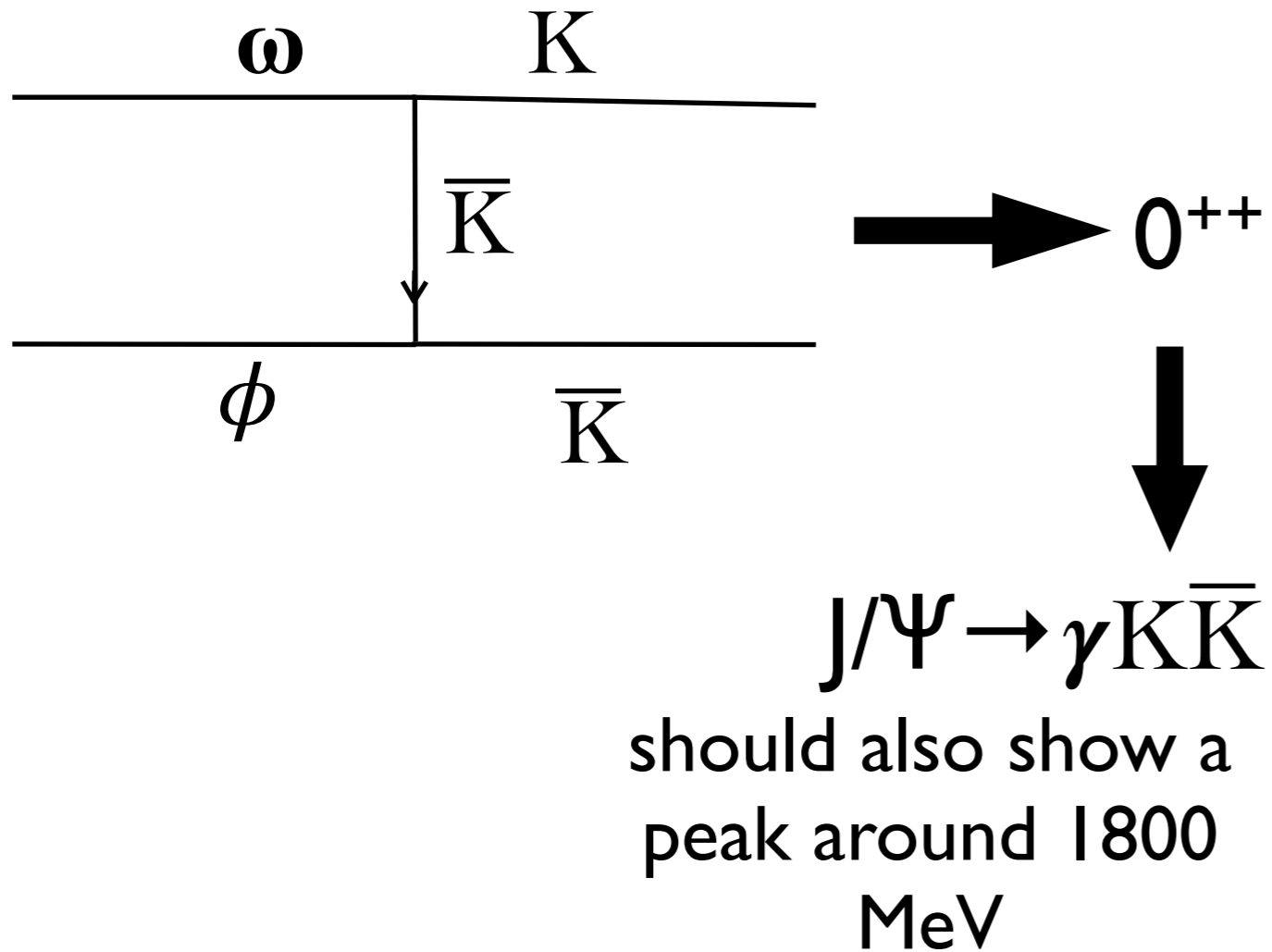


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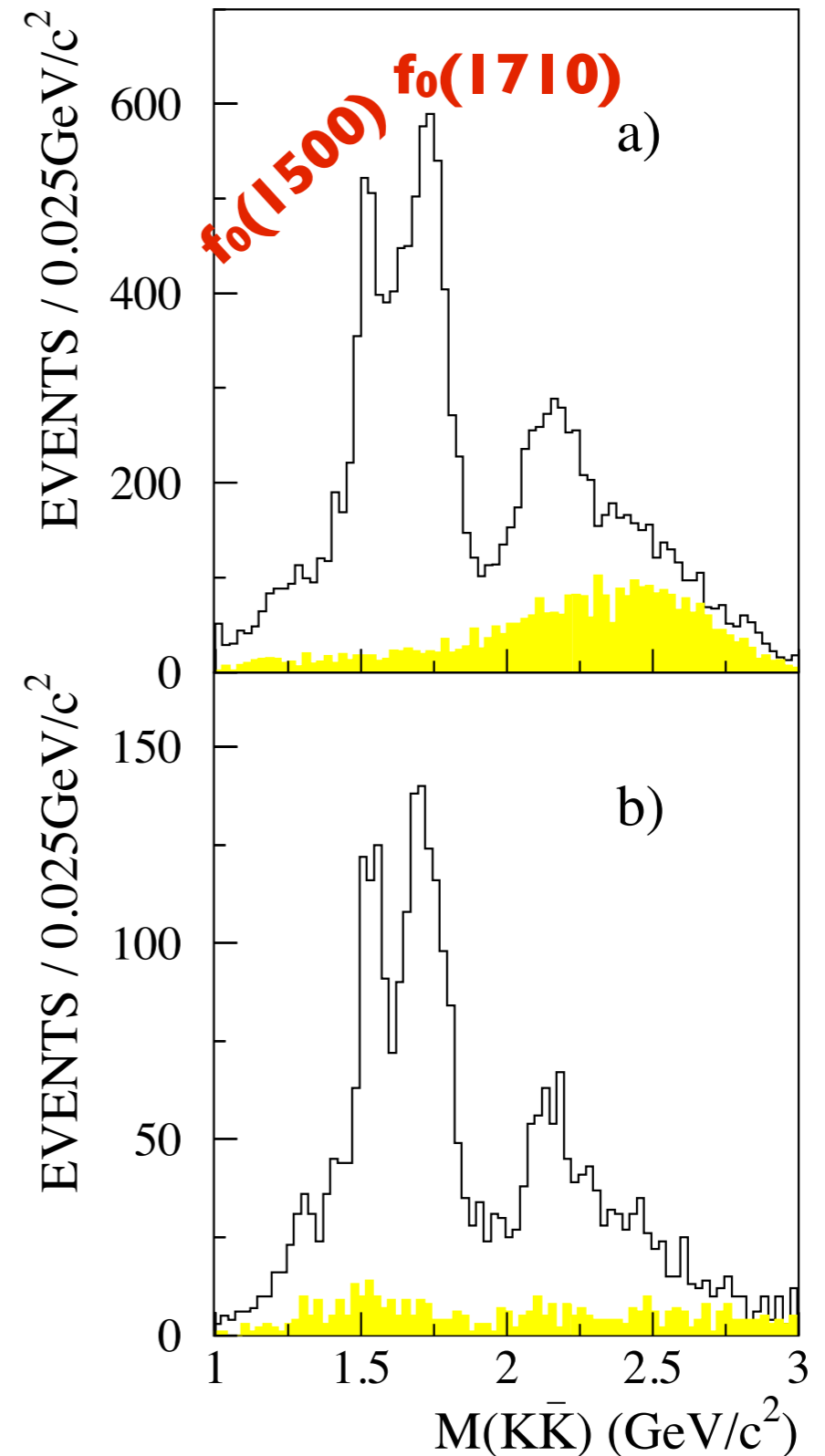


- ✦ Decay mechanisms for $f_0(1790)$ to pions
- ✦ Decay to K anti-K suppressed
- ✦ The resonance structure found in the $\omega\phi$ mass spectrum cannot be related with $f_0(1790)$.

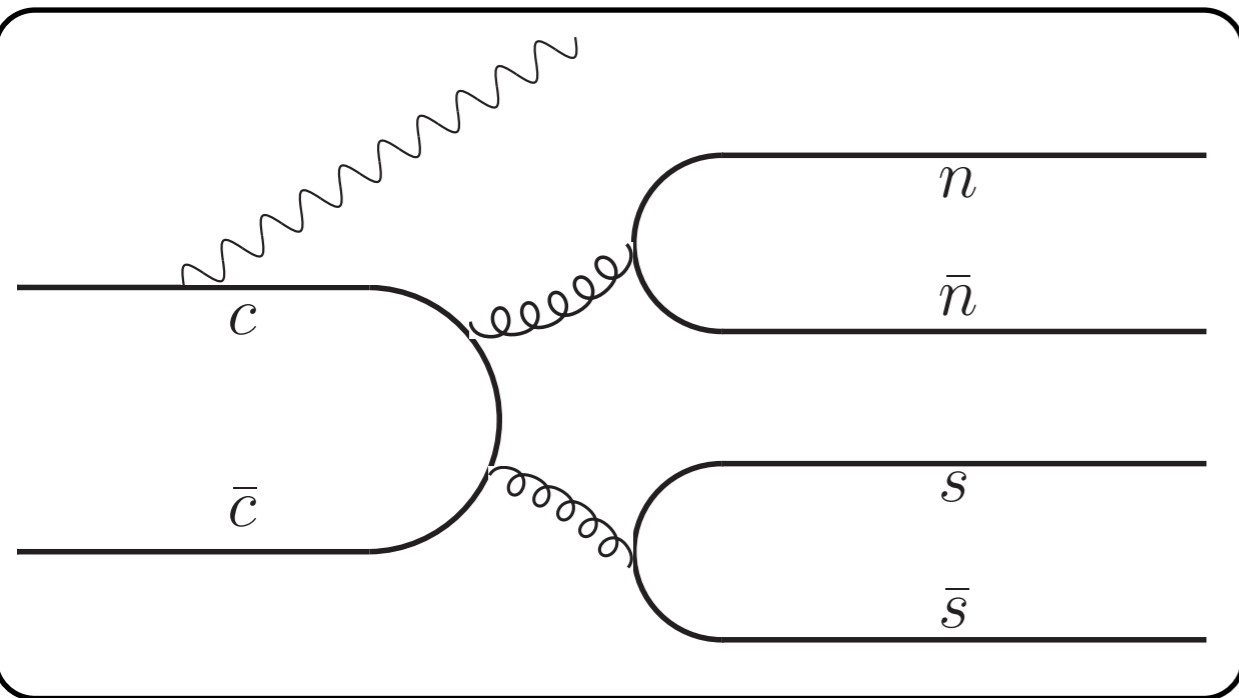
The $J/\psi \rightarrow \gamma \omega \phi$ decay: Flaw in the BES' interpretation?



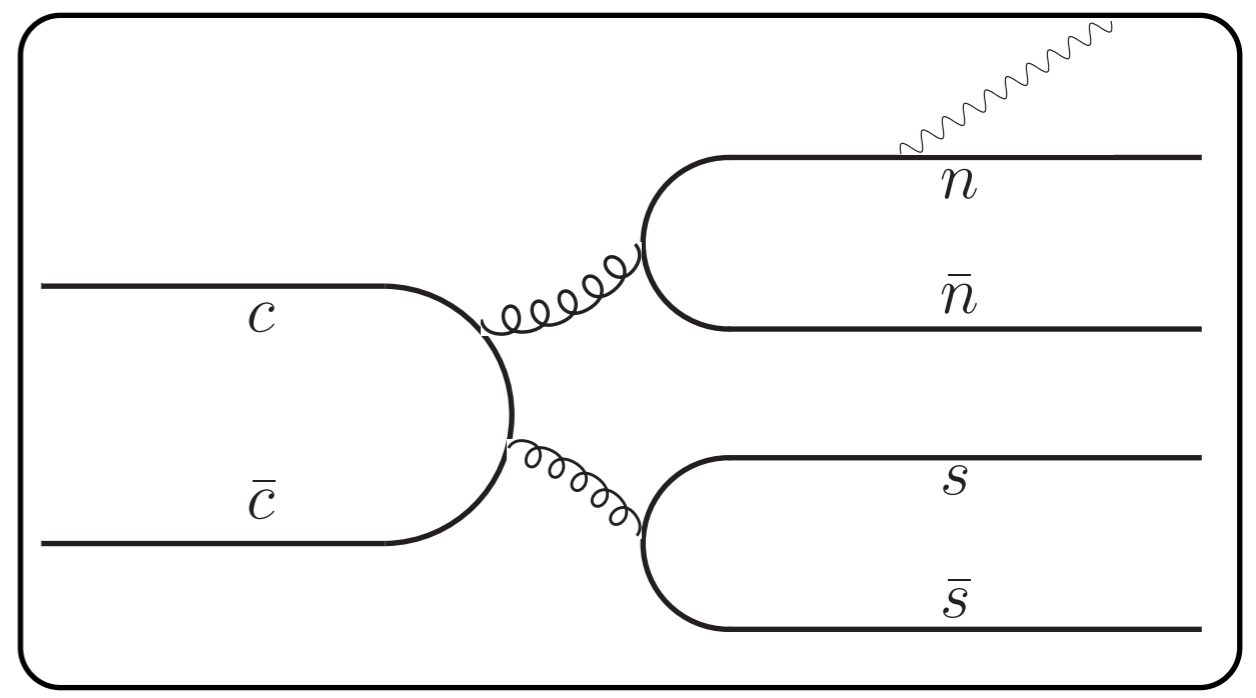
Ref: J. Z. Bai et al. [BES Collaboration],
Phys. Rev. D 68, 052003 (2003)



Formalism to study this process:



(a)



(b)

Two mechanisms of the J/Ψ radiative decays.

* Diagram (b) has been shown to be suppressed (see: *Phys Rept. 174 (1989) 67*, *Eur. Phys. J. A44 (2010) 305*, etc.).

* **DIAGRAM (A) \longrightarrow SU(3) FLAVOR SINGLET FINAL STATE.**

* **VECTOR MESONS FINAL STATE INTERACTION WRITTEN IN TERMS OF A T-MATRIX OBTAINED USING EFFECTIVE FIELD THEORY FOLLOWING *Ref: L. S. Geng and E. Oset, Phys. Rev. D79 (2009) 074009*, WHERE $f_0(1710)$ HAS BEEN FOUND AS A DYNAMICALLY GENERATED RESONANCE.**

Formalism:

- ★ To get an SU(3) singlet in the final state we write:

$$M = \begin{pmatrix} u\bar{u} & u\bar{d} & u\bar{s} \\ d\bar{u} & d\bar{d} & d\bar{s} \\ s\bar{u} & s\bar{d} & s\bar{s} \end{pmatrix}$$

- ★ IT IS THEN EASY TO SHOW THAT $M \cdot M = M \times (u\bar{u} + d\bar{d} + s\bar{s})$  **TR[M.M] GIVES AN SU(3) FLAVOR SINGLET.**

$$V = \begin{pmatrix} \frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & \rho^+ & K^{*+} \\ \rho^- & -\frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & K^{*0} \\ K^{*-} & \bar{K}^{*0} & \phi \end{pmatrix}$$

- ★ IN EFFECTIVE FIELD THEORY APPROACH ONE WRITES THE VECTOR FIELDS AS

- ★ AND CALCULATES TR[V.V]

$$VV_{\text{SU}(3) \text{ singlet}} = \rho^0\rho^0 + \rho^+\rho^- + \rho^-\rho^+ + \omega\omega + K^{*+}K^{*-} + K^{*0}\bar{K}^{*0} + K^{*-}K^{*+} + \bar{K}^{*0}K^{*0} + \phi\phi$$

Formalism:

✦ isospin projections of different VV channels:

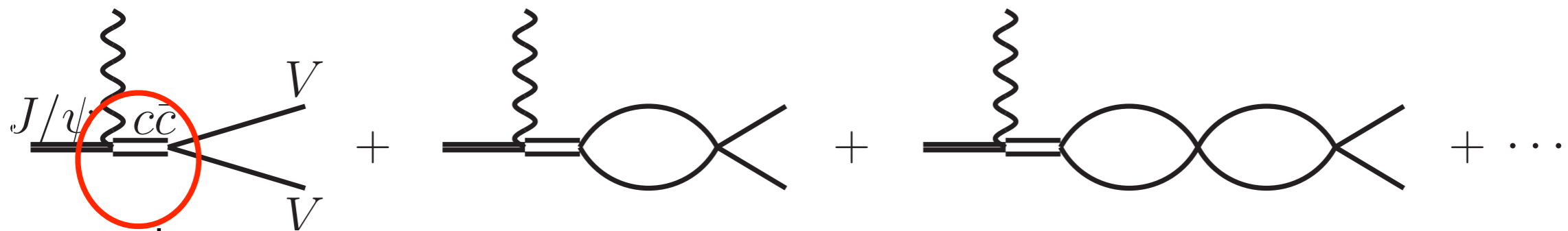
$$|\rho\rho\rangle_{I=0} = -\frac{1}{\sqrt{6}}|\rho^0\rho^0 + \rho^+\rho^- + \rho^-\rho^+\rangle,$$

$$|K^*\bar{K}^*\rangle_{I=0} = -\frac{1}{2\sqrt{2}}|K^{*+}K^{*-} + K^{*0}\bar{K}^{*0} + K^{*-}K^{*+} + \bar{K}^{*0}K^{*0}\rangle$$

$$|\omega\omega\rangle_{I=0} = \frac{1}{\sqrt{2}}|\omega\omega\rangle,$$

$$|\phi\phi\rangle_{I=0} = \frac{1}{\sqrt{2}}|\phi\phi\rangle,$$

✦ **USING THESE STATES, AND RELATING $\text{TR}[M.M]$ WITH $\text{TR}[V.V]$, WE CAN CALCULATE THE WEIGHT FACTOR FOR THE HADRONIZATION OF THE Q ANTI-Q TO DIFFIERENT STATES.**



$A\omega_j$

$$t_{J/\Psi \rightarrow \gamma\phi\omega} = A \sum_{j=1}^4 w_j G_j t_{j \rightarrow \phi\omega}$$

weight of the overlap function between the hadron and quark states loop function

Formalism:

$$t_{J/\Psi \rightarrow \gamma \phi \omega} = A \sum_{j=1}^4 w_j G_j t_{j \rightarrow \phi \omega}$$

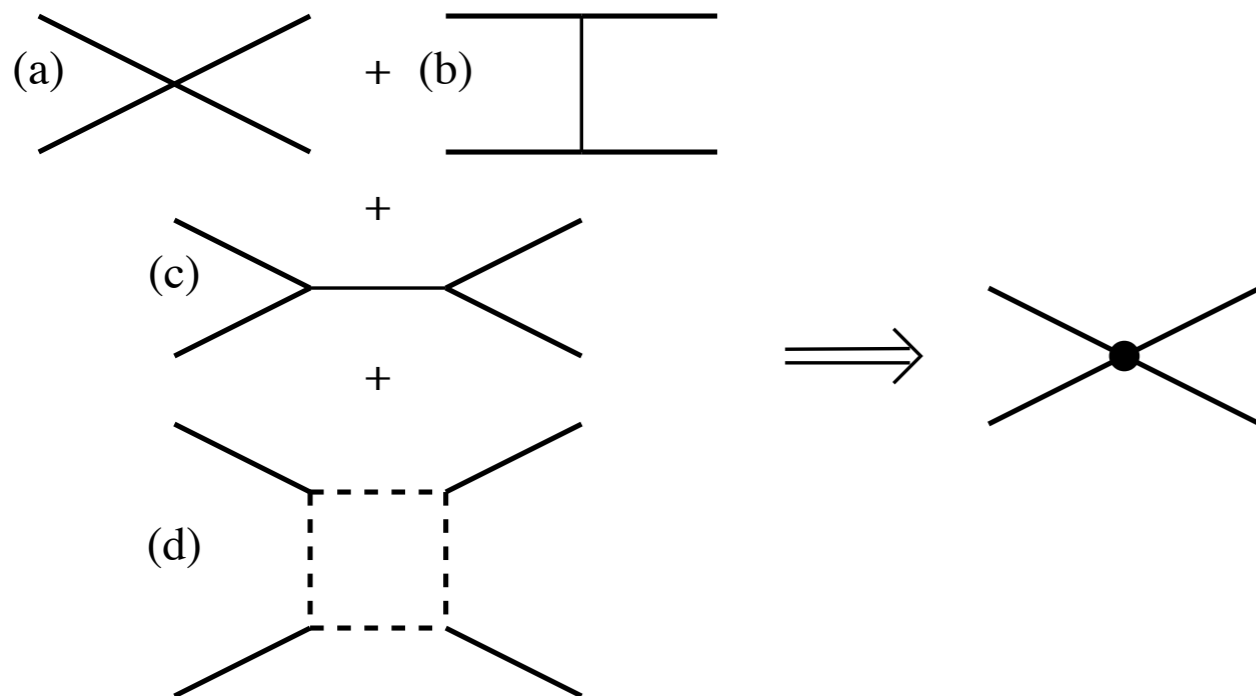


Vector-Vector meson Amplitude → Ref: Geng and Oset, Phys.Rev.D79, (2009) 074009.

Kernel



Bethe-Salpeter Equation



- $f_0(1710)$ found as dynamically generated state

- Use the coupling of the channels to the corresponding pole in the complex plane)

$$t_{i \rightarrow j} = \frac{g_i g_j}{s - M_R^2 + i M_R \Gamma_R}$$

Formalism:

- With the $J/\Psi \rightarrow \gamma \omega \phi$ amplitude we calculate the $\omega \phi$ mass distribution as

$$\frac{d\Gamma}{dM_{\text{inv}}} = \frac{1}{(2\pi)^3} \frac{1}{4M_{J/\Psi}^2} p_\gamma \bar{q}_\omega |t_{J/\Psi \rightarrow \gamma \phi \omega}|^2$$

$\omega \phi$ invariant mass

where,

$$p_\gamma = \frac{\lambda^{1/2}(M_{J/\Psi}^2, 0, M_{\text{inv}}^2)}{2M_{J/\Psi}}$$

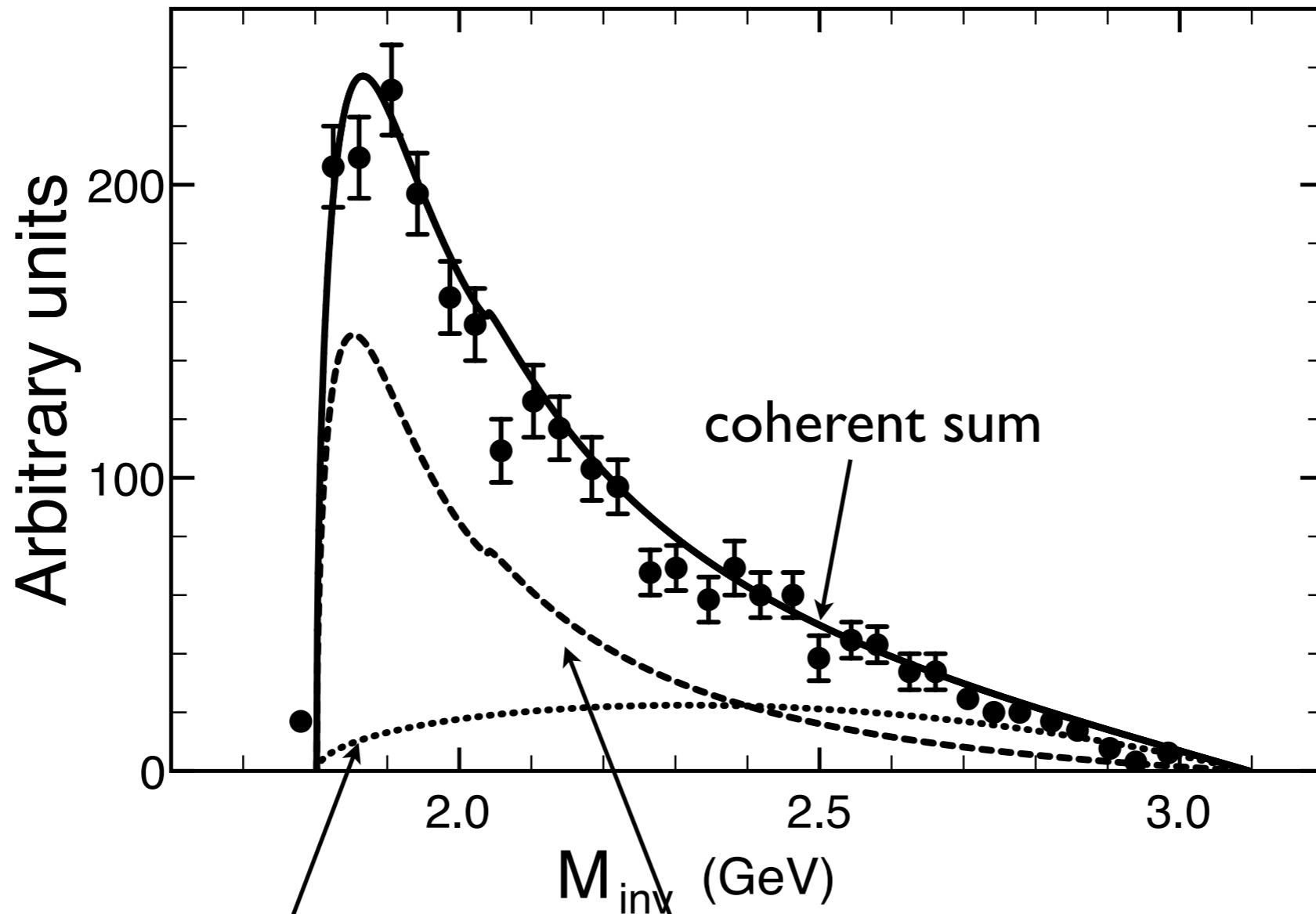
photon momentum in the J/Ψ rest frame

$$\bar{q}_\omega = \frac{\lambda^{1/2}(M_{\text{inv}}^2, m_\omega^2, m_\phi^2)}{2M_{\text{inv}}}$$

ω momentum in the $\omega \phi$ rest frame

Results:

$\omega\phi$ mass distribution



constant background

contribution from the $f_0(1710)$ resonance

Results:

- We also calculated the Branching ratio of the $J/\Psi \rightarrow \gamma \omega \phi$ amplitude

$$\frac{B(J/\Psi \rightarrow \gamma R \rightarrow \gamma \phi \omega)}{B(J/\Psi \rightarrow \gamma f_0)} = 0.14^{+0.12}_{-0.07}.$$

from exptl data

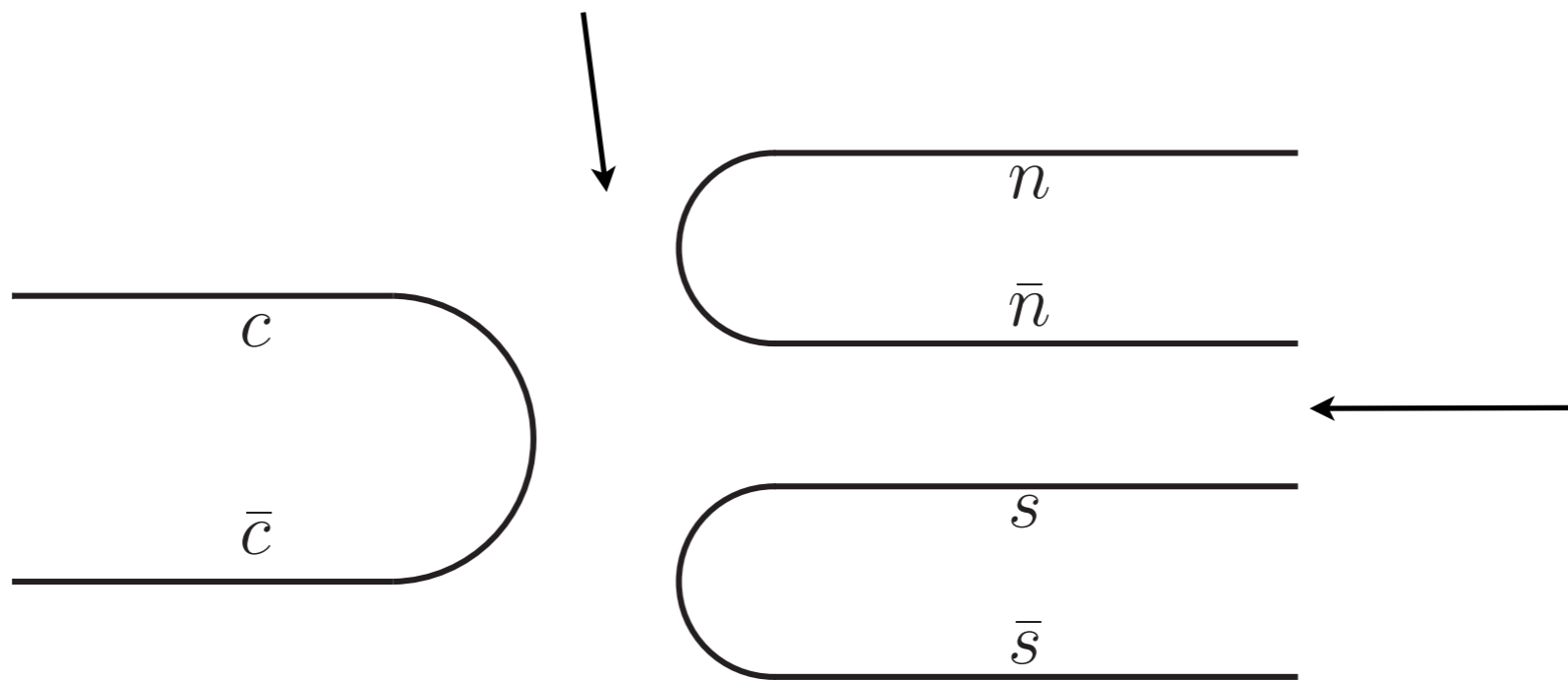
Our result: $0.15^{+0.07}_{-0.04}$

Summary:

- We argue that the cross section enhancements found in the data on the $J/\psi \rightarrow \gamma \omega \phi$ and the $J/\psi \rightarrow \pi^+ \pi^- \phi$ decay in the similar energy region are due to two distinct resonances.
- We find a scalar resonance in the $\pi\pi$ $f_0(980)$ system with the properties very similar to the $f_0(1790)$ found in the $\pi^+ \pi^-$ spectrum in the $J/\psi \rightarrow \pi^+ \pi^- \phi$ decay.
- We find an explanation of the suppressed decay of $f_0(1790)$ to K -anti- K channel.
- Further, we interpret the peak near 1800 MeV in the $J/\psi \rightarrow \gamma \omega \phi$ decay as the signature of the $f_0(1710)$ resonance which is dynamically generated within the effective field theory calculations of the VV systems.

Summary:

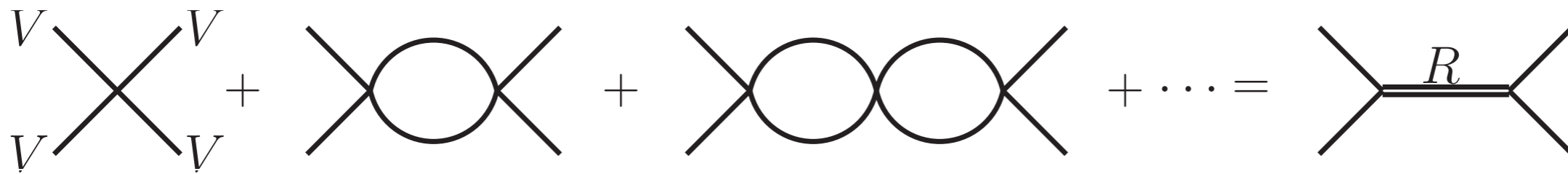
- This explains why no peak is seen in the K anti- K mass distribution near 1800 MeV.
- We can reproduce the experimental data (mass distribution and branching ratio) obtained by the BES collaboration.
- Thus, there are two scalar resonances in 1700-1800 MeV region: $f_0(1710)$ and $f_0(1790)$.



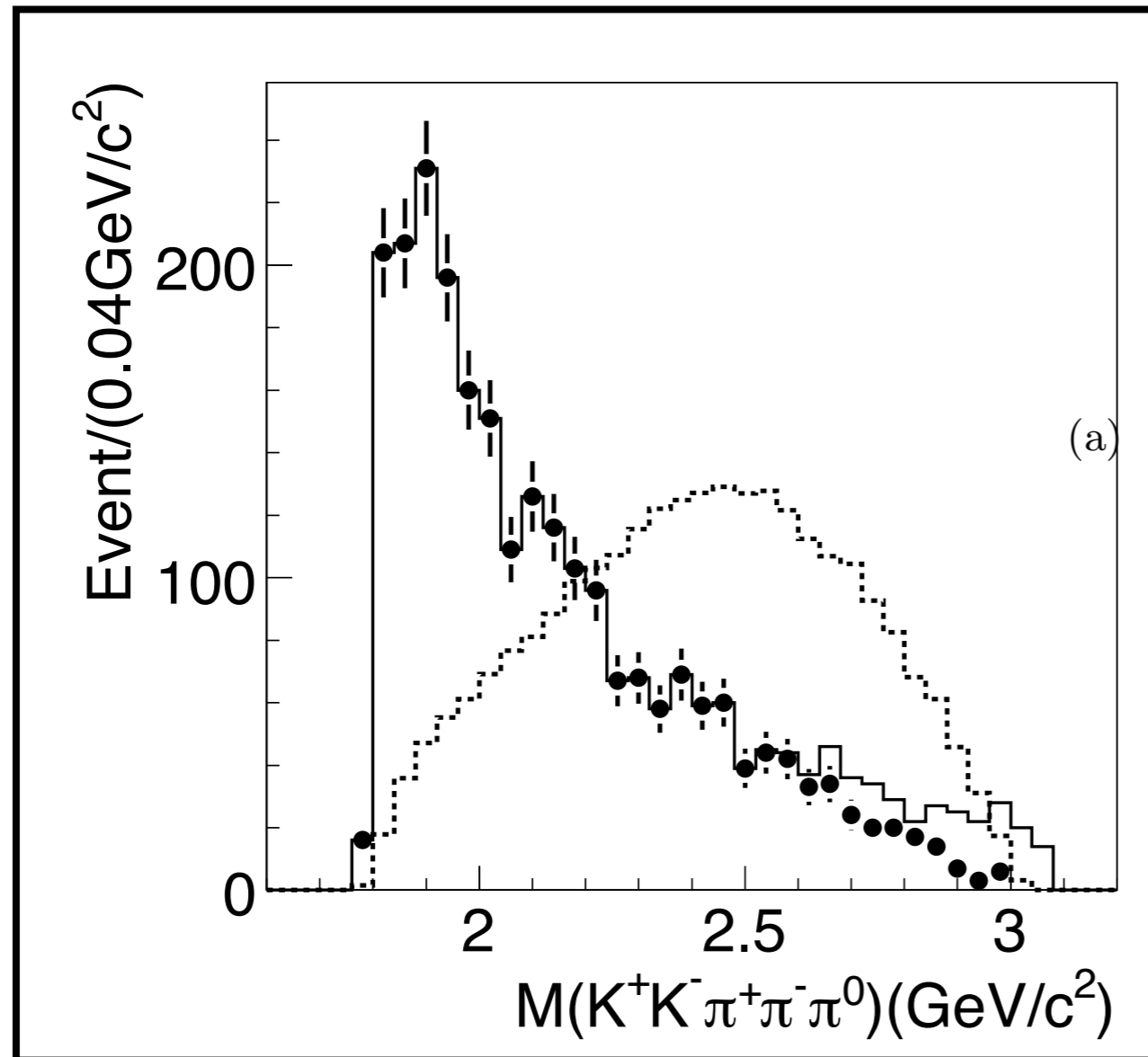
✦ Doubly OZI suppressed

Formalism

- ★ $f_0(1710)$ has been found to arise due to two vector meson dynamics. (Ref: L. S. Geng and E. Oset, Phys. Rev. D79 (2009) 074009).



- ★ IT WAS FOUND TO COUPLE DOMINANTLY TO THE K^* ANTI- K^* CHANNEL.
- ★ COUPLED CHANNELS: $\rho\rho, \omega\omega, \Phi\Phi, K^* \text{ anti-}K^*, \omega\Phi$.



arXiv:1209.4813 [hep-ex]

$$M = 1795 \pm 7 + 23 - 5 \text{ MeV}$$

$$\Gamma = 95 \pm 10 + 78 - 34 \text{ MeV}$$

HIGHER STATISTICS RESULTS FROM BESIII