

Reanalysis of the $e^+e^- \rightarrow D^*\bar{D}^*\pi$ reaction and the claim for the $Z_c(4025)$ resonance

Alberto Martínez Torres

(in collaboration with K. P. Khemchandani, F. S. Navarra, M. Nielsen and E. Oset)

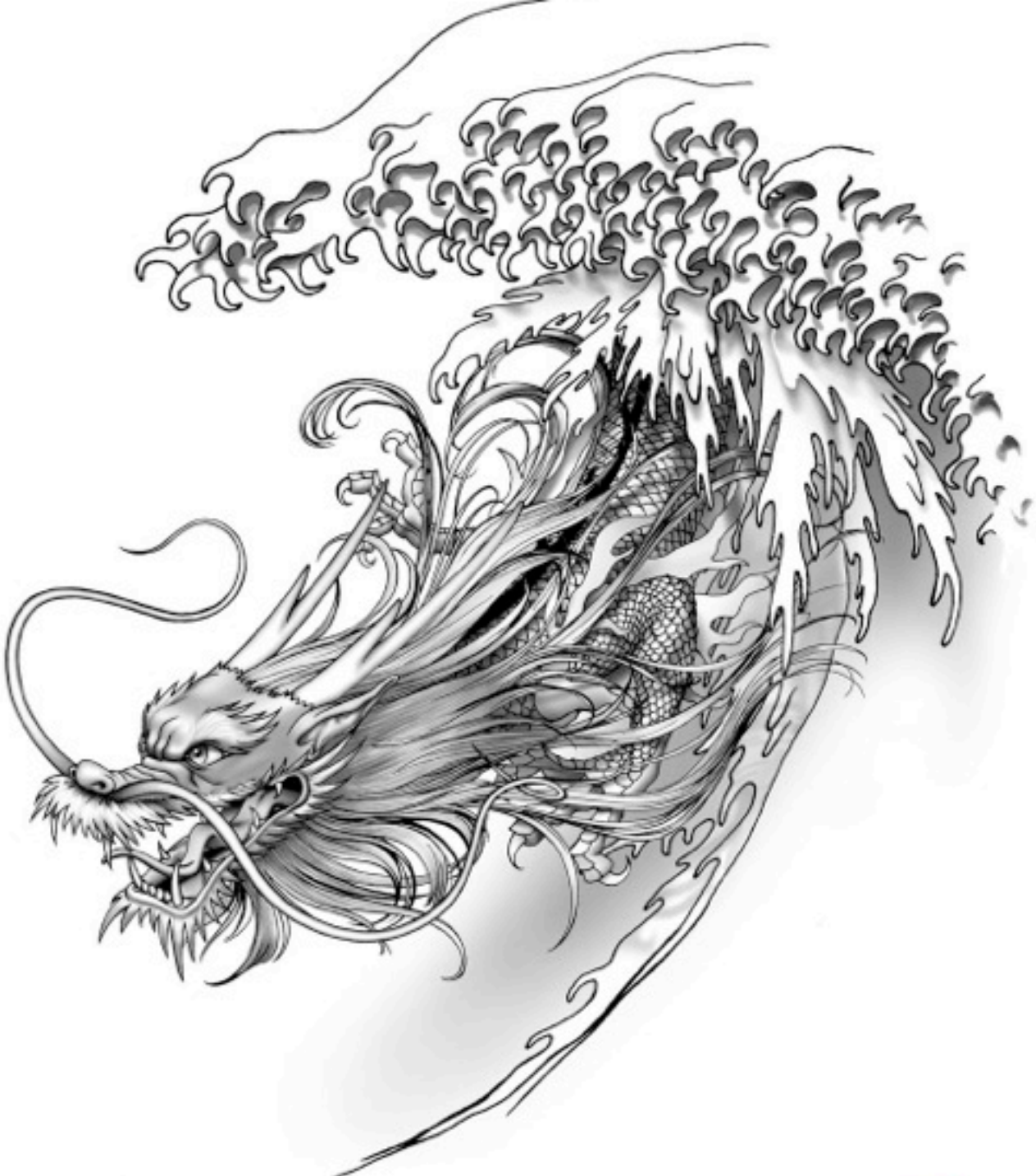
Instituto de Física, Universidade de São Paulo, Brazil,
26-10-2013, Beihang University, China.

Reanalysis of the $e^+e^- \rightarrow D^*D^*\pi$ reaction and the claim for the $Z_c(4025)$ resonance

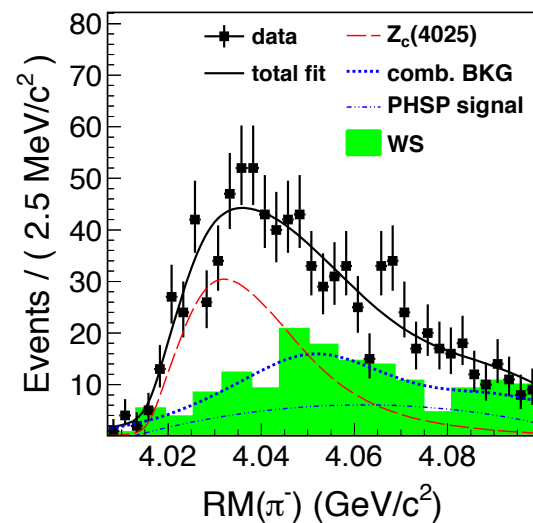
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- BESIII claims the existence of a resonance in the reaction $e^+e^- \rightarrow (D^* \bar{D}^*)^\pm \pi^\mp$ at $\sqrt{s} = 4.26$ GeV (arXiv:1308.2760 [hep-ex]).



$Z_c(4025)$ {

- Mass $(4026.3 \pm 2.6 \pm 3.7)$ MeV
- width $(24.8 \pm 5.6 \pm 7.7)$ MeV
- $I=1, J^P=1^+$ ($D^* \bar{D}^*$ in S-wave)

- Theoretical interpretations: 2^+ tetraquark state, $1^+ D^* \bar{D}^*$ states using HQSS, QCD sum rules, pion exchange, etc.¹

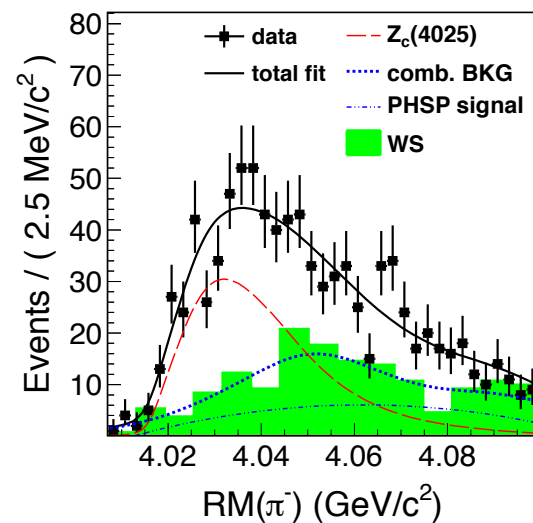


Masses compatible with $Z_c(4025)$, but large uncertainties

¹ Guo, Hidalgo-Duque, Nieves, PRD88,054007 (2013); Chen, Steele, Du, Zhu, arxiv: 1308.5060[hep-ph].
Cui, Liu, Huang, arxiv: 1308.3625 [hep-ph]; He, Liu, Sun, Zhu, arxiv: 1308.2999; Qiao, Tang, arxiv: 1308.3439 [hep-ph]

INTRODUCTION

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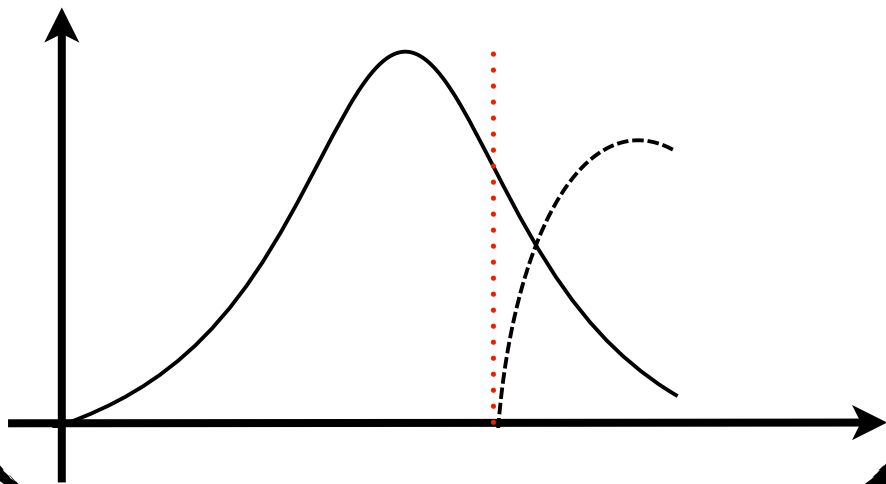
INTRODUCTION



- The peak is just 10 MeV above the threshold.
- Peaks close to the threshold can be due to a state below the threshold (EPJA36,189; PLB719,388; arxiv:1306.6594 [hep-ph]).
- In Wan, Sun, et al., arxiv:1308.3158, they show some enhancement close to threshold can occur.

INTRODUCTION

A Bound state?

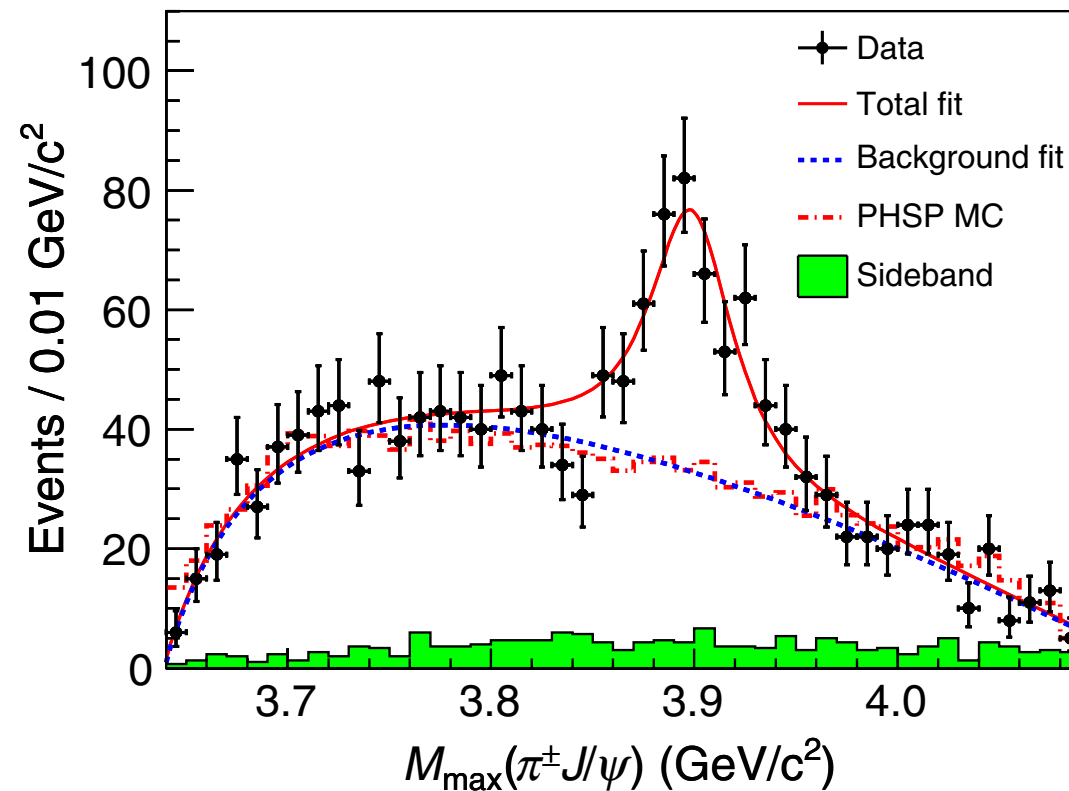


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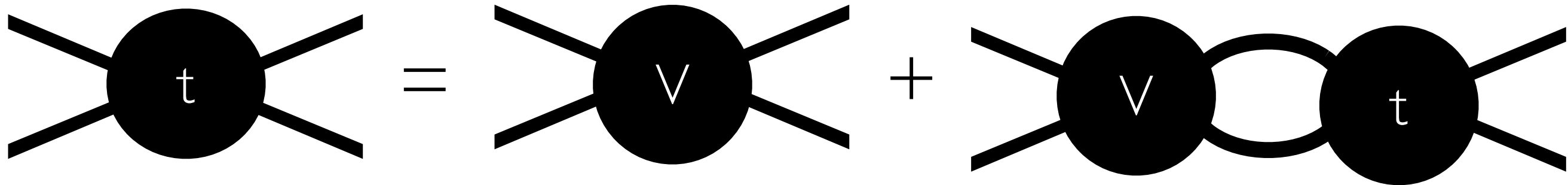
- If $J^P = 1^+$, Z_c can decay to $\pi J/\psi$. The process $e^+e^- \rightarrow \pi^+ \pi^- J/\psi$ at $\sqrt{s} = 4.26$ GeV only shows the $Z_c(3900)$ (BESIII, PRL 110, 252001).



- A single channel with an energy independent potential can generate bound states, but not resonances (Yamagata-Nieves-Oset, PRD83, 014003).

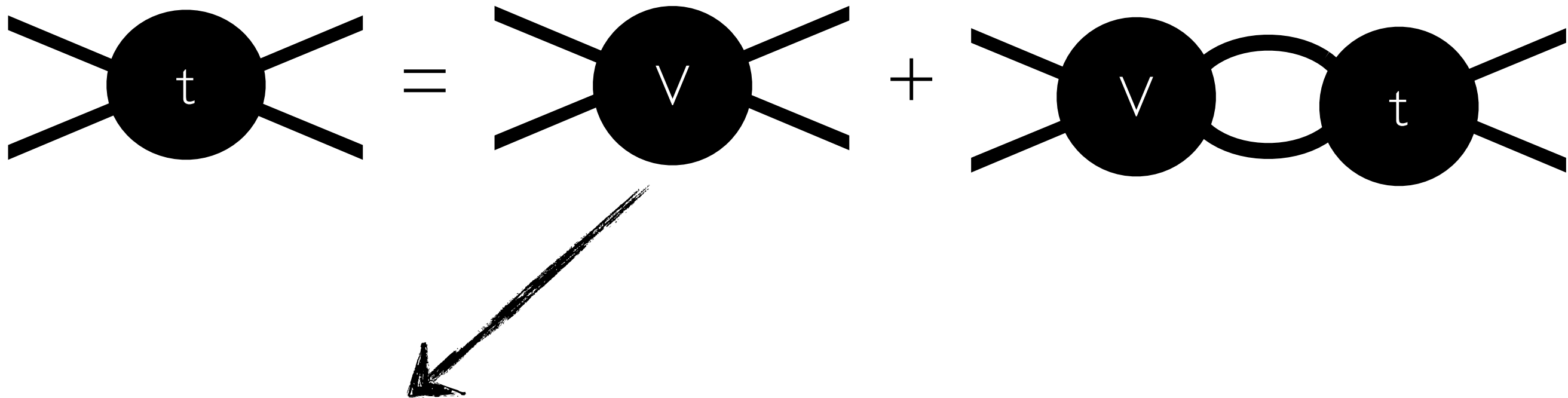
THE $D^* \bar{D}^*$ SYSTEM

- Studied using effective field theories based on the hidden local symmetry and solving the Bethe-Salpeter equation (Molina, Oset, PRD80, 114013).



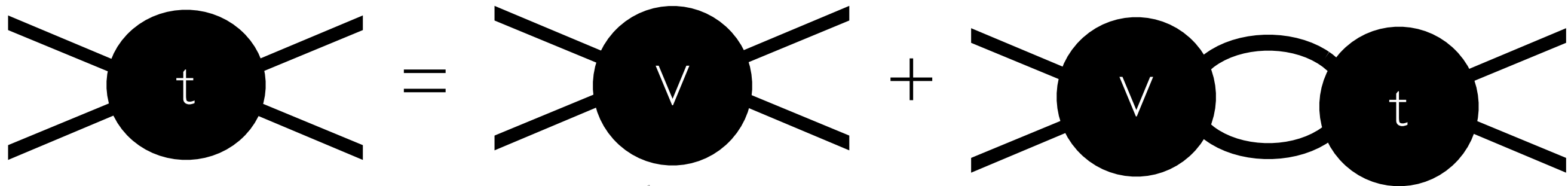
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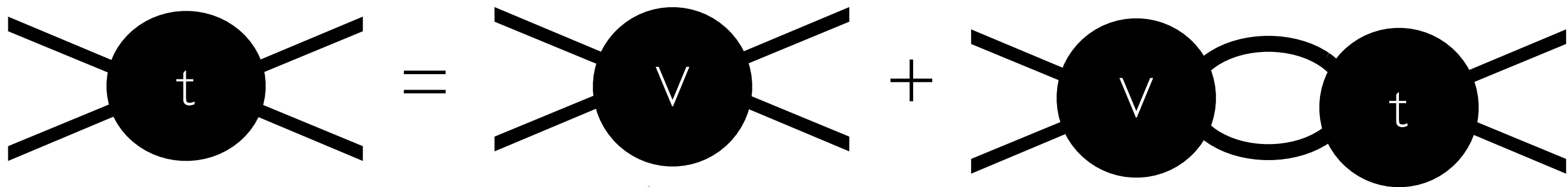
$$P^{(0)} = \frac{1}{3} \vec{\epsilon} \cdot \vec{\epsilon}' \delta_{km},$$

$$P^{(1)} = \frac{1}{2} (\epsilon_m \epsilon'_k - \epsilon_k \epsilon'_m),$$

$$P^{(2)} = \frac{1}{2} (\epsilon_m \epsilon'_k + \epsilon_k \epsilon'_m) - \frac{1}{3} \vec{\epsilon} \cdot \vec{\epsilon}' \delta_{km}$$

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$Z_c ?$

Mass (3960-3990) MeV

width (120-170) MeV

$l=1, J^P=2^+$

THE $D^* \bar{D}^*$ SYSTEM

- QCD sum rules (Khemchandani, Martínez Torres, Nielsen, Navarra et al., arxiv: 1310.0862 [hep-ph])

$$j_{\mu\nu}(x) = [\bar{c}_a(x) \gamma_\mu u_a(x)] [d_b(x) \gamma_\nu c_b(x)]$$

$$\Pi_{\mu\nu\alpha\beta}(q^2) = i \int d^4x e^{iqx} \langle 0 | T [j_{\mu\nu}(x) j_{\alpha\beta}^\dagger(0)] | 0 \rangle$$

$$\mathcal{P}^{(0)} = \frac{1}{3} \Delta^{\mu\nu} \Delta^{\alpha\beta},$$

$$\mathcal{P}^{(1)} = \frac{1}{2} (\Delta^{\mu\alpha} \Delta^{\nu\beta} - \Delta^{\mu\beta} \Delta^{\nu\alpha}),$$

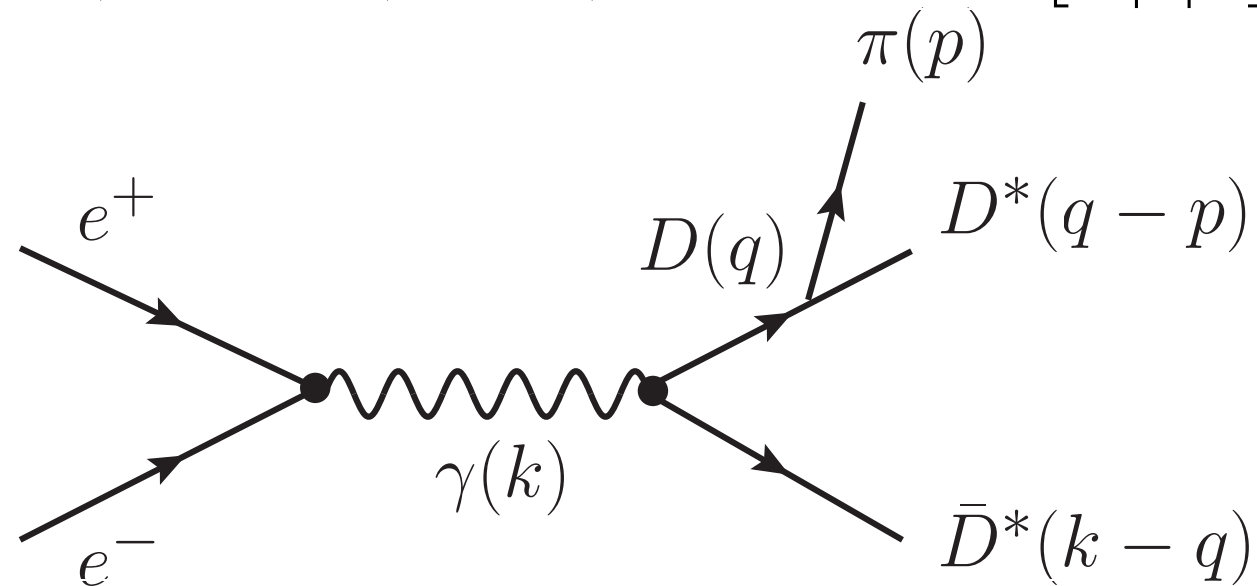
$$\mathcal{P}^{(2)} = \frac{1}{2} (\Delta^{\mu\alpha} \Delta^{\nu\beta} + \Delta^{\mu\beta} \Delta^{\nu\alpha}) - \frac{1}{3} \Delta^{\mu\nu} \Delta^{\alpha\beta}$$

$$\Delta_{\mu\nu} \equiv -g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2}.$$

- Results: three nearly spin degenerated states ($0^+, 1^+, 2^+$) with masses 3950 ± 100 MeV.

FORMALISM

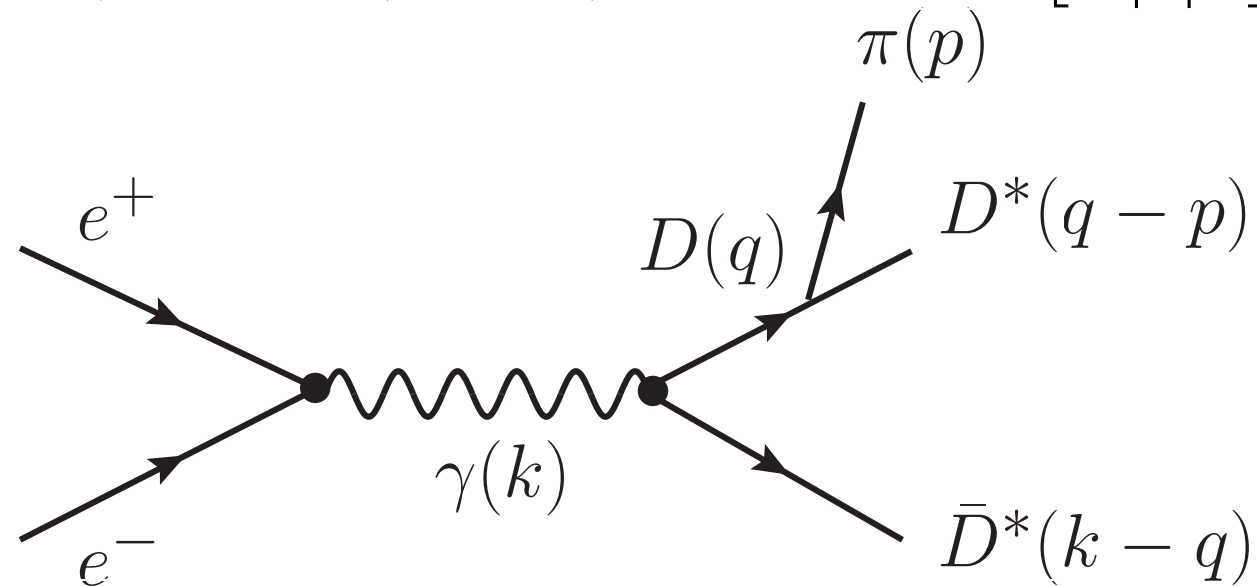
- D -wave production of a 2^+ bound state (A. Martínez Torres, K. P. Khemchandani, F. S. Navarra, M. Nielsen, E. Oset, arXiv:1310.1119 [hep-ph])



$$t \propto k^0 \epsilon^{ijk} L_i q_j (q+p)_m \frac{1}{q^2 - m_D^2 + i\epsilon} \epsilon_k(\bar{D}^*) \epsilon_m(D^*)$$

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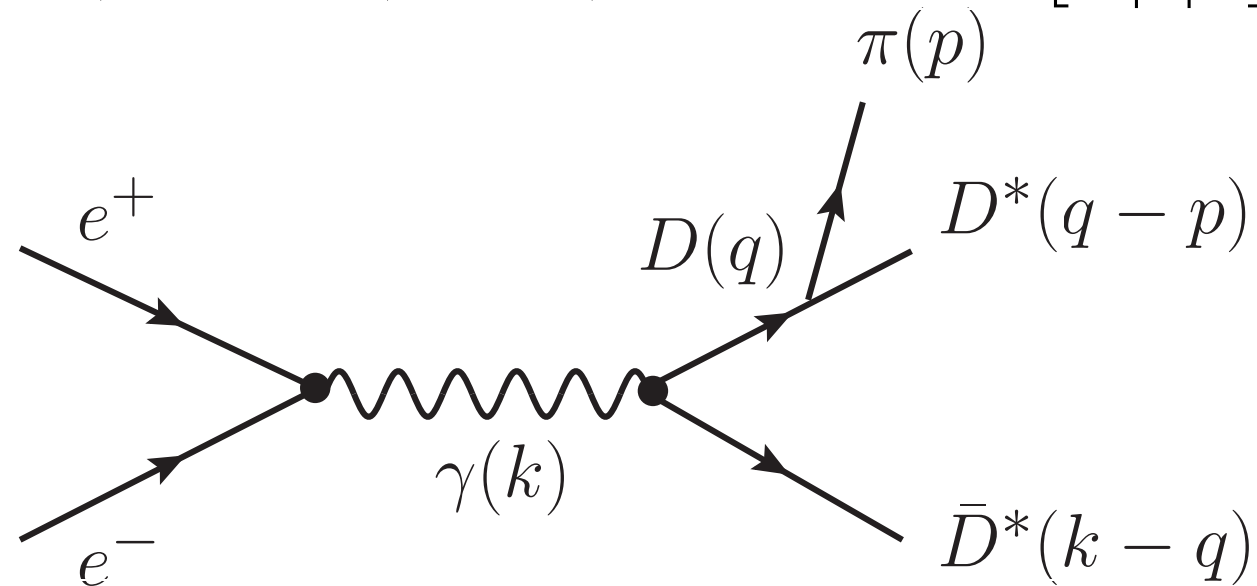


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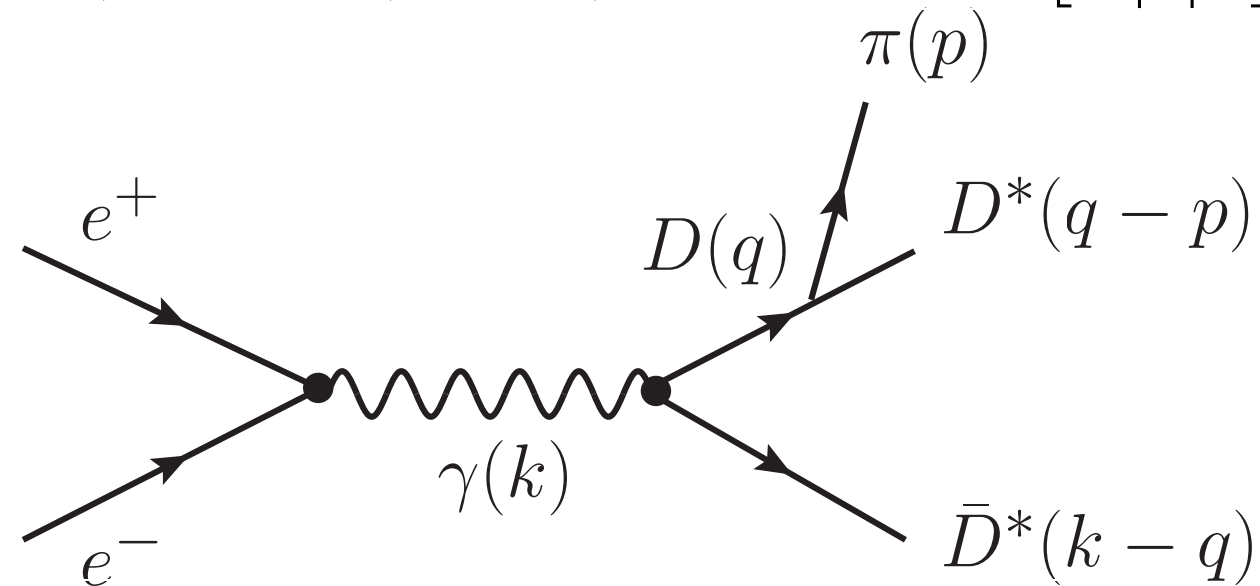


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D -wave

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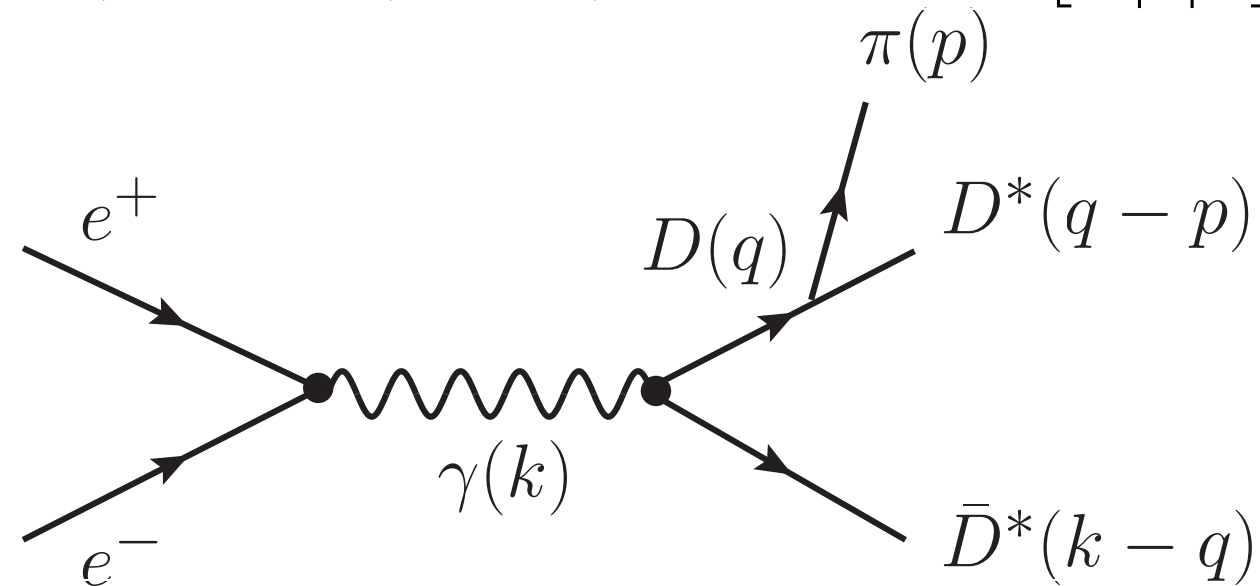


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\swarrow D -wave \swarrow

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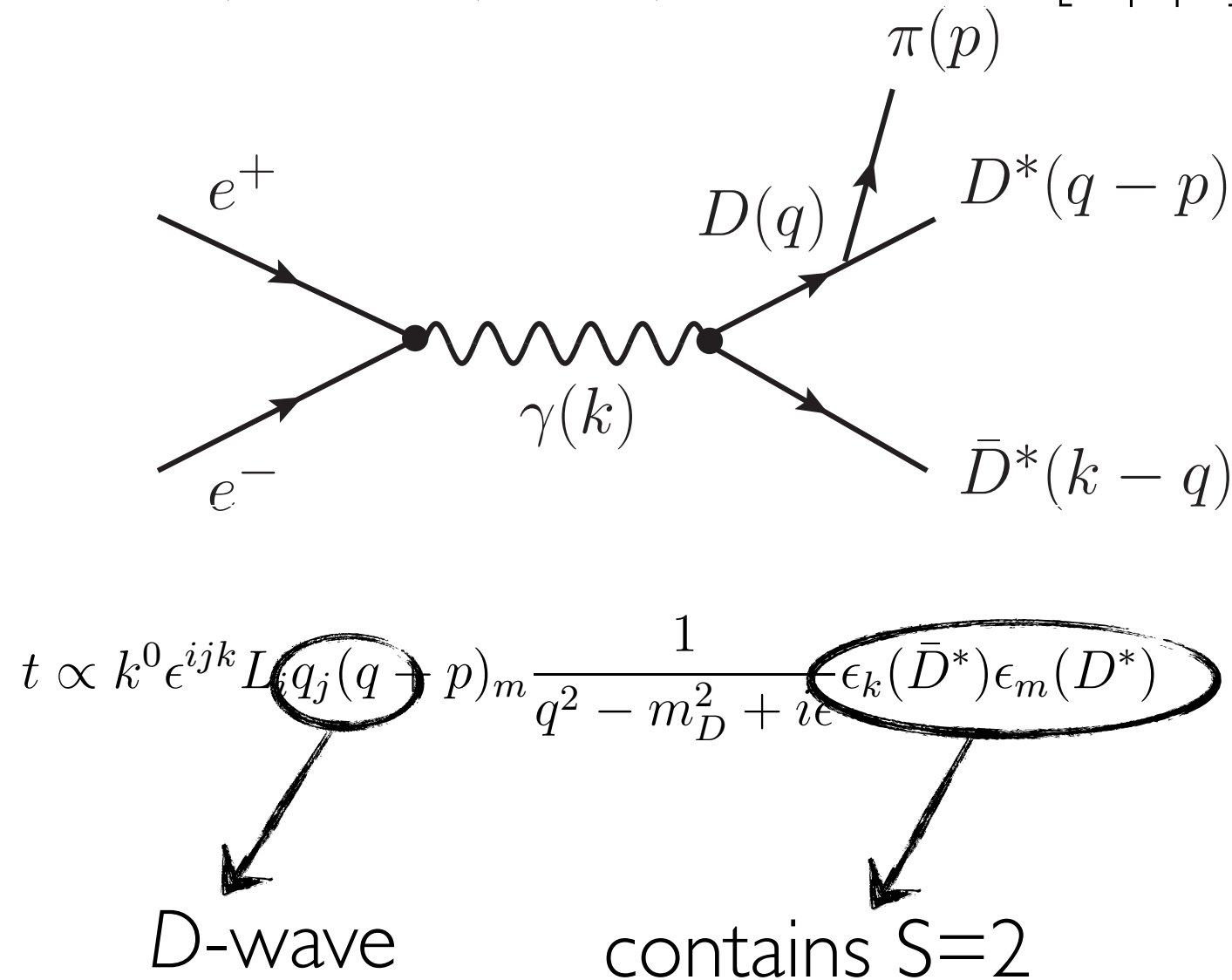


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\swarrow
D-wave
 \swarrow
contains $S=2$

FORMALISM

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- The D -wave character and the spin 2 structure is preserved upon interaction of the final $D^* \bar{D}^*$ states

FORMALISM

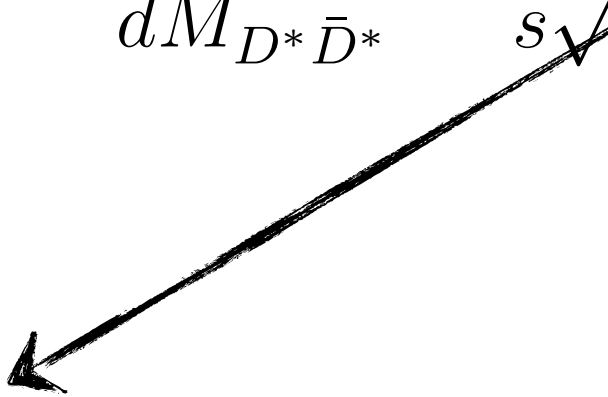
- Invariant mass distribution:

$$\frac{d\sigma}{dM_{D^*\bar{D}^*}} = \frac{m_e^2}{s\sqrt{s}} p\tilde{q} (|T|^2 F_L + B) + \text{WS}$$

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momentum

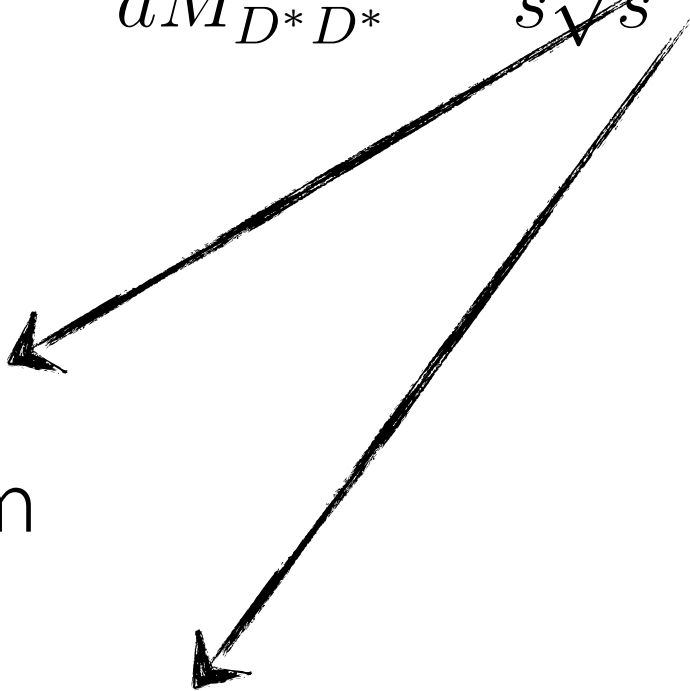


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D^* momentum
in $D^*\bar{D}^*$ rest frame

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$$T = \frac{A}{M_{D^*\bar{D}^*}^2 - M_R^2 + iM_R\Gamma_R}$$

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phase space
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combinatorial
backgrounds
(D^+ with a π of
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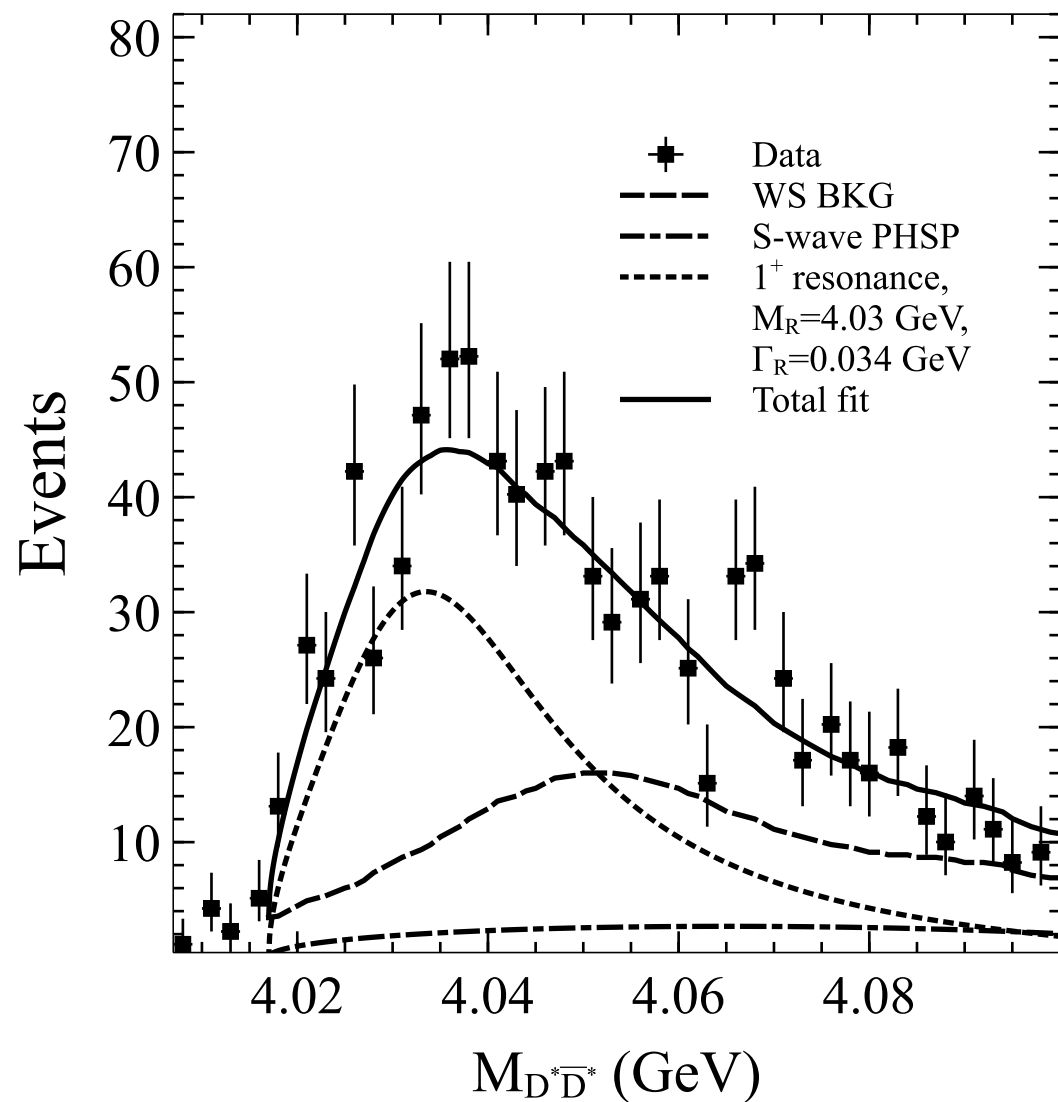
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- We consider A, B, M_R, Γ_R as parameters and perform a fit to the data.
- Good fit: $\chi^2/\text{n.d.o.f} \sim 1$ (BES III experiment: $\chi^2/\text{n.d.o.f} = 0.92$)

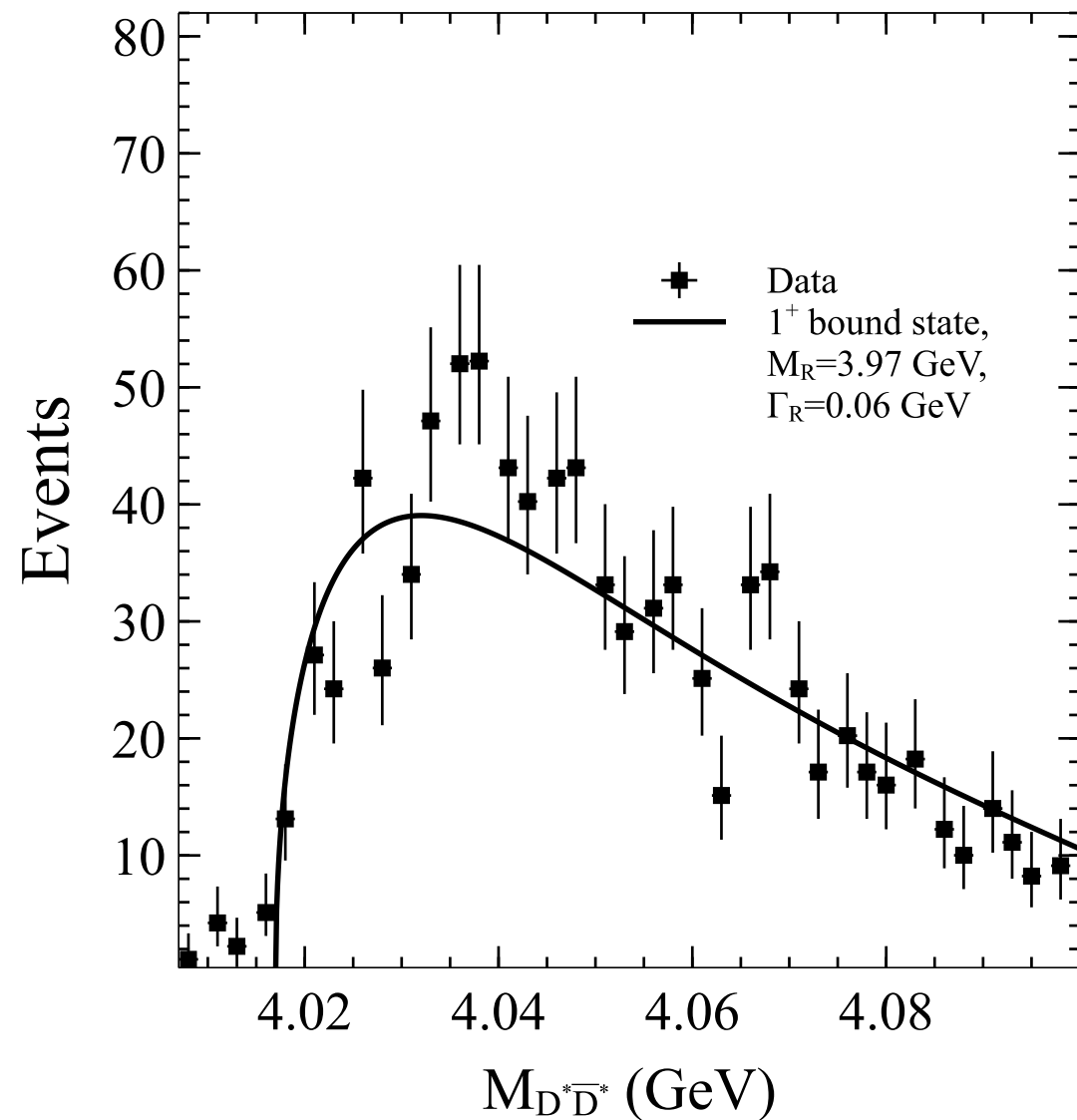
RESULTS

As BESIII



1^+ resonance produced in S-wave
($M=4030$ MeV, $\Gamma=34$ MeV)

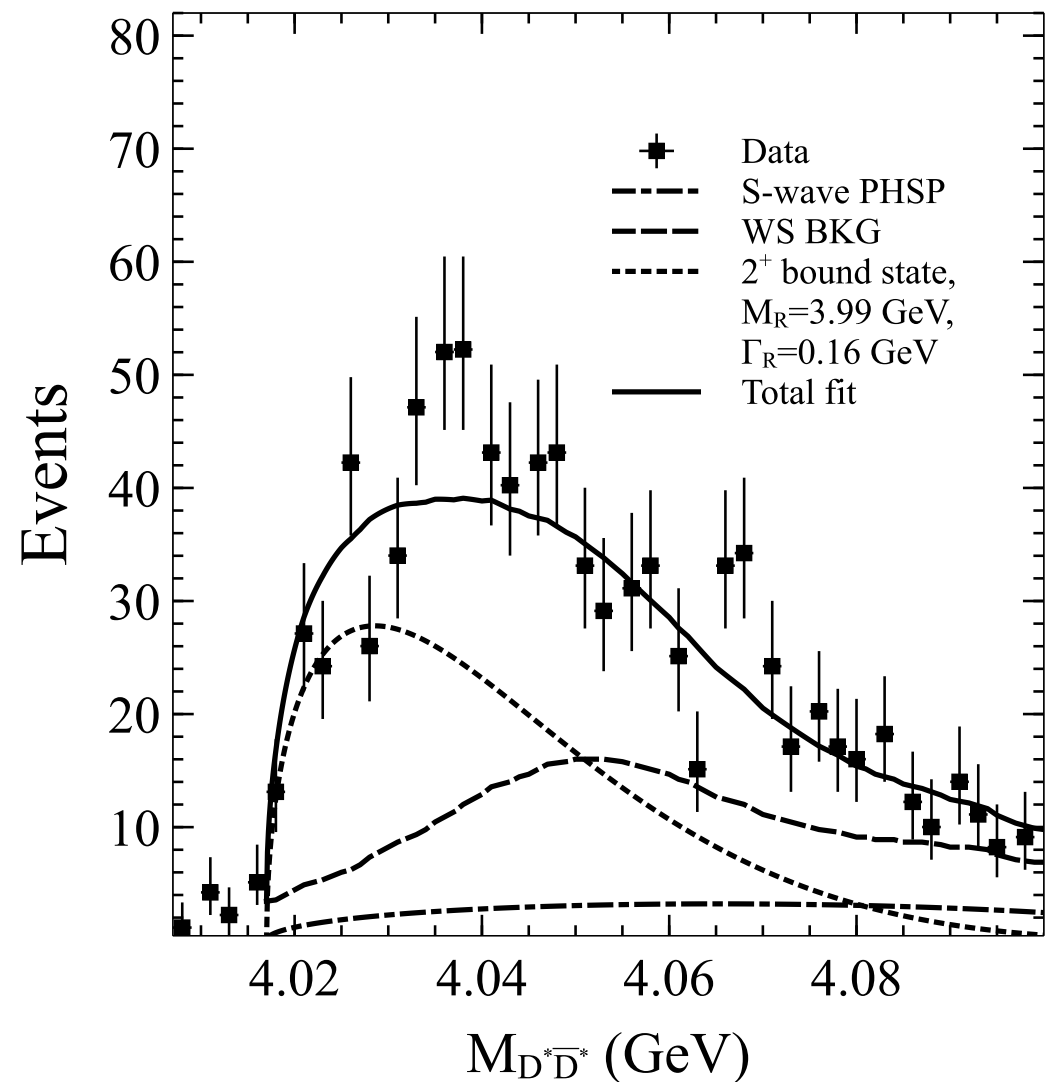
Alternative



1^+ bound state produced in S-wave
($M=3970$ MeV, $\Gamma=60$ MeV)

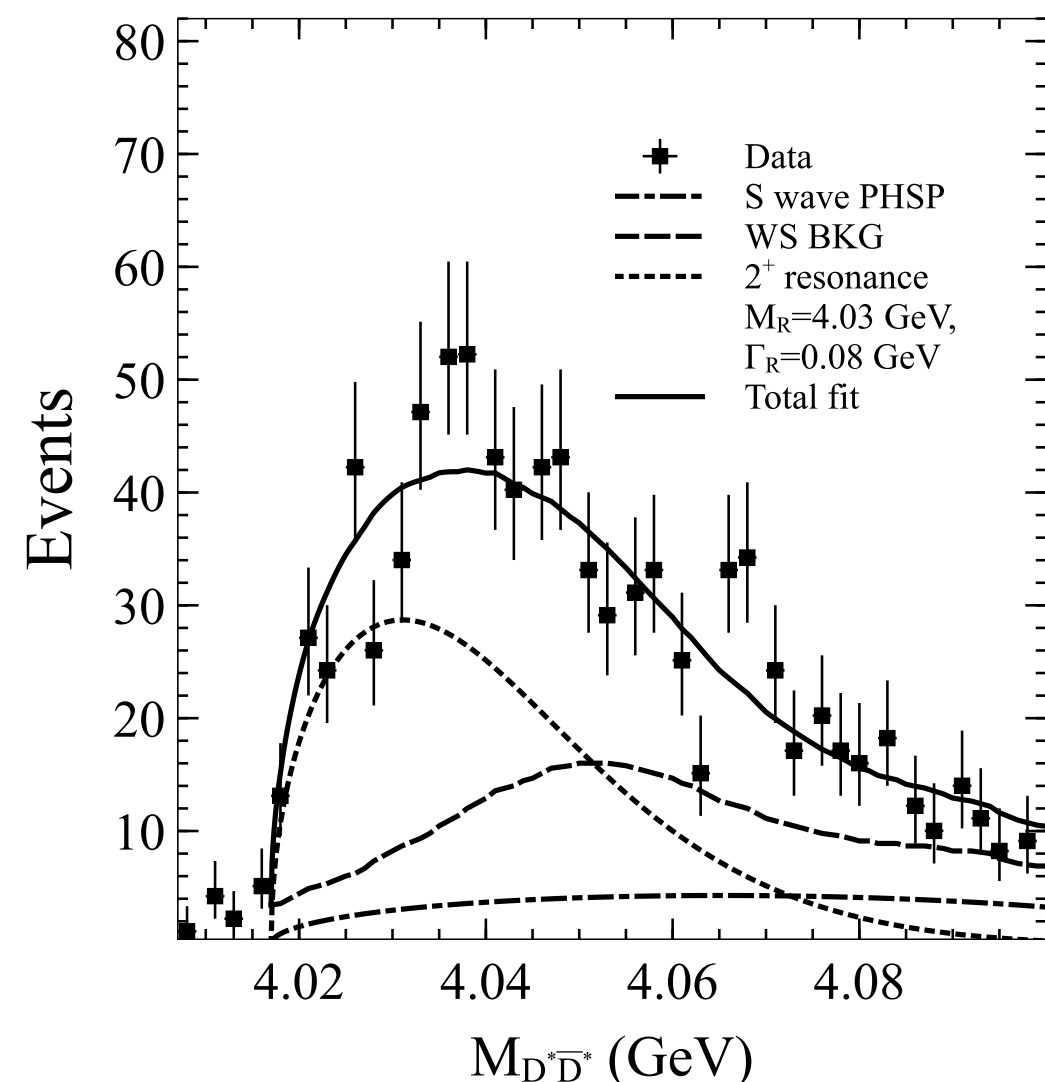
RESULTS

Alternative



2^+ bound state produced in D -wave
($M=3990$ MeV, $\Gamma=160$ MeV)

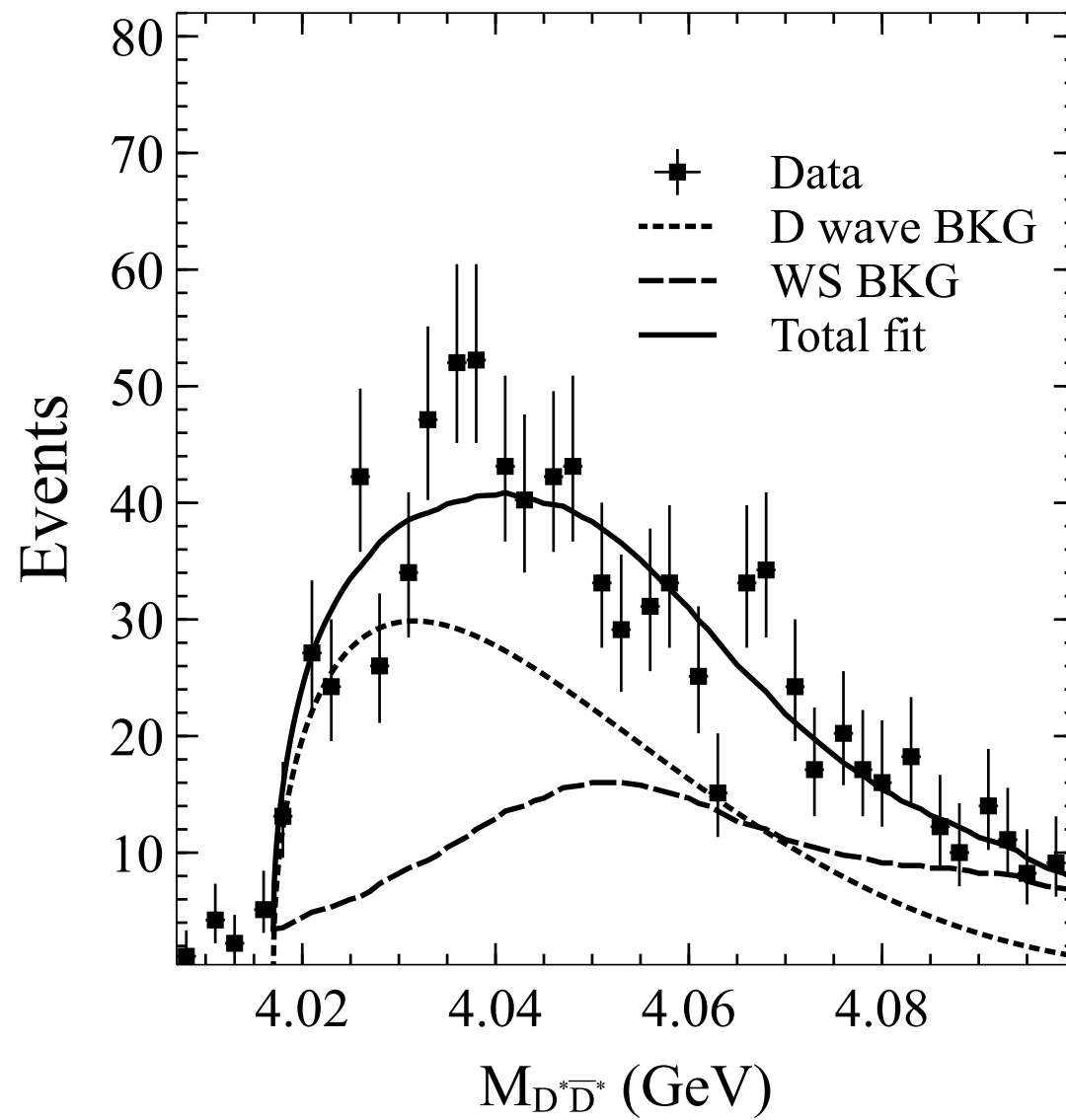
Alternative



2^+ resonance produced in D -wave
($M=4030$ MeV, $\Gamma=80$ MeV)


RESULTS

Alternative

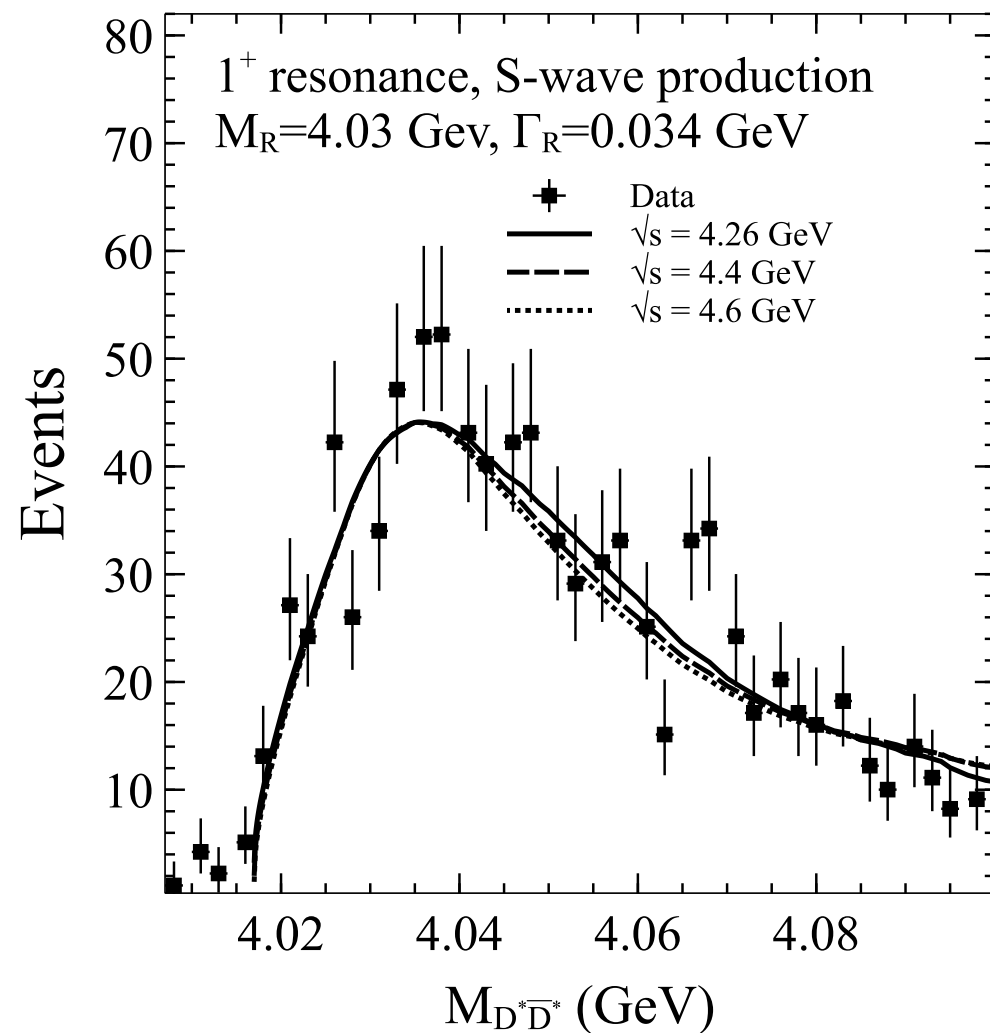


D-wave background

RESULTS

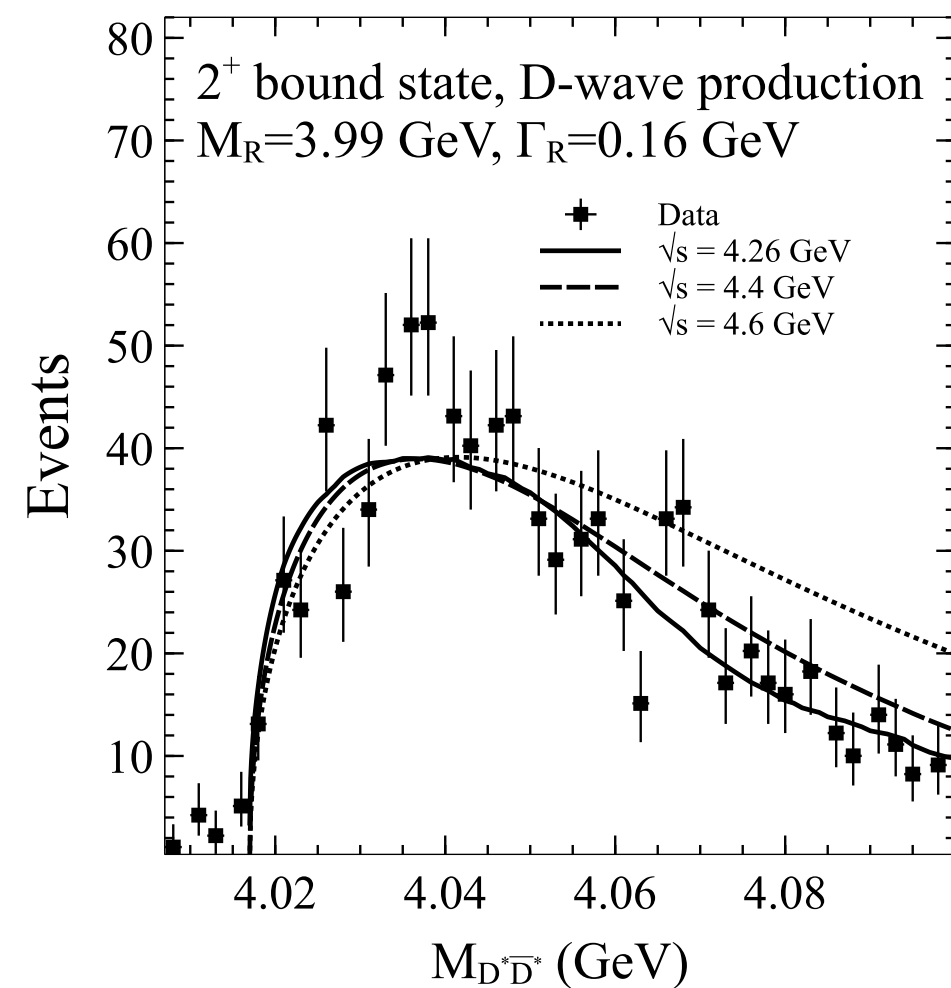
- Is there a way to know which of the different options is responsible for the signal found?  Change CM energy

As BESIII



1⁺ resonance produced in S-wave
($M=4030$ MeV, $\Gamma=34$ MeV)

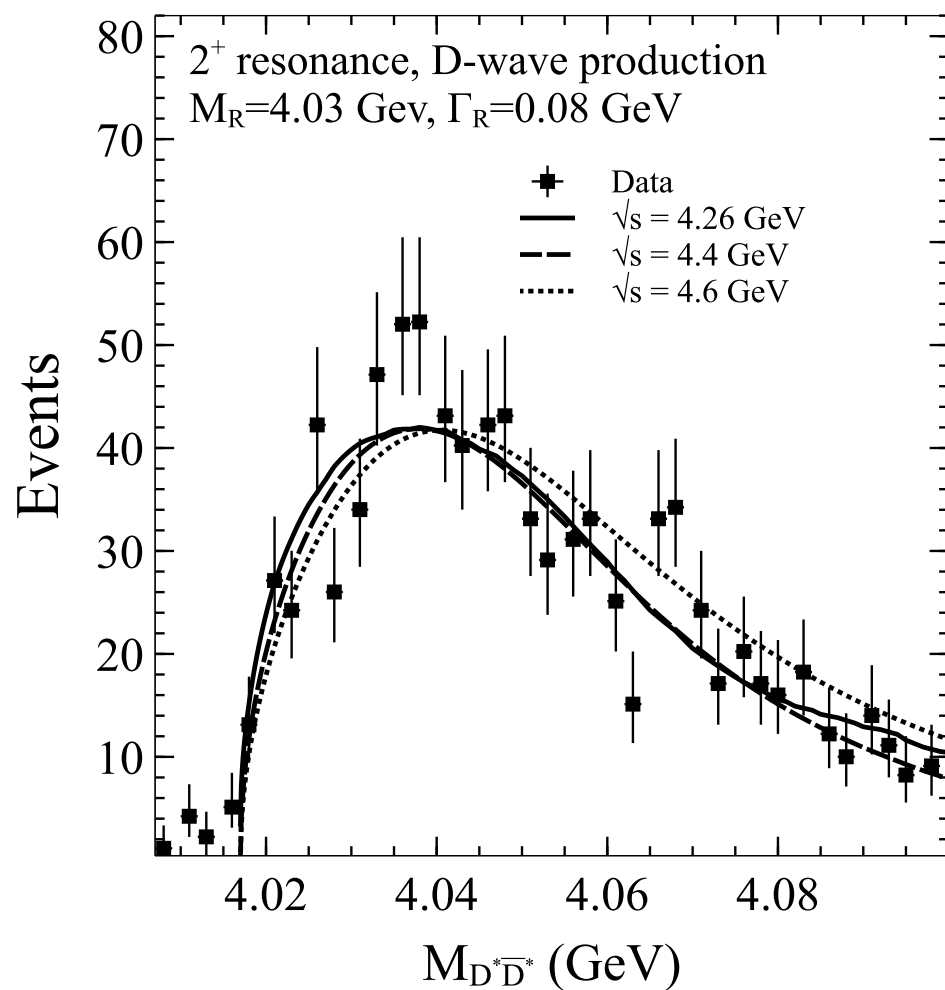
Alternative



2⁺ bound state produced in D-wave
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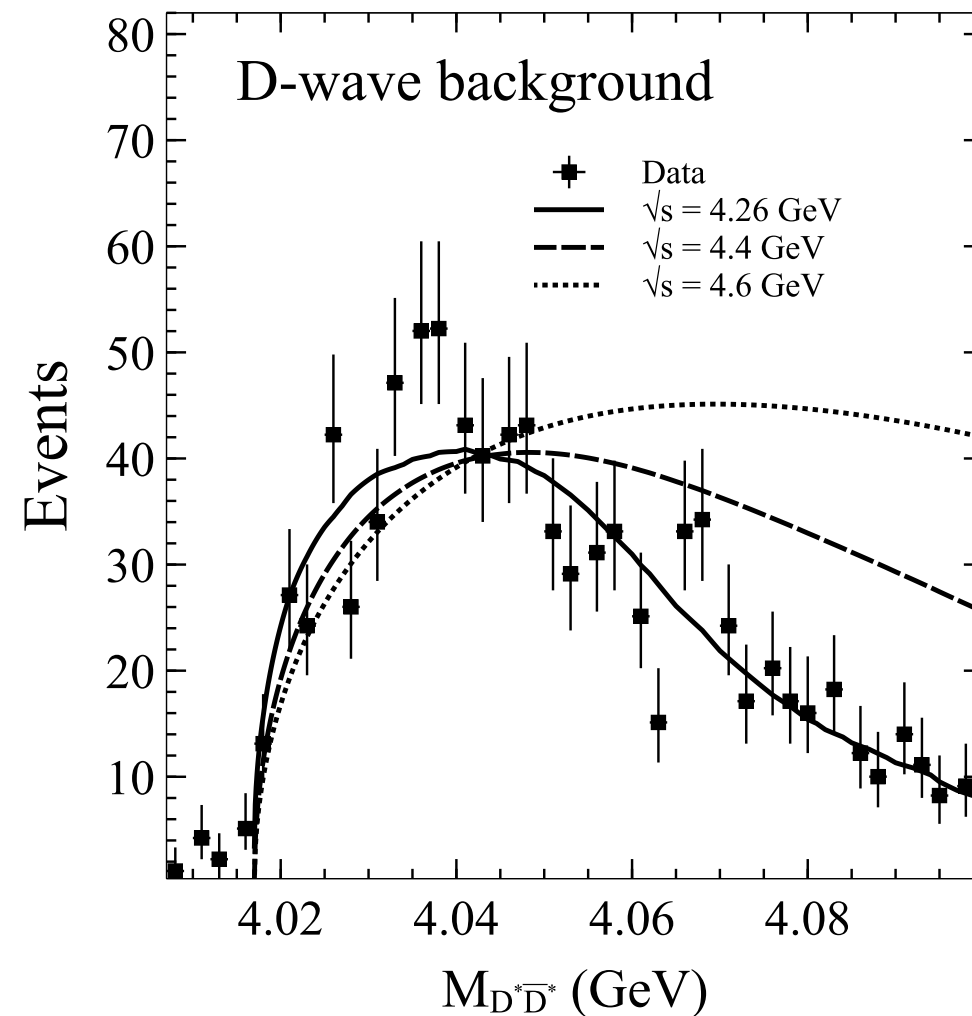
RESULTS

Alternative



2⁺ resonance produced in *D*-wave
($M=4030$ MeV, $\Gamma=80$ MeV)

Alternative



D-wave background

CONCLUSIONS

- We have obtained the $D^* \bar{D}^*$ invariant mass distribution associated to the $e^+e^- \rightarrow (D^* \bar{D}^*)^\pm \pi^\mp$ reaction.
- We have found that the signal related to a the $Z_c(4025)$ can also correspond to a 2^+ bound state, a 2^+ resonance or just to a D -wave background.
- All of them are equally plausible.
- Studying the dependence of the invariant mass distribution with the CM energy it could be possible to distinguish between a resonance (1^+ or 2^+) and a 2^+ bound state.