

# Neutrino Mass Hierarchy from Supernova Neutrinos



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MPI for Physics, Munich

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# Outline

**Supernova (SN) as Neutrino Source**

**Oscillation of SN Neutrinos**

**Signatures of Neutrino Mass Hierarchy**

**Conclusions**

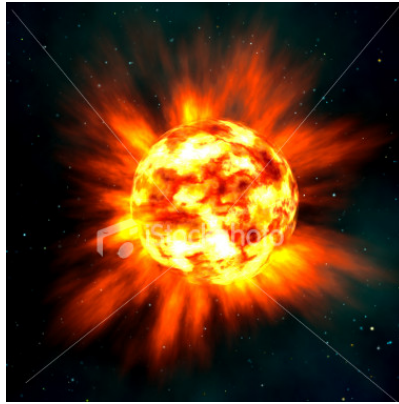
# Outline

**Supernova (SN) as Neutrino Source**

**Oscillation of SN Neutrinos**

**Signatures of Neutrino Mass Hierarchy**

**Conclusions**



Supernova one of the most energetic events in nature.

Terminal phase of a massive star ( $M > 8 \sim 10 M_{\odot}$ )

Collapses and ejects the outer mantle in a shock wave driven explosion.

**ENERGY SCALES:**  $\sim 10^{53}$  erg : 99% energy is emitted by Neutrinos (Energy  $\sim 10$  MeV).

**TIME SCALE:** The duration of the burst lasts  $\sim 10$  s.

# Neutrino Emission Phases

## Neutronization burst

- Shock breakout
- De-leptonization of outer core layers
- **Duration ~ 25 ms**

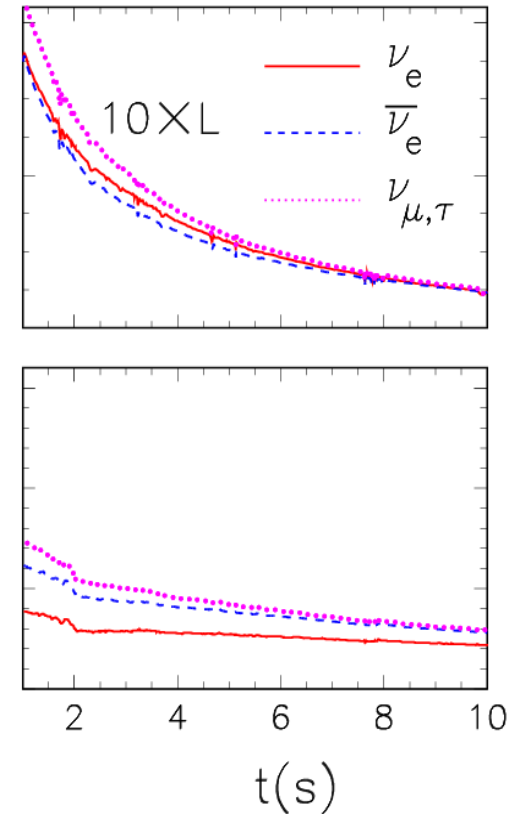
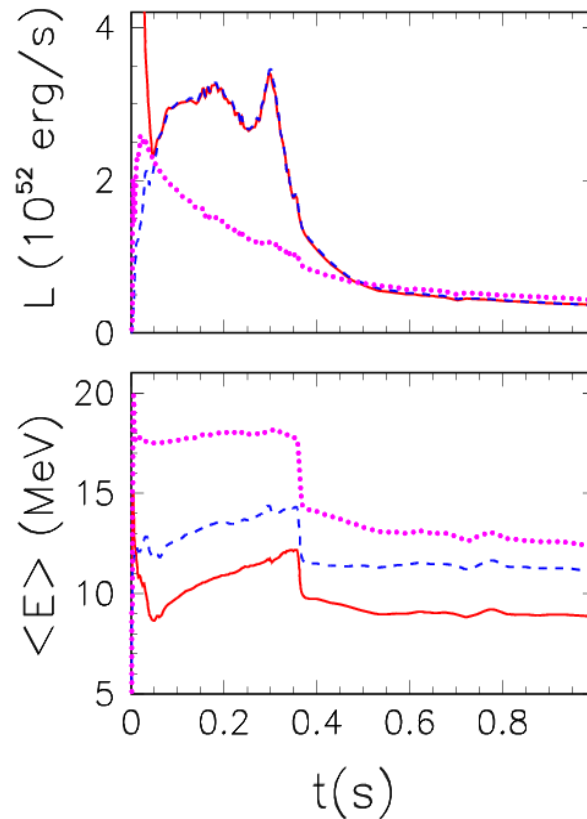
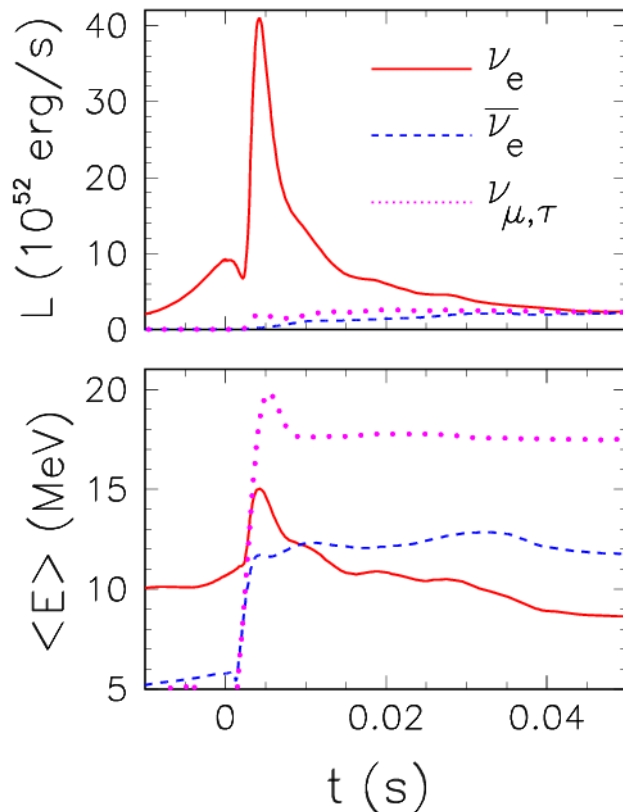
## Accretion

- powered by infalling matter
- Stalled shock

**Accretion: ~ 0.5 s ; Cooling: ~ 10 s**

## Cooling

- Cooling by  $\nu$  diffusion



# Plan of the talk

**Supernova (SN) as Neutrino Source**

**Oscillation of SN Neutrinos**

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# SN $\nu$ Flavor Evolution

The flavor evolution in matter is described by the non-linear MSW equations:

$$i \frac{d}{dx} \psi_\nu = (H_{vac} + H_e + H_{\nu\nu}) \psi_\nu$$

In the standard 3 $\nu$  framework

- $H_{vac} = \frac{U M^2 U^\dagger}{2E}$

**Kinematical mass-mixing term**

- $H_e = \sqrt{2} G_F \text{diag}(N_e, 0, 0)$

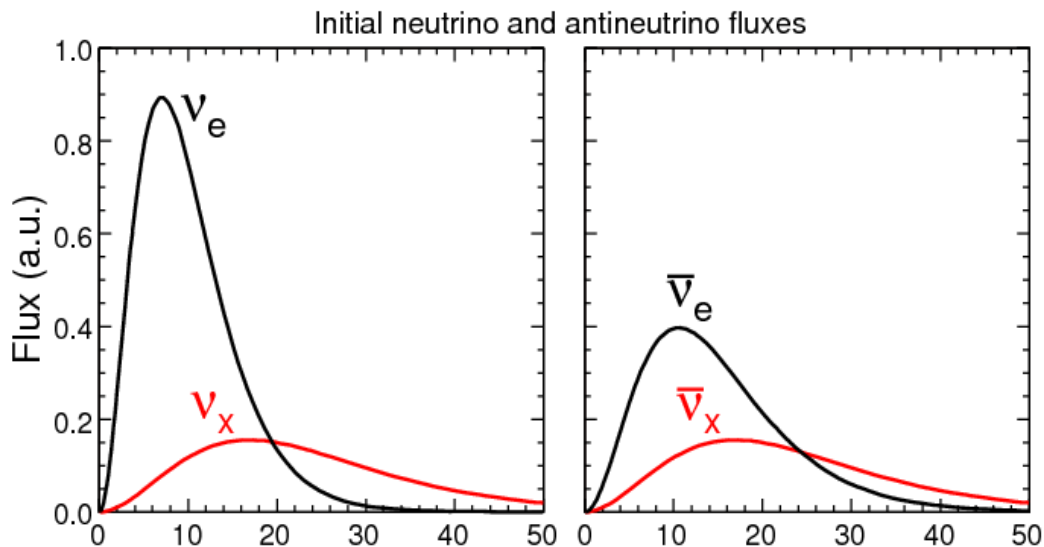
**Dynamical MSW term (in matter)**

- $H_{\nu\nu} = \sqrt{2} G_F \int (1 - \cos \theta_{pq}) (\rho_q - \bar{\rho}_q) dq$

**Neutrino-neutrino interactions term  
(non-linear)**

# Spectral Splits in the Accretion Phase

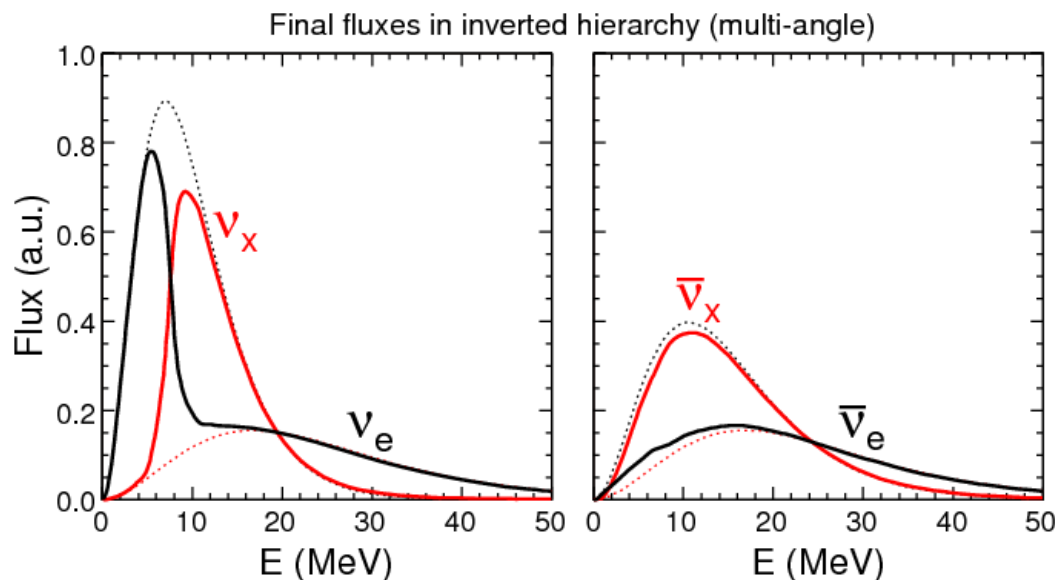
[Fogli, Lisi, Marrone, Mirizzi, arXIV: 0707.1998 [hep-ph] ]



Initial fluxes typical of  
accretion phase at  
neutrinosphere ( $r \sim 10$  km)

$$F_{\nu_e} : F_{\bar{\nu}_e} : F_{\nu_x} = 2.4 : 1.6 : 1.0$$

**Inverted mass  
hierarchy (IH)**



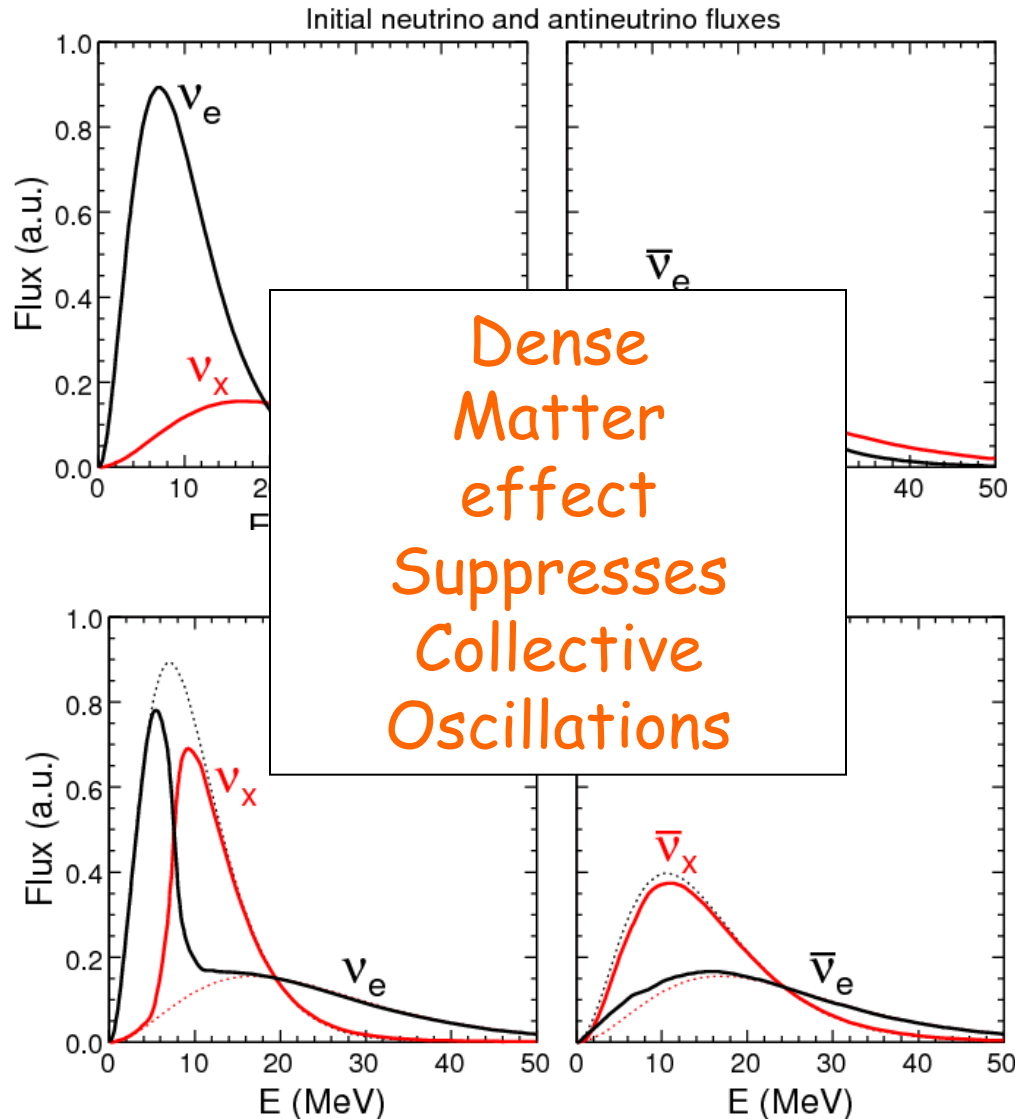
Fluxes at the end of collective  
effects ( $r \sim 200$  km)

**Nothing happens in  
Normal Hierarchy (NH)**



# Suppression of Collective effects

Dense matter ( $n_e$ ) dominates over nu-nu interaction ( $n_\nu$ ).



[ S.C., Fischer, Mirizzi,  
Saviano & Tomas  
PRL 107:151101, 2011  
PRD 84:025002, 2011

Sarikas, Raffelt, Hüdepohl &  
Janka  
PRL 108:061101, 2012

Dasgupta, P. O'Connor, Ott  
PRD 85:065008, 2012]

# Suppression of Collective effects

Predictions are robust when collective effects are suppressed, i.e.:

## 1) Neutronization burst ( $t < 20$ ms)

large  $\nu_e$  excess and  $\nu_x$  deficit

[Hannestad et al., [astro-ph/0608695](#)]

## 2) Accretion phase ( $t < 500$ ms)

Dense matter term dominates over  $\nu$ - $\nu$  interaction term.

[[S.C](#), Fischer, Mirizzi, Saviano & Tomas

PRL 107:151101, 2011  
PRD 84:025002, 2011]

# SN neutrino Flux at Earth

## Neutronization burst & Accretion Phase:

Normal Hierarchy (NH):

$$F_{\nu_e} = F_{\nu_x}^0$$

$$F_{\bar{\nu}_e} = \cos^2 \vartheta_{12} (F_{\bar{\nu}_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

Inverted Hierarchy (IH):

$$F_{\nu_e} = \sin^2 \vartheta_{12} (F_{\nu_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

$$F_{\bar{\nu}_e} = F_{\nu_x}^0$$

-

# Plan of the talk

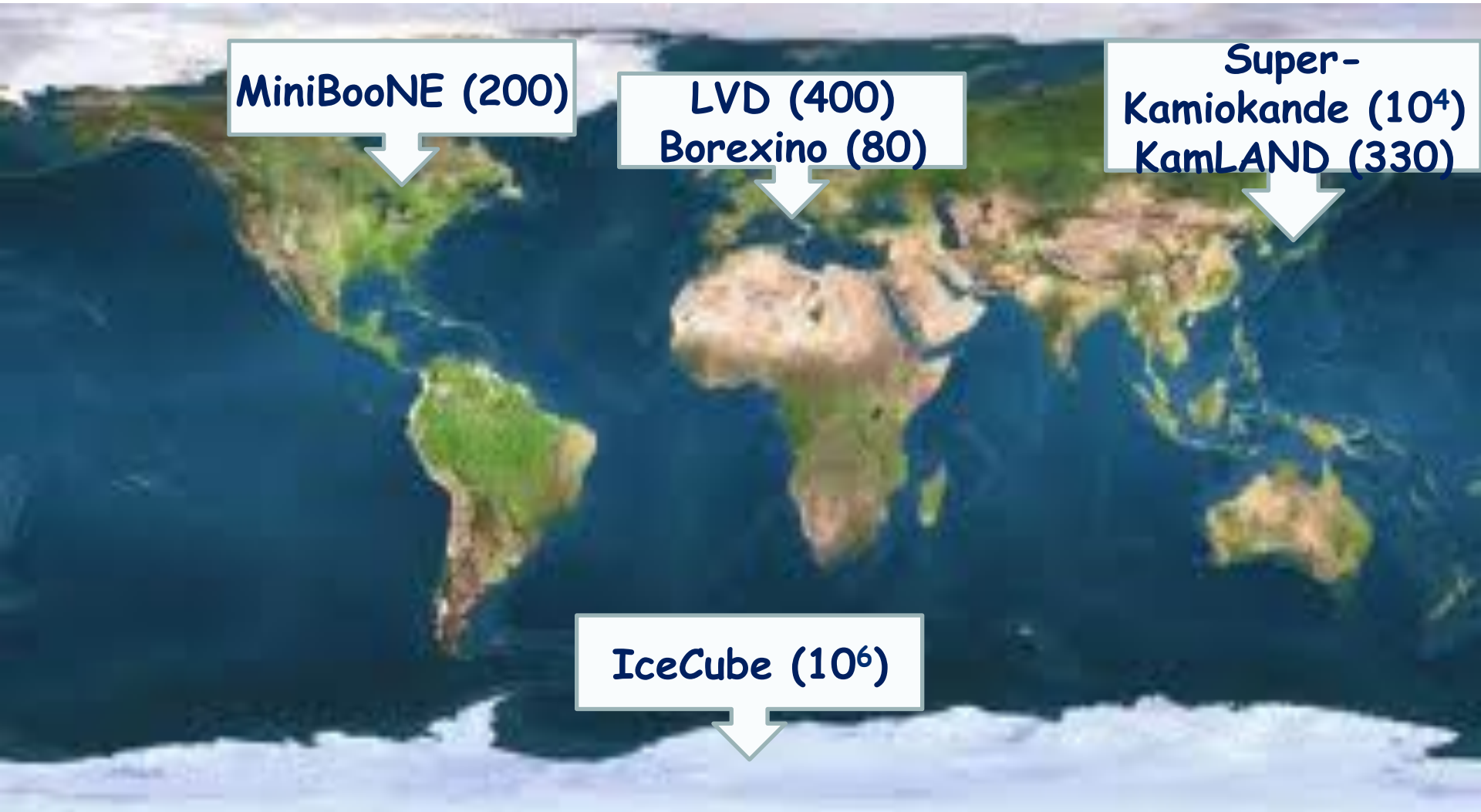
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# Large Detectors for Supernova Neutrinos

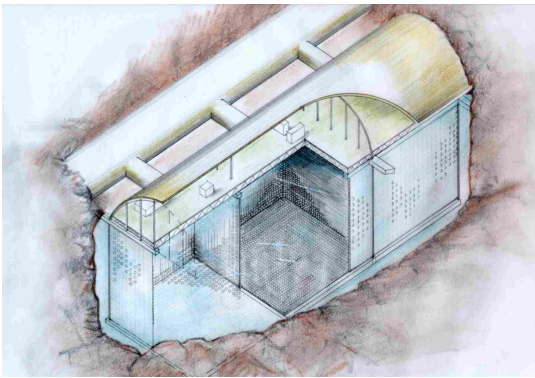


In brackets events for a "fiducial SN" at distance 10 kpc

# Next generation Detectors for Supernova Neutrinos

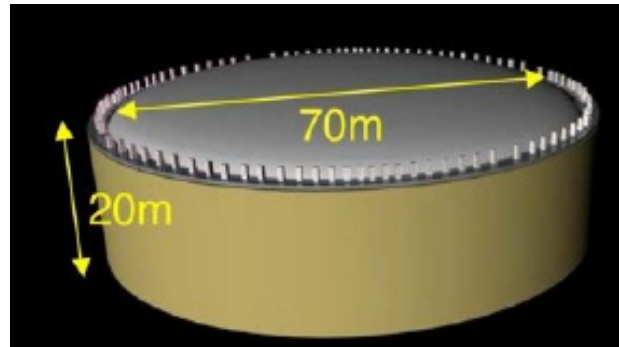
Next-generation large volume detectors might open a new era in SN neutrino detection:

Mton Cherenkov



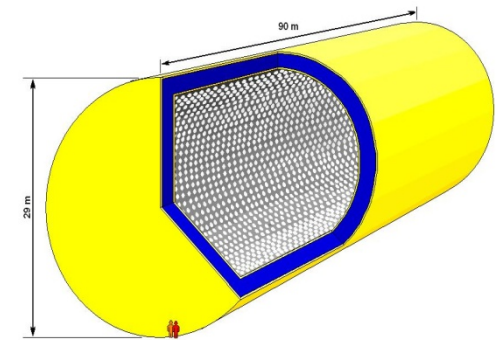
UNO, MEMPHYS,  
HYPER-K

LAr TPC



GLACIER

Scintillator

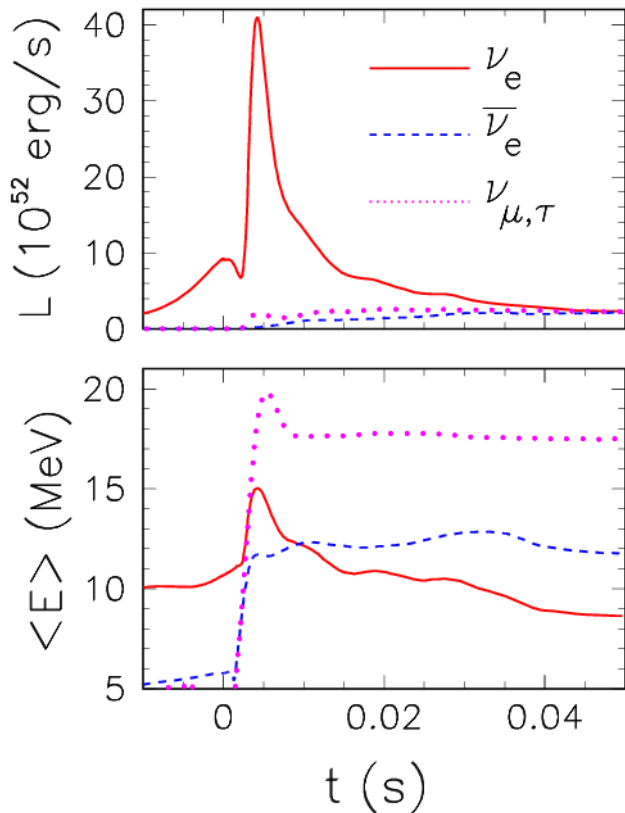


LENA

# Neutrino Emission Phases

## Neutronization burst

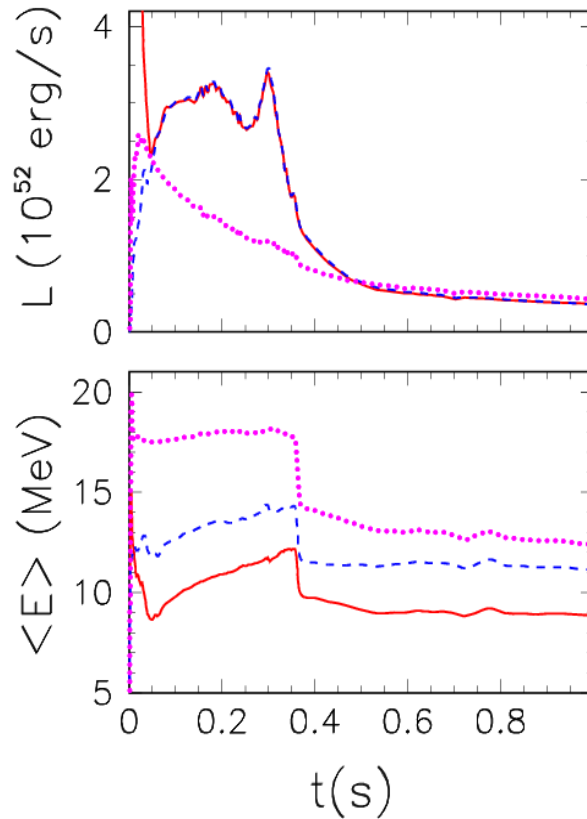
- Shock breakout
- De-leptonization of outer core layers
- **Duration ~ 25 ms**



## Accretion

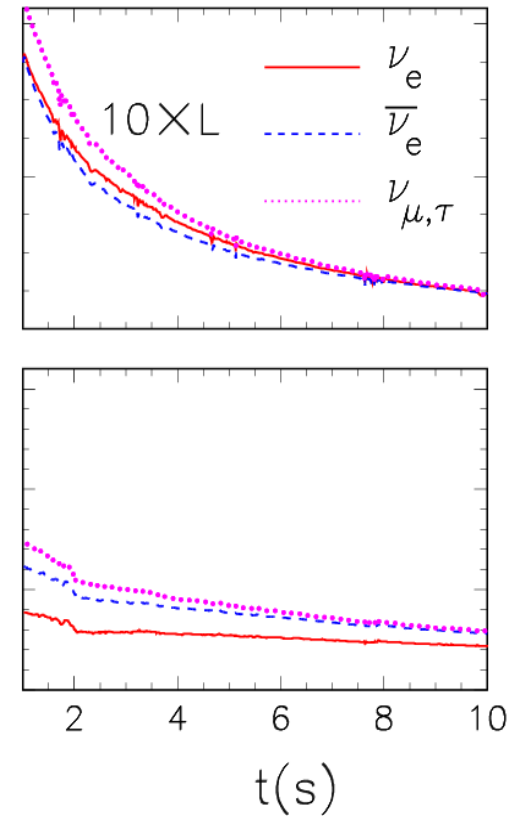
- powered by infalling matter
- Stalled shock

**Accretion: ~ 0.5 s ; Cooling: ~ 10 s**



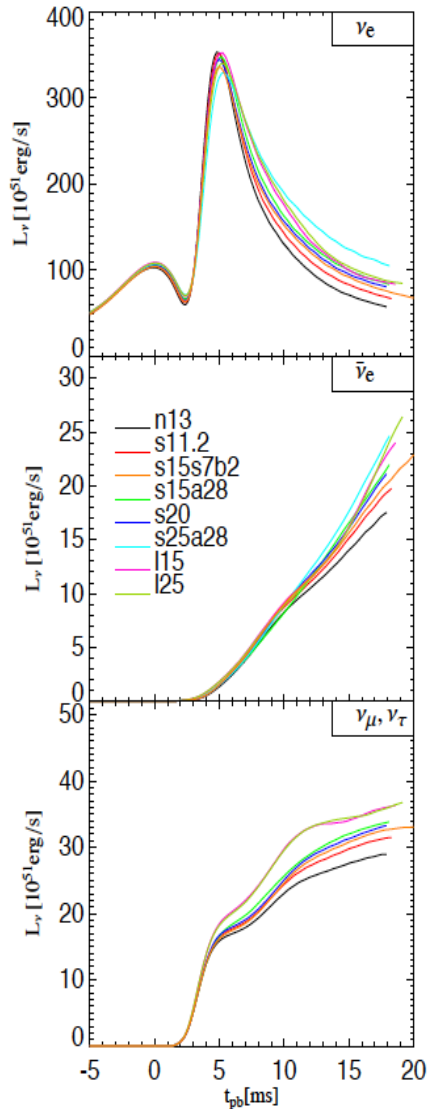
## Cooling

- Cooling by  $\nu$  diffusion

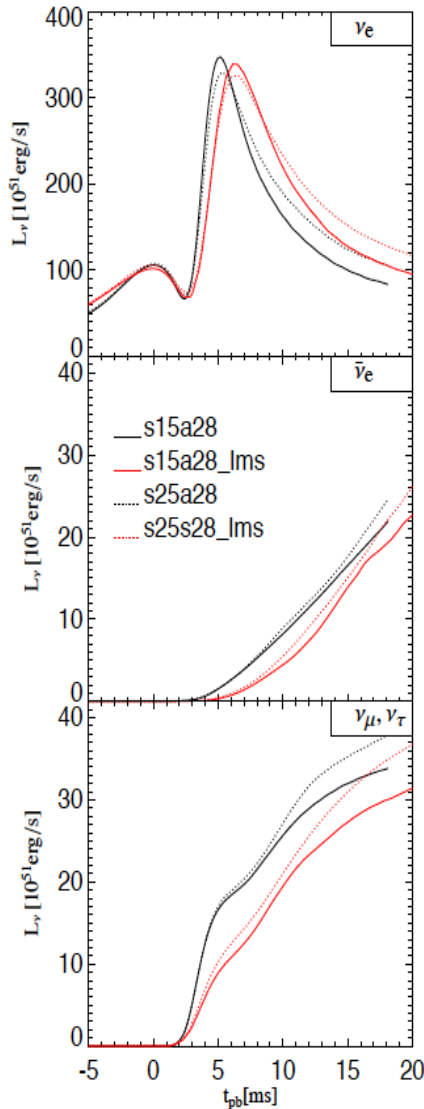


# Neutronization Burst : Model Independence

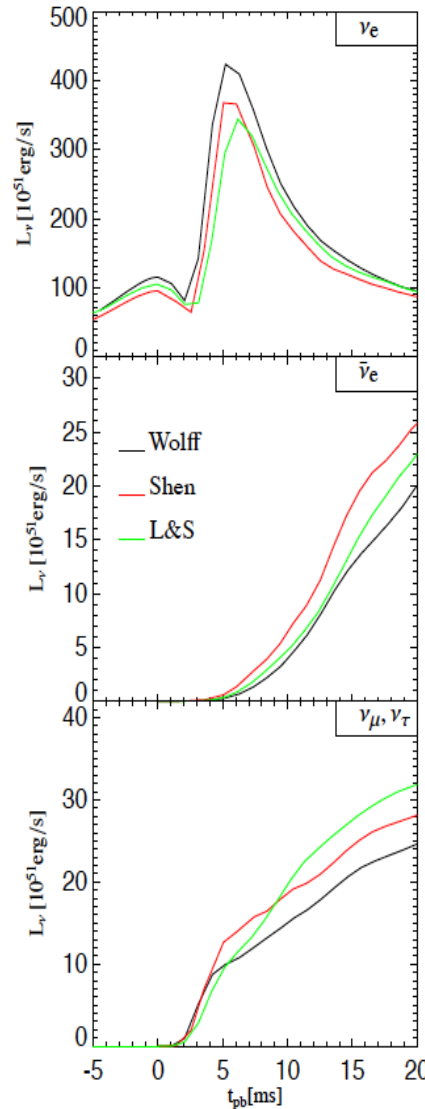
Different  
mass



Neutrino  
Transport



Nuclear  
EoS



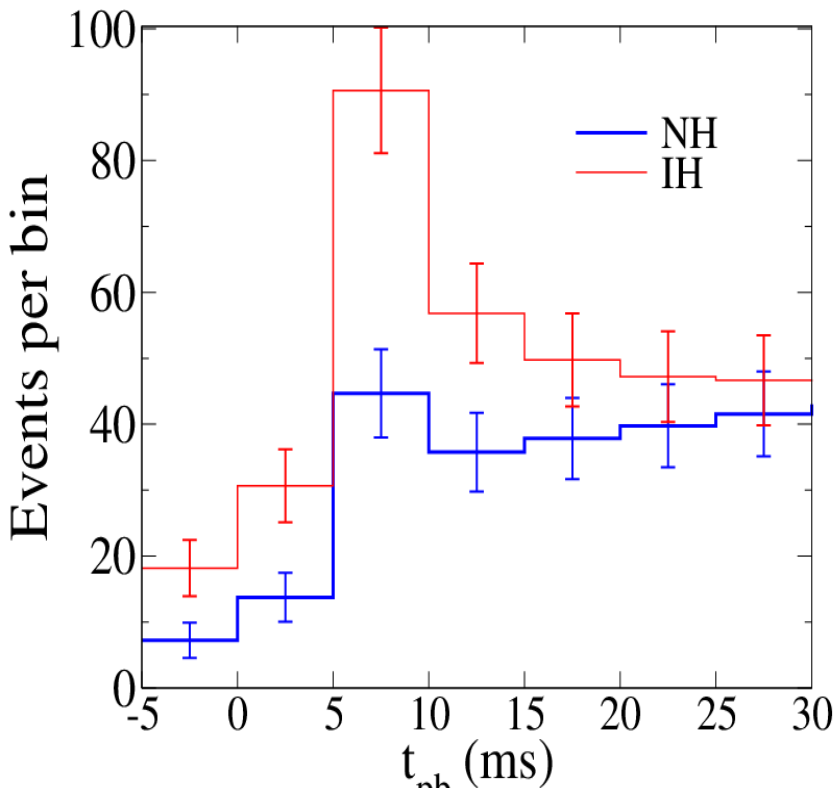
'Standard  
Candle'  
for  
SN Neutrino

[M.Kachelriess et al,  
hep-ph/0412082]



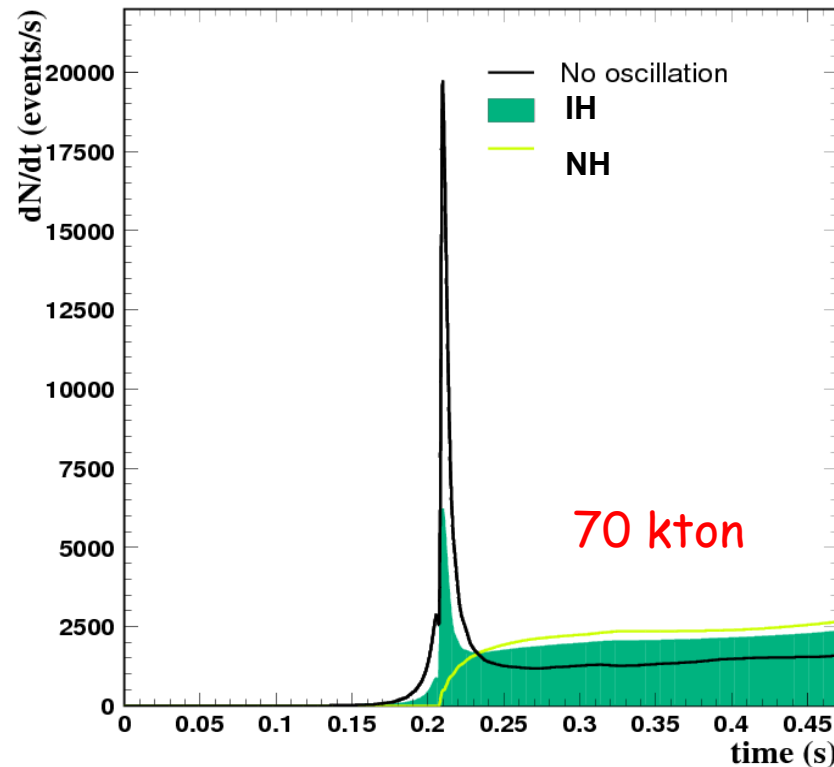
# Oscillations in the Neutronization Burst

Water Cherenkov ( $\nu_{e,x} e^- \longrightarrow \nu_{e,x} e^-$ )



[M.Kachelriess et al, hep-ph/0412082]

Liq Ar TPC  $\nu_e {}^{40}\text{Ar CC}$

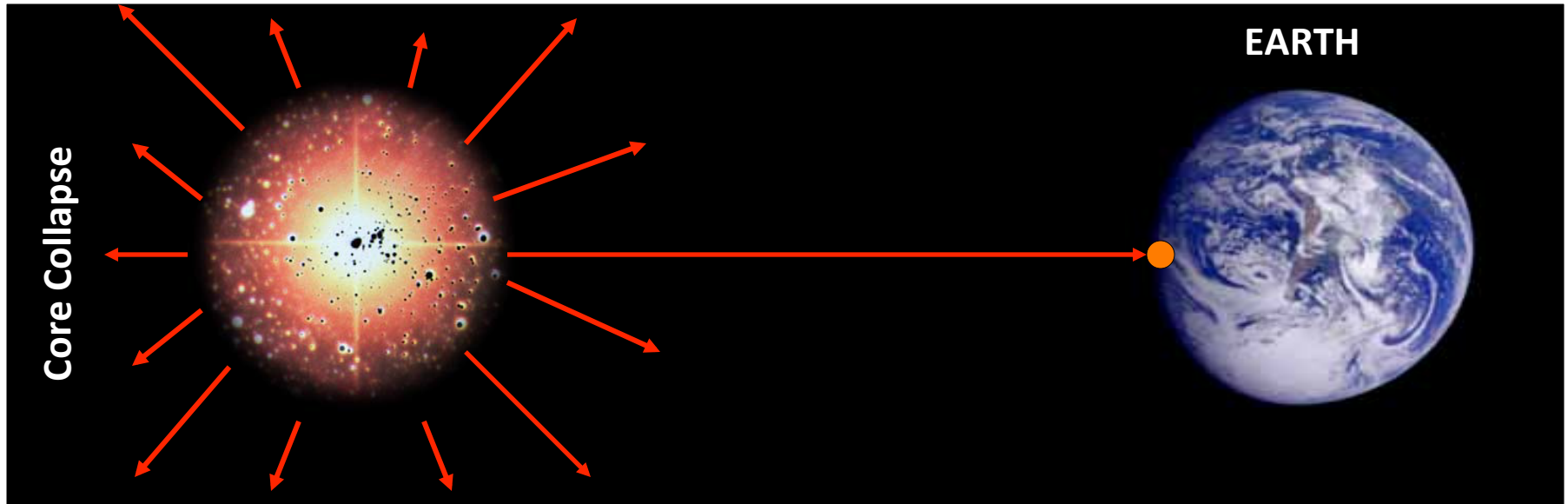


[I.Gil-Botella & A.Rubbia, hep-ph/0307244]

- Peak is absent  $\longrightarrow$  NH ( $F_{\nu_e} = F_{\nu_x}^0$ )
- Peak is seen  $\longrightarrow$  IH ( $F_{\nu_e} = \sin^2 \vartheta_{12}(F_{\nu_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$ )

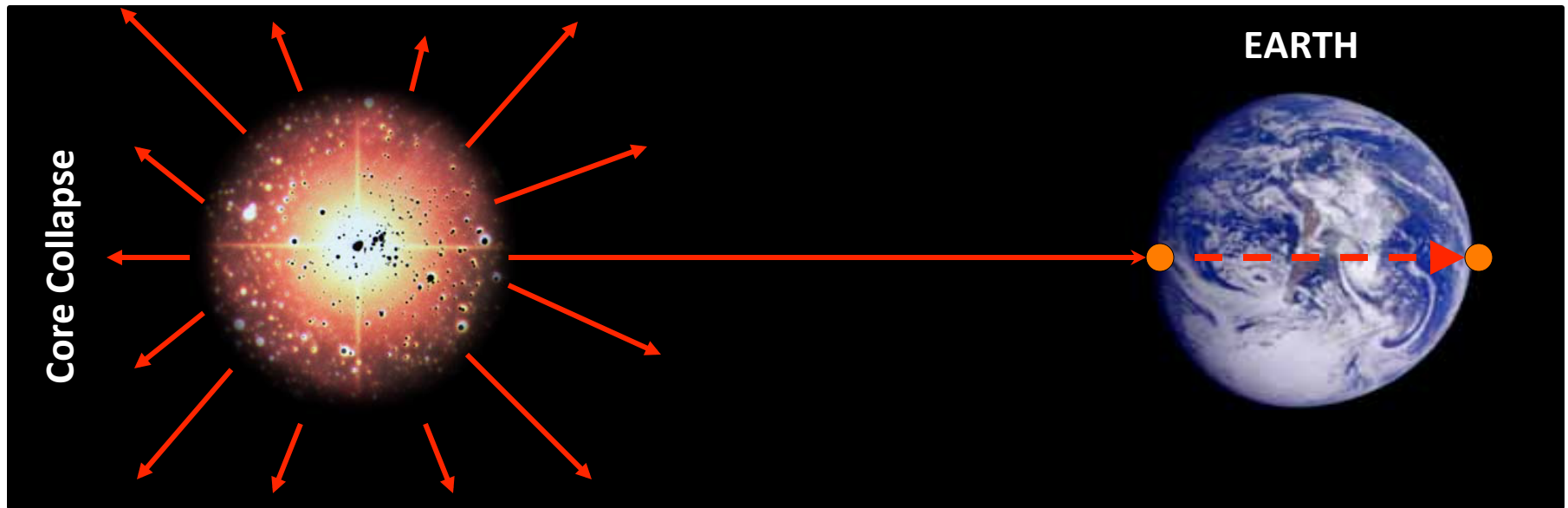
# SN neutrino Flux at Earth

Earth Matter Effect:



# SN neutrino Flux at Earth

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# SN neutrino Flux at Earth

Earth Matter Effect:

$$F_{\bar{e}}^D = \sin^2 \theta_{12} F_{\bar{x}}^0 + \cos^2 \theta_{12} F_{\bar{e}}^0 + \Delta F^0 \bar{A}_{\oplus} \sin^2(12.5 \overline{\Delta m_{\oplus}^2} L/E)$$

Normal Hierarchy (NH):

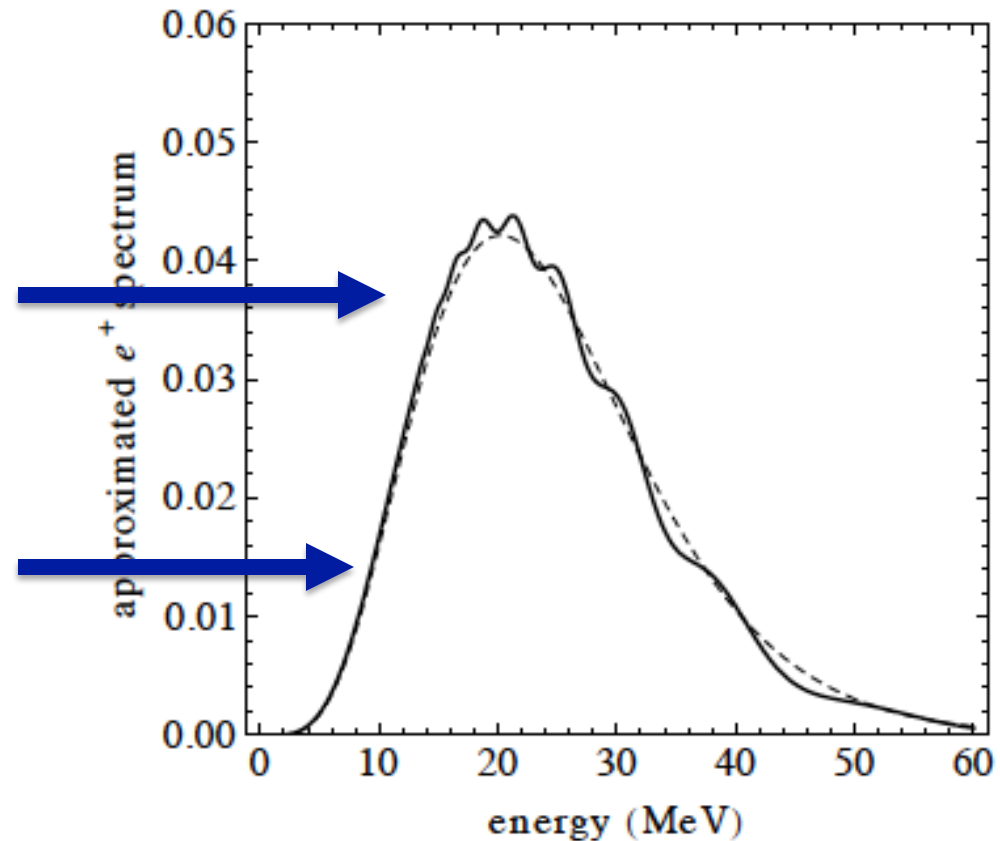
$$F_{\nu_e} = F_{\nu_x}^0 \quad (\text{No E.M.})$$

$$F_{\bar{\nu}_e} = \cos^2 \theta_{12} (F_{\bar{\nu}_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

Inverted Hierarchy (IH):

$$F_{\nu_e} = \sin^2 \theta_{12} (F_{\nu_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

$$F_{\bar{\nu}_e} = F_{\nu_x}^0 \quad (\text{No E.M.})$$



# SN neutrino Flux at Earth

Earth Matter Effect:

$$F_{\bar{e}}^D = \sin^2 \theta_{12} F_{\bar{x}}^0 + \cos^2 \theta_{12} F_{\bar{e}}^0 + \Delta F^0 \bar{A}_{\oplus} \sin^2(12.5 \overline{\Delta m_{\oplus}^2} L/E)$$

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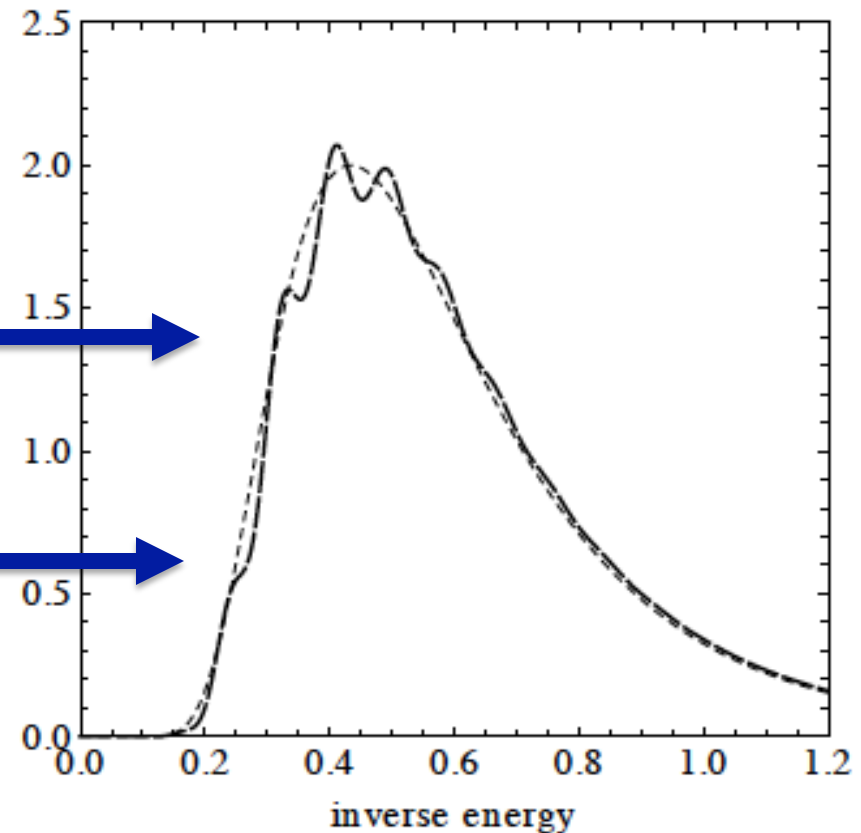
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Normal Hierarchy (NH):

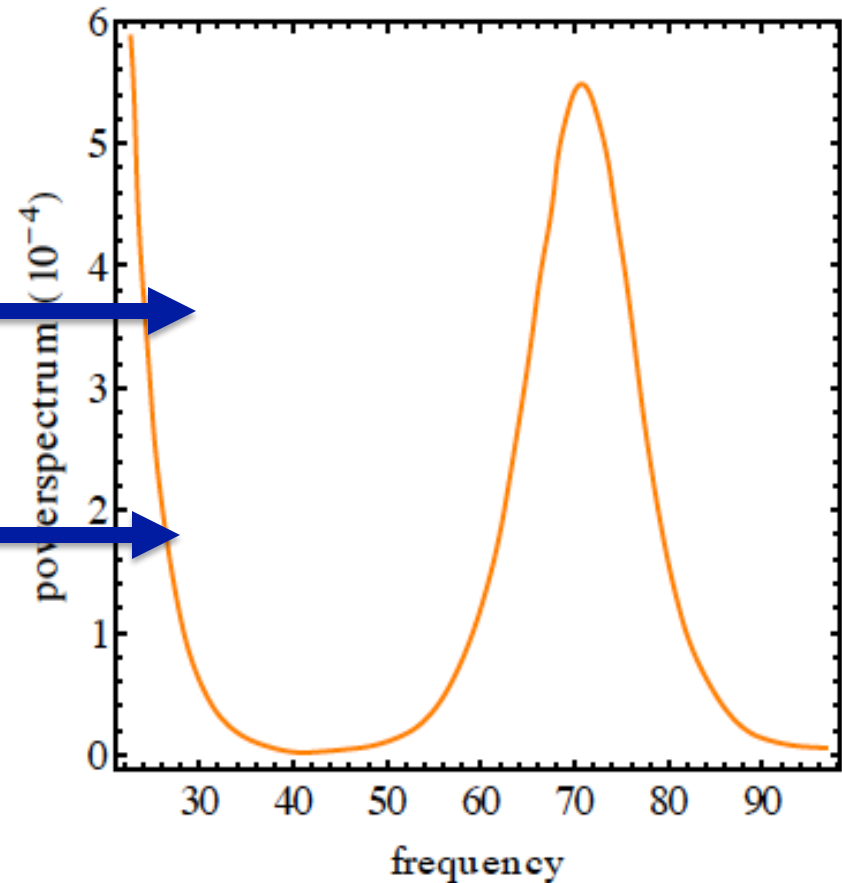
$$F_{\nu_e} = F_{\nu_x}^0 \quad (\text{No E.M.})$$

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Inverted Hierarchy (IH):

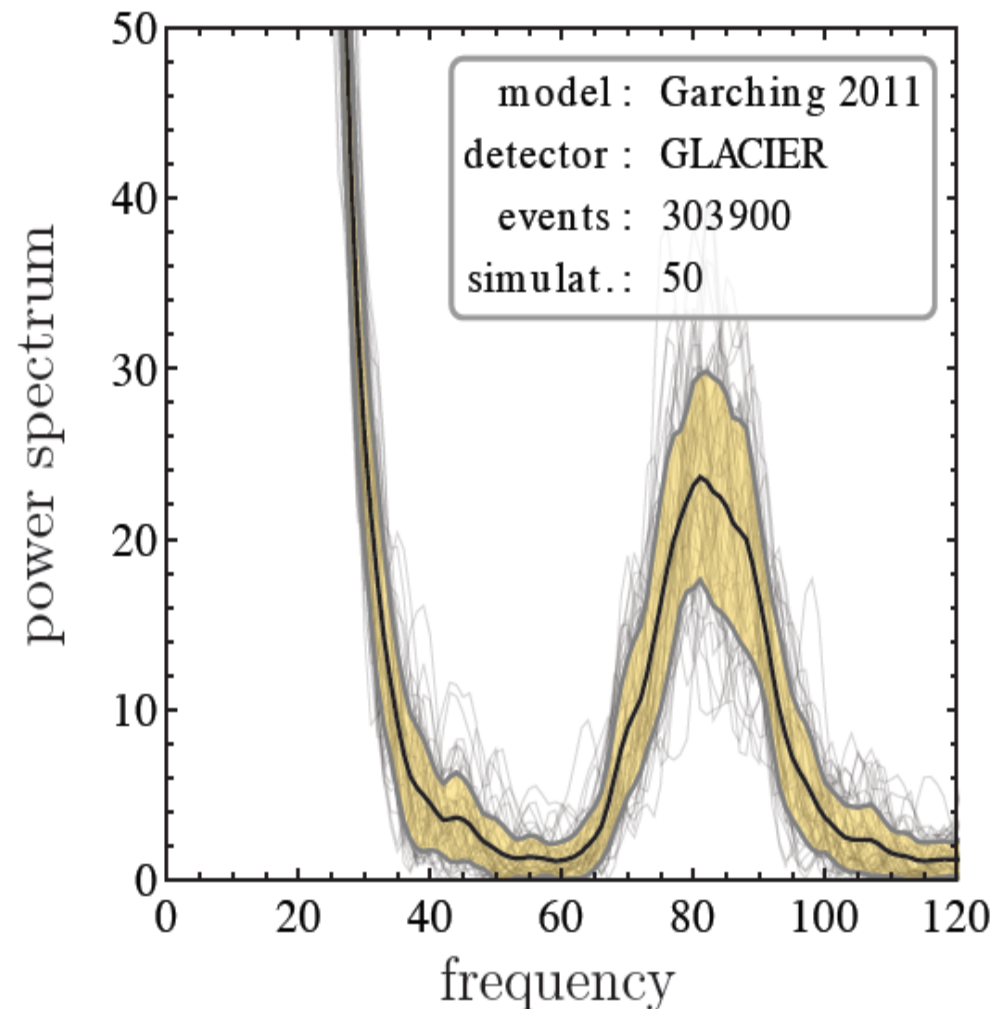
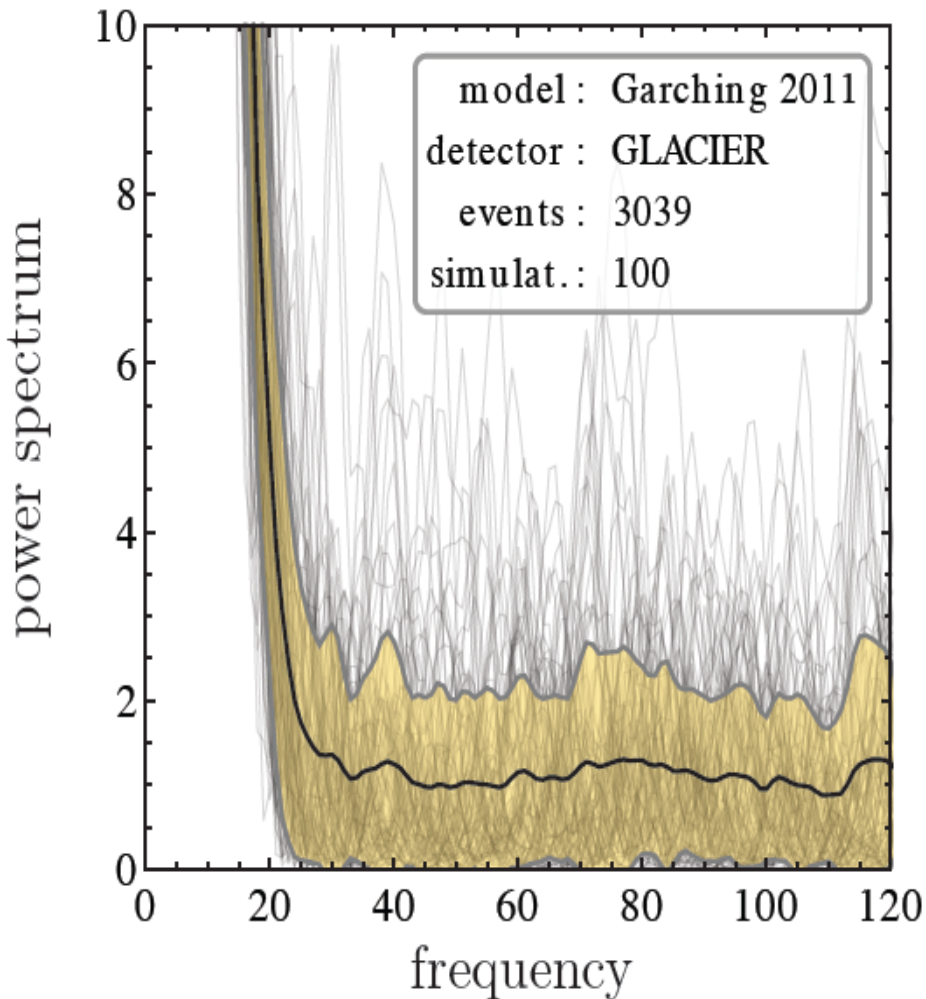
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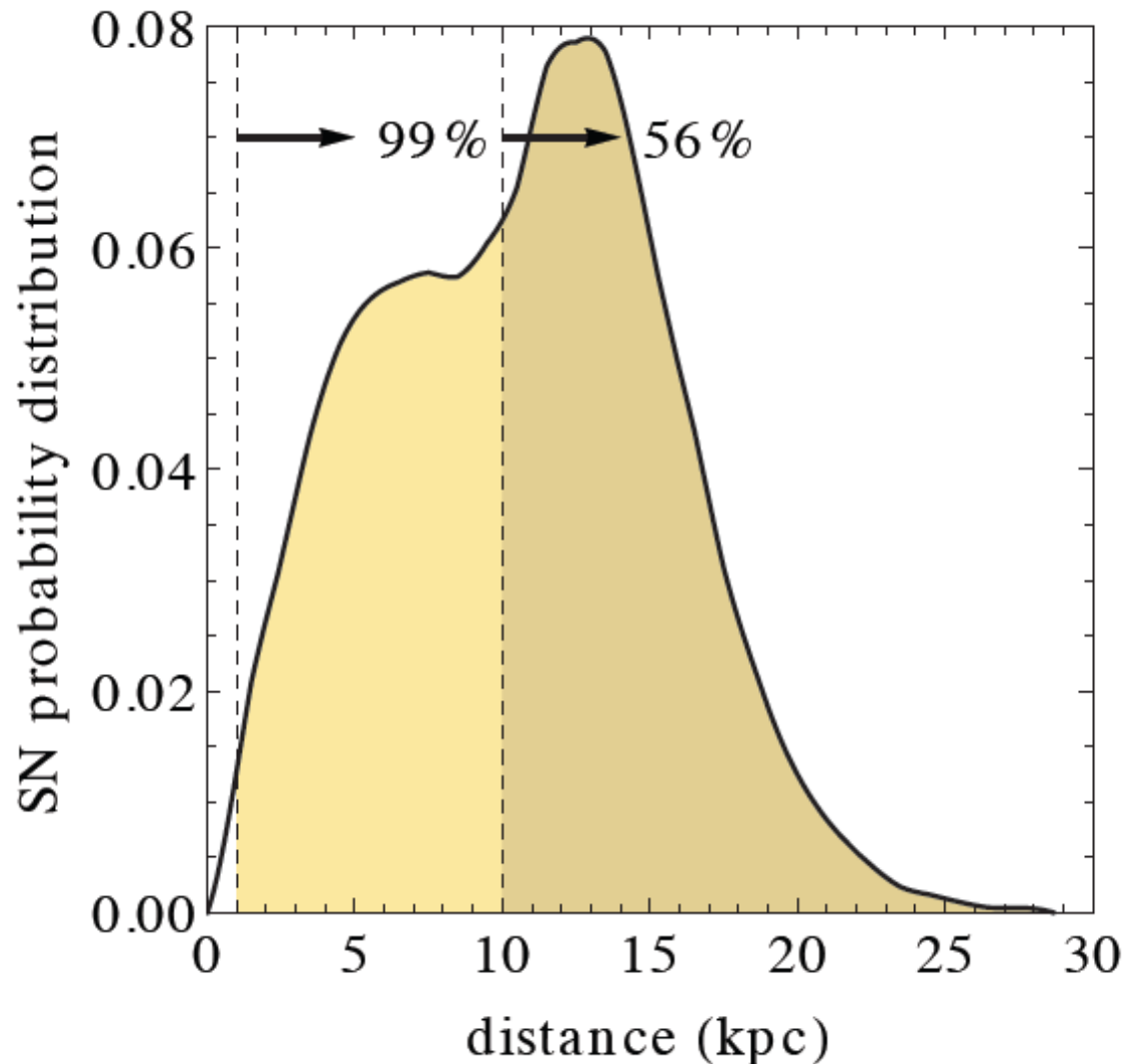
# SN neutrino Flux at Earth

Earth Matter Effect:



[ Borriello, S.C, Mirizzi, Serpico; PRD 86 (2012) ]

# Galactic SN Distribution



Possible sub-kpc candidate:

Red supergiant Betelguse

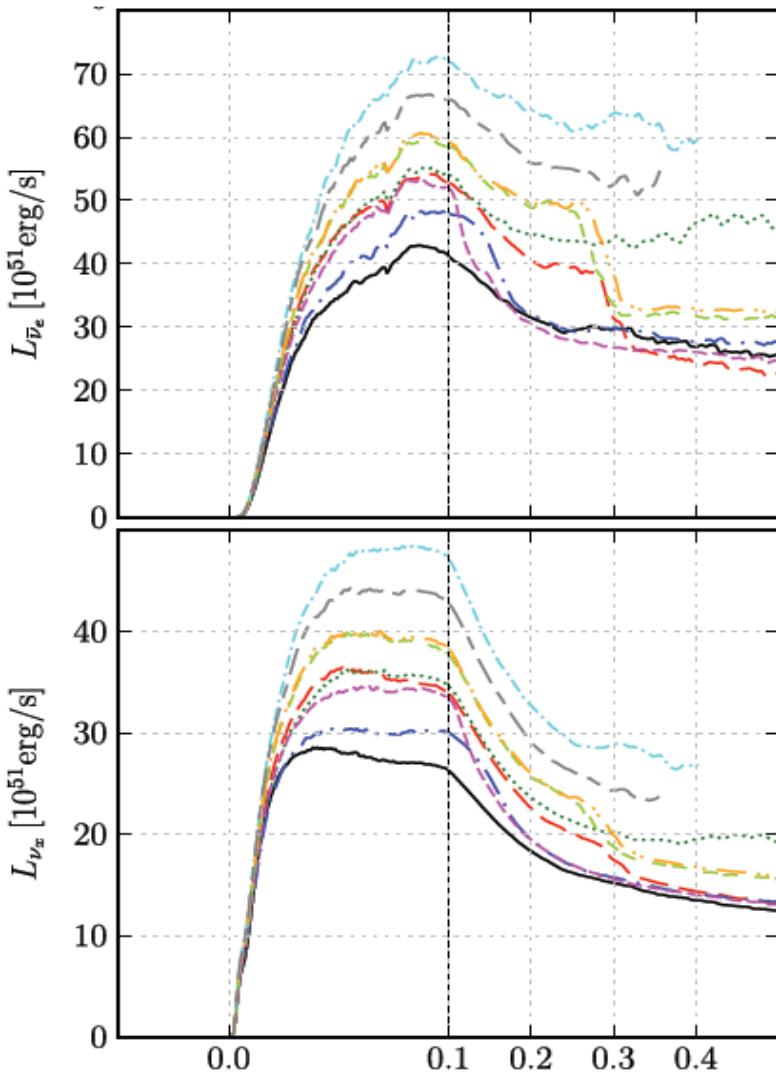
distance~ 0.2 kpc

Event count~ 10s of million

[ Mirizzi, Raffelt & Serpico; (2006) ]



# Rise time Analysis: Hierarchy Determination



*Garching group, 2011*

- High degeneracy of  $\nu_e$  and  $e$ , suppresses  $\bar{\nu}_e$  production.
- $\bar{\nu}_e$  more in equilibrium with environment than  $\nu_x$ .

Flux of  $\nu_x$  rises faster than  $\bar{\nu}_e$

$$\text{NH: } F_{\bar{\nu}_e} = \cos^2 \vartheta_{12} (F_{\bar{\nu}_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

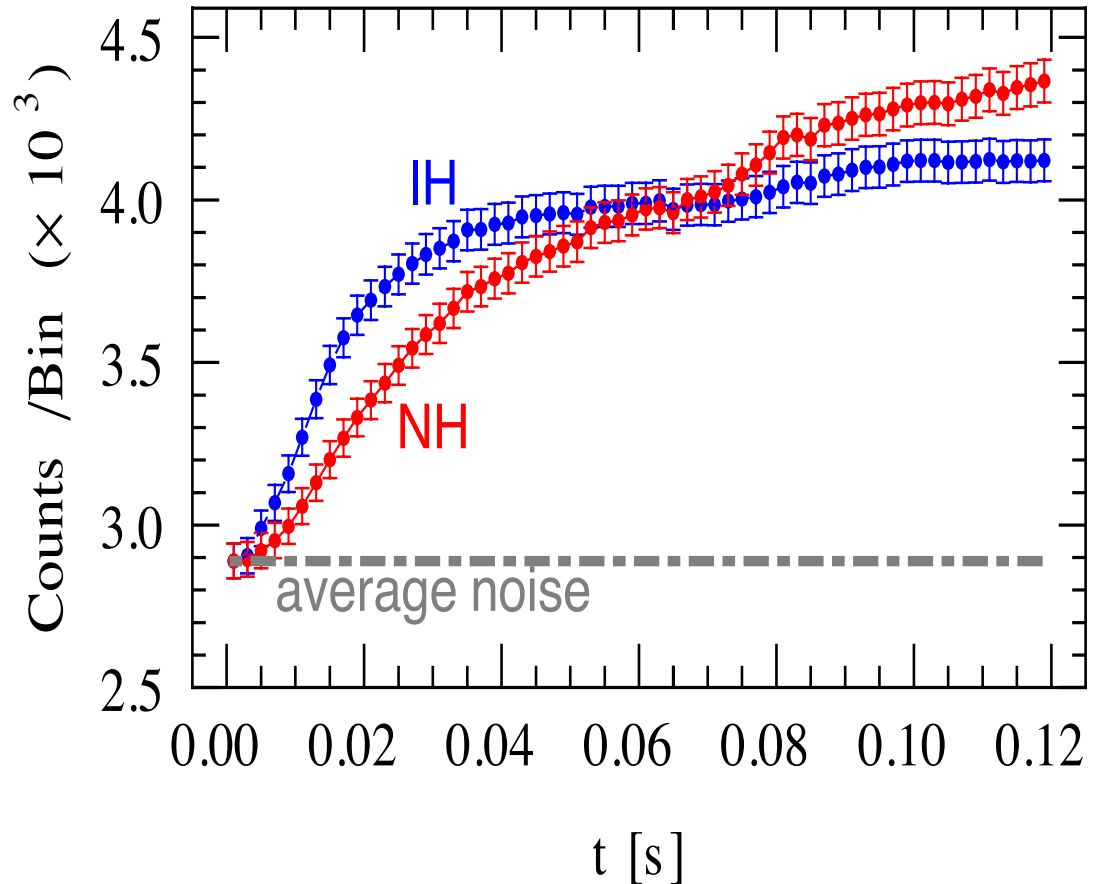
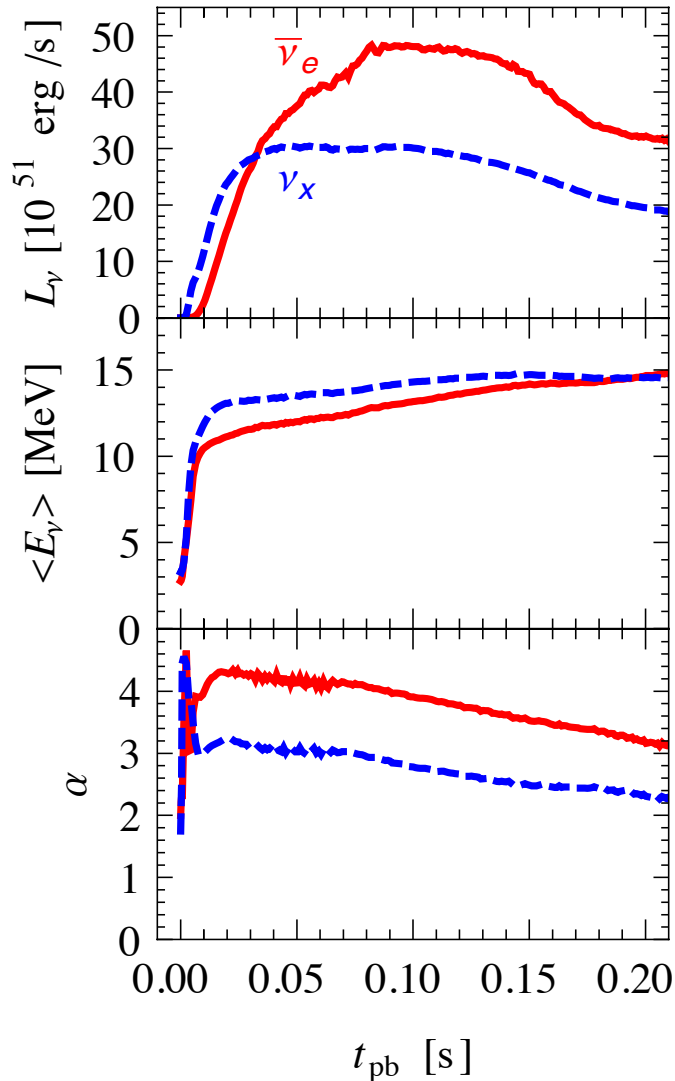
$$\text{IH: } F_{\bar{\nu}_e} = F_{\nu_x}^0$$

Flux in IH ( $\nu_x$ ) rises faster than NH ( $\nu_x, \bar{\nu}_e$ )

[Serpico, S.C, Fischer, Hüdepohl, Janka & Mirizzi  
PRD 85:085031,2012 ]

# Rise time Analysis: Hierarchy Determination

15 Solar Mass  
in Ice-Cube



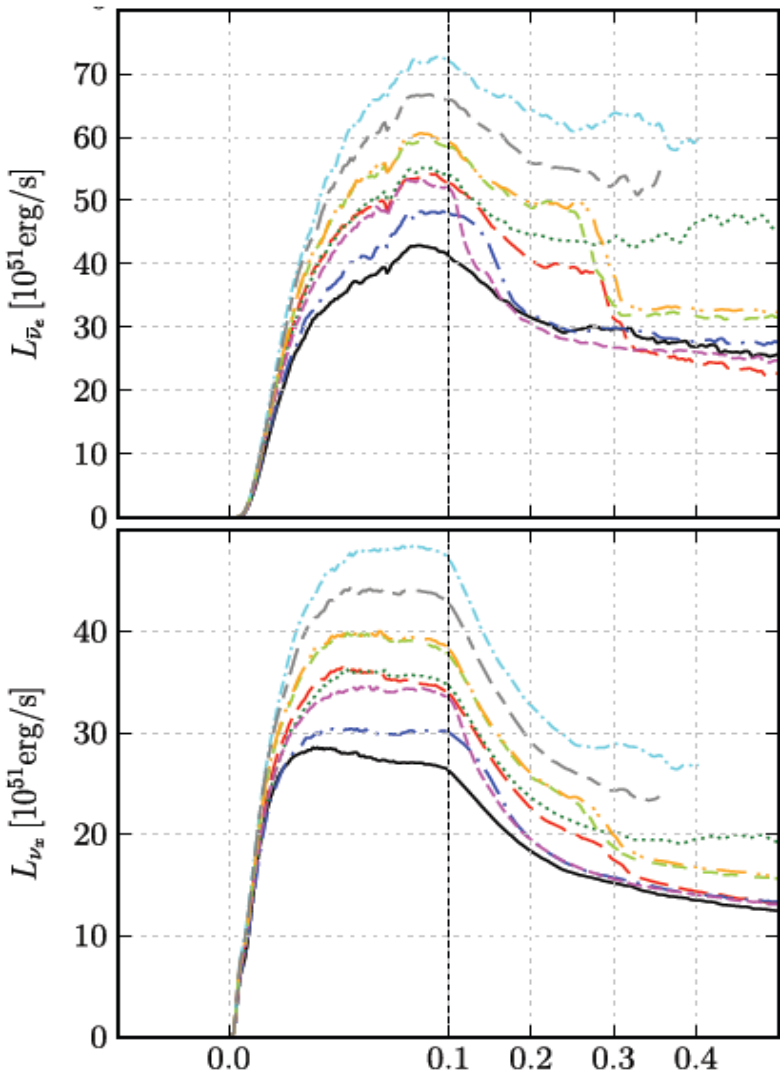
Flux in IH rises faster than NH

[Serpico, S.C, Fischer, Hüdepohl, Janka & Mirizzi  
PRD 85:085031, 2012 ]

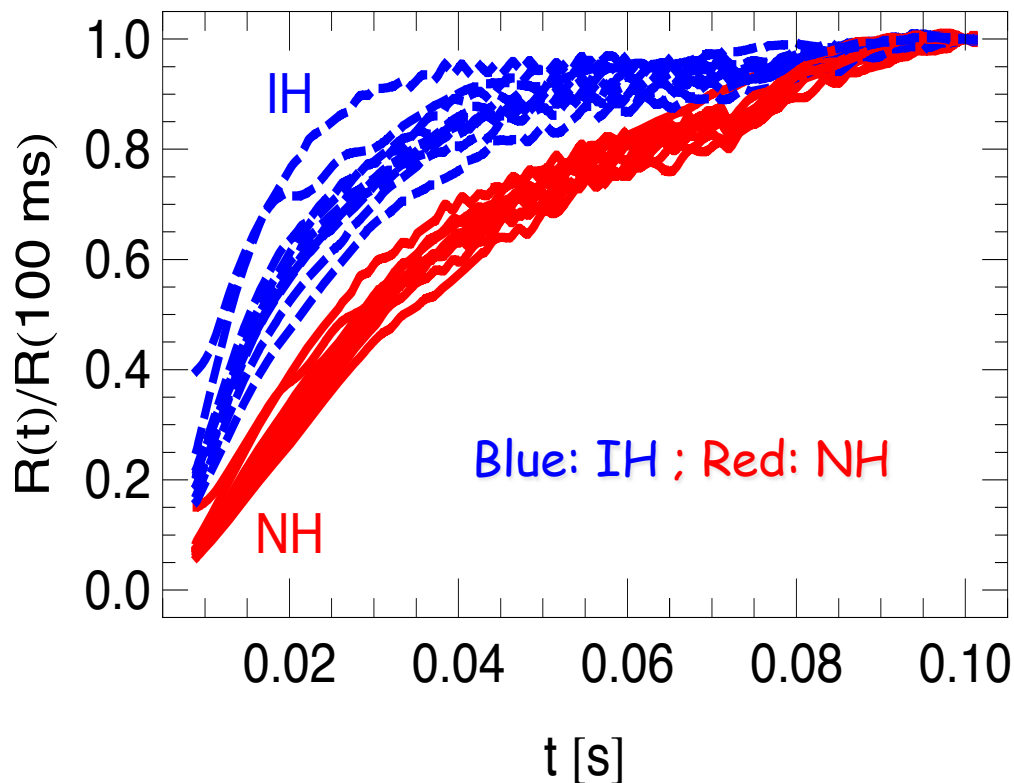
# Rise time Analysis: Hierarchy Determination

Normalized Count rate :

10 different models (12  $M_{\odot}$ -40  $M_{\odot}$ )



*Garching group, 2011*



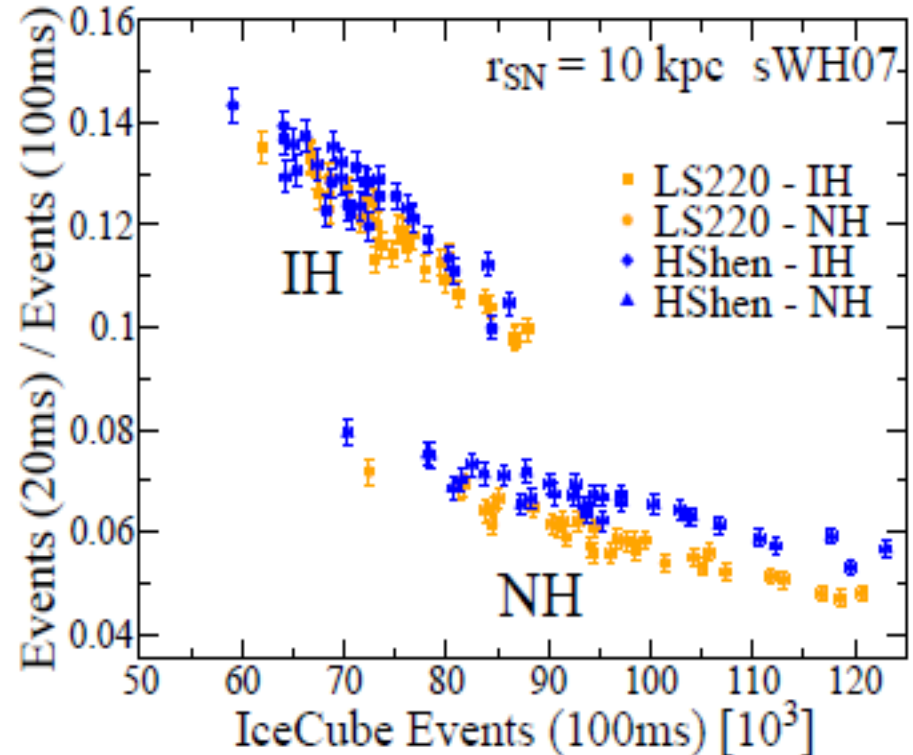
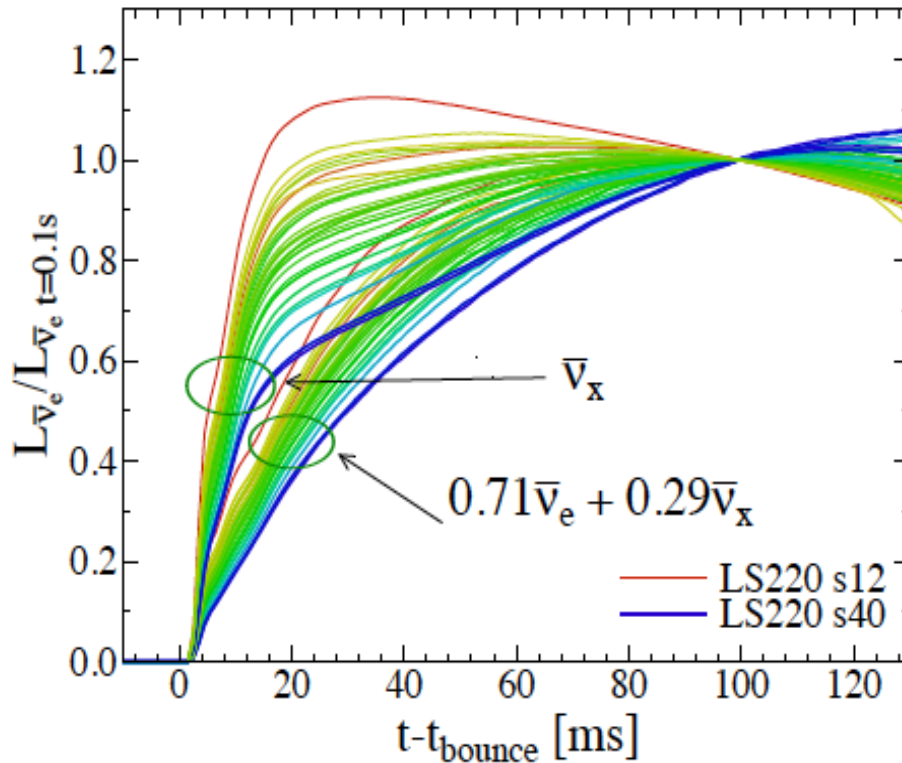
Flux in IH rises faster than NH

[Serpico, S.C, Fischer, Hüdepohl, Janka & Mirizzi  
PRD 85:085031, 2012 ]

# Rise time Analysis: Hierarchy Determination

Normalized Count rate :  
32 different models

[C.D. Ott et al. Neutrino 2012, Japan, 1212.4250]



It would be important in future to study the robustness of the rise time signature with more and more accurate simulations.

# Conclusions

- Observing SN neutrinos is the next frontier of low-energy neutrino astronomy.
- Collective effects are suppressed in early SN phases, implying hierarchy sensitivity at large  $\theta_{13}$ .
- Neutronization phase is the best phase to probe mass hierarchy.
- Earth Matter effect: Detectable for Sub-kpc SNe.
- Rise time of SNe signal contains hierarchy information.



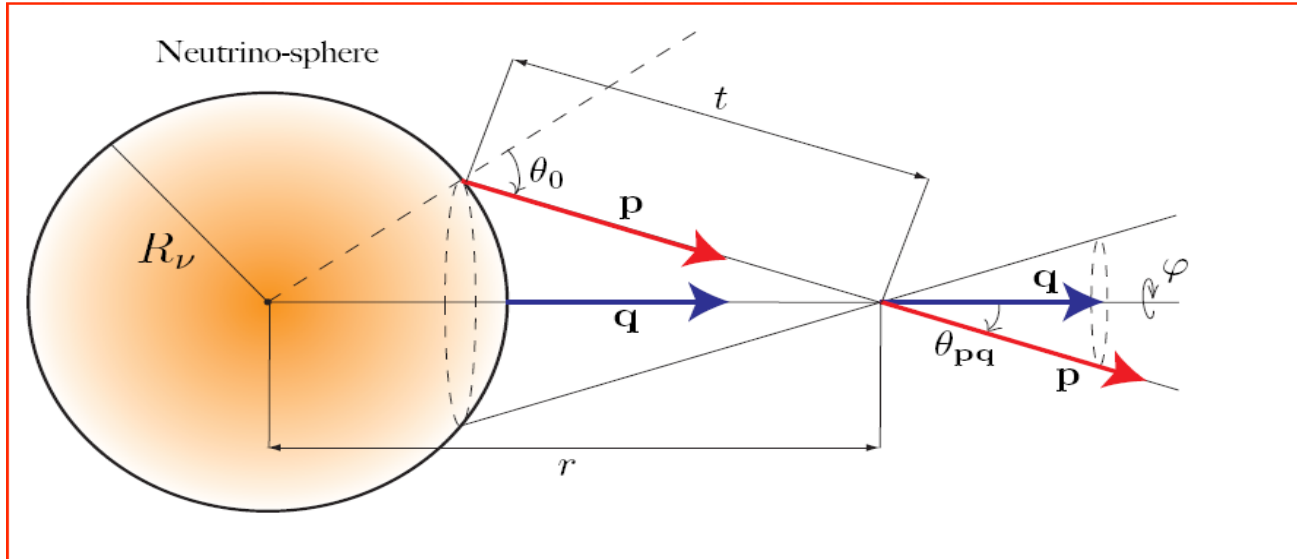
The background of the slide is a reproduction of the painting 'The Starry Night' by Vincent van Gogh. It features a dark, swirling night sky filled with numerous bright, glowing stars and a large, luminous crescent moon in the upper right. In the foreground, a dark, jagged cypress tree stands on the left, and a small village with a church spire is visible in the lower right. The overall style is characterized by visible, expressive brushstrokes.

LOOKING FORWARD  
FOR THE NEXT  
**GALACTIC SN !**

**Thank You !**



# Appendix: Matter Suppression



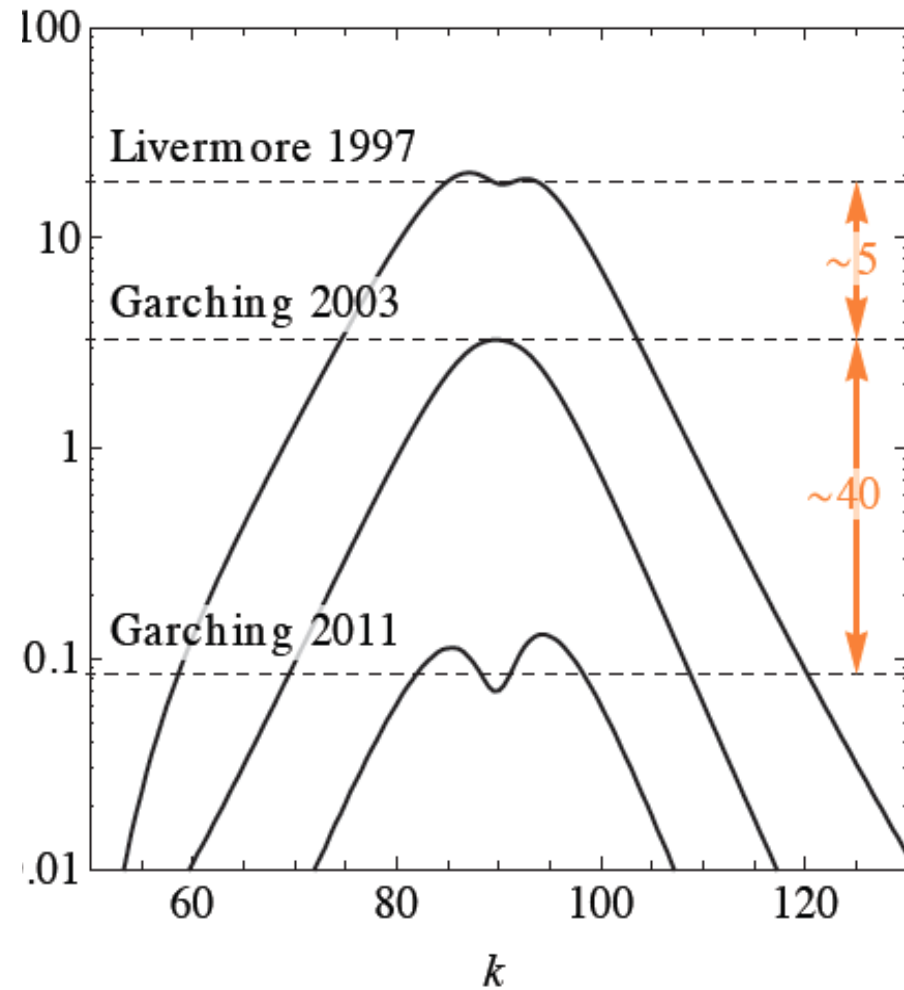
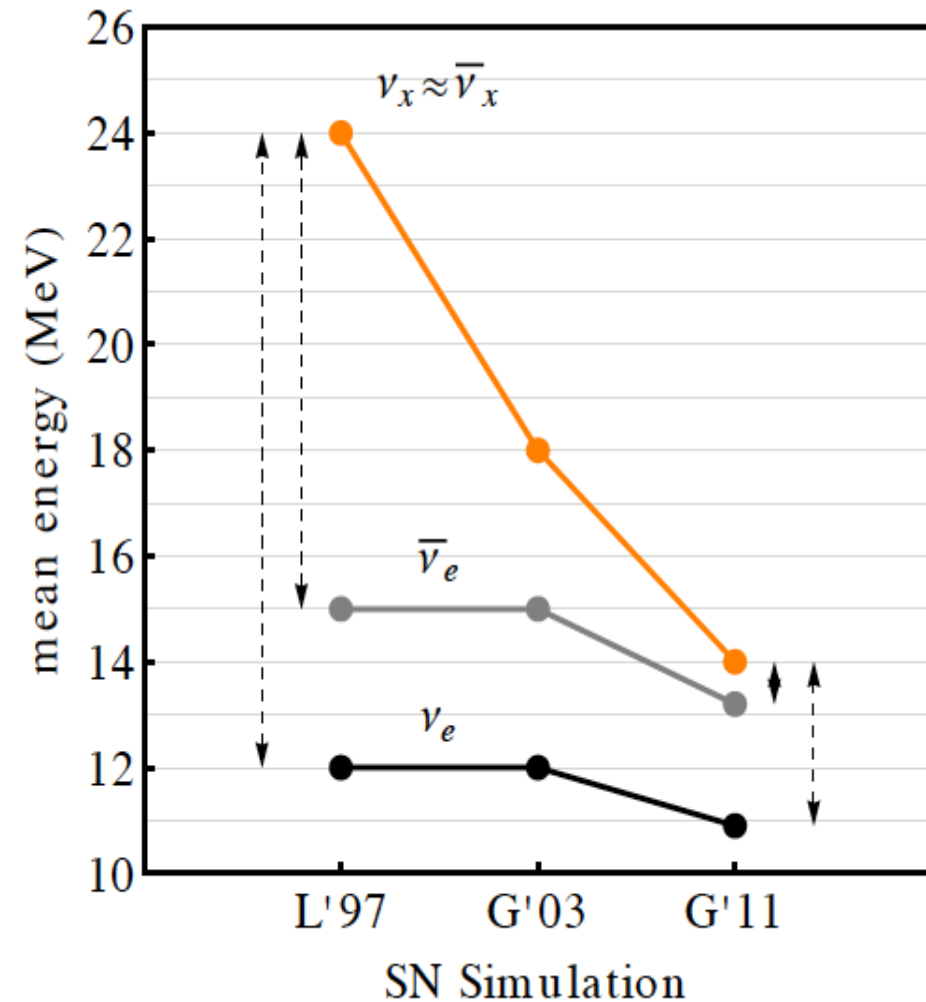
- Neutrinos emitted from spherical source, travel on different trajectories.
- Different oscillation phases for neutrinos traveling in different paths.
- Strong  $\nu$ - $\nu$  interaction can overcome trajectory dependent dispersion.

Collective conversion requires :  $\mathbf{n}_e \ll \mathbf{n}_\nu$

Collective conversion is matter Suppressed :  $\mathbf{n}_e \gtrsim \mathbf{n}_\nu$

# Appendix: SN antineutrino Flux at Earth

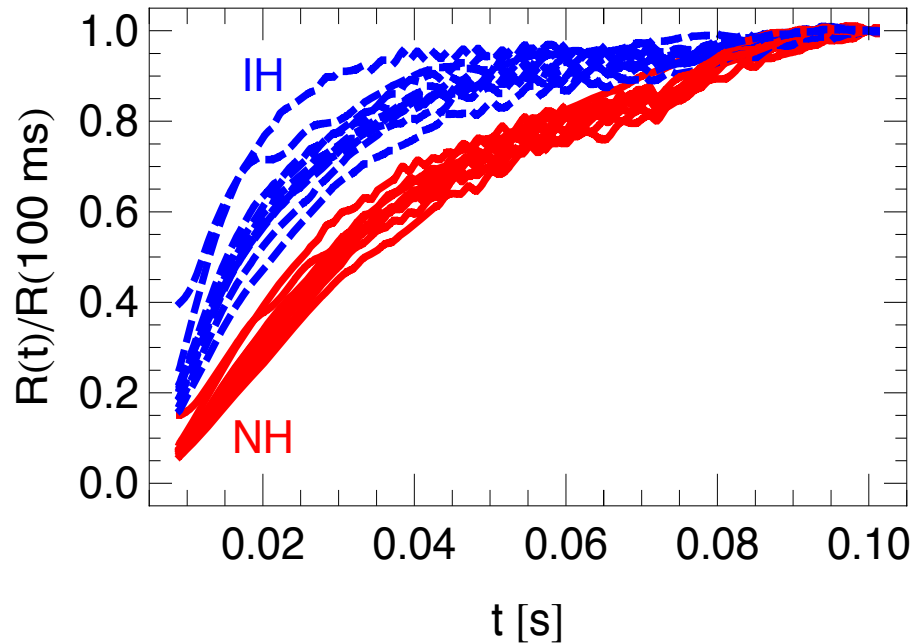
## Earth Matter Effect:



[ Borriello, S.C, Mirizzi, Serpico; PRD 86 (2012) ]



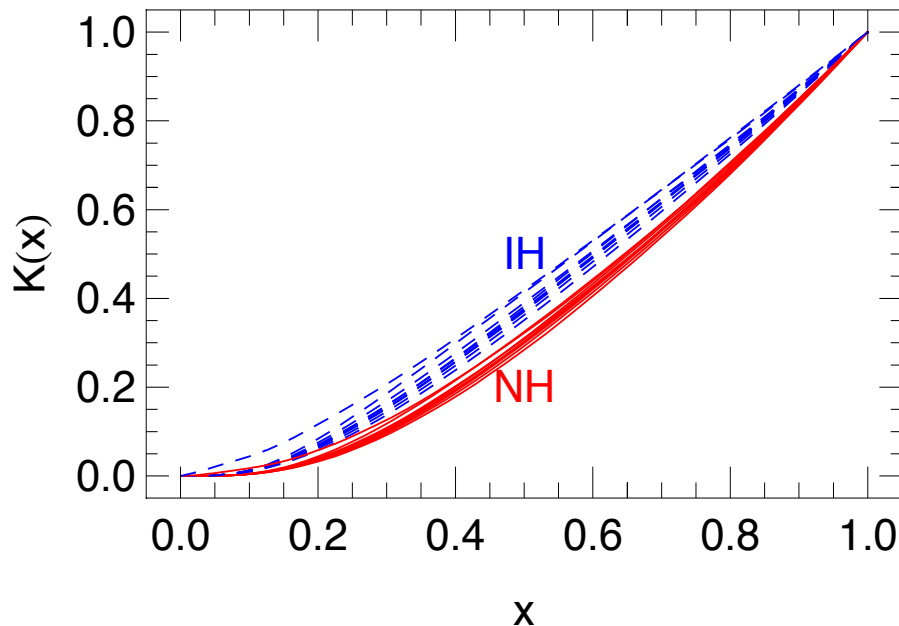
# Appendix: Rise time Analysis: Hierarchy Determination



Count rate (normalized to  
value at 100 ms)  
10 different models, masses  
12 to 40  $M_{\text{sun}}$   
[Blue: IH ; Red: NH]

For Statistical analysis  
introduce  
Cumulative Time Distribution  $K(x)$

$$x = R(t)/R(t_{\text{end}})$$



$$K(x) = \frac{\int_0^x dt R(t)}{\int_0^{t_{\text{end}}} dt R(t)}$$

# Appendix: Rise time Analysis: Hierarchy Determination

Kolmogorov-Smirnov Statistics :

$$\mathcal{D}_{\infty}(K_i^A, K_j^B) = \max_{x \in [0;1]} |K_i^A(x) - K_j^B(x)|$$

Distance between  
any randomly picked **NH** "model"  
from **average IH** one  
is significantly above  
the one from **average NH** ones  
and well expected statistical errors.

Assessing "theory/numerical" error  
requires detailed study over other  
simulations with comparable  
sophistication.

