

Neutrino Mass Hierarchy from Supernova Neutrinos



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MPI for Physics, Munich

Beijing, Nufact August 19-24, 2013



Outline

Supernova (SN) as Neutrino Source

Oscillation of SN Neutrinos

Signatures of Neutrino Mass Hierarchy

Conclusions

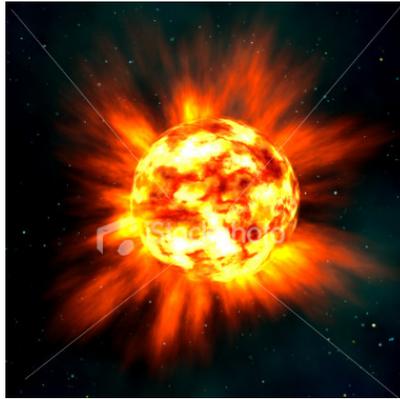
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Supernova one of the most energetic events in nature.

Terminal phase of a massive star ($M > 8\sim 10 M_{\odot}$)

Collapses and ejects the outer mantle in a shock wave driven explosion.

ENERGY SCALES: $\sim 10^{53}$ erg : 99% energy is emitted by Neutrinos (Energy ~ 10 MeV).

TIME SCALE: The duration of the burst lasts ~ 10 s.

Neutrino Emission Phases

Neutronization burst

- Shock breakout
- De-leptonization of outer core layers
- **Duration ~ 25 ms**

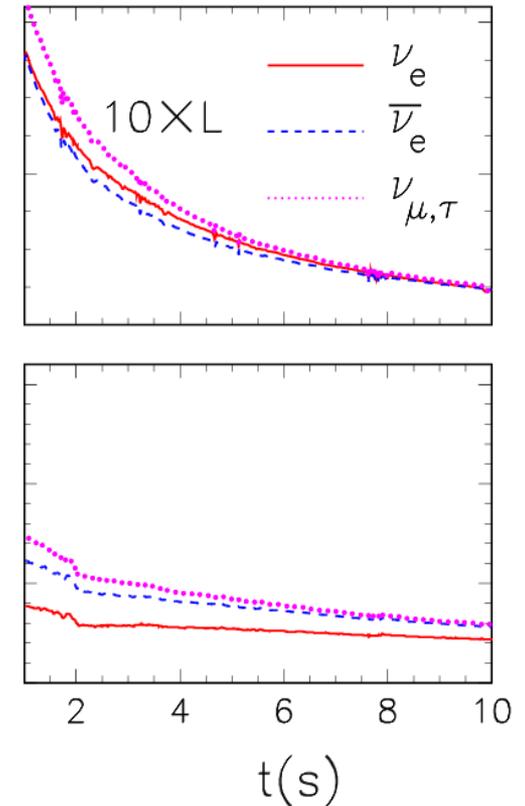
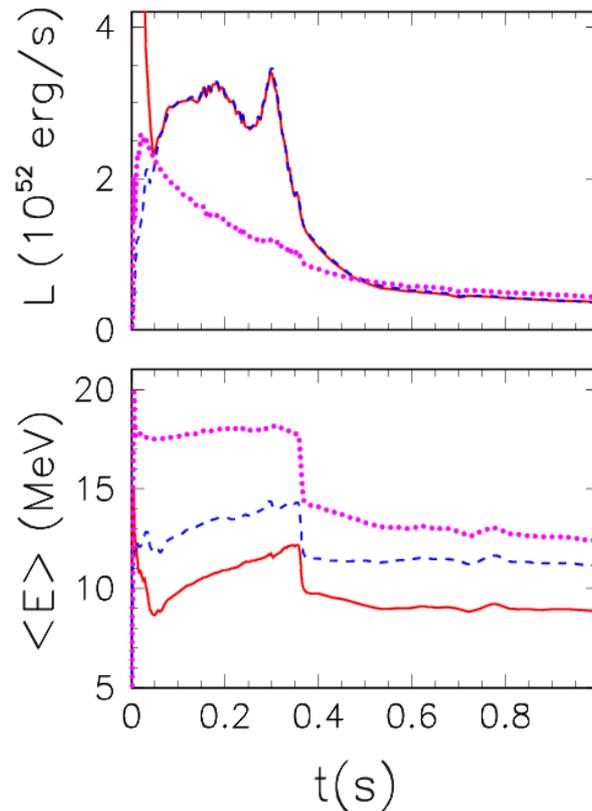
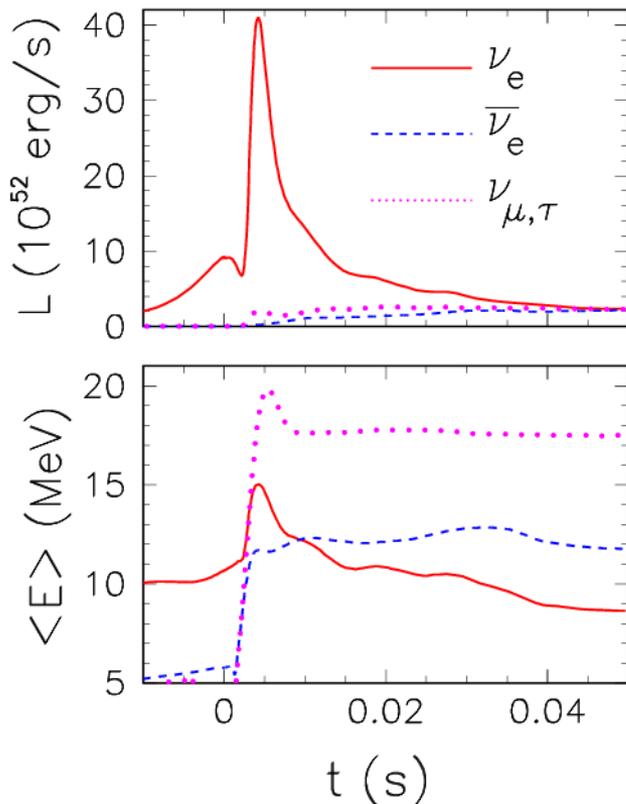
Accretion

- powered by infalling matter
- Stalled shock

Accretion: ~ 0.5 s ; Cooling: ~ 10 s

Cooling

- Cooling by ν diffusion



Plan of the talk

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SN ν Flavor Evolution

The flavor evolution in matter is described by the non-linear MSW equations:

$$i \frac{d}{dx} \psi_\nu = (H_{vac} + H_e + H_{\nu\nu}) \psi_\nu$$

In the standard 3 ν framework

- $H_{vac} = \frac{U M^2 U^\dagger}{2E}$

Kinematical mass-mixing term

- $H_e = \sqrt{2} G_F \text{diag}(N_e, 0, 0)$

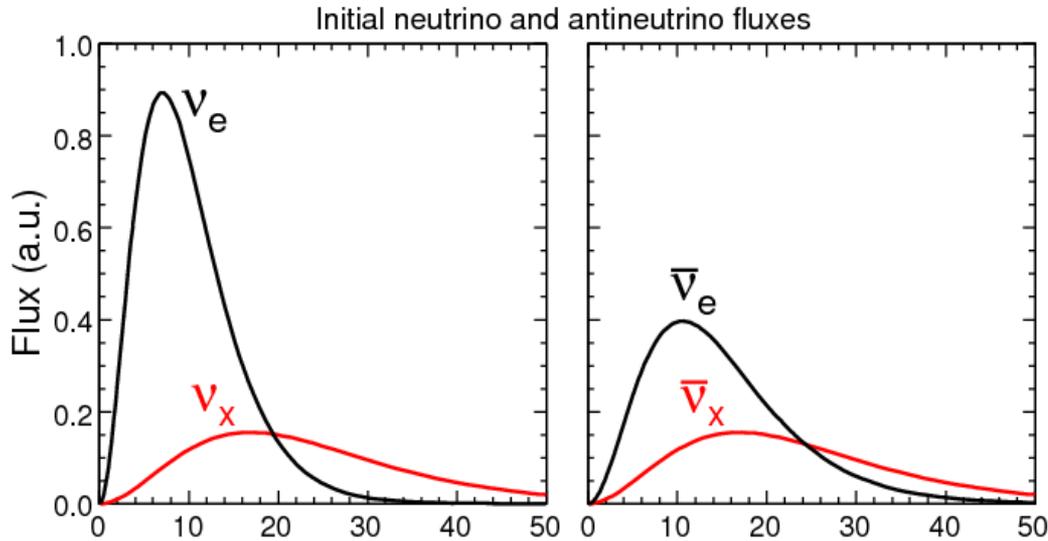
Dynamical MSW term (in matter)

- $H_{\nu\nu} = \sqrt{2} G_F \int (1 - \cos \theta_{pq}) (\rho_q - \bar{\rho}_q) dq$

**Neutrino-neutrino interactions term
(non-linear)**

Spectral Splits in the Accretion Phase

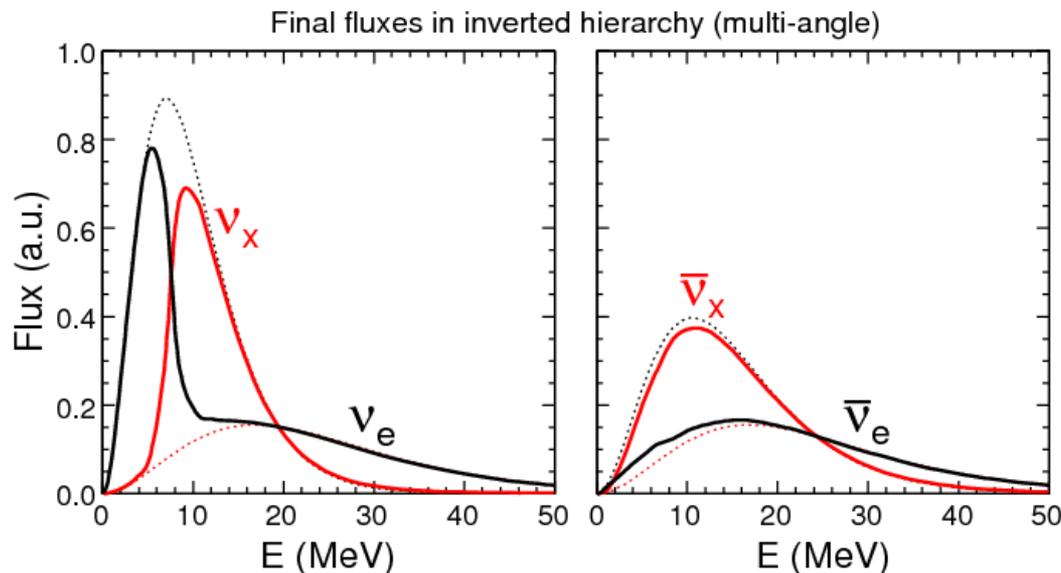
[Fogli, Lisi, Marrone, Mirizzi, arXiv: 0707.1998 [hep-ph]]



Initial fluxes typical of accretion phase at neutrinosphere ($r \sim 10$ km)

$$F_{\nu_e} : F_{\bar{\nu}_e} : F_{\nu_x} = 2.4 : 1.6 : 1.0$$

Inverted mass hierarchy (IH)

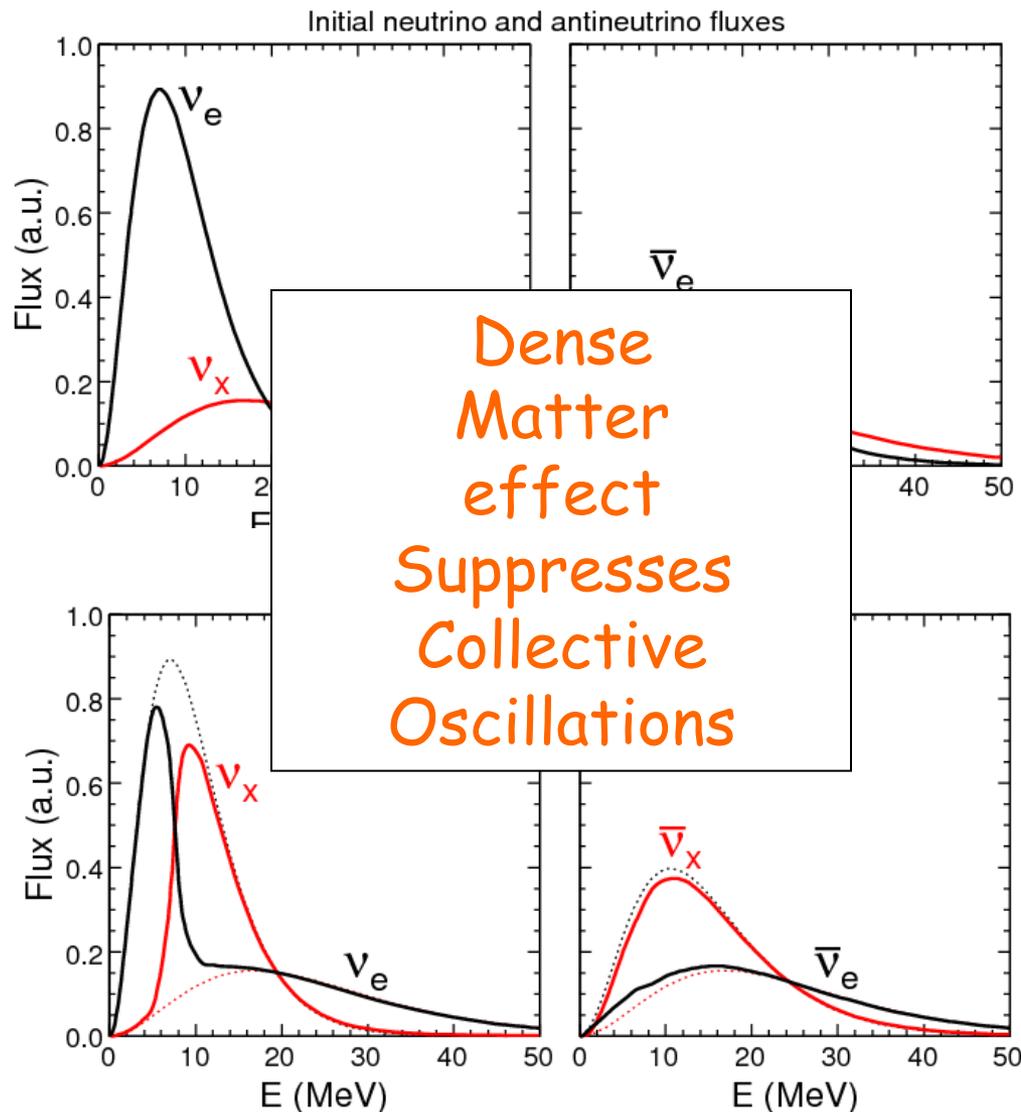


Fluxes at the end of collective effects ($r \sim 200$ km)

Nothing happens in Normal Hierarchy (NH)

Suppression of Collective effects

Dense matter (n_e) dominates over ν - ν interaction (n_ν).



[S.C., Fischer, Mirizzi,
Saviano & Tomas
PRL 107:151101, 2011
PRD 84:025002, 2011

Sarikas, Raffelt, Hüdepohl &
Janka
PRL 108:061101, 2012

Dasgupta, P. O'Connor, Ott
PRD 85:065008, 2012]

Suppression of Collective effects

Predictions are robust when collective effects are suppressed, i.e.:

1) Neutronization burst ($t < 20$ ms)

large ν_e excess and ν_x deficit

[Hannestad et al., [astro-ph/0608695](#)]

2) Accretion phase ($t < 500$ ms)

Dense matter term dominates over ν - ν interaction term.

[[S.C.](#), Fischer, Mirizzi, Saviano & Tomas

PRL 107:151101, 2011
PRD 84:025002, 2011]

SN neutrino Flux at Earth

Neutronization burst & Accretion Phase:

Normal Hierarchy (NH):

$$F_{\nu_e} = F_{\nu_x}^0$$

$$F_{\bar{\nu}_e} = \cos^2 \vartheta_{12} (F_{\bar{\nu}_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

Inverted Hierarchy (IH):

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-

Plan of the talk

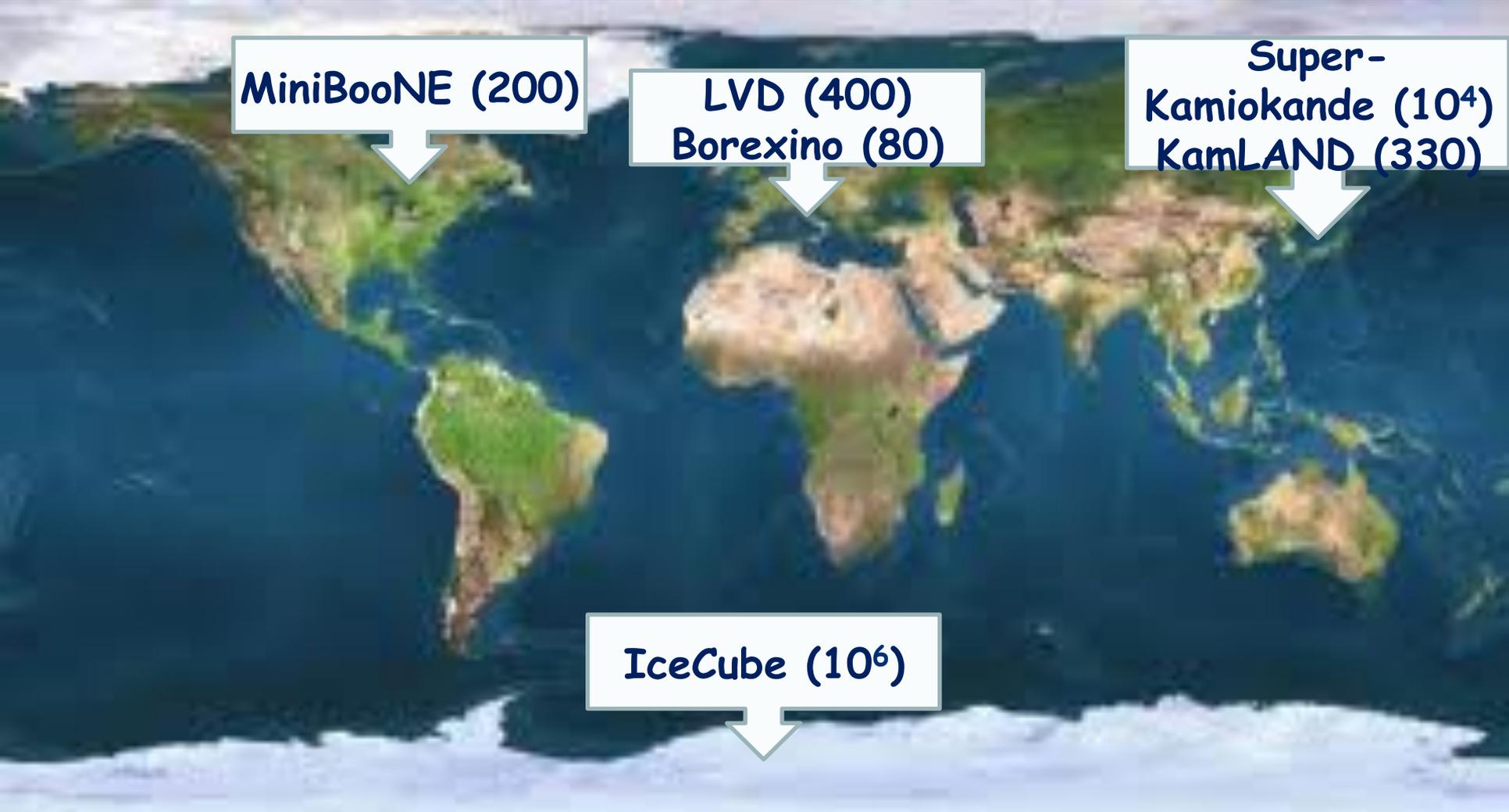
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Large Detectors for Supernova Neutrinos

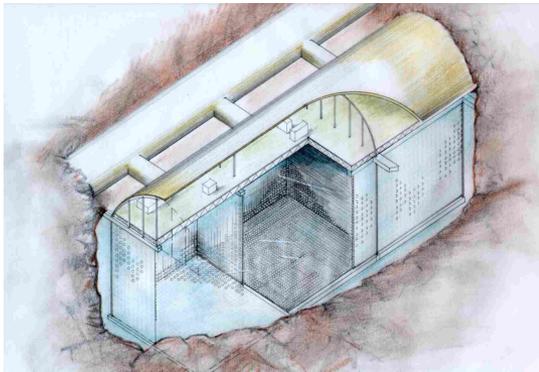


In brackets events for a "fiducial SN" at distance 10 kpc

Next generation Detectors for Supernova Neutrinos

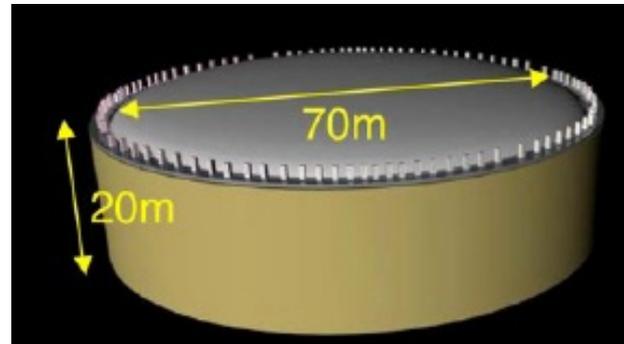
Next-generation large volume detectors might open a new era in SN neutrino detection:

Mton Cherenkov



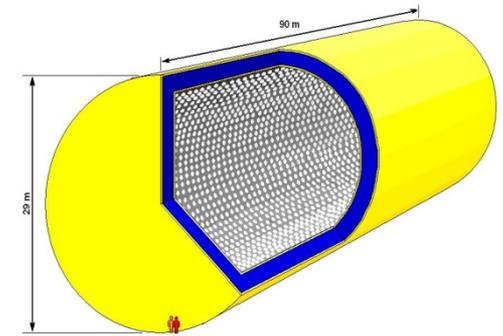
**UNO, MEMPHYS,
HYPER-K**

LAr TPC



GLACIER

Scintillator



LENA

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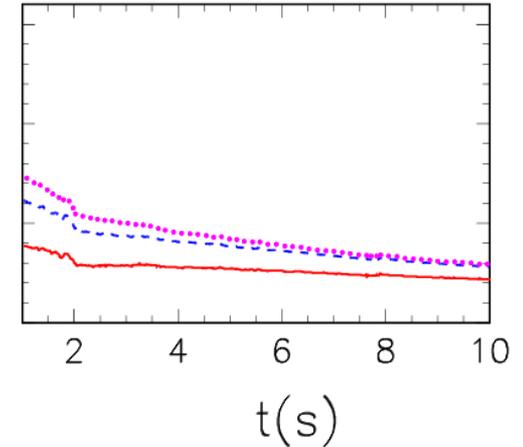
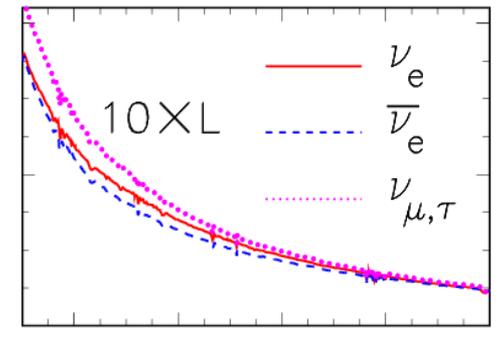
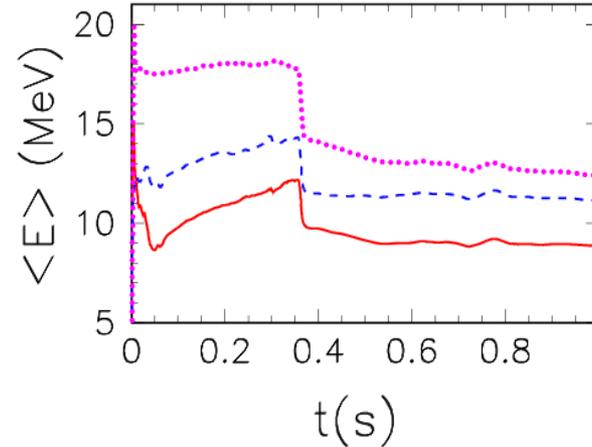
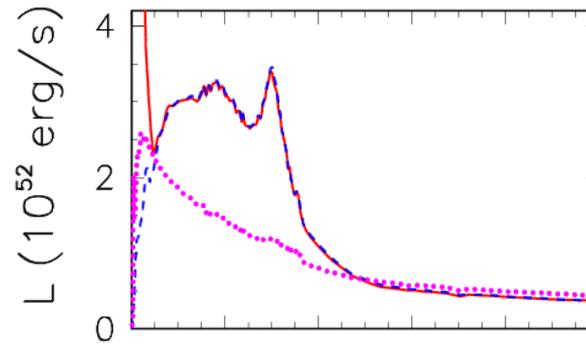
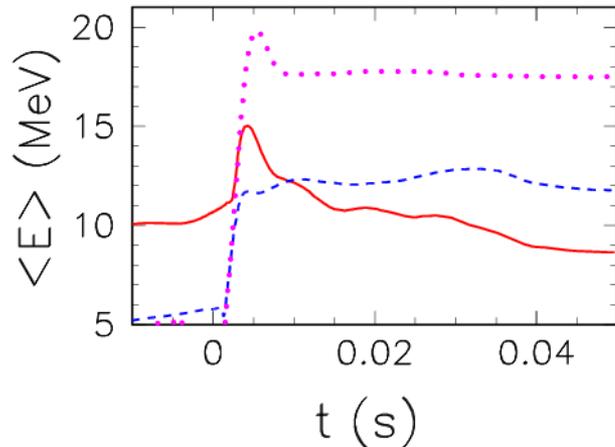
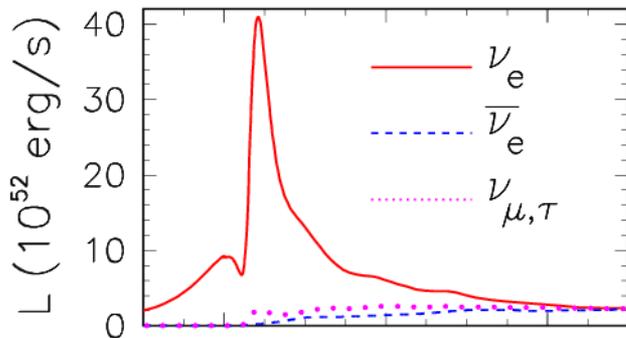
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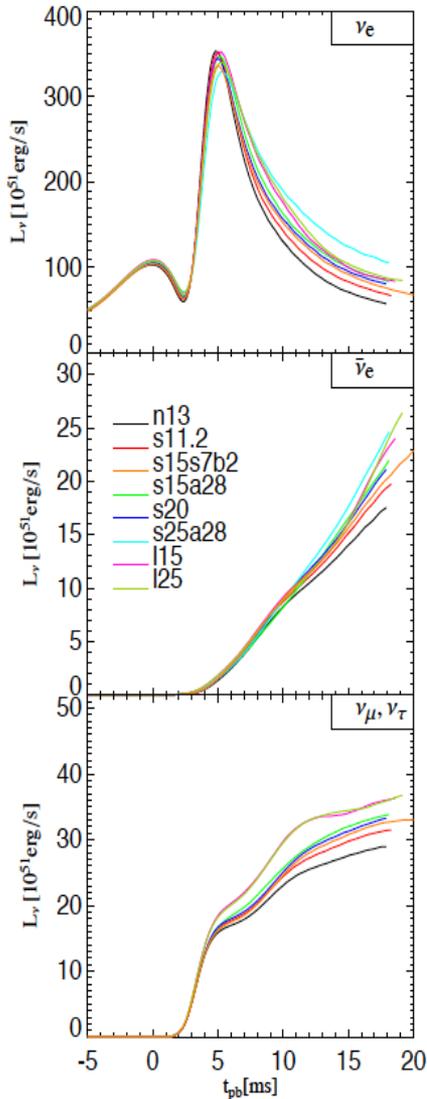
Cooling

- Cooling by ν diffusion

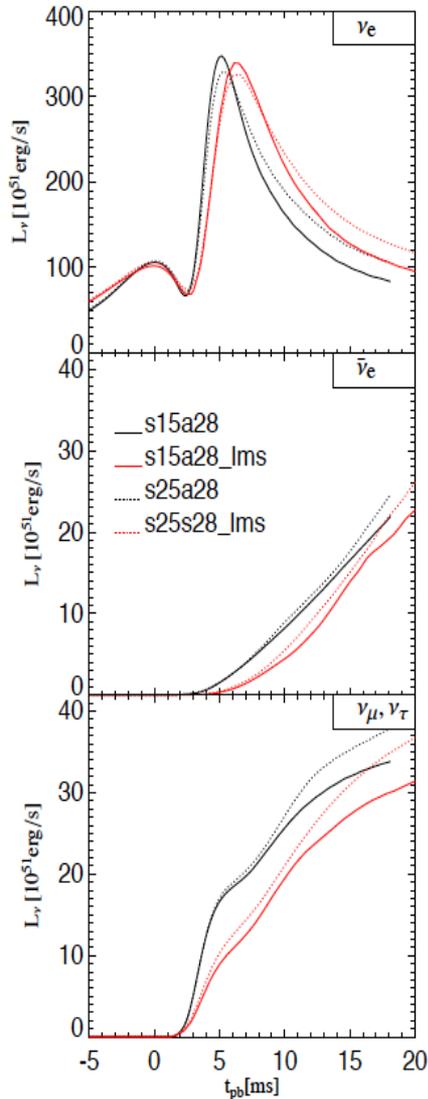


Neutronization Burst : Model Independence

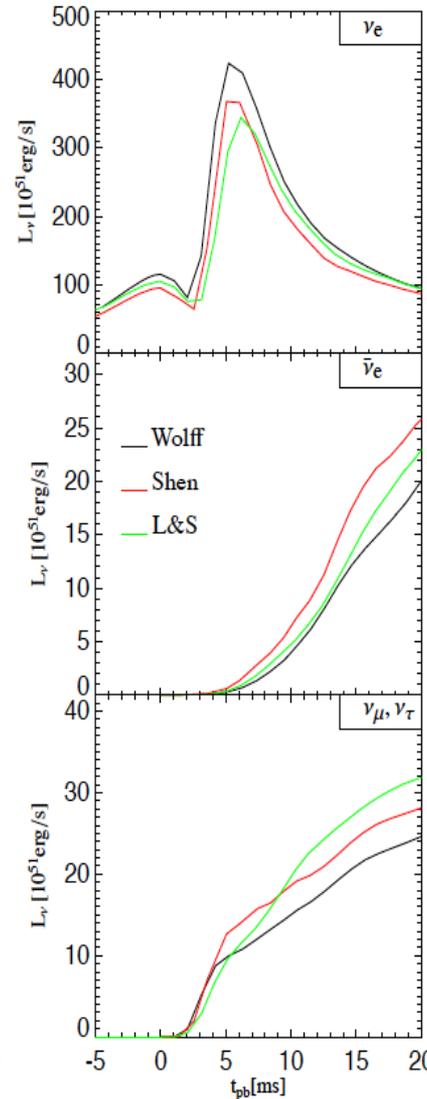
Different mass



Neutrino Transport



Nuclear EoS

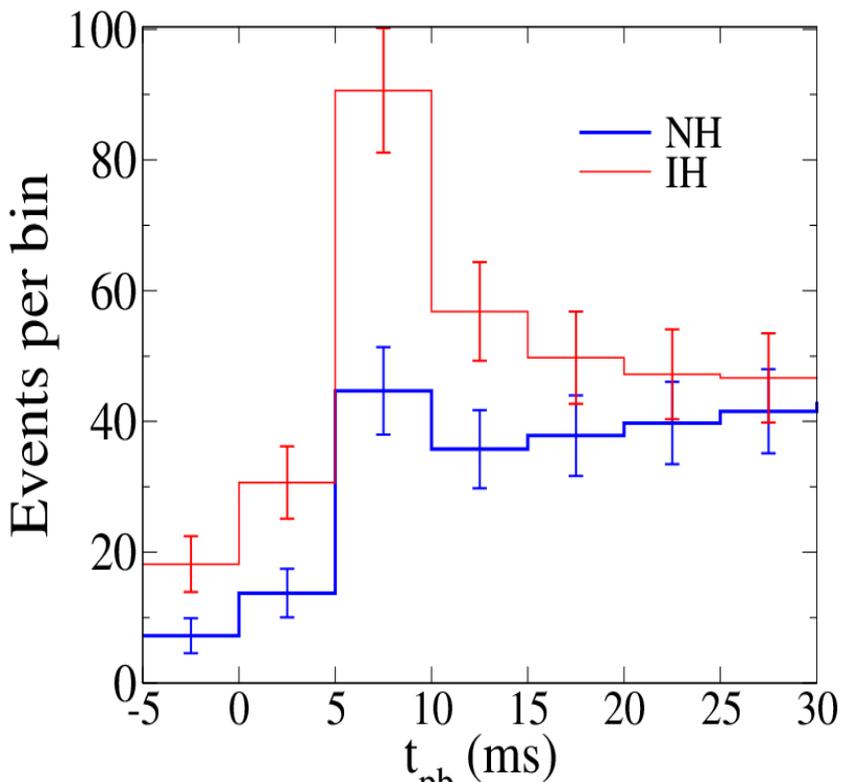


'Standard Candle'
for
SN Neutrino

[M.Kachelriess et al,
hep-ph/0412082]

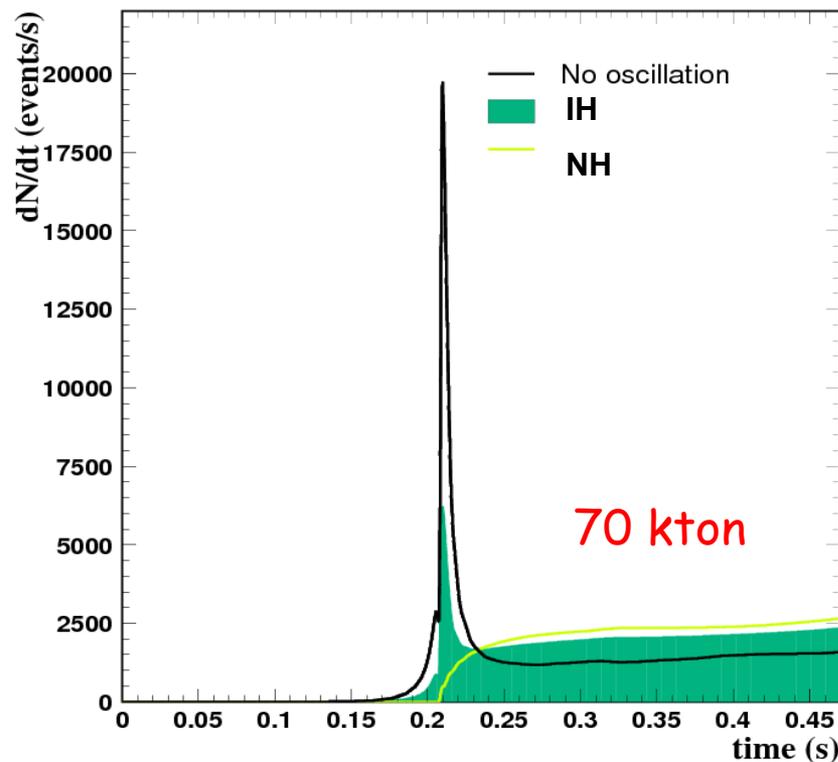
Oscillations in the Neutronization Burst

Water Cherenkov ($\nu_{e,x} e^- \longrightarrow \nu_{e,x} e^-$)



[M.Kachelriess et al, hep-ph/0412082]

Liq Ar TPC ν_e ^{40}Ar CC

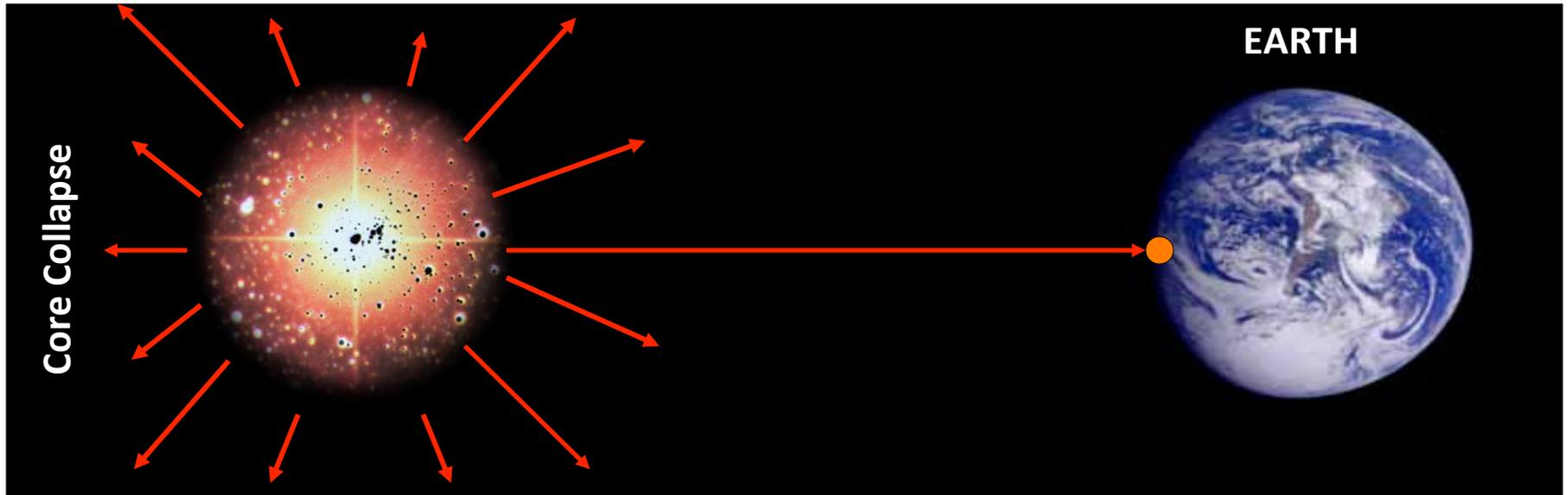


[I.Gil-Botella & A.Rubbia, hep-ph/0307244]

- Peak is absent \longrightarrow NH ($F_{\nu_e} = F_{\nu_x}^0$)
- Peak is seen \longrightarrow IH ($F_{\nu_e} = \sin^2 \vartheta_{12}(F_{\nu_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$)

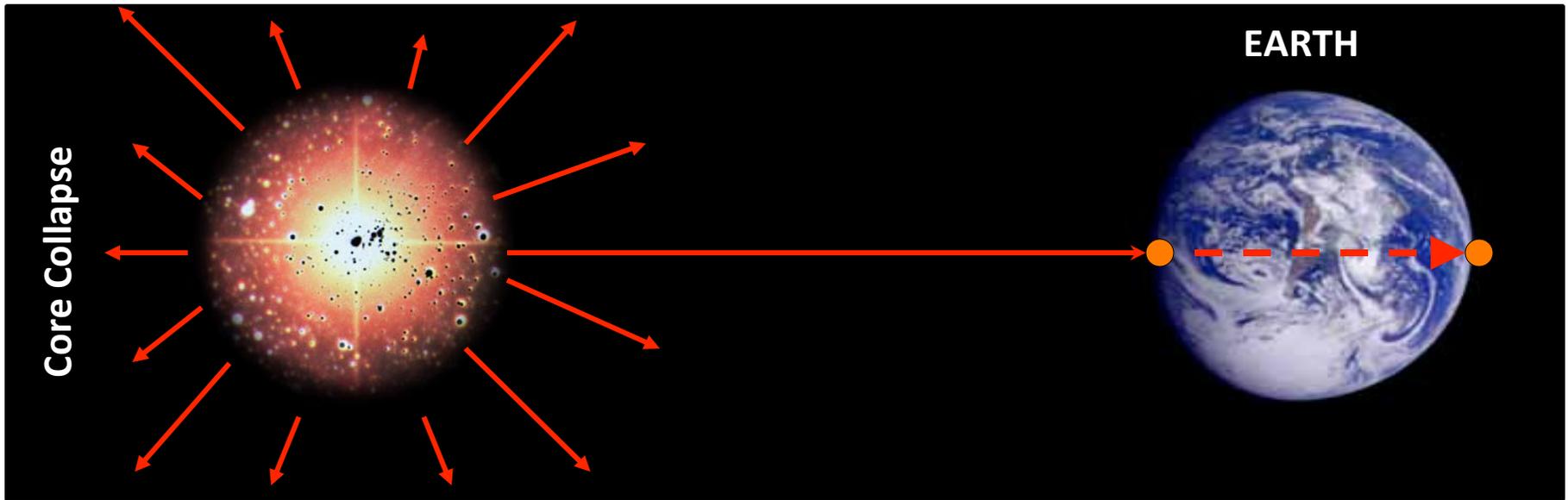
SN neutrino Flux at Earth

Earth Matter Effect:



SN neutrino Flux at Earth

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SN neutrino Flux at Earth

Earth Matter Effect:

$$F_{\bar{e}}^D = \sin^2 \theta_{12} F_{\bar{x}}^0 + \cos^2 \theta_{12} F_{\bar{e}}^0 + \Delta F^0 \bar{A}_{\oplus} \sin^2(12.5 \overline{\Delta m_{\oplus}^2} L/E)$$

Normal Hierarchy (NH):

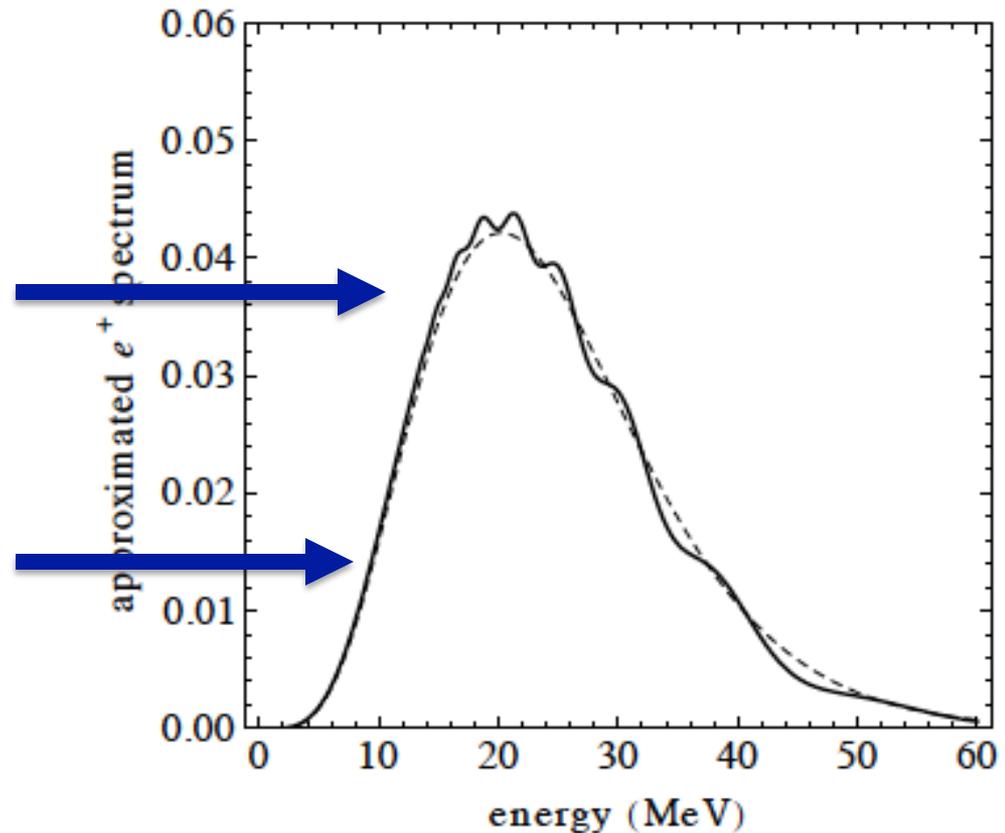
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Inverted Hierarchy (IH):

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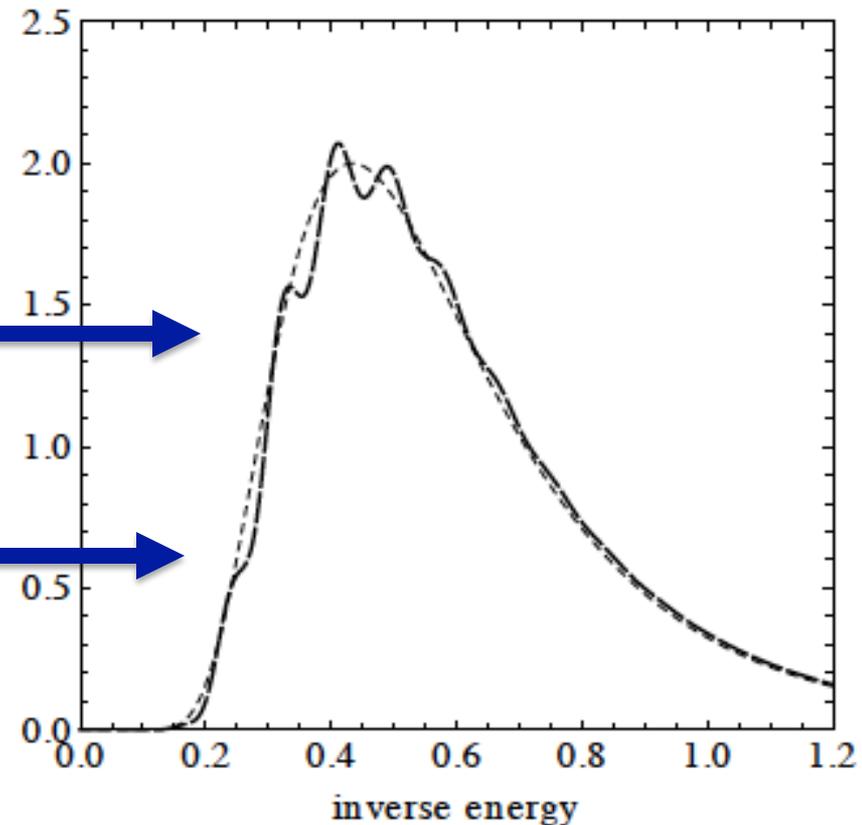
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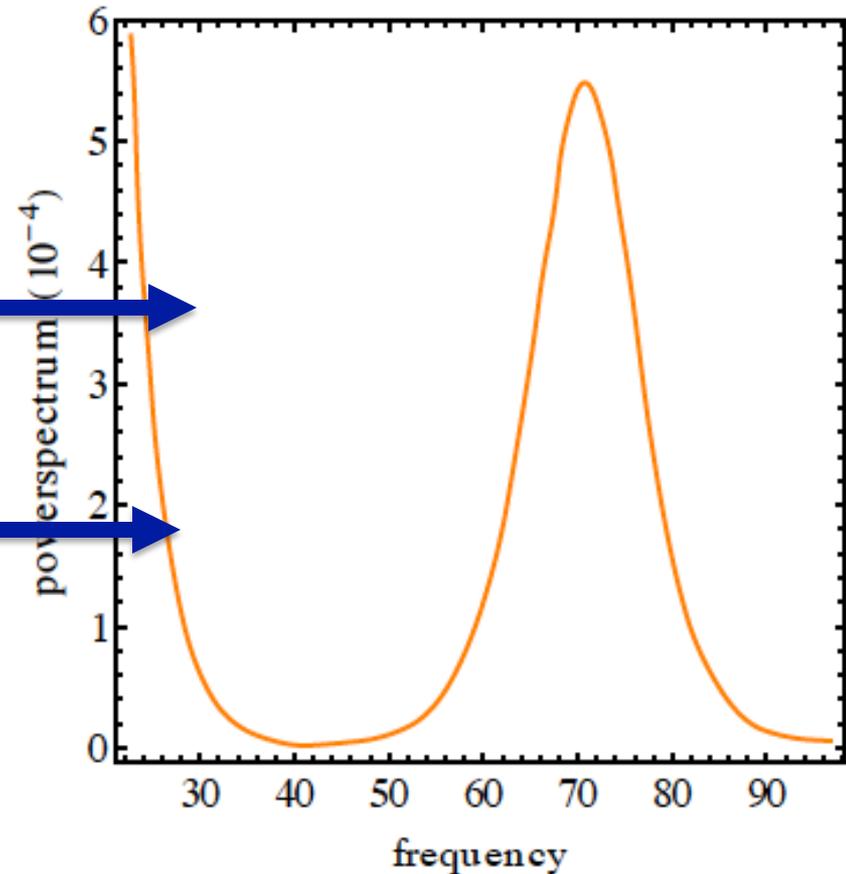
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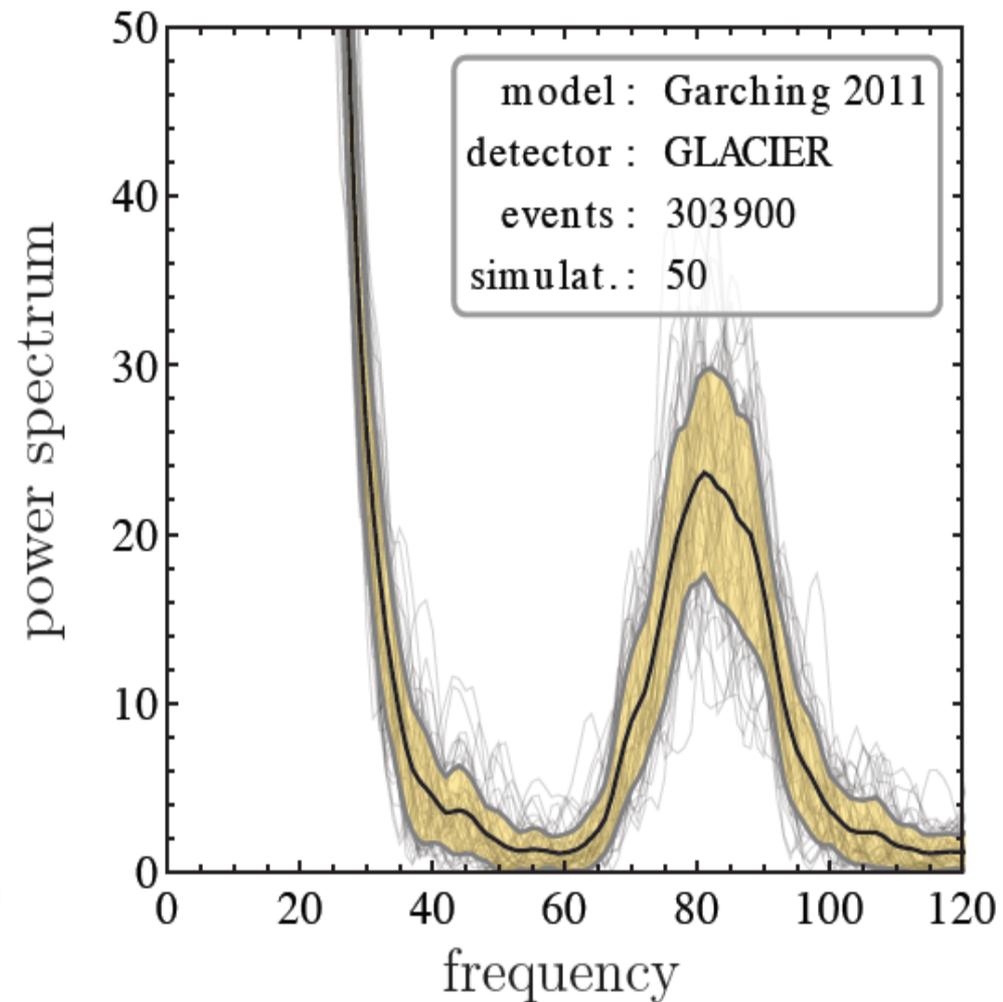
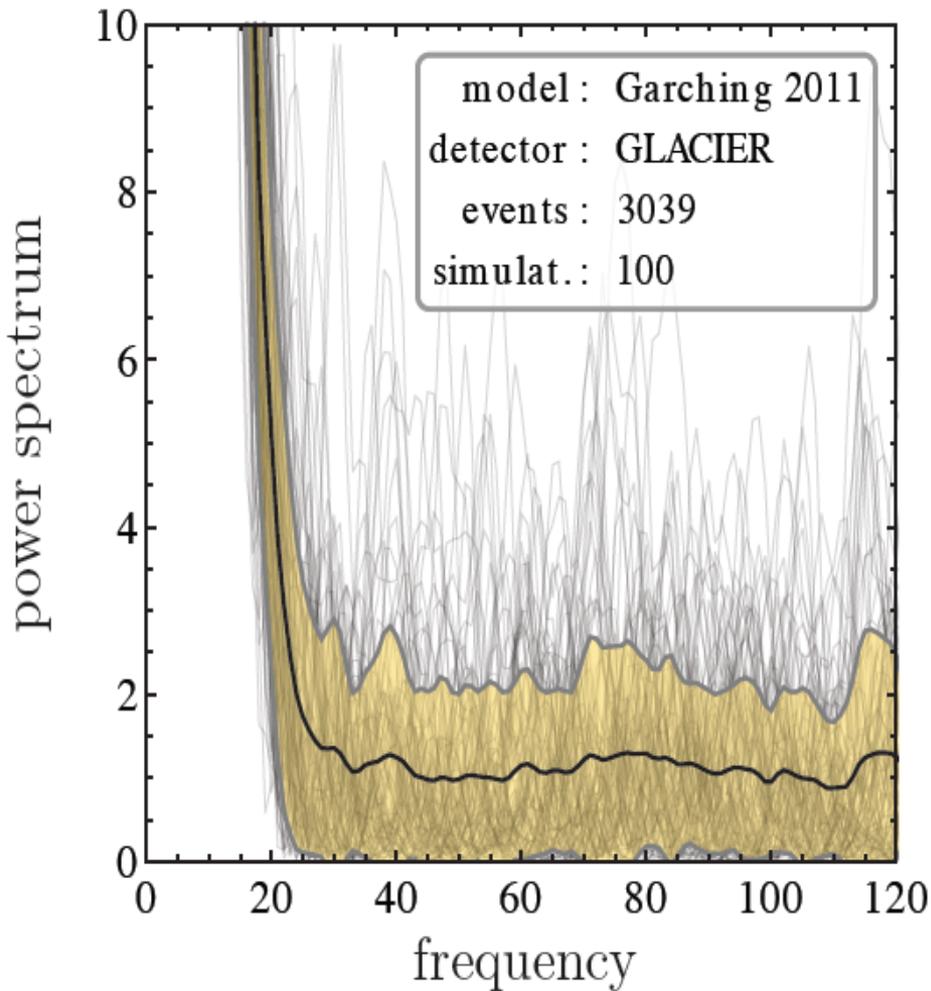
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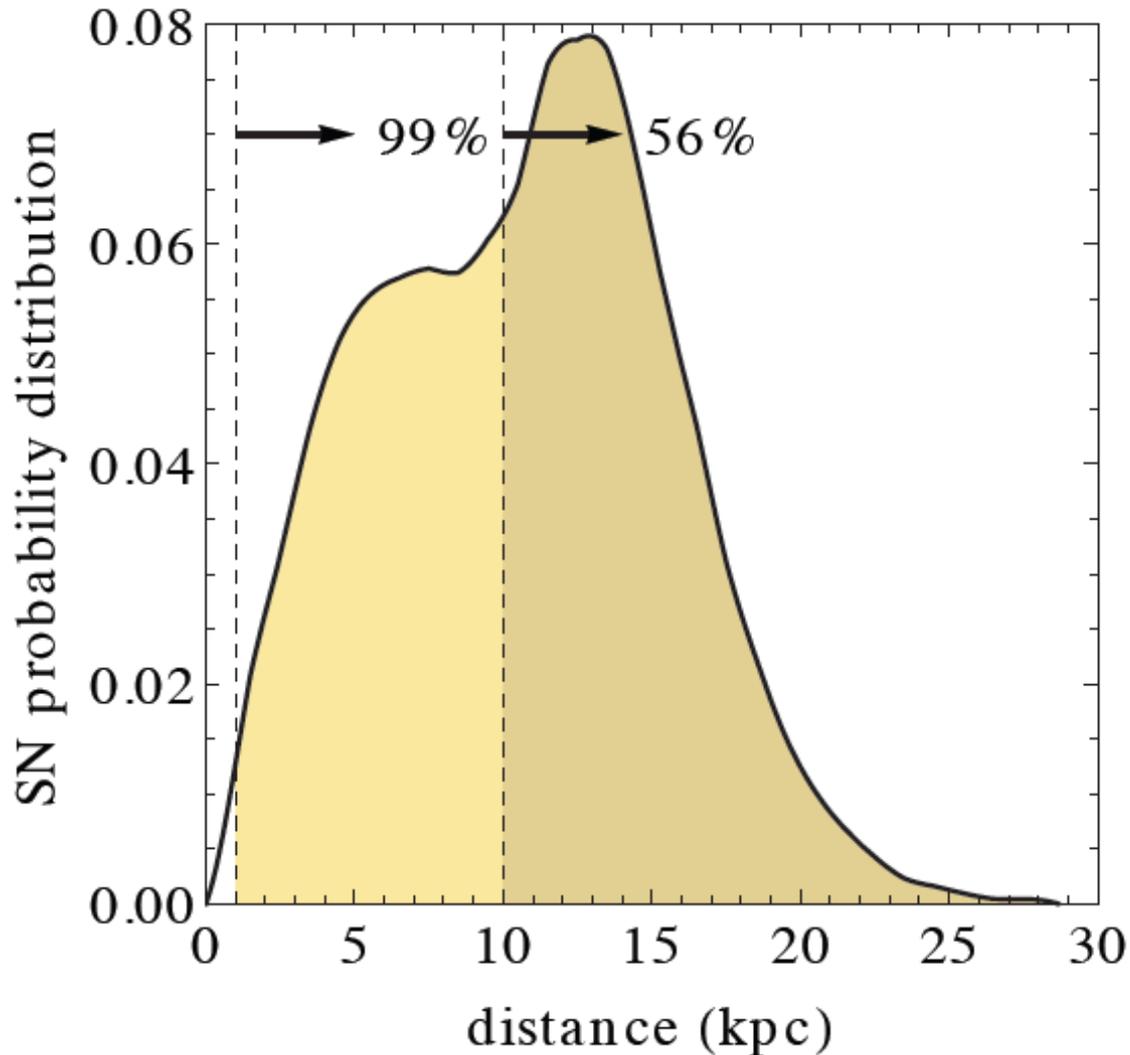
SN neutrino Flux at Earth

Earth Matter Effect:



[Borriello, S.C, Mirizzi, Serpico; PRD 86 (2012)]

Galactic SN Distribution



Possible sub-kpc candidate:

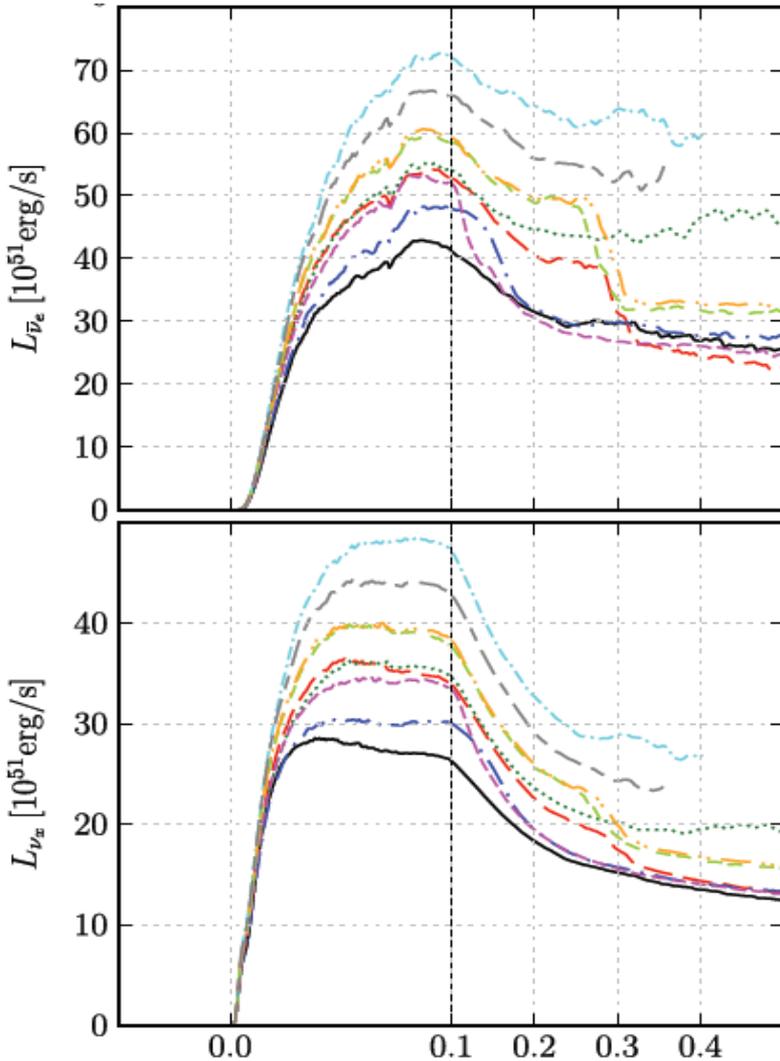
Red supergiant Betelguse

distance \sim 0.2 kpc

Event count \sim 10s of million

[Mirizzi, Raffelt & Serpico; (2006)]

Rise time Analysis: Hierarchy Determination



Garching group, 2011

- High degeneracy of ν_e and e , suppresses $\bar{\nu}_e$ production.
- $\bar{\nu}_e$ more in equilibrium with environment than ν_x .

Flux of ν_x rises faster than $\bar{\nu}_e$

$$\text{NH: } F_{\bar{\nu}_e} = \cos^2 \vartheta_{12} (F_{\bar{\nu}_e}^0 - F_{\nu_x}^0) + F_{\nu_x}^0$$

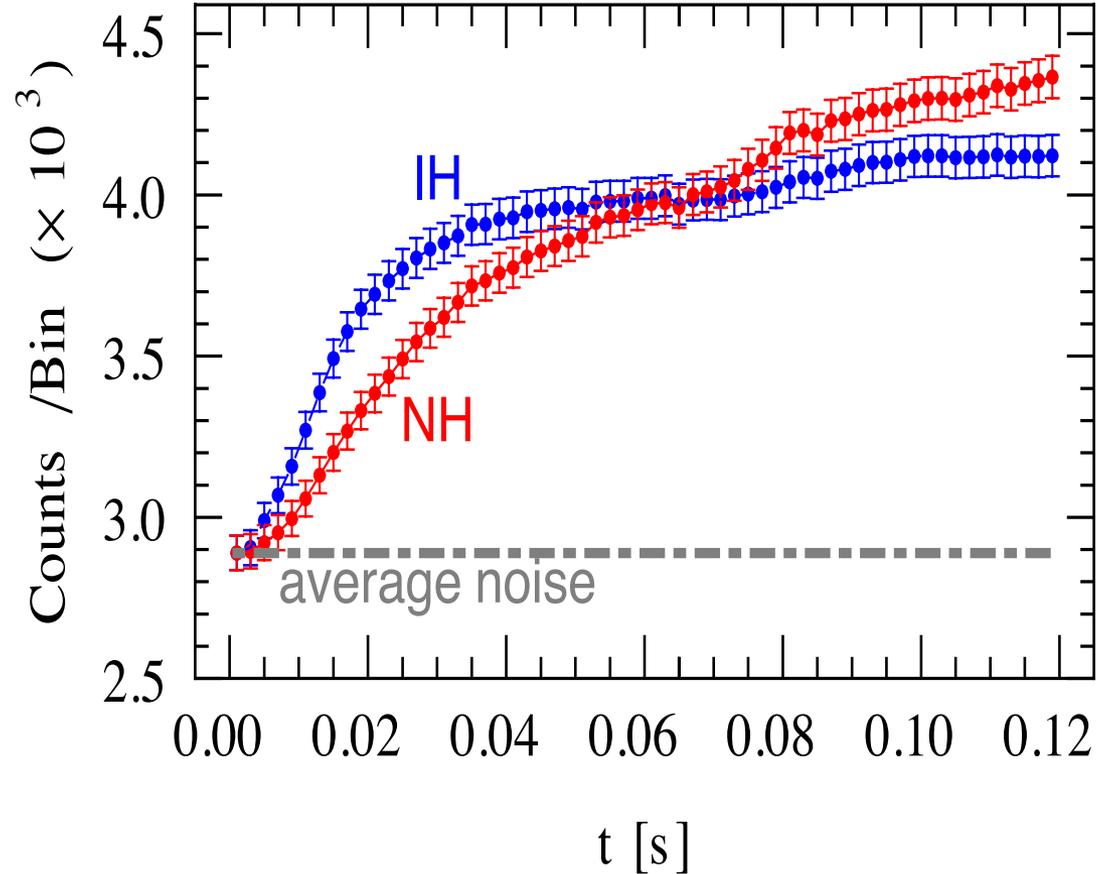
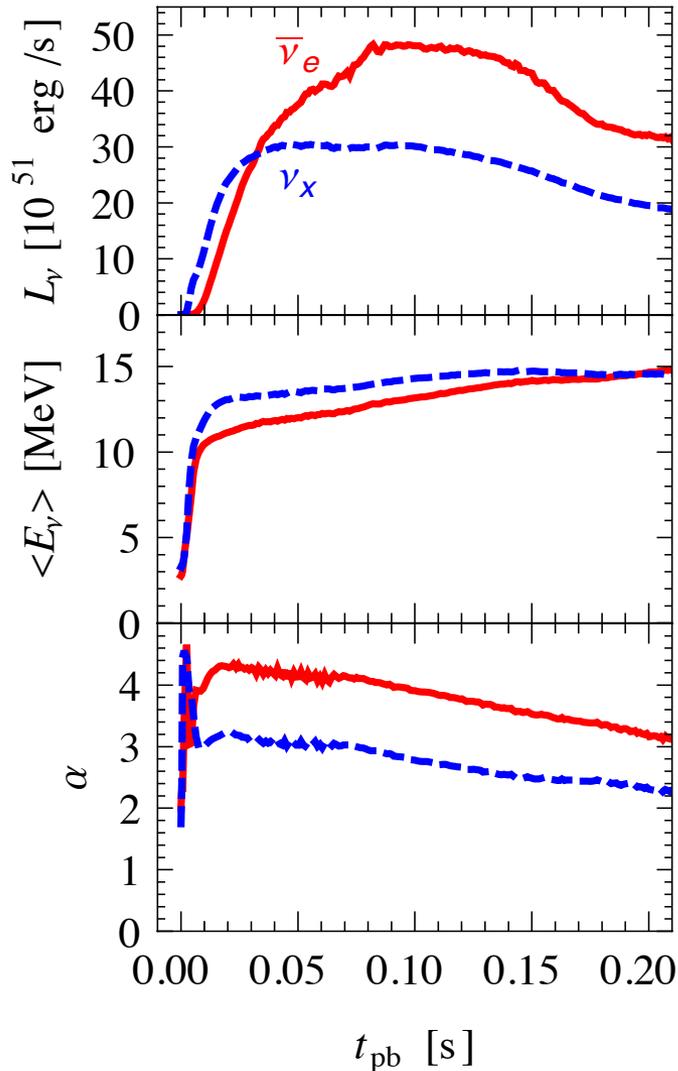
$$\text{IH: } F_{\bar{\nu}_e} = F_{\nu_x}^0$$

Flux in IH (ν_x) rises faster than NH ($\nu_x, \bar{\nu}_e$)

[Serpico, S.C, Fischer, Hüdepohl, Janka & Mirizzi
PRD 85:085031, 2012]

Rise time Analysis: Hierarchy Determination

15 Solar Mass
in Ice-Cube



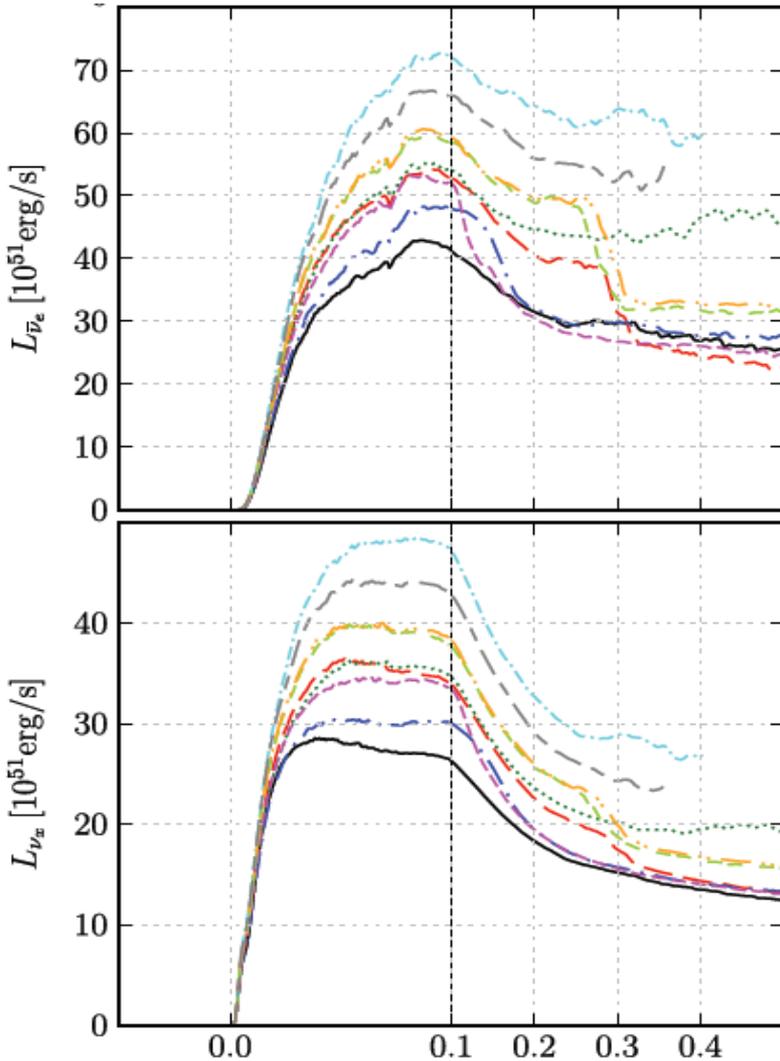
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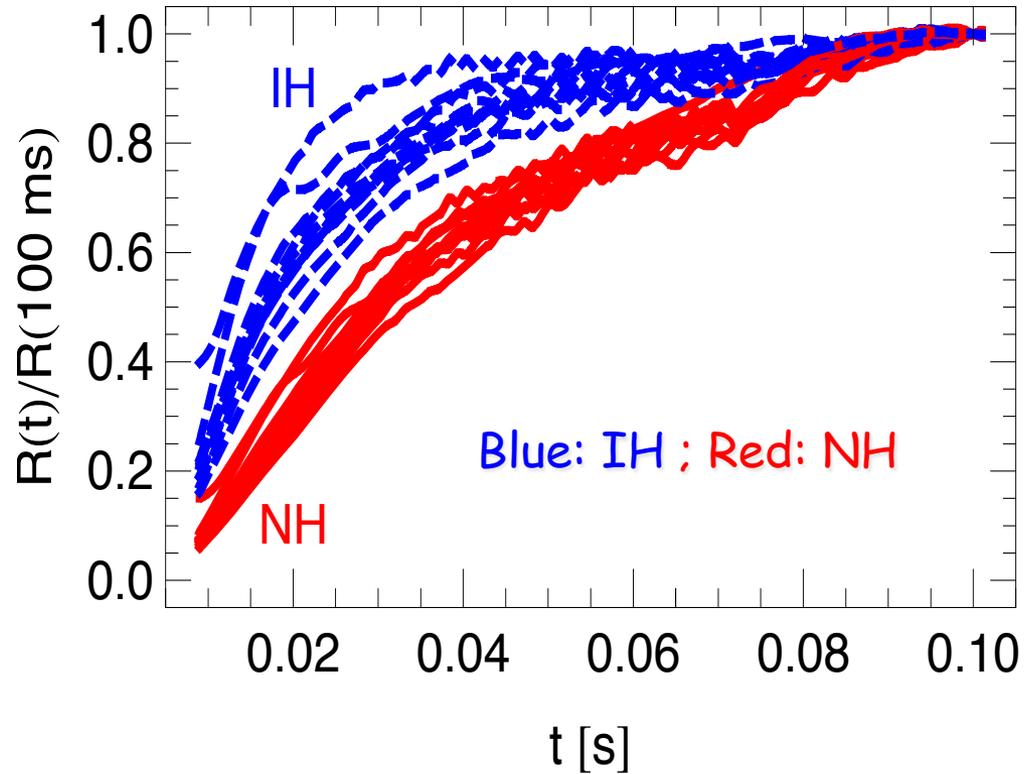
Rise time Analysis: Hierarchy Determination

Normalized Count rate :

10 different models (12 M_{\odot} -40 M_{\odot})



Garching group, 2011



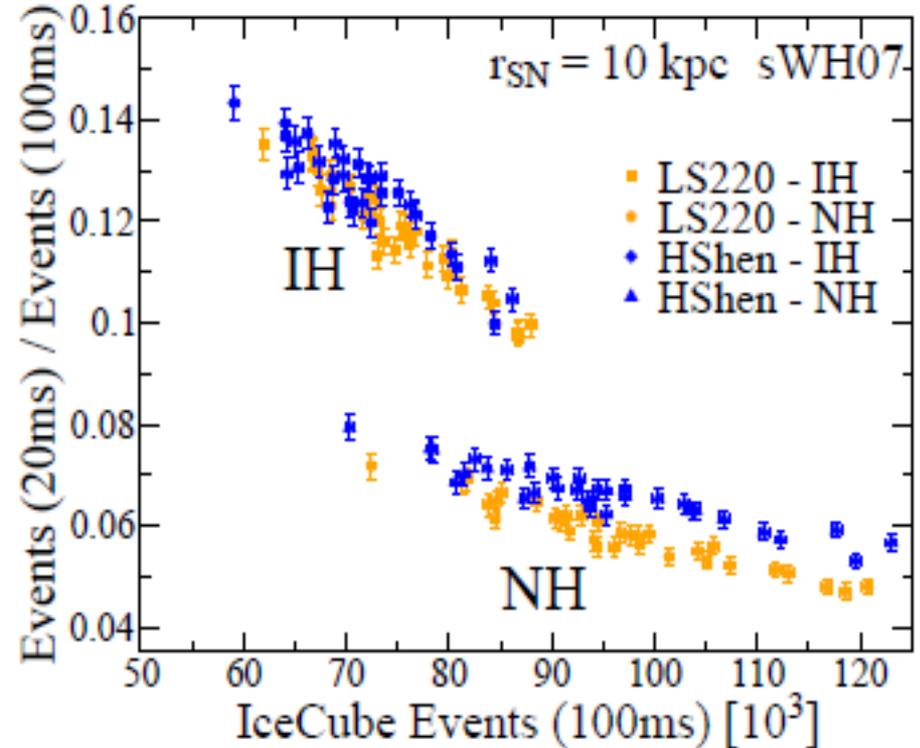
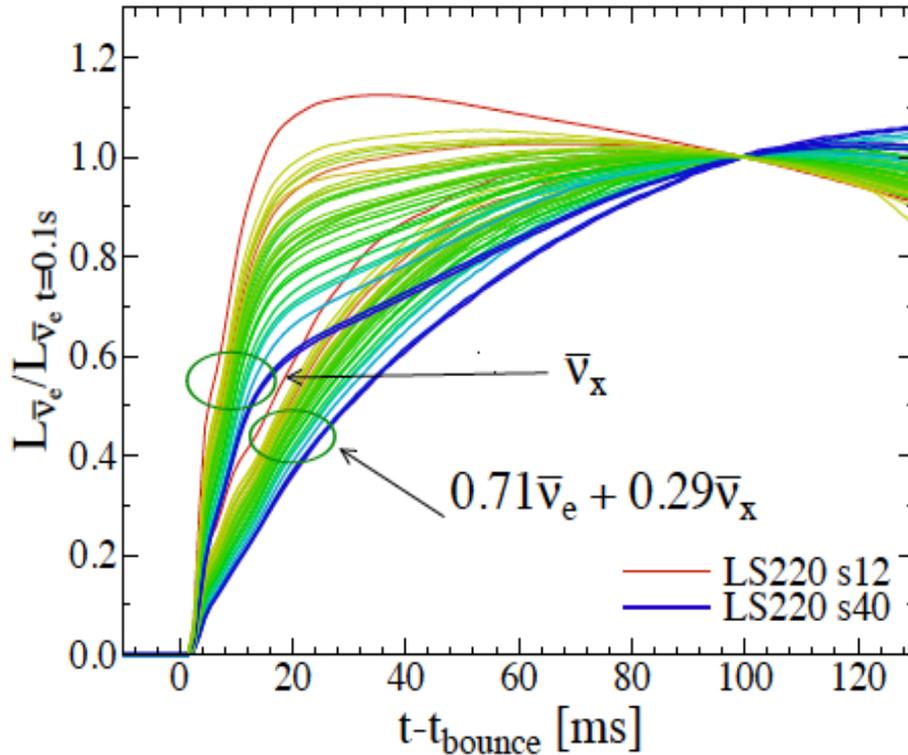
Flux in IH rises faster than NH

[Serpico, S.C, Fischer, Hüdepohl, Janka & Mirizzi
PRD 85:085031, 2012]

Rise time Analysis: Hierarchy Determination

Normalized Count rate :
32 different models

[C.D. Ott et al. Neutrino 2012, Japan, 1212.4250]



It would be important in future to study the robustness of the rise time signature with more and more accurate simulations.

Conclusions

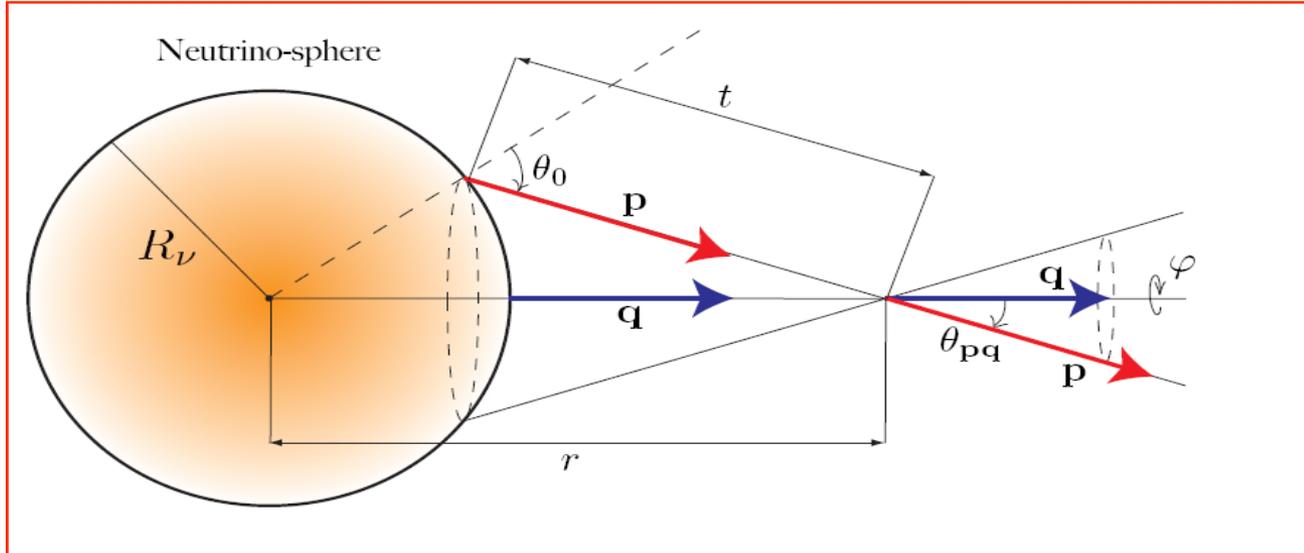
- Observing SN neutrinos is the next frontier of low-energy neutrino astronomy.
- Collective effects are suppressed in early SN phases, implying hierarchy sensitivity at large θ_{13} .
- Neutronization phase is the best phase to probe mass hierarchy.
- Earth Matter effect: Detectable for Sub-kpc SNe.
- Rise time of SNe signal contains hierarchy information.

The background of the slide is a reproduction of the painting 'The Starry Night' by Vincent van Gogh. It features a turbulent, swirling blue sky filled with bright, glowing yellow stars and a large, luminous crescent moon. In the foreground, a dark, jagged cypress tree stands on the left, and a small village with a church spire is visible in the distance under the night sky.

LOOKING FORWARD
FOR THE NEXT
GALACTIC SN !

Thank You !

Appendix: Matter Suppression



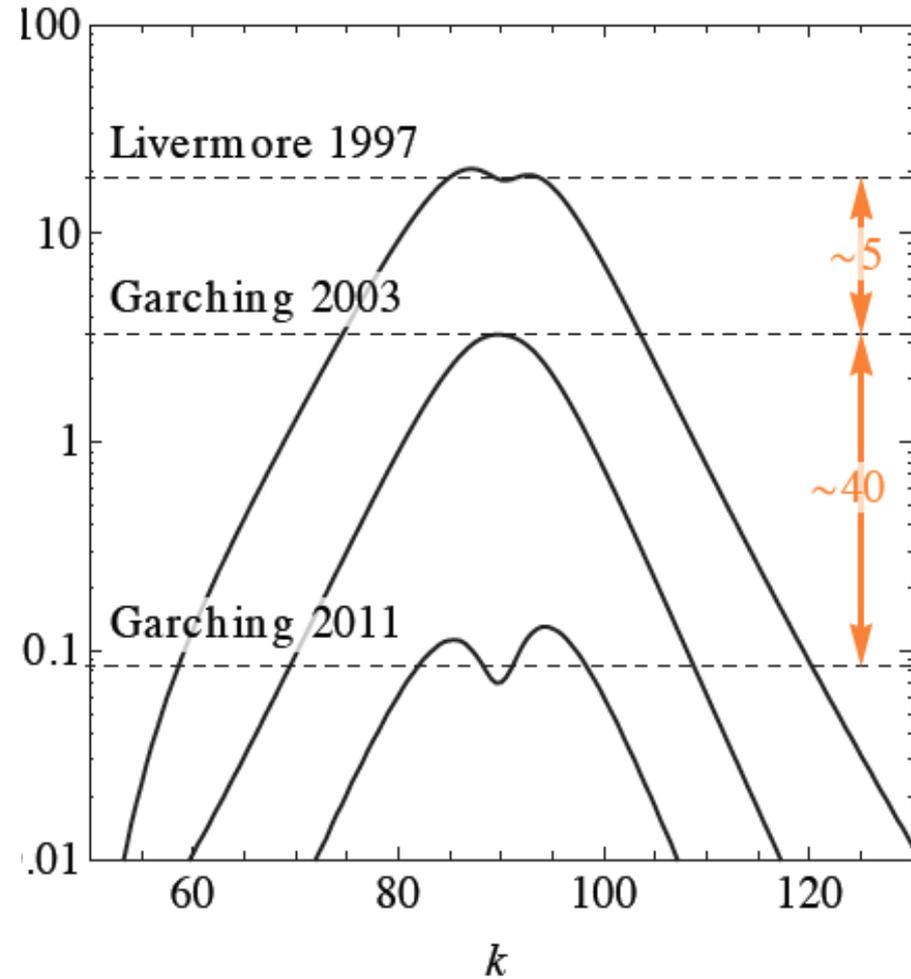
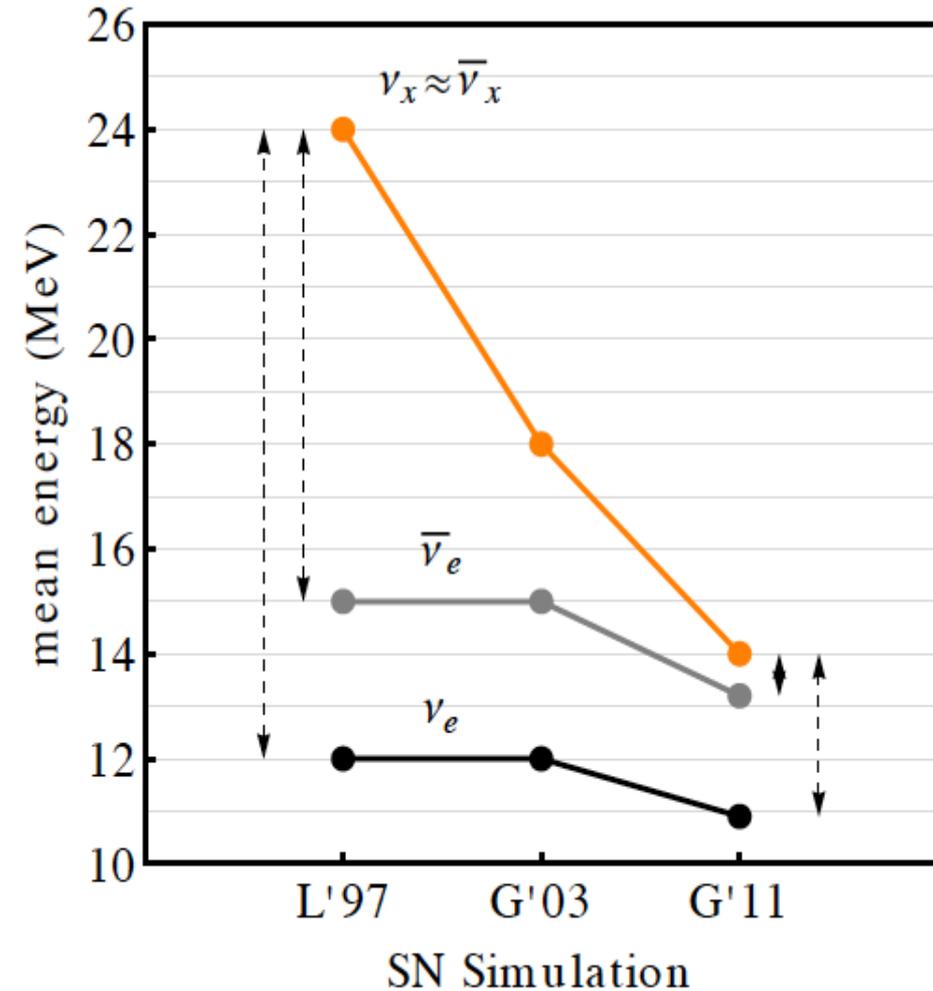
- Neutrinos emitted from spherical source, travel on different trajectories.
- Different oscillation phases for neutrinos traveling in different paths.
- Strong ν - ν interaction can overcome trajectory dependent dispersion.

Collective conversion requires : $\mathbf{n}_e \ll \mathbf{n}_\nu$

Collective conversion is matter Suppressed : $\mathbf{n}_e \gtrsim \mathbf{n}_\nu$

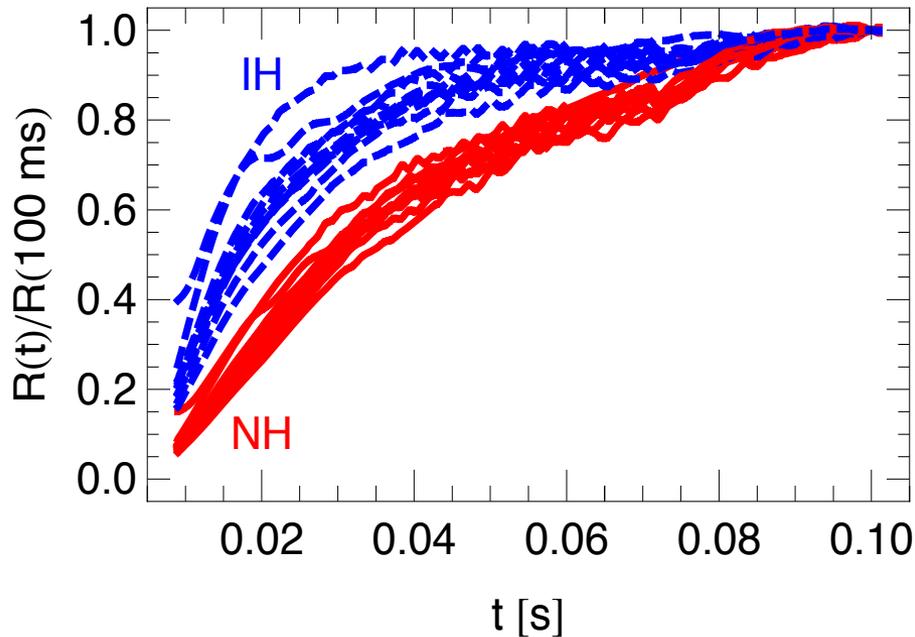
Appendix: SN antineutrino Flux at Earth

Earth Matter Effect:



[Borriello, S.C, Mirizzi, Serpico; PRD 86 (2012)]

Appendix: Rise time Analysis: Hierarchy Determination

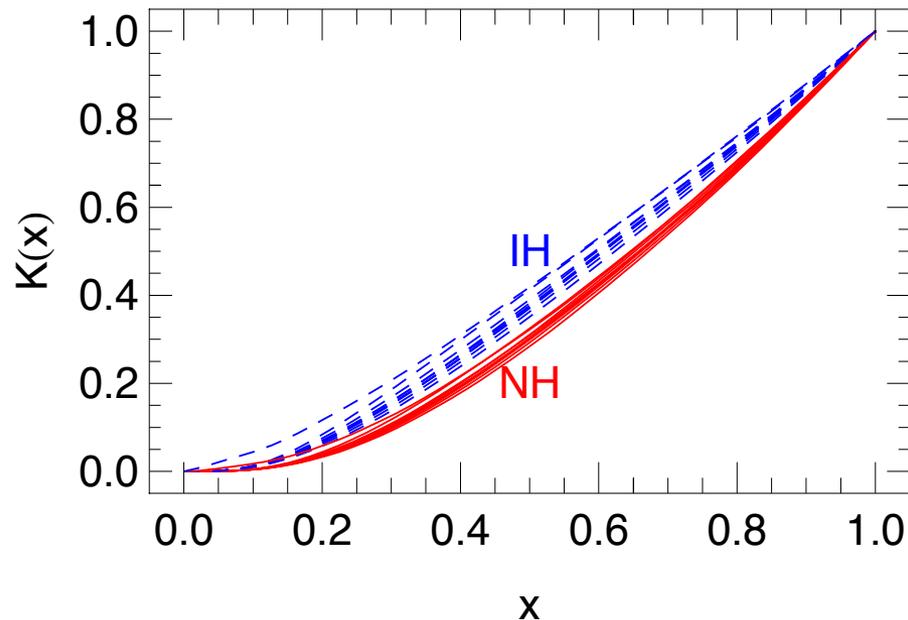


Count rate (normalized to
value at 100 ms)
10 different models, masses
12 to 40 Msun
[Blue: IH ; Red: NH]

For Statistical analysis
introduce
Cumulative Time Distribution $K(x)$

$$x = R(t)/R(t_{\text{end}})$$

$$K(x) = \frac{\int_0^x R(t) dt}{\int_0^1 R(t) dt}$$

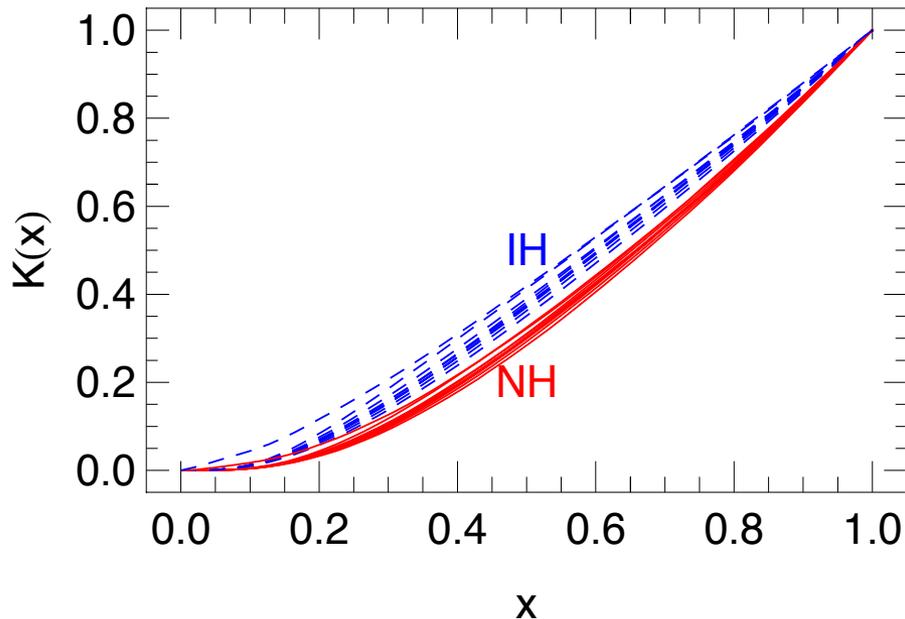
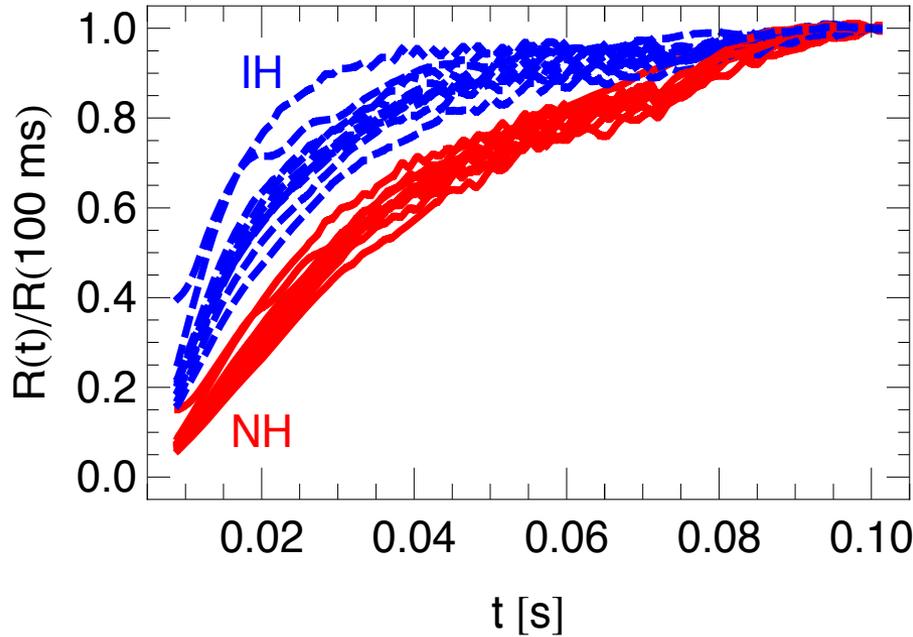


Appendix: Rise time Analysis:

Hierarchy Determination

Kolmogorov-Smirnov Statistics :

$$D_{\infty}(K_i^A, K_j^B) = \max_{x \in [0;1]} |K_i^A(x) - K_j^B(x)|$$



Distance between
any randomly picked **NH "model"**
from **average IH** one
is significantly above
the one from **average NH** ones
and well expected statistical errors.

Assessing "theory/numerical" error
requires detailed study over other
simulations with comparable
sophistication.