

# FCC-ee Beam Energy Measurement Suggestion

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# Talk outline

- Introduction: resonant depolarization
- Introduction: inverse Compton scattering
- Conventional spectrometer
- Spectrometer & laser calibration
- Discussion

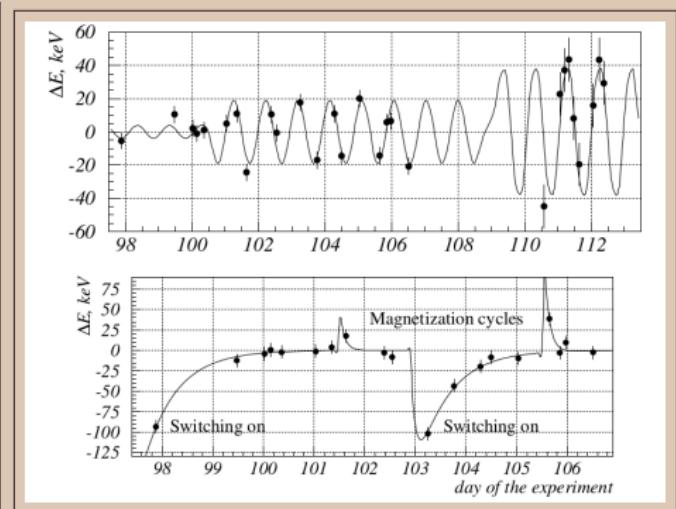
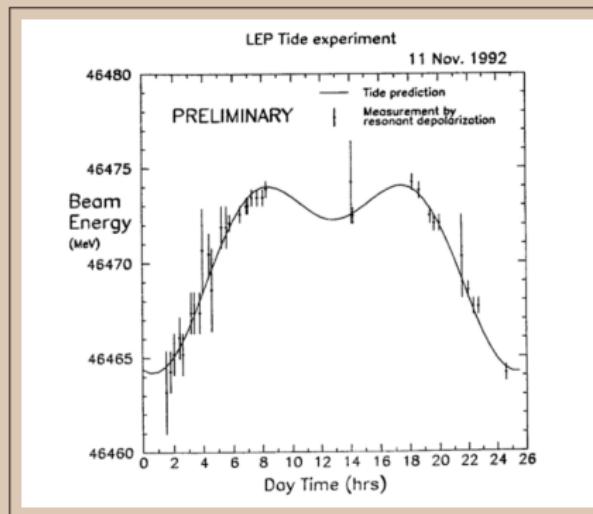
# Resonant Depolarization (RD)

The energy scale in particle physics is established due to the resonant depolarization technique on  $e^+e^-$  colliders:

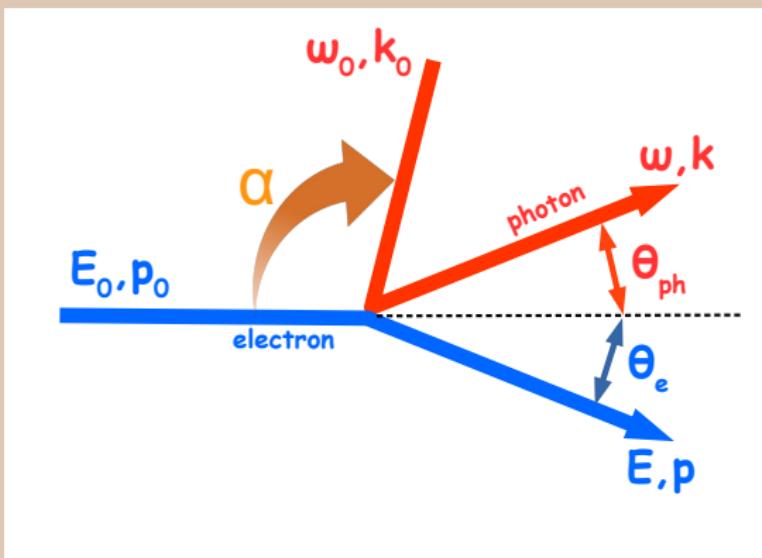
VEPP-2(M), SPEAR, DORIS, VEPP-4(M), CESR, LEP ...

RD requires: a) polarization, b) polarimeter, c) depolarizer (?)

Allows to have  $\Delta E/E \simeq 10^{-6}!$

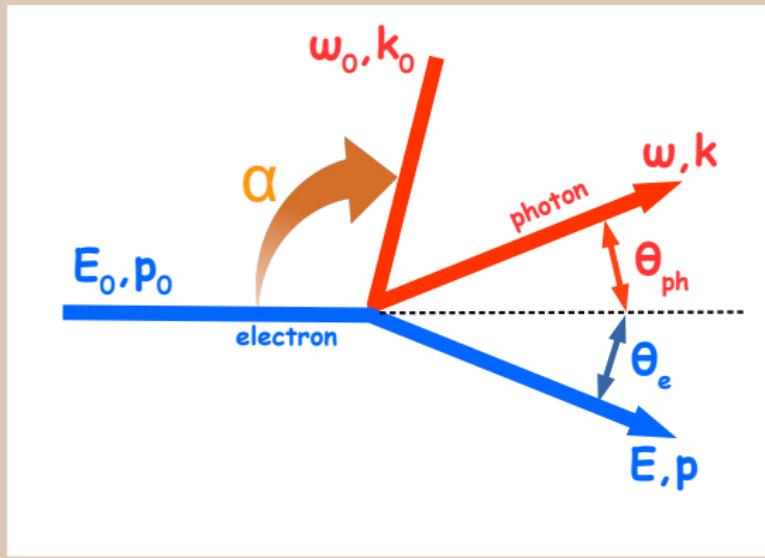


# Compton Scattering



# Coulomb Scattering

Inverse case:  $\alpha = \pi$ ,  $\theta_e = \theta_{ph} = 0$



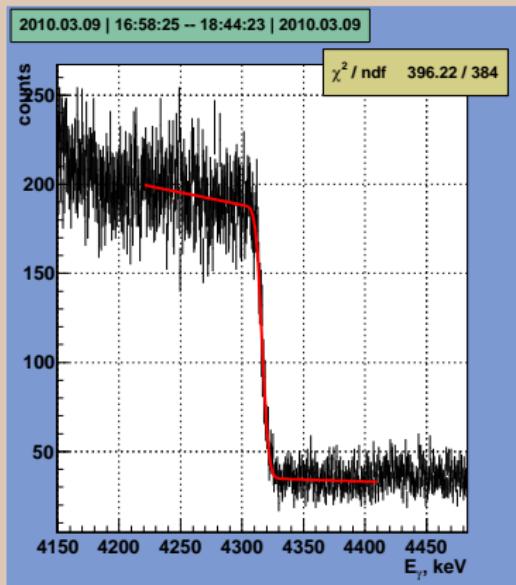
$$\boxed{\omega_{max} = E_0 \frac{\kappa}{1 + \kappa}} \quad \kappa = \frac{4\omega_0 E_0}{m^2}$$

# Laser for beam energy calibration at $e^+e^-$ colliders

VEPP-4M<sup>(2005)</sup>, BEPC-II<sup>(2010)</sup>, VEPP-2000<sup>(2012)</sup>

$$E_0 = \frac{\omega_{max}}{2} \left( 1 + \sqrt{1 + \frac{m^2}{\omega_0 \omega_{max}}} \right)$$

$$\frac{\Delta E_0}{E_0} \gtrsim 3 \times 10^{-5} \text{ for } E_0 < 2 \text{ GeV}$$



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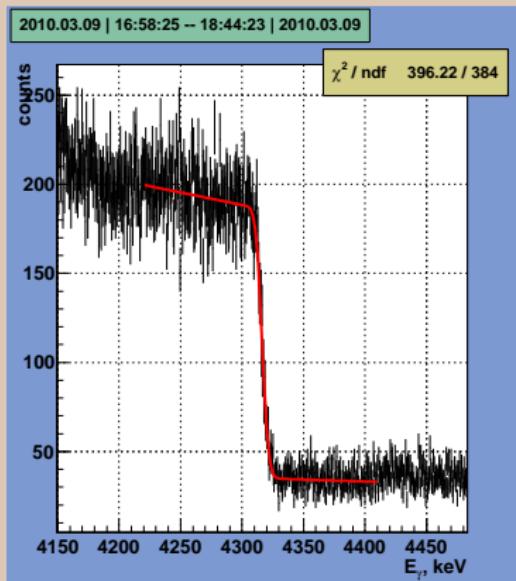
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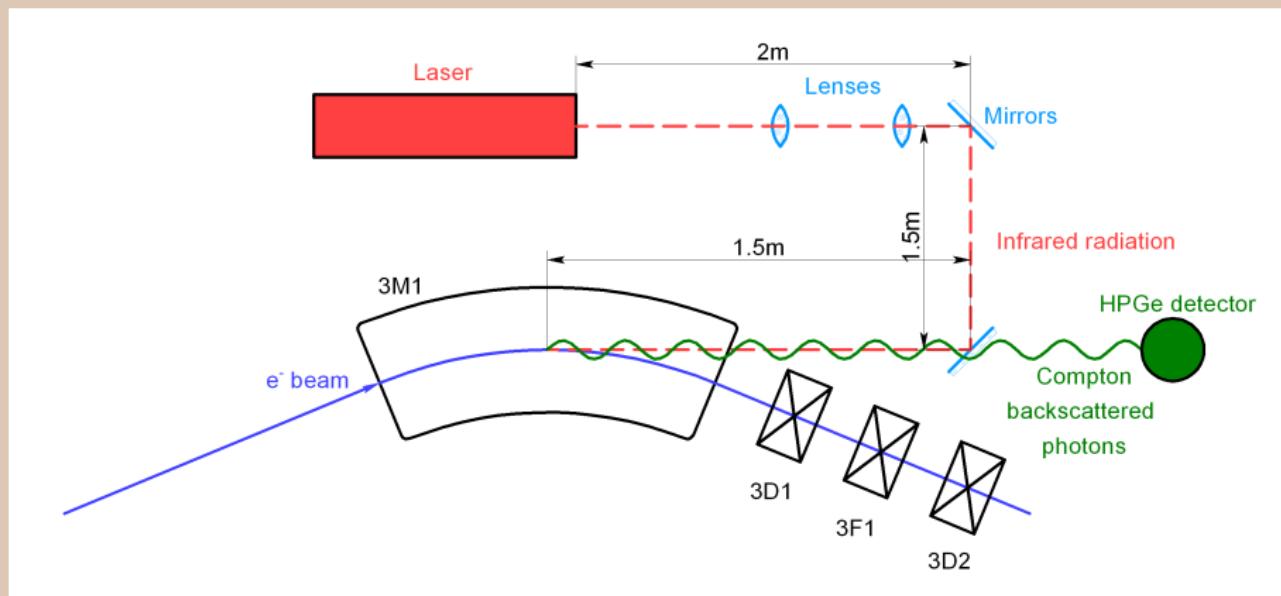
BES-III Collaboration

$$m_\tau = (1776.91 \pm 0.12^{+0.10}_{-0.13}) \text{ MeV}/c^2$$

Phys. Rev. D90 (2014) 012001

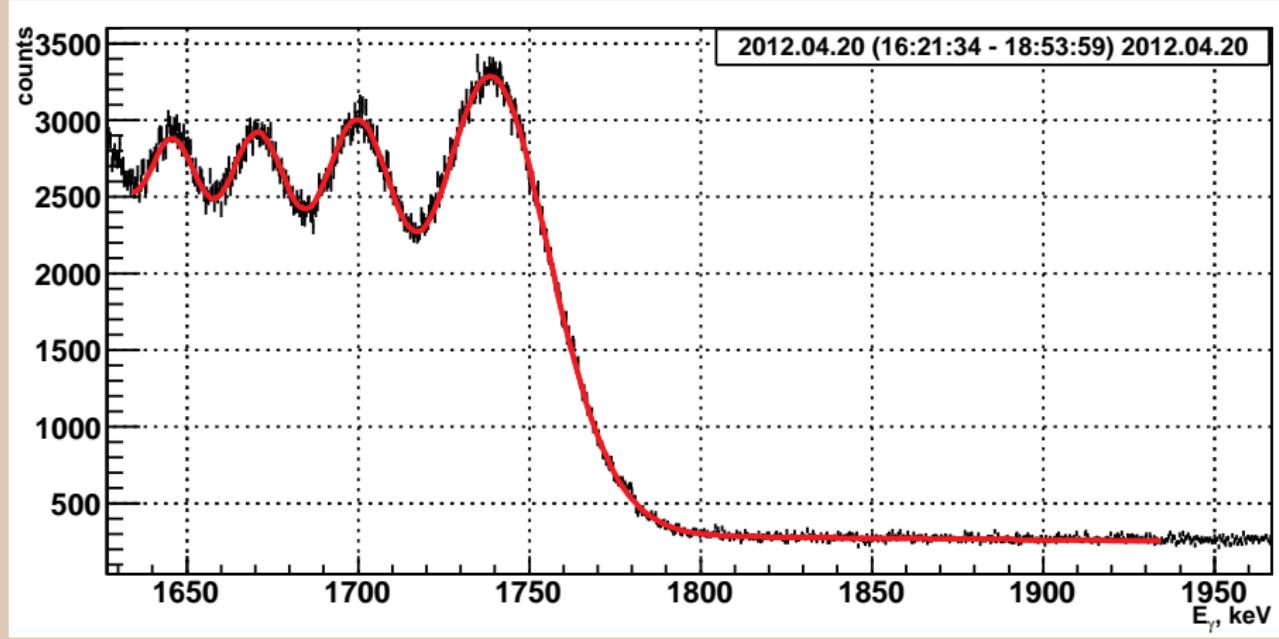


# VEPP-2000

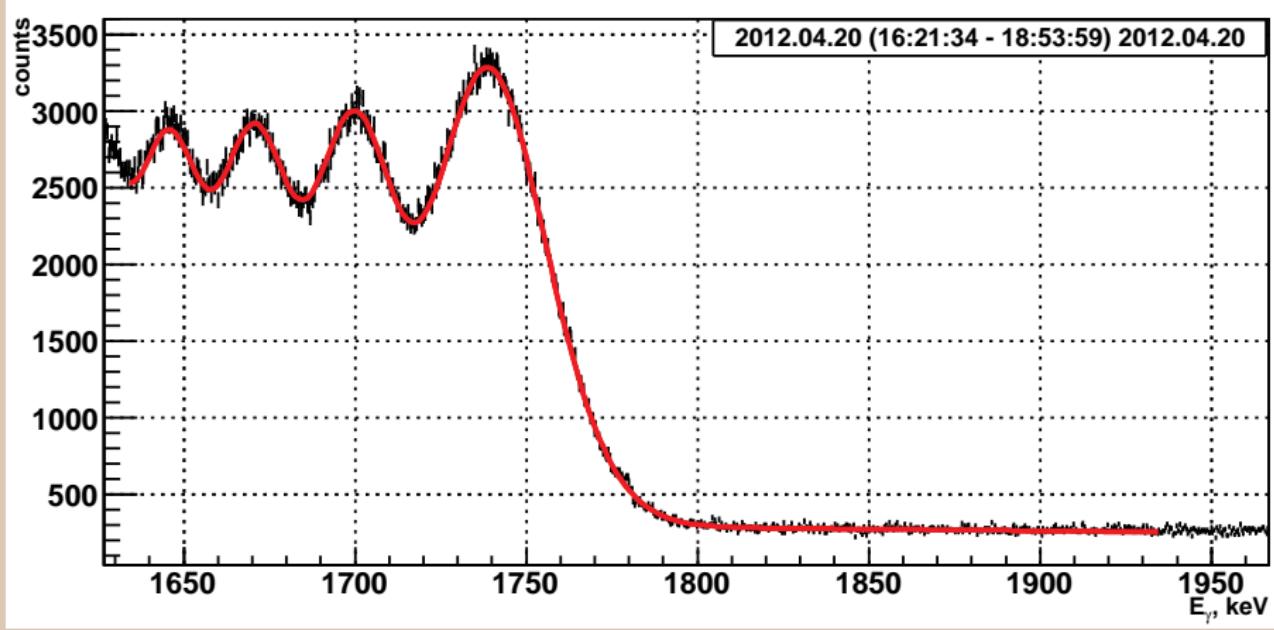


Beam orbit radius in the VEPP-2000 dipole  $R = 140$  cm

# VEPP-2000 puzzle



# VEPP-2000 puzzle

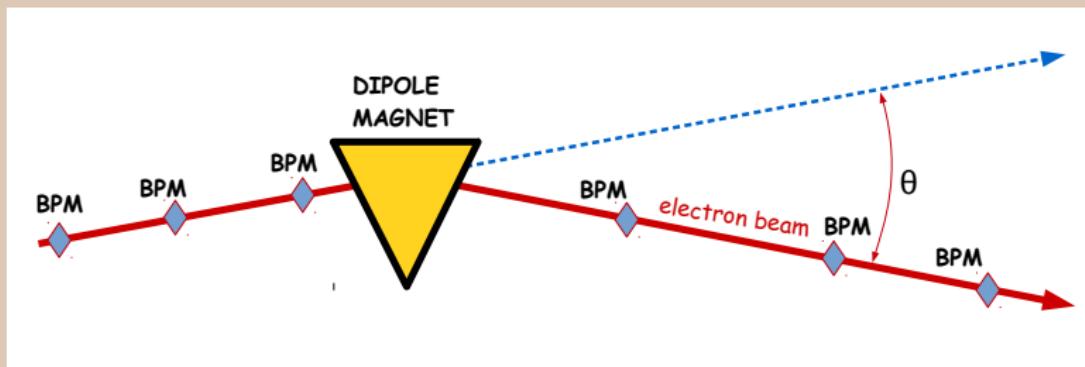


$\chi^2/NDF = 773/745$ , Prob. = 0.23,  
 $E = 993.662 \pm 0.016$  MeV,  $B = 2.388 \pm 0.004$  T,  $\sigma = 810 \pm 40$  ppm.

Phys. Rev. Lett. 110 (2013) 140402

# Conventional spectrometer

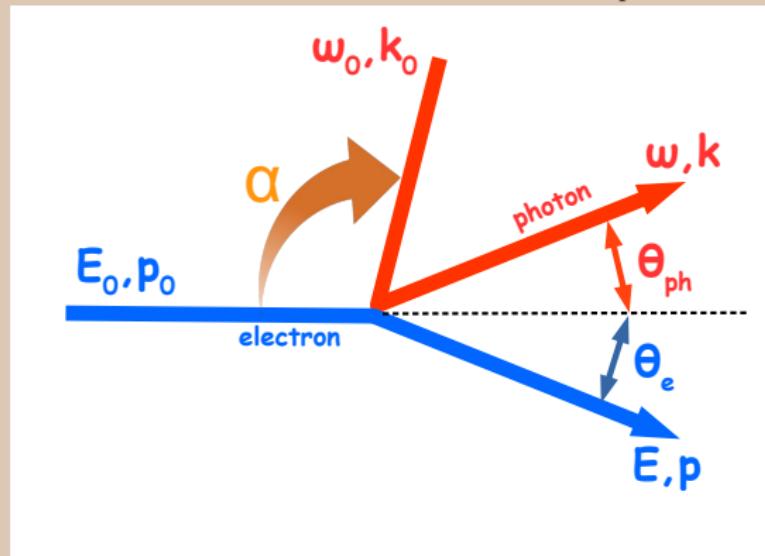
One of the complementary approaches for the beam energy determination at LEP – high energy runs.



Access to the beam energy:  $E_0 = \frac{c \int B ds}{\theta}$

# Coulomb Scattering

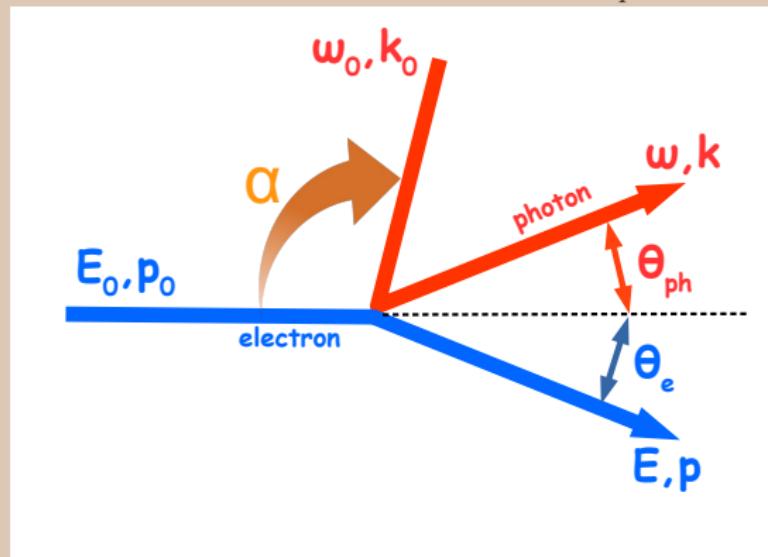
$$E_0 \gg m \gg \omega_0, \alpha = \pi, \theta_e = \theta_{ph} = 0$$



$$\boxed{\omega_{max} = E_0 \frac{\kappa}{1 + \kappa}} \quad \kappa = \frac{4\omega_0 E_0}{m^2}$$

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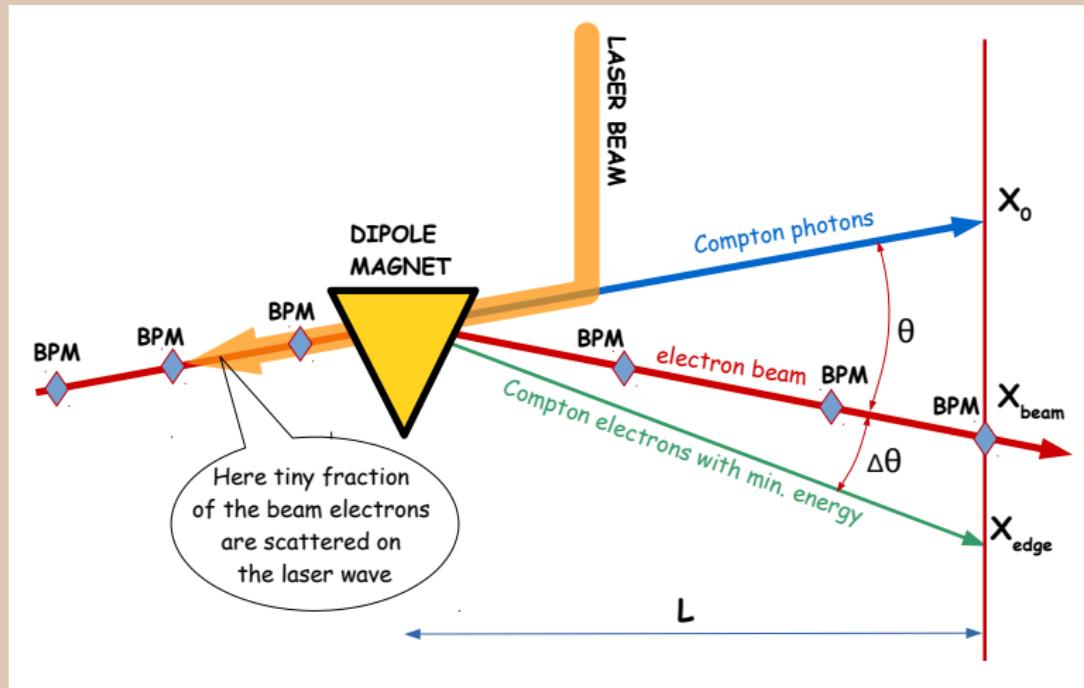


$$\omega_{max} = E_0 \frac{\kappa}{1 + \kappa}$$

$$\kappa = \frac{4\omega_0 E_0}{m^2}$$

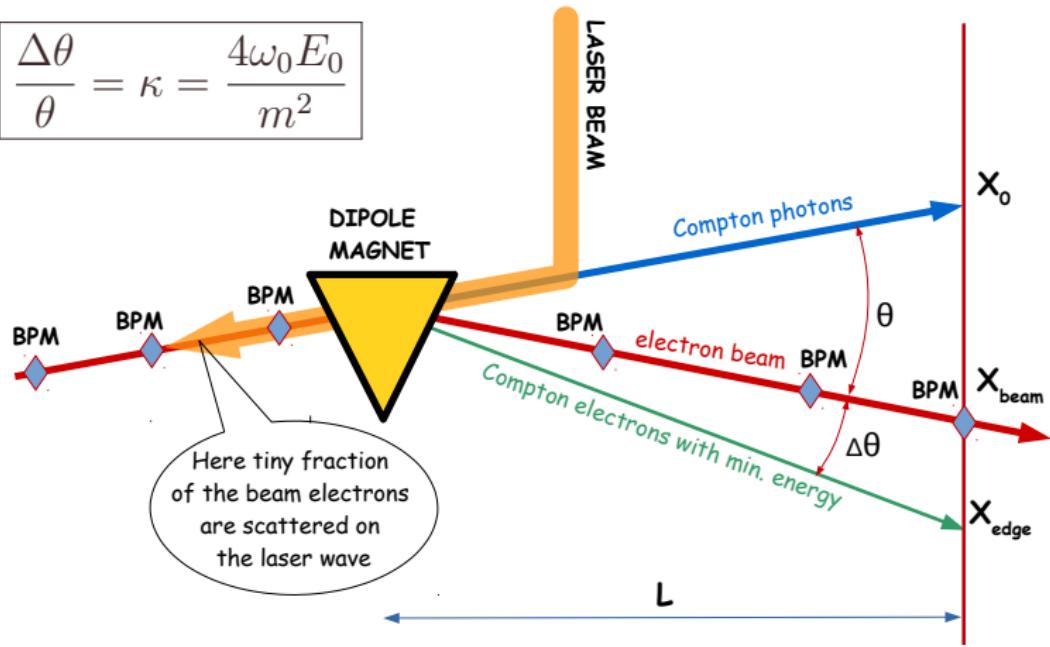
$$E_{min} = E_0 - \omega_{max} = E_0 \frac{1}{1 + \kappa}$$

# Spectrometer with laser calibration (suggestion)



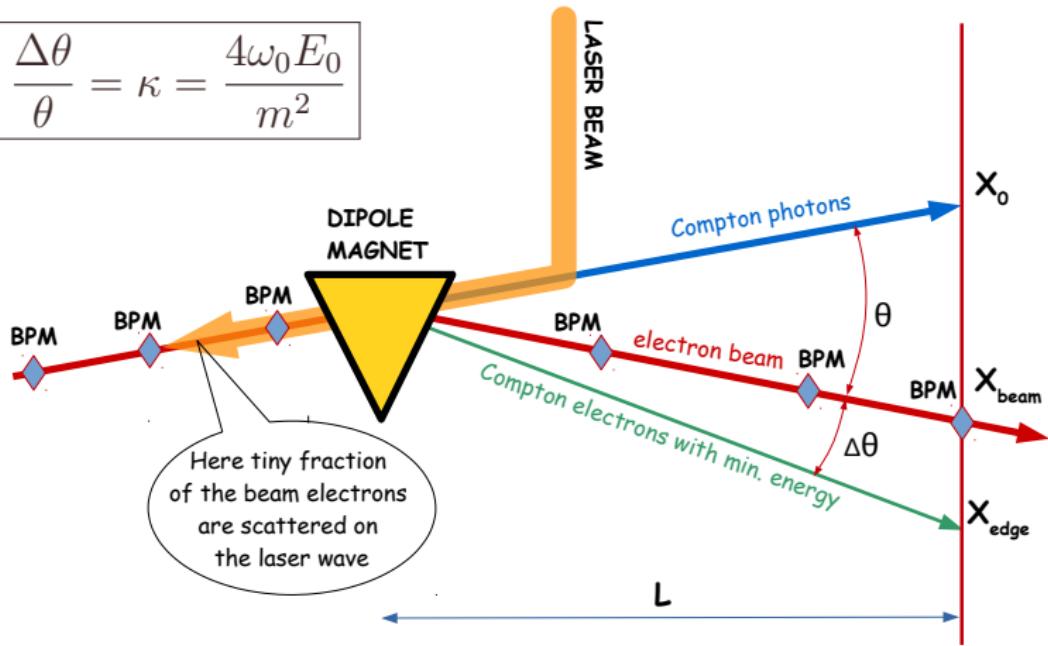
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$$\frac{\Delta\theta}{\theta} = \kappa = \frac{4\omega_0 E_0}{m^2}$$



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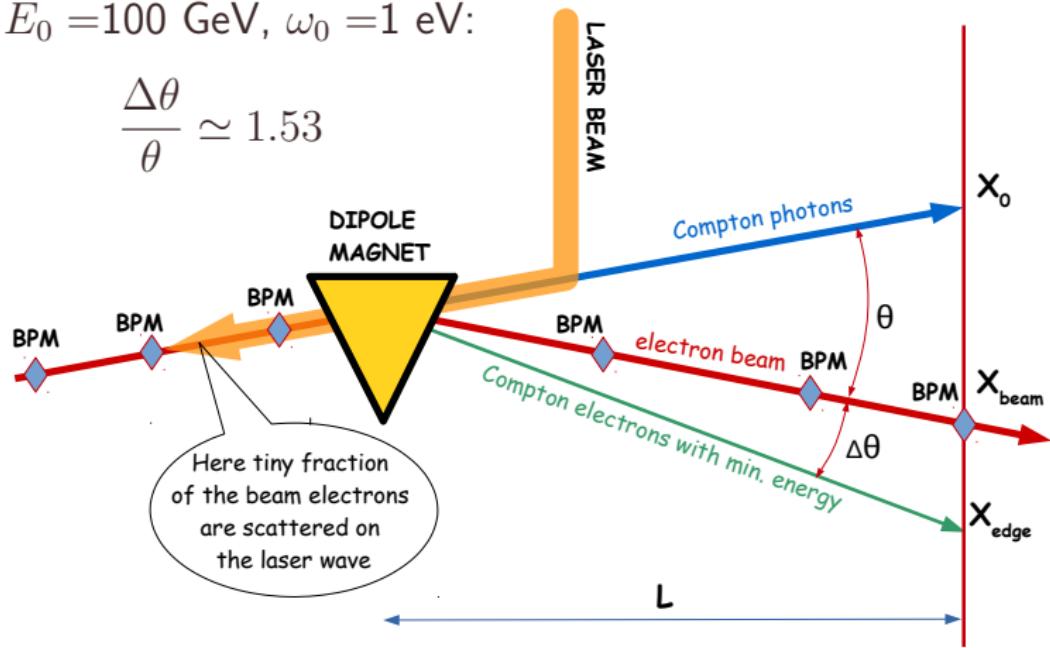


$$\text{Access to the beam energy: } E_0 = \frac{\Delta\theta}{\theta} \times \frac{m^2}{4\omega_0}$$

# Spectrometer with laser calibration (suggestion)

$$E_0 = 100 \text{ GeV}, \omega_0 = 1 \text{ eV}:$$

$$\frac{\Delta\theta}{\theta} \simeq 1.53$$



$$\text{Access to the beam energy: } E_0 = \frac{\Delta\theta}{\theta} \times \frac{m^2}{4\omega_0}$$

# Rough accuracy estimation

- Assume  $10 \mu\text{m}$  accuracy for  $[X_{beam} - X_0]$  and  $[X_{edge} - X_{beam}]$ .
- For  $\Delta E/E \simeq 10^{-5}$ :  $[X_{beam} - X_0] \simeq [X_{edge} - X_{beam}] \simeq 1 \text{ m}$ .
- For example, this is  $\theta \simeq 10 \text{ mrad}$  and  $L \simeq 100 \text{ m}$ .

# Discussion: the weaknesses of suggestion

- it is necessary to ensure equality of integrals of magnetic field for electrons with very different energies;
- the installation dimensions seems to be larger than one would like to have;
- three different types of coordinate detectors must work together to measure distances with high precision in absolute units.

# Discussion: the strengths of suggestion

- it aims to measure the absolute energy of the electron beam and does not require measurement of bending field in absolute scale;
- backscattering of laser radiation is a proven tool for beam energy calibration at low energy machines;
- looks tempting the possibility to measure energy and polarization of the beam by the same apparatus;
- use of different laser wavelengths will definitely help to control some of possible systematic uncertainties;
- conventional spectrometer remains in service and provides *independent information* about the beam energy;
- the calibration procedure for coordinate-sensitive detectors does not directly depend on particles energies.

# Acknowledgement

Thank you for your attention!