

Molecular Interpretation of $D_{s0}^*(2317)$ and $D_{s1}(2460)$

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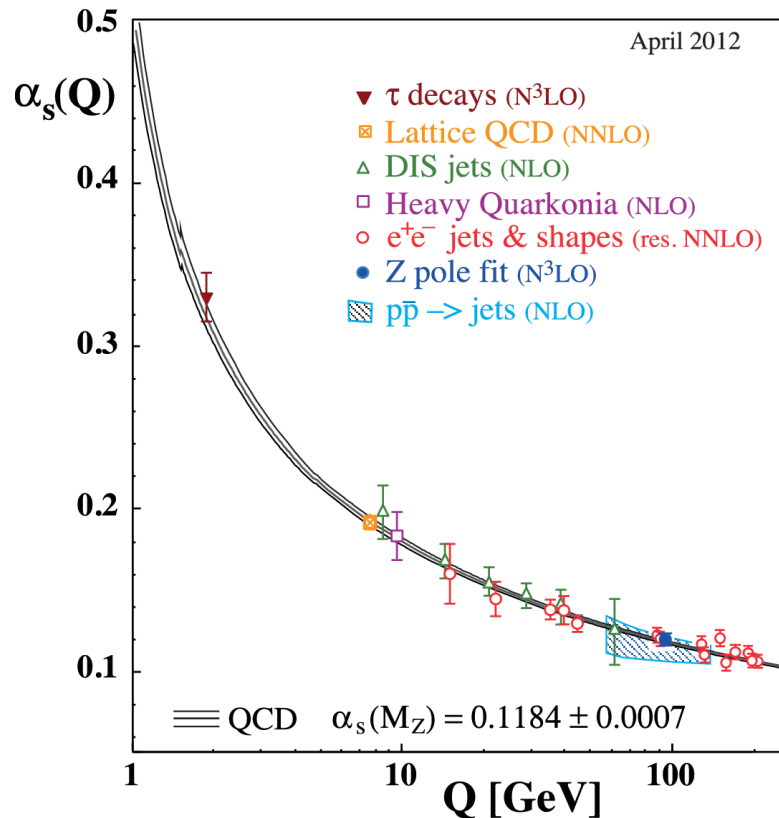
In Collaboration with
F.-K. Guo, H. Griebhammer, C. Hanhart, U.-G. Meißner



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Quantum Chromodynamics (QCD):



- **High Energies:**
Asymptotic Freedom, perturbation theory
- **Low Energies:**
Lattice, Effective Field Theories

Heavy Meson Chiral Perturbation Theory

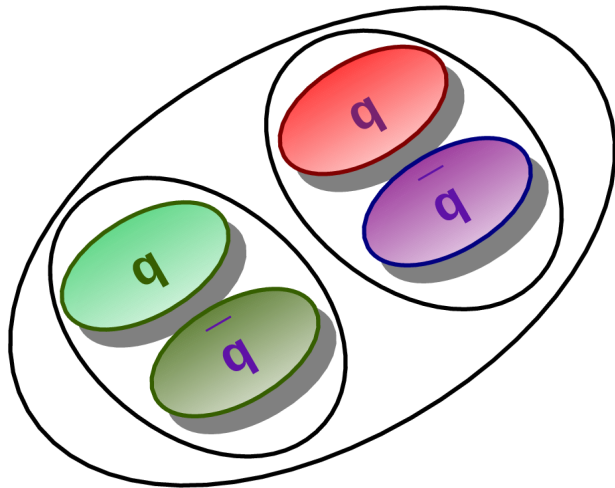
- No quarks and gluons
- **Mesons** as effective d.o.f.: $\pi, K, D^{(*)}, B^{(*)}, \dots$
- Incorporates Chiral & Heavy Quark Symmetry

Confinement:

Only **color-neutral objects**
can be observed

Classic Examples \longrightarrow

- Mesons: $q\bar{q}$
- Baryons: qqq



- Formed from **interactions** of
- **two or more hadrons**
- Classic example: **Deuteron** as **Proton-Neutron** bound state
- Large number of **new candidates** in the previous decade

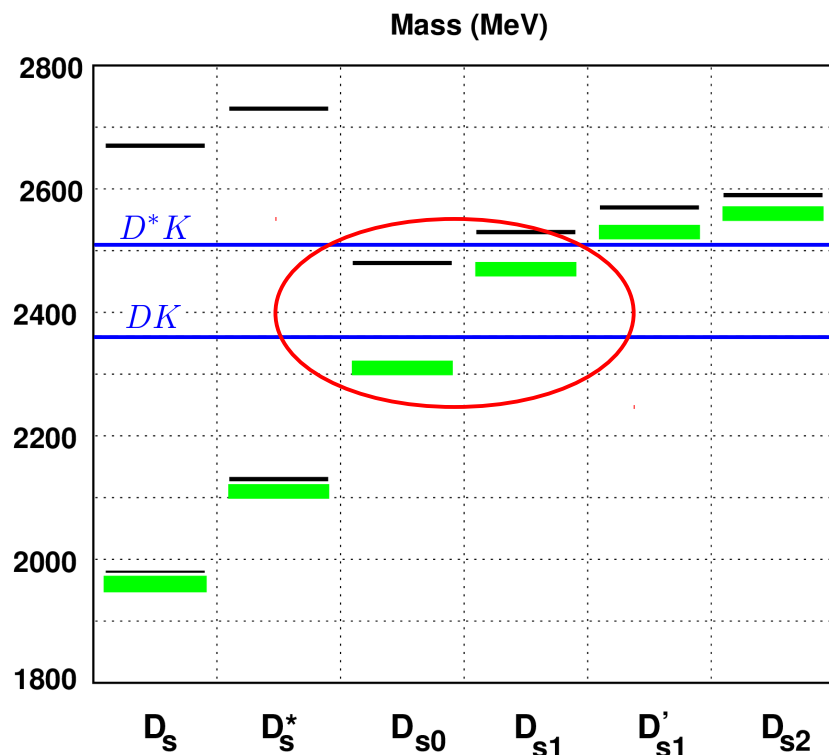
Weinberg's Formula:

Probability λ to find the **physical state** in the **two-hadron state** related to **coupling to constituents** g

$$g^2 = 16 \pi \lambda^2 \frac{(m_1 + m_2)^2}{\mu} \sqrt{-2\mu (M - m_1 - m_2)}$$

$D_{s0}^*(2317)$ and $D_{s1}(2460)$: Experimental Facts

E. Swanson: Physics Reports 429 (2006) 243 – 305}



Experimental Facts

- Discovery by BaBar and Cleo-c in 2003
- Narrow resonances in $D_s^{(*)}\pi$
- $m_{D_{s1}} - m_{D_{s0}^*} \simeq m_{D^*} - m_D$
- Quantum numbers: $I=0$, $J^P = 0^+(1^+)$
→ match S-wave $D^{(*)}K$ pairs

Candidates for DK and D^*K molecules!

But: These features can be incorporated in Quark Model

→ Find Quantities that are sensitive to the (molecular) nature!

- Light Quark Mass Dependence of Binding Energy → Lattice
- Radiative & Hadronic Decay Widths

$D_{s0}^*(2317)$ and $D_{s1}(2460)$: Dynamical Generation

MC, F.-K. Guo, H. Griebhammer, C. Hanhart and U.-G. Meißner, Eur. Phys. J. A50 (2014) 9, 149

$$T = V + VGV + VGVGV + \dots$$

Lippmann Schwinger Eq.:

$$\Rightarrow T = V [1 - GV]^{-1}$$

- Coupled Channels with $I=0$ and $S=1$:

$$V(s) = \begin{pmatrix} V_{DK \rightarrow DK}(s) & V_{DK \rightarrow D_s \eta}(s) \\ V_{D_s \eta K \rightarrow DK}(s) & V_{D_s \eta \rightarrow D_s \eta}(s) \end{pmatrix} \quad G(s) = \begin{pmatrix} G_{DK}(s) & 0 \\ 0 & G_{D_s \eta}(s) \end{pmatrix}$$

- Full LO and NLO Lagrangian for Heavy-Light scattering, LECs from Lattice

- Fix Subtraction Constant to mass of $D_{s0}^*(2317)$

$$\begin{aligned} m_{D_{s0}^*} &= 2317 \text{ MeV} & m_{D_{s1}} &= (2457.8 \pm 6.7) \text{ MeV} \\ m_{D_{s0}^*}^{Exp} &= (2317.8 \pm 0.6) \text{ MeV} & m_{D_{s1}}^{Exp} &= (2459.5 \pm 0.6) \text{ MeV} \end{aligned}$$

- Extract Coupling

$$g_{DK} = (9.0 \pm 0.5) \text{ GeV}$$

$$g_{D^*K} = (10.0 \pm 0.3) \text{ GeV}$$

Weinberg: Molecular Component

$$P(DK, D_{s0}) = (77.8 \pm 4.3) \quad P(D^*, D_{s1}) = (81.0 \pm 3.6)$$

Backed by Lattice Calculation,
See Yesterday's Talk by Eulogio Oset!

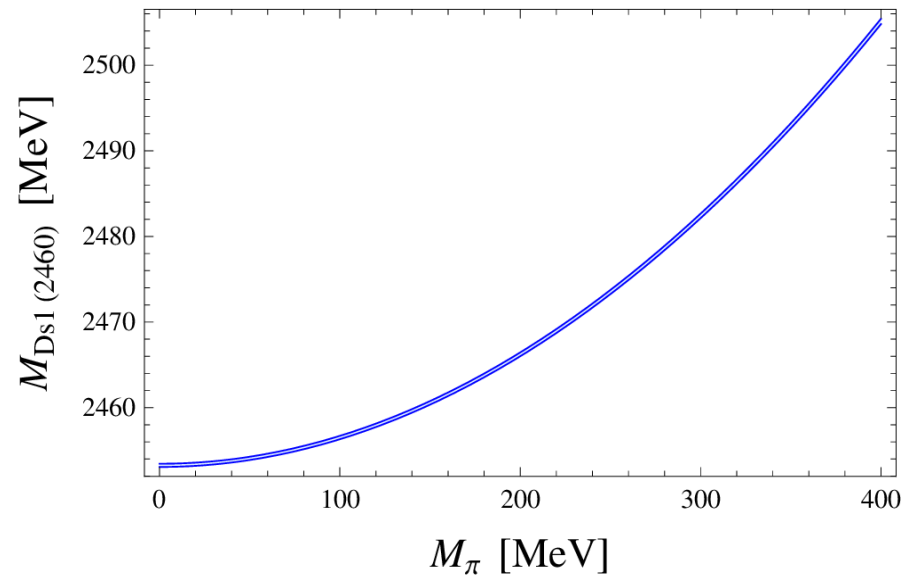
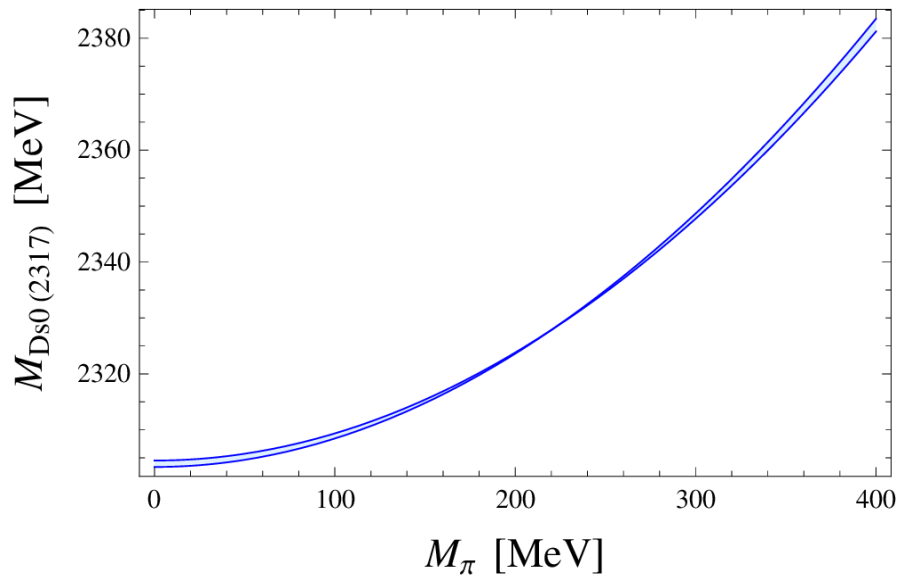
$$P(DK, D_{s0}) = (72 \pm 12)$$

$$P(D^*K, D_{s1}) = (63 \pm 16)$$

A. M. Torres, E. Oset, S. Prelovsek and A. Ramos, arXiv:1412.1706 [hep-lat]

$D_{s0}^*(2317)$ and $D_{s1}(2460)$: Pion Mass Dependence

MC, F.-K. Guo, C. Hanhart and U.-G. Meißner, Eur. Phys. J. A 47 (2011) 19



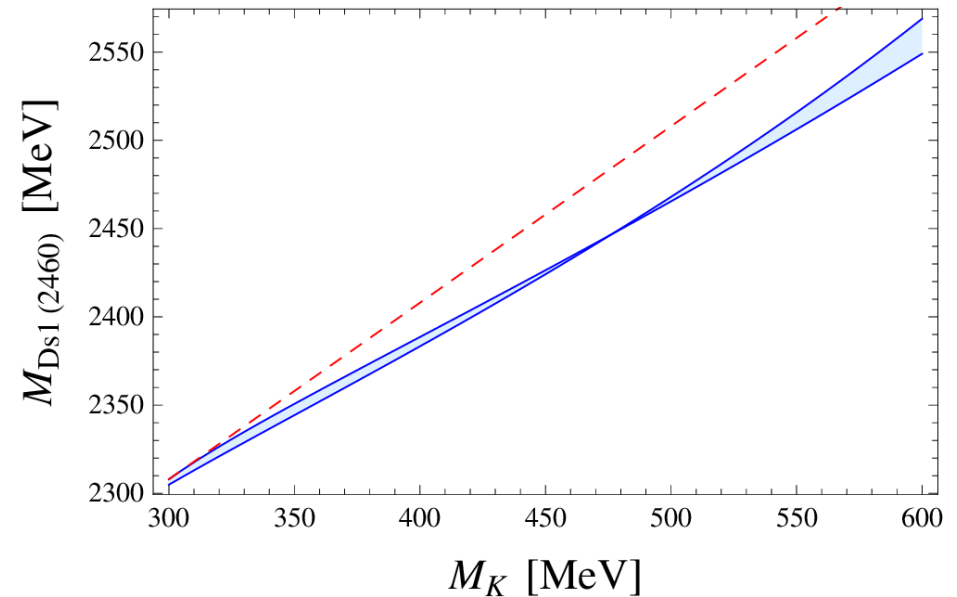
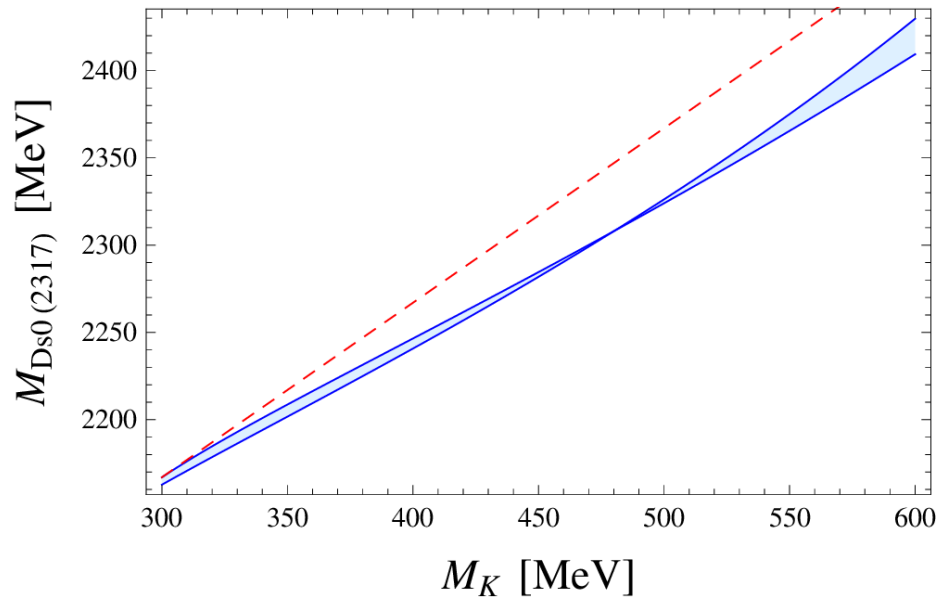
- Pion Mass Dependence enters via DK Loops in both cases, but Weinberg's Formula:
 - Pure $c\bar{s}$ state: g_{DK} small \leftrightarrow weak pion mass dependence
 - Molecule $(c\bar{q})(q\bar{s})$: g_{DK} maximal \leftrightarrow strong pion mass dependence

Interpretation backed by Lattice Calculation

D. Mohler, C. B. Lang, L. Leskovec, S. Prelovsek and R. M. Woloshyn, Phys. Rev. Lett. **111**, 222001 (2013)

$D_{s0}^*(2317)$ and $D_{s1}(2460)$: Kaon Mass Dependence

MC, F.-K. Guo, C. Hanhart and U.-G. Meißner, Eur. Phys. J. A 47 (2011) 19



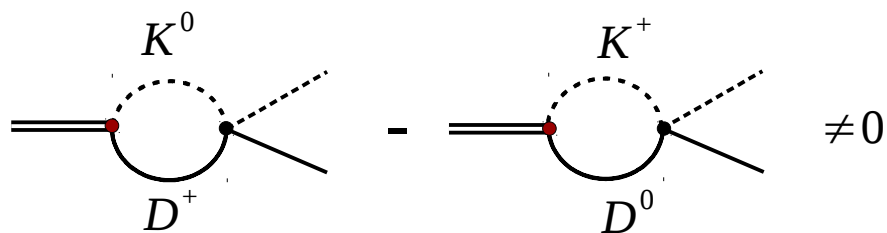
- Bound State of D and K: $M = M_D + M_K - \varepsilon$
 - Kaon mass dependence **linear, slope unity**
- Compact State ($c\bar{s}$): Compare Kaon ($q\bar{s}$)
 - Kaon mass dependence **quadratic**

$D_{s0}^*(2317)$ and $D_{s1}(2460)$: Hadronic Decays

L. Liu, K. Orginos, F.-K. Guo, C. Hanhart and U.-G. Meißner, Phys. Rev. D **87** (2013) 014508

Two contributions shift the stable poles on the complex planes to the second Riemann sheet: $s = M + i\Gamma/2$

- Particle Masses Charged/Neutral

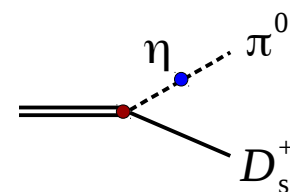


$$m_{K^0} - m_{K^+} = 3.9 \text{ MeV}$$

$$m_{D^+} - m_{D^0} = 4.8 \text{ MeV}$$

$$m_{D^{*+}} - m_{D^{*0}} = 3.3 \text{ MeV}$$

- π - η mixing



$$\begin{pmatrix} \tilde{\pi}^0 \\ \tilde{\eta} \end{pmatrix} = \begin{pmatrix} \cos \epsilon_{\pi^0 \eta} & \sin \epsilon_{\pi^0 \eta} \\ -\sin \epsilon_{\pi^0 \eta} & \cos \epsilon_{\pi^0 \eta} \end{pmatrix} \begin{pmatrix} \pi^0 \\ \eta \end{pmatrix}$$

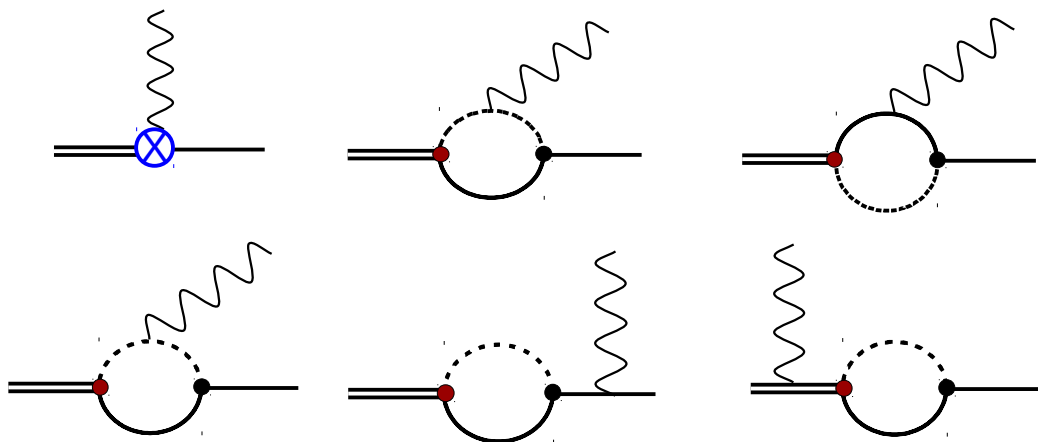
$$\epsilon_{\pi^0 \eta} = \frac{1}{2} \arctan \left(\frac{\sqrt{3} m_d - m_u}{2 m_s - \hat{m}} \right) \sim 0.01$$

$$\Gamma(\rightarrow D_s^* \pi^0) = (133 \pm 22) \quad \Gamma(\rightarrow D_s^* \pi^0) = (66 \pm 22)$$

1-2 Orders of magnitude larger than for $c \bar{s}$ mesons!

$D_{s0}^*(2317)$ and $D_{s1}(2460)$: Radiative Decays

MC, F.-K. Guo, H. Griebhammer, C. Hanhart and U.-G. Meißner, Eur. Phys. J. A50 (2014) 9, 149



- Coupling from Residues
- Sum of all Loops is finite
- Contact Term fixed in $D_{s1} \rightarrow D_s \gamma$
- Power Counting: **Contact Term and Loop at same order**
→ **Not dominated by loops**

$$\Gamma(D_{s0}^* \rightarrow D_s^* \gamma) = (10.1 \pm 4.5) \text{ keV}$$

$$\Gamma(D_{s1} \rightarrow D_s \gamma) = (26.2 \pm 12.4) \text{ keV}$$

$$\Gamma(D_{s1} \rightarrow D_s^* \gamma) = (26.5 \pm 11.0) \text{ keV}$$

$$\Gamma(D_{s1} \rightarrow D_{s0}^* \gamma) = (1.3 \pm 0.5) \text{ keV}$$

- Results for ratios Radiative/Hadronic Decays compatible with experiment
- Equal contributions for contact term and loops
→ only loops sensitive to molecular nature
- Values too small even for FAIR

Heavy Quark Flavor Symmetry
relates charm and bottom sector! \rightarrow Predictions for
 BK and B^*K possible

$$m_{B_{s0}} = (5663 \pm 48) \text{ MeV} \quad m_{B_{s1}} = (5712 \pm 48) \text{ MeV}$$

Smaller Degeneracy between
charged and neutral bottom mesons
 \rightarrow small hadronic width expected:

$$B_{s0} \rightarrow B_s \pi^0 = (0.8 \pm 0.8) \text{ keV}$$
$$B_{s1} \rightarrow B_s^* \pi^0 = (1.8 \pm 1.8) \text{ keV}$$

Radiative Decays more promising discovery channel:

$$B_{s0} \rightarrow B_s^* \gamma = (32.6 \pm 20.8) \text{ keV} \quad B_{s1} \rightarrow B_s \gamma = (4.1 \pm 10.9) \text{ keV}$$
$$B_{s1} \rightarrow B_s^* \gamma = (46.9 \pm 33.6) \text{ keV} \quad B_{s1} \rightarrow B_{s0} \gamma = (0.02 \pm 0.02) \text{ keV}$$

- Interpretation of $D_{s0}(2317)$ and $D_{s1}(2460)$ as $D^{(*)}K$ molecules
 - Explains features that Quark model cannot
- Light Meson Mass Dependence of Binding Energy:
Linear in m_K , Quadratic in m_π → Lattice
- Two-Body Decays:
 - Hadronic Decays $\sim O(100 \text{ keV})$
 - Radiative Decays $\sim O(10 \text{ keV})$
 - Hadronic Decay Widths distinctive in mol. Picture
- Prediction: Partner States in Open Bottom Sector
Best chance for Discovery: Radiative Decays $B_s^{(*)} \gamma$

谢谢！