



**Circular Electron Positron Collider**

# **SRF Cavity Design for CEPC PDR Scheme**

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2016.04.08

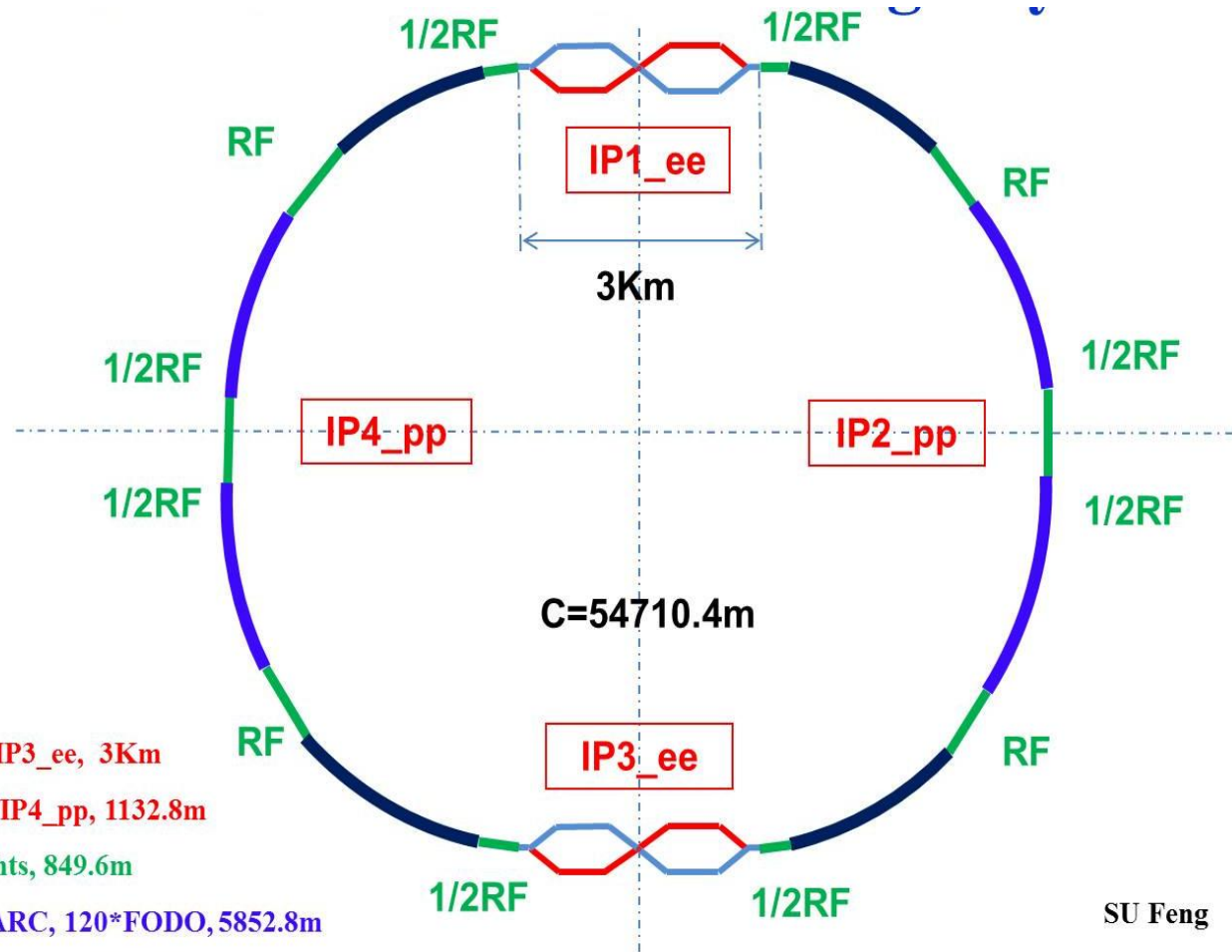


# Outline

- Cavity design
  - Cell number
  - Cavity type
- HOM power analysis for multiple time-structure
- Multi-bunch instability caused by RF cavity
- Summary



# CEPC PDR scheme



IP1\_ee/IP3\_ee, 3Km

IP2\_pp/IP4\_pp, 1132.8m

4 Straights, 849.6m

4 Long ARC, 120\*FODO, 5852.8m

4 Short ARC, 100\*FODO, 4908.8m

SU Feng

2015.10.12

# Beam parameters

(wangdou20160219)

	<i>Pre-CDR</i>	<i>H-high lumi.</i>		<i>H-low power</i>		<i>Z</i>
Number of IPs	2	2		2		2
Energy (GeV)	120	120		120		45.5
Circumference (km)	54	54		54		54
SR loss/turn (GeV)	3.1	2.96		2.96		0.062
Half crossing angle (mrad)	0	14.5	<b>15</b>	11.5	<b>15</b>	<b>15</b>
Piwinski angle	0	2	<b>2.5</b>	2	<b>2.6</b>	<b>8.5</b>
$N_p$ /bunch ( $10^{11}$ )	3.79	3.79	<b>2.85</b>	2.81	<b>2.67</b>	<b>0.46</b>
Bunch number	<b>50</b>	<b>50</b>	<b>50</b>	<b>40</b>	<b>44</b>	<b>1100</b>
Beam current (mA)	16.6	16.9	<b>16.9</b>	10.1	<b>10.5</b>	<b>45.4</b>
SR power /beam (MW)	<b>51.7</b>	<b>50</b>	<b>50</b>	<b>30</b>	<b>31.2</b>	<b>2.8</b>
Bending radius (km)	6.1	6.2	<b>6.2</b>	6.2	<b>6.2</b>	<b>6.1</b>
Momentum compaction ( $10^{-5}$ )	3.4	3.0	<b>2.5</b>	2.6	<b>2.2</b>	<b>3.5</b>
$\beta_{IP}$ x/y (m)	0.8/0.0012	0.306/0.0012	<b>0.25/0.00136</b>	0.22/0.001	<b>0.268</b> <b>/0.00124</b>	<b>0.08/0.001</b>
Emittance x/y (nm)	6.12/0.018	3.34/0.01	<b>2.45/0.0074</b>	2.67/0.008	<b>2.06 /0.0062</b>	<b>0.62/0.002</b>
Transverse $\sigma_{IP}$ (um)	69.97/0.15	32/0.11	<b>24.8/0.1</b>	24.3/0.09	<b>23.5/0.088</b>	<b>7/0.046</b>
$\xi_x$ /IP	0.118	0.04	<b>0.03</b>	0.04	<b>0.032</b>	<b>0.005</b>
$\xi_y$ /IP	0.083	0.11	<b>0.11</b>	0.11	<b>0.11</b>	<b>0.084</b>
$V_{RF}$ (GV)	<b>6.87</b>	<b>3.7</b>	<b>3.62</b>	<b>3.6</b>	<b>3.53</b>	<b>0.12</b>
$f_{RF}$ (MHz)	650	650	<b>650</b>	650	<b>650</b>	<b>650</b>
Nature $\sigma_z$ (mm)	2.14	<b>3.3</b>	<b>3.1</b>	<b>3.2</b>	<b>3.0</b>	<b>3.9</b>
Total $\sigma_z$ (mm)	<b>2.65</b>	<b>4.4</b>	<b>4.1</b>	<b>4.2</b>	<b>4.0</b>	<b>4.0</b>
HOM power/cavity (kw)	3.6	3.3	<b>2.2</b>	1.5	<b>1.3</b>	<b>0.99</b>
Energy spread (%)	0.13	0.13	<b>0.13</b>	0.13	<b>0.13</b>	<b>0.05</b>
Energy acceptance (%)	2	2	<b>2</b>	2	<b>2</b>	
Energy acceptance by RF (%)	6	<b>2.2</b>	<b>2.2</b>	<b>2.2</b>	<b>2.1</b>	<b>1.1</b>
$n_\gamma$	0.23	0.49	<b>0.47</b>	0.47	<b>0.47</b>	<b>0.27</b>
Life time due to beamstrahlung_cal (minute)	47	53	<b>36</b>	41	<b>32</b>	
$F$ (hour glass)	0.68	0.73	<b>0.82</b>	0.69	<b>0.81</b>	<b>0.95</b>
$L_{max}$ /IP ( $10^{34}\text{cm}^{-2}\text{s}^{-1}$ )	2.04	2.97	<b>2.96</b>	2.03	<b>2.01</b>	<b>3.61</b>



# Cell number

- 5 cell cavity was designed for Pre-CDR scheme. Is it suitable for PDR scheme?
- Selection basis:
  - Accelerating gradient
  - HOMs
  - HOM power
  - HOM power coupler
  - Impedance
  - Cryogenic
  - Transient beam loading
  - Cost
  - .....

# Comparison of different schemes

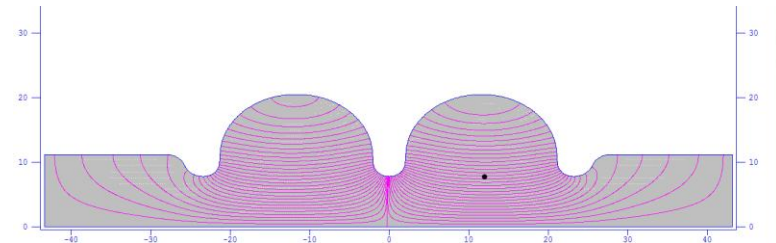
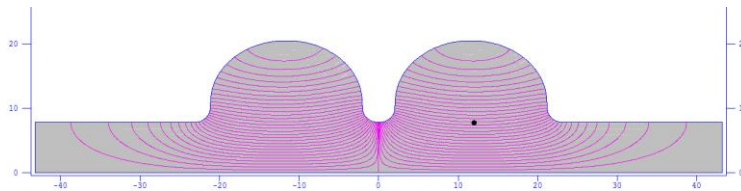
	High-lumi crossing angle=30mrad		Low power crossing angle=30mrad	
Cell no.	5	2	5	2
$Q_0$	$4 \times 10^{10}$	$2 \times 10^{10}$	$4 \times 10^{10}$	$2 \times 10^{10}$
$R/Q$ ( $\Omega$ )	514	212.7	514	212.7
$k_{\text{HOM}}$ /cavity (V/pC)	1.4	0.55	1.47	0.59
Ave. RF power/cavity (kW)	263.29	261.56	163.83	163.04
HOM power/cavity (kW)	2.87	1.14	1.33	0.54
Cavity voltage (MV)	9.6	9.6	9.2	9.2
Gradient (MV/m)	8.4	20.9	8.0	19.9
Detuning frequency (kHz)	-2.97	-1.23	-1.76	-0.73
Cavity bandwidth (kHz)	7.9	3.3	5.4	2.2
Cavity effective length (m)	1.153	0.461	1.153	0.461
Stored energy/cavity (J)	44.2	106.9	40.3	97.3
Cavity wall loss/cavity (W)	4.5	21.8	4.1	19.9



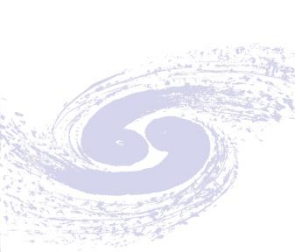
# Cavity design

■  $R_{\text{tube}} = 78 \text{ mm}$

■  $R_{\text{tube}} = 112.2 \text{ mm}$



		$R_{\text{tube}} = 78 \text{ mm}$	$R_{\text{tube}} = 112.2 \text{ mm}$
Cut off frequency	MHz	TM01: 1471 TE11: 1126	TM01: 1022 TE11: 783
$R/Q$	$\Omega$	212.7	206.3
$k_{\text{HOM}}$ ( $\sigma = 4 \text{ mm}$ )	(V/pC)	0.593	1.346
Average HOM power (low power 30mrad scheme)	kW	0.54	1.226
Pulsed HOM power	kW	9.11	20.68



# HOM power for multiple time-structure

## ■ Beam parameters:

- H-Low power & crossing angle=30 mrad scheme

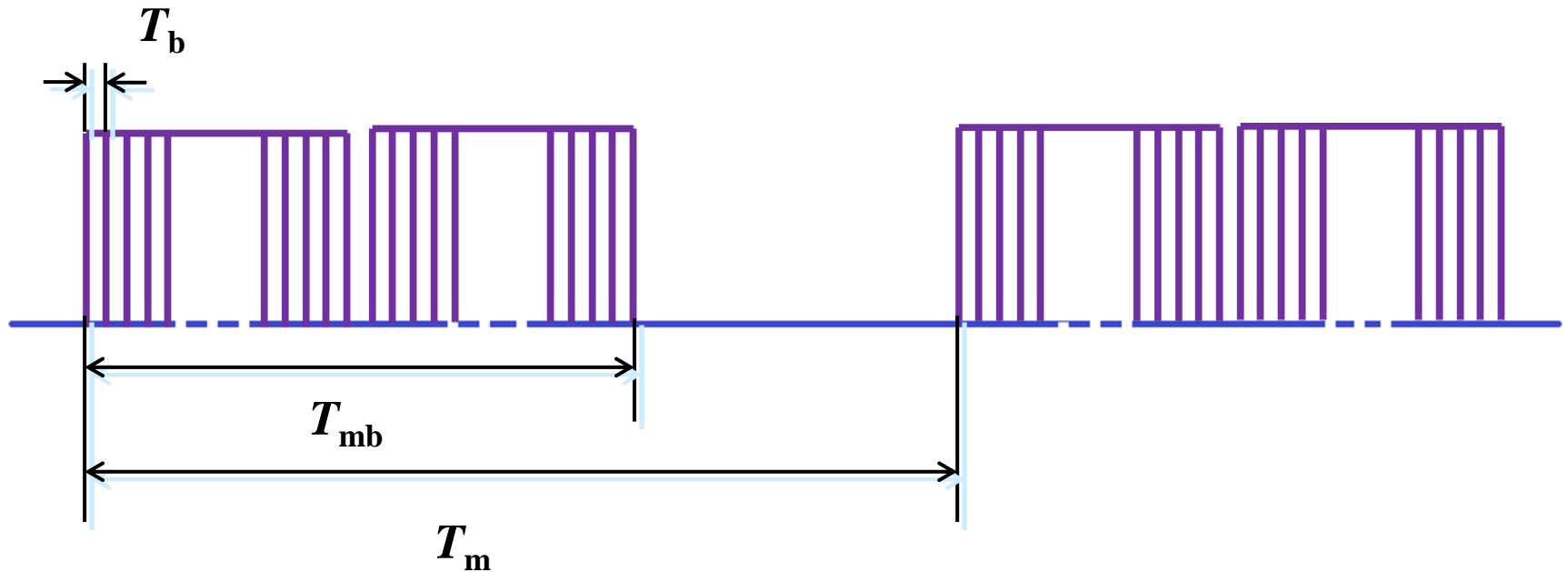
## ■ Time structure:

- Cavity location: IP1 & IP3
- Cavity location: IP2 & IP4





# Time structure 1: IP1 & IP3



**Macro-pulse period:  $T_m = 180 \mu\text{s}$**

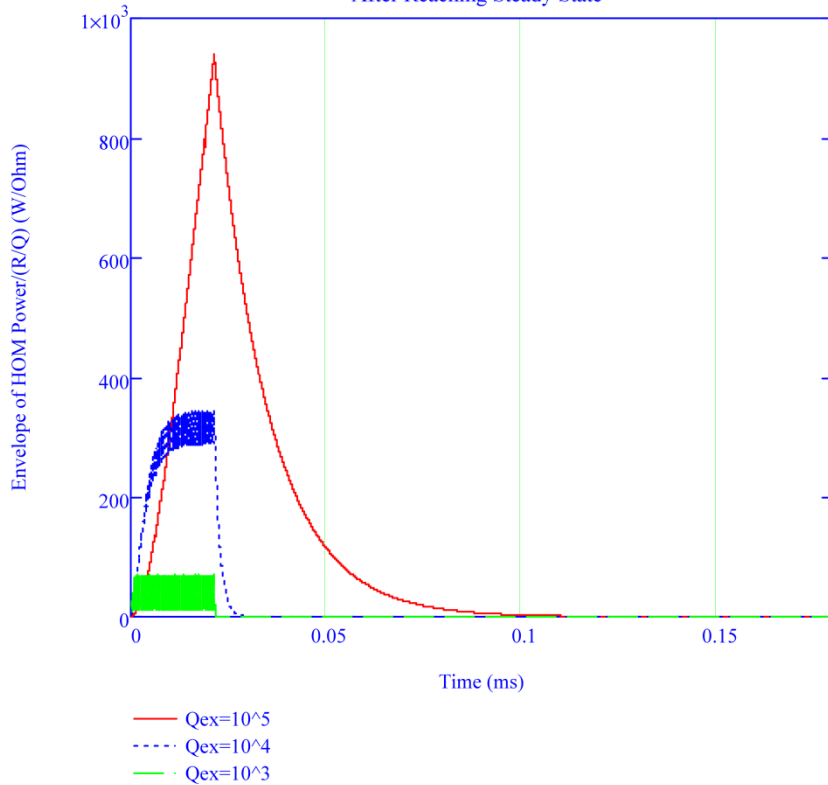
**Pulse length:  $T_{mb} = 21.4 \mu\text{s}$**

**Macro-pulse gap length :  $T_G = T_m - T_{mb} = 158.4 \mu\text{s}$**

**Time spacing between bunches:  $T_b = 243.1 \text{ ns}$**

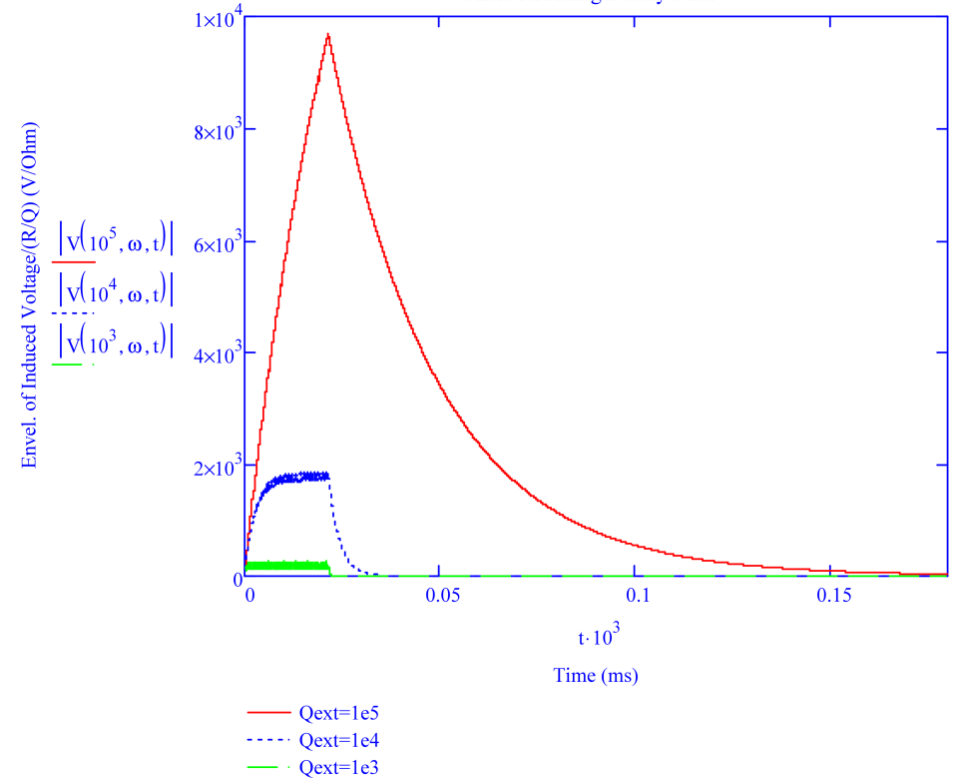
# Induced voltage & HOM power

After Reaching Steady State



Induced voltage in  $T_m$

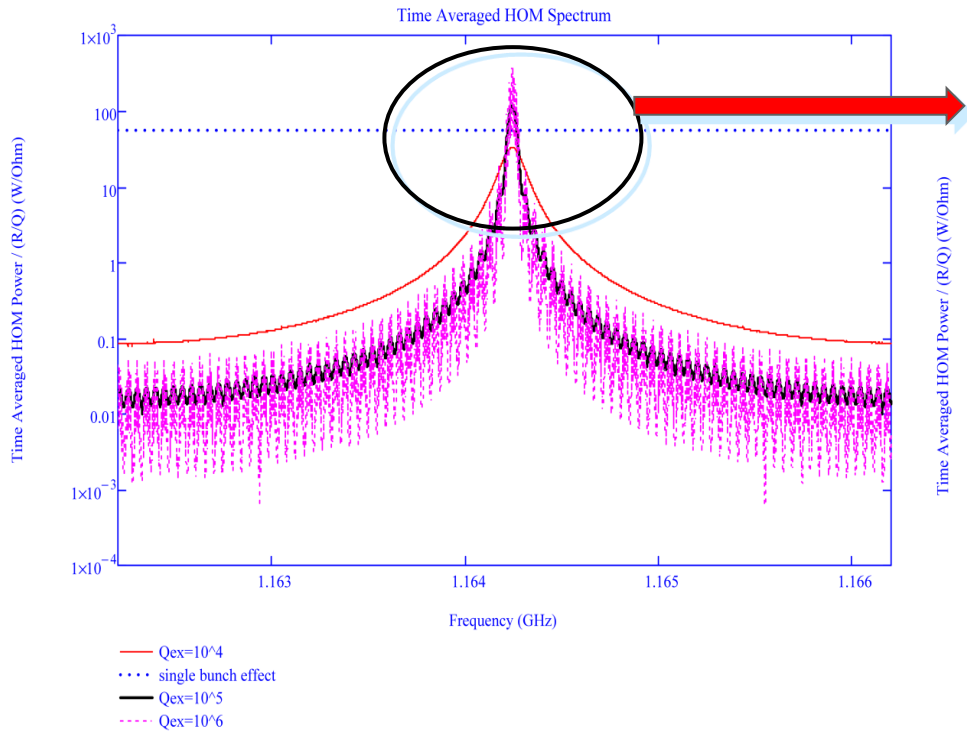
After Reaching Steady State



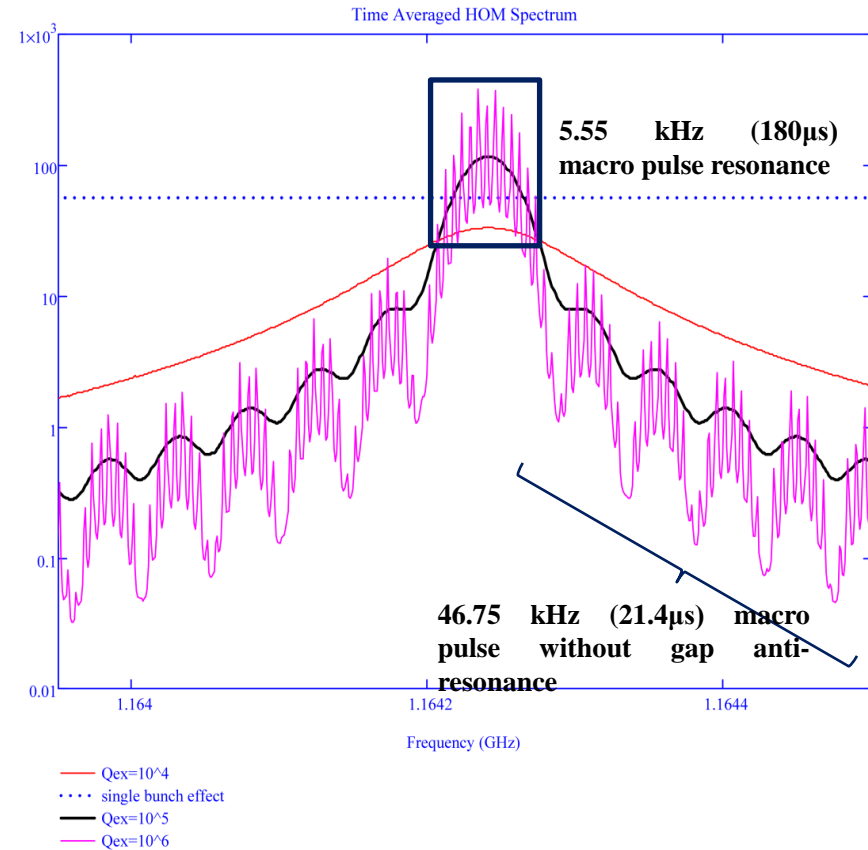
Induced power in  $T_m$

$f=1.164$  GHz, near TM011 mode !

# Time averaged HOM power-1

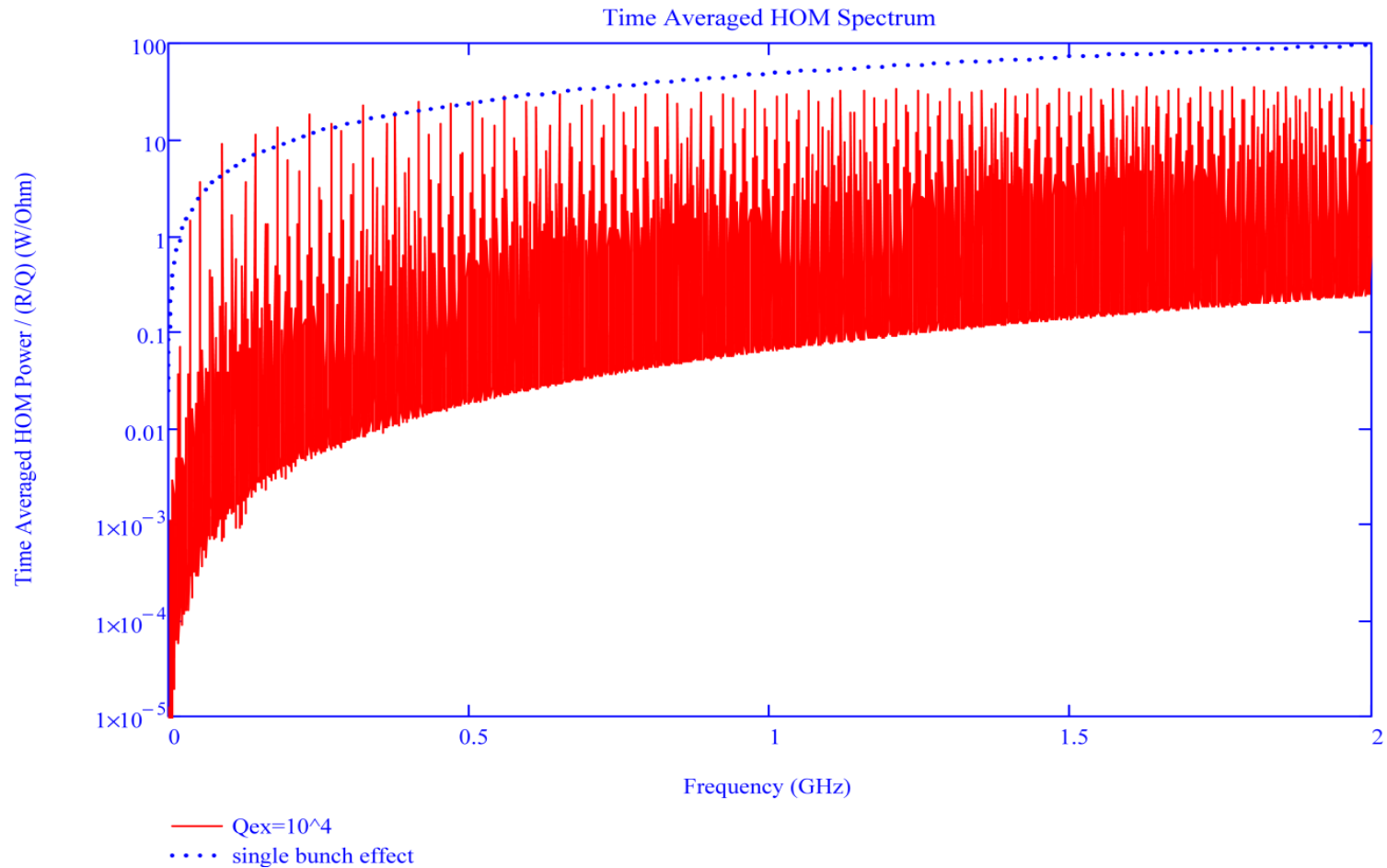


Bandwidth: 4 MHz



Bandwidth: 0.55 MHz

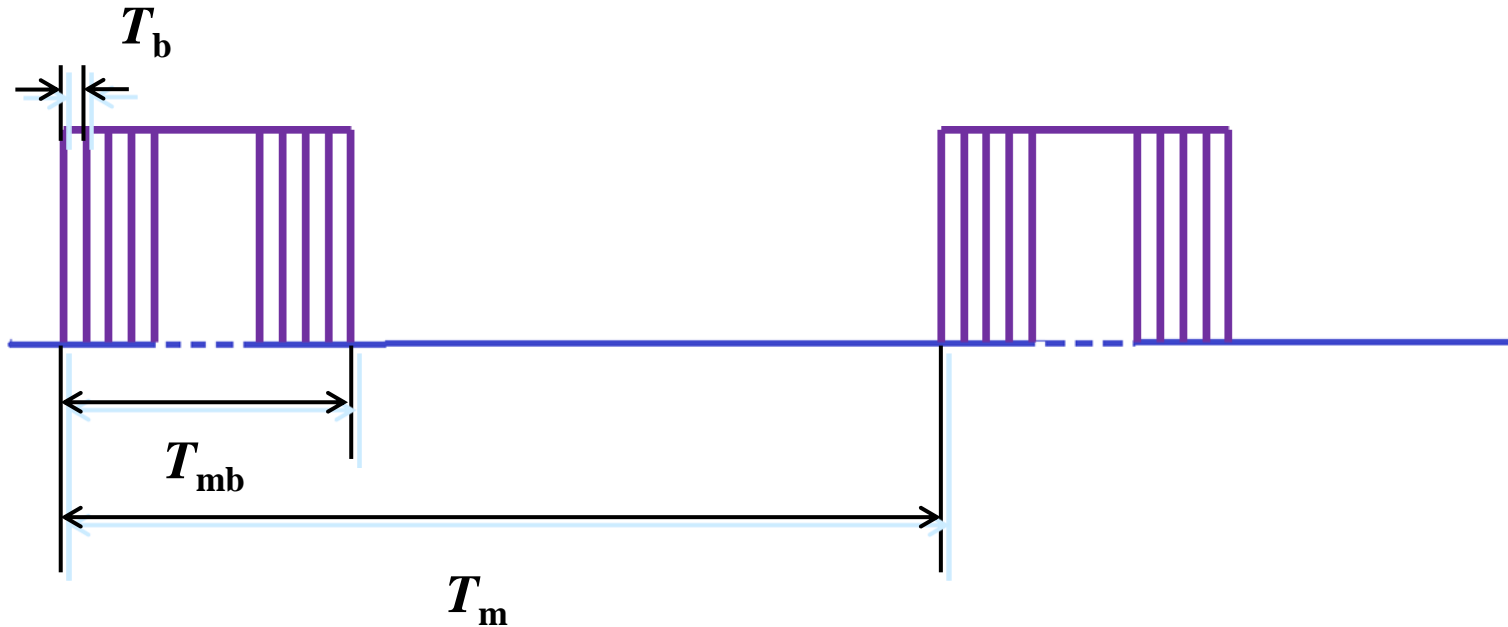
# Time averaged HOM power-2



Bandwidth: 2 GHz



# Time structure 1: IP2 & IP4



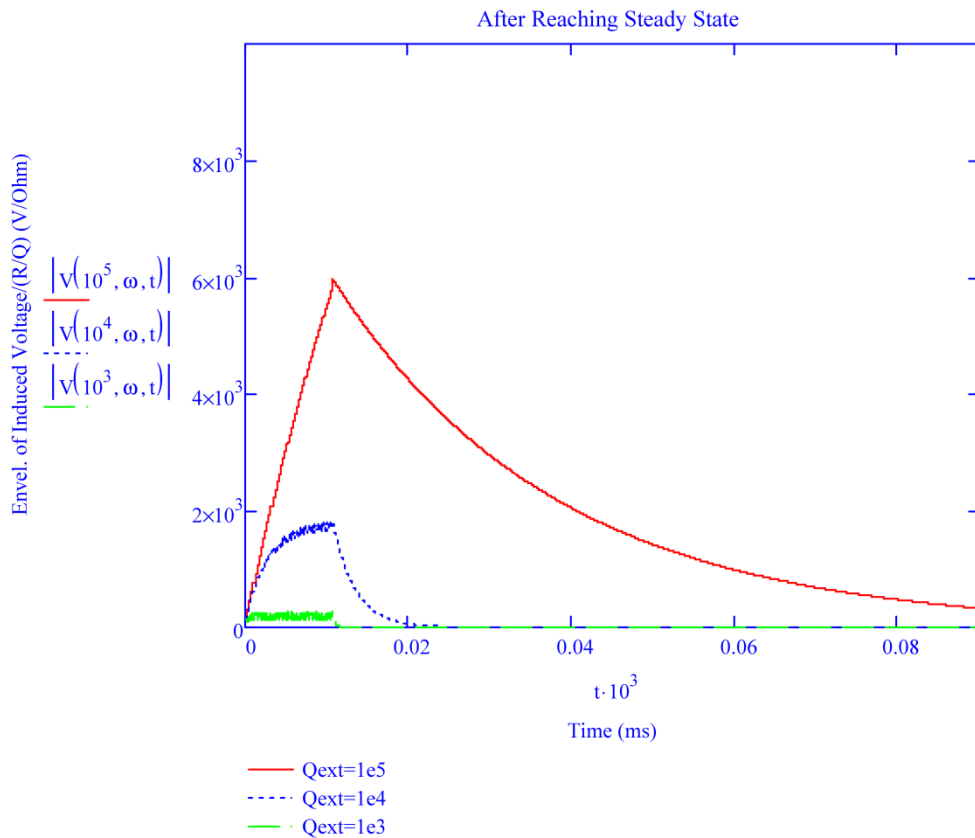
**Macro-pulse period:  $T_m = 90.06 \mu\text{s}$**

**Pulse length:  $T_{mb} = 10.7 \mu\text{s}$**

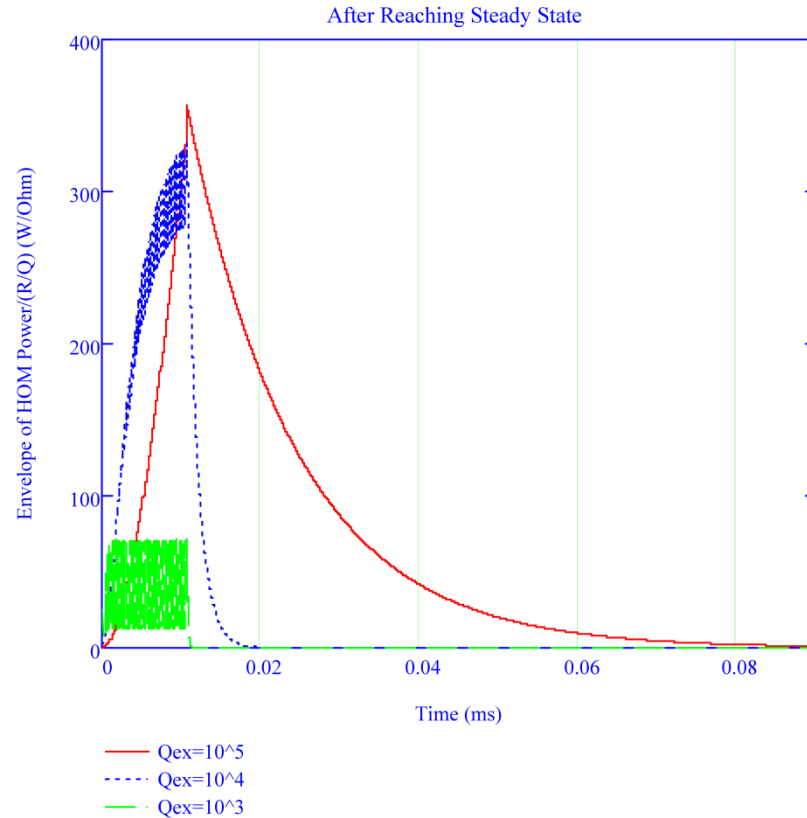
**Macro-pulse gap length :  $T_G = T_m - T_{mb} = 79.37 \mu\text{s}$**

**Time spacing between bunches:  $T_b = 243.1 \text{ ns}$**

# Induced voltage & HOM power



Induced voltage in  $T_m$

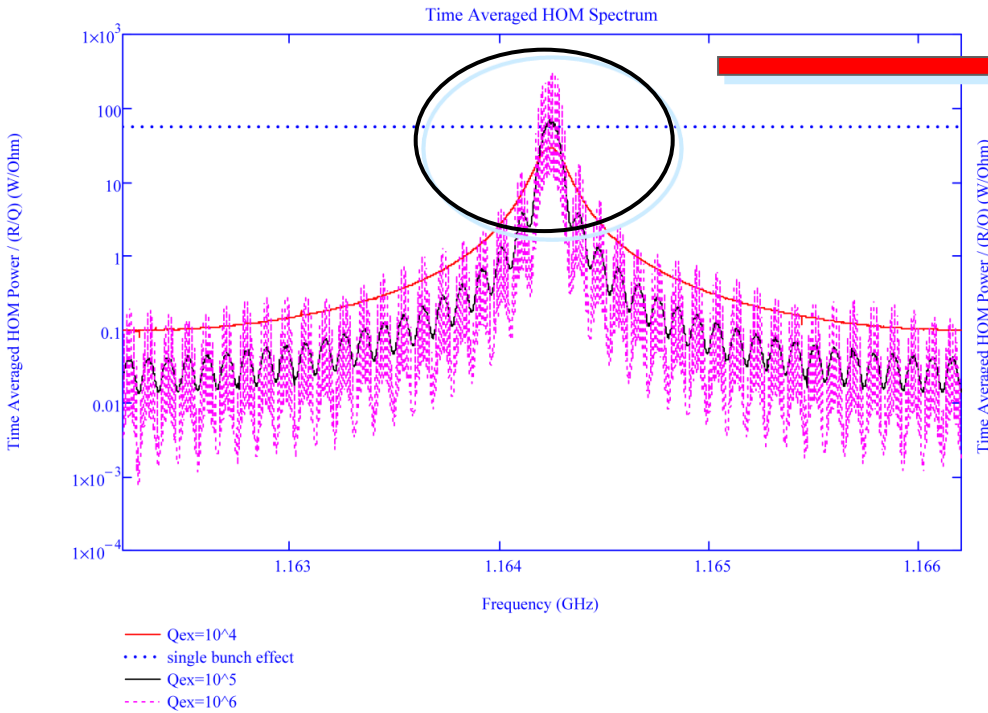


Induced power in  $T_m$

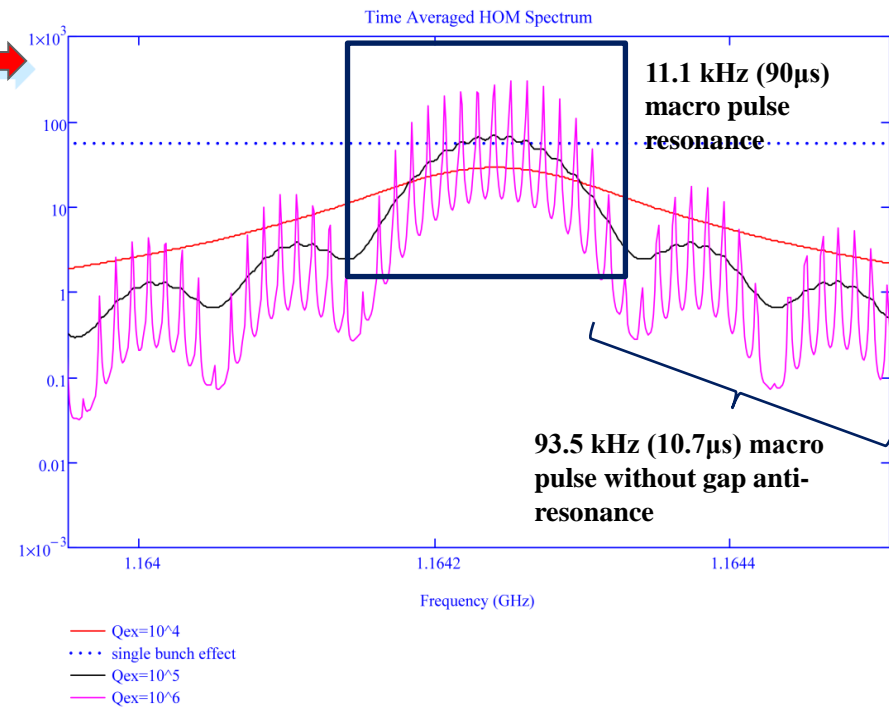
$f=1.164$  GHz, near TM011 mode !



# Time averaged HOM power-1



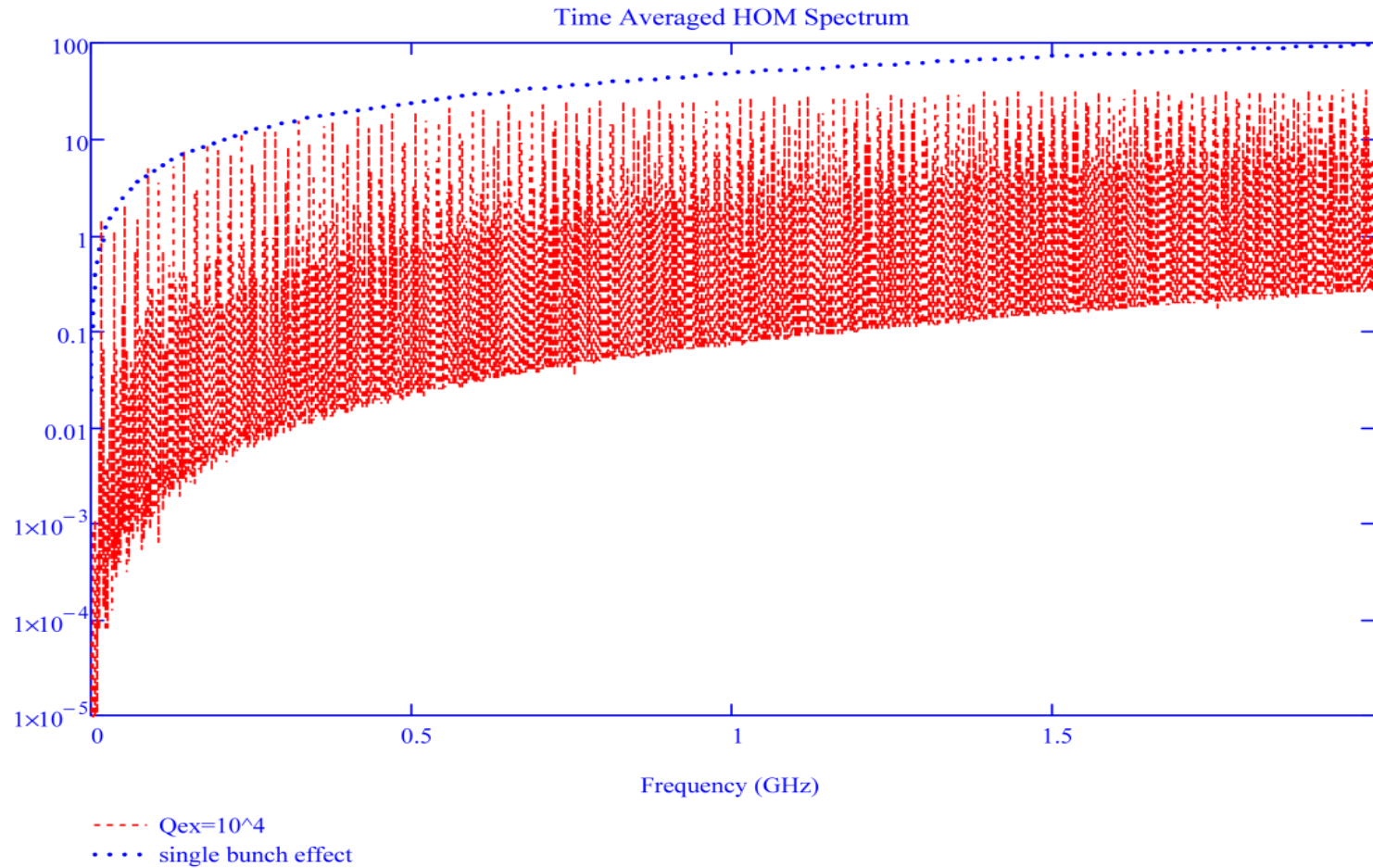
Bandwidth: 4 MHz



Bandwidth: 0.5 MHz



# Time averaged HOM power-2



Bandwidth: 2 GHz



# Crude estimates of Multi bunch instability caused by RF cavity

- In the resonant condition, the threshold shunt impedances are

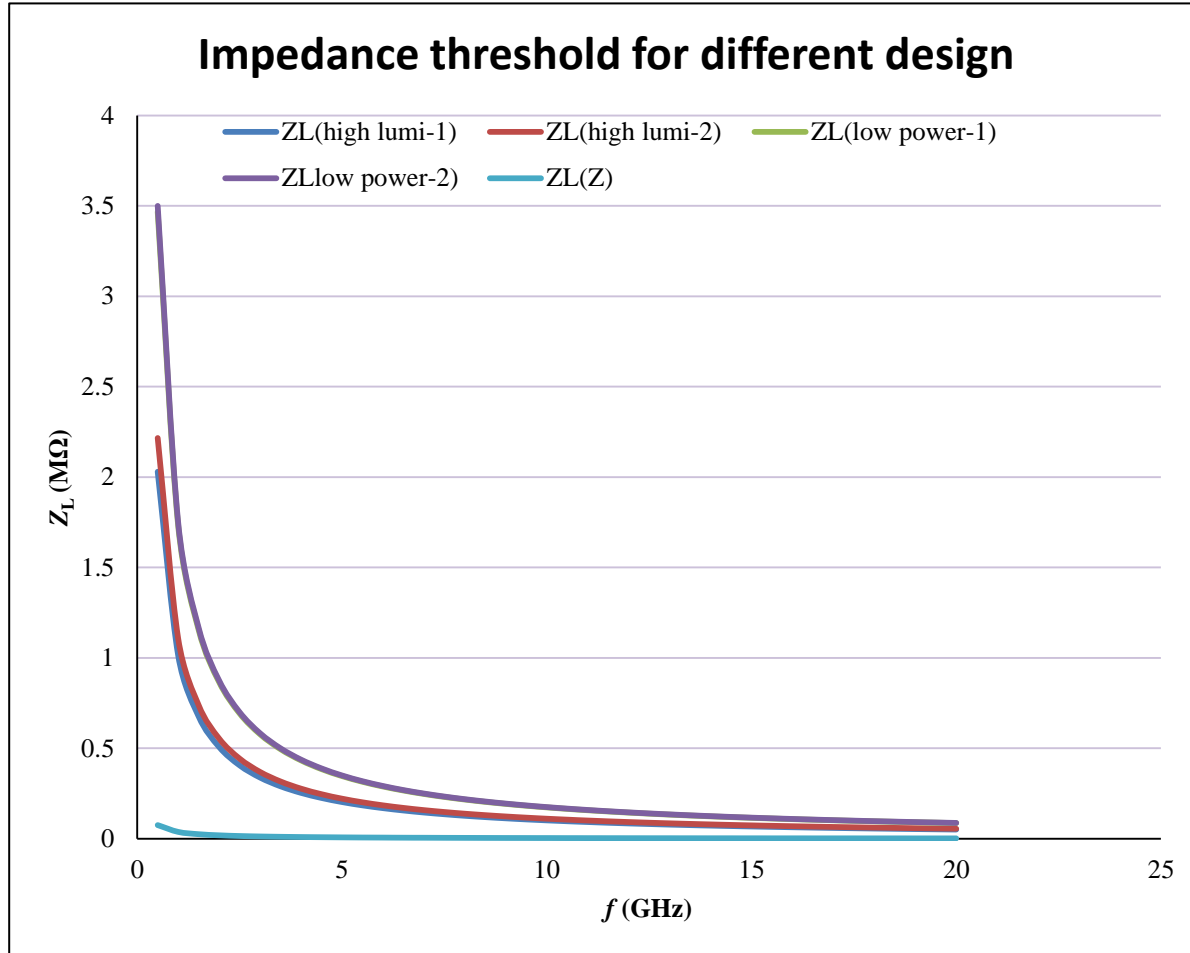
$$R_L^{thresh} = \frac{2(E_0 / e)v_s}{N_c f_L I_0 \alpha_p \tau_z} = \frac{2(U_0 / e)v_s}{N_c f_L I_0 \alpha_p T_0}$$

$$R_T^{thresh} = \frac{2(E_0 / e)}{N_c f_{rev} I_0 \beta_{x,y} \tau_{x,y}} = \frac{U_0 / e}{N_c f_{rev} I_0 \beta_{x,y} T_0}$$

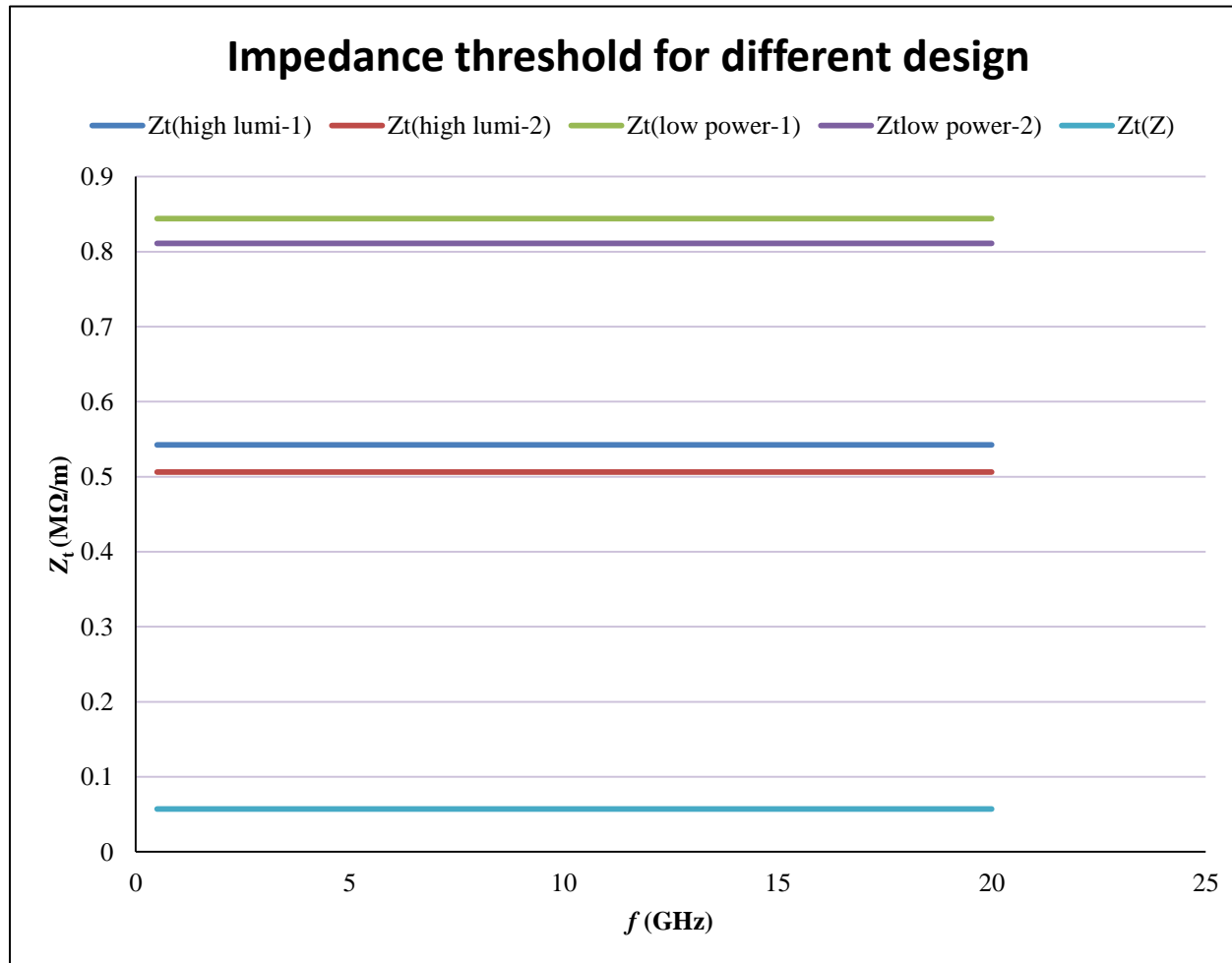
[1]. Byrd, J. and J. Corlett. *Study of Coupled-bunch Collective Effects in the ALS*. in *Particle Accelerator Conference, Proceedings of the 1993*. IEEE

[2]. Emery, L. *Coupled-bunch instability study of multi-cell deflecting mode cavities for the Advanced Photon Source*. in *Particle Accelerator Conference, 2007*. PAC. IEEE.

# Longitudinal impedance threshold



# Transverse impedance threshold





# Requirement for $Q_e$

monopole	$f$ (MHz)	$R/Q$ ( $\Omega$ ) (2 cell)	$R/Q^*$ ( $\Omega$ ) (1 cell)	$Q_e$ (H-low power)	$Q_e$ (Z-2 cell)	$Q_e$ (Z-1 cell)
TM011	1165.536	63.4	33.63	$4.74 \times 10^4$	$1.02 \times 10^3$	$1.95 \times 10^3$
TM020	1384.302	1.128	0.095	$2.24 \times 10^6$	$4.83 \times 10^4$	$5.85 \times 10^5$
dipole	$f$ (MHz)	$R/Q$ ( $\Omega/m$ ) (2 cell)	$R/Q^{**}$ ( $\Omega/m$ ) (1 cell)	$Q_e$ (H-low power)	$Q_e$ (Z-2 cell)	$Q_e$ (Z-1 cell)
TE111	844.666	276.62	131.03	$5.86 \times 10^3$	$4.13 \times 10^2$	$8.72 \times 10^2$
TM110	907.469	414.84	353.04	$3.91 \times 10^3$	$2.75 \times 10^2$	$3.23 \times 10^2$
TM111	1279.043	----	219.98	----	----	$5.19 \times 10^2$
TE121	1468.139	12.61	0.749	$1.29 \times 10^5$	$9.06 \times 10^3$	$1.52 \times 10^5$

\*  $k_{//mode} = 2\pi f \cdot (R/Q) / 4$  [V/pC]

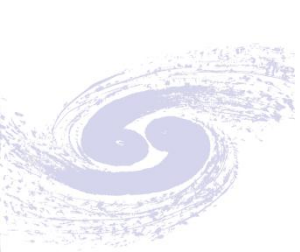
\*\*  $k_{\perp mode} = 2\pi f \cdot (R/Q) / 4$  [V/(pC·m)]

- Higgs: low power & 30 mrad crossing angle, 384 2-cell cavity
- Z: 32 2-cell or 1-cell cavity



# Summary

- 2 cell cavity is chosen for PDR-Higgs design.
- Multi-bunch instability caused by the RF cavity need to be further studied.
- HOM coupler considerations.
- .....



# Multi-bunch instability for bunch train scheme

## ■ CESR[1]

- Using a tracking code 'Oscil' to study the longitudinal dynamics of multi-bunch beams.

## ■ APS[2]

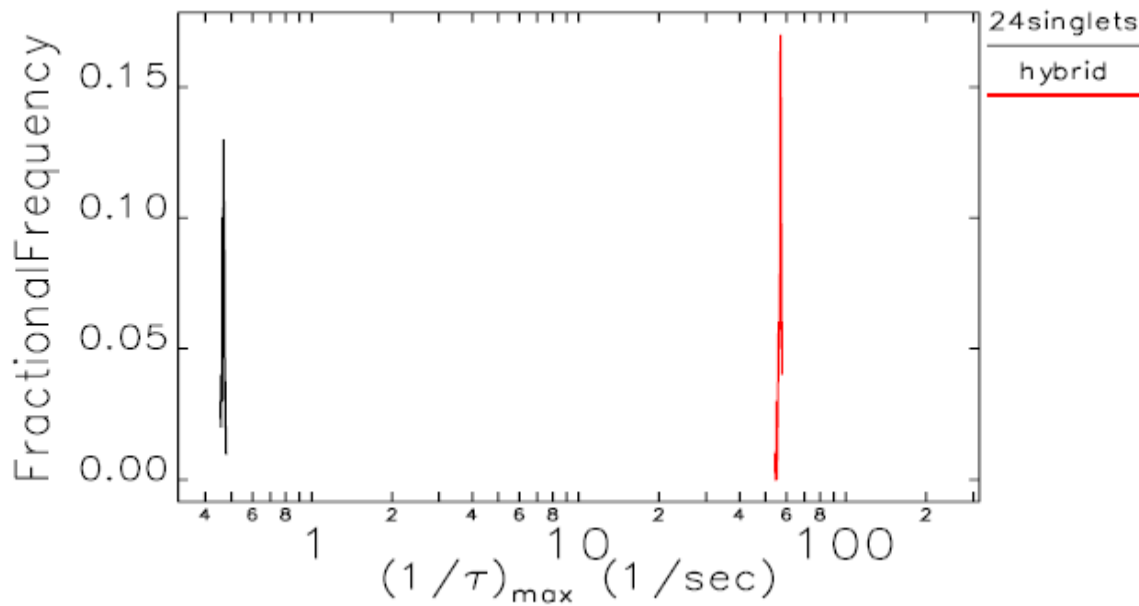
- Using a code 'clinchor' .

[1]. Fromowitz, D. *Simulation of longitudinal multibunch instabilities in CESR*. in *Particle Accelerator Conference, Proceedings of the 1999*. IEEE.

[2]. Emery, L. *Coupled-bunch instability study of multi-cell deflecting mode cavities for the Advanced Photon Source*. in *Particle Accelerator Conference, 2007. PAC. IEEE*.



# APS results



- 24 singlets:  
24 equidistant bunches
- Hybrid  
Single bunch of 16 mA  
+ a 56 bunch train .  
56 bunch train: 8  
groups of 7  
consecutive bunches  
spaced by 24 buckets.

Histogram of possible longitudinal growth rate from four 3 cell cavities.

We found that the growth rates were generally greater for the hybrid mode pattern, probably because of so much charge within 500 ns out of the 3.68- $\mu$ s revolution time.