

# *Understanding the quarkonium production mechanism from polarization measurements*

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# Outline

I.  $J/\psi$  polarization puzzle

II. Recent progress

III. Rotation-invariant observables

IV. Summary

# $\psi'$ surplus

## ► $\psi'$ surplus at Tevatron

- Data overshoot CSM calculation by a factor of 30 at high  $p_T$
- Fragmentation contribution included
- Other mechanism is needed

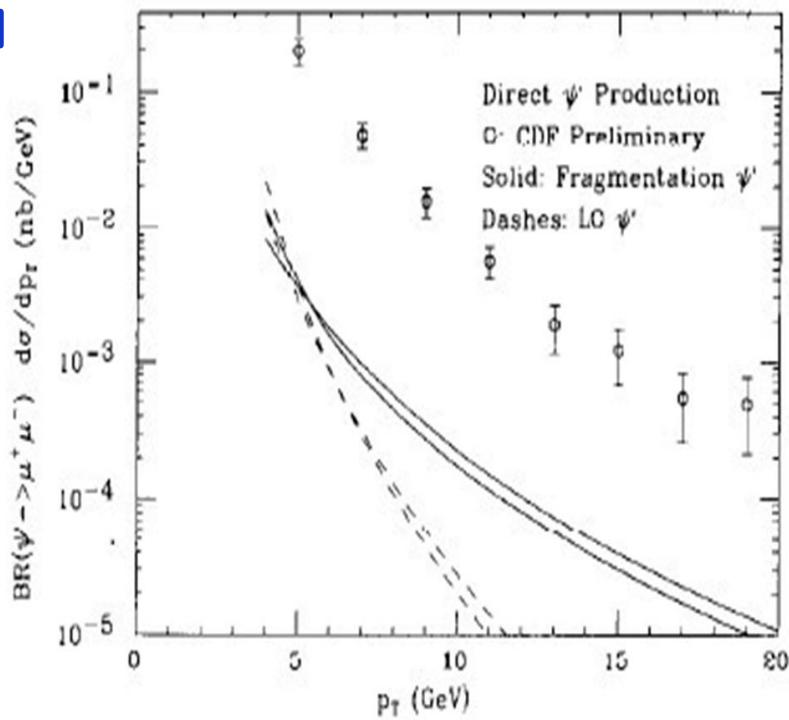
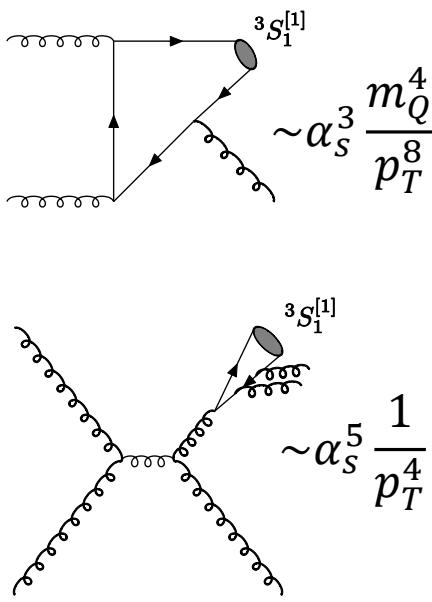


Fig. 4. Preliminary CDF data for prompt  $\psi'$  production (O) compared with theoretical predictions of the total fragmentation contribution (solid curves) and the total leading-order contribution (dashed curves).

# NRQCD and CO mechanism

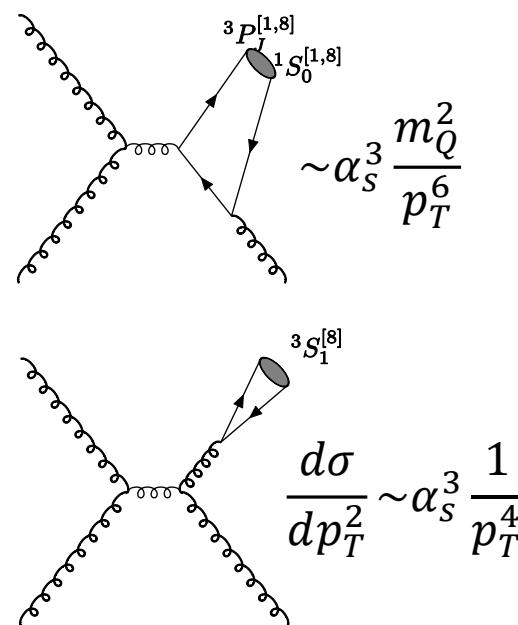
## ➤ NRQCD factorization

Bodwin, Braaten, Lepage, 9407339

$$d\sigma_\psi = \sum_{i,j,n} \int dx_1 dx_2 \underbrace{\int_{\Lambda_{QCD}} G_{i/A} G_{j/B}}_{m_c} \times \underbrace{\hat{\sigma}[ij \rightarrow c\bar{c}[n] + X]}_{m_c v} \times \underbrace{\langle O_n^\psi \rangle}_{m_c v}$$

## ➤ CO mechanism

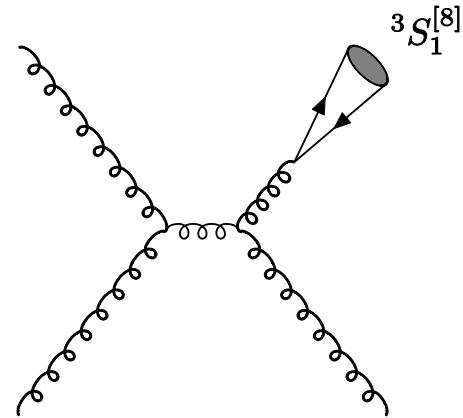
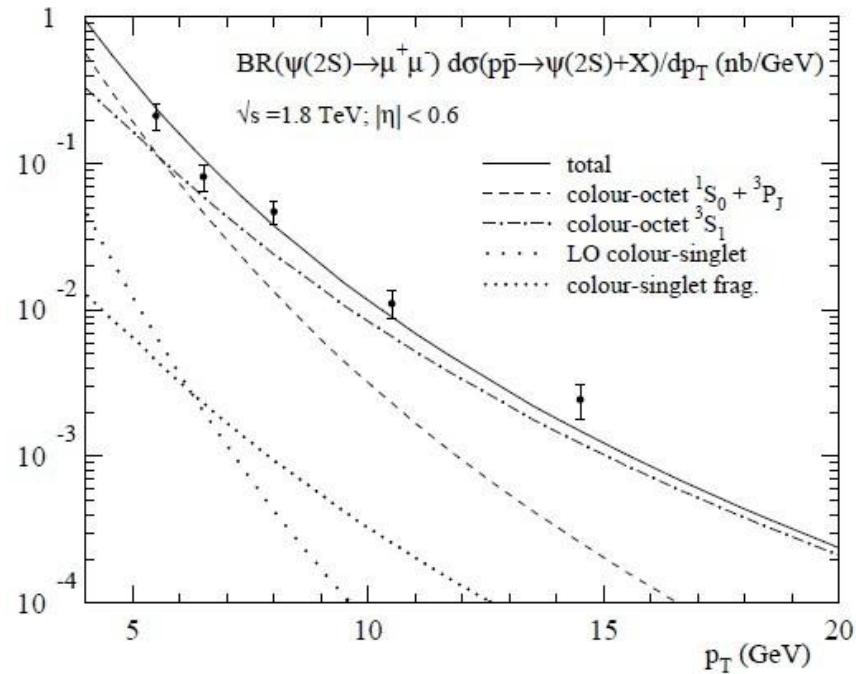
States	$p_T$ behavior at LO
$^3S_1^{[1]}$	$p_T^{-8}$
$^3S_1^{[8]}$	$p_T^{-4}$
$^1S_0^{[8]}$	$p_T^{-6}$
$^3P_J^{[8]}$	$p_T^{-6}$



# $^3S_1^{[8]}$ dominance

## ➤ LO NRQCD calculation

- $^3S_1^{[8]}$  dominant at high  $p_T$
- Predicts transverse polarization



Kramer, 0106120

# Polarization puzzle

➤  $\psi \rightarrow l^+ l^-$

- $W(\cos \theta, \phi) \propto \frac{1}{3+\alpha} (1 + \alpha \cos^2 \theta)$
- LO NRQCD prediction contradicts with CDF data

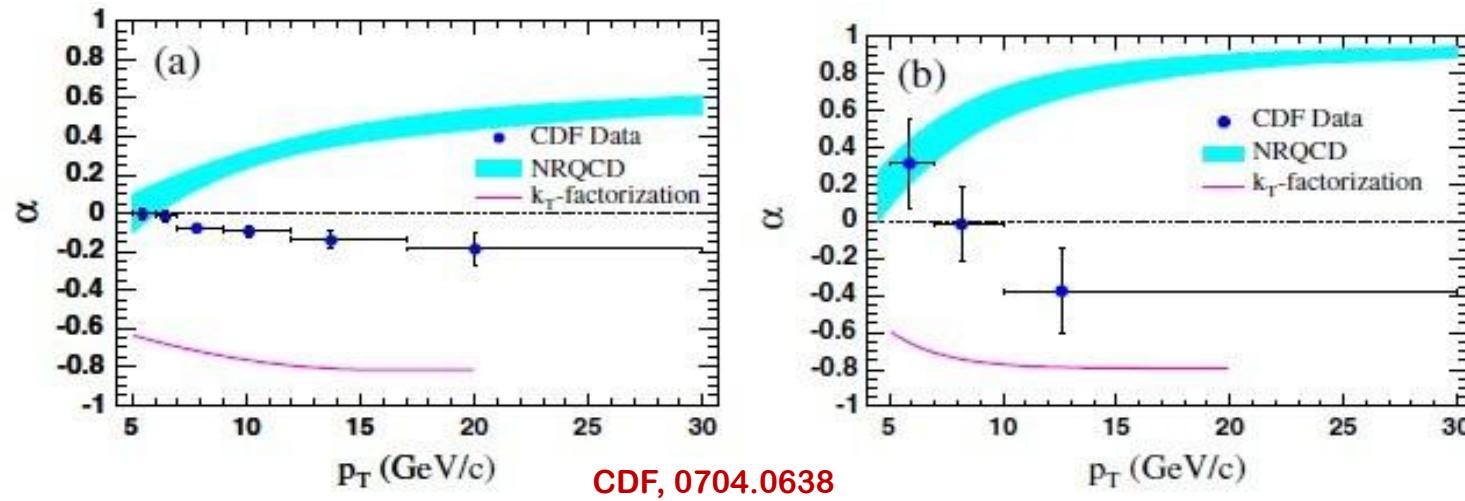


FIG. 4 (color online). Prompt polarizations as functions of  $p_T$ : (a)  $J/\psi$  and (b)  $\psi(2S)$ . The band (line) is the prediction from NRQCD [4] (the  $k_T$ -factorization model [9]).

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# Theoretical side: high order calculation

- 0703113: Campbell, Maltoni, Tramontano

NLO, cross section, S-wave

- 0802.3727: Gong, Wang

NLO, polarization, S-wave

- 0806.3282: Artoisenet, Campbell, Lansberg, Maltoni, Tramontano

NNLO\*, S-wave

- 1002.3987: YQM, Wang, Chao
- 1009.3655: YQM, Wang, Chao
- 1009.5662: Butenschöen, Kniehl

NOT fully  
comprehensive!!!

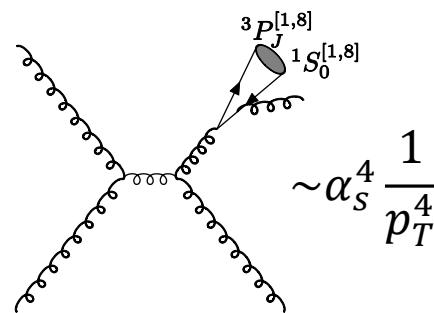
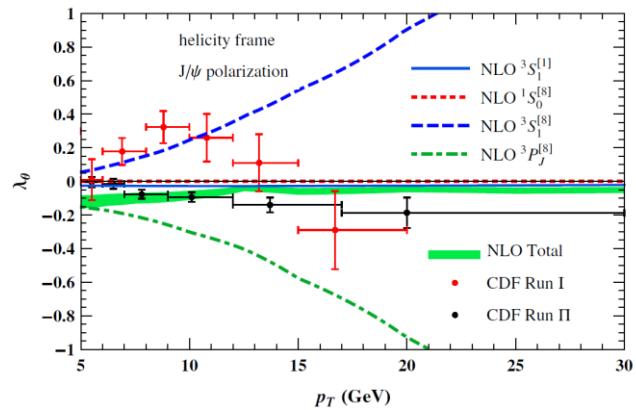
Complete NLO (S- and P-wave), cross section

- 1201.1872: Butenschöen, Kniehl
- 1201.2675: Chao, YQM, Shao, Wang, Zhang
- 1205.6682: Gong, Wan, Wang, Zhang

Complete NLO (S- and P-wave), with polarization

# Explain $J/\psi$ polarization

- Transverse polarization cancelled between  $^3S_1^{[8]}$  and  $^3P_J^{[8]}$  channel at NLO,  $^1S_0^{[8]}$  may dominate



Chao, YQM, Shao, Wang, Zhang, 1201.2675

- $^1S_0^{[8]}$  dominant mechanism: agreed by new studies

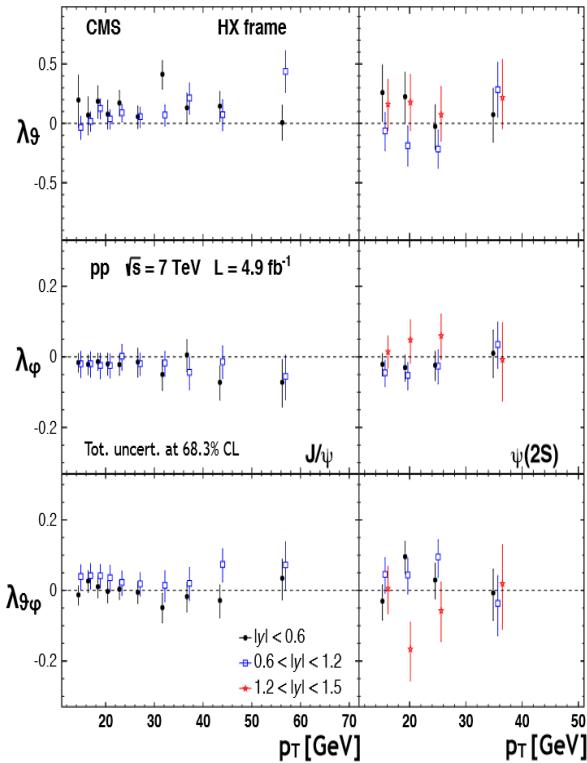
Bodwin, Chung, Kim, Lee, 1403.3612

Faccioli, Knunz, Lourenco, Seixas, Wohri, 1403.3970

# Experimental side: better measurements

- General observable distribution for dilepton decay of inclusive produced vector meson

$$W(\cos\vartheta, \varphi) \propto \frac{1}{(3 + \lambda_\vartheta)} (1 + \lambda_\vartheta \cos^2 \vartheta + \lambda_\varphi \sin^2 \vartheta \cos 2\varphi + \lambda_{\vartheta\varphi} \sin 2\vartheta \cos \varphi)$$



- “Full” double angle analyses
- To avoid bias in single angle analyses

# SO(2) rotation invariant observable

## ➤ Experimentally commonly used reference frames

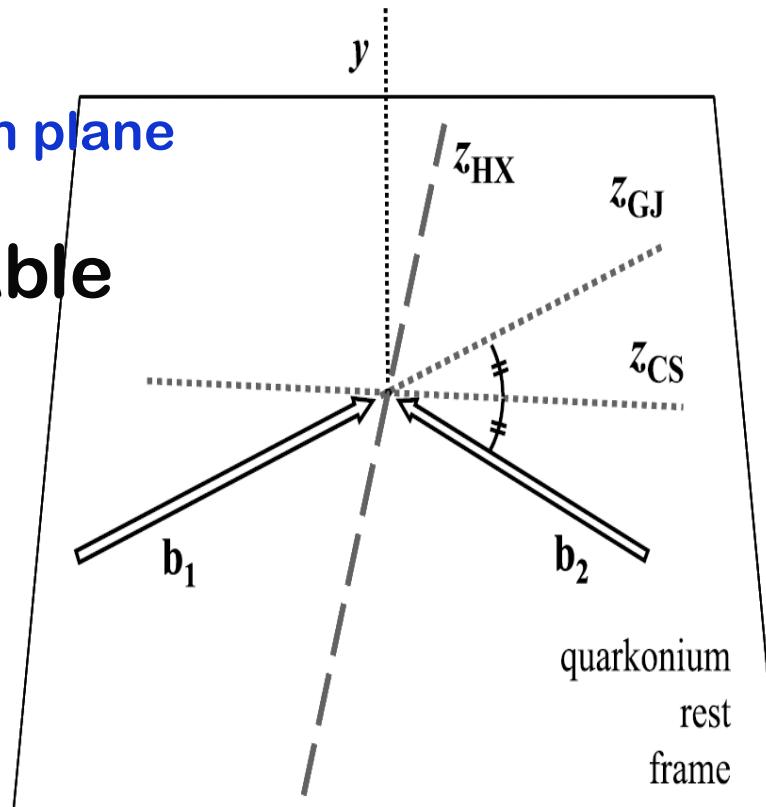
- S-channel helicity frame, Collins-Soper frame, Gottfried-Jakson frame
- Related by a rotation in the production plane

## ➤ Frame independent observable

$$\tilde{\lambda} \equiv \mathcal{F}_{\{-3,0,1\}} = \frac{\lambda_\vartheta + 3\lambda_\varphi}{1 - \lambda_\varphi}$$

Faccioli, Lourenco, Seixas, Wohri, 1006.2738

- On behind the rotation invariant of Lam-Tung relation



# Another SO(2) rotation invariant observable

- Using complicated algebra, another invariant is found

$$\lambda^* \equiv \frac{1 + \Delta/4}{\sqrt{\Delta^2 + 4\lambda_{\theta\phi}^2}} = \frac{1 + (\lambda_\theta - \lambda_\phi)/4}{\sqrt{(\lambda_\theta - \lambda_\phi)^2 + 4\lambda_{\theta\phi}^2}}$$

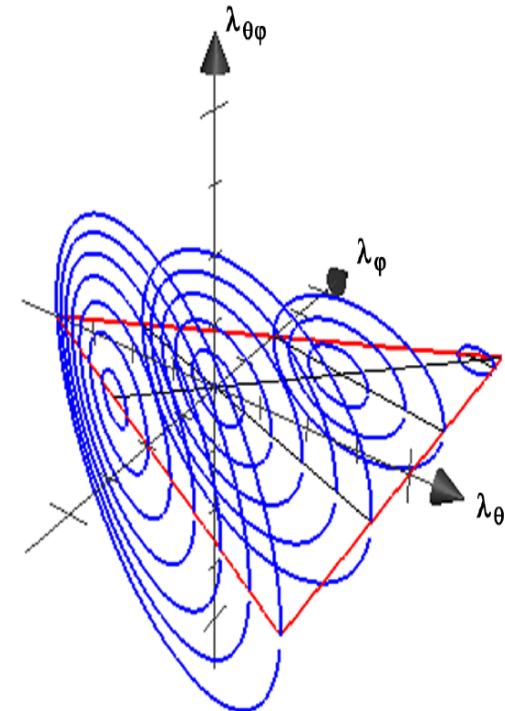


FIG. 1 (color online). Ellipses of rotation in the space of the coefficients of the angular distribution are illustrated, showing four sets corresponding to  $\tilde{\lambda} = -1, 0, 3, 37$  (see Sec. V).

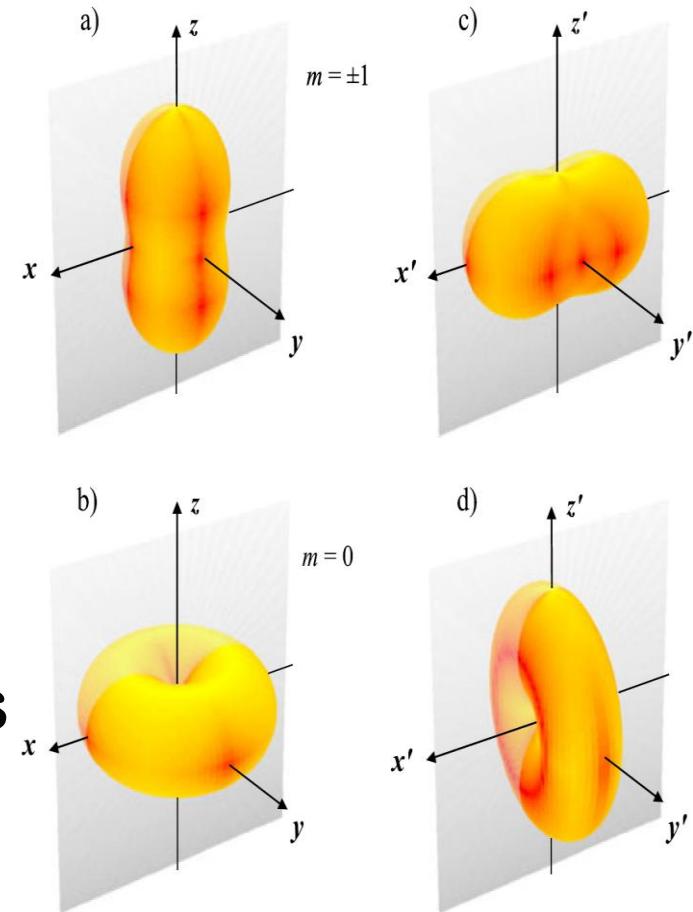
Palestini, 1012.2485

# Properties of invariants

## ➤ Nice feature of rotation invariants

- Experimental axis can be different from natural axis
- Less sensitive to detector acceptances
- Can be checked between measurements from different reference frame

Faccioli, Lourenco, Seixas, Wohri, 1006.2738



## ➤ Find out all rotation invariants

- SO(3) rotation invariants can be even powerful

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# Angular distribution

- General angular distribution of probe particle B in the rest frame of decay particle A

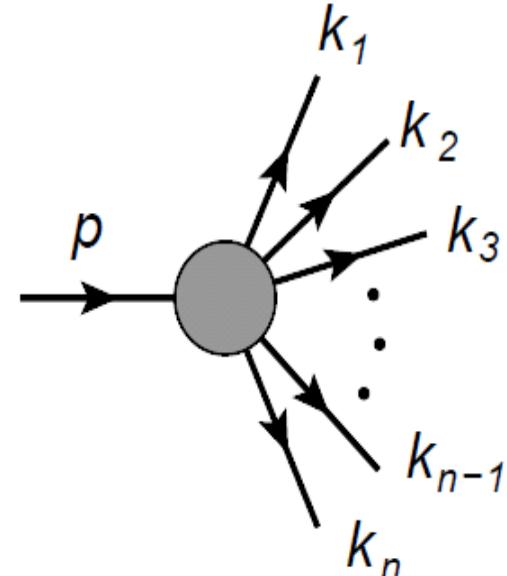
$$\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega_B} \equiv f(\theta, \phi) = \sum_{l=0}^{2J} \sum_{m=-l}^l f_{l,m} Y_{lm}(\theta, \phi)$$

YQM, Zhang, Qiu, in progress

$$f_{l,-m} = (-1)^m f_{l,m}^*$$

$$f_{0,0} = \frac{1}{\sqrt{4\pi}}$$

- Degree of freedom:  $4J^2 + 4J$
- There should be  $4J^2 + 4J - 3$  SO(3) rotation invariants,  
 $4J^2 + 4J - 1$  SO(2) rotation invariants



# SO(3) rotation invariants

- Invariants resulted from the unitarity of rotation

$$W_l = \sum_{m=-l}^l |f_{l,m}|^2, \quad l = 1, 2, \dots, 2J$$

- Invariants obtained by integration over all space angle

$$W_{J,n} = \int d\Omega \left[ f(\theta, \phi) - \frac{1}{4\pi} \right]^n, \quad n = 1, 2, \dots$$

- All SO(3) rotation invariants can be found by this method

# SO(2) rotation invariants

- Express distribution in bases of eigen functions of  $J_y$

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega_B} = \sum_{l=0}^{2J} \sum_{m=-l}^l g_{l,m} \bar{Y}_{lm}(\theta, \phi)$$

- Under SO(2) ration in the  $x - z$  plane:

$$g'_{l,m} = e^{im\delta} g_{l,m}$$

- SO(2) rotation invariants

$$T_{l,0} = g_{l,0},$$

$$T_{l,l} = |g_{l,l}|^2$$

- Other SO(2) rotation invariants are not independent

# Decay of spin- $\frac{1}{2}$ particle

## ➤ Angular distribution

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega} = \frac{1}{4\pi} \left[ 1 + 2A_\theta \cos \theta + 2A_\phi \sin \theta \cos \phi + 2A_{\perp\phi} \sin \theta \sin \phi \right]$$

- SO(3) rotation invariants

$$W_1 = \frac{A_\theta^2 + A_\phi^2 + A_{\perp\phi}^2}{3\pi}$$

- SO(2) rotation invariants

$$T_{1,0} = \frac{A_\phi^\perp}{\sqrt{3\pi}}$$

# Decay of spin–1 particle

- Angular distribution—assuming parity conserved

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega} = \frac{1}{4\pi(1 + \frac{\lambda_\theta}{3})} \left[ 1 + \lambda_\theta \cos^2 \theta + \lambda_\phi \sin^2 \theta \cos 2\phi + \lambda_{\theta\phi} \sin 2\theta \cos \phi \right. \\ \left. + \lambda_{\perp\phi} \sin^2 \theta \sin 2\phi + \lambda_{\perp\theta\phi} \sin 2\theta \sin \phi \right].$$

- SO(3) rotation invariants

$$W_2 = \frac{1}{5\pi} \frac{\lambda_\theta^2 + 3(\lambda_\phi^2 + \lambda_{\theta\phi}^2 + \lambda_{\perp\phi}^2 + \lambda_{\perp\theta\phi}^2)}{(3 + \lambda_\theta)^2}$$

$$W_3 = \frac{(\lambda_\theta + 3\lambda_\phi)(2\lambda_\theta^2 - 6\lambda_\theta\lambda_\phi + 9\lambda_{\theta\phi}^2) + 9(\lambda_\theta\lambda_{\perp\theta\phi}^2 - 2\lambda_\theta\lambda_{\perp\phi}^2 + 6\lambda_{\theta\phi}\lambda_{\perp\theta\phi}\lambda_{\perp\phi} - 3\lambda_\phi\lambda_{\perp\theta\phi}^2)}{70\pi^2(3 + \lambda_\theta)^3}$$

# Decay of spin–1 particle (con.)

- SO(2) rotation invariants, equivalent to  $\tilde{\lambda}$  and  $\lambda^*$ , respectively

$$T_{2,0} = -\frac{1}{2\sqrt{5\pi}} \frac{\lambda_\theta + 3\lambda_\phi}{3 + \lambda_\theta},$$

$$T_{2,2} = \frac{3}{40\pi} \frac{(\lambda_\theta - \lambda_\phi)^2 + 4\lambda_{\theta\phi}^2}{(3 + \lambda_\theta)^2}$$

- In frames where  $\lambda_{\perp\phi}$  and  $\lambda_{\perp\theta\phi}$  vanish, SO(3) invariants reduced to

$$\frac{\lambda_\theta^2 + 3\lambda_\phi^2 + 3\lambda_{\theta\phi}^2}{(3 + \lambda_\theta)^2},$$

$$\frac{(\lambda_\theta + 3\lambda_\phi)(2\lambda_\theta^2 - 6\lambda_\theta\lambda_\phi + 9\lambda_{\theta\phi}^2)}{(3 + \lambda_\theta)^3}$$

Equivalent to the two SO(2) invariants

# Summary

- More observables are needed to fully understand polarization puzzle
- All SO(3) or SO(2) rotation-invariant observables are constructed
- These observables potentially useful for both quarkonium physics and other physics

*Thank you!*

*Back up*

# Discovery: $J/\psi$ polarization

- ◆ Fit to  $J/\psi$  cross section requires a very small

$$M_1 = \langle O\left(^3S_1^{[8]}\right) \rangle - 0.56 \langle O\left(^3P_0^{[8]}\right) \rangle / m_c^2$$

YQM, Wang, Chao, 1009.3655

- ◆ Transverse polarization proportional to

$$M'_1 = \langle O\left(^3S_1^{[8]}\right) \rangle - 0.52 \langle O\left(^3P_0^{[8]}\right) \rangle / m_c^2$$

Chao,YQM,Shao,Wang,Zhang,1201.2675

- Cross section requires small transverse polarization—  
consistent with data!!!