

CalcHEP - calculator for High Energy Physics micrOMEAGs - calculation of DM properties

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<http://theory.sinp.msu.ru/~pukhov/calchep.html>

<http://lapth.cnrs.fr/micromegas>

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Main features

- **Language C**
- **Symbolic calculation of squared diagrams**. CalcHEP uses built-in symbolic calculator. Result of calculation can be presented in formats of **Reduce**, **Mathematica**, **C**.
- **Tree level** calculations in **Unitary** and **Feynman** gauges. The last one is free of diagram cancellation at high energies
- **Two modes of calculation**
 - a) **GUI** with menus and help facilities. Good for beginners.
 - b) **batch** mode, **subprocess cycle**
- **Model files**
 - a) can be generated by **LanHEP**, **feynRules**
 - b) effective loop induced vertices for H decay
 - c) spin 3/2 and 2
 - d) color sextets and **333** vertex.

- **Les Houches Interface**
 - a) **SLHA** interface with spectrum generators (SuSpect, SoftSUSY)
 - b) **LHAPDF5** & **LHAPDF6** link and export.
 - c) events (LEF)
- **Run-time generation** and dynamic linking of new codes. It allows 'on fly' **width calculation** including 1->3, 1->4 channels and virtual W/Z contribution.
- **Paralleling** for symbolic and numerical calculations.
Batch mode - **PC farms**
GUI - **fork** and **threads**.
- **Generation of codes** of matrix element for other packages (**micrOMEGAs**)

How to start to work

Compilation: needs gcc and X11-devel (with h-files)

```
cd calchep_3.6.28  
make
```

Starting GUI session

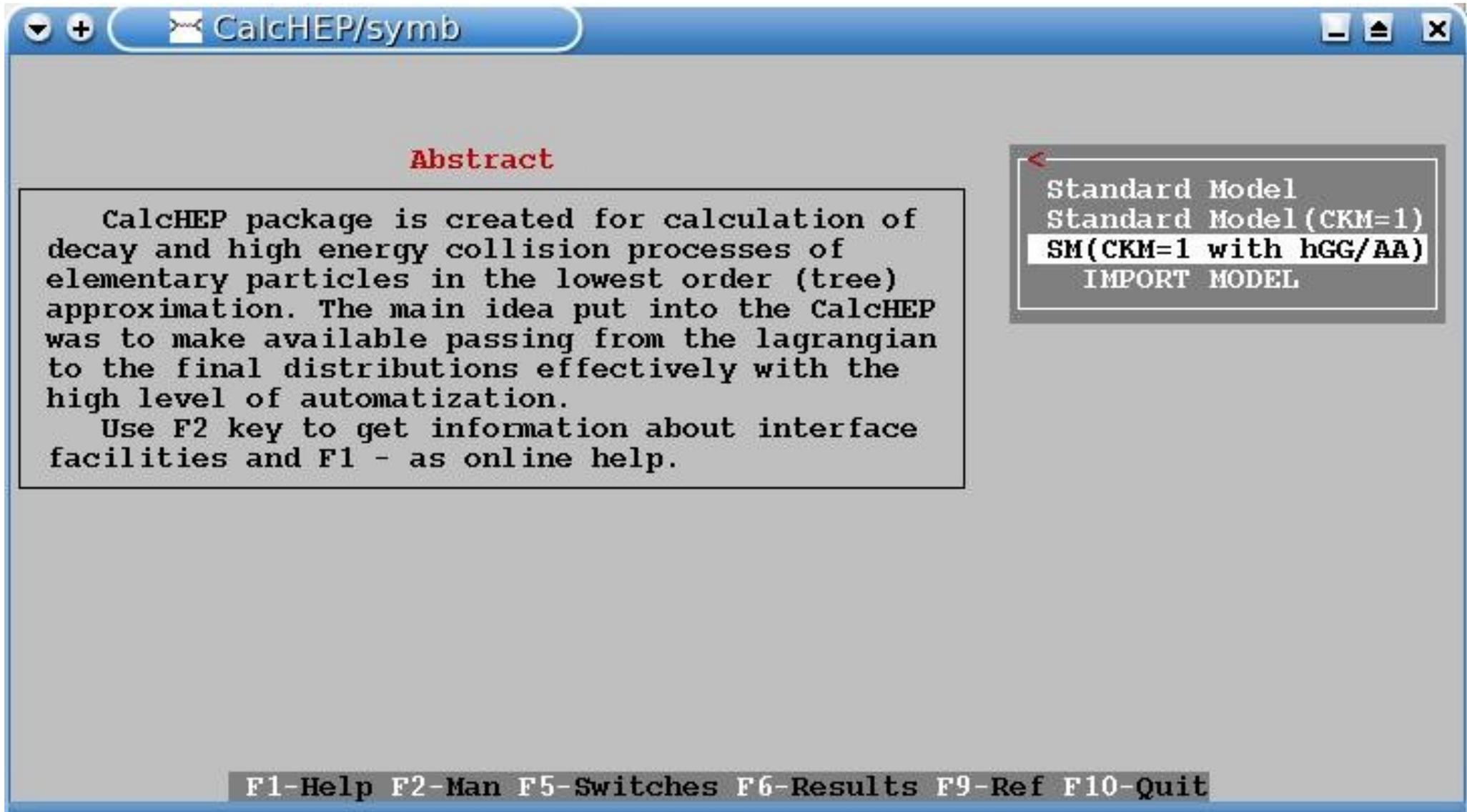
```
cd work  
./calchep
```

Starting batch session

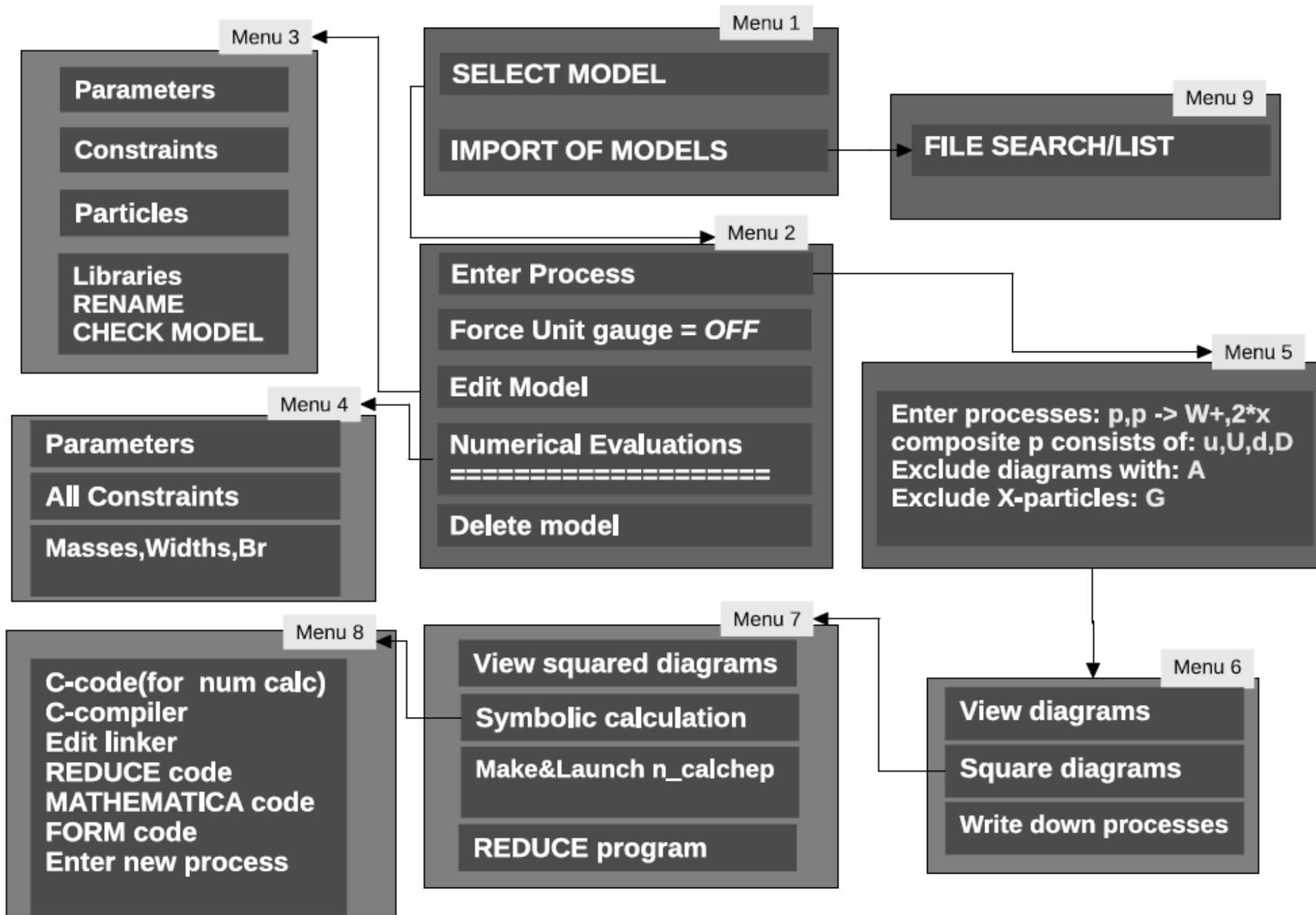
```
cd work  
./calchep_batch batch_file
```

180 pages manual is disposed on CalcHEP web site.

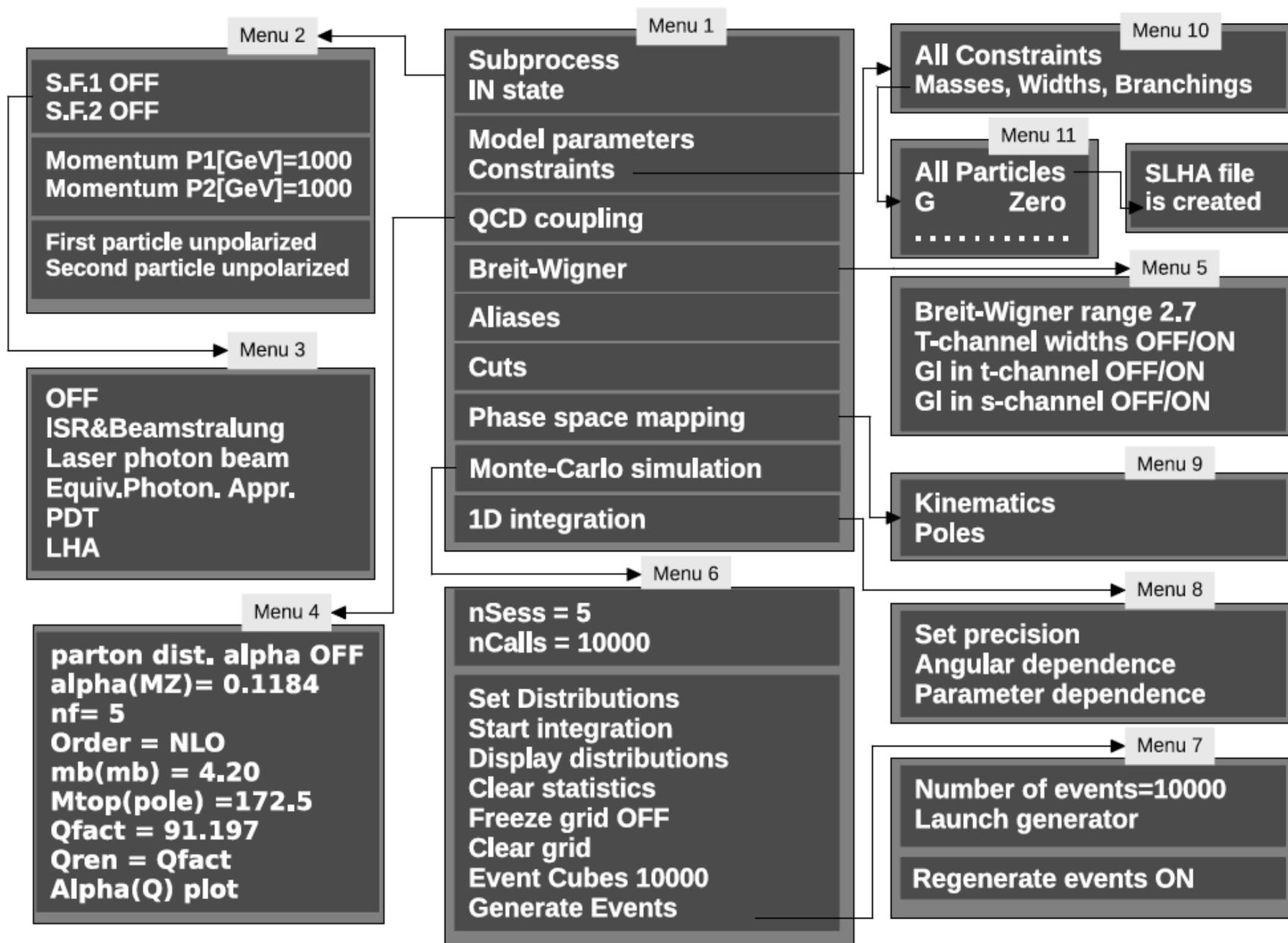
Graphic interface



CalcHEP menu structure: symbolic part



Menu structure of the numerical part



Automatic width calculation

- Code for particle widths are **generated** and compiled in **run time** and **linked dynamically**.
- **1->2, 1->3, 1->4** decays are tested subsequently until open channels are detected.
- To take into account **radiation corrections** of Higgs decay effective quark masses are used:

$$M_q^{\text{Eff}}(Q) \sim M_q^{\text{Run}}(Q/3) \quad \text{where } Q = \text{Higgs Mass}$$

- There is an option to calculate widths for processes with **virtual W/Z**. CalcHEP a) calculates width of process where W is replaced of e^+, ν b) takes into account branching; c) takes into account relation between 1->3 and 1->4 widths.
- **h->G,G** and **G->AA** can be treated via effective vertexes.
- Quite realistic description of Higgs decay can be obtained by this way. SM and MSSM widths and branching where compared with **HDECAY**

H->GG && H->AA for SM, MSSM, ...

Feynman rules

G	G	h		-4*LGGh*Rqcdh		(p1.p2*m1.m2-p1.m2*p2.m1)
G	G	G	h	-4*LGGh*GG*Rqcdh		...
A	A	h		-4*LAAh		(p1.p2*m1.m2-p1.m2*p2.m1)

Constraints

aQCDh		alphaQCD(Mh)/pi
Rqcdh		sqrt(1+149/12*aQCDh+68.6482*aQCDh^2-212.447*aQCDh^3)
LGGh		-cabs(hGGeven(Mh, aQCDh, 3, % spin/2, color, mass, coupling 1, 3, Mtp, 1/VEV, 1, 3, Mbp, 1/VEV, 1, 3, Mcp, 1/VEV))
Quq		4/9
Qdq		1/9
LAAh		-cabs(hAAeven(Mh, aQCDh, 2, % spin/2, color, mass, coupling 2, 1, MW, 2/VEV, 1, 1, Ml, 1/VEV) +Quq*hAAeven(Mh, aQCDh, 2, 1, 3, Mtp, 1/VEV, 1, 3, Mcp, 1/VEV) +Qdq*hAAeven(Mh, aQCDh, 1, 1, 3, Mbp, 1/VEV))

QCD NLO corrections are included.

LanHEP for H->GG & H->AA

At level of model generation LanHEP has a function `CoefVrt`

`_h=[h,H], _p=[c,b,t,1]` in parameter `a_hF__p`
`=CoefVrt([anti(_p),_p,_h]) / (mass _p)`.

which selects a coupling at vertex. When

`LG Gh = -cabs(hGGeven(M_h, aQCD_h, 3,`
`1, 3, Mbp, a_hF_b, 1, 3, Mcp, a_hF_c, 1, 3, Mtp, a_hF_t)`
`).`

For odd Higgs one can use

`CoefVrt([anti(_p),_p,_h],[gamma5,im])`

One create *decaySLHA.txt* file which contains quantum numbers, masses, widths, and branching for all particles or to test properties of each particle separately.

Model: SM(CKM=1 with hGG/AA)

Abstract

CalcHEP package is created for calculation of decay and high energy collision processes of elementary particles in the lowest order (tree) approximation. The main idea put into the CalcHEP was to make available passing from the lagrangian to the final distributions effectively with the high level of automatization.

Use F2 key to get information about interface facilities and F1 - as online help.

Questions: <https://answers.launchpad.net/calchep>

Bugs: <https://bugs.launchpad.net/calchep>

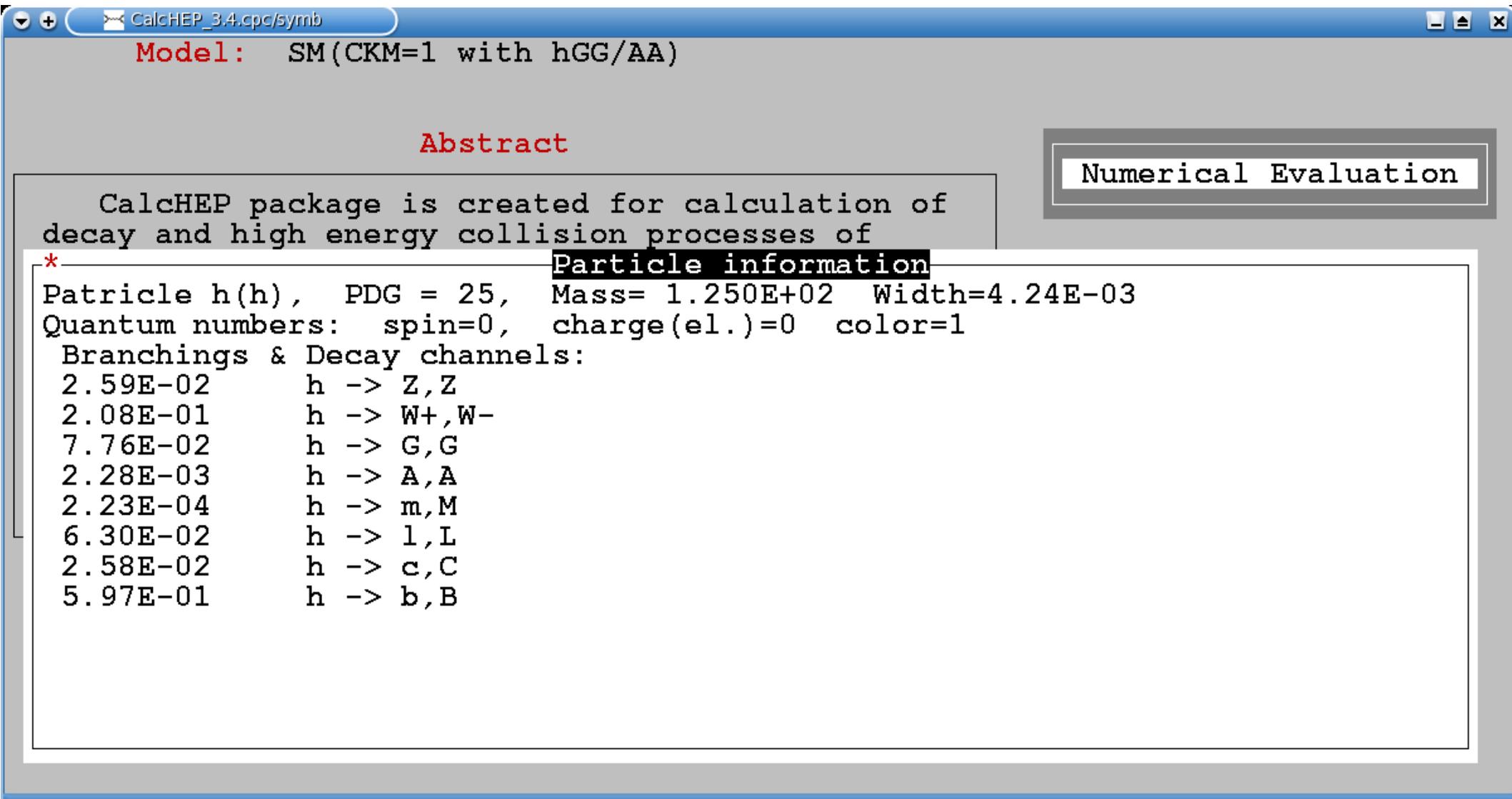
Numerical Evaluation

All Particles -> SLHA	
G	Zero
A	Zero
Z	9.1188E+01
W+	8.0385E+01
h	1.2500E+02
e	Zero
ne	Zero
m	1.0570E-01
nm	Zero
l	1.7770E+00
nl	Zero
d	Zero
u	Zero

PgDn

F1-Help F2-Man F5-Switches F6-Results F9-Ref F10-Quit

Higgs decay



CalcHEP_3.4.cpc/symb

Model: SM(CKM=1 with hGG/AA)

Abstract

CalcHEP package is created for calculation of decay and high energy collision processes of

Numerical Evaluation

*** Particle information**

Particle h(h), PDG = 25, Mass= 1.250E+02 Width=4.24E-03
Quantum numbers: spin=0, charge(el.)=0 color=1

Branchings & Decay channels:

2.59E-02	h -> Z,Z
2.08E-01	h -> W+,W-
7.76E-02	h -> G,G
2.28E-03	h -> A,A
2.23E-04	h -> m,M
6.30E-02	h -> l,L
2.58E-02	h -> c,C
5.97E-01	h -> b,B

Model implementation: SLHAplus

SLHAplus is a library of auxiliary functions used for model realization. Now it includes

a) **functions for SLHA interface (file exchange):**

`slhaRead(fileName, mode)`

`slhaVal(BlockName, Scale, N_key_symbols, keys ...)`

Example:

Block MASS

25 125

`Mh=slhaVal("MASS", 0.,1,25)`

BLOCK STAUMIX # Stau Mixing Matrix

1 1 4.86991070E-02 # cos(theta_tau)

1 2 9.98813495E-01 # sin(theta_tau)

2 1 -9.98813495E-01 # -sin(theta_tau)

`ZI12=slhaVal("STAUMIX", QSUSY, 2, 1, 2)`

If `mode&4==0` SLHA width is used instead of automatic width calculation

SLHAplus: other functions

b) **functions for diagonalizing of mass matrices** : i) real symmetric ii) hermitian; iii) complex; iv) complex symmetric. based of Jacobi algorithm (arXiv:1008.0181). Special

```
NeDiag |rDiagonal(4, MG1, zero, -MZ*SW*cb, MZ*SW*sb, MG2, MZ*CW*cb,
              -MZ*CW*sb, zero, -mu, zero)
MNE1   |MassArray(NeDiag, 1)
MNE2   |MassArray(NeDiag, 2)
Zn11   |MixMatrix(NeDiag, 1, 1)
Zn12   |MixMatrix(NeDiag, 1, 2)
```

c) Functions to construct effective hGG and hAA vertices at NLO level **HGGEven/Odd** and **hAAEven/Odd** presented above.

d) **QCD functions** for running alpha QCD, masses, effective Yukawa couplings.

Effective vertices

CalcHEP allows only 3 and 4 legs vertices with limited types of color structures

$\bar{3}\bar{3}$, $3\bar{3}\bar{8}$, $8\bar{8}$, $8\bar{8}\bar{8}$, $3\bar{3}\bar{3}$, $\bar{3}\bar{3}\bar{3}$, $6\bar{6}$, $6\bar{6}\bar{8}$, $3\bar{3}\bar{6}$, $\bar{3}\bar{3}\bar{6}$

Auxillary field with point-like propagator can be used to construct multi-leg vertices and vertices with other color structures. Usually LanHEP solves this problem. Suppose we need $L = k\bar{t}\sigma_{\mu\nu}\hat{\lambda}^a t \cdot F_a^{\mu\nu}$ Then in terms of LanHEP

item $k*i/2*T*gamma^mu*gamma^nu*lambda^a*t*$
 $(deriv^mu*G^nu^a-deriv^nu*G^mu^a+i*GG*f_{SU3}^a^b^c*G^mu^b*G^nu^c)$.

Interaction

P1	p2	p3	p4	totFcat	Lorentz part
T	t	G		k/2	G(p3)*G(m3)-G(m3)*G(p3)
G	G	~01.t		1/2	m1.m3*m2.M3-m1.M3*m2.m3
T	t	~00.t		k*GG	G(M3)*G(m3)

Particles

P	aP	PDG	spin2	mass	width	color	aux	*	!
~00	~01		2	Maux	0	8	!*	*	!

* - point-like prop
 ! - self conjugation

Available [B]SM models

SM, IDM – included in CalCHEP distribution.

MSSM, NMSSM, CPVMSSM – calchep web page
and micrOMEGAs

LHM, UMSSM, Z3M, Z4M - micrOMEGAs

Structure functions

- **CalcHEP contains several build-in structure functions for e^+e^-**
ISR+Beamstrahlung
Equivalent photo approximation
Laser photons
- **Link with LHAPDF5 and LHAPDF6**
`export LHAPDFPATH=path_to_LHAPDF_library`
One should see
`ls $LHAPDFPATH/libLHAPDF.so`
If `LHAPDFPATH` is not defined then **dummy** library is linked.
- One can export **LHAPDF6** tables into CalcHEP
`CalcHEP/bin/lhapdf2odt LHAPDF6/share/LHAPDF/CT10 0`
creates file `CN10:0.pdt` for `CalcHEP/pdTables`
- By default `CalcHEP/pdTables` contains
`CT10.pdt` `NNPDF23_lo_as_0130.LHgrid.pdt`
`cteq6l1.pdt` `MRST2004qed_proton.pdt`
`NNPDF23_lo_as_0130_qed.pdt`

There is a way to compare different structure functions.

```
(sub)Process: s, S -> m, M  
Monte Carlo session: 1(begin)
```

IN state

```
#IT Cross section[pb] E
```

```
S.F.1: LHA:CT10:0:1
```

```
S.F.2: LHA:cteq6l1:0:1
```

```
First particle momentum[GeV]
```

```
Second particle momentum[GeV]
```

```
First particle unpolarized
```

```
Second particle unpolarized
```

PDF plots

x-Min = 1.000E-05

x-Max = 1.000E+00

q-Min = 1.500E+00

q-Max = 1.000E+04

Npoints = 100

q0 = 91.19GeV

x0 = 1.00E-01

log scale argument ON

Display plot x*F(x)

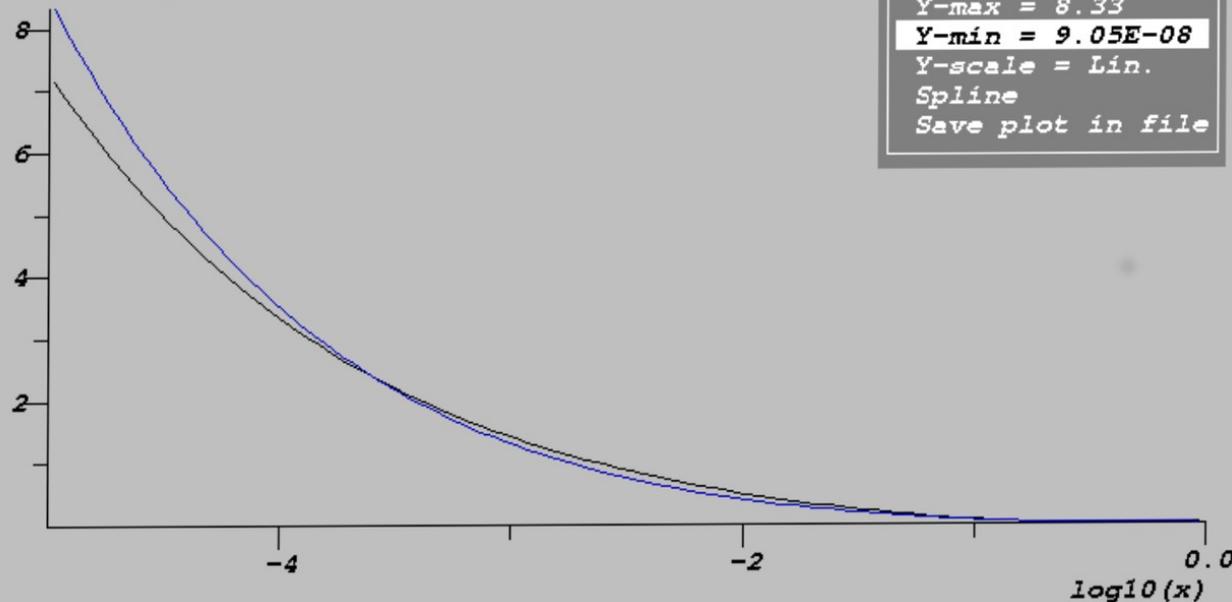
Display plot F(x)

Display plot F(Q)

both PDF1&PDF2 ON

x*F(x, Q=9.12E+01)

pdf1(s); pdf2(S);



Y-max = 8.33
Y-min = 9.05E-08
Y-scale = Lin.
Spline
Save plot in file

Mouse: log10(x)=-3.23E+00 pdf1(s)=1.73E+00 pdf2(S)=1.65E+00

F1-Help F2-Man F5-Options F6-Results F8-Calc F9-Ref

List of built-in functions for QCD scale cuts and distributions.

- A** - Angle in degree units
- C** - Cosine of angle
- D** - Jet separation $\min(p_{T1}^2, p_{T2}^2) * (\cosh(d_{\text{Rapidity}}) - \cos(d_{\text{AzimuthAngle}}))$
- J** - Jet cone angle
- E** - Energy of the particle set
- M** - Mass of the particle set
- P** - Cosine of the angle between the first particle in the list and the direction of boosting of the particle set into the rest frame of the particles set
- T** - Transverse momentum (P_t) of the particle set
- Y** - Rapidity of the particle set
- N** - Pseudo-rapidity of the particle set
- Z** - Transverse energy

U*user* user defined function via `usrfun("user")`

Aliases, Cuts, Distributions

Subprocess
IN state
Model parameters
Constraints
QCD coupling
Breit-Wigner
Aliases
Cuts
Phase space mapping
Monte Carlo simulation

In case of **identical** particles constructing distributions **F** CalcHEP normally **sums** all possibilities. But **F^(F`)** and **F_** evaluate **max** and **min** values.

If cut/distribution can not be realized, then it is ignored.

Composites				
Clr	Del	Size	Read	ErrMes
				Name > Comma separated list of particles
p*				G,d,D,u,U,s,S,c,C,b,B

Cuts					3
Clr	Del	Size	Read	ErrMes	
!		Parameter	> Min bound < >	Max bound <	
T(p*)			50		
J(p*,p*)			0.5		
N(p*)			-5		5

Distributions						
Clr	Del	Size	Read	ErrMes		
Parameter_1 >	Min_1	< >	Max_1	< Parameter_2 >	Min_2	< >
T(b)	10		1200			
T(B)	10		1200			
N(b)	1-5		15			
N(B)	1-5		15			
M(b,B)	10		1500			
M(W+,b)	10		1500			
T(b)	10		1500	IM(b,B)	10	1500

Definition of QCD scale

Suppose one would like to calculate cross section
 $p, p \rightarrow \text{Jet}, dm, dm$
for scale

$$Q = 0.5 * (PT(\text{JeT}) + ME).$$

It can be done by one definition for all subprocesses

$$Q = 0.5 * (T("p*") + Z("dm", "dm"))$$

Integration and generation of events

Slightly improved Vegas with thread paralleling is used for integration and events generation

- First Vegas cycle is used for grid adaptation.
- Second Vegas cycle is used to get profile of integrand – find maxima of for subcubes and estimate efficiency of events generation. Filling of histograms.
- **Events generation.** Events have weights \sim cross section of process. If Vegas finds a point where integrand exceeds maximum detected on step 2 then weight increased **or** more events are generated in the given sub-cube.

Files generated in Monte Carlo session

Monte Carlo session generates `distr_N` file which contains distributions. N is session number which increases automatically when user changes parameters.

- `$CALCHEP/bin/show_distr distr_N`

allows to display distribution. CalcHEP creates plot which can be saved in PAW, GNUPLOT, and ROOT formats.

- `$CALCHEP/bin/sum_distr distr_N1 distr_N2 ... > distr_sum`

creates sum of distributions obtained in different sessions.

Monte Carlo session generates `event_N` files. To make a summary LHE file (subprocesses summation and decays implementation) one can use

- `$CALCHEP/bin/event_mixer Luminosity nEvents directories`

Resulting file is `events_mixer.lhe` . File `decaySLHA.txt` (if it exists) is added to define q-numbers, widths, and branching of BMS particles.

Simple batch scripts.

CalcHEP/bin directory contains several scripts which performs cycle calculations in batch mode

name_cycle pcm_cycle subproc_cycle par_scan
par_scan_sum

They have to be launched from *work/results* directory where *n_calchep* compiled in symbolic session is disposed. For example,

```
../bin/subprocess_sycle Nevents
```

performs cycle over all subprocesses and generates LHE file with information about decays of BSM particles. These scripts really See explanation in [CALCHEP/bin/README](#) or in manual.

The **calchep_batch** program

- All steps of calculation can be done in batch mode by one command

```
./calchep_batch <input file>
```
- Control of calculation can be done via WEB browser. Before calculation the program writes on the screen name of **html** file. For example:

Open the following link in your browser:

file:///home/pukhov/CALCHEP/calchep_3.6.28/work/html/index.html

- One can use parallel calculation of batch task on PS farm.

Example of input file for calchep_batch command

Model: Standard Model(CKM=1)
Model changed: False
Gauge: Feynman

Process: p,p->W,b,B
Decay: W->le,n
Composite: p=u,U,d,D,s,S,c,C,b,B,G
Composite: W=W+,W-
Composite: le=e,E,m,M
Composite: n=ne,Ne,nm,Nm
Composite: jet=u,U,d,D,s,S,c,C,b,B,G

pdf1: cteq6l 1(proton)
pdf2: cteq6l 1(proton)
p1: 4000
p2: 4000

Run parameter: Mh
Run begin: 120
Run step size: 5
Run n steps: 3

alpha Q : M45

Cut parameter: M(b,B)
Cut invert: False
Cut min: 100

Dist parameter: M(b,B)
Dist min: 100
Dist max: 200
Dist n bins: 100
Dist title: p,p->W,b,B
Dist x-title: M(b,B) (GeV)

Dist parameter: M(W,jet)
Dist min: 100
Dist max: 200
Dist n bins: 100
Dist title: p,p->W,b,B
Dist x-title: M(W,jet) (GeV)

Number of events (per run step): 10000
Filename: pp_Wbb_enbb

nSess_1: 5
nCalls_1: 100000
nSess_2: 5
nCalls_2: 100000

#Parallelization method: local
Parallelization method: pbs

Max number of nodes: 2
Max number of processes per node: 2

<http://theory.npi.msu.su/~pukhov/calchep.html>

CalcHEP - a package for calculation of Feynman diagrams and integration over multi-particle phase space.

Authors - Alexander Pukhov, Alexander Belyaev, Neil Christensen

The main idea of CalcHEP is to enable one to go directly from the Lagrangian to the cross sections and distributions effectively, with a high level of automation. The package can be compiled on any Unix platform.

General information

[Main features](#), [Acknowledgments](#), [News&Bugs](#), [Publications&Lectures](#), [Contributions](#)

Manual

[calchep_man_3.3.6.pdf](#) (manual for version 3.3.6, July 19, 2012)

[HEP computer tools](#) (Lecture by Alexander Belyaev)

See also: [Dan Green, High Pt physics at hadron colliders](#) (Cambridge University Press)

Code download.

[Licence](#), [Installation](#), [Current version 3.6.27\(20.07.2016\)](#), [Archive](#)

Models:

[MSSM_10.14\(15.10.2014\)](#), [NMSSM_8.15\(25.08.2015\)](#), [CPVMSSM_10.14\(16.10.2014\)](#), [SUSY models By A.Semenov](#), [LeptoQuarks](#), [5DSM](#), [6DSM](#)

Model database [HEPMDB](#)

Related packages on Web:

Packages for model generation: [LanHEP](#), [FeynRules](#), [SARAH](#)

RGE and spectrum calculation: [SuSpect](#), [Isajet](#), [SoftSUSY](#), [SPHeno](#), [CPsuperH](#), [NMSSMTools](#)

Particle widths in MSSM: [SUSY-HIT](#), [HDECAY](#)

Parton showers: [PYTHIA](#)

Contacts

Email: calchep@googlegroups.com

Launchpad service: [Ask a question](#), [File a bug](#)

micrOMEGAs

CalcHEP has an option to generate code of matrix elements for other programs.

micrOMEGAs program is created for calculation of Dark Matter observables. It needs matrix elements to calculate cross sections of DM annihilation and its scattering on atomic nuclei. It uses CalcHEP routine

```
numout*cc=newProcess(char*name);
```

For example:

```
newProcess("e,E->m,M");//  $e^-, e^+ \rightarrow \mu^-, \mu^+$ 
```

All matrix elements are generated only one time and stored on disk as shared libraries.

- To calculate matrix element **micrOMEGAs** uses **cc->interface->sqme**(nSubproc,GG,momenta,&errode)
- To get information about particles included in reaction **cc->interface->pinf**(nSubproc,nParticle,&Mass,&PDG)
- To get information about quantum number of particles **cc->interface->pinfAux**(nSubproc,nParticle,
&spin2,&color,&neutral);
- To change numerical numerical value of variables **assignVal**(name,newValue)
- To calculate constraints **calcMainFunc()**
- To check mass and widths:
pMass(pName), **pWidth**(pName, decayList)

micrOMEGAs assumes existence of some discrete symmetry which leads to MD stability, for instance **Z₂**.

Names of particles with non-zero charge have to be started with “~” to help micrOMEGAs to recognize DM sector.

- **sortOddParicles()** calculates constrains, mass spectrum and detects the lightest odd particle, **CDM1**, cold Dark Matter.
 - **micrOMEGAs** calculates **DM relic density**.
 $\Omega h^2 = \text{darkOmega}(\&Xf, \text{Besp}, \text{fast})$
 $X_f = M_{\text{cdm}} / T_{\text{freeze-out}}$ Beps controls co-annihilation.
 - **Direct Detection signal**
nucleonAmplitudes(CMD, AsiP, AsdP, AsiN, AsdN)
 - Signals of **indirect detection**: Spectra of DM annihilation in galactic halo
calcSpectrum(mode, SpA, SpE, SpP, SpNe, SpNm, SpNI, &err)
propagation routines also included in micrOMEGAs.
 - **Neutrino telescope** signal: DM annihilation in the center of Sun/Earth.
neutrinoFlux(DMvelocityDist, forSun[Earth], nuFlux, nuBarFlux)

Astro&Colliders- 1606.03834

Astrophysical and collider BSM signal search.

Mainly based on interface with external packages via SLHA

- *HiggsBounds/HiggsSignals* arXiv 1305.1933, 1311.0055,
- *Lilith* arXiv 1502.04138
micrOMEGAs calculates widths, branching for Higgses and their couplings with SM, passes them to *Lilith/Higgs...* , gets exclusion level
- *masslimits()* checks that at least one BSM particle has a mass larger than LEP limits.
- *Zinvisible()* checks that $\text{width}(Z \rightarrow \text{invisible}) < 0.5 \text{ GeV}$
- *LspNlsp_LEP()* the same in case of small $l_{sp} - N_{lsp}$ mass difference.
- *Smodels* (arXiv 1412.1745) test LHC constraints on Dark Sector particles for models with Z_2 internal symmetry (squarks, sleptons, charginos). *micrOMEGAs* calculates all $p, p \rightarrow \text{Dark Sector (SUSY)}$ reactions, passes them to *SMODELS* with SLHA decay tables and gets exclusion level.