

Echo Tomography of Black Hole Accretion Flows with application to NGC 5548

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24 Oct 2016

Echo Mapping Methods
Continuum reverberations
BLR reverberations
Tilted inner disks ?

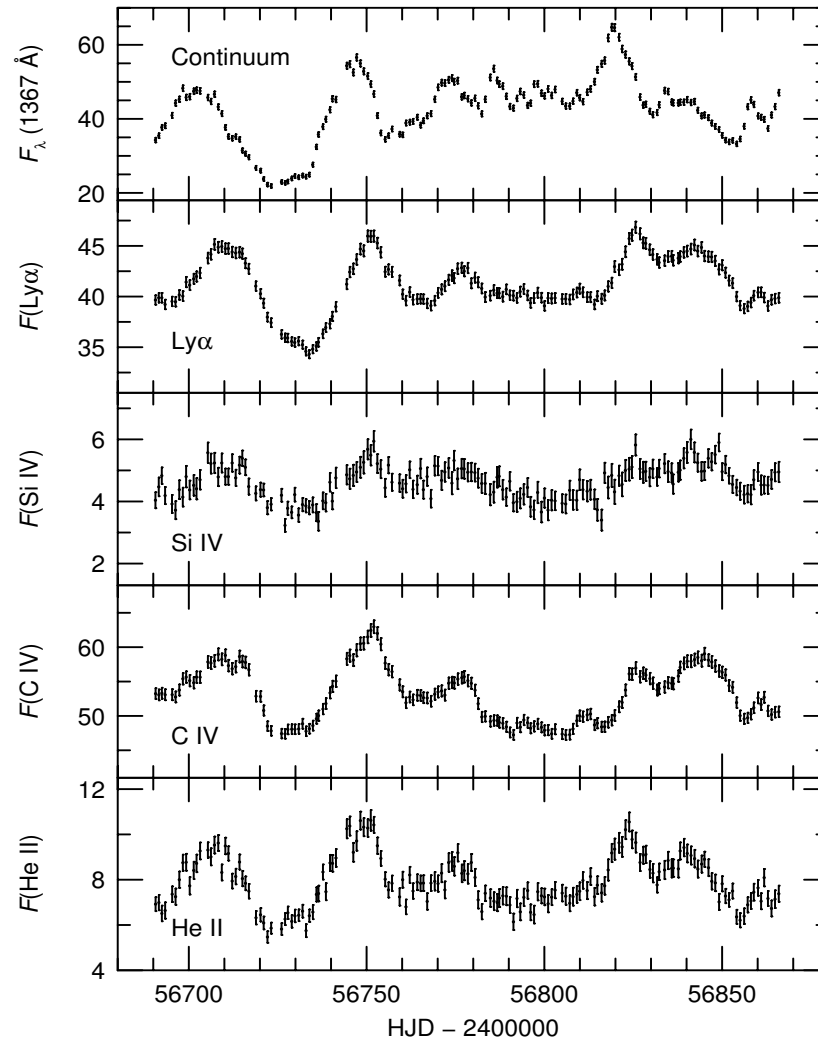
CCF Lags => BLR sizes

AGN STORM HST PROGRAM

Mean lags relative to
1367 Å continuum

Ly α	6.19 ± 0.27 days
Si IV	5.44 ± 0.70 days
C IV	5.33 ± 0.46 days
He II	2.50 ± 0.33 days

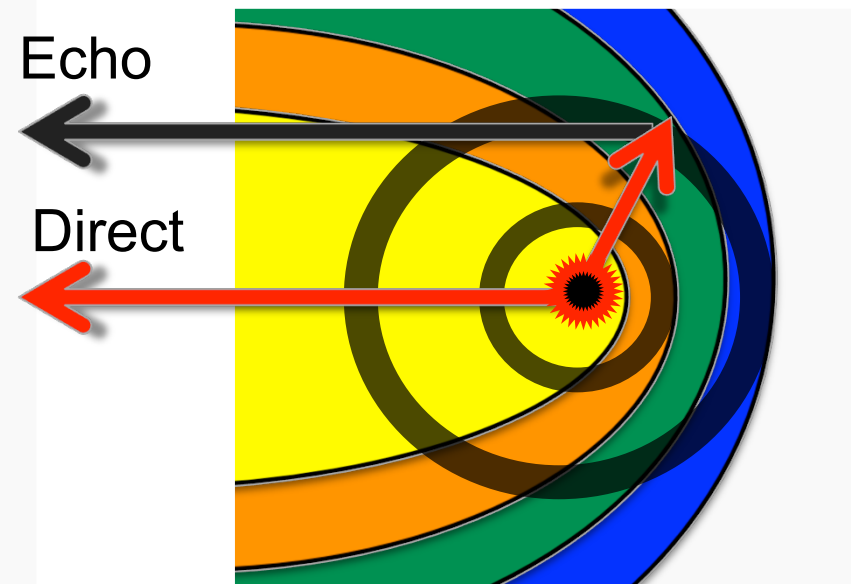
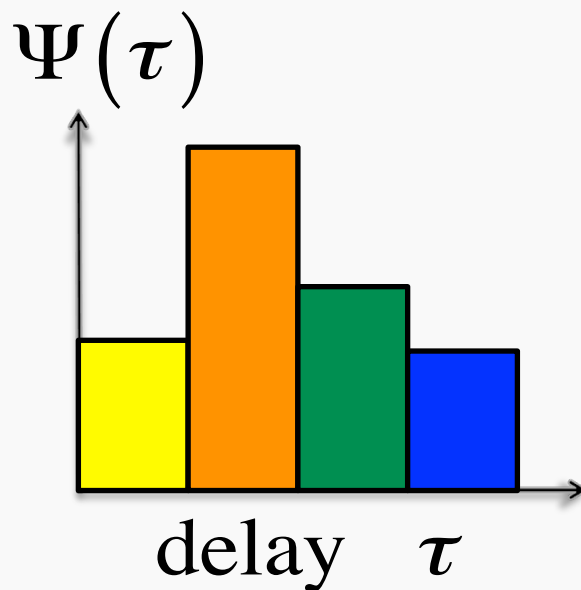
Cross-correlation lags
 $\langle \tau \rangle \sim R / c$
=> radius R of
emission-line region



De Rosa et al, 2015

Beyond CCF lags: Echo Tomography

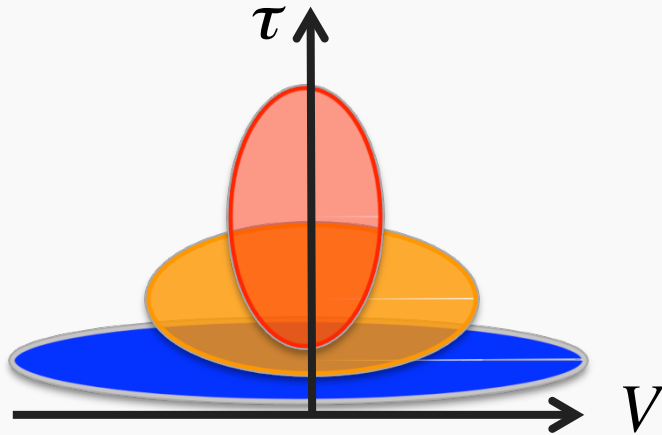
Light travel time delay τ “slices up” the region
on iso-delay paraboloids. => micro-arcsec resolution.



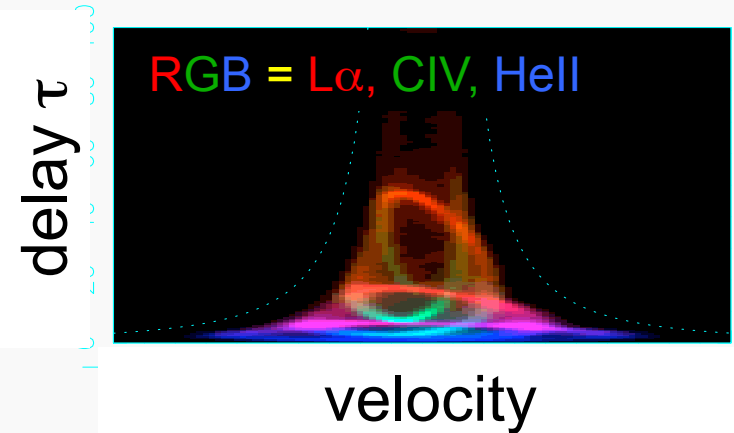
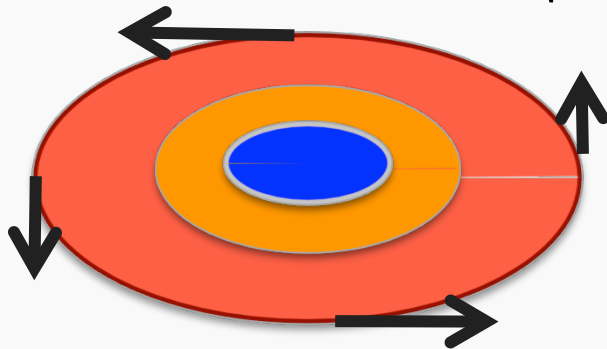
$$\tau = \frac{R}{c}(1 + \cos\theta)$$

2D: Velocity-Delay Maps $\Psi(v, \tau)$

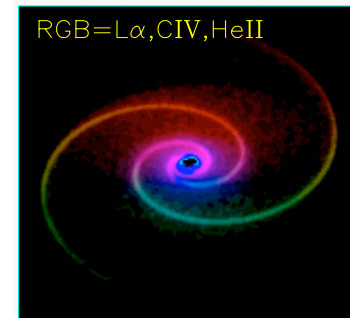
Simulation: Photo-ionised Keplerian disk with spiral density waves



$$\tau = \frac{R}{c} (1 + \sin i \cos \theta) \quad v = \sqrt{\frac{GM}{R}} \sin i \sin \theta$$



sky view:



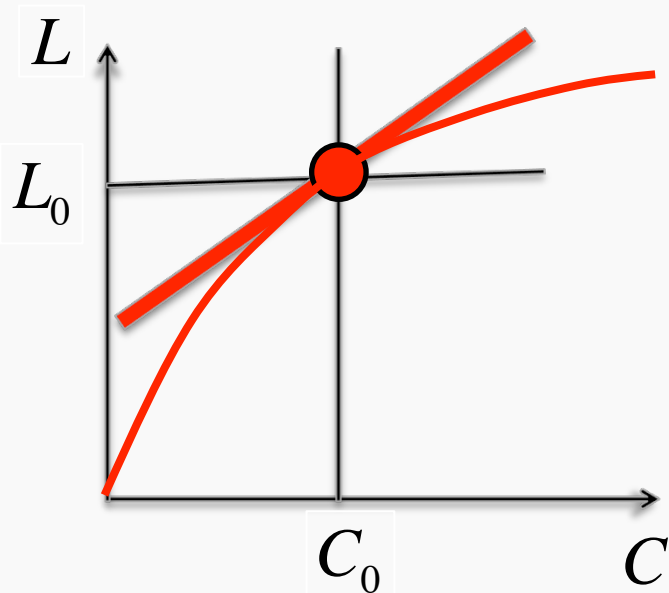
Linearised Echo Model

Lightcurve model:

Continuum: $C(t) = C_0 + \Delta C(t)$

Line: $L(t) = L_0 + \int_0^{\tau_{\max}} \Psi(\tau) \Delta C(t - \tau) d\tau$

model parameters : $C(t), L_0, \Psi(\tau)$.



Tangent-curve approximation
to **non-linear** line responses

Neglects curvature of $L(C)$

MEMEecho fits

Lightcurves => Delay Maps : $\Psi(\tau)$

Emission-Line
Lightcurve

$L(t)$

+

Continuum
Lightcurve

$C(t)$

+

Maximum
Entropy Fit

=

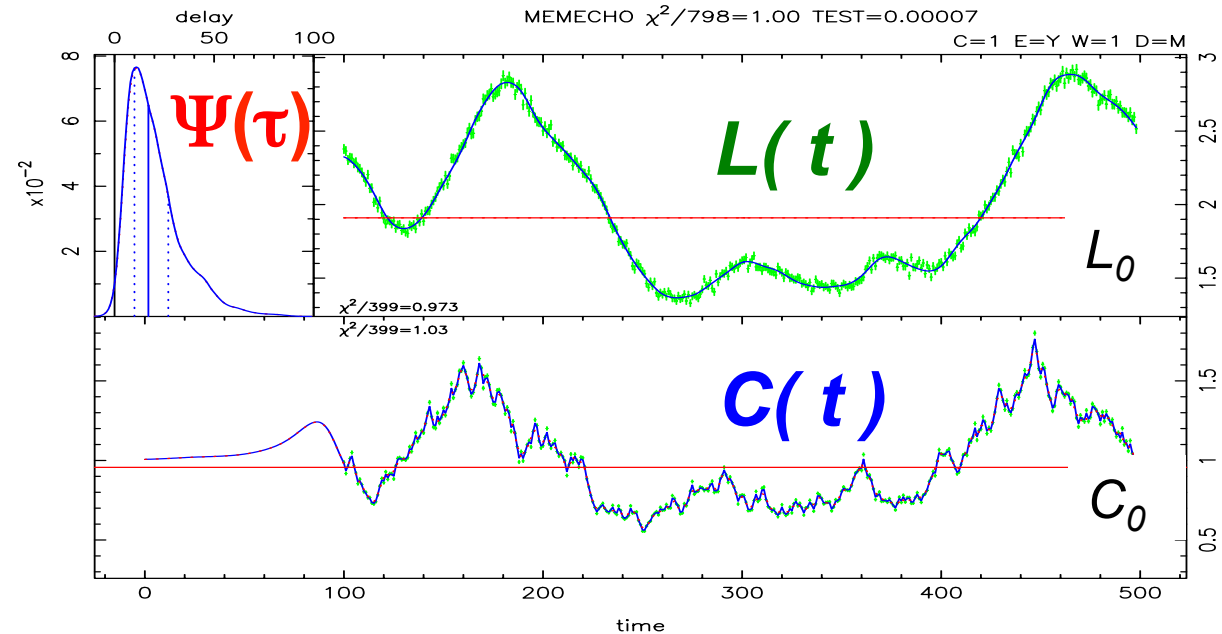
Delay Map

$\Psi(\tau)$

Linearised echo model:

Continuum: $C(t) = C_0 + \Delta C(t)$

Line: $L(t) = L_0 + \int_0^{\tau_{\max}} \Psi(\tau) \Delta C(t - \tau) d\tau$



model parameters : $C(t), L_0, \Psi(\tau)$.

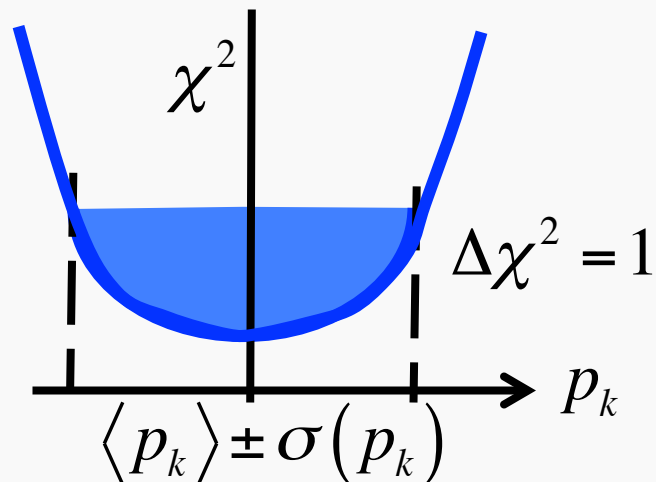
MEMEcho : Maximum Entropy Fits

$$\Pr(\text{Model} | \text{Data}) \propto \exp\{-\chi^2 / 2\} \exp\{\alpha S / 2\}$$

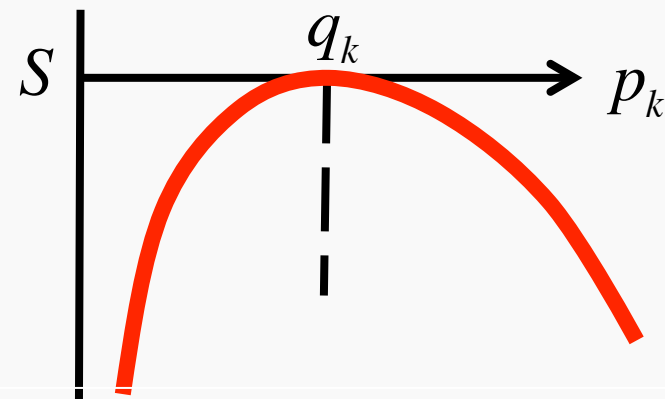
$$\chi^2 = \sum_i^{N_{\text{dat}}} \left(\frac{D_i - \mu_i}{\sigma_i} \right)^2$$

$$S = \sum_k^{N_{\text{pix}}} p_k - q_k - p_k \ln(p_k / q_k)$$

1. Fit the data. $\alpha \Rightarrow 0$



2. Keep it “simple”. $\alpha \Rightarrow \infty$



$p_k > 0$. $S_{\text{max}} = 0$, when $p_k = q_k$.

default values: e.g. $q_k = (p_{k-1} p_{k+1})^{1/2}$

Maximum Entropy Trajectory

Trajectory in parameter space, where $\nabla\chi^2 \propto \nabla S$, parameterised by α .

Simplest Model

$$\alpha \Rightarrow \infty$$

maximum entropy

$$p_k \Rightarrow q_k$$

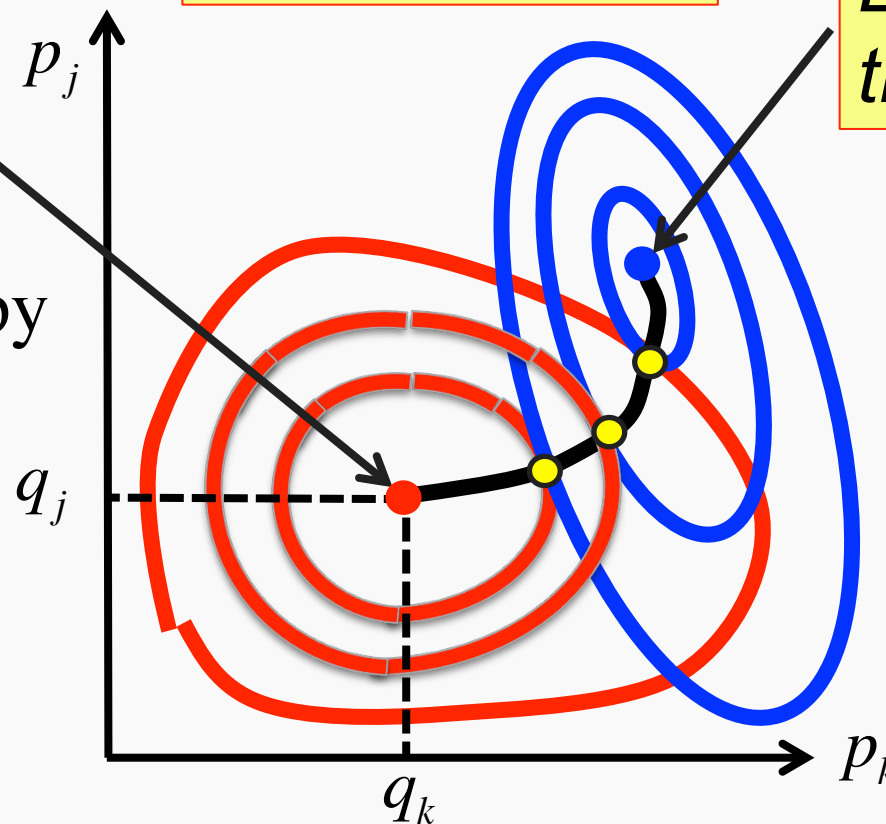
$$S \Rightarrow S_{\max} = 0$$

minimise $\chi^2 - \alpha S$

Best fit to the data

$$\alpha \Rightarrow 0$$

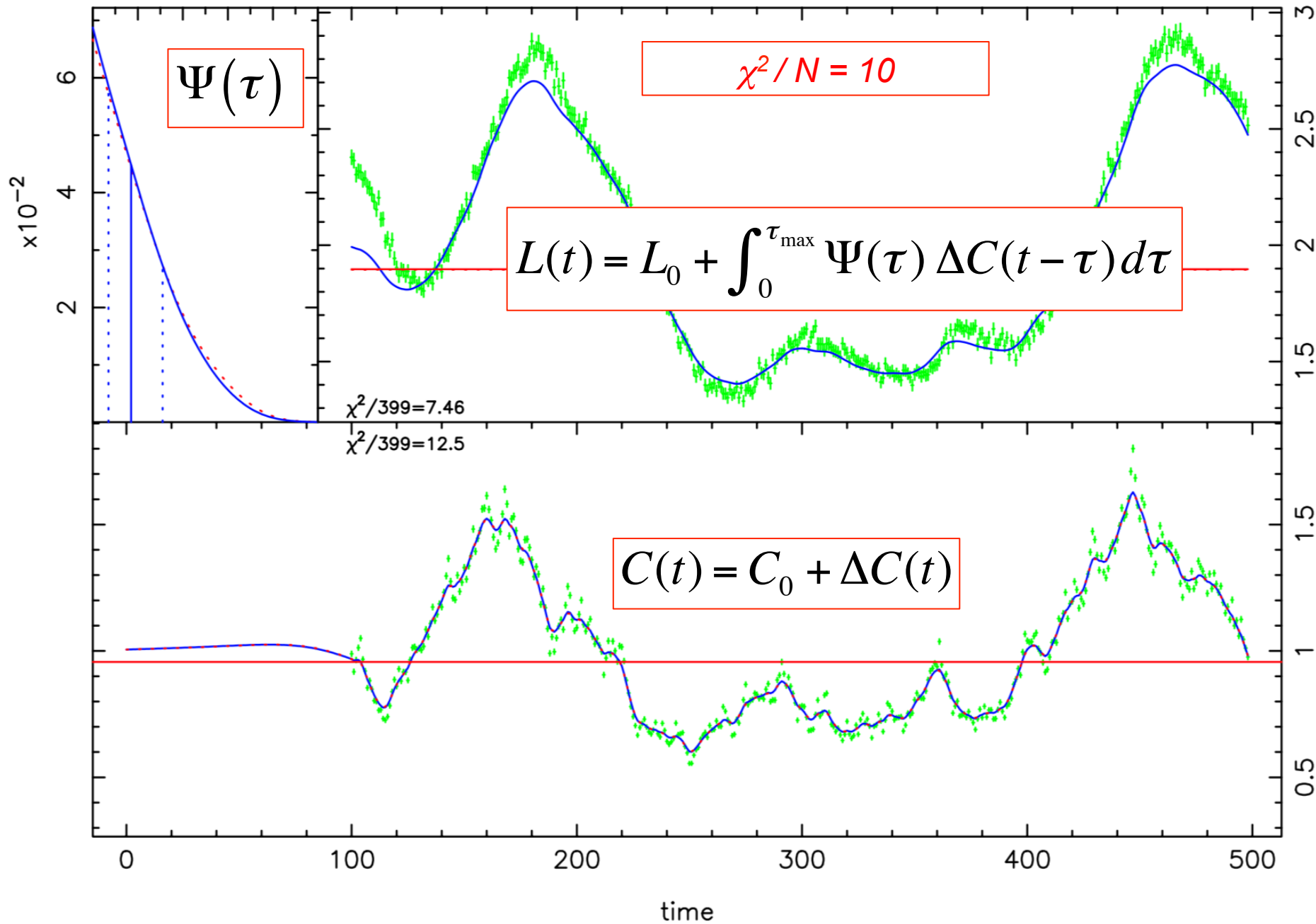
$$\chi^2 \Rightarrow \chi^2_{\min}$$



MEMECHO $\chi^2/798=10.0$ TEST=0.00006

delay
0 20 40 60 80 100

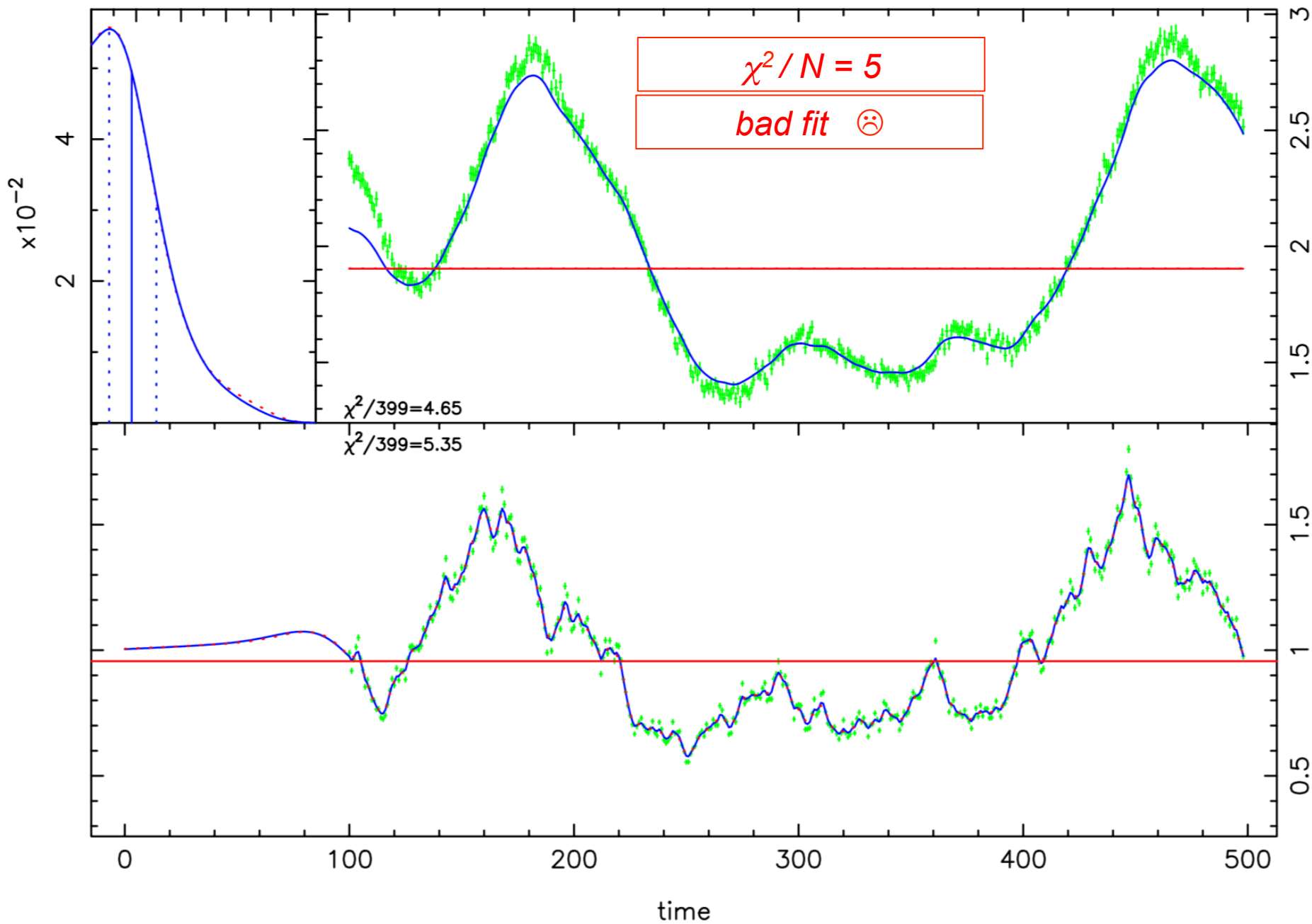
C=10 E=Y W=1 D=M



MEMECHO $\chi^2/798=5.00$ TEST=0.00006

delay
0 20 40 60 80 100

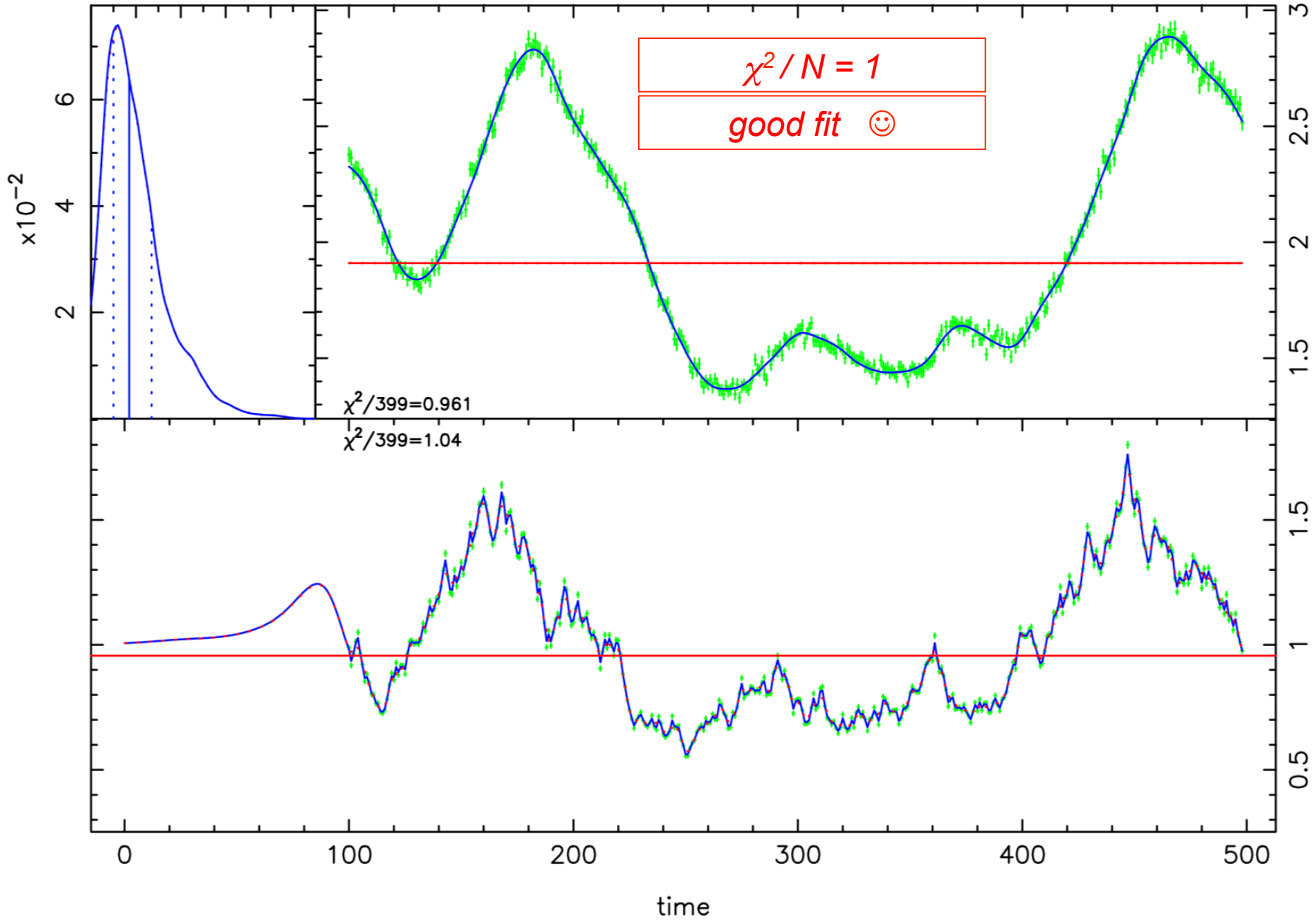
C=5 E=Y W=1 D=M



delay
0 20 40 60 80 100

MEMECHO $\chi^2/798=1.00$ TEST=0.00007

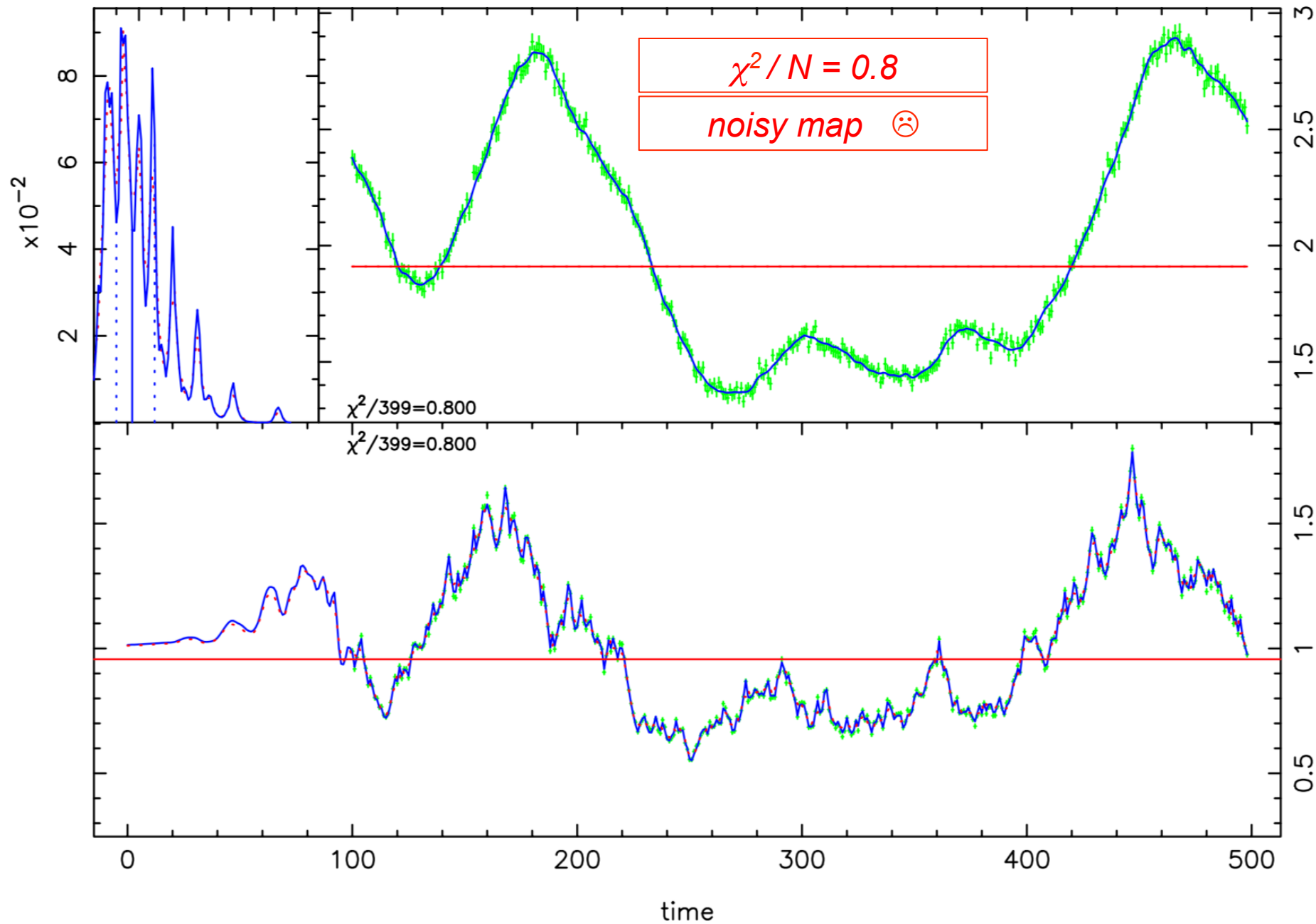
C=1 E=Y W=1 D=M



delay
0 20 40 60 80 100

MEMECHO $\chi^2/798=0.800$ TEST=0.00007

C=0.8 E=Y W=1 D=M



2014 STORM Campaign NGC 5548

STORM = Space Telescope and Optical Reverberation Mapping

PI: Brad Peterson

Published or submitted :

I : *HST*-COS observations – De Rosa+ 2015 ApJ 806:128

II : *Swift-HST* continuum observations.– Edelson+ 2015 ApJ 806:129

III : Continuum interband lags, FUV through z – Fausnaugh+ 2016 ApJ 821:56

IV : Anomalous behavior of UV emission lines – Goad+ 2016 ApJ 824:1

V : Optical emission line variations – submitted, Pei+

VI : [Accretion disk modeling](#) – submitted, Starkey+

In progress or planned :

Heuristic models of the UV emission lines – Kriss+

Chandra X-ray observations – Mathur+

[Velocity-delay maps](#) – Horne+

Dynamical modeling – Pancoast+

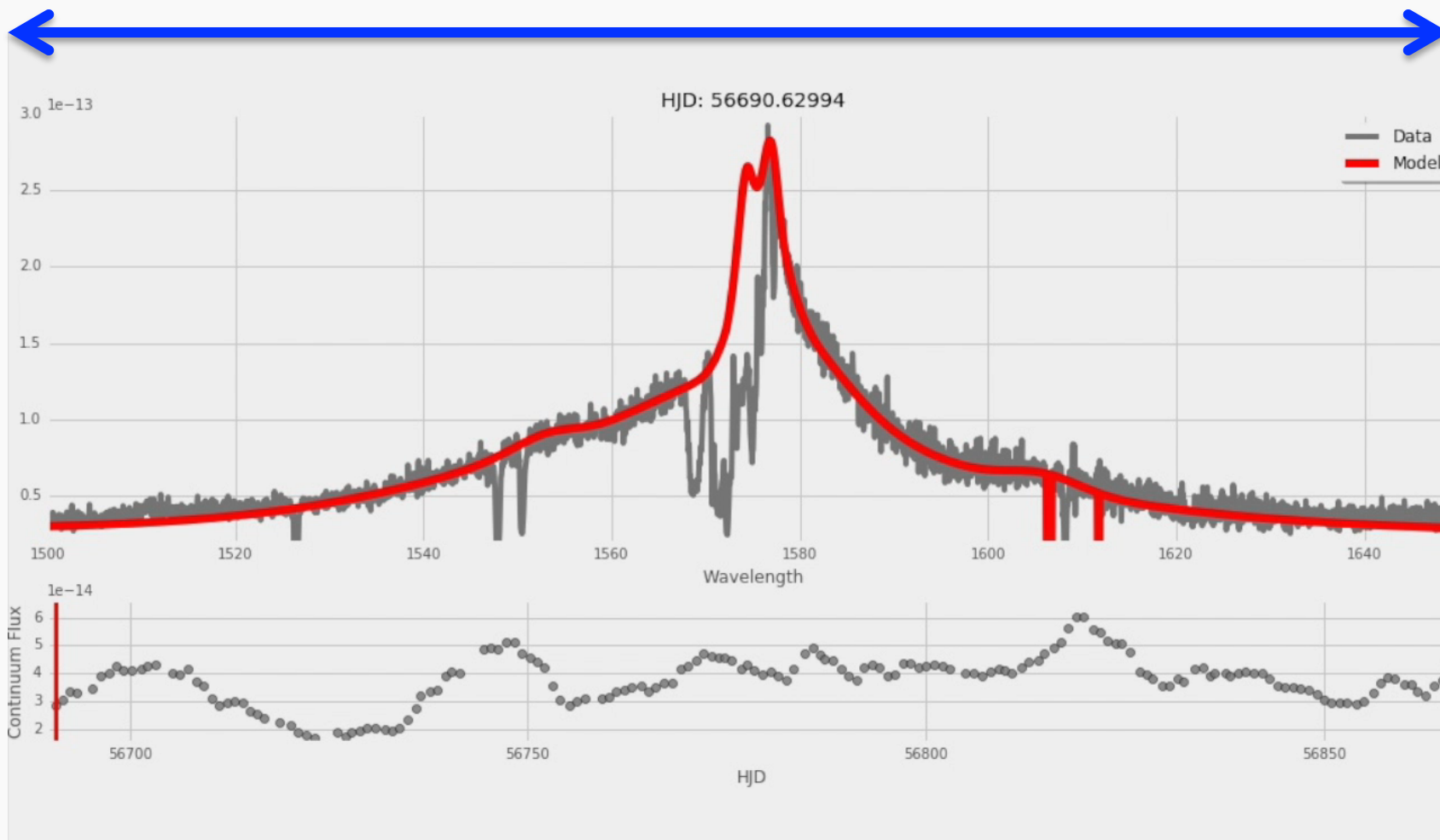
Absorption line variations – Kriss+

Photoionization modeling – TBD

NIR and *Spitzer* observations – TBD

STORM Campaign NGC 5548 C IV Variations

6 months

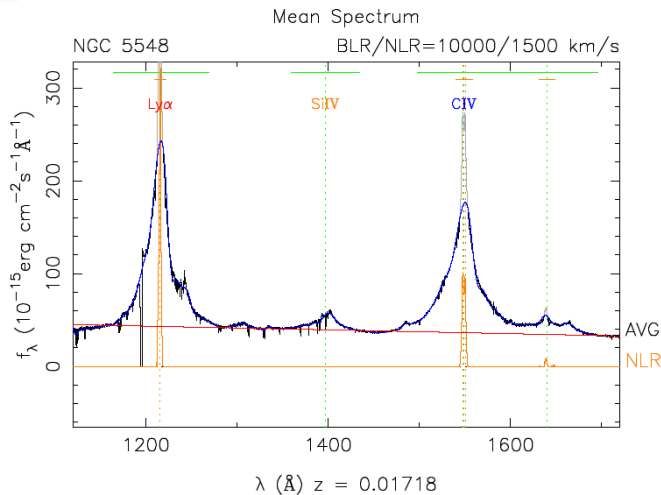


HST : Mean and RMS Spectra Line and Continuum Lightcurves

PrepSpec Analysis of HST data from *De Rosa et al, 2015*.

$A(\lambda)$

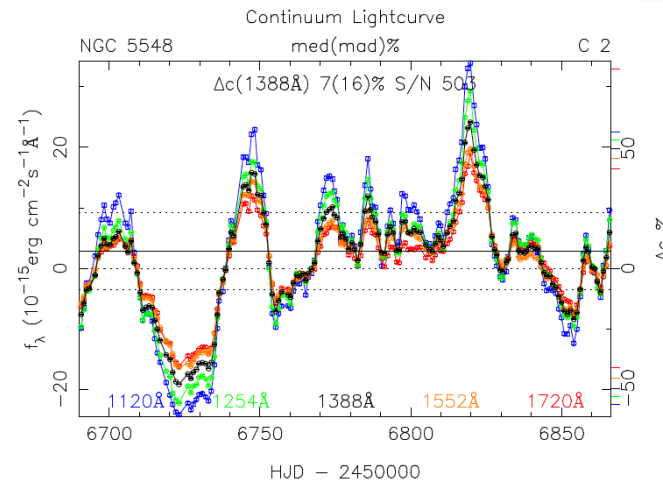
Mean
spectrum



(b)

$C(t|\lambda)$

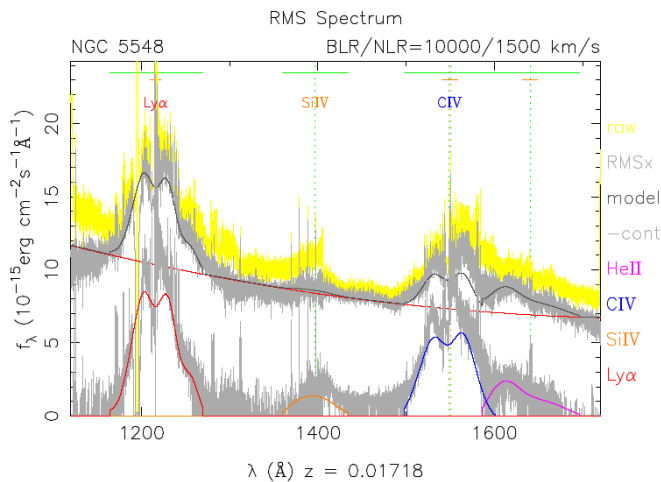
Continuum
lightcurves



(d)

$B(\lambda)$

RMS
spectrum

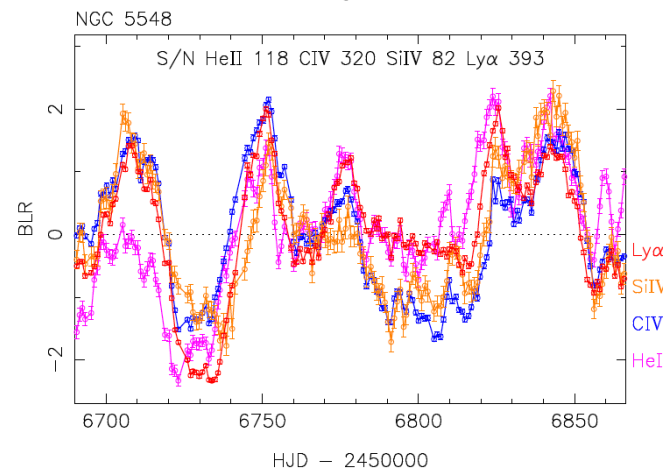


(b)

BLR Lightcurve

$L(t)$

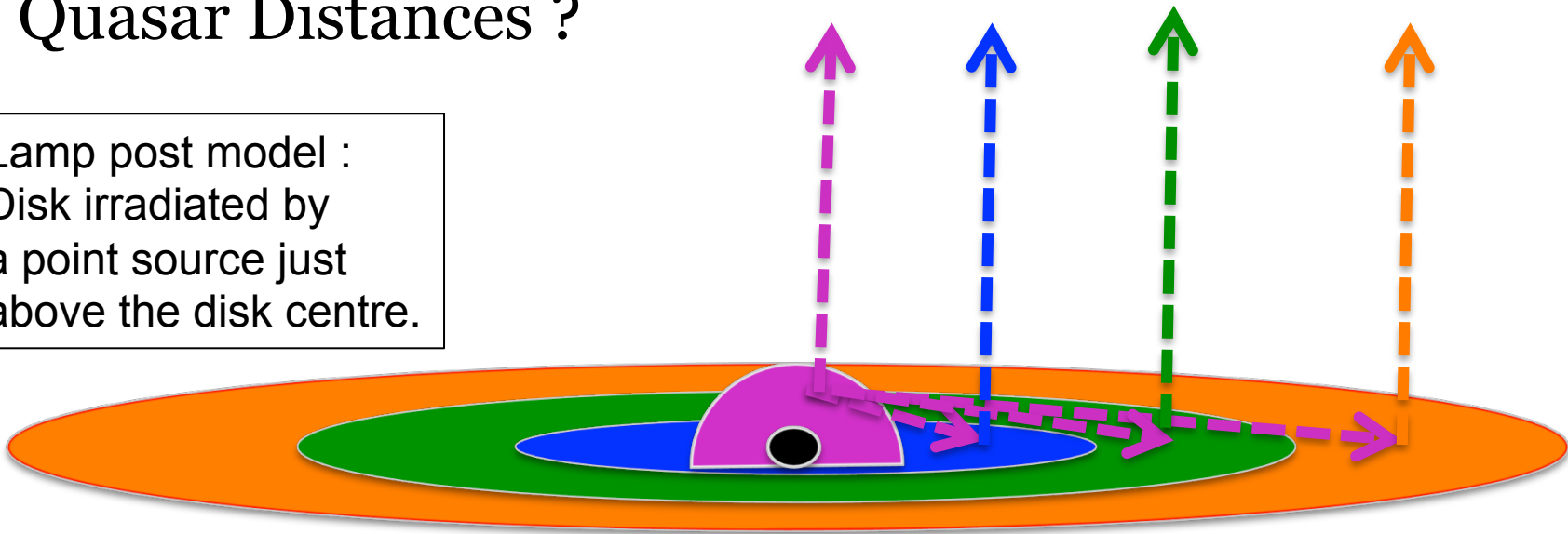
BLR
lightcurves



Continuum Echo Mapping : $T(R)$ profiles of Accretion Disks

- Measure the **time delay spectrum** $\tau(\lambda)$
- To find the **disk temperature profile** $T(R)$
- Test disk models: $T \sim (M \dot{M})^{1/4} R^{-3/4}$
- Measure Mass x Accretion Rate ($M \dot{M}$)
- Quasar Distances ?

Lamp post model :
Disk irradiated by
a point source just
above the disk centre.



Accretion Disk Reverberations

Disk Theory:

$$T \propto (M \dot{M})^{1/4} R^{-3/4}$$

$$L_{\nu} \propto (M \dot{M})^{2/3} \lambda^{-1/3}$$

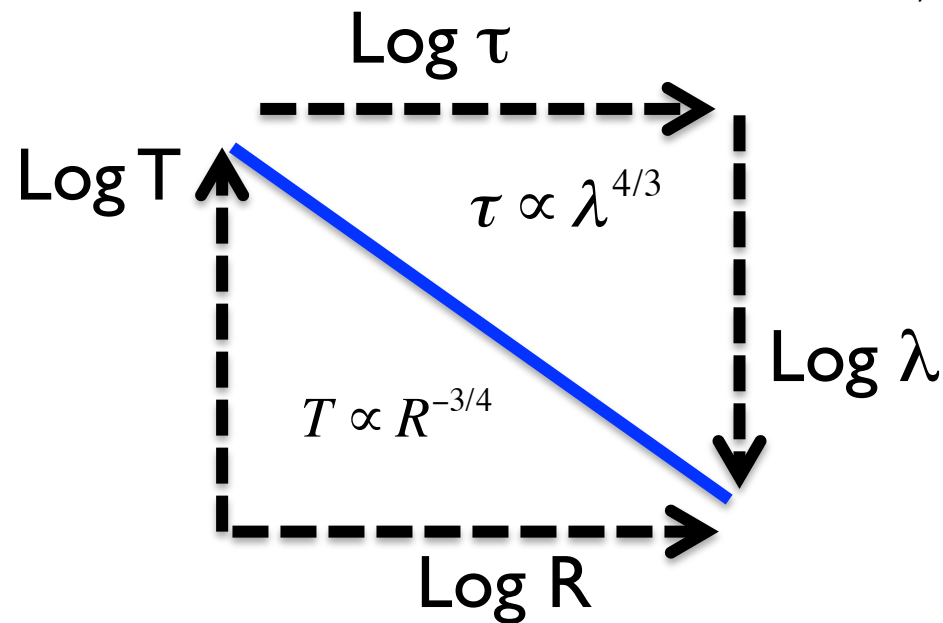
$$R \sim c \tau$$

$$T \sim \frac{hc}{k \lambda}$$

Observables:

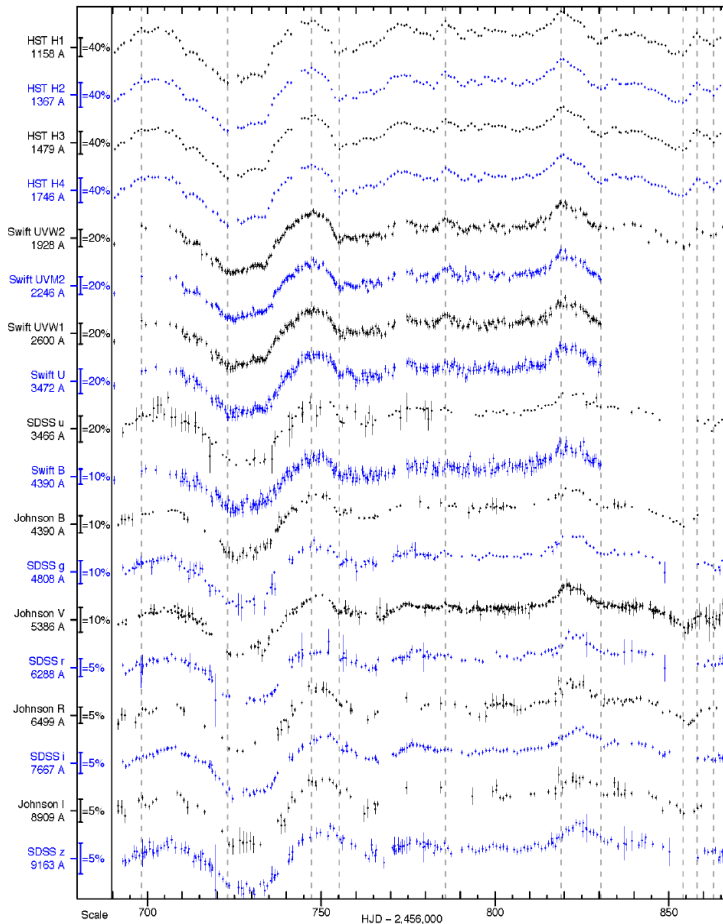
$$\tau \propto (M \dot{M})^{1/3} \lambda^{4/3}$$

$$F_{\nu} \propto L_{\nu} \cos(i) / D^2$$



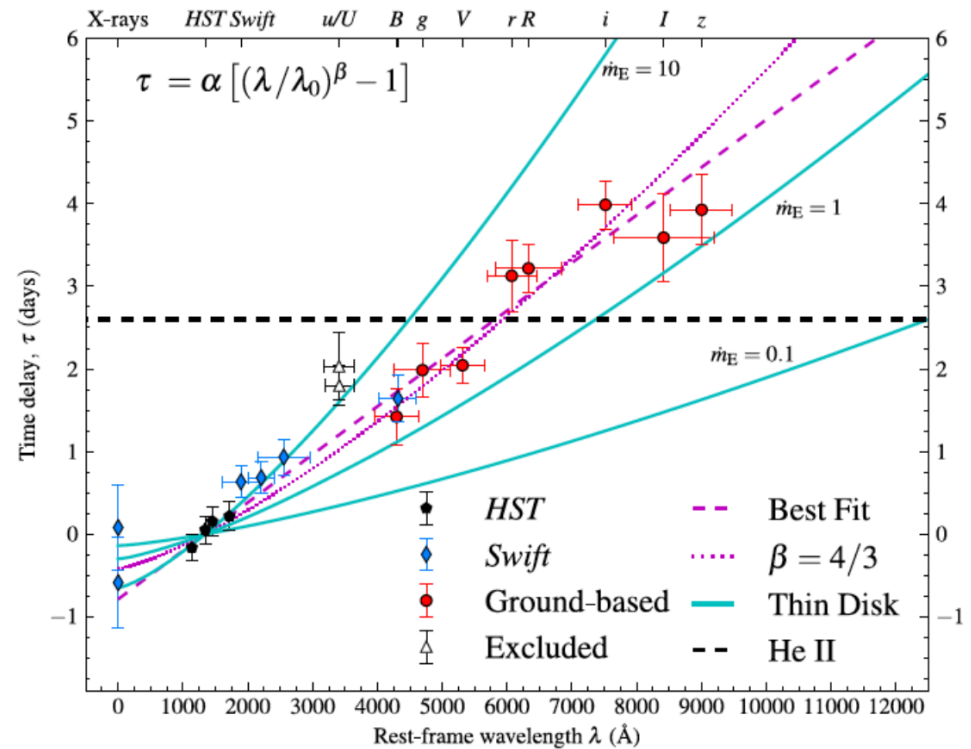
Lightcurves => Delay Spectrum

UV (1150 Å)



Optical (9000 Å)

Keith Horne, SUPA St Andrews

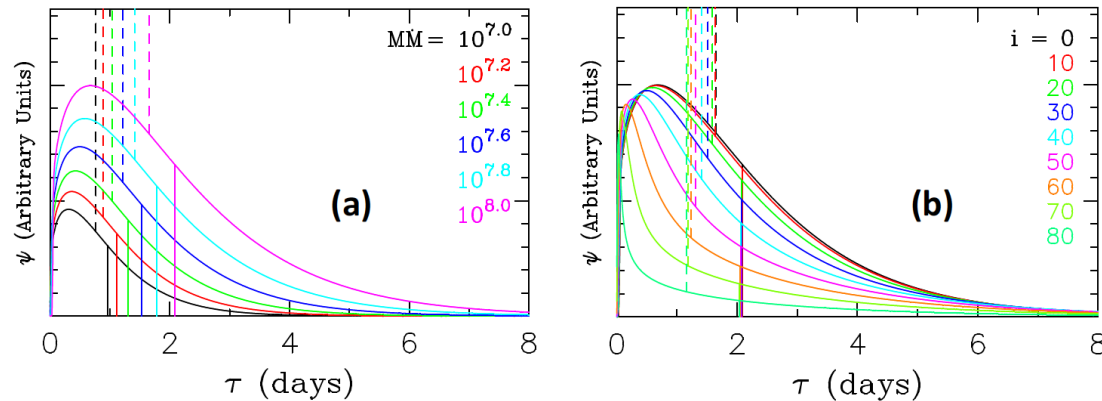


UV lightcurves (HST, Swift)
 Optical lightcurves (LCO+LT+... many telescopes)
 Cross-correlate to find time delay vs wavelength.

Fausnaugh et al. 2016

Lijiang – 2016 Oct 24

Blackbody Disk Delay Maps



Mean delay
 $\tau \sim (M \dot{M})^{1/3} \lambda^{4/3}$
 Independent of
 disk inclination.

Delay map shape
 depends on
 disk inclination

$$\tau(r, \theta) \approx \frac{r}{c} (1 + \sin i \cos \theta)$$

$$T^4(r, t) = \frac{3GM\dot{M}}{8\pi\sigma r^3} + \frac{L_x(t - \tau(r, \theta))(1 - a)h_x}{4\pi\sigma r^3}$$

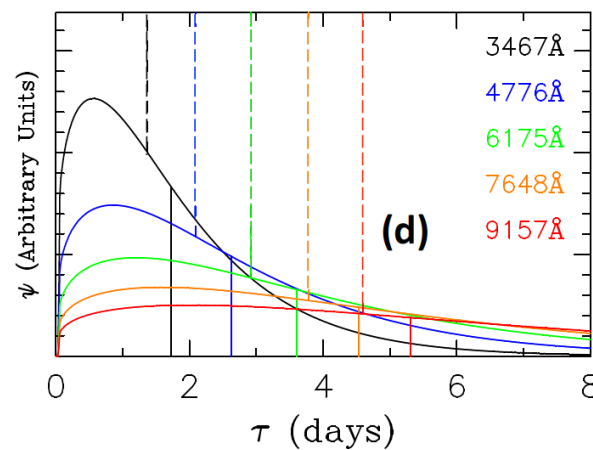
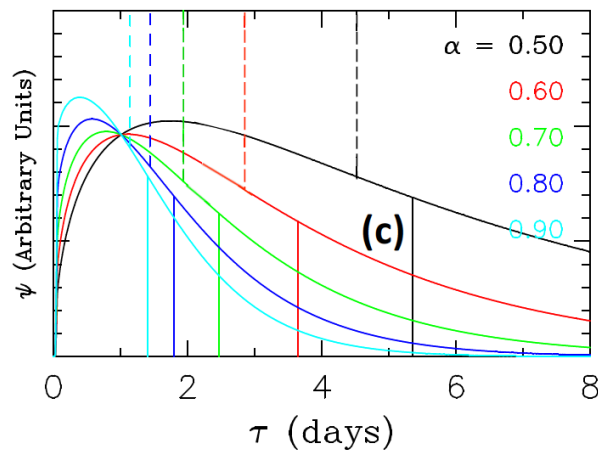
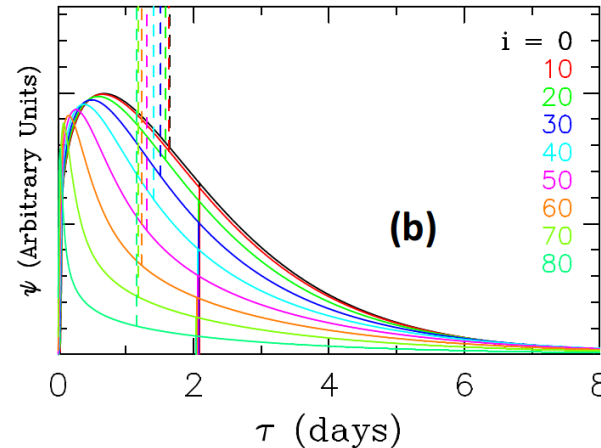
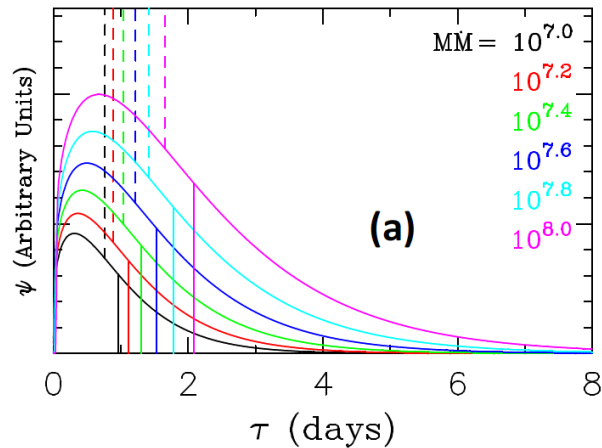
$$F_\nu(t, \lambda) \equiv \iint B_\nu(T(r, t), \lambda) \frac{r dr d\theta \cos i}{D^2}$$

$$\Psi(\tau, \lambda) \equiv \frac{dF_\nu(t, \lambda)}{dL_x(t - \tau)} = \iint \frac{B_\nu}{dT} \frac{dT}{dL_x} \frac{r dr d\theta \cos i}{D^2} \delta(\tau - \tau(r, \theta))$$

Blackbody Disk Delay Maps

$$T(R) = T_1 (R/R_1)^{-\alpha}$$

Starkey et al., 2016



Mean delay
 $\tau \sim (M \dot{M})^{1/3} \lambda^{4/3}$
 Independent of
 disk inclination.

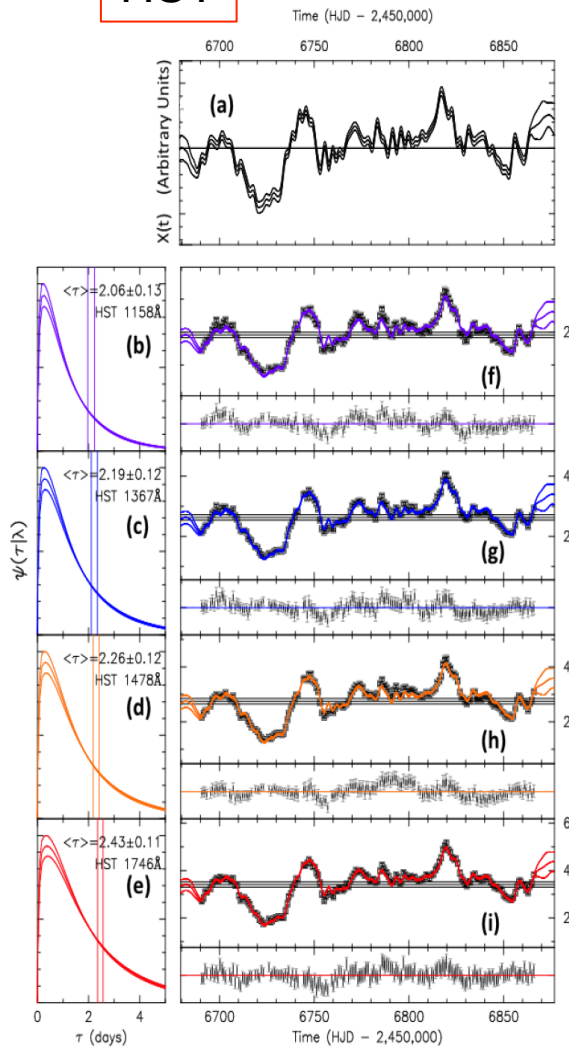
Delay map shape
 depends on
 disk inclination

And slope α of $T(r)$
 temperature profile

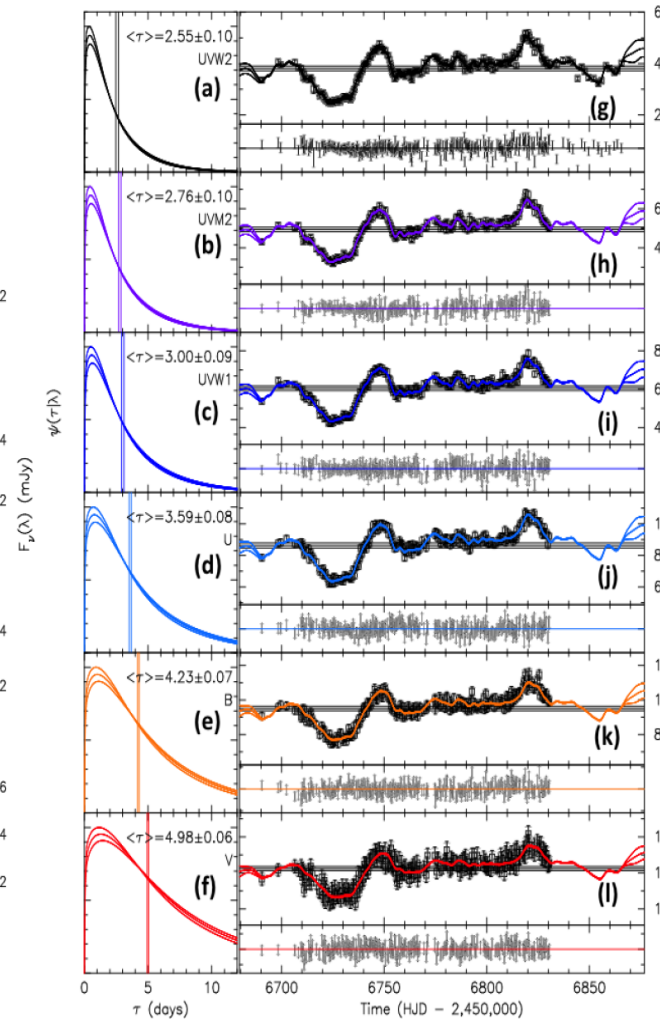
Theory: $\alpha = 3/4$

CREAM : MCMC Lightcurve Fits

HST

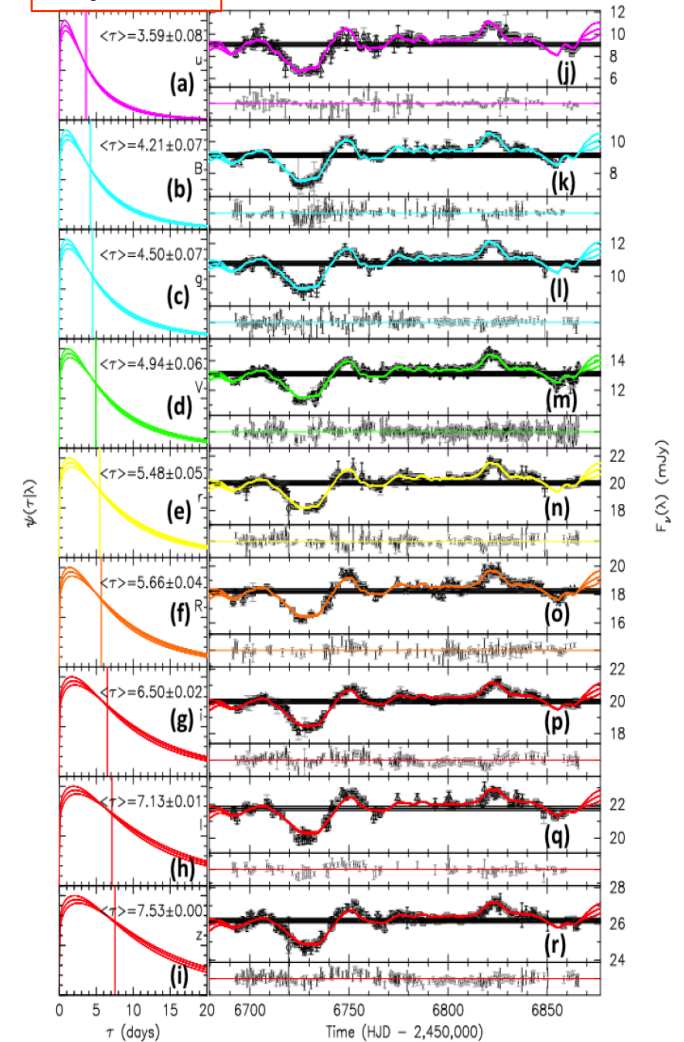


Swift UV/OT



Optical

Starkey et al.

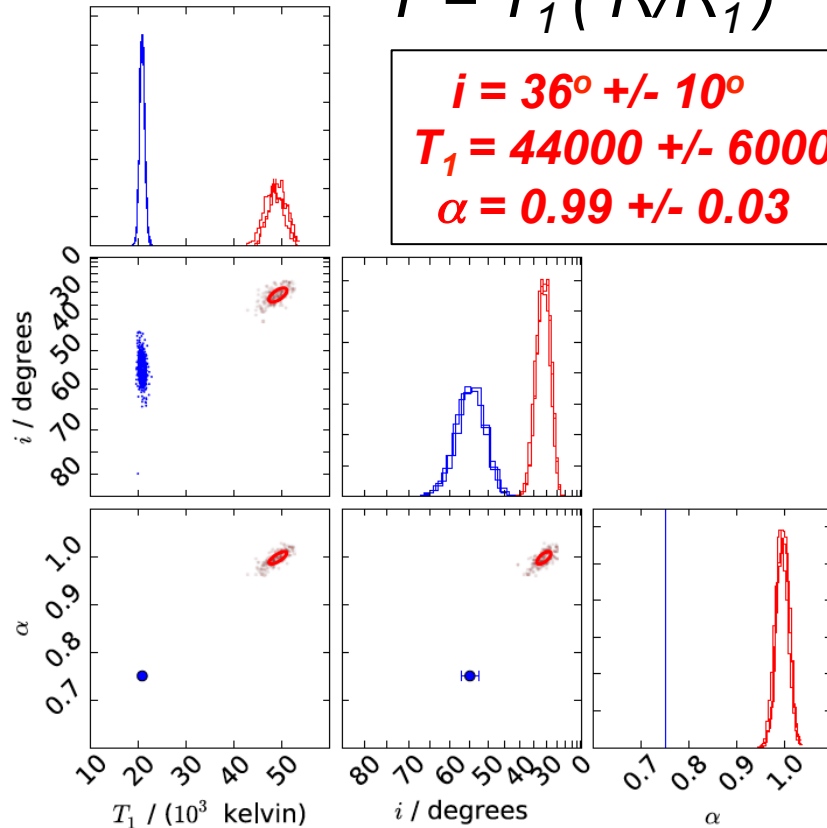


T(R) Profile

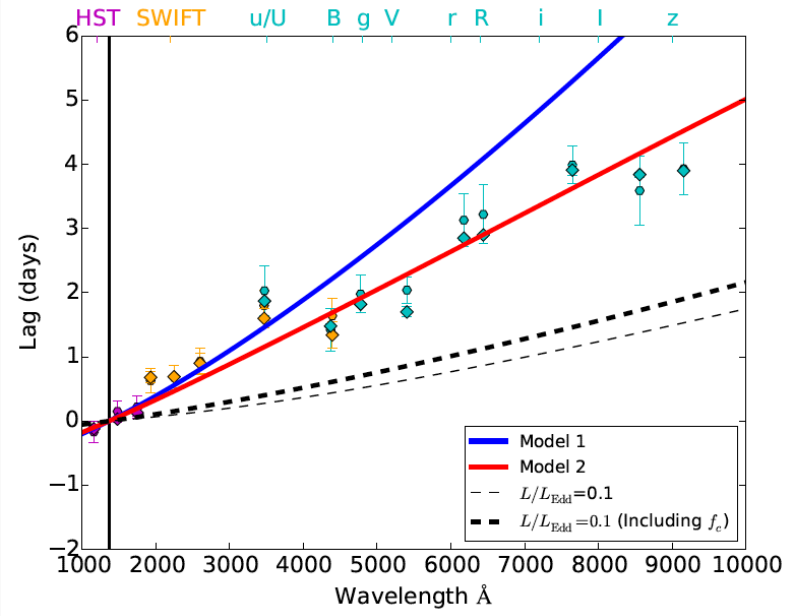
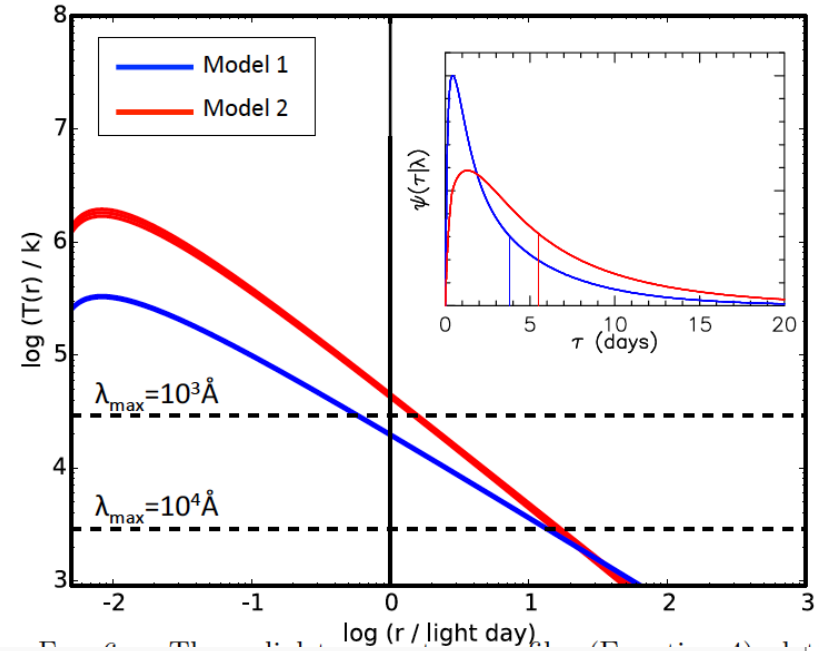
T(R) profile **steeper than expected**.
 $T \sim R^{-1}$ rather than $R^{-3/4}$.

$$T = T_1 (R/R_1)^{-\alpha}$$

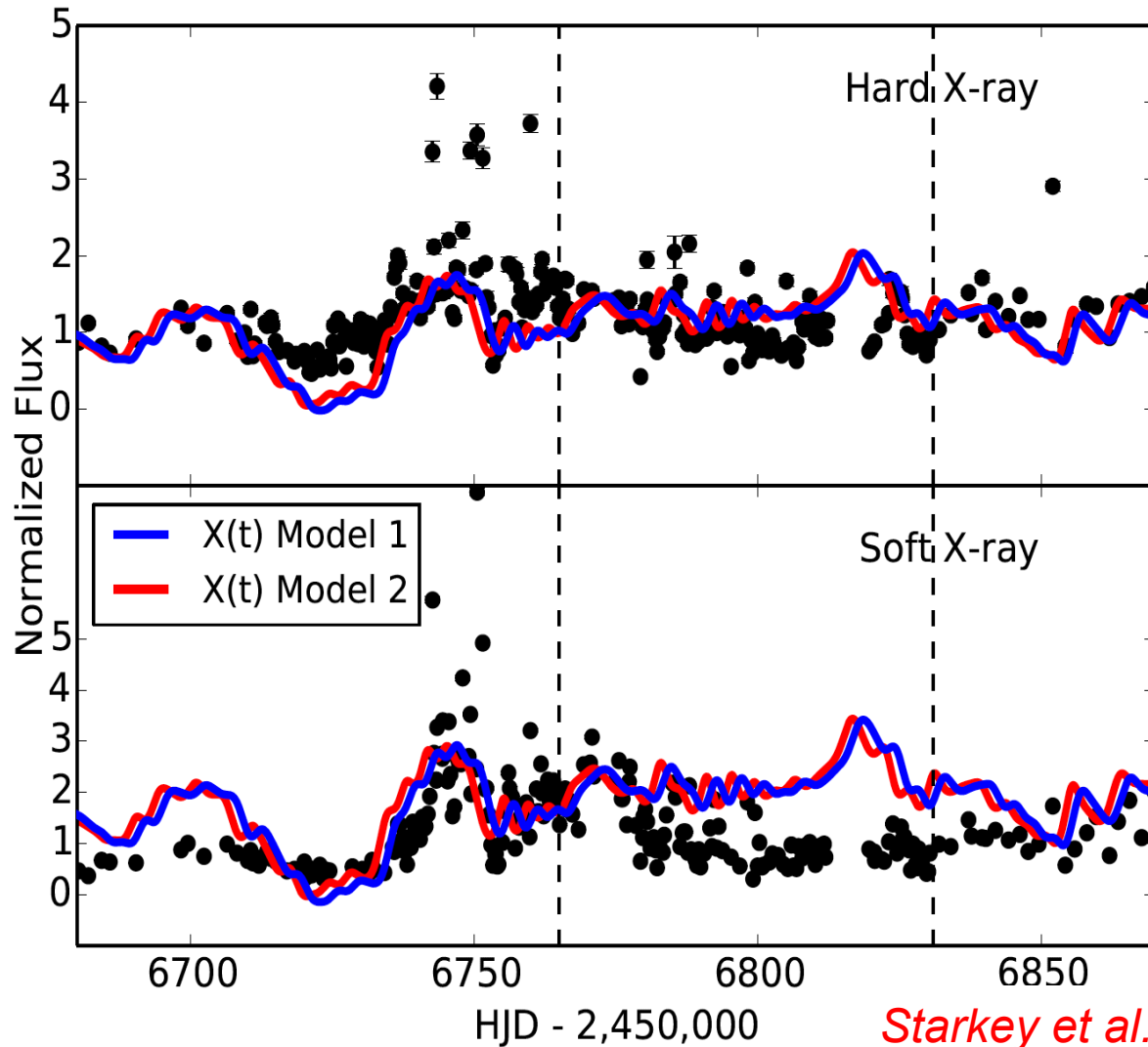
$i = 36^\circ \pm 10^\circ$
 $T_1 = 44000 \pm 6000 \text{ K}$
 $\alpha = 0.99 \pm 0.03$



Starkey et al., submitted



X-rays vs Driving Lightcurve



X-ray variations don't match the required driving lightcurve

Starkey et al., submitted

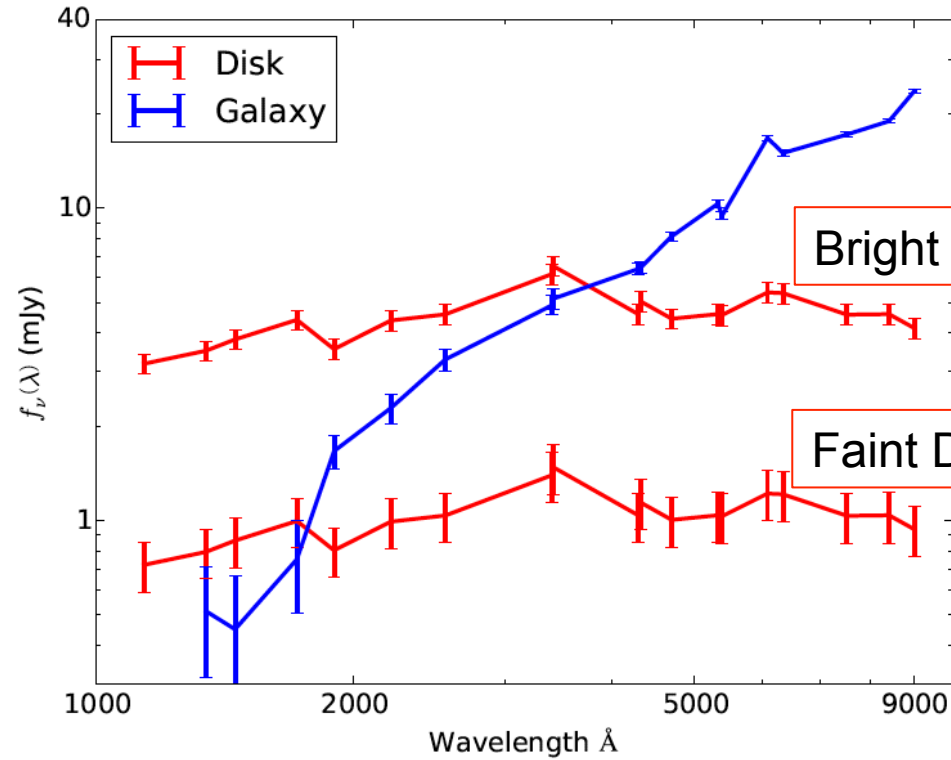
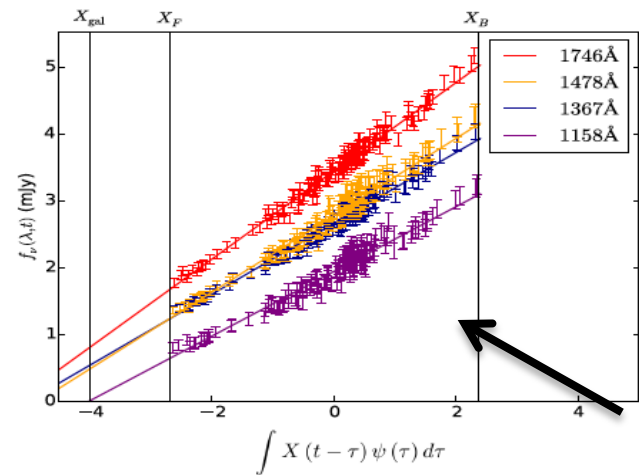
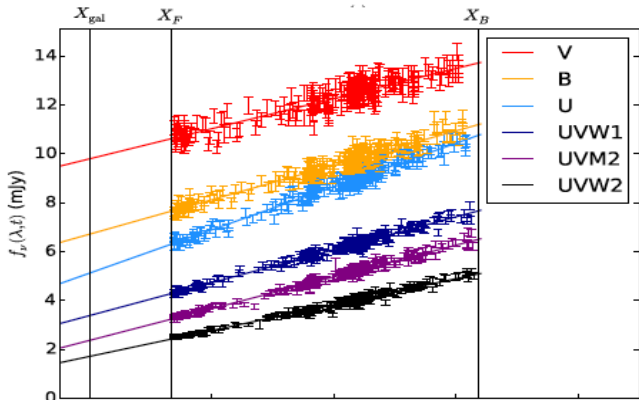
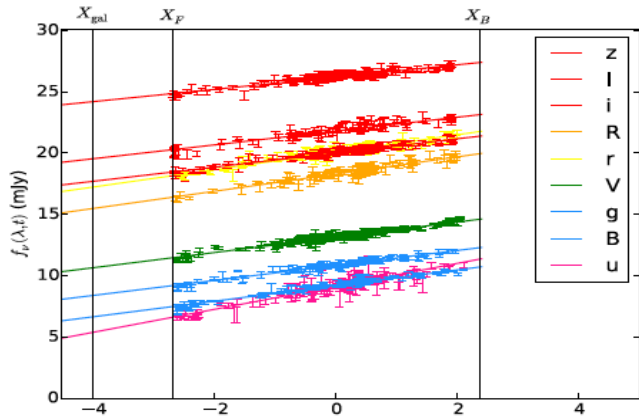
Disk Spectrum

Variations isolate the Disk spectrum

$$F(\lambda, t) = A(\lambda) + S(\lambda) X(t)$$

$$= G(\lambda) + S(\lambda) (X(t) - X_G)$$

$$\langle X \rangle = 0 \quad \langle X^2 \rangle = 1$$

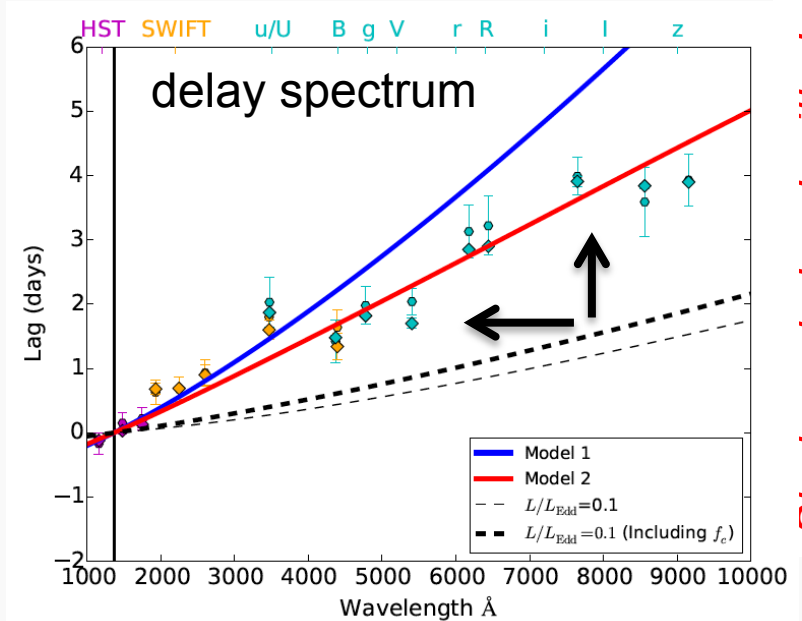
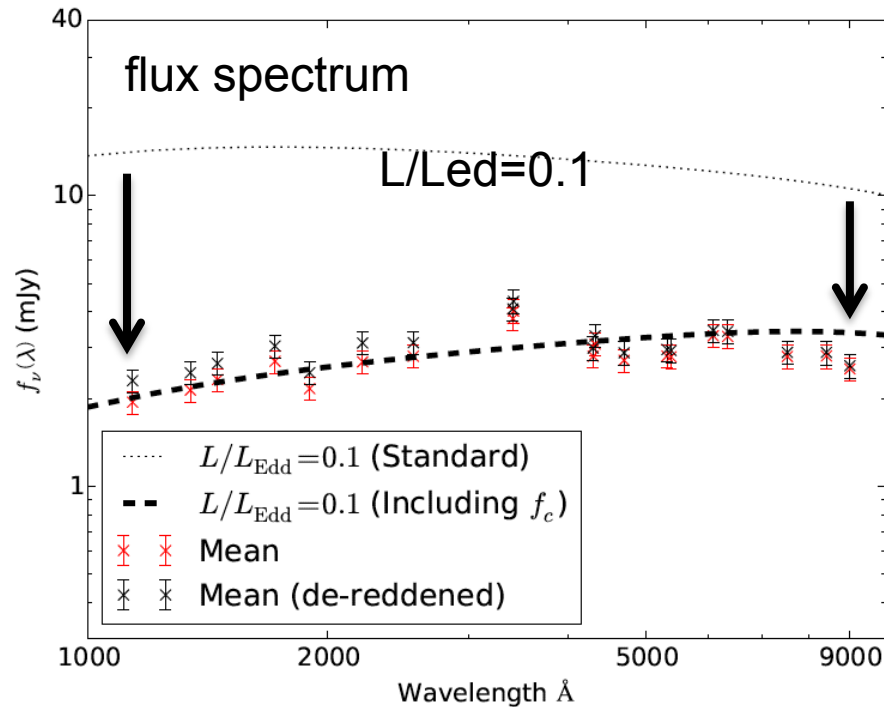


Note linear variations

Starkey et al. submitted

Standard Disk Model Fails

Disk flux spectrum is redder and fainter than expected ($L/L_{\text{Edd}}=0.1$)
 Disk delay spectrum is hotter and steeper than expected



Starkey et al. submitted

Questions:

Why does the standard disk model fail ?
 Disk spectrum is too faint and red.
 $T(r)$ is too hot and steep.

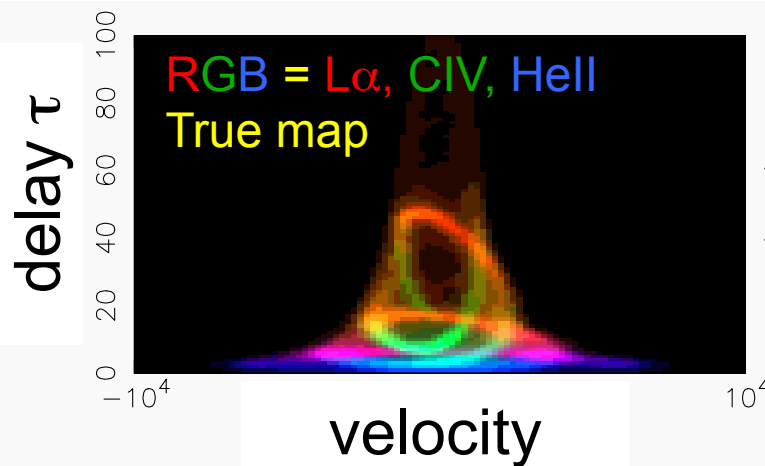
Answers: (=New Questions)

Dust ? (affects flux but not delay)
 Higher black hole mass ? (raises L_{Edd})
 Diffuse continuum from BLR ?
 Partial irradiation (shadows) ?
 Tilted inner disk ?

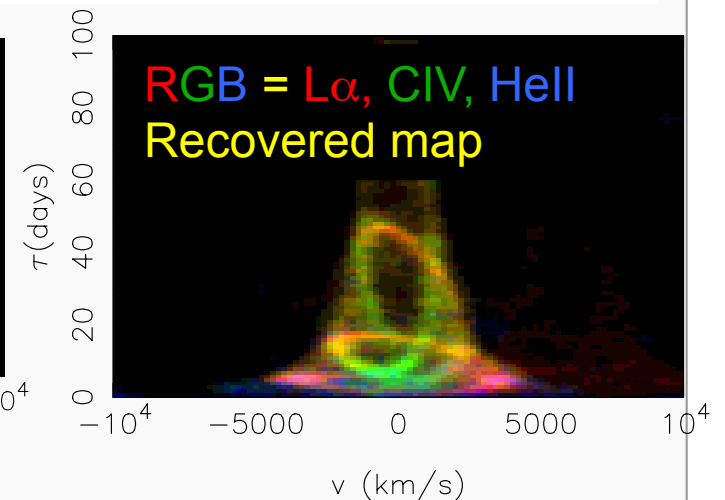
Velocity-Delay Maps : $\Psi(v,\tau)$ from Simulated HST data

MEMEcho
recovers
 $\Psi(v,\tau)$
from
simulated
HST data

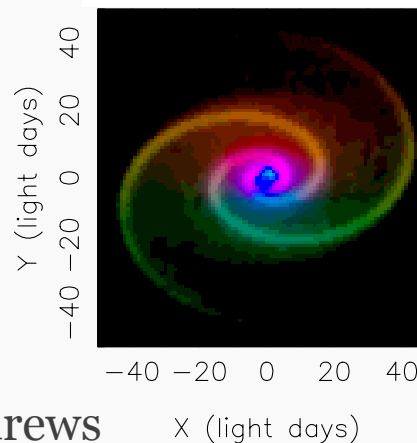
Velocity-Delay Map



Velocity-Delay Map



sky view:

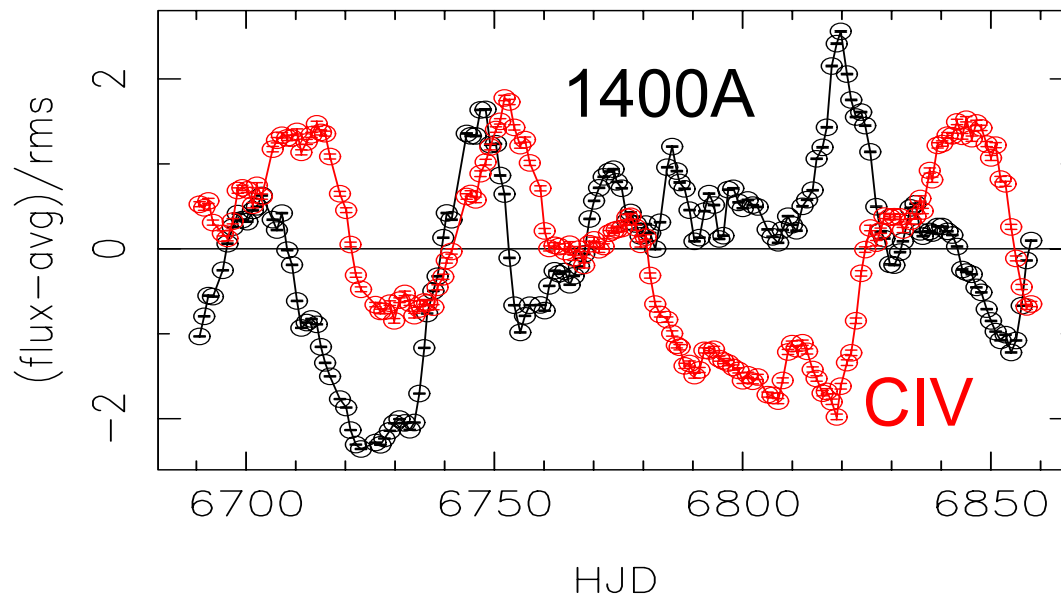


Evident features:

- Virial envelope
- Spiral structure
- Radial ionisation
- Azimuthal anisotropy

But : HST line variations are NOT simple continuum echos ☹️

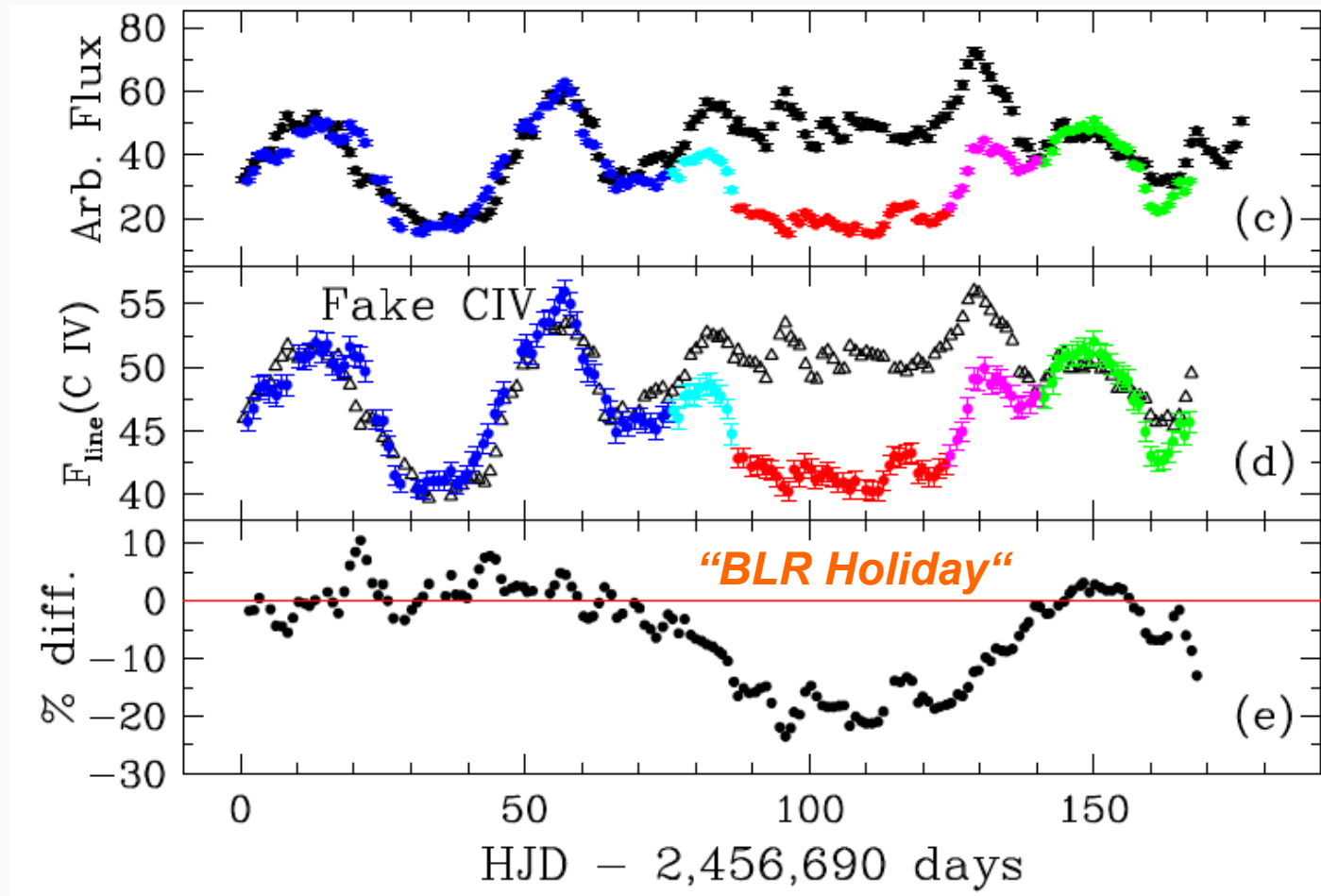
NGC 5548 HST



- Fast (5-20d) variations correlate, with clear (5-10d) lags.
- Slow (100d) variations may anti-correlate.
- **Linerarised echo model fails to fit the line variations ☹️.**

Line Responses “De-cohere” 60 Days into STORM Campaign

Temporary Obscuration ? Change in the SED ?

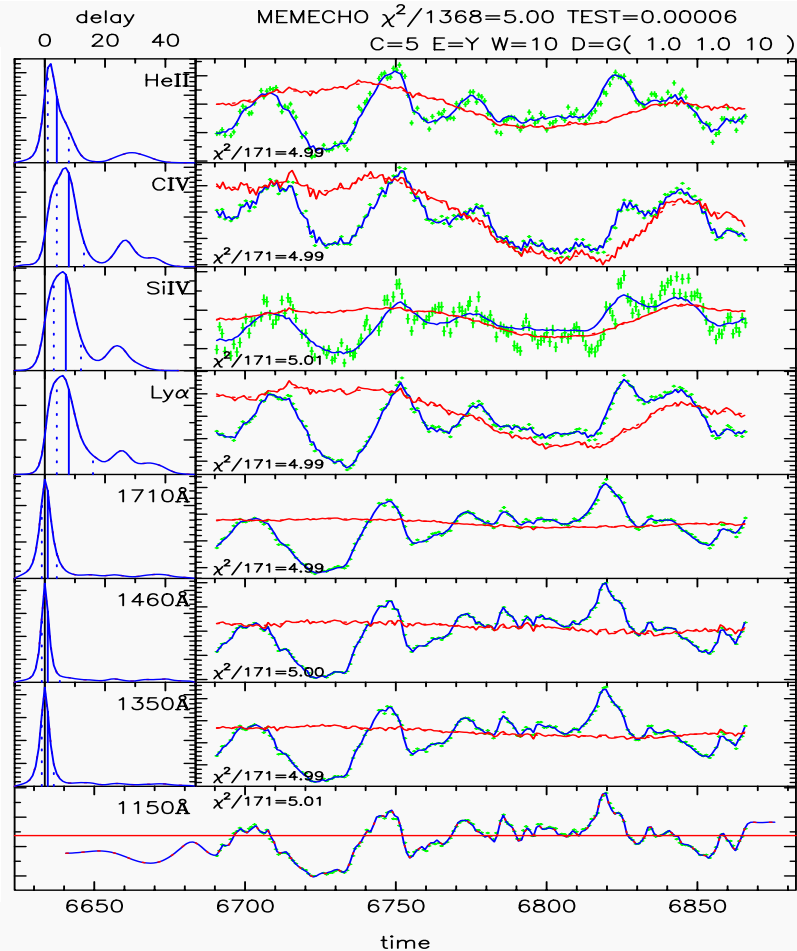


Goad et al. 2016

HST Lightcurves -> Delay Maps : $\Psi(\tau)$

Linearised Echo
Model Fails !

Model lines as
continuum echos
+
slow variations



He II

C IV

Si IV

Ly α

1710A

1460A

1360A

1150A

Velocity-Delay Maps : $f(\lambda, t) \rightarrow \Psi(v, \tau)$

HST spectra

$$f(\lambda, t)$$

=>

500 lightcurves

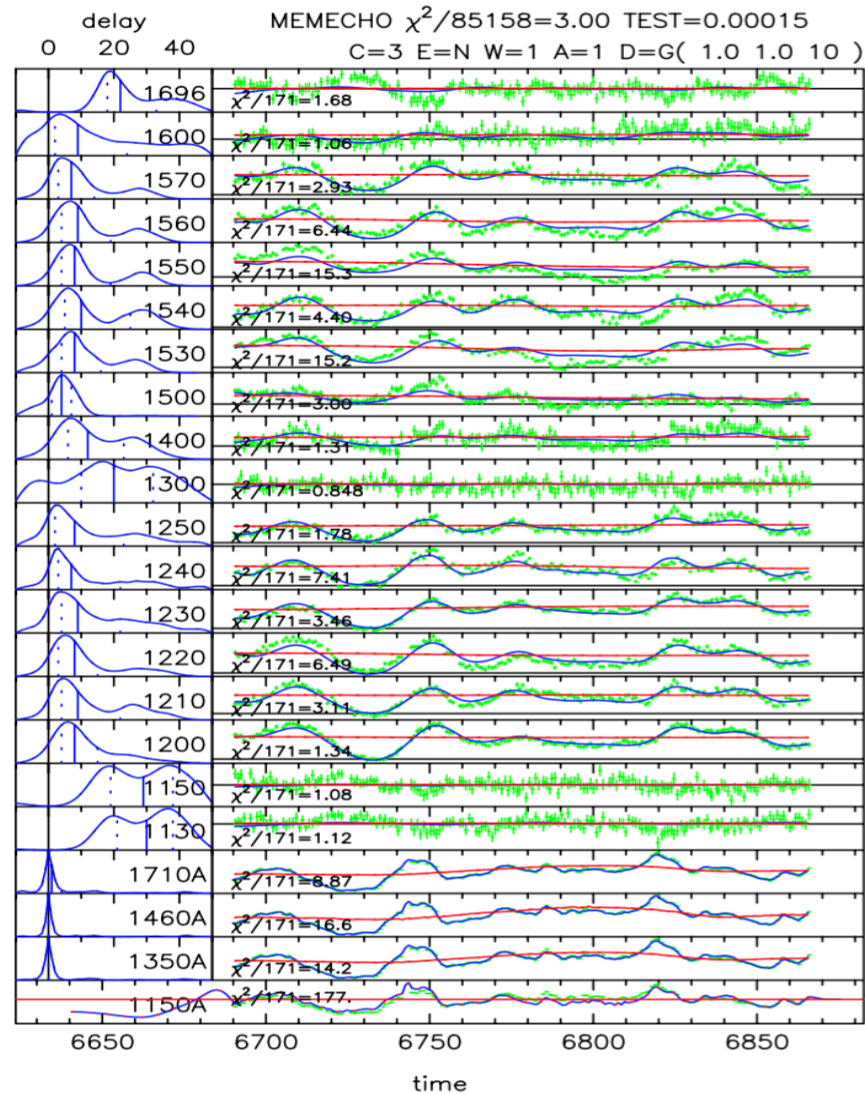
+

MEMECHO fit

=>

500 delay maps

$$\Psi(v, \tau)$$



C IV

Ly α

1150-1710
continuum

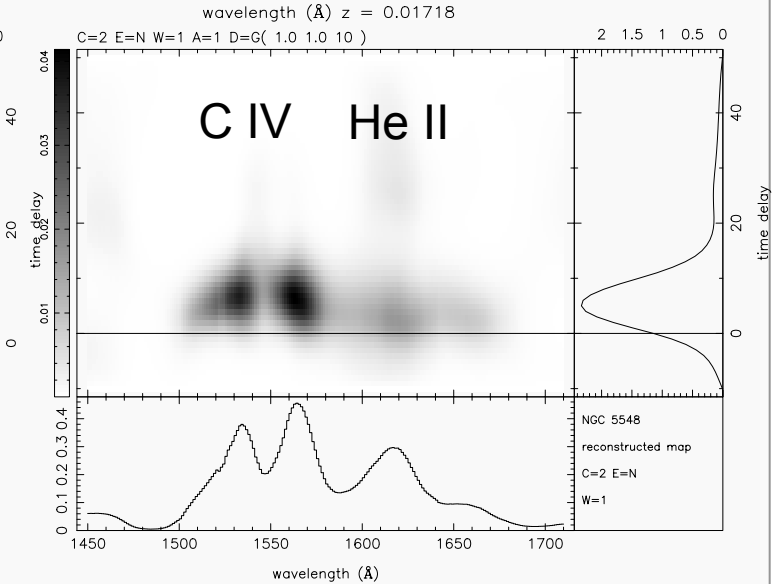
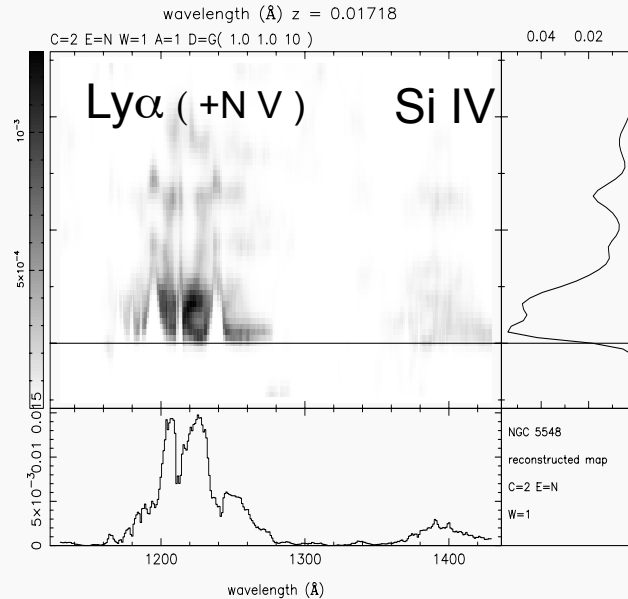
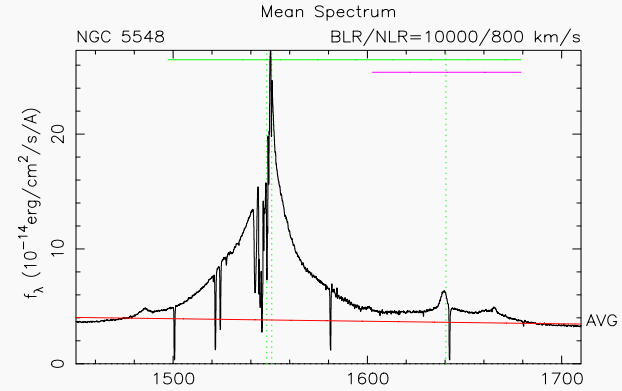
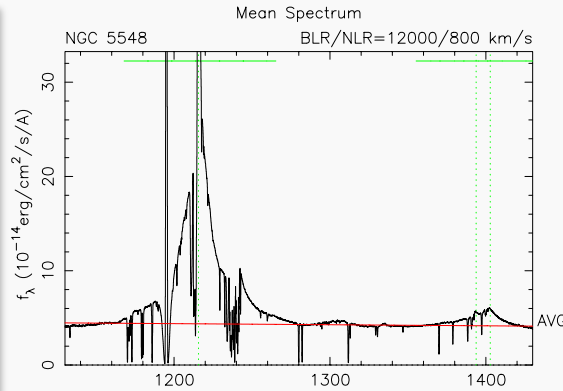
First MEMEEcho fits (2015 Jan)

$\Psi(v, \tau)$ distorted by absorption lines ☹️

Velocity-delay maps
 $\Psi(v, \tau)$

Distorted by absorption lines. ☹️

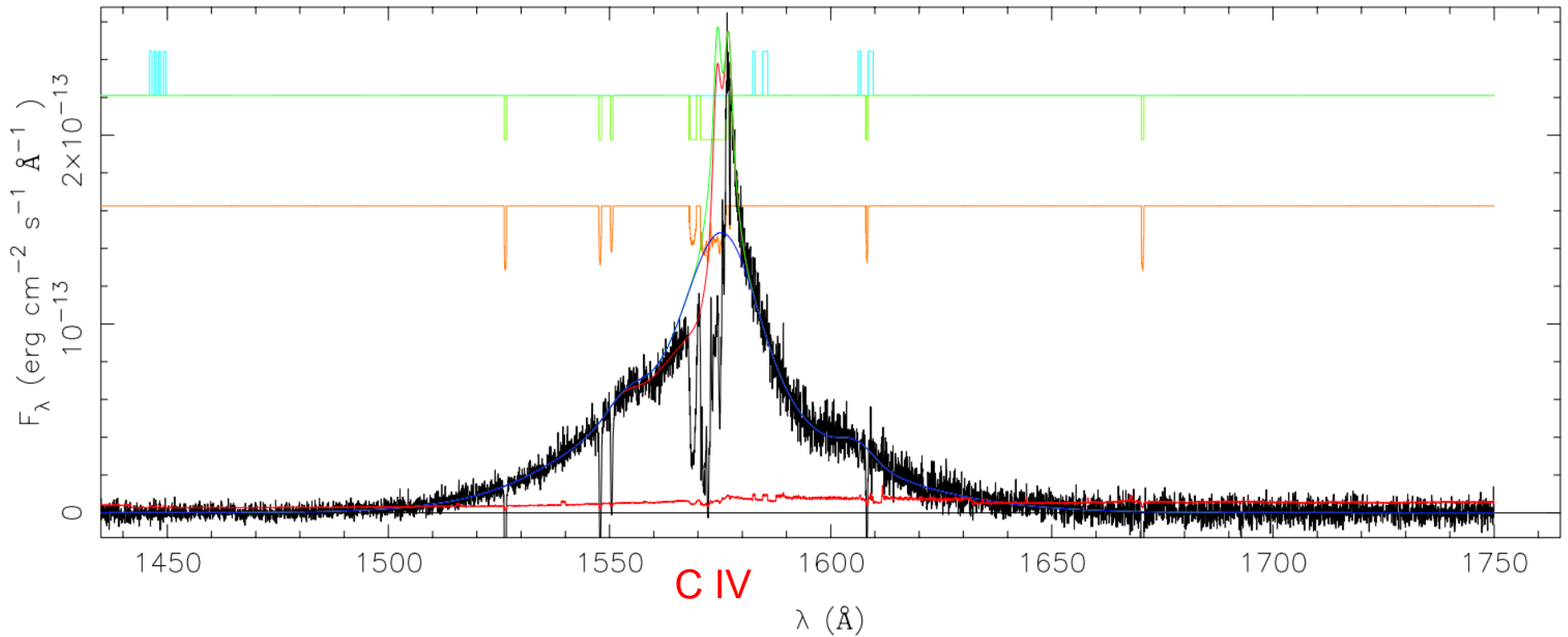
To be improved...



Spectral Modeling analysis (2016 Jul)

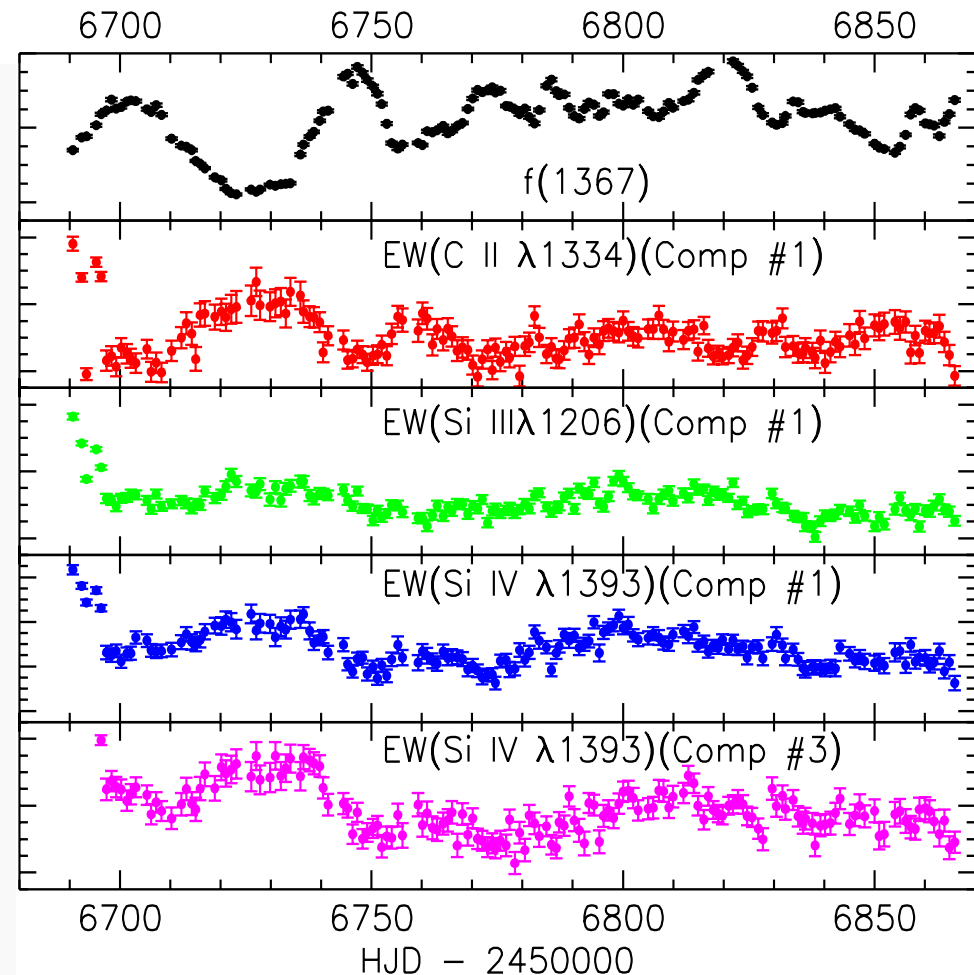
(de Rosa, Ely, Kriss) Use to remove absorption lines.

001 storm_models_v01.txt 56690.62994



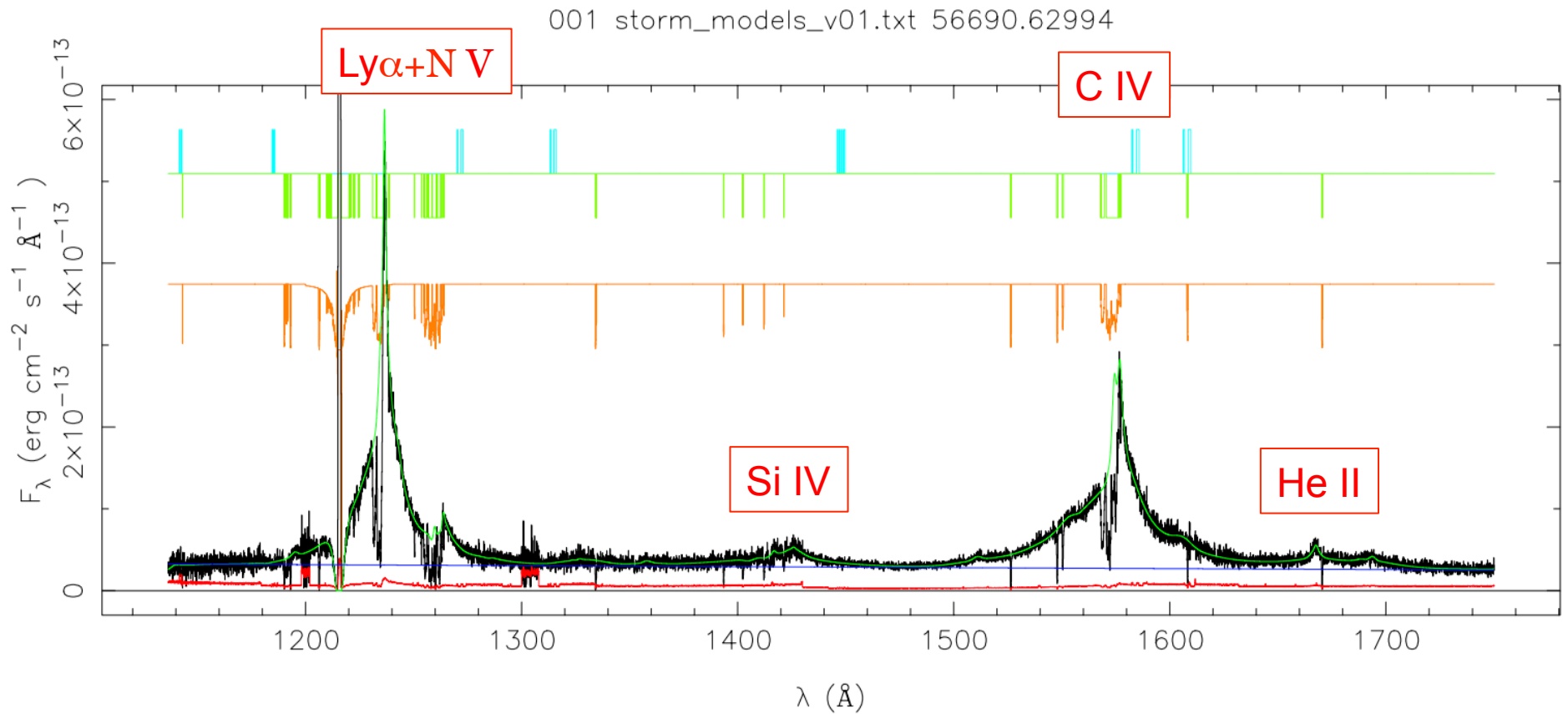
Narrow Absorption Lines

- See the same continuum that we do.
- Response time is **recombination time**.
- Vary in strength with continuum flux *at their ionization energy*.
- Track changes in the ionising SED

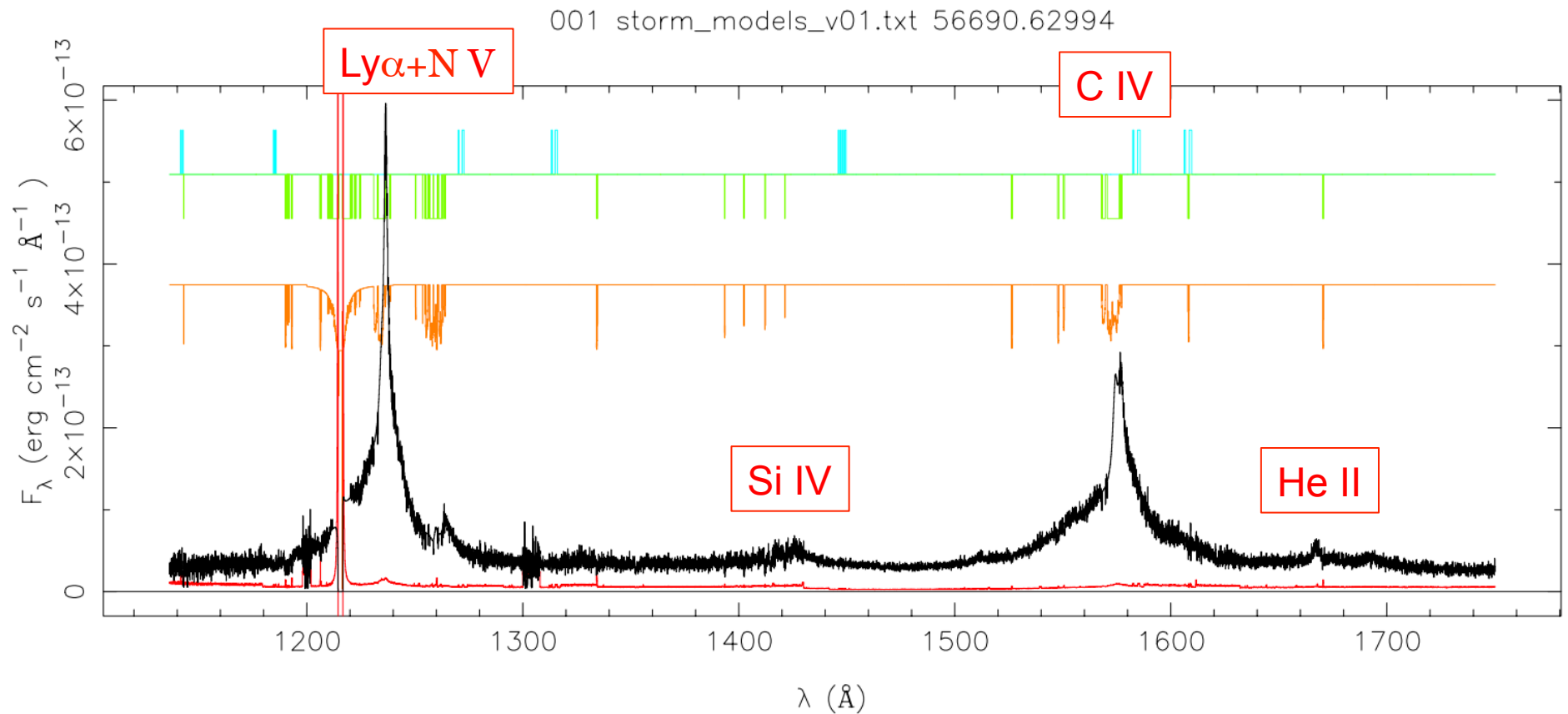


Kriss et al. in prep

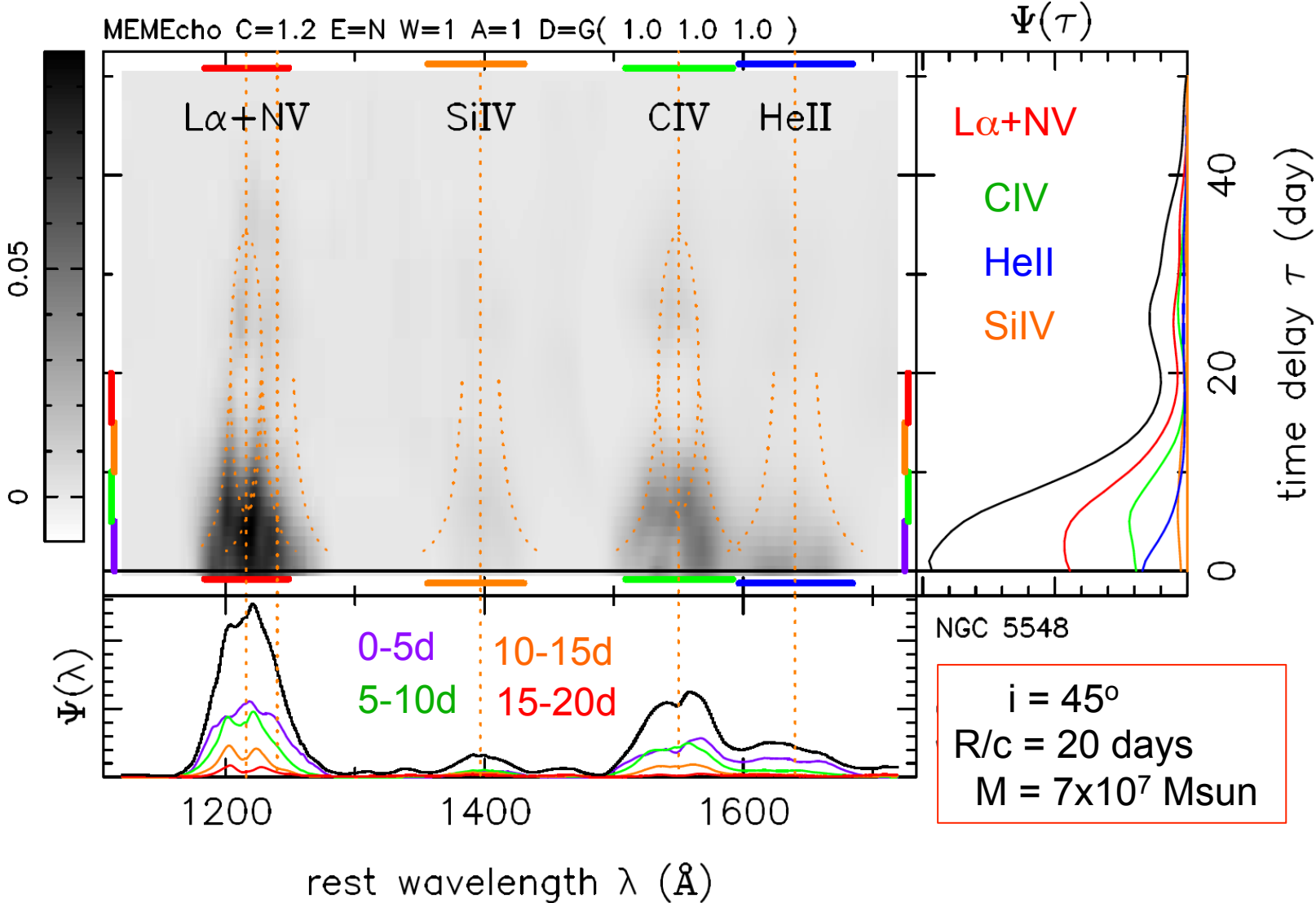
Absorption Lines Modeled



Absorption Lines Removed ☺

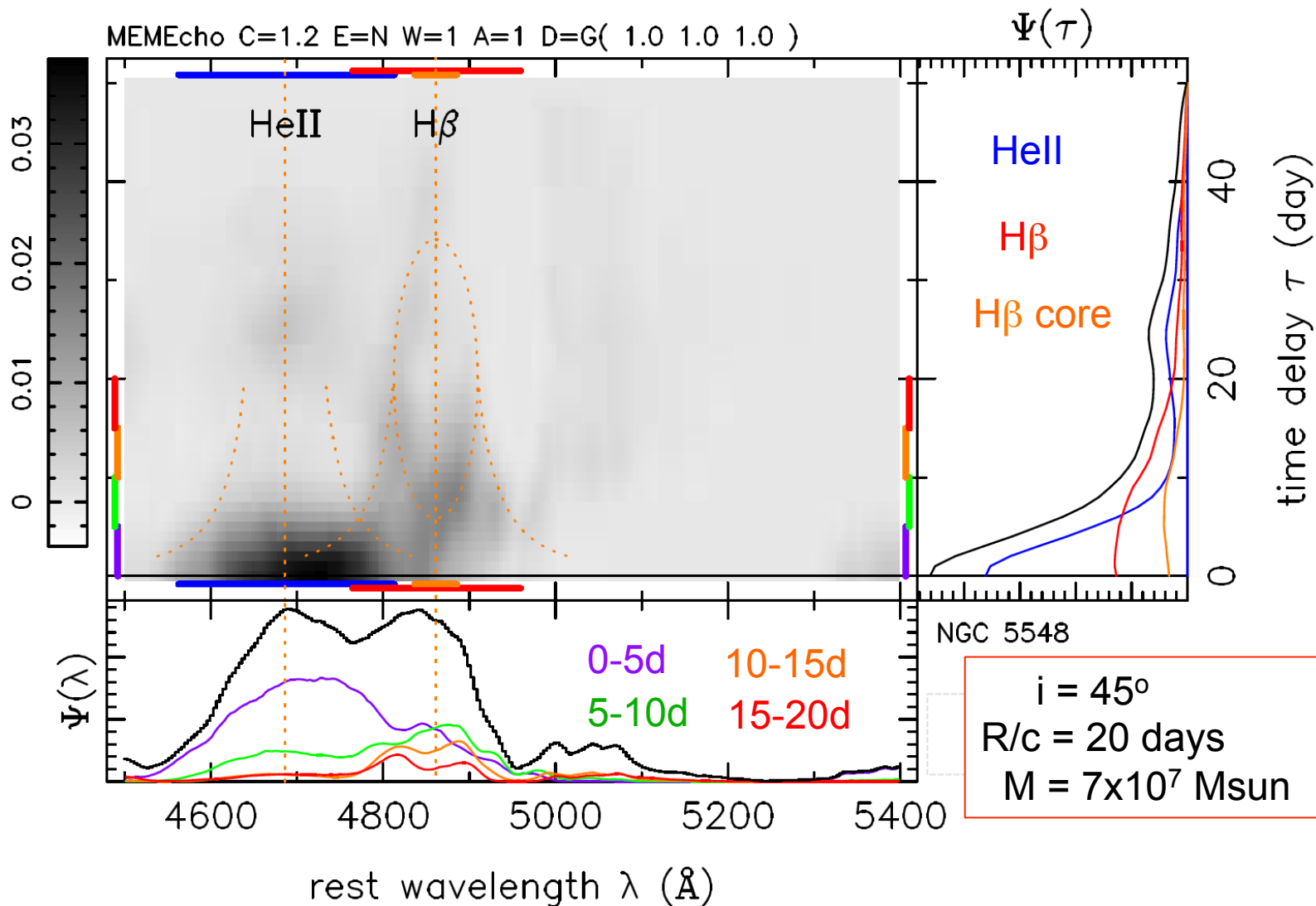


HST (UV lines) Velocity-Delay Map

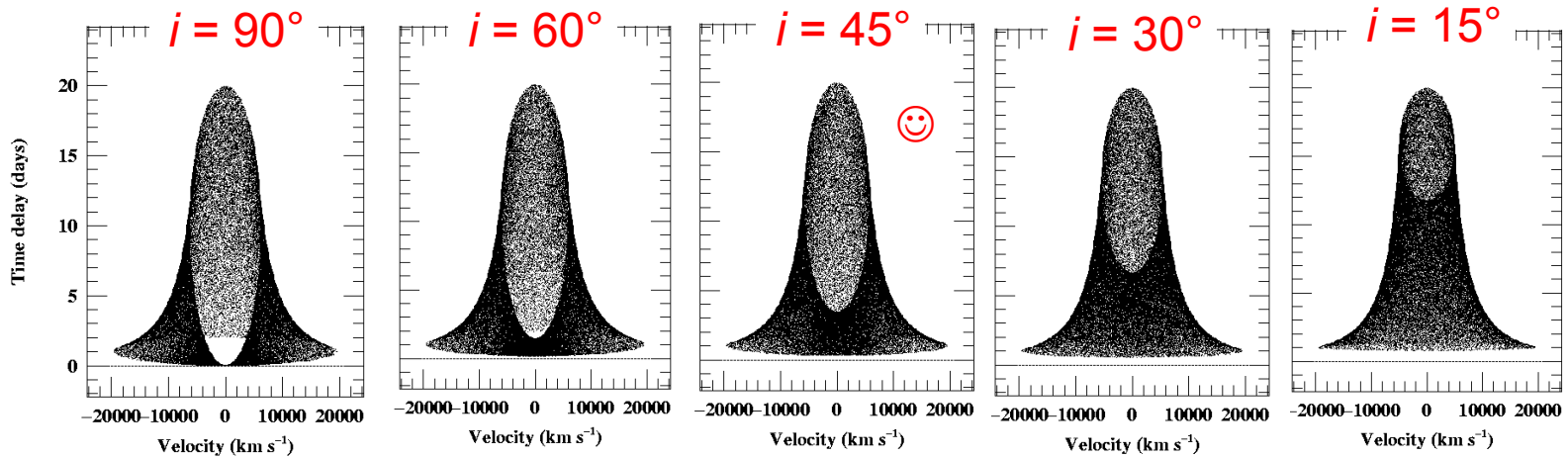


Optical lines : Velocity-Delay Map

MEMEcho fit to MDM data from *Pei et al, submitted*.



Comparison with Toy Models

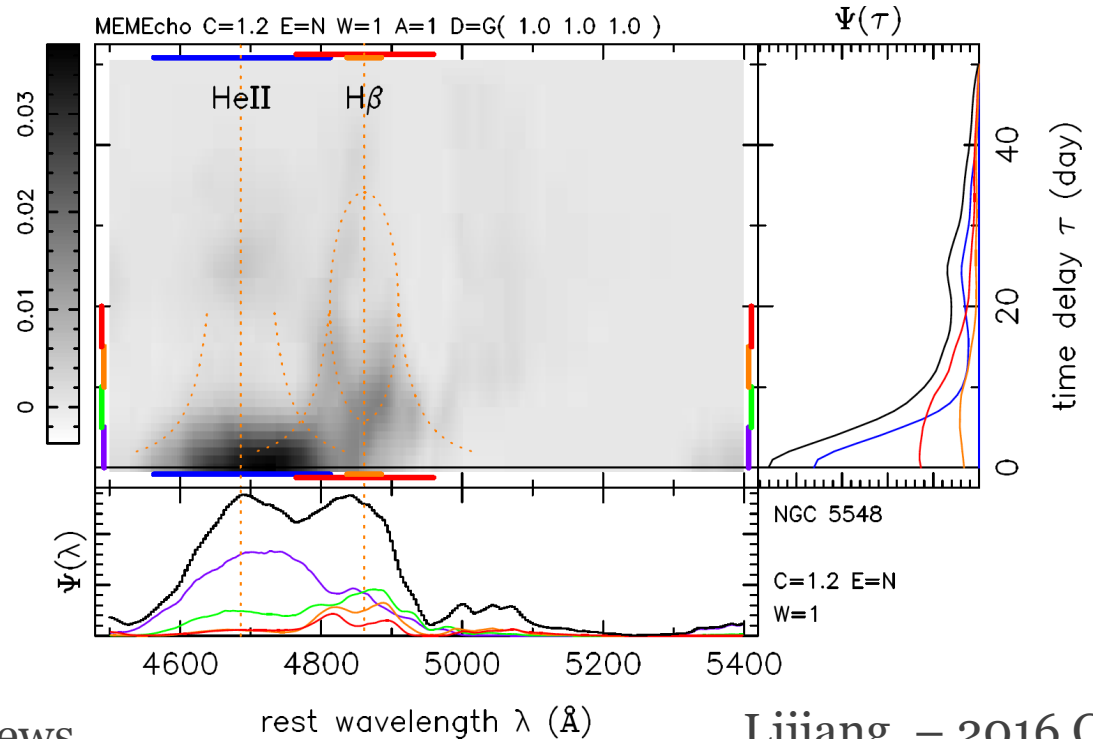


Keplerian Envelope
+ Elliptical Ring



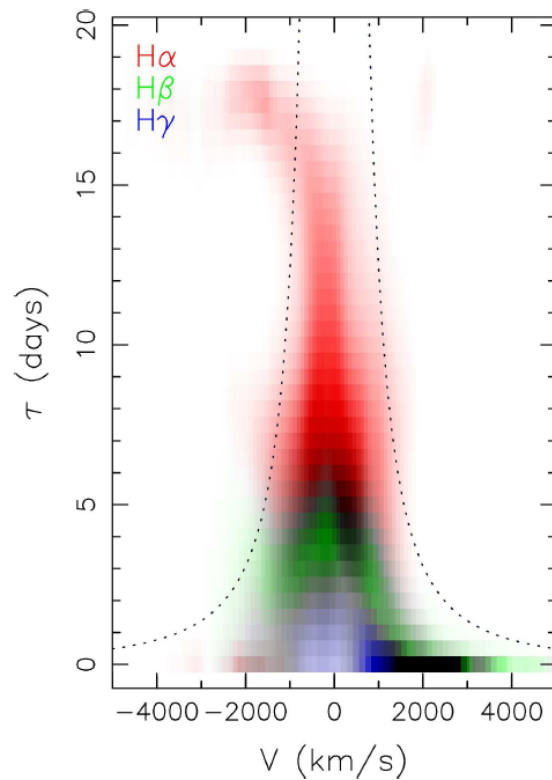
Disk-like Geometry
and Kinematics
2 to 20 light days

$i = 45^\circ$
 $R/c = 20$ days
 $M = 7 \times 10^7 M_{\text{sun}}$

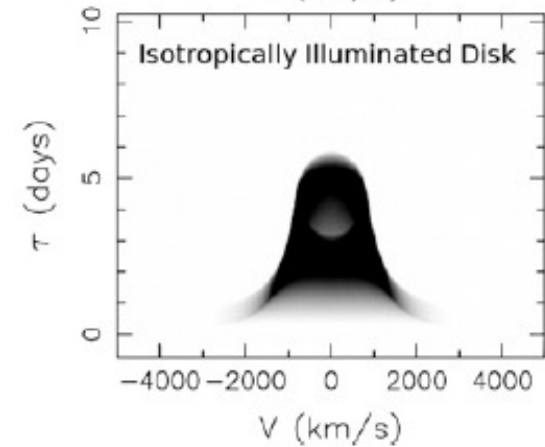
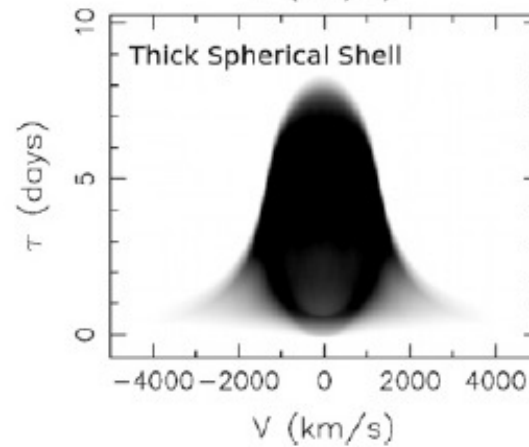
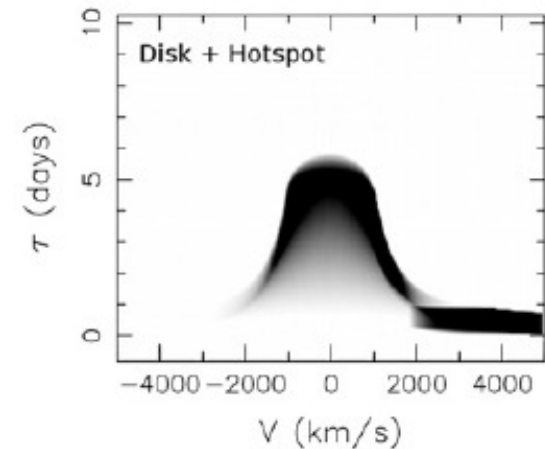
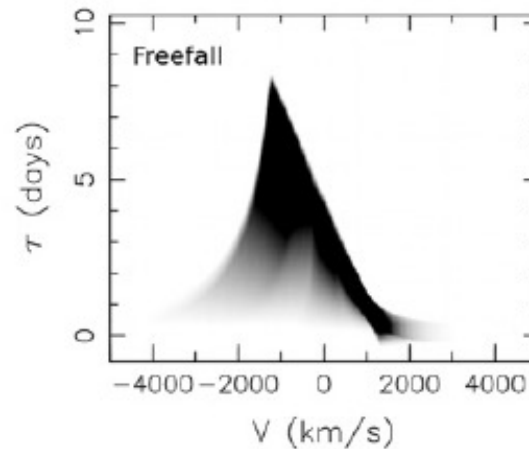


Arp 151 : BLR Maps and Toy Models

Arp 151 LAMP data :



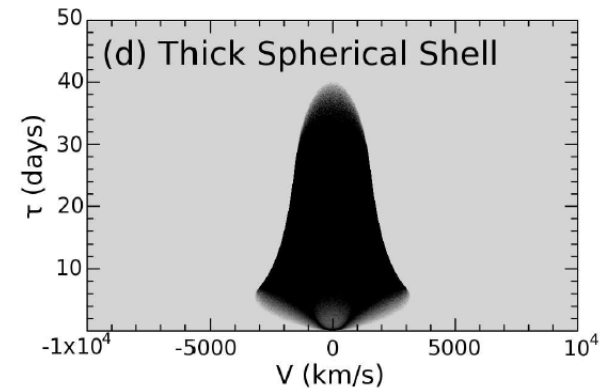
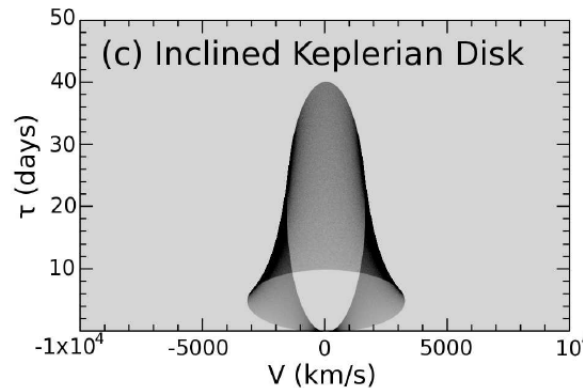
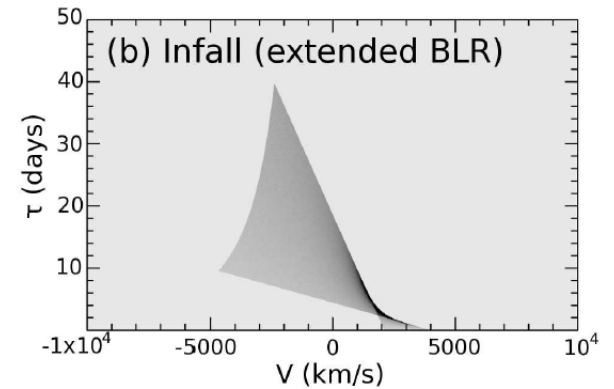
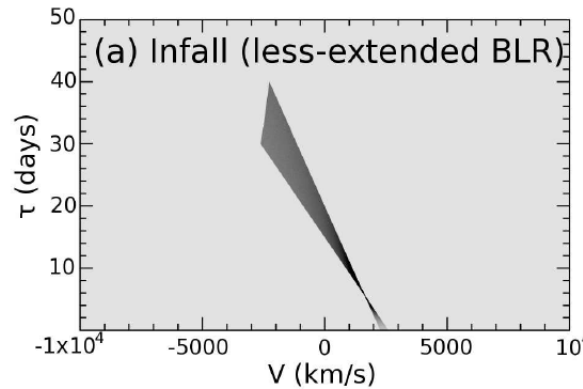
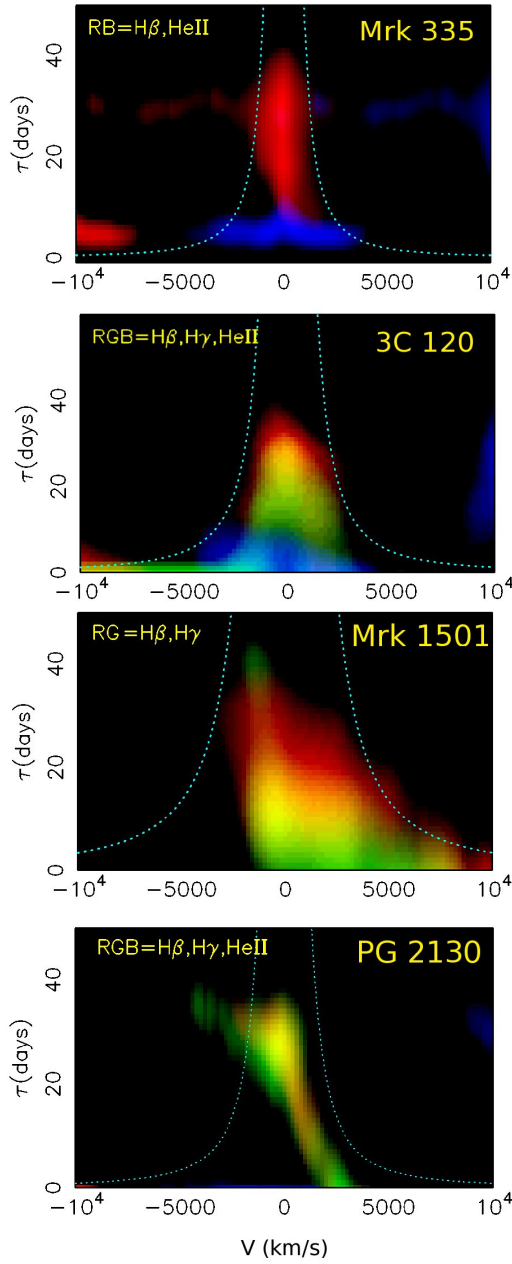
Bentz et al. 2010



BLR Diversity

A variety of velocity-delay structures is seen.
How reliable / repeatable are these maps?
Is every AGN flow different ?

Grier et al. 2013, ApJ 764, 47



Lamp Post => Tilted Inner Disk ?

- Black hole spin mis-aligned (expected)
 - ✦ Bardeen-Petterson effect : Lens-Thirring torques align inner disk with BH spin
- Self-illumination (as in close binary stars)
 - ✦ X-FUV : multiple reprocessing increases and smears reprocessing time.
 - ✦ UV-IR : $T(r)$ steeper than $r^{-3/4}$
- Anisotropic irradiation pattern
 - ✦ $T(r) \Rightarrow T(r, \theta)$
 - ✦ $\Psi(V, \tau)$ red/blu asymmetry sans in/out flow
 - ✦ Object-object diversity
- Precession ?
 - ✦ Observable?

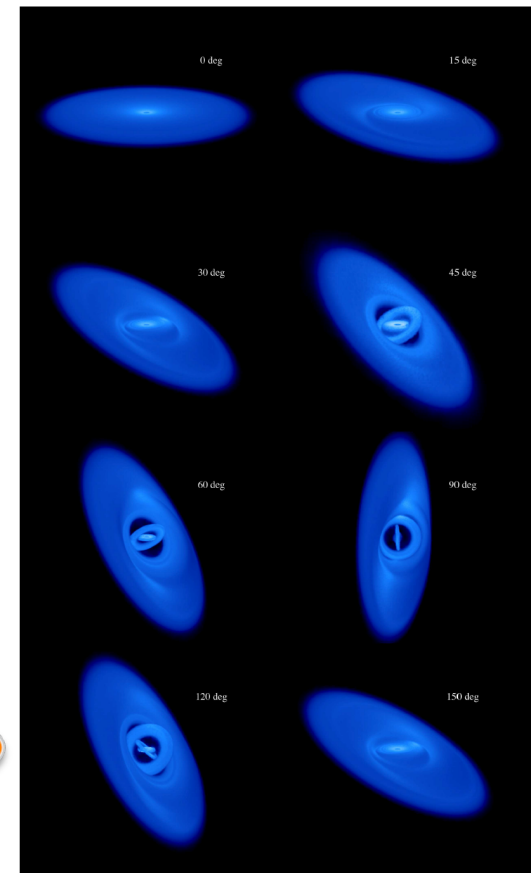


Starkey et al. in prep

Keith Horne, SUPA St Andrews

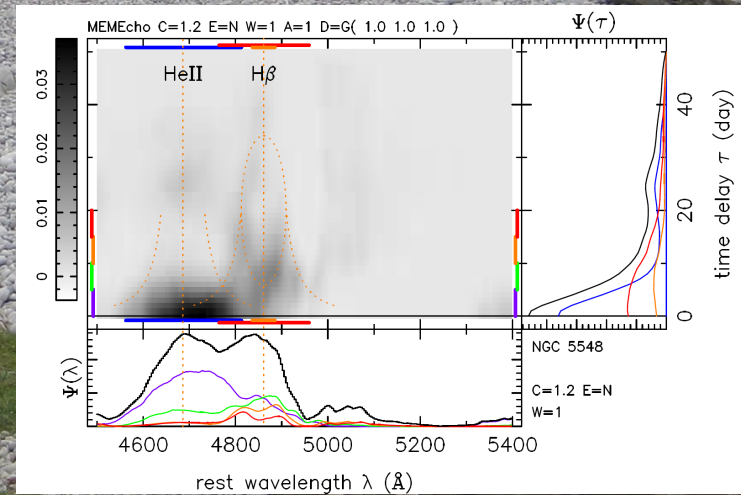
*Nealon, Price, Nixon
2015 MNRAS*

3d SPH simulations



Lijiang – 2016 Oct 24

Thanks for Listening



Keith Horne, SUPA St Andrews

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