

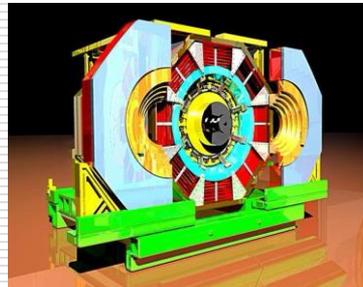
Baryons strike back in BESIII

Evidence for a new $2g1\gamma$ virtual charmonium decay ?

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Why to understand Baryons is important

- ❑ Visible mass in the Universe is due essentially to the strong force binding quarks inside the Nucleon
 - ❑ Many Meson features come from QED \rightarrow QCD, once $\alpha \rightarrow \alpha_s$
Baryons: no analogue in QED and unique QCD feature
 - But why Baryon Skyrme model (no q , π 's soliton) so successful ?
Baryons really fully understood ?
 - ❑ Vector charmonium, 3S_1 , and BB_{bar} linked: 3 gluons \rightarrow 3 qq_{bar} pairs
 - $^3S_1 \rightarrow BB_{\text{bar}}$ fully understood ?
 - Not the angular distributions $1 + \alpha \cos^2\theta$:
why α change sign in J/ψ or $\psi(3686) \rightarrow \Lambda\Lambda / \Sigma\Sigma$?
- why $\alpha_p \neq \alpha_n$, while $B_p \sim B_n$, in $\psi(3686) \rightarrow NN_{\text{bar}}$?**

$\Psi(3686) \rightarrow NN_{\text{bar}}$ Branching Ratios

- $\sim 23400 pp_{\text{bar}}$ and $2650 nn_{\text{bar}}$ events have been selected, obtaining
 $B[\Psi(3686) \rightarrow pp_{\text{bar}}] = (3.06 \pm 0.02 \pm 0.13) \cdot 10^{-4}$,
 $B[\Psi(3686) \rightarrow nn_{\text{bar}}] = (3.09 \pm 0.06 \pm 0.14) \cdot 10^{-4}$.
- The close B values, within small errors, would suggest interference between strong and em decay is small (positive in the pp_{bar} and negative in the nn_{bar} decay), i.e. their relative phase $\phi \sim 90^\circ$.
- In the case of $J/\psi \rightarrow NN_{\text{bar}}$, close B values were also achieved :
 $B[J/\psi \rightarrow pp_{\text{bar}}] = (2.112 \pm 0.004 \pm 0.031) \cdot 10^{-3}$,
 $B[J/\psi \rightarrow nn_{\text{bar}}] = (2.07 \pm 0.01 \pm 0.17) \cdot 10^{-3}$.
- So far, so good. Up to a certain point.

$\Psi(3686) \rightarrow N N_{\text{bar}}$ Angular Distributions

- Fitting $\psi(3686) \rightarrow NN_{\text{bar}}$ with $1 + \alpha \cos^2 \theta$:

$$\alpha_p = 1.03 \pm 0.06 \pm 0.03, \quad \alpha_n = 0.47 \pm 0.15 \pm 0.15$$

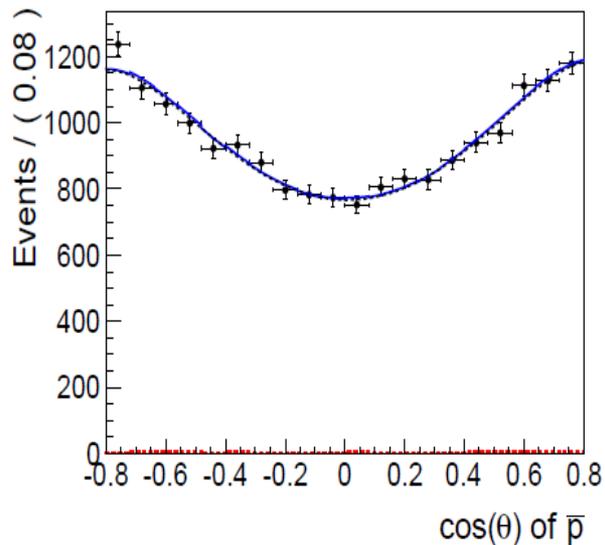
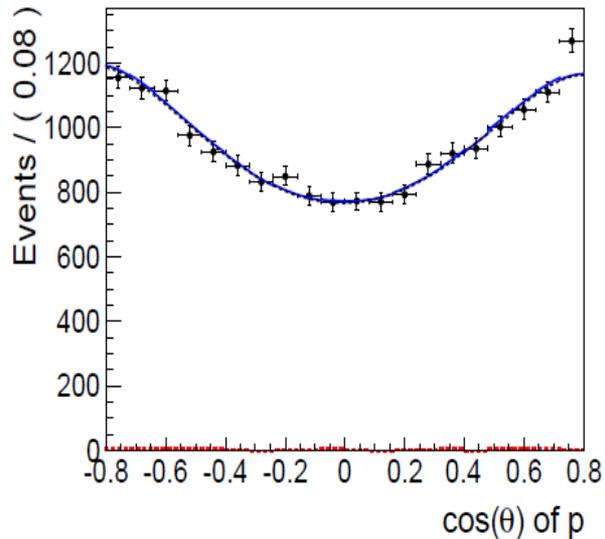
- i.e. pp_{bar} and nn_{bar} angular distribution are quite different, in spite of similar B.
- Furthermore α_p is close to the limit $|\alpha_p| \leq 1$.
- No evidence of a $\cos \theta$ term, i.e. no forward/backward asymmetry.

- Conversely, in the case of $J/\psi \rightarrow NN_{\text{bar}}$ it was obtained:

$$\alpha_p = 0.595 \pm 0.012 \pm 0.015, \quad \alpha_n = 0.50 \pm 0.04 \pm 0.21$$

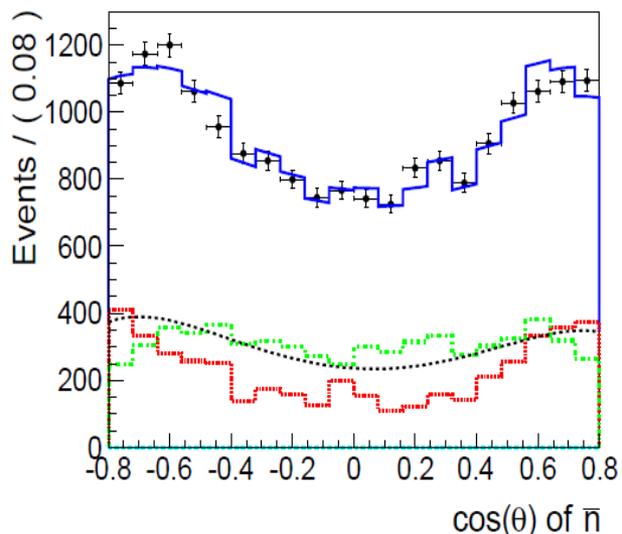
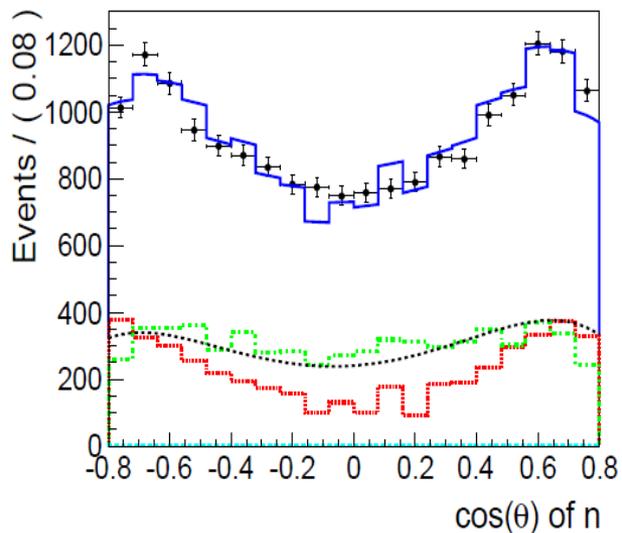
consistent with a phase, between strong and em decay, $\phi \sim 90^\circ$.

$\Psi(3686) \rightarrow p\bar{p}$ Angular Distribution



. Fit to $\cos(\theta)$ of p and \bar{p} with the formula $N_{sig}[(1 + \alpha \cos^2(\theta))\epsilon(\theta) + N_{bg}f_{bg}]$. The top one is of p , the bottom one is of \bar{p} . The error bars are data, the solid blue lines are the fit curves, the dashed red lines at the bottom of each plot are the backgrounds.

$\Psi(3686) \rightarrow n n_{\text{bar}}$ Angular Distribution



Separated fits to $\cos\theta$ distributions of n and \bar{n} . The data is shown in error bars. The fitted result is shown in solid blue curve. The signal shape is from the formula $(1 + \alpha \cos^2\theta)\epsilon(\theta)$, and is drawn on the plot in dashed black curve. Backgrounds are described by three components: shapes from continuum in dotted red, inclusive MC in dash-dotted green, and tiny contribution from $\psi' \rightarrow \gamma \chi_{cJ}, \chi_{cJ} \rightarrow n \bar{n}$ (not included in inclusive MC) in long-dashed cyan. All the amplitudes are fixed to the results from the fit to θ_{open} , only the variable of α is floating in the fit.

Magnetic B_M and Electric B_E Branching Ratios

- In e^+e^- annihilation the FF squared $|G_M|^2$ and $|G_E|^2$ are defined:
 - $d\sigma (e^+e^- \rightarrow BB_{\text{bar}})/d\cos\theta \sim [|G_M|^2 (1+\cos^2\theta) + 4 (M_B/W)^2 |G_E|^2 \sin^2\theta]$
 - $\sigma (e^+e^- \rightarrow BB_{\text{bar}}) \sim [|G_M|^2 + 2 (M_B/W)^2 |G_E|^2]$

- Accordingly, in a Vector Meson V decay B_M and B_E can be defined:
 - $B(V \rightarrow Bb_{\text{bar}}) = B_M + \tau \cdot B_E$, $\tau = 2 \cdot [M_N/M_{\psi'}]^2 \sim 0.13$
 - $d\sigma (V \rightarrow BB_{\text{bar}})/d\cos\theta \sim B \cdot [1 + \alpha \cdot \cos^2\theta]$
 $\alpha = [B_M - 2 \cdot \tau \cdot B_E] / [B_M + 2 \cdot \tau \cdot B_E]$ (by def. $|\alpha| \leq 1$).
 - τ small $\rightarrow B_E$ small effect on B
 - B and $\alpha \rightarrow B_M$ and B_E

Magnetic B_M and Electric B_E Branching Ratios

□ Toy MC to evaluate B_M and B_E errors from B and α :

Statistical and systematic errors added in quadrature

$$B_M[\psi(3686) \rightarrow nn_{\text{bar}}] = (2.60 \pm 0.26) \cdot 10^{-4} ,$$

$$B_E[\psi(3686) \rightarrow nn_{\text{bar}}] = (3.77 \pm 1.74) \cdot 10^{-4} .$$

□ In the pp_{bar} case, to avoid unphysical values, toy MC gaussian error simulation rejected any time $|\alpha_p| > 1$:

$$B_M[\psi(3686) \rightarrow pp_{\text{bar}}] = (3.02 \pm 0.13) \cdot 10^{-4} ,$$

$$B_E[\psi(3686) \rightarrow pp_{\text{bar}}] = (0.28 \pm 0.23) \cdot 10^{-4} .$$

□ Or, even better, simulating $0.95 \leq \alpha_p \leq 1$ with 68% probability, according to a Bayes approach:

$$B_M[\psi(3686) \rightarrow pp_{\text{bar}}] = (3.02 \pm 0.13) \cdot 10^{-4} ,$$

$$B_E[\psi(3686) \rightarrow pp_{\text{bar}}] = (0.24 \pm 0.18) \cdot 10^{-4} .$$

Phases between Strong and EM decays

- ❑ PQCD: asymptotically $B_E/B_M \rightarrow 0$, due to helicity conservation. But it cannot be the explanation of $\psi(3686)$ B_E behaviour, since it should be the same for pp_{bar} and nn_{bar} .
- ❑ Let exploit a possible interference between strong and em decay, assuming it is not the same for pp_{bar} and nn_{bar} .
 - Unfortunately the continuum $e^+e^- \rightarrow pp_{\text{bar}}$ is poorly measured at $W \sim 3.68$ GeV and there are poor information on $|G_E/G_M|$.
 - BaBar and BESIII: $\sigma(e^+e^- \rightarrow pp_{\text{bar}}) \sim (1.6 \pm 0.5)$ pb at $W \sim 3.68$ GeV
 $B_E/B_M \sim 1$ within a large uncertainty
(arXiv:1302.0055[hep-ex]1Feb2013, X.Zhu thesis)
 - Lacking any information, assume the same for $e^+e^- \rightarrow nn_{\text{bar}}$
 - Therefore $B_{\text{em}} = B[\psi(3686) \rightarrow \mu\mu] / \sigma(e^+e^- \rightarrow \mu\mu) \cdot \sigma(e^+e^- \rightarrow NN_{\text{bar}}) \sim 2 \cdot 10^{-6}$

For pp_{bar} and nn_{bar} assume: $B_M \sim B_E \sim B_{\text{em}}$

Phases between Strong and EM decays

□ Connecting pp_{bar} and nn_{bar} , it is assumed:

- $B_M^p = |S_M \cdot e^{i\phi} + E_M^p|^2 = |S_M|^2 + |E_M^p|^2 + 2 \cdot |S_M| \cdot |E_M^p| \cdot \cos\phi$
- $B_M^n = |S_M \cdot e^{i\phi} + E_M^n|^2 = |S_M|^2 + |E_M^n|^2 - 2 \cdot |S_M| \cdot |E_M^n| \cdot \cos\phi$
- Opposite sign in the interference term comes from opposite E_M sign

The two equations with two unknown (S_M and $\cos\phi$) can be solved.

Fluctuating B_M and E_M within the quoted errors, it is found:

$$S_M^2 = 2.79 \pm 0.15, \quad \phi_M = 63^\circ \pm 19^\circ$$

$$S_M^2 > 0, \quad |\cos\phi| < 1 : 94\% \text{ C.L.}$$

Results consistent with the expectation.

A better ϕ measurement requires a better continuum knowledge that is a **scan below and at $\psi(3686)$!**

A G parity violating Amplitude in $\psi(3686) \rightarrow p\bar{p}$?

- **No chance to find a solution for $p\bar{p}$ Electric decay, B_E^p : 0.2% C.L. to have $S_E^2 > 0$, $|\cos\phi| < 1$.**
- Therefore, additional to the strong amplitude S , it is assumed a G parity Violating Amplitude T in $B_E[\psi(3686) \rightarrow p\bar{p}]$, that is added to S negatively, to explain vanishing B_E in $p\bar{p}$, while there will be S only in B_E in $n\bar{n}$.
- In the following this assumption will be exploited, trying to determine T and the consistency of this approach

A G parity violating Amplitude in $\psi(3686) \rightarrow p\bar{p}$?

- Still assuming E^n and E^p have opposite signs, em decays may interfere negatively too or don't, as in the B_M case however T values achieved are the same, within the errors

- $\phi = 180^\circ$

$$\sqrt{B_{E^n}} = S^n + |E^n| \quad , \quad \sqrt{B_{E^p}} = S^p + |E^p|,$$

$$S^p = S^n + T$$

$$T = \sqrt{B_{E^p}} - \sqrt{B_{E^n}} - (|E^p| - |E^n|) \quad (< 0)$$

or

- $\phi = 90^\circ$

$$B_{E^n} = |S^n|^2 + |E^n|^2 \quad , \quad B_{E^p} = |S^p|^2 + |E^p|^2,$$

$$S^p = S^n + T$$

$$T = \sqrt{(B_{E^p} - |E^p|^2)} - \sqrt{(B_{E^n} - |E^n|^2)} \quad (< 0)$$

A G parity violating Amplitude in $\psi(3686) \rightarrow p\bar{p}$?

- Systematic errors in B^p and in B^n are partially correlated, so in the following statistical errors only are considered, extracting T from B_E^p and B_E^n :

$$B_E [\psi(3686) \rightarrow n\bar{n}] = (3.69 \pm 1.20) \cdot 10^{-4} ,$$

$$B_E [\psi(3686) \rightarrow p\bar{p}] = (0.22 \pm 0.16) \cdot 10^{-4}$$

- Therefore

$$|\tau T^2| \sim (2.7 \pm 1.0) \cdot 10^{-5} \text{ at the } \psi(3686)$$

- 99.9 % C.L. that $\tau T^2 < 0$

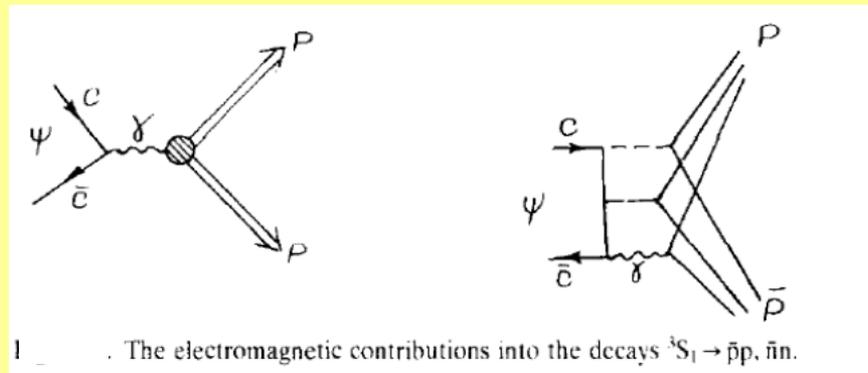
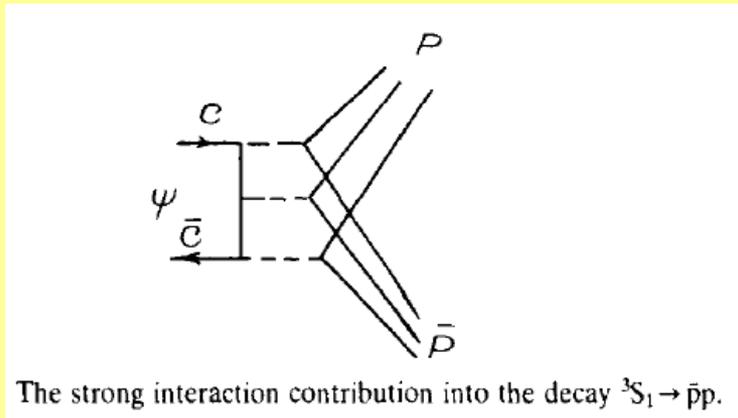
- **90. % C.L. that $\tau T^2 > 0.8 \cdot 10^{-5}$ (in comparison $B^p \sim 3 \cdot 10^{-4}$)**

A further Strong Amplitude in $J/\psi \rightarrow pp_{\text{bar}}$ too ?

- $\tau = 2 \cdot [M_N/M_{J/\psi}]^2 \sim 0.18$
Statistical and systematic errors still added in quadrature
 - $B_M[J/\psi \rightarrow nn_{\text{bar}}] = (17.6 \pm 2.0) \cdot 10^{-4}$,
 $B_E[J/\psi \rightarrow nn_{\text{bar}}] = (16.7 \pm 7.8) \cdot 10^{-4}$.
 - $B_M[J/\psi \rightarrow pp_{\text{bar}}] = (18.7 \pm 0.3) \cdot 10^{-4}$,
 $B_E[J/\psi \rightarrow pp_{\text{bar}}] = (13.0 \pm 0.7) \cdot 10^{-4}$.
 - $S_M^2 = 17.6 \pm 1.0$, $\phi_M = 84.7^\circ \pm 9.5^\circ$,
 $S_E^2 = 14.2 \pm 3.9$, $\phi_E = 100.8^\circ \pm 32.2^\circ$
 - $|\tau T^2| \sim (0.9 \pm 3.4) \cdot 10^{-5}$ at the J/ψ
- S_E too big to extract the G parity Violating Amplitude, if any

$\psi(3686) \rightarrow p\bar{p}$ decay via $2g1\gamma_{\text{virtual}}$

- A contribution from $\psi(3686) \rightarrow 2g1\gamma_{\text{virt}} \rightarrow N\bar{N}$ is expected.



$\psi(3686) \rightarrow pp_{\text{bar}}$ decay via $2g1\gamma_{\text{virtual}}$

- There will be 3 amplitudes, where the virtual γ will produce alternatively one of the 3 possible qq_{bar} pairs, inside NN_{bar} . Each amplitude will be proportional to the charge of the corresponding q , so that, adding the 3 amplitudes, the total will be proportional to the Baryon charge.
- Therefore the **contribution to nn_{bar} will vanish.**
While the **contribution to pp_{bar} should be negative.**
- Conversely in the case of a **negative Baryon, like Σ^- ,** $2g1\gamma_{\text{virt}}$ **contribution should interfere positively,** increasing B_E in pp_{bar} with respect to nn_{bar} .
It has to be evaluated.
- Since the $2g1\gamma_{\text{virt}}$ amplitude is small, it is difficult to check if contributes to B_M too

$\psi(3686) \rightarrow p\bar{p}$ decay via $2g1\gamma_{\text{virtual}}$

- S. Pacetti (BESIII 2015 Coll. Meeting, Shanghai Jiao Tong Un, June) has already discussed the $2g1\gamma_{\text{virtual}}$ contribution, showing the experimental evidence, according the present data on $J/\psi \rightarrow \pi\pi$ decay and $e^+e^- \rightarrow \pi\pi$, close to J/ψ :

$$\begin{aligned} \mathbf{B(J/\psi \rightarrow 2g1\gamma_{\text{virt}} \rightarrow \pi\pi)} &\sim \mathbf{10^{-4}}, \\ \mathbf{B(\psi(3686) \rightarrow 2g1\gamma_{\text{virt}} \rightarrow \pi\pi)} &\sim \mathbf{0.5 \cdot 10^{-5}}, \end{aligned}$$

and a quantitative successful **model**: $\gamma_{\text{virt}} \leftarrow \eta' \rightarrow \pi\pi$.

- The order of magnitude of the present result is close:

$$\mathbf{B(\psi' \rightarrow 2g1\gamma_{\text{virt}} \rightarrow NN_{\text{bar}})} \sim \mathbf{(2.7 \pm 1.0) \cdot 10^{-5}}$$

$$\mathbf{B(\psi' \rightarrow 2g1\gamma_{\text{virt}} \rightarrow NN_{\text{bar}}) / B(\psi' \rightarrow 3g \rightarrow NN_{\text{bar}})} \sim \mathbf{0.09 \pm 0.03}$$

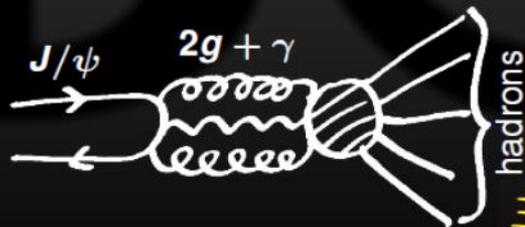
WHAT IS MISSING?



$$B(J/\psi \rightarrow 3g) = \alpha_s^3(M_{J/\psi}) \frac{|\psi(0)|^2 D_{\text{QCD}}}{\Gamma_{J/\psi}}$$



$$B(J/\psi \rightarrow \mu^+ \mu^-) = \alpha^2 \frac{|\psi(0)|^2 D'_{\text{QCD}}}{\Gamma_{J/\psi}}$$



$$B(J/\psi \rightarrow 2g + \gamma) = \alpha_s^2(M_{J/\psi}) \alpha \frac{|\psi(0)|^2 D''_{\text{QCD}}}{\Gamma_{J/\psi}}$$

Strong G-parity violation?

DECAYS OF J/ψ AND $\psi(2S)$ INTO $\pi^+\pi^-$

$M \rightarrow \pi^+\pi^-$	$\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ (nb)	$\mathcal{B}_\gamma(M \rightarrow \pi^+\pi^-)$	$\mathcal{B}_{\text{PDG}}(M \rightarrow \pi^+\pi^-)$
$M = J/\psi$	$(9 \pm 3) \times 10^{-3}$ at $\sqrt{q^2} = 3 \text{ GeV}$	$(0.54 \pm 0.18) \times 10^{-4}$	$(1.47 \pm 0.14) \times 10^{-4}$
$M = \psi(2S)$	$(2.4 \pm 0.8) \times 10^{-3}$ at $\sqrt{q^2} = M_{\psi(2S)}$	$(2.2 \pm 0.7) \times 10^{-6}$	$(7.8 \pm 2.6) \times 10^{-6}$

* Cross sections have been obtained by **extrapolating** BaBar data by means of the Gounaris-Sakurai model

* In case of J/ψ the discrepancy between \mathcal{B}_γ and \mathcal{B}_{PDG} is

$$\frac{\mathcal{B}_{\text{PDG}} - \mathcal{B}_\gamma}{\delta[\mathcal{B}_{\text{PDG}} - \mathcal{B}_\gamma]} \Big|_{J/\psi} = 4.1 \pm 1.0$$

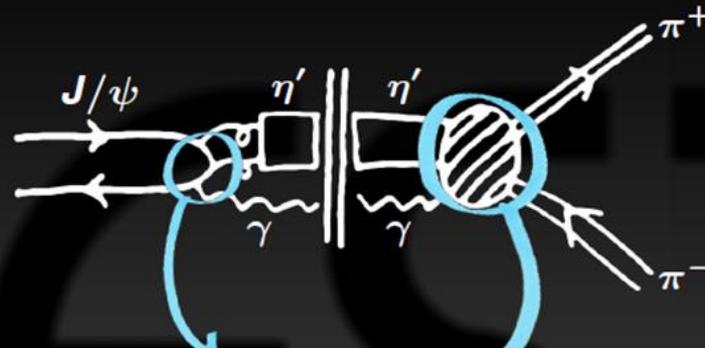
**4.1 sigma effect
for J/ψ**

* Also in case of $\psi(2S)$ there is discrepancy but, due to the larger error

$$\frac{\mathcal{B}_{\text{PDG}} - \mathcal{B}_\gamma}{\delta[\mathcal{B}_{\text{PDG}} - \mathcal{B}_\gamma]} \Big|_{\psi(2S)} = 2.1 \pm 1.0$$

**2.1 sigma effect
for $\psi(2S)$**

AN ESTIMATE OF $\mathcal{A}_{2g\gamma}$ FOR THE DECAY $J/\psi \rightarrow \pi^+\pi^-$

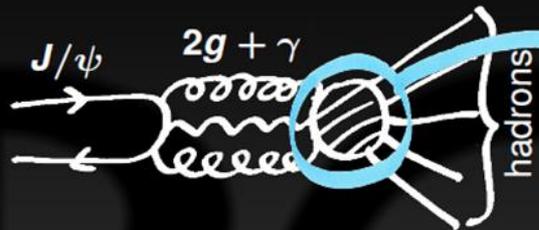


$$|\text{Im}[\mathcal{A}_{\eta'\gamma}]| = \frac{1}{48\pi} \frac{M_{J/\psi}^4 |g_{\eta'\gamma}^{J/\psi}| |g_{\eta'\gamma}^{\pi\pi}|}{\sqrt{(M_\rho^2 - M_{J/\psi}^2)^2 + \Gamma_\rho^2 M_\rho^2}} \sqrt{\frac{M_{J/\psi}^2}{4} - M_\pi^2} \left(1 - \frac{M_{\eta'}^2}{M_{J/\psi}^2}\right)^3$$

The coupling constants are obtained from experimentally known decay rates

- * $\Gamma(\eta' \rightarrow \pi^+\pi^-\gamma) \rightarrow |g_{\eta'\gamma}^{\pi\pi}|$
- * $\Gamma(J/\psi \rightarrow \eta'\gamma) \rightarrow |g_{\eta'\gamma}^{J/\psi}|$

HOW TO ESTIMATE THE $2g + \gamma$ CONTRIBUTION



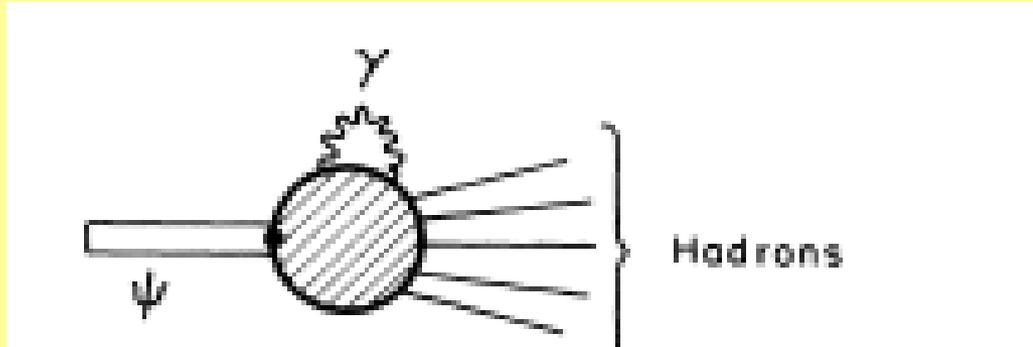
- * It is difficult to compute the $\mathcal{A}_{2g\gamma}$ contribution to $\mathcal{A}(J/\psi \rightarrow \mathcal{H}_q)$
- * In particular, the hadronization mechanism $2g + \gamma \rightarrow \mathcal{H}_q$ is unknown
- * Only $3g/(2g + \gamma)$ relative rates are easily computable, having the same number of vector bosons...

In case of G -parity-conserving decays $J/\psi \rightarrow \mathcal{H}_q$

$$\frac{\mathcal{B}(J/\psi \rightarrow 3g \rightarrow \mathcal{H}_q)}{\mathcal{B}(J/\psi \rightarrow 2g + \gamma \rightarrow \mathcal{H}_q)} = \frac{\alpha_s(M_{J/\psi})}{\alpha} \frac{D_{\text{QCD}}}{D'_{\text{QCD}}} = 7.28 \pm 0.92$$

$\psi(3686) \rightarrow p\bar{p}$ decay via $2g1\gamma_{\text{virtual}}$

- M.S.Chanowitz (P.R. D12 (1975) 918) also considered 1 γ_{virt}



- and made an estimation, assuming $\alpha_s \sim 0.3$ at the $\psi(3686)$:

$$\mathbf{B(J/\psi \rightarrow 2g1\gamma_{\text{virt}} \rightarrow H) / B(J/\psi \rightarrow 3g \rightarrow H) \sim 16/5 \alpha / \alpha_s P \sim 0.08 P,}$$

- P is a factor to take into account "the effective coupling of the photon to $q\bar{q}$ in the $c\bar{c}$ decay volume", ranging from α to 1. According to the present results P should be close to 1.

$\psi(3686) \rightarrow p\bar{p}$ decay via $2g1\gamma_{\text{virtual}}$

- V.L.Cherniak and A.R.Zitniski (Phys.Rep. 112, 3 (1984) 173) also considered $1\gamma_{\text{virt}}$, and made an estimation, on the basis of PQCD, applied on both $1\gamma_{\text{virt}}$ vertices (generation and hadronization), assuming $\alpha_s \sim 0.3$:

$$A(\text{J}/\psi \rightarrow 2g1\gamma_{\text{virt}} \rightarrow \text{H}) / A(\text{J}/\psi \rightarrow 3g \rightarrow \text{H}) \sim 4/5 \alpha_s / \alpha_s$$

$$\mathbf{B(\text{J}/\psi \rightarrow 2g1\gamma_{\text{virt}} \rightarrow \text{H}) / B(\text{J}/\psi \rightarrow 3g \rightarrow \text{H}) \sim 0.4 \cdot 10^{-3}}$$

- Chanowitz questioned the factor 4/5 and the validity of PQCD in the hadronization regime.
 - Actually, according V.L.Cherniak and A.R.Zitniski, by the same token : $A(\text{J}/\psi \rightarrow 2g1\gamma_{\text{virt}} \rightarrow \pi\pi) \sim 0$ in contradiction with present data, as shown by Simone.

Temporary Conclusions

- A contribution from $\psi(3686) \rightarrow 2g1\gamma_{\text{virt}} \rightarrow NN_{\text{bar}}$ is expected and likely found in the vanishing Electric Proton Branching Ratio B_E^p , with respect to the Electric Neutron Branching Ratio B_E^n .

- It turns out:

$$B(\psi(3686) \rightarrow 2g1\gamma_{\text{virt}} \rightarrow NN_{\text{bar}}) \sim (2.8 \pm 1.9) \cdot 10^{-5}$$

(99.4% CL that $B > 0$, 90% CL that $B > 3 \cdot 10^{-6}$)

and there is **a negative interference between 3g and 2g1 γ_{virt}**

- The evidence of this G parity violation is good, according the achieved CL. Unfortunately statistics is not enough to get also good accuracy
- Present theoretical predictions are affected by lack of knowledge concerning the hadronization

Temporary Conclusions

- ❑ Opposite behaviour is expected in the Σ^- and Σ^+ branching ratios, to be evaluated
- ❑ A better determination would shed light on the hadronization mechanism (validity of PQCD)
- ❑ B_M phase, between strong and em decay, $\phi_M = 63^\circ \pm 19^\circ$, but present continuum knowledge has large uncertainties -> scan below and at $\psi(3686)$!
- ❑ Work in progress, however, once more.....



BARYONS STRIKE BACK IN BESIII