# Measurements of $\sigma\left(\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi \mathbf{X}\right)$ in Range from 3.645 to 3.891 GeV 

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## OUTLINE

- Introduction
- Measurements of Cross Sections
- Analysis of Observed Cross Sections
- Summary


## Introduction

Measurements of cross sections for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi \mathbf{X}$ would help better understanding
$\checkmark$ the anomaly line-shape of cross sections for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow$ hadrons observed at the BES-II Expt.

$\checkmark$ the non-open charm decays of heavy cc-bar states or cc-bar-like states
$\checkmark$ the dynamics of heavy charmonium production and decays
$\checkmark$ the non-DD decays of $\psi(3770)$ decays
It would also help in searching for new structure(s) in the open-charm energy region

## Data Samples \& Software

$>$ Data Samples
$-44.5 \mathrm{pb}^{-1} @ 3.650 \mathrm{GeV}$
$-928 \mathrm{pb}^{-1} @ 3.773 \mathrm{GeV}$

- About 2 pb $^{-1}$ fast $\psi(\mathbf{3 6 8 6})$ scan data


## New <br> reconstructed data and a complete New Analysis

- About 70 pb $^{-1}$ energy scan data taken in range from 3.700 to 3.891 GeV
>Software
- BOSS software 6.6.4.p01
- Monte Carlo events were generated with KKMC + BesEvtGen


## Event Selection

$>$ Charged track selection

- $\left|\mathrm{R}_{\mathrm{xy}}\right|<1.0 \mathrm{~cm}$ and $\left|\mathrm{R}_{\mathrm{z}}\right|<10.0 \mathrm{~cm}$;
- |cose| < 0.93
$-|\cos \theta|<0.81$ for leptons (to reject Bhabha scattering events);
$>$ Lepton selection
$-1.0 \mathrm{GeV}<\mathrm{p}<0.47 \mathrm{E}_{\mathrm{cm}}$
$-\mathrm{E} / \mathrm{p}>0.7$ for electron
$-0.05<\mathrm{E} / \mathrm{p}<0.35$ for muon
$>$ Photon selection:

$-\mathrm{E}_{\mathrm{EMC}}>25(50) \mathrm{MeV}$ for barrel (end-cap) calorimeter
$-\theta_{\gamma, \text { charge }}>10^{\circ}$
$-0 \leq \mathrm{TDC} \leq 14$


## Event Selection

$>$ Number of good charged tracks and photons satisfy:

- $\mathrm{N}_{\text {good }}=2$ and $\mathrm{N}_{\gamma} \geq 2$
- $3 \leq \mathrm{N}_{\text {good charge }} \leq 4$
$>$ Other requirements
$-1^{+1}$ opening angle $\theta_{\text {e+e- or } \mu+\mu-}<179^{\circ}$
- Charged tracks not identified as

leptons are subject to particle identification (based on
$\mathrm{dE} / \mathrm{dx}$ and TOF): $\mathrm{CL}(\pi)>\mathrm{CL}(\mathrm{K})$ to select $\pi^{+/-}$
$>$ Signal of J/ $\psi \mathbf{X}$
Examine invariant mass of $\mathrm{I}^{+1-}$ to get number of $\mathrm{J} / \Psi \mathrm{X}$ events from data set


## Lepton-pair Mass Spectra

Only show a few mass spectra as an example (More plots in Back Up slides)






The signal and background shapes are described by MC-Shape of the mass distribution of lepton pair and $2^{\text {nd }}$ order Chebychev polynomial, respectively.
Fitting these $\mathbf{M}_{\| I}$ spectra yields the observed number of signal events for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi \mathbf{X}$ at these energy points.

## Background Subtraction

- Major background: $\mathbf{e}^{+} \mathbf{e}^{-} \rightarrow\left(\gamma_{\text {ISR }}\right) \mathrm{J} / \psi \rightarrow \mathrm{l}^{+} \mathrm{l}^{-}$

- The mis-identification rate is determined from MC simulation:

$$
\eta=(0.200 \pm 0.024) \%
$$

- The expected cross section is calculated using resonance parameters of J/ $\psi$.

- The number of background events:

$$
N_{\mathrm{BCK}}=L \times \sigma_{J / \psi} \eta
$$

## Monte Carlo Events \& Efficiencies

$>$ Monte Carlo events are generated with the BES-III Standard ISR KKMC + EvtGen MC generator.
$-\pi^{0}$ and $\eta$ are set to decay into any possible final states;
$-\mathrm{J} / \psi$ is set to decay into $\mathrm{e}^{+} \mathrm{e}^{-}$or $\mu^{+} \mu^{-}$;

- The ratio of each process is determined with its branching fraction.
$>$ In determination of the efficiency for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi \mathrm{X}$, we consider the mixture of the $\psi(3686)$ and $\psi(3770)$ decay into these final states.


## Monte Carlo Events \& Efficiencies

- $\psi(3686) \rightarrow \mathrm{J} / \psi \mathbf{X}$

| $\psi(3686) \rightarrow$ | Br | Ratio | MODEL |
| :---: | :---: | :---: | :---: |
| $\mathrm{J} / 4 \pi^{+} \pi^{-}$ | $(34.45 \pm 0.30) \%$ | 0.5631 | JPIPI+PHOTOS VLL |
| $\mathrm{J} / 4 \pi^{0} \pi^{0}$ | (18.13 $\pm 0.31) \%$ | 0.2963 | JPIPI + PHOTOS VLL |
| $\mathrm{J} / \psi \eta$ | $(3.36 \pm 0.05) \%$ | 0.0549 | HELAMP+PHOTOS VLL |
| $\mathrm{J} / \psi \pi^{0}$ | $(0.1268 \pm 0.0032) \%$ | 0.0021 | HELAMP+PHOTOS VLL |
| $\gamma \chi_{00}, \chi_{00} \rightarrow \gamma \mathrm{~J} / \psi$ | $(9.99 \pm 0.27) \% \times(1.27 \pm 0.06) \%$ | 0.0021 | P2GC0+S2GV+PHOTOS VLL |
| $\gamma \chi_{\text {cl }}, \chi_{\text {cl }} \rightarrow \gamma \mathrm{J} / \psi$ | $(9.55 \pm 0.31) \% \times(33.9 \pm 1.2) \%$ | 0.0529 | P2GC1+AV2GV+PHOTOS VLL |
| $\gamma \chi_{\text {c2 }}, \chi_{\text {c2 }} \rightarrow \gamma \mathrm{J} / \psi$ | $(9.11 \pm 0.31) \% \times(19.2 \pm 0.7) \%$ | 0.0286 | P2GC2+PHSP+PHOTOS VLL |



- $\psi(3770) \rightarrow \mathbf{J} / \psi \mathbf{X}$

| $\psi(3770) \rightarrow$ | Br | Ratio | MODEL |
| :---: | :---: | :---: | :---: |
| $\mathrm{J} / \psi \pi^{+} \pi^{-}$ | $(1.93 \pm 0.28) \times 10^{-3}$ | 0.3956 | JPIPI+PHOTOS VLL |
| $\mathrm{J} / 4 \pi^{0} \pi^{0}$ | $(8.0 \pm 3.0) \times 10^{-4}$ | 0.1640 | JPIPI+PHOTOS VLL |
| $\mathrm{J} / \psi \eta$ | $(9.0 \pm 4.0) \times 10^{-4}$ | 0.1845 | HELAMP + PHOTOS VLL |
| $\gamma \chi_{00}, \chi_{00} \rightarrow \gamma \mathrm{~J} / \psi$ | $(7.3 \pm 0.9) \times 10^{-3} \times(1.27 \pm 0.06) \%$ | 0.0190 | P2GCO+S2GV+PH0TOS VLL |
| $\chi_{\text {cl }} \chi_{\text {c }} \chi_{\text {cl }} \rightarrow \gamma \mathrm{J} / \psi$ | $(2.9 \pm 0.6) \times 10^{-3} \times(33.9 \pm 1.2) \%$ | 0.2015 | P2GC1+AV2GV+PHOTOS VLL |
| $\gamma \chi_{c_{22}} \chi_{\mathrm{c}_{2} \rightarrow \gamma \mathrm{~J} / \psi}$ | $9.0 \times 10^{-4} \times(19.2 \pm 0.7) \%$ | 0.0354 | PHSP+PHSP+PHOTOS VLL |



- Efficiency of $\mathbf{e}^{+} \mathbf{e}^{-} \rightarrow \mathbf{J} / \boldsymbol{\psi} \mathbf{X}$

$$
\bar{\epsilon}=\frac{1}{\sigma_{\mathrm{J} / \psi \mathrm{X}}^{\psi(3686)}+\sigma_{\mathrm{J} / \psi \mathrm{X}}^{\psi(3770)}}\left(\sigma_{\mathrm{J} / \psi \mathrm{X}}^{\psi(3686)} \times \epsilon_{\psi(3686)}+\sigma_{\mathrm{J} / \psi \mathrm{X}}^{\psi(3770)} \times \epsilon_{\psi(3770)}\right)
$$

## Observed Cross Sections

## Cross Sections

$$
\sigma^{\mathrm{obs}}=\frac{N^{\mathrm{obs}}\left(e^{+} e^{-} \rightarrow J / \psi X\right)}{L \times \mathcal{E} \times B\left(J / \psi \rightarrow l^{+} l^{-}\right)}
$$

- $N^{\text {obs: }}$ Number of signal events;
- $L$ : Luminosity;
- $\varepsilon$ : Efficiency
- $B$ : Branching fraction of $J / \psi \rightarrow l^{+} l^{-}$


Analysis of this observed cross section needs the expectedobserved cross sections for this final state, which can be obtained with BW function and ISR sampling function.

## Number of events \＆Cross Sections

| $E_{\text {max }}(\mathrm{GNV})$ | $N_{\text {d／}}^{\text {dim }}$ | $N_{\text {mick }}^{\text {bim }}$ | $C\left(\mathrm{nb}^{-1}\right)$ | $5^{4 / 4 / 4 x}$ | ${ }^{5} \mathrm{C} / \mathrm{MX}$ | $\mathrm{g}_{\mathrm{j} / \mathrm{dx}}^{\text {P／}}$ |  | $5_{\sqrt{1 / \psi}} \mathrm{x}$ | －（ab） |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3．4451 | $8.9 \pm 6.1$ | $20 \pm 0.1$ | 限环62 $\pm 2.4146$ |  | 0.5490 | 0.0 .593 | 0.0012 | 0.54 .15 | $0.1802 \pm 0.1002$ |
| 1.8989 | $9.1 \pm 3.7$ | $0.2 \pm 0.0$ | $4.1467 \pm 0.71{ }^{2}$ | 0.15714 | 0.5661 | 1.6863 | 0.0021 | 0.5714 | $2.800 \pm 1.1107$ |
| 3.879 | $10.7 \pm 4.1$ | $0.2 \pm 0.0$ |  | 0.51518 | 0．5665 | 2 228 | 0.0021 | 0.5716 | $5.3414 \pm 1.3001$ |
| 2.8059 | $15.9 \pm 4.8$ | $0.2 \pm 0.0$ | 42609 $\pm 0.716$ | 0.51518 | 0.5670 | 488884 | 0.0022 | 0.5718 | $4.4887 \pm 1.48 \mathrm{EL}$ |
| 1．8818 | $20.4 \pm 5.5$ | $0.2 \pm 0.0$ |  | 0.15720 | 0.5674 | 8.81814 | 0.0022 | 0.5720 | $5.7637 \pm 1.55 \cdot 40$ |
| 1．8822 | $4.4 \pm 8.0$ | $0.2 \pm 0.0$ | 60．960 $\pm 0.7277$ | 0.6720 | 0.5875 | 13．19．67 | 0.0022 | 0.5720 | $14.2315 \pm 2.2315$ |
| 2．8826 | $80.1 \pm 9.8$ | $0.2 \pm 0.0$ | $61.152 \pm \pm 0.7287$ | 0.57721 | 0.5877 | 22．238 | 0.0029 | 0．572 | 2． $2.29 \pm \pm 2.85$ |
| 3．8484 | $249.8 \pm 10.0$ | $0.2 \pm 0.0$ | $61.7628 \pm 0.7809$ | 0.16728 | 0.5880 | 64．19\％ | 0.0029 | 0.5729 | $62.4359 \pm 4.6395$ |
| 2．8840 | $469.1 \pm 7.9$ | $0.2 \pm 0.0$ | 60．0911 $\pm 0.7202$ | 0.15724 | 0.5889 | 18.2804 | 0.0029 | 0.574 | 138．1535土 6.5448 |
| 2．8848 | $776.3 \pm 2.8$ | $0.2 \pm 0.0$ | $48.7171 \pm 0.70 .40$ | 0.15725 | 0.5885 | W\％．015 | 0.0024 | 0.5725 | $23.4413 \pm 9.2 .678$ |
| 2．8848 | $85.0 \pm 31.4$ | $0.1 \pm 0.0$ | $3.8799 \pm 0.88 .85$ | 0.16725 | 0.588 | 267.1420 | 0.0024 | 0.5725 | \＄15．1202 12.6028 |
| 3.8854 | $1090.2 \pm 37.8$ | $0.1 \pm 0.0$ | $38.0840 \pm 0.8197$ | 0.15728 | 0.5689 | \＄56．078 | 0.0024 | 0.5728 | 401．9608 14.6235 |
| 2．880 | $1097.4 \pm 34.8$ | $0.1 \pm 0.0$ | $41.1700 \pm 0.8488$ | 0.16727 | 0.6591 | 416．188 | 0.0024 | 0.5727 | 900．0002 13.8770 |
| 2．8888 | $1068.4 \pm 37.6$ | $0.1 \pm 0.0$ | $40.144 \pm 0.8402$ | 0.15728 | 0.5954 | 400.2688 | 0.0025 | 0.5728 | 988．6\％00 13.7678 |
| ${ }^{2.8873}$ | $878.8 \pm 30.5$ | $0.1 \pm 0.0$ | 40.6850 | 0.1572 | 0.5696 | 927．2611 | 0.0025 | 0.5729 | 317，6458 12.1385 |
| 3.8874 | $82.2 \pm$ \％2． | $0.1 \pm 0.0$ | $40.0975 \pm 0.0440$ | 0.1672 | 0.5697 | 311.8015 | 0.0025 | 0.5729 | 9016065 11.0000 |
| 1．8890 | $300.9 \pm 18.6$ | $0.1 \pm 0.0$ | $40.668 \pm \pm 0.6540$ | 0.67312 | 0.5001 | 100.9777 | 0.0028 | 0.5779 | 100．1990土 6.944 |
| 3.8920 | $73.0 \pm 2.8$ | $0.1 \pm 0.0$ | $41.6615 \pm 0.6864$ | 0.6737 | 0.7515 | 2 Cm 2156 | 0.0028 | 0.5737 | $25.7451 \pm 3.4688$ |
| 1．8984 | $4.5 \pm 8.1$ | $0.2 \pm 0.0$ | $4.68670 \pm 0.734 .3$ | 0.1574 | 0.6792 | 14．9660 | 0.0031 | 0.5744 | $14.5745 \pm 2.4021$ |
| 3.7002 | $32.5 \pm 8.4$ | $0.2 \pm 0.0$ | 阿708 $\pm 0.79 \%$ | 0.15760 | 0.5748 | 10．4916 | 0.0034 | 0.5750 | $9.9414 \pm 1.865$ |
| 1.7055 | $7.9 \pm 5.5$ | $0.2 \pm 0.0$ | $0.4076 \pm 0.8060$ | 0.15769 | 0.5764 | T． 8.1777 | 0.0099 | 0.5759 | $5.405 \pm \pm 1.9393$ |
| Continud an nuxt page |  |  |  |  |  |  |  |  |  |

# Number of events \& Cross Sections 

| $E_{\text {cme }}(\mathrm{CeV})$ | $N_{\text {d/¢ }}^{\text {asm }}$ | $N_{\text {max }}^{\text {OEM }}$ | $\mathcal{L}\left(\mathrm{nb}^{-1}\right)$ | $5^{4 / 2 / 2 x}$ | $\varepsilon_{j / 20 x}^{\text {¢ (3ive }}$ | $\sigma^{+1 / 2 / 2 x}$ | $a^{4 / 20 x}$ |  | $\sigma$ (mb) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.7136 | $44.6 \pm 7.8$ | $0.3 \pm 0.0$ | $106.1170 \pm 1.0643$ | 0.5771 | 0.5791 | 5.4790 | 0.0049 | 0.5771 | 8.0002土 1.0748 |
| 3.7215 | $41.8 \pm 7.7$ | $0.4 \pm 0.0$ | $136.0653 \pm 1.2068$ | 0.5781 | D.5814 | 4.2963 | D.0063 | 0.5781 | $4.4327 \pm 0.8257$ |
| 3.7296 | $74.7 \pm 10.1$ | $0.7 \pm 0.0$ | $229.2308 \pm 1.5709$ | 0.5792 | 0.5837 | 3.5229 | D.008 | 0.5792 | $4.6081 \pm 0.6417$ |
| 3.7368 | $113.6 \pm 13.0$ | $1.5 \pm 0.1$ | $494.1513 \pm 2.3094$ | 0.5801 | 0.5855 | 3.0389 | 0.0117 | 0.5801 | $3.2954 \pm 0.3824$ |
| 3.7454 | $213.4 \pm 17.7$ | $2.8 \pm 0.2$ | $955.3906 \pm 3.2190$ | 0.5810 | D.5874 | 2.6113 | D.0181 | 0.5810 | $3.1983 \pm 0.2688$ |
| 3.7470 | $287.8 \pm 20.7$ | $4.1 \pm 0.3$ | $1409.9051 \pm 3.9121$ | 0.5812 | 0.5878 | 2.5447 | D.0199 | 0.5813 | $2.9163 \pm 0.2129$ |
| 3.7493 | $391.9 \pm 24.7$ | $6.6 \pm 0.5$ | $2278.7528 \pm 4.9773$ | 0.5815 | 0.5883 | 2.4547 | 0.0228 | 0.5816 | $2.4458 \pm 0.1571$ |
| 3.7508 | $540.0 \pm 29.0$ | $8.6 \pm 0.6$ | $2979.2289 \pm$ E.6927 | 0.5816 | 0.5886 | 2.3994 | 0.0280 | 0.5817 | $2.6834 \pm 0.1411$ |
| 3.7530 | $611.9 \pm 31.0$ | $2.5 \pm 0.7$ | $3317.8297 \pm 6.0108$ | 0.5819 | 0. 58890 | 23227 | 0.0288 | 0.5820 | $2.6255 \pm 0.1359$ |
| 3.7544 | $563.7 \pm 30.0$ | 2.8 $\pm 0.7$ | $3426.9142 \pm 6.1112$ | 0.5820 | 0.5893 | 2.2763 | 0.0317 | 0.5821 | $2.3392 \pm 0.1268$ |
| 3.7558 | $691.0 \pm 33.2$ | $11.1 \pm 0.8$ | $3883.0165 \pm 6.5083$ | 0.5821 | 0.5895 | 2.2918 | 0.0348 | 0.5822 | $2.6336 \pm 0.1298$ |
| 3.7587 | $769.2 \pm 34.7$ | $12.7 \pm 0.9$ | $4451.5634 \pm 6.9739$ | 0.5824 | 0.5901 | 2.1448 | D.0428 | 0.5826 | $2.4577 \pm 0.1128$ |
| 3.7617 | $716.4 \pm 34.0$ | $12.7 \pm 0.9$ | $4503.1528 \pm 7.0189$ | 0.6827 | 0.5906 | 2.0617 | D.0530 | 0.5829 | $2.2684 \pm 0.1002$ |
| 3.7645 | $469.6 \pm 27.8$ | $2.9 \pm 0.7$ | $3292.6249 \pm 6.0069$ | 0.58380 | 0.5911 | 1.9896 | D.0842 | 0.5833 | $2.0194 \pm 0.1220$ |
| 3.7674 | $927.5 \pm 23.3$ | $6.9 \pm 0.5$ | $2448.9605 \pm 5.1843$ | 0.8832 | 0.5915 | 1.9201 | 0.0764 | 0.58335 | $1.8504 \pm 0.1374$ |
| 3.7702 | $243.1 \pm 20.3$ | $5.6 \pm 0.4$ | $2021.5679 \pm 4.7135$ | 0.5835 | 0. 5920 | 1.8574 | D.0865 | 0.5839 | $1.6049 \pm 0.1449$ |
| 3.7731 | $214.4 \pm 19.5$ | $5.1 \pm 0.4$ | $1831.6311 \pm 4.4906$ | 0.5837 | D.E.5924 | 1.7966 | 0.0920 | 0.5841 | $1.6483 \pm 0.1536$ |
| 9.7760 | $245.9 \pm 20.0$ | $5.0 \pm 0.4$ | $1829.4733 \pm 4.4900$ | 0.5840 | 0. 5928 | 1.7398 | 0.0914 | 0.5844 | $1.8978 \pm 0.1577$ |
| 3.7789 | $277.0 \pm 21.2$ | $6.4 \pm 0.4$ | $1958.8374 \pm 4.6491$ | 0.5842 | 0. 5933 | 1.6858 | 0.0839 | 0.5846 | $2.0004 \pm 0.1562$ |
| 3.7818 | $283.9 \pm 21.6$ | $5.9 \pm 0.4$ | $2158.7390 \pm 4.8840$ | 0.88 .4 | 0.5935 | 1.6354 | 0.0735 | 0.5848 | $1.8571 \pm 0.1443$ |
| 3.7847 | $327.6 \pm 23.2$ | $6.9 \pm 0.5$ | $2658.7382 \pm 5.3213$ | 0.5847 | D. 5939 | 1.5879 | D.0827 | 0.5850 | $1.8090 \pm 0.1307$ |
| 3.7873 | $36.4 .8 \pm 24.7$ | $7.7 \pm 0.5$ | $28.40 .9075 \pm 5.6136$ | 0.58 .49 | 0. 5942 | 1.5475 | 0.0540 | 0.5852 | $1.8097 \pm 0.1262$ |
| 3.7915 | $430.6 \pm 28.9$ | $2.5 \pm 0.7$ | $3542.76 .57 \pm 6.2762$ | 0.6852 | 0.E.546 | 1.4864 | D.0426 | 0.5855 | $1.7104 \pm 0.1009$ |
| 3.7952 | $484.5 \pm 28.5$ | $10.8 \pm 0.8$ | $4060.9093 \pm 6.7263$ | 0.5854 | 0.5950 | 1.4363 | D.0351 | 0.5856 | $1.6780 \pm 0.1010$ |
| 3.7989 | $408.0 \pm 27.6$ | $10.4 \pm 0.7$ | $3941.2619 \pm 6.6372$ | 0.5856 | 0. 5953 | 1.3896 | 0.0293 | 0.5858 | $1.4508 \pm 0.1004$ |
| 3.8030 | $268.0 \pm 22.5$ | $7.1 \pm 0.5$ | $2701.8225 \pm 6.4977$ | 0.5859 | 0.5957 | 1.3400 | 0.0245 | 0.5861 | $1.3775 \pm 0.1197$ |
| 3.8068 | $168.5 \pm 18.2$ | 4.6 $\pm 0.3$ | $1785.8710 \pm 4.4484$ | 0.6881 | 0.5960 | 1.2987 | 0.0211 | 0.5863 | $1.3938 \pm 0.1481$ |
| 3.8099 | $121.8 \pm 14.9$ | $3.3 \pm 0.2$ | $1258.1692 \pm 3.7680$ | 0.6883 | 0.5962 | 1.2661 | 0.0188 | 0.5864 | $1.3535 \pm 0.1700$ |
| 3.8128 | $87.9 \pm 12.8$ | $2.3 \pm 0.2$ | $899.8812 \pm 3.1812$ | 0.6885 | 0.5964 | 1.2371 | D.0170 | 0.5866 | $1.3657 \pm 0.2043$ |
| 3.8160 | $66.5 \pm 11.1$ | $1.8 \pm 0.1$ | $682.4762 \pm 2.7732$ | 0.5888 | D.5966 | 1.2065 | 0.0154 | 0.5867 | $1.1519 \pm 0.2338$ |
| 3.8240 | $31.4 \pm 7.8$ | $1.0 \pm 0.1$ | $400.9634 \pm 2.1290$ | 0.5870 | 0.E970 | 1.1360 | 0.0123 | 0.5871 | $1.0877 \pm 0.2792$ |
| 3.8319 | $45.2 \pm 8.2$ | $0.7 \pm 0.1$ | $285.6685 \pm 1.8016$ | 0.5874 | 0.E.5972 | 1.0738 | D.0101 | 0.5875 | $2.2340 \pm 0.4120$ |
| 3.8400 | $22.1 \pm 6.5$ | $0.7 \pm 0.0$ | $281.1397 \pm 1.7910$ | 0.5877 | Q.E.5974 | 1.0165 | D.0086 | 0.5878 | $1.0014 \pm 0.3315$ |
| 3.8479 | $19.7 \pm 6.1$ | $0.7 \pm 0.0$ | $277.4507 \pm 1.7823$ | 0.5879 | Q.E975 | 0.9689 | D.0074 | 0.58880 | $0.9826 \pm 0.3151$ |
| 3.8561 | $16.4 \pm 5.8$ | $0.8 \pm 0.1$ | $319.9245 \pm 1.9191$ | 0.6881 | 0.5976 | 0.9182 | D.0065 | 0.58882 | $0.6999 \pm 0.2697$ |
| 3.8640 | $14.9 \pm 5.5$ | $0.7 \pm 0.1$ | $301.2150 \pm 1.8657$ | 0.5883 | D.5975 | 0.8764 | 0.0057 | 0.5884 | $0.6744 \pm 0.2615$ |
| 3.8719 | $38.1 \pm 8.1$ | $1.2 \pm 0.1$ | $514.1173 \pm 2.4421$ | 0.5885 | 0.E.5974 | 0.8379 | D.0052 | 0.5886 | $0.9717 \pm 0.2266$ |
| 388809 | $14.4 \pm 5.0$ | $0.4 \pm 0.0$ | $190.1108 \pm 1.4884$ | 0.5886 | 0.5972 | 0.7979 | D.0046 | 0.5886 | $1.0611 \pm 0.3765$ |
| 3.8909 | $8.2 \pm 4.4$ | $0.4 \pm 0.0$ | $183.4354 \pm 1.4658$ | 0.5887 | D.E.5970 | 0.7574 | 0.0041 | 0.5887 | $0.6073 \pm 0.3439$ |
| 3.6474 | $28.3 \pm 12.5$ | $8.1 \pm 0.6$ | $2280.9188 \pm 4.8176$ | 0.5651 | D.E50.4 | 0.0691 | 0.0012 | 0.5648 | $0.1338 \pm 0.0825$ |
| 3.6594 | $21.1 \pm 12.0$ | $7.8 \pm 0.6$ | $2217.7081 \pm 4.7789$ | 0.6684 | 0.5637 | 0.0819 | 0.0019 | 0.5662 | $0.0893 \pm 0.0806$ |
| 3.7269 | $239.4 \pm 18.7$ | $2.7 \pm 0.2$ | $896.6686 \pm 3.1023$ | 0.6788 | 0. 58829 | 3.7473 | 0.0077 | 0.5788 | $3.8425 \pm 0.3099$ |
| 3.7359 | $63.6 \pm 10.3$ | $1.0 \pm 0.1$ | $337.73 .42 \pm 1.9090$ | 0.5800 | 0.5853 | 3.0919 | 112 | 0.5800 | $2.6921 \pm 0.4432$ |
| 3.7379 | $87.1 \pm 11.3$ | $1.0 \pm 0.1$ | $329.6545 \pm 1.8872$ | 0.5802 | 0.58557 | 2.9765 | 0.0123 | 0.5802 | $3.7934 \pm 0.4982$ |
| 3.6500 | $183.4 \pm 54.8$ | $157.5 \pm 11.3$ | $44490.0000 \pm 20.0000$ | 0.6657 | D.5518 | 0.DET5 | 0.0013 | 0.5654 | $0.0087 \pm 0.0184$ |
| 3.7730 | $124069.9 \pm 479.6$ | $2568.8 \pm 184.2$ | $927670.0000 \pm 100.0000$ | 0.5837 | D. E 924 | 1.7986 | 0 | 0.5841 | $1.8890 \pm 0.0075$ |
| 3.6861 | 4593716.1 $\pm 2311.3$ | $533.9 \pm 38.3$ | $162800.0000 \pm 10.0000$ | 0.5727 | D. 5692 | 419.9274 | 0.0024 | 0.5727 | $415.0918 \pm 0.2104$ |

## 

| Source | Systematic uncertainty (\%) |
| :--- | :---: |
| $\theta_{\ell^{+} \ell^{-}}<179^{\circ}$ cut | 0.0 |
| $\left\|\cos \theta_{\ell}\right\|<0.81$ cut | 0.4 |
| $E_{\text {EMC }} / p$ cut | 0.3 |
| Momentum cut | 0.2 |
| $N_{\text {good }}$ and $N_{\gamma}$ cut | 0.4 |
| Fit to $M_{\ell^{+} \ell^{-}}$spectrum | 1.5 |
| MC modeling | 0.9 |
| $\pi$ identification | 1.0 |
| $\mathcal{B}\left(J / \psi \rightarrow \ell^{+} \ell^{-}\right)$ | 0.4 |
| Background subtraction $N_{\mathrm{BCK}}^{\mathrm{obs}}$ | $<0.1$ |
| Luminosity | 1.0 |
| Total | 2.4 |

## Expected-Observed Cross Section

$$
\begin{gathered}
\sigma_{J / \psi X}^{\text {expected }}(s)=\int_{0}^{\infty} d s^{\prime} G\left(s, s^{\prime}\right) \int_{0}^{x_{\text {max }}} d x F \\
\sigma^{\mathrm{dress}}(\mathrm{~s}) \text { is dressed cross sectior } \\
G\left(s, s^{\prime}\right)=\frac{1}{\sqrt{2 \pi} \sigma_{E_{\text {BEPC..I }}}} \exp \left[-\frac{\left(\sqrt{s}-\sqrt{s^{\prime}}\right)^{2}}{2 \sigma_{E_{\text {BPPC.. }}^{2}}^{2}}\right]
\end{gathered}
$$

Effective c.m. energy

Nominal
c.m. energy
$F(x, s)$ is sampling function
Kuraev \& Fadin

$$
F(x, s)=\beta x^{\beta-1} \delta^{V+S}+\delta^{H}
$$

$$
\beta=\frac{2 \alpha}{\pi}\left(\ln \frac{s}{m_{e}^{2}}-1\right)
$$

$$
\delta^{V+S}=1+\frac{3}{4} \beta+\frac{\alpha}{\pi}\left(\frac{\pi^{2}}{3}-\frac{1}{2}\right)-\frac{\beta^{2}}{24}\left(\frac{1}{3} \ln \frac{s}{m_{e}^{2}}+2 \pi^{2}-\frac{37}{4}\right)
$$

$$
\delta^{H}=\delta_{1}^{H}+\delta_{2}^{H} \quad \delta_{1}^{H}=-\beta\left(1-\frac{x}{2}\right)
$$

$$
\delta_{2}^{H}=\frac{1}{8} \beta^{2}\left[4(2-x) \ln \frac{1}{x}-\frac{1+3(1-x)^{2}}{x} \ln (1-x)-6-x\right]
$$

## Amplitude Analysis

$\sigma_{\mathrm{J} / \psi \mathrm{X}}^{\mathrm{Dress}}(S)=A_{\psi(3686)}+e^{\mathrm{i} \phi 1} A_{1}+e^{\mathrm{i} \phi 2} A_{2}+\left.\ldots\right|^{2}$
$\mathrm{A}_{\psi(3686)}$ is BW amplitude for $\psi(\mathbf{3 6 8 6}) \rightarrow \mathrm{J} / \psi \mathrm{X}$ decays
$A_{1}, A_{2}, \ldots$ are other $B W$ amplitudes for structures $S \rightarrow J / \psi$ X decays
$\phi 1, \phi 2, \ldots$ are relative phase of the amplitudes
$\chi^{2}$ fit to the observed cross sections

$$
\chi^{2}=\sum_{i=1}^{n}\left[\frac{\sigma_{\mathrm{J} / \Psi \mathrm{X}}^{o b s}(S)_{i}-\sigma_{\mathrm{J} / \Psi \mathrm{X}}^{\text {expected }}(S)_{i}}{\Delta_{\sigma_{J / \Psi \mathrm{X}}^{o s,}}(S)_{i}}\right]^{2}
$$

$\sigma_{\mathrm{J} / \mu \mathrm{X}}^{\text {expected }}(S)$ is the expected cross sections

## Fit the Observed Cross Sections

$>$ Hypotheses \#1
Assuming that there is $\psi(3686)$ only

## Our measurements :




| Parameter | Solution |
| :---: | :---: |
| $\chi^{2}$ | 128.326 |
| $n_{\text {prts }}-n_{\text {PRMT }}$ | $68-3=65$ |
| Energy Spread $[\mathrm{MeV}]$ | $1.4382 \pm 0.006 \pm 0.003$ |
|  |  |
| $M_{\psi(3686)}\left[\mathrm{MeV} / c^{2}\right]$ | $3686.10 \pm 0.02 \pm 0.01 \pm 0.00$ |
| $\Gamma_{\psi(368)}^{e}\left(\mathrm{keV} / c^{2}\right]$ | 2.34 |
| $\psi_{\psi(3686)}^{\text {tot }}[\mathrm{keV}]$ | 296 |
| $B(\psi(3686) \rightarrow \mathrm{J} / \psi \mathrm{X})[\%]$ | $66.69 \pm 0.239 \pm 1.60 \pm 1.12$ |
|  |  |

$\mathrm{E}_{\mathrm{cm}}[\mathrm{GeV}]$

## Fit the Observed Cross Sections

$>$ Hypotheses \#2
Assuming that there are $\psi(3686)$ and $\psi(3770)$ only


Our measurements :
$\mathrm{B}[\psi(3686) \rightarrow \mathrm{J} / \psi \mathrm{X}]=$ ( $\mathbf{6 4 . 2 6} \pm \mathbf{0 . 4 0} \pm 1.51 \pm \mathbf{1 . 0 8}$ )\%
$\mathrm{B}[\psi(3770) \rightarrow \mathrm{J} / \psi \mathrm{X}]=$ ( $1.21 \pm 0.83 \pm 0.03 \pm 0.00) \%$
$\phi_{1}=(-168.3 \pm 51.0 \pm 0.0 \pm 0.3)^{\circ}$
Summing over the known Bfs for exclusive modes given in PDG yields

$$
\mathrm{B}[\psi(3770) \rightarrow \mathrm{J} / \psi \mathrm{X}]=(1.4 \pm 0.1) \%
$$

## Fit the Observed Cross Sections

> Hypotheses \#3
Assuming that there are $\psi(3686), \mathrm{S}_{1}(3760)$ and $\mathrm{S}_{2}(3780)$


| Parameter | Solution 1 |
| :---: | :---: |
|  |  |
| $\mathrm{M}_{\psi(\text { (3686) }}\left[\mathrm{MeV} / \mathrm{c}^{2}\right]$ |  |
|  | $\begin{gathered} \pm 0.34 \\ 296 \\ 20.88 \\ 62.88 .84 \pm 1.51 \\ \pm 0.15 \end{gathered}$ |
| $\mathrm{M}_{s(3760)}\left[\mathrm{MeV} / \mathrm{c}^{2}\right]$ | $\begin{array}{r} 3763.5 \pm 5.5 \pm 0.1 \\ \pm 0.4 \end{array}$ |
|  | $\begin{gathered} \begin{array}{c}  \pm 0.4 \\ 0.186 \\ 12.8 \pm 12.3 \pm 0.1 \end{array} \end{gathered}$ |
| $B[s(3760) \rightarrow \mathrm{J} / \psi \mathrm{X}][\%]$ <br> $\phi_{1}$ [degree] | $\begin{gathered} \pm .96 \pm \begin{array}{l}  \pm 0.4 \\ 4.19 \\ 23.17 \\ 23.9 \pm 61.30 \\ \hline 0.3 \pm 1.2 \end{array} \end{gathered}$ |
|  | $\pm 4.5$ |
| $\mathrm{M}_{s(3780)}\left[\mathrm{MeV} / \mathrm{c}^{2}\right]$ | ${ }^{3780.7} \pm 10.9 \pm 0.1$ |
|  | $\begin{gathered} \pm .0 .4 \\ \text { 0.243 } \\ 27.7 \pm 12.7 \pm 0.1 \end{gathered}$ |
| $\left.{ }_{B[s(3780)} \rightarrow \mathrm{J} / \psi \mathrm{X}\right][\%]$ | ( |
| $\phi_{2}$ [degree] |  |

The signal significance of the Di-structure(s) decay into $\mathrm{J} / \psi \mathrm{X}$ is more than $4 \sigma$ [from analyzing the observed cross sections]

## Fit the Observed Cross Sections



## Four Solutions

| Parameter | Solution1 | Solution2 | Solution3 | Solution4 |
| :---: | :---: | :---: | :---: | :---: |
| $\chi^{2}$ $n_{\text {pnts }}-n_{\text {PRMT }}$ Energy Spread $[\mathrm{MeV}]$ | $\begin{gathered} \hline 66.497 \\ 68-11=57 \\ 1.352 \pm 0.017 \pm 0.000 \\ \pm 0.003 \end{gathered}$ | $\begin{gathered} \hline 76.497 \\ 68-11=57 \\ 1.351 \pm 0.017 \pm 0.006 \\ \pm 0.003 \end{gathered}$ | $\begin{gathered} 76.641 \\ 68-11=57 \\ 1.351 \pm 0.020 \pm 0.006 \\ \pm 0.003 \end{gathered}$ | $\begin{gathered} \hline 76.600 \\ 68-11=57 \\ 1.350 \pm 0.019 \pm 0.006 \\ \pm 0.003 \end{gathered}$ |
| $\begin{gathered} \mathrm{M}_{\psi(3686)}\left[\mathrm{MeV} / \mathrm{c}^{2}\right] \\ \Gamma_{\psi(3686)}^{e e}\left[\mathrm{keV} / \mathrm{c}^{2}\right] \\ \psi_{\psi(3686)}^{\text {tot }}[\mathrm{keV}] \end{gathered}$ | $\begin{gathered} 3686.00 \pm 0.03 \pm 0.00 \\ \pm 0.00 \\ 2.34 \\ 296 \end{gathered}$ | $\begin{gathered} 3686.00 \pm 0.03 \pm 0.00 \\ \pm 0.00 \\ 2.34 \\ 296 \end{gathered}$ | $\begin{gathered} 3686.00 \pm 0.03 \pm 0.00 \\ \pm 0.00 \\ 2.34 \\ 296 \end{gathered}$ | $\begin{gathered} 3686.0 \pm 0.01 \pm 0.00 \\ \pm 0.00 \\ 2.34 \\ 296 \end{gathered}$ |
| $B(\psi(3686) \rightarrow \mathrm{J} / \psi \mathrm{X})[\%]$ | $\begin{gathered} 62.88 \pm 0.84 \pm 1.51 \\ \pm 0.15 \end{gathered}$ | $\begin{gathered} 63.06 \pm 0.70 \pm 1.51 \\ \pm 0.15 \end{gathered}$ | $\begin{gathered} 62.76 \pm 0.89 \pm 1.51 \\ \pm 0.15 \end{gathered}$ | $\begin{aligned} 63.07 & \pm 0.72 \pm 1.51 \\ & \pm 0.15 \end{aligned}$ |
| $\mathrm{M}_{s(3760)}[\mathrm{MeV}$ | $\begin{gathered} 3763.5 \pm 5.5 \pm 0.1 \\ \pm 0.4 \\ 0.186 \end{gathered}$ | $\begin{aligned} & 3763.5 \pm 5.7 \pm 0.1 \\ & \pm 0.4 \\ & 0.186 \end{aligned}$ | $\begin{aligned} & 3767.5 \pm 6.0 \pm 0.1 \\ & \pm 0.4 \\ & 0.186 \end{aligned}$ | $\begin{aligned} 3766.1 & \pm 13.6 \pm 0.1 \\ & \pm 0.4 \\ & 0.186 \end{aligned}$ |
| $\begin{gathered} \Gamma_{s(3760)}^{e e}\left[\begin{array}{c} \left.\mathrm{keV} / \mathrm{c}^{2}\right] \\ \Gamma_{s(3760)}^{\text {tot }}\left[\begin{array}{l} \text { ot } \end{array}[\mathrm{MeV}]\right. \end{array} .\right. \end{gathered}$ | $\begin{gathered} 0.186 \\ 12.8 \pm 12.3 \pm 0.1 \end{gathered}$ | $\begin{gathered} 0.186 \\ 12.8 \pm 12.5 \pm 0.1 \end{gathered}$ | $\begin{gathered} 0.186 \\ 20.1 \pm 8.4 \pm 0.1 \end{gathered}$ | $\begin{gathered} 0.186 \\ 18.3 \pm 11.5 \pm 0.1 \end{gathered}$ |
| $\begin{gathered} B[s(3760) \rightarrow \mathrm{J} / \psi \mathrm{X}][\%] \\ \phi_{1}[\text { degree }] \end{gathered}$ | $\begin{aligned} & \pm 0.4 \\ 4.96 \pm & 10.19 \pm 0.17 \\ & \pm 0.30 \\ 233.9 & \pm 61.3 \pm 1.2 \\ & \pm 4.5 \end{aligned}$ | $\begin{aligned} & \pm 0.4 \\ 5.52 \pm & 12.62 \pm 0.17 \\ & \pm 0.30 \\ -88.4 & \pm 103.1 \pm 1.2 \\ & \pm 1.7 \end{aligned}$ | $\begin{aligned} & \pm 0.4 \\ 38.94 & \pm 57.44 \pm 0.17 \\ & \pm 2.40 \\ -105.3 .1 & \pm 139.0 \pm 1.2 \\ & \pm 2.0 \end{aligned}$ | $\begin{gathered} \pm 0.4 \\ 21.48 \pm 51.58 \pm 0.17 \\ \quad \pm 1.34 \\ -52.2 \pm 206.3 \pm 1.2 \\ \pm 1.0 \end{gathered}$ |
| $\begin{gathered} \mathrm{M}_{s(3780)}\left[\mathrm{MeV} / c^{2}\right] \\ \Gamma_{s(3780)}^{e e}\left[\mathrm{keV} / c^{2}\right] \end{gathered}$ | $\begin{aligned} 3780.7 & \pm 10.9 \pm 0.1 \\ & \pm 0.4 \\ & 0.243 \end{aligned}$ | $\begin{aligned} 3780.7 & \pm 11.1 \pm 0.1 \\ & \pm 0.4 \\ & 0.243 \end{aligned}$ | $\begin{aligned} & 3773.7 \pm 5.9 \pm 0.1 \\ & \pm 0.4 \\ & 0.243 \end{aligned}$ | $\begin{aligned} & 3775.6 \pm 17.1 \pm 0.1 \\ & \pm 0.4 \\ & 0.243 \end{aligned}$ |
| $\Gamma_{s(3780)}^{\text {tot }}[\mathrm{MeV}]$ | $\begin{gathered} 27.7 \pm 12.7 \pm 0.1 \\ \pm 0.2 \end{gathered}$ | $\begin{gathered} 27.7 \pm 12.8 \pm 0.1 \\ \pm 0.2 \end{gathered}$ | $\begin{gathered} 29.1 \pm 19.1 \pm 0.1 \\ \pm 0.2 \end{gathered}$ | $\begin{gathered} 29.1 \pm 25.3 \pm 0.1 \\ \pm 0.2 \end{gathered}$ |
| $\begin{gathered} B[s(3780) \rightarrow \mathrm{J} / \psi \mathrm{X}][\%] \\ \phi_{2}[\text { degree }] \end{gathered}$ | $\begin{aligned} & \pm 0.2 \\ & 7.77 \pm 10.40 \pm 0.41 \\ & \pm 0.20 \\ & 128.7 \pm 108.7 \pm 0.1 \\ & \pm 6.4 \\ & \hline \end{aligned}$ | $\begin{gathered} \pm 0.2 \\ 9.50 \pm 25.80 \pm 0.41 \\ \quad \pm 0.24 \\ 173.0 \pm 56.8 \pm 0.1 \\ \\ \pm 8.7 \\ \hline \end{gathered}$ | $\begin{gathered} \pm 0.2 \\ 41.78 \pm 33.50 \pm 0.41 \\ \pm 1.07 \\ 99.3 \pm 94.3 \pm 0.1 \\ \pm 5.0 \\ \hline \end{gathered}$ | $\begin{gathered} \pm 0.2 \\ 27.78 \pm 27.19 \pm 0.41 \\ \pm 0.71 \\ 172.0 \\ \pm 70.3 \pm 0.1 \\ \\ \pm 8.6 \end{gathered}$ |

## Comparison with BES-II Result

BES-III $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi$ X
$\mathrm{M}_{1}=3763.5 \pm 5.5 \pm 0.4 \mathrm{MeV}$
$\Gamma_{1}=12.8 \pm 12.3 \pm 0.4 \mathrm{MeV}$
$M_{2}=3780.7 \pm 10.9 \pm 4.7 \mathrm{MeV}$
$\Gamma_{2}=27.7 \pm 12.7 \pm 0.2 \mathrm{MeV}$


BES-II $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow$ hadrons
$M_{1}=3762.6 \pm 11.8 \pm 0.5 \mathrm{MeV}$
$\Gamma_{1}=49.9 \pm 32.1 \pm 0.1 \mathrm{MeV}$
$M_{2}=3781.0 \pm 1.3 \pm 0.5 \mathrm{MeV}$
$\Gamma_{2}=19.3 \pm 3.1 \pm 0.1 \mathrm{MeV}$


This $\mathrm{J} / \psi \mathrm{X}$ result confirms (at $\sim 4.5 \sigma$ ) the BES-II observation of Di-Structure $\mathrm{Rs}(3770)$ in the range from 3.71 to 3.87 GeV .

## Conclusion

$>$ We measured the observed cross sections for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi \mathrm{X}$ in range from 3.645 to 3.87 GeV .
> To well describe the line-shape of these observed cross sections, needing one more BW amplitude additional $\psi(3770)$.
> We observed the Di-Structures "S(3760)+S(3780)" in J/ $\mathbf{~ X ~}$ ( $\mathrm{X}=$ anything) final states, and the parameters of the Di -structure are consistent within errors with those measured at BES-II.

$$
\begin{aligned}
& \text { BES-III } \mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{J} / \psi \mathbf{X} \\
& \mathrm{M}_{1}=3763.5 \pm 5.5 \pm 0.4 \mathrm{MeV} \\
& \Gamma_{1}=12.8 \pm \mathbf{1 2 . 3} \pm 0.4 \mathrm{MeV} \\
& \mathrm{M}_{2}=3780.7 \pm 10.9 \pm 4.7 \mathrm{MeV} \\
& \Gamma_{2}=27.7 \pm 12.7 \pm 0.2 \mathrm{MeV} \\
& \text { BES-II }{ }^{+} \mathrm{e}^{-} \rightarrow \text { hadrons } \\
& \mathrm{M}_{1}=3762.6 \pm 11.8 \pm 0.5 \mathrm{MeV} \\
& \Gamma_{1}=49.9 \pm 32.1 \pm 0.1 \mathrm{MeV} \\
& \mathrm{M}_{2}=3781.0 \pm 1.3 \pm \mathbf{0 . 5} \mathrm{MeV} \\
& \Gamma_{2}=19.3 \pm 3.1 \pm 0.1 \mathrm{MeV}
\end{aligned}
$$

## Thank You!

## Comparison of Data and Monte Carlo






## NJStempatic Jincertainty

## Selection of $\ell^{+} \ell^{-}$

## Sources

1. Uncertainty in angle cut $\left(\theta_{\ell^{+} \ell^{-}}<179^{\circ}\right)$ for the leptons
2. Uncertainty in polar angle cut $\left(\left|\cos \theta_{\ell}\right|<0.81\right)$ for the charged tracks
3. Uncertainty in lepton PID

$$
\begin{aligned}
& e^{ \pm} E_{\mathrm{EMC}} / p>0.7 \\
& \mu^{ \pm} 0.05<E_{\mathrm{EMC}} / p<0.35
\end{aligned}
$$

4. Uncertainty in momentum cut ( $1.0<p<0.47 \times E_{\mathrm{cm}}$ )

Mehtod

- Compare the corresponding efficiencies for data and MC events, which are measured using the lepton samples selected from the $\psi(3686) \rightarrow \pi^{+} \pi^{-} J / \psi, J / \psi \rightarrow$ $\ell^{+} \ell^{-}$process


## Systematic Uncertainty

$$
\theta_{\ell^{+} \ell^{-}}<179^{\circ} \mathrm{Cut}
$$



|  | $N_{\text {tot }}$ | $N_{\text {cut }}$ | $R \equiv N_{\text {cut }} / N_{\text {tot }}$ |
| :--- | :---: | :---: | :---: |
| data | 1456805 | 1437505 | $0.9868 \pm 0.0001$ |
| MC | 1322668 | 1305311 | $0.9869 \pm 0.0001$ |
| $R_{\text {data }} / R_{\text {MC }}-1$ | $(-0.01 \pm 0.01) \%$ |  |  |

## Systematic Uncertainty

$\left|\cos \theta_{\ell}\right|<0.81$ Cut


|  | $N_{\text {tot }}$ | $N_{\text {cut }}$ | $R \equiv N_{\text {cut }} / N_{\text {tot }}$ |
| :--- | :---: | :---: | :---: |
| data | 1456805 | 1259484 | $0.8646 \pm 0.0003$ |
| MC | 1322668 | 1139355 | $0.8614 \pm 0.0003$ |
| $R_{\text {data }} / R_{\text {MC }}-1$ |  | $(0.37 \pm 0.05) \%$ |  |

## NJStemeticerning

$$
e^{ \pm} \mathrm{PID}
$$



|  | $N_{\text {tot }}$ | $N_{\text {cut }}$ | $R \equiv N_{\text {cut }} / N_{\text {tot }}$ |
| :--- | :---: | :---: | :---: |
| data | 803718 | 786977 | $0.9792 \pm 0.0002$ |
| MC | 783994 | 770110 | $0.9823 \pm 0.0001$ |
| $R_{\text {data }} / R_{\mathrm{MC}}-1$ | $(-0.32 \pm 0.02) \%$ |  |  |

## Systematic Uncertainty

## $\mu^{ \pm}$PID



|  | $N_{\text {tot }}$ | $N_{\text {cut }}$ | $R \equiv N_{\text {cut }} / N_{\text {tot }}$ |
| :--- | :---: | :---: | :---: |
| data | 653087 | 644969 | $0.9876 \pm 0.0001$ |
| MC | 538674 | 532596 | $0.9887 \pm 0.0001$ |
| $R_{\text {data }} / R_{\text {MC }}-1$ | $(-0.12 \pm 0.02) \%$ |  |  |

## Systematic Uncertainty

## Momentum Cut



|  | $N_{\text {tot }}$ | $N_{\text {cut }}$ | $R \equiv N_{\text {cut }} / N_{\text {tot }}$ |
| :--- | :---: | :---: | :---: |
| data | 1456805 | 1435805 | $0.9856 \pm 0.0001$ |
| MC | 1322668 | 1306778 | $0.9880 \pm 0.0001$ |
| $R_{\text {data }} / R_{\text {MC }}-1$ |  | $(-0.24 \pm 0.01) \%$ |  |

## Systematic Uncertainty

## $N_{\text {good }}$ and $N_{\gamma}$ Cut

- After subtracting QED and $\gamma_{\text {ISR }} J / \psi$ backgrounds



|  | $N_{\text {tot }}$ | $N_{\text {cut }}$ | $R \equiv N_{\text {cut }} / N_{\text {tot }}$ |
| :--- | :---: | :---: | :---: |
| data | 4644114 | 4454535 | $0.9592 \pm 0.0001$ |
| MC | 57820 | 55682 | $0.9630 \pm 0.0008$ |
| $R_{\text {data }} / R_{\mathrm{MC}}-1$ |  | $(-0.40 \pm 0.08) \%$ |  |

## NJEtenngitc Uncentainty

## Fit to $M_{\ell+\ell-}$ Spectrum

- Nominal fit: $N_{\text {obs }}=124069.9 \pm 479.6$ at $E_{\mathrm{cm}}=3.773 \mathrm{GeV}$

1. Signal shape

- Crystal Ball function - 0.53\%

2. Background shape

- $4^{\text {th }}$ order polynomial $-0.63 \%$

3. Fit region - $0.88 \%$
4. Bin width $-0.93 \%$

- Total systematic uncertainty from fit to mass spectrum:
$\sqrt{0.53^{2}+0.63^{2}+0.88^{2}+0.93^{2}} \%=1.52 \%$


## NJStampatic Uncentainty

## Efficiency

- Vary the normalization of several of the largest components ( $J / \psi \pi^{+} \pi^{-}, J / \psi \pi^{0} \pi^{0}$ ) based on branching fraction uncertainties

- The maximum changes (0.86\%) is taken as systematic uncertainty


## NJEtennatic Jincertainty

## Quoted Systematic Uncertainties

- $\pi$ PID
- 1.0\% per pion
- Weighted by the distribution of charged track multiplicity at $E_{\mathrm{cm}}=3.686 \mathrm{GeV}$

| $N_{\text {good }}$ | $N_{\text {obs }}$ | $\Delta(\%)$ |
| :---: | :---: | :---: |
| 2 | 1989790 | 0.0 |
| 3 | 763368 | 1.0 |
| 4 | 1980909 | 2.0 |
| Average | 3734067 | 1.0 |

- Branching Fraction
- $\mathcal{B}\left(J / \psi \rightarrow \ell^{+} \ell^{-}\right)=(11.932 \pm 0.046) \%(P D G 2016)$
- 0.39\%
- Luminosity
- 1.0\% (Chin. Phys. C 37, 123001 (2013))


## Invariant mass spectra at each energy







Everis( (0.01 Gol)










## Invariant mass spectra at each energy













至







## Invariant mass spectra at each energy








## Invariant mass spectra at each energy





彩












为


(ip) of hand


## Invariant mass spectra at each energy






