

# Search for the $h_c(2P)$

Using

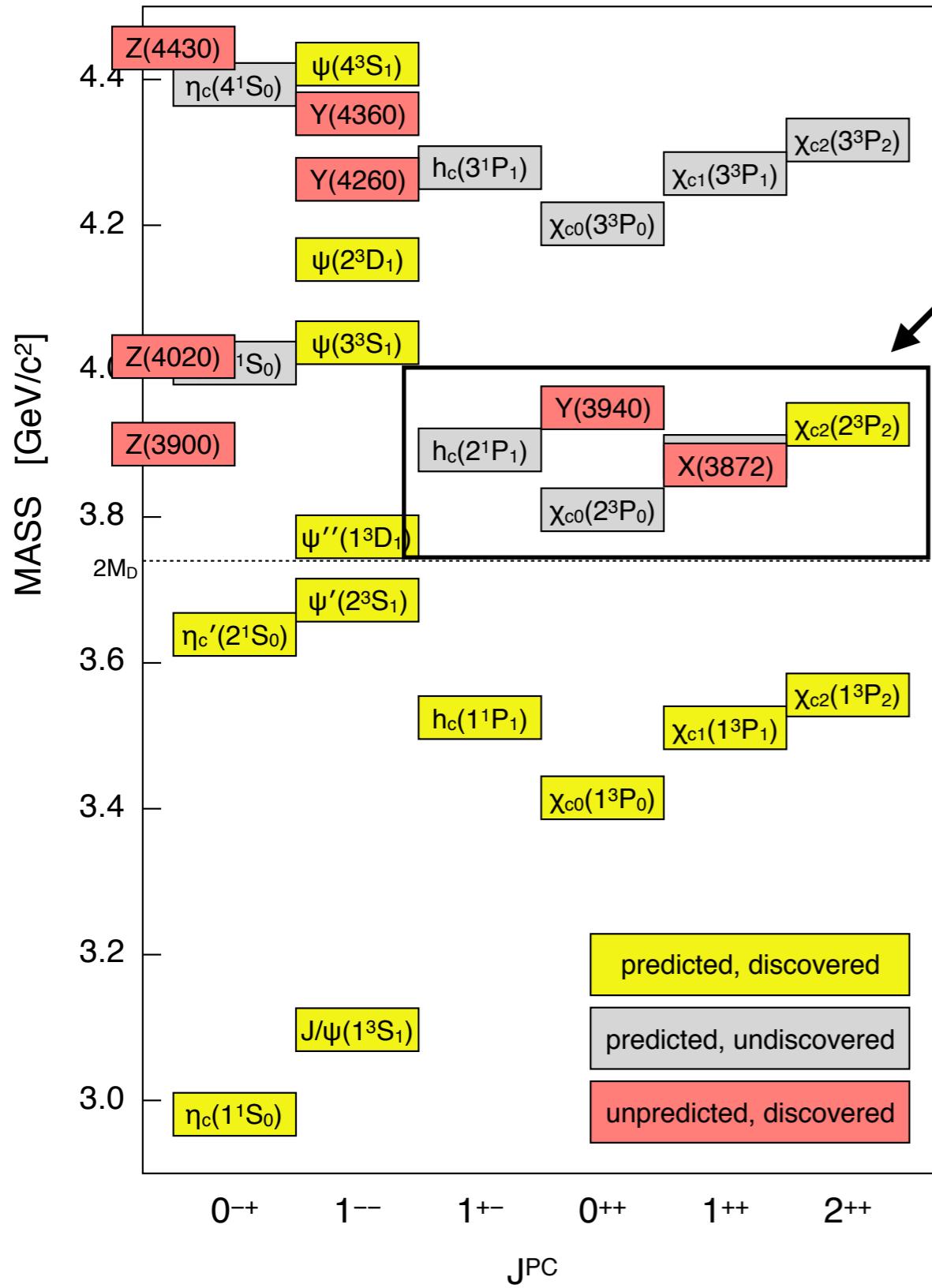
$$e^+ e^- \rightarrow \pi^+ \pi^- h_c(2P)$$

with

$$h_c(2P) \rightarrow D^+ D^{*-}$$

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Indiana University  
June 13, 2017*

# Overview of the $h_c(2P)$



The region around 3.9 GeV is unclear...  
 $X(3872)$ ,  $X(3915)$ ,  $Y(3940)$ ,  $Z(3930)$ ,  $X(3940)$   
 Which are conventional and which aren't?

Finding the  $h_c(2P)$  could bring clarification.

Cross sections for  $\pi^+\pi^-\psi(1S,2S)$  and  $\pi^+\pi^-h_c(1P)$  are on the order of 50 – 100 pb; we probably expect the same for  $\pi^+\pi^-h_c(2P)$ .

Furthermore, mass and decay width predictions for the  $h_c(2P)$  exist:

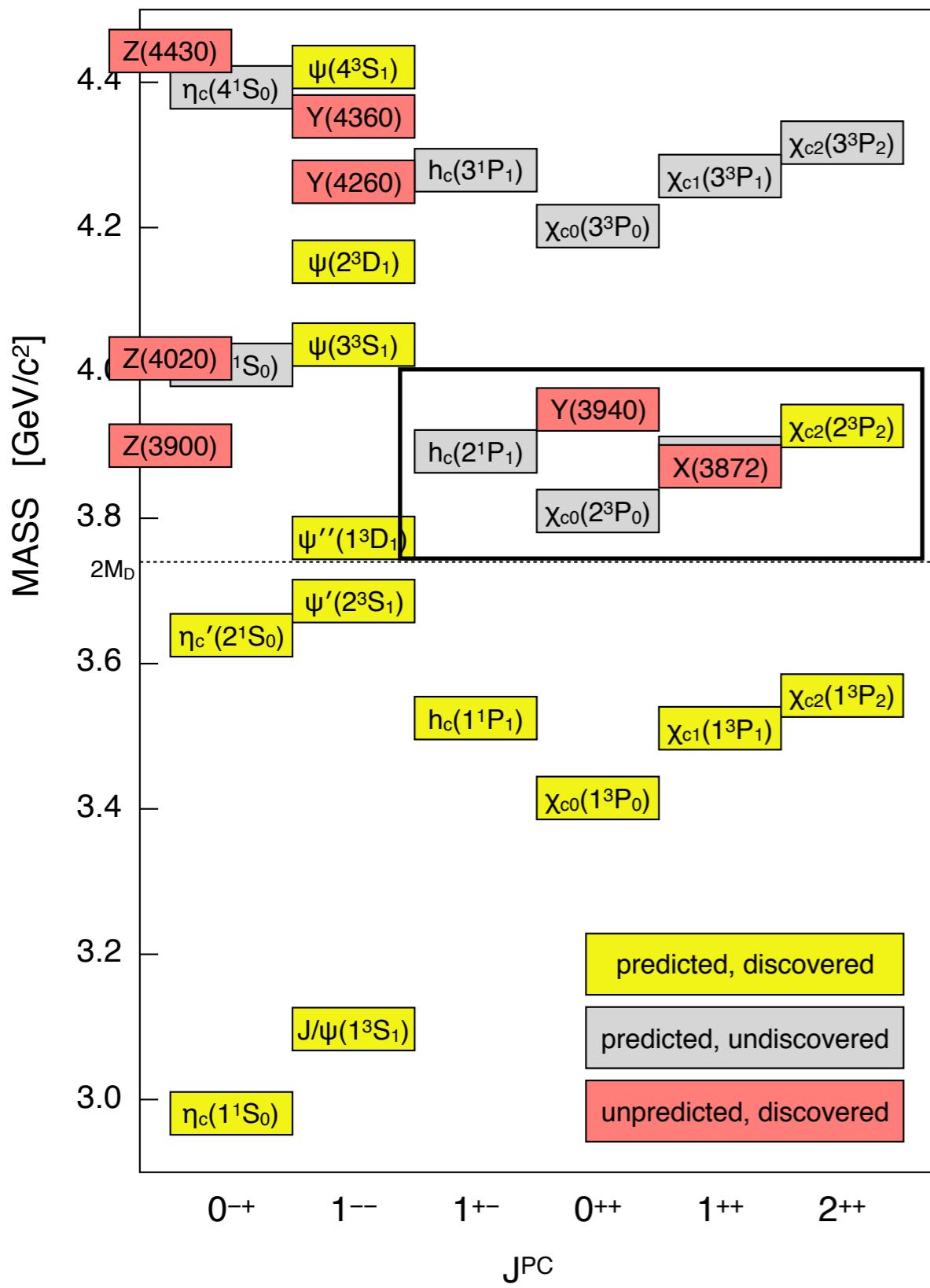
PHYSICAL REVIEW D **72**, 054026 (2005)

## Higher charmonia

T. Barnes,<sup>1,\*</sup> S. Godfrey,<sup>2,†</sup> and E. S. Swanson<sup>3,‡</sup>

# Overview of the $h_c(2P)$

PHYSICAL REVIEW D 72, 054026 (2005)



## Higher charmonia

T. Barnes,<sup>1,\*</sup> S. Godfrey,<sup>2,†</sup> and E. S. Swanson<sup>3,‡</sup>

## 2P Mass Predictions:

Multiplet	State	Expt.	Input (NR)	Theor. NR	Theor. GI
2P	$\chi_2(2^3P_2)$			3972	3979
	$\chi_1(2^3P_1)$			3925	3953
	$\chi_0(2^3P_0)$			3852	3916
	$h_c(2^1P_1)$			3934	3956

## 2P DD Decay Width Predictions:

Meson	State	Mode	$\Gamma_{\text{thy}}$ (MeV)	Amps. ( GeV <sup>-1/2</sup> )
$\chi_2(3972)$	$2^3P_2$	DD	42	${}^1D_2 = +0.0992$
		DD*	37	${}^3D_2 = -0.1172$
		$D_s D_s$	0.7	${}^1D_2 = +0.0202$
		<i>total</i>	80	
$\chi_1(3925)$	$2^3P_1$	DD*	165	${}^3S_1 = +0.2883$
				${}^3D_1 = -0.0525$
$\chi_0(3852)$	$2^3P_0$	DD	30	${}^1S_0 = +0.1025$
$h_c(3934)$	$2^1P_1$	DD*	87	${}^3S_1 = -0.1847$
				${}^3D_1 = -0.0851$

# Strategy

- I. Measure the  $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$  cross section.
- II. Search for  $\pi^+\pi^-h_c(2P)$  with  $h_c(2P) \rightarrow D^+D^{*-}$ .
- III. Compare to  $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$ .

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$ Cross Section

Reconstruct  $\pi^+\pi^-D^+$  with  $D^+ \rightarrow K^-\pi^+\pi^+$  (*and charge conjugate, always implied*).

Isolate the reaction by finding the  $D^+$  in  $K^-\pi^+\pi^+$  and looking for the  $D^{*-}$  in the  $(K^-\pi^+\pi^+)\pi^+\pi^-$  missing mass. Use all combinations.

Use standard track and angle requirements for all tracks.

Only use PID for the kaon:  $P(K) > P(\pi)$  and  $P(K) > 10^{-3}$ .

Use three classes of data:

**SIGNAL MC:** Includes  $\pi^+\pi^-D^+D^{*-}$  and its charge conjugate.

*The charge-conjugate channel is an irreducible background, since  $D^{*+} \rightarrow \pi^0 D^+$ .*

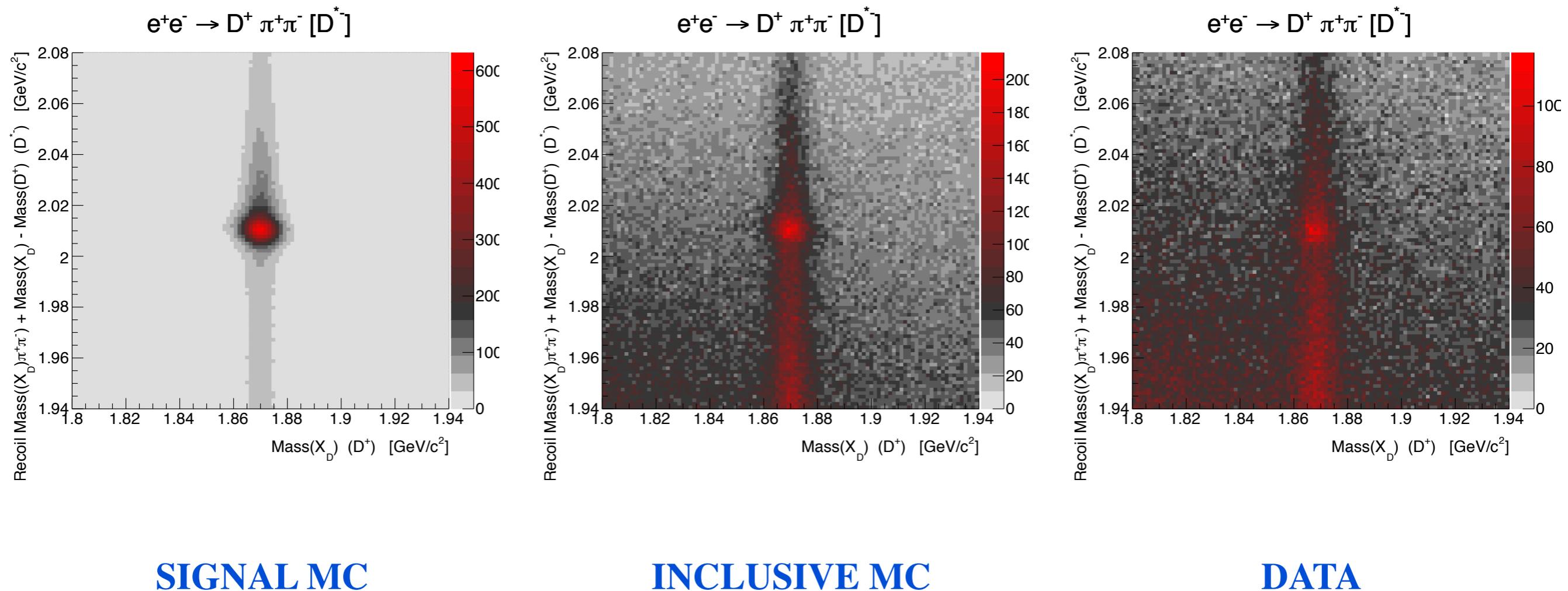
**INCLUSIVE MC:** (1) Includes full samples of inclusive DDbar MC at 4.42 and 4.60 GeV (*including important channels of the form  $\pi D^* D^*$* ).

(2) We also add 200 pb each for all charge combinations of the form  $\pi\pi D D^*$  (*which includes signal as well as potential peaking backgrounds*).

**DATA:** Currently use all of the 2014 data: 4420, 4470, 4530, 4575, 4600 MeV (*but should eventually also include the 4360 data from 2013*).

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$ Cross Section

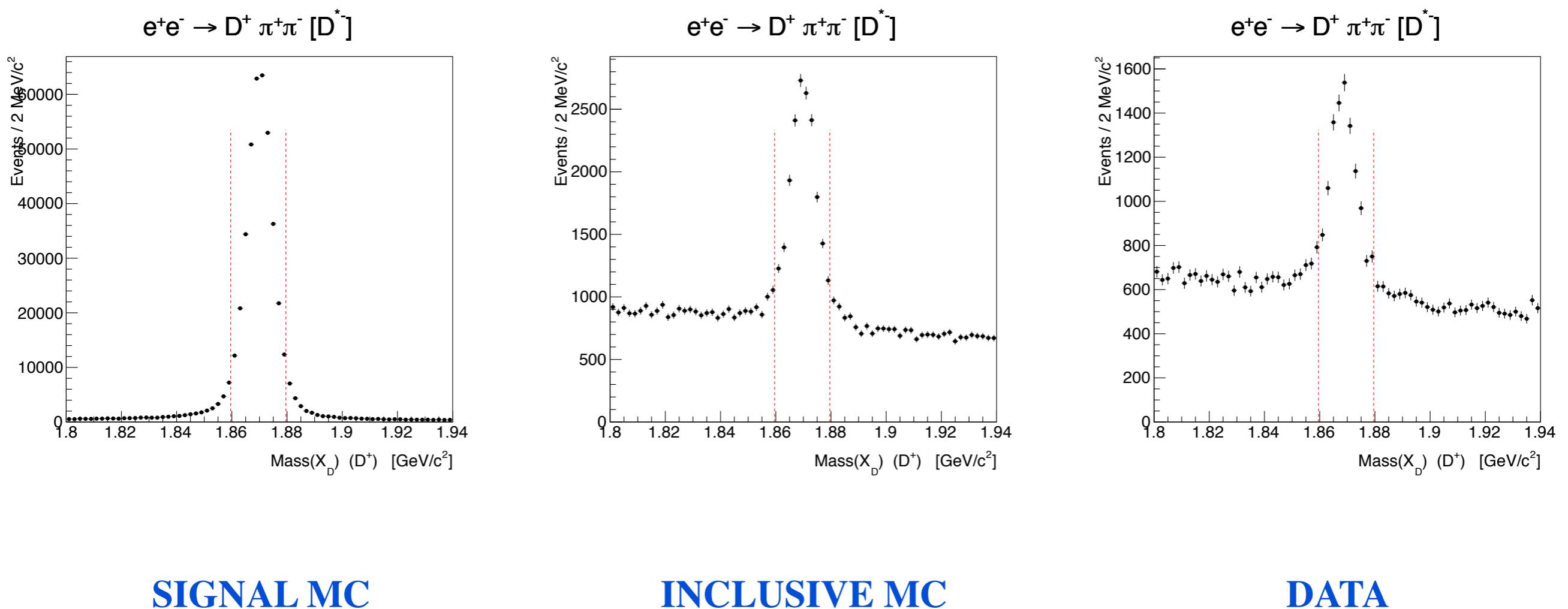
- \* Find the  $D^+$  using the  $D^+ \rightarrow K^-\pi^+\pi^+$  mass (*x-axis*).
- \* Find the  $D^{*-}$  using the  $D^+\pi^+\pi^-$  recoil mass [ $RM((K^-\pi^+\pi^+)\pi^+\pi^-) + M(K^-\pi^+\pi^+) - M(D^+)$ ] (*y-axis*).



(Using all 2014 data: 4420, 4470, 4530, 4575, 4600.)

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$ Cross Section

\* Select the  $D^+$  by requiring  $\text{Mass}(K^-\pi^+\pi^+)$  be within 10 MeV of the  $D^+$  mass.



**SIGNAL MC**

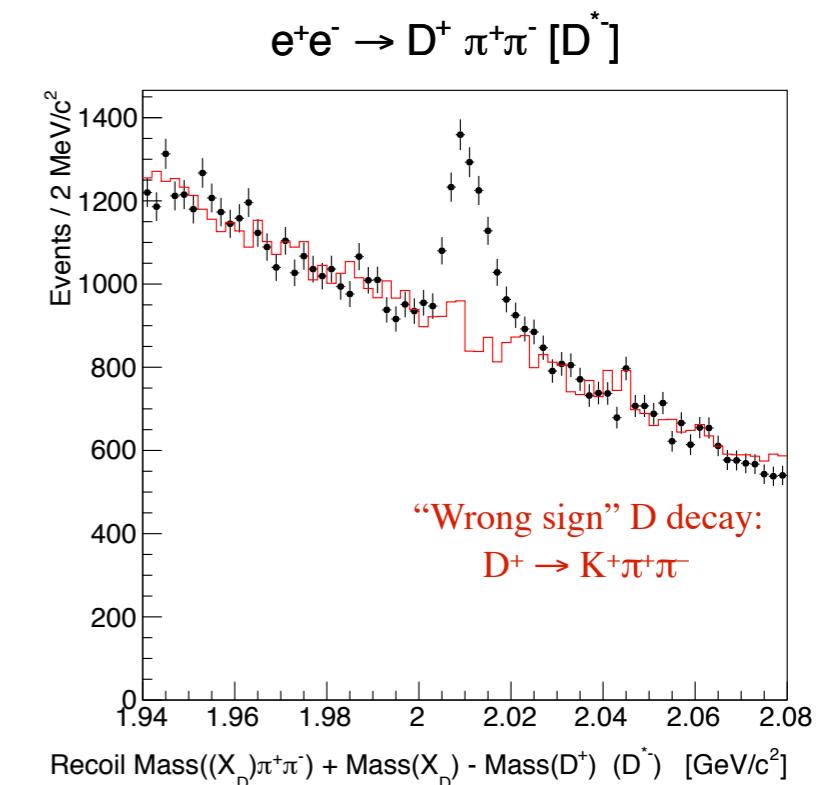
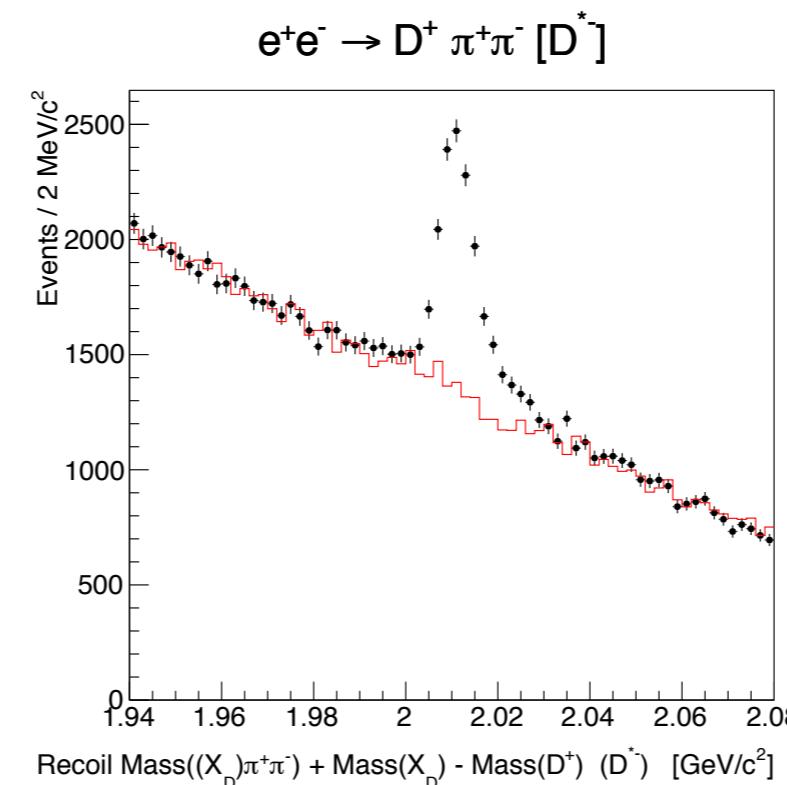
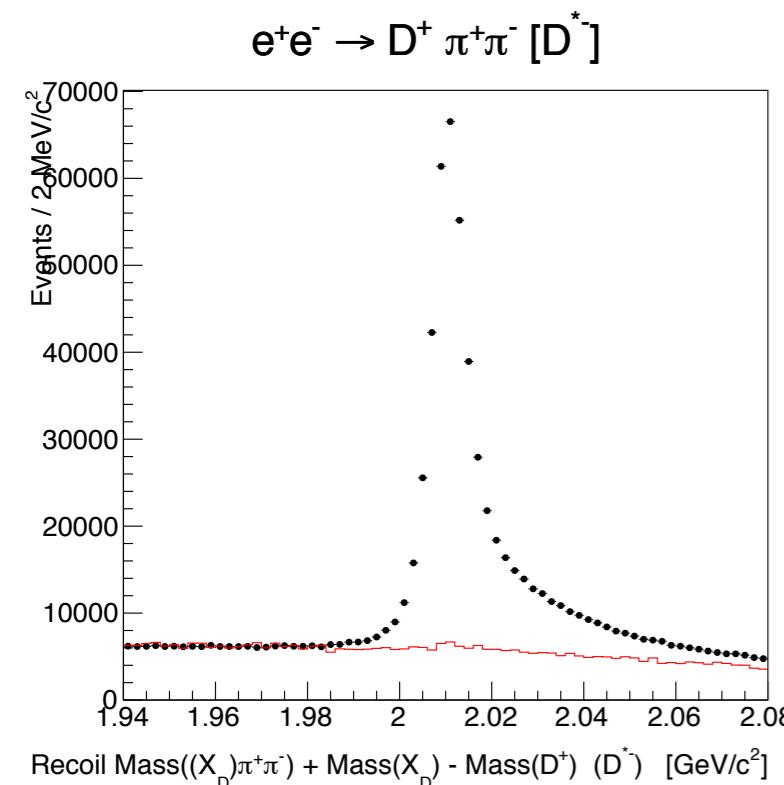
**INCLUSIVE MC**

**DATA**

(Using all 2014 data: 4420, 4470, 4530, 4575, 4600.)

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$ Cross Section

- \* After selecting  $D^+$  candidates, there is a clear peak for the  $D^{*-}$  in the  $D^+\pi^+\pi^-$  recoil mass.
- \* The “wrong-sign”  $D^+$  decay to  $K^+\pi^+\pi^-$  describes the background shape well.



**SIGNAL MC**

**INCLUSIVE MC**

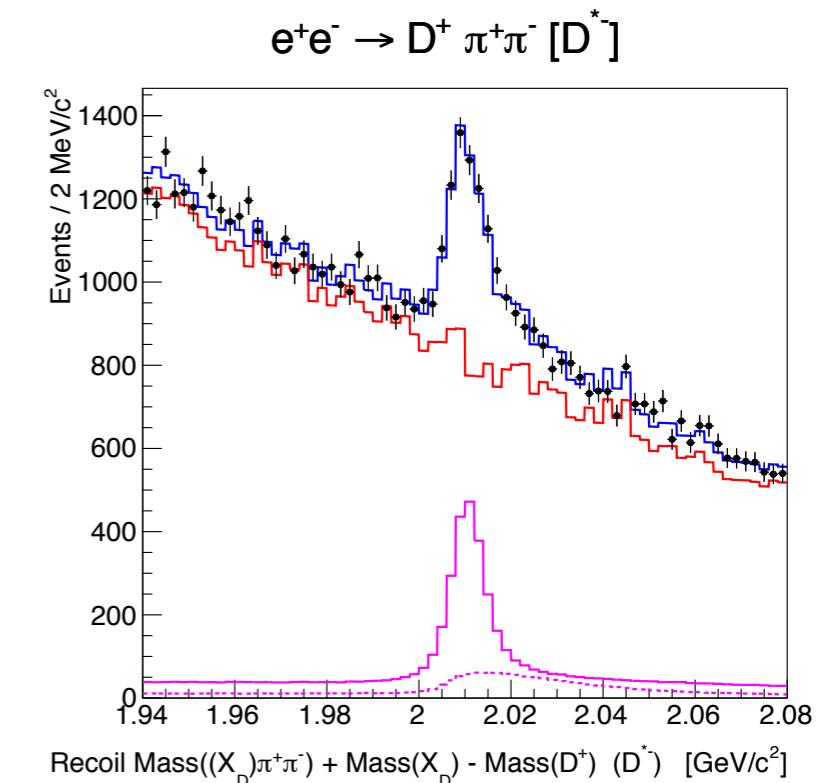
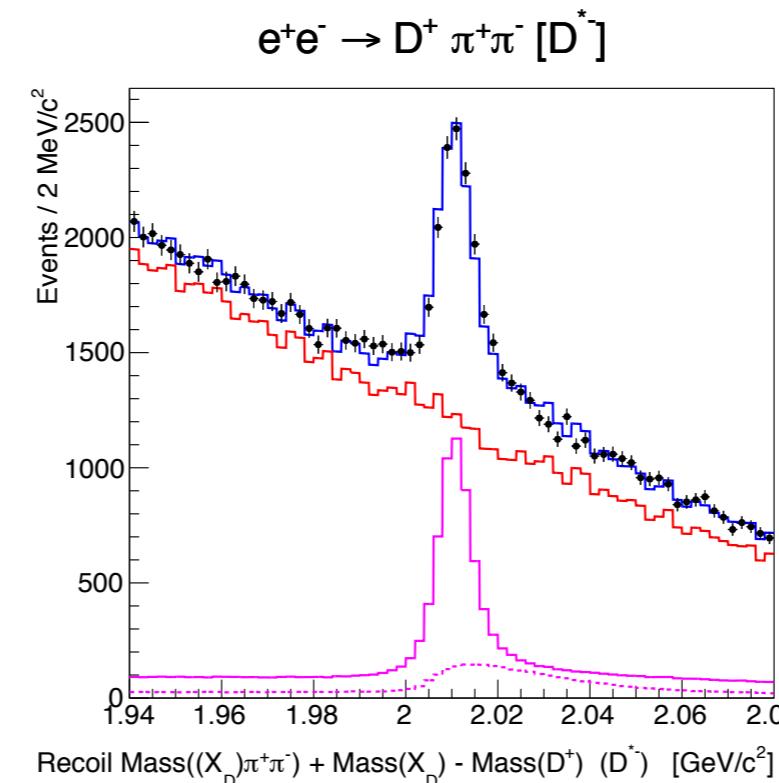
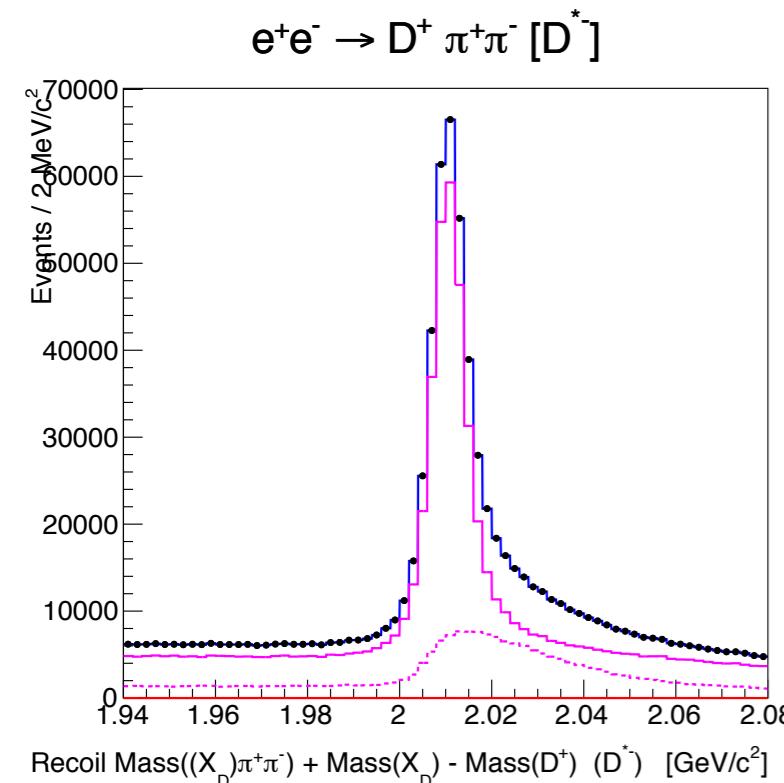
**DATA**

*(Using all 2014 data: 4420, 4470, 4530, 4575, 4600.)*

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$ Cross Section

Fits (*current technique*), three free parameters:

- \* Take the **signal shape** from signal MC (*there are two components – the charge conjugate is an irreducible background, the ratio is fixed*).
- \* Take the **background shape** from the wrong sign D decay and multiply by a 1st order polynomial (*maybe not necessary*).



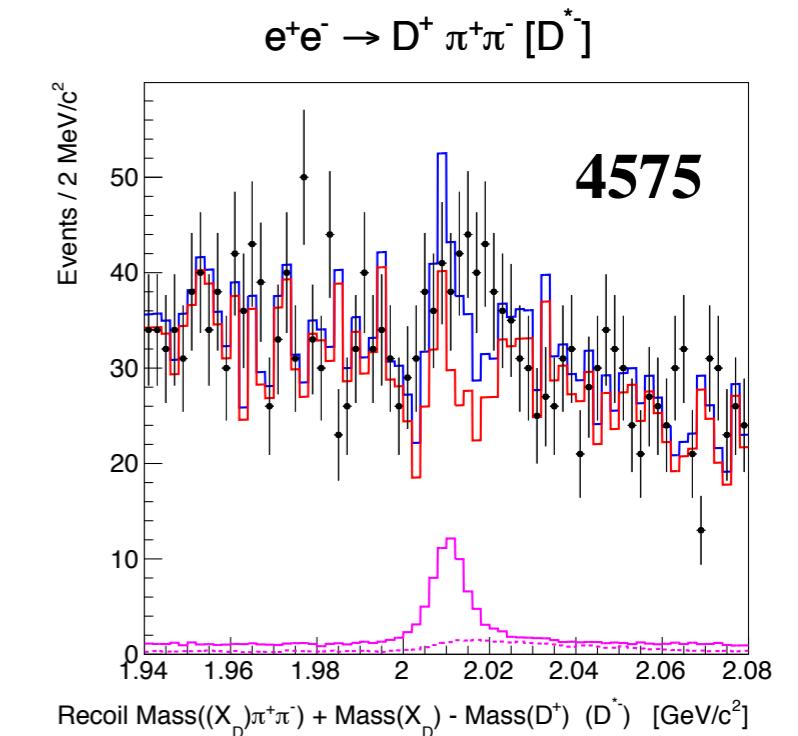
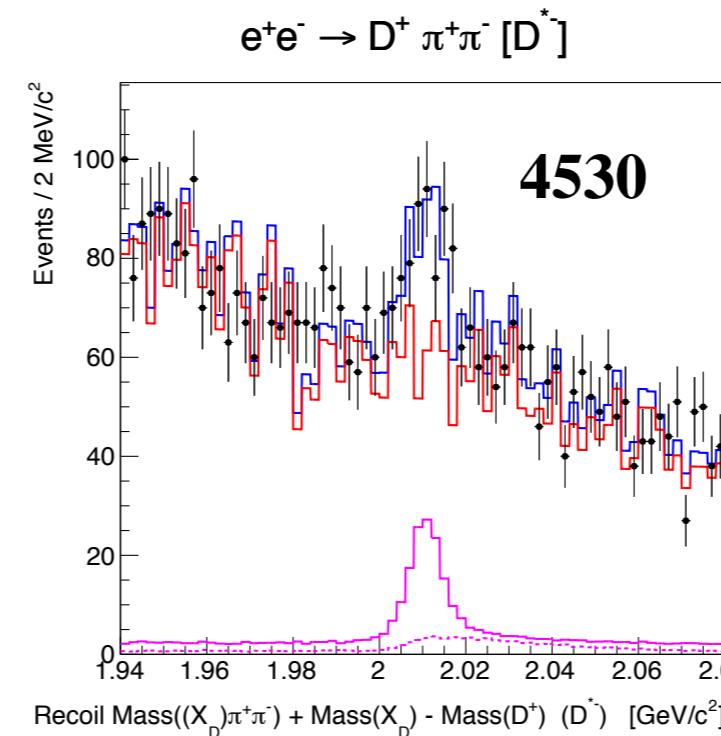
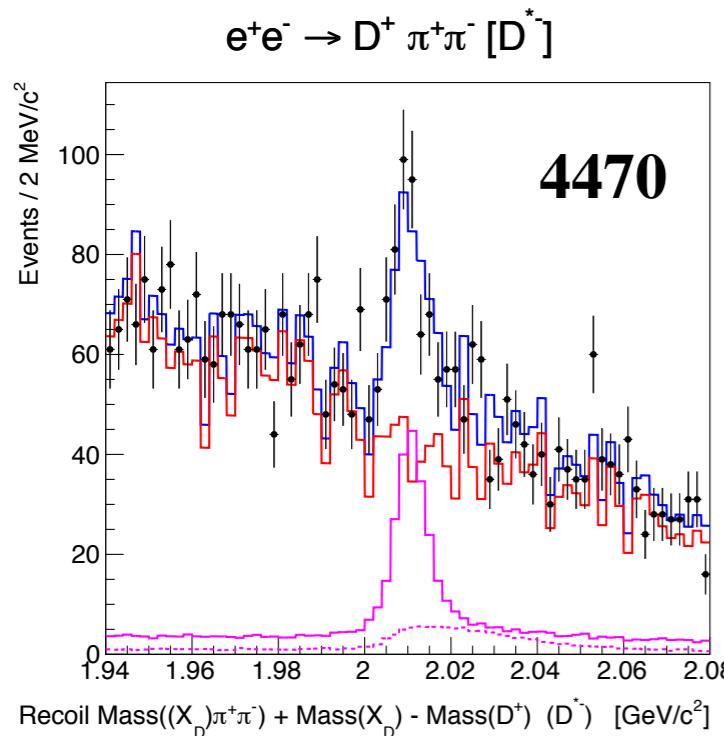
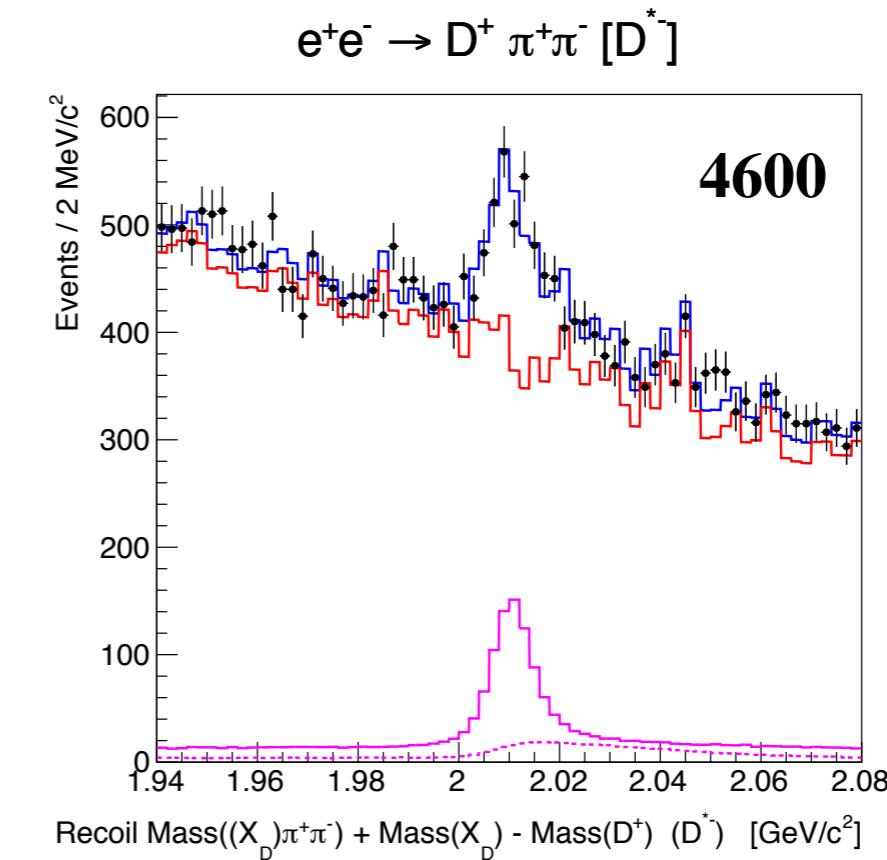
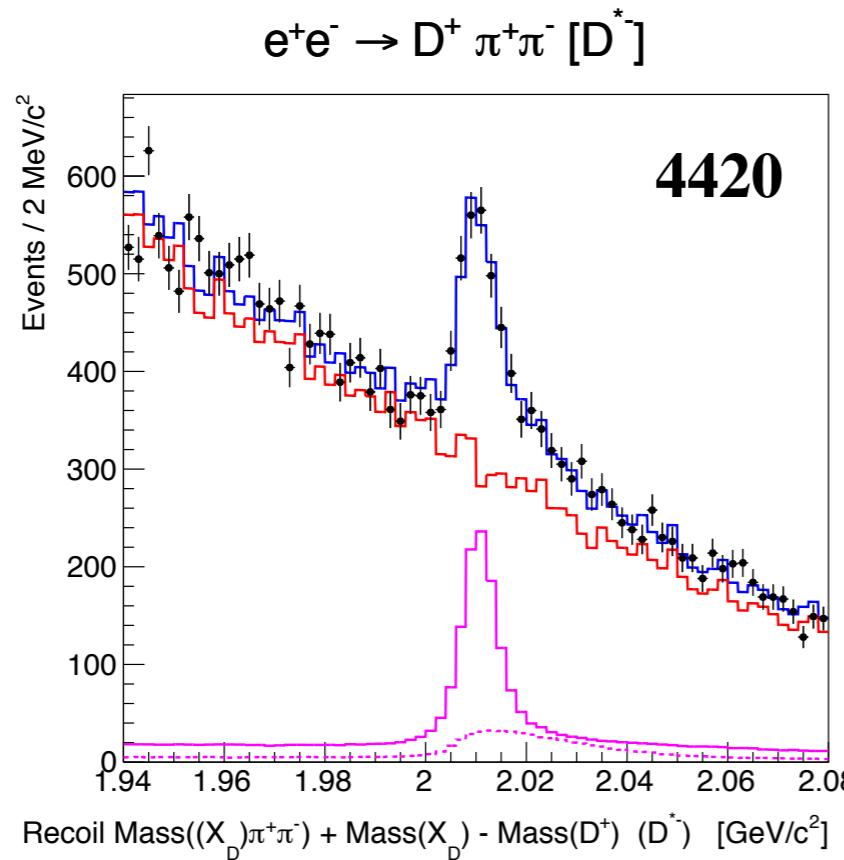
SIGNAL MC

INCLUSIVE MC

DATA

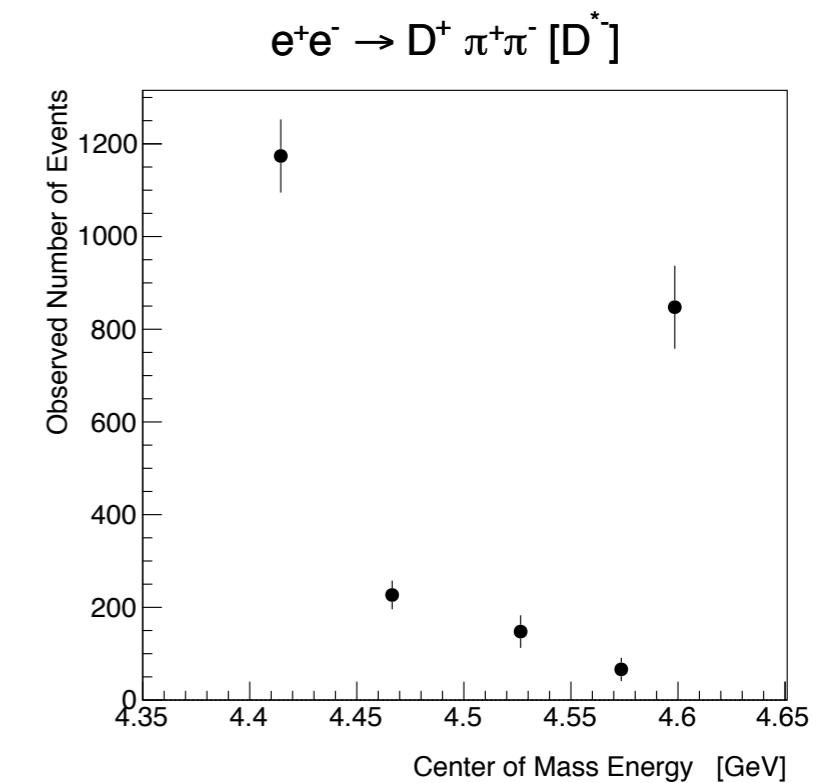
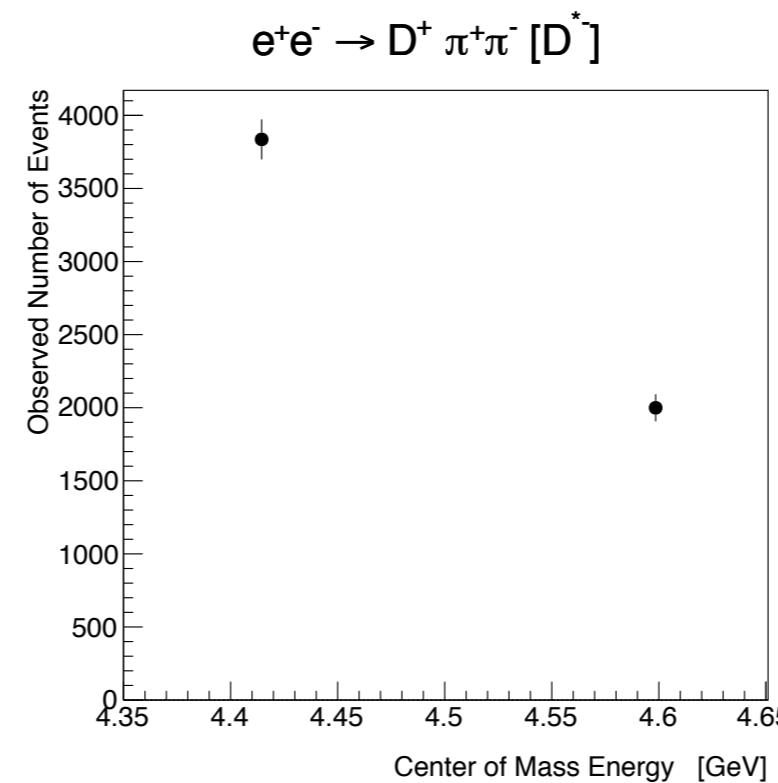
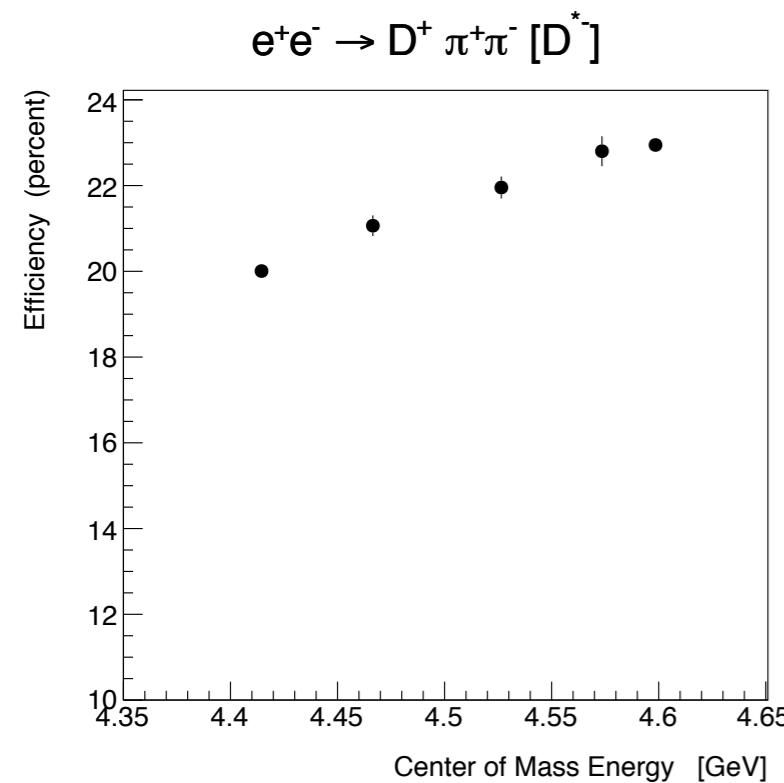
(Using all 2014 data: 4420, 4470, 4530, 4575, 4600.)

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^- D^+D^{*-}$ Cross Section



# I. Measure the $e^+e^- \rightarrow \pi^+\pi^- D^+D^{*-}$ Cross Section

- \* Find the efficiency and number of observed events from the fits.



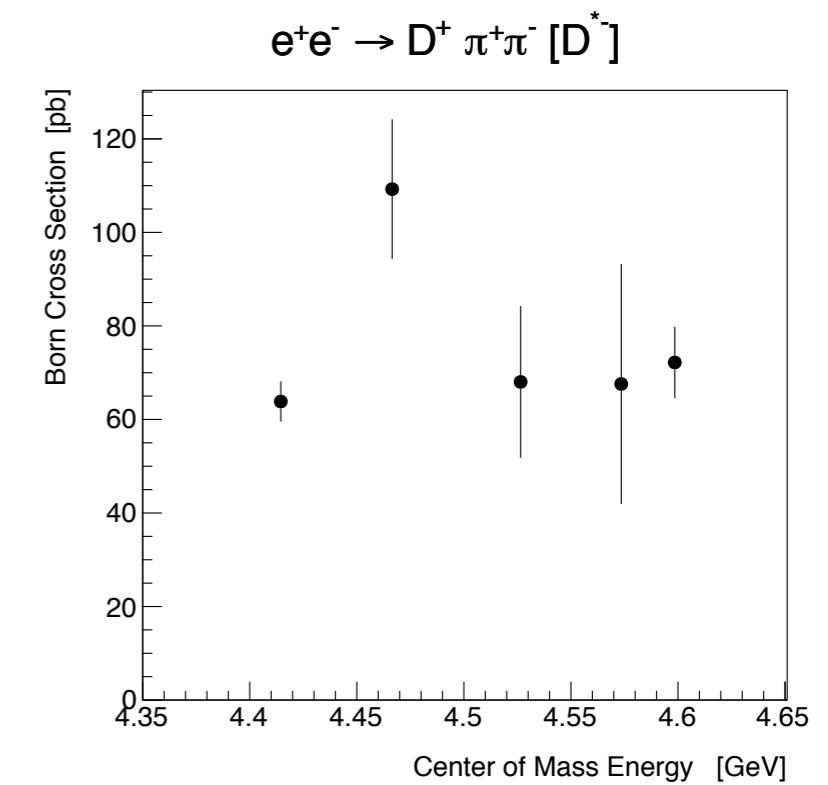
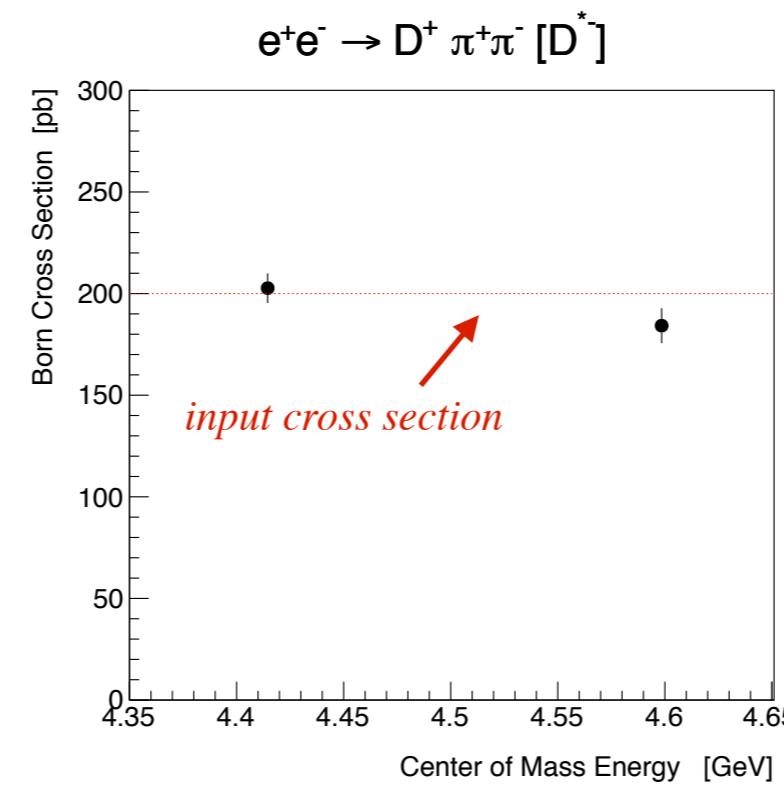
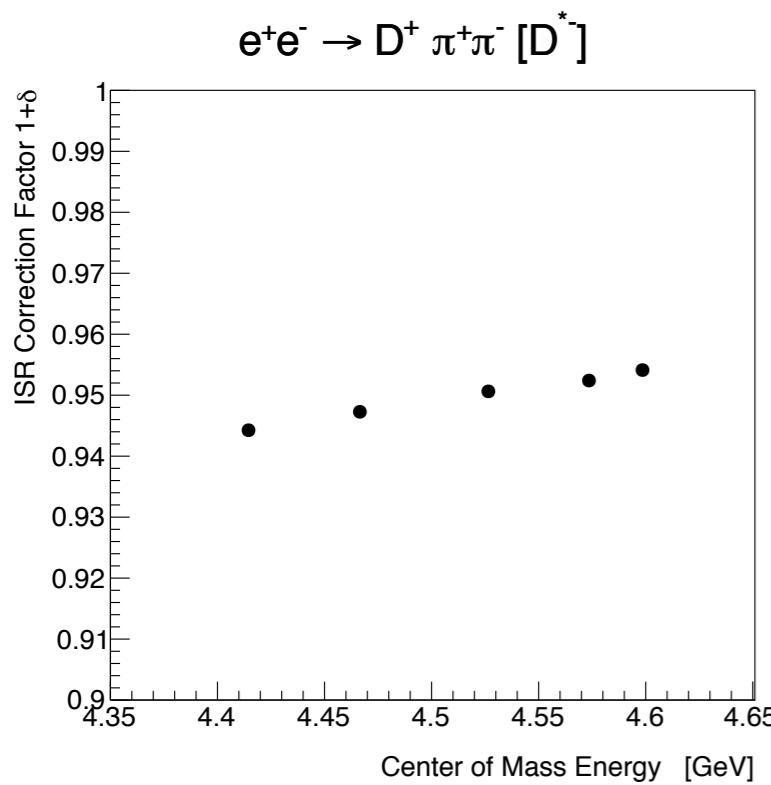
**SIGNAL MC**  
*(assuming flat cross section  
for ISR calculation)*

**INCLUSIVE MC**

**DATA**

# I. Measure the $e^+e^- \rightarrow \pi^+\pi^- D^+D^{*-}$ Cross Section

- \* Get the ISR correction factor from SIGNAL MC.
- \* Divide INCLUSIVE MC and DATA by the efficiency, luminosity, D branching fraction, and ISR correction factor to get the Born Cross Section.



**SIGNAL MC**  
*(assuming flat cross section  
for ISR calculation;  
threshold = 4.2 GeV)*

**INCLUSIVE MC**

**DATA**

# Strategy

I. Measure the  $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$  cross section.

The cross section is ~60 pb, consistent with  $\pi^+\pi^-\psi(1S,2S)$  and  $\pi^+\pi^-h_c(2P)$ .

*Systematic Errors: luminosity; tracking; fitting; ISR.*

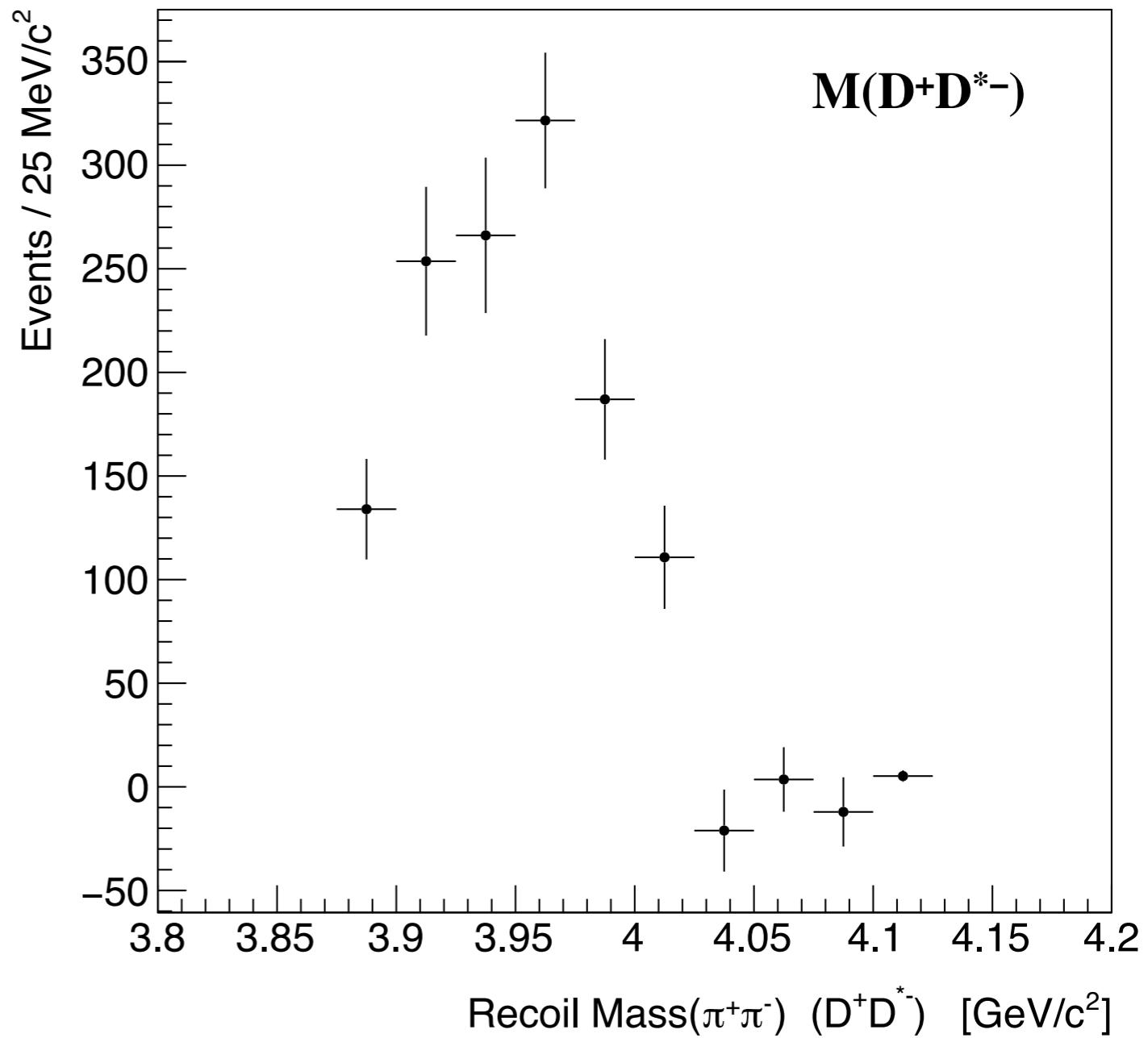
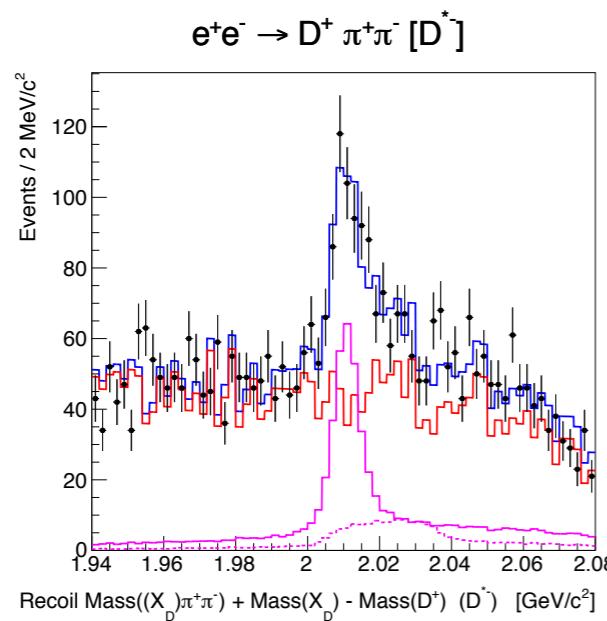
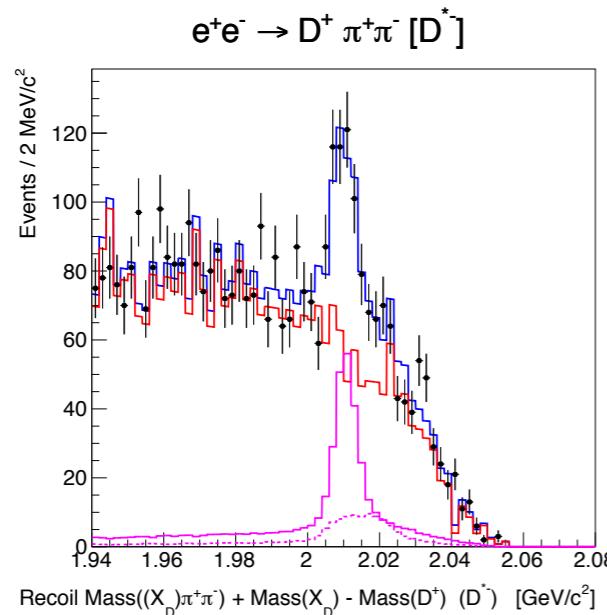
II. Search for  $\pi^+\pi^-h_c(2P)$  with  $h_c(2P) \rightarrow D^+D^{*-}$ .

III. Compare to  $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$ .

## II. Search for $\pi^+\pi^-h_c(2P)$ with $h_c(2P) \rightarrow D^+D^{*-}$

Fit the  $D^{*-}$  as a function of  $M(D^+D^{*-})\dots$

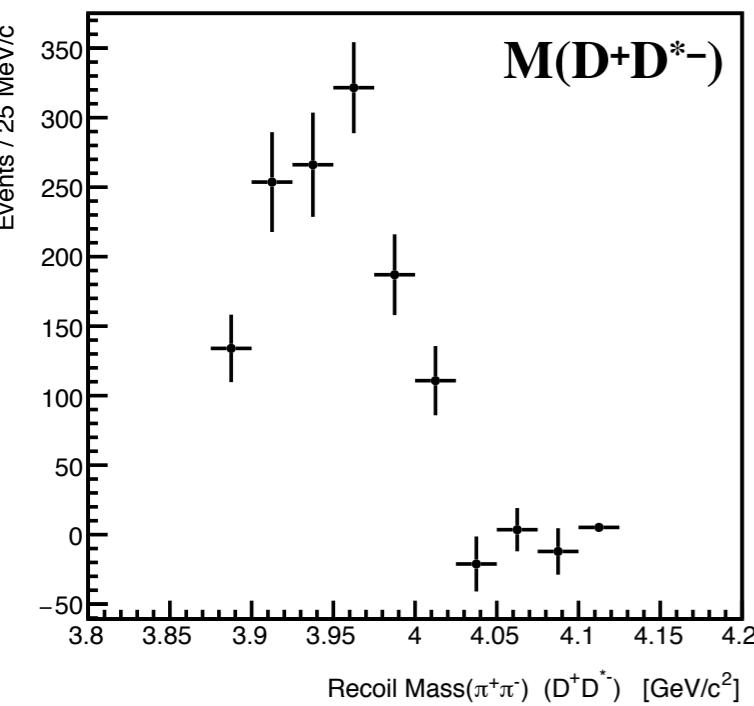
Data at  $E_{CM} = 4420$  MeV



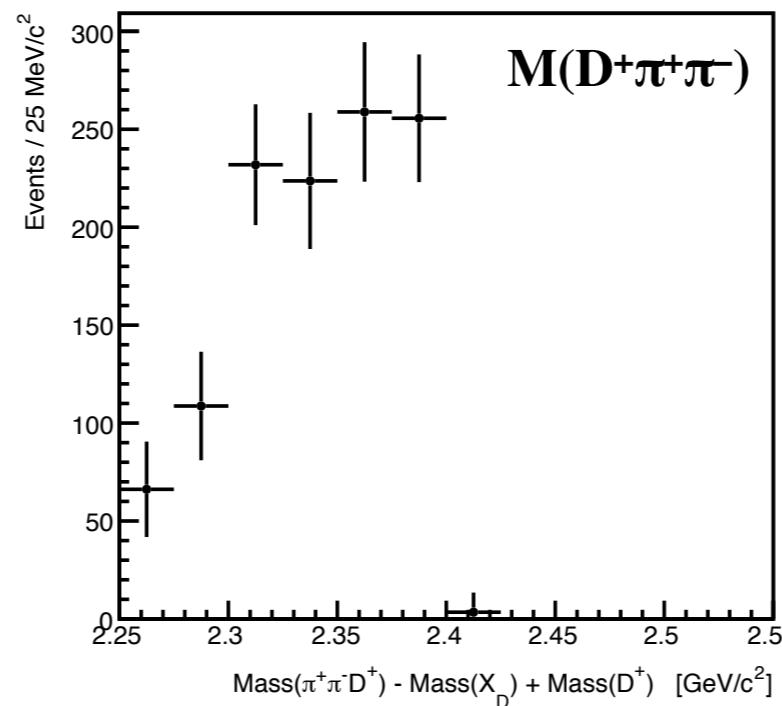
Also look at  $M(D^+\pi^+\pi^-)$  (where there could be a  $D_1(2420)$ ),  
and  $\cos\vartheta_{\pi\pi}$  (which should follow  $1 + \cos^2\vartheta_{\pi\pi}$  for the  $h_c(2P)$ )...

## II. Search for $\pi^+\pi^-h_c(2P)$ with $h_c(2P) \rightarrow D^+D^{*-}$

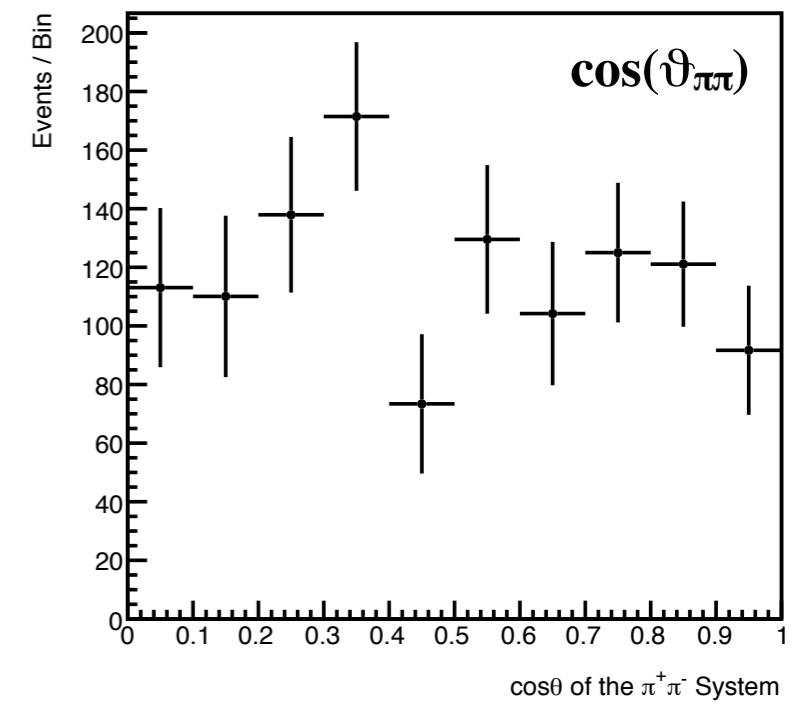
**Data at  $E_{CM} = 4420$  MeV**



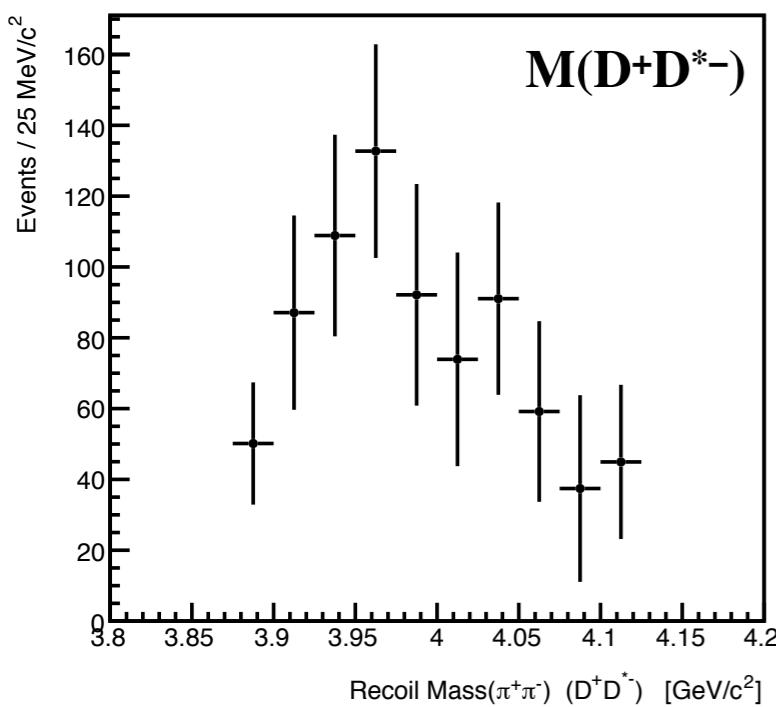
**Data at  $E_{CM} = 4420$  MeV**



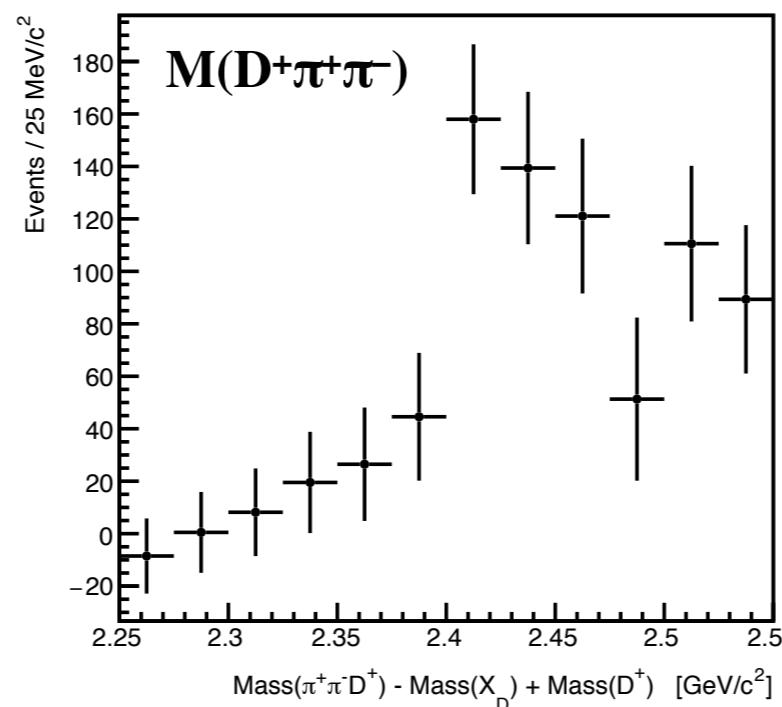
**Data at  $E_{CM} = 4420$  MeV**



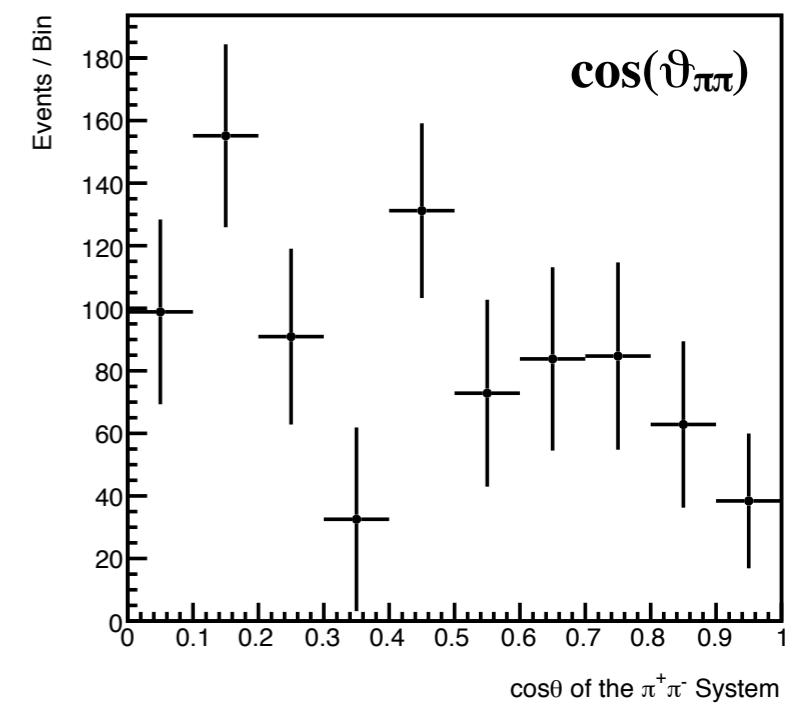
**Data at  $E_{CM} = 4600$  MeV**



**Data at  $E_{CM} = 4600$  MeV**



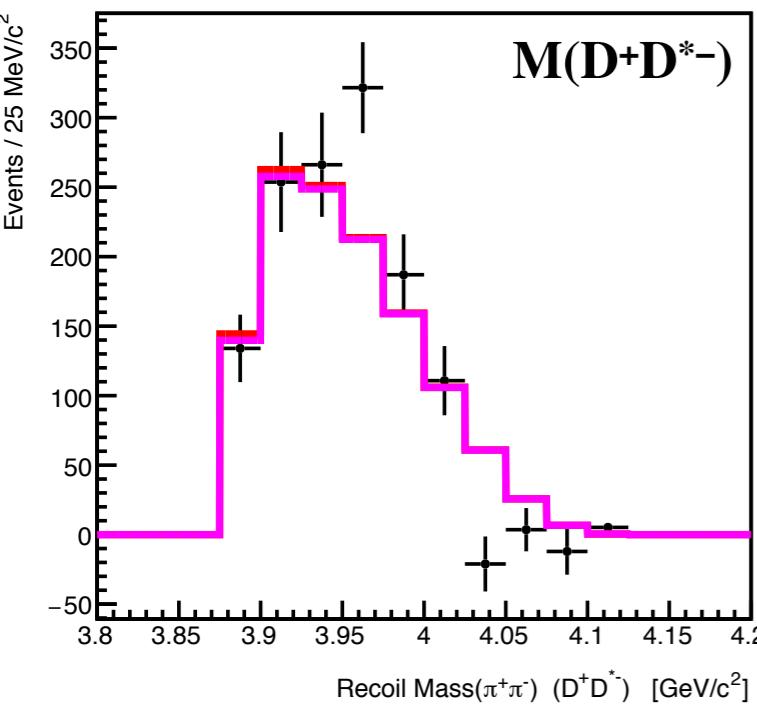
**Data at  $E_{CM} = 4600$  MeV**



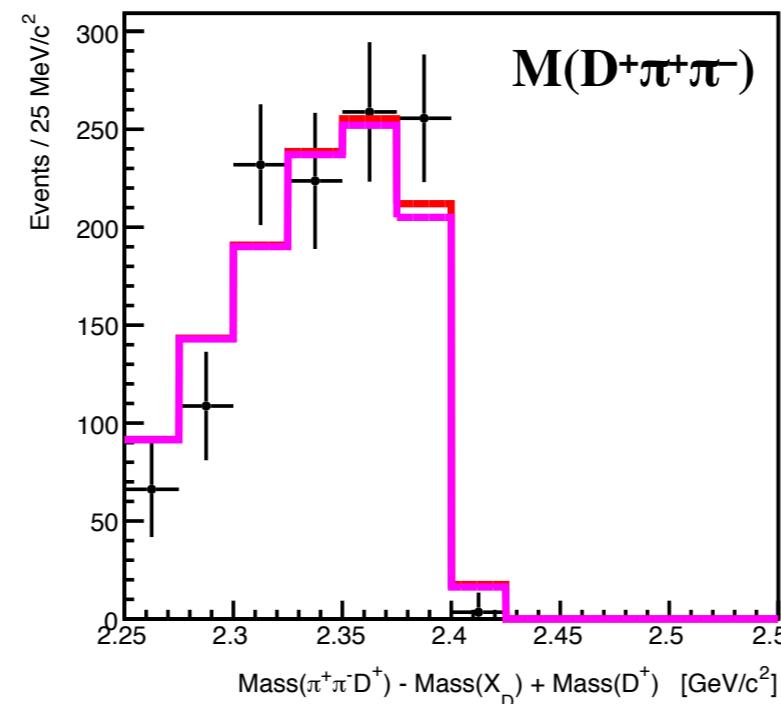
\* Distributions for  $M(D^+D^{*-})$ ,  $M(D^+\pi^+\pi^-)$ , and  $\cos(\vartheta_{\pi\pi})$ .

## II. Search for $\pi^+\pi^-h_c(2P)$ with $h_c(2P) \rightarrow D^+D^{*-}$

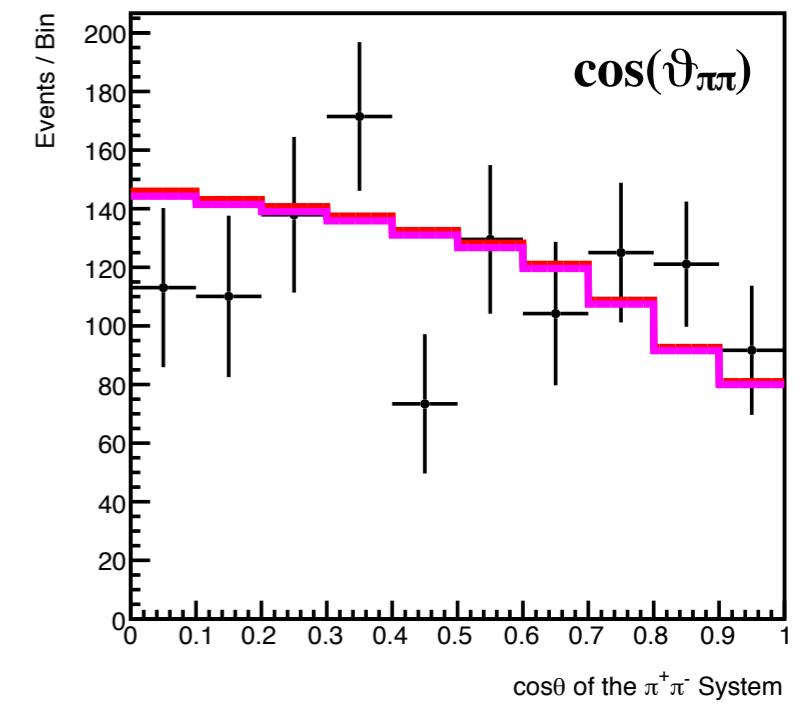
**Data at  $E_{CM} = 4420$  MeV**



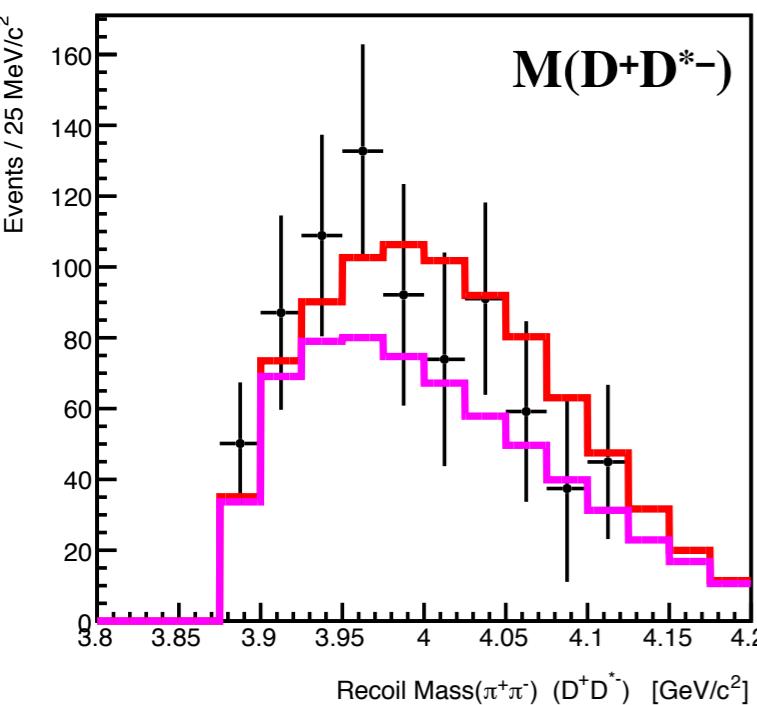
**Data at  $E_{CM} = 4420$  MeV**



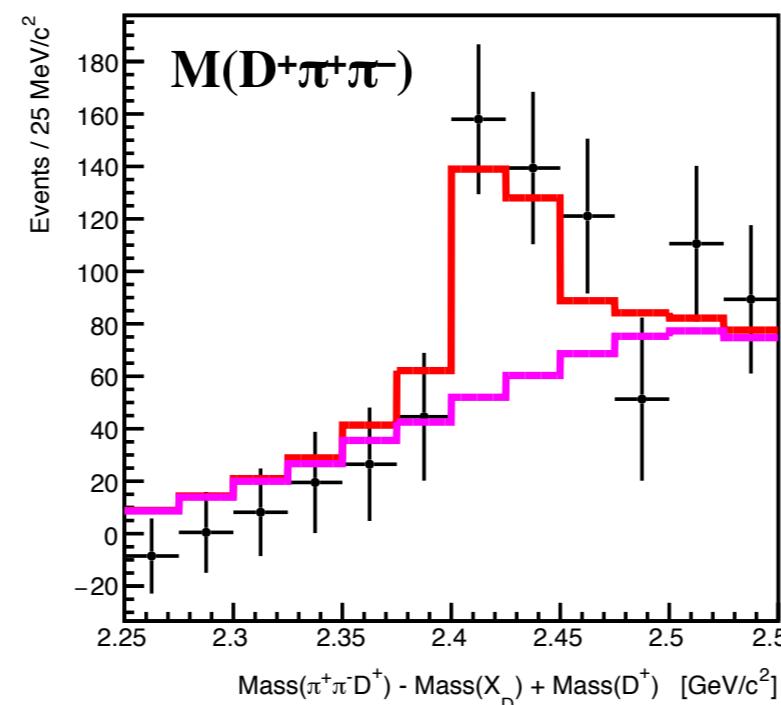
**Data at  $E_{CM} = 4420$  MeV**



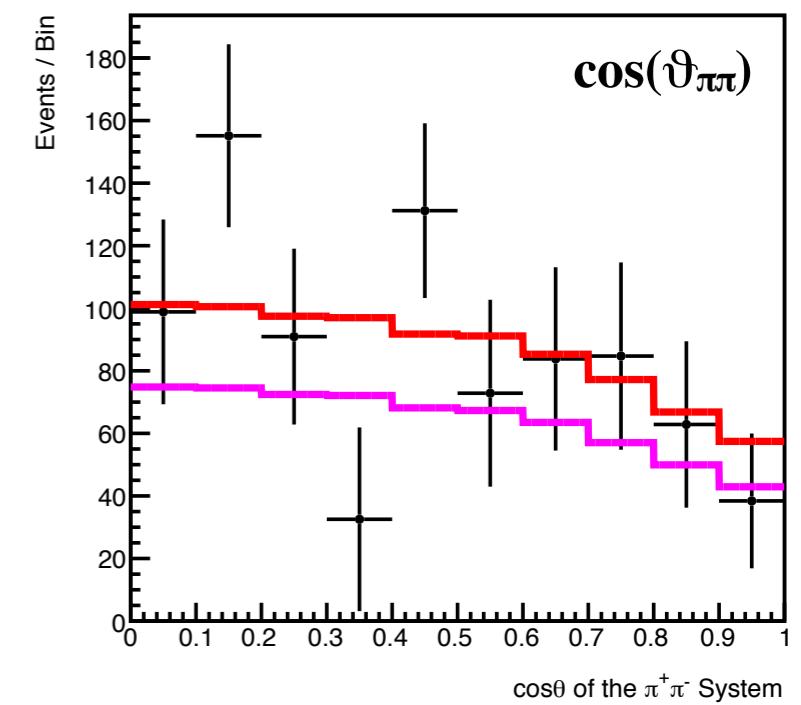
**Data at  $E_{CM} = 4600$  MeV**



**Data at  $E_{CM} = 4600$  MeV**



**Data at  $E_{CM} = 4600$  MeV**

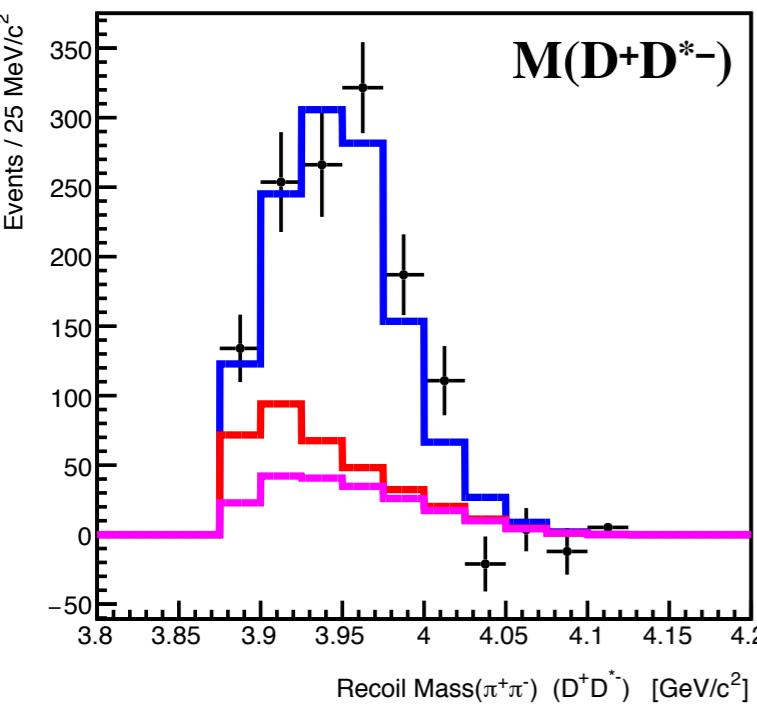


\* Perform simultaneous fits at 4420 and 4600 using **Phase Space** and **D<sub>1</sub><sup>+</sup>(2420)D<sup>\*-</sup>**.

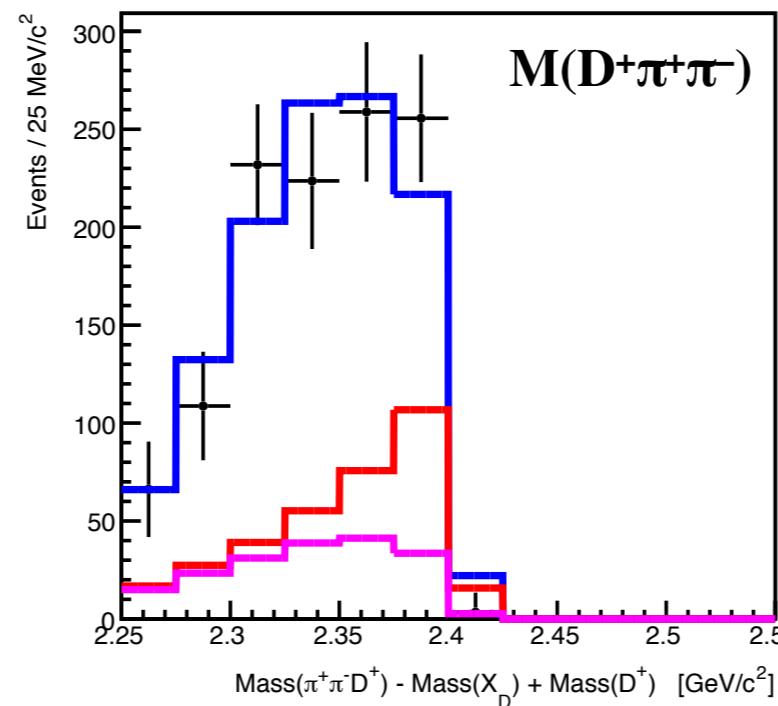
$$\chi^2 = 82.7$$

## II. Search for $\pi^+\pi^-h_c(2P)$ with $h_c(2P) \rightarrow D^+D^{*-}$

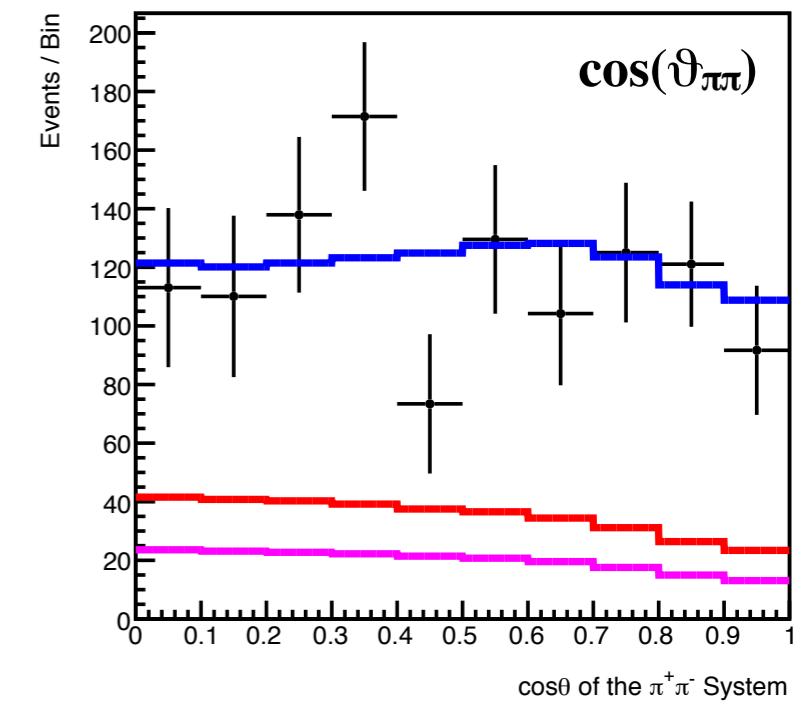
Data at  $E_{CM} = 4420$  MeV



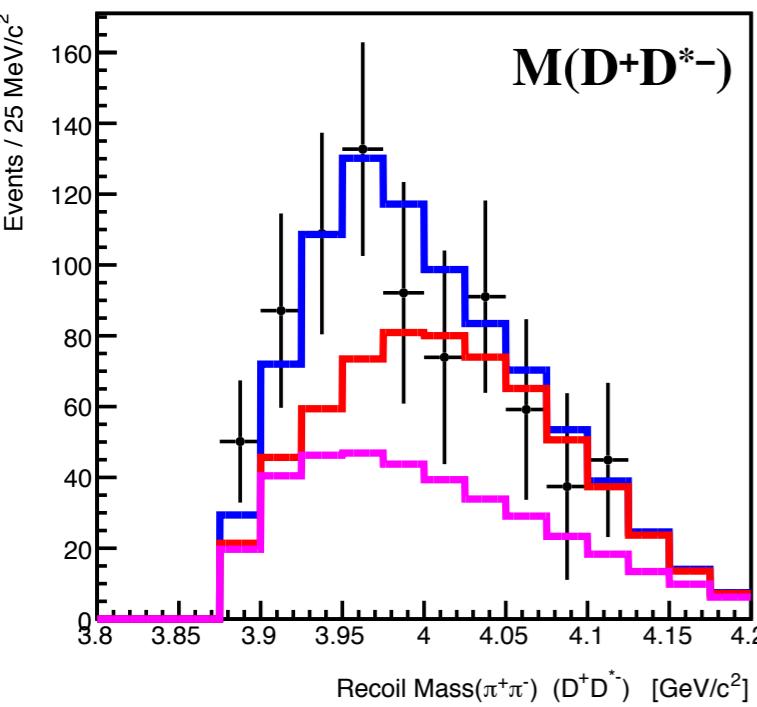
Data at  $E_{CM} = 4420$  MeV



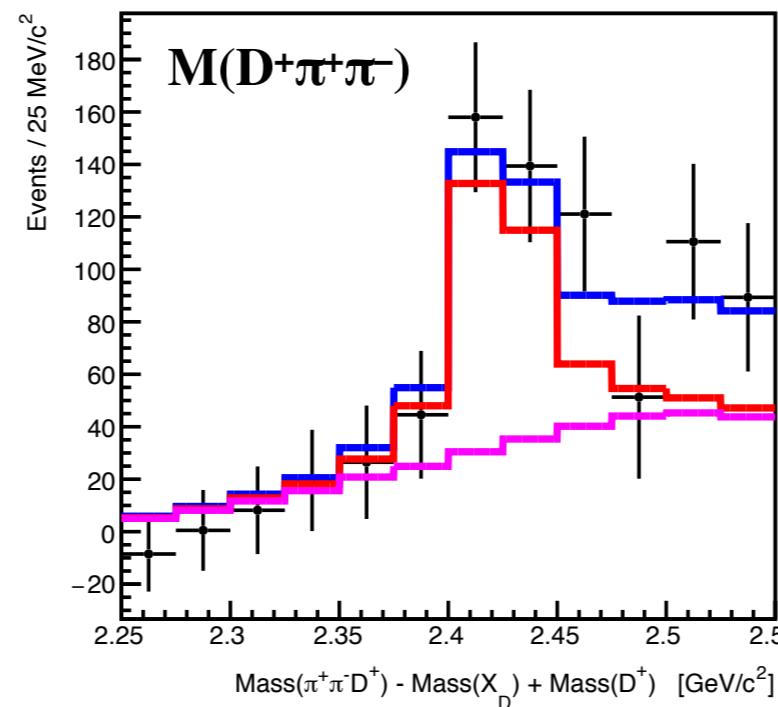
Data at  $E_{CM} = 4420$  MeV



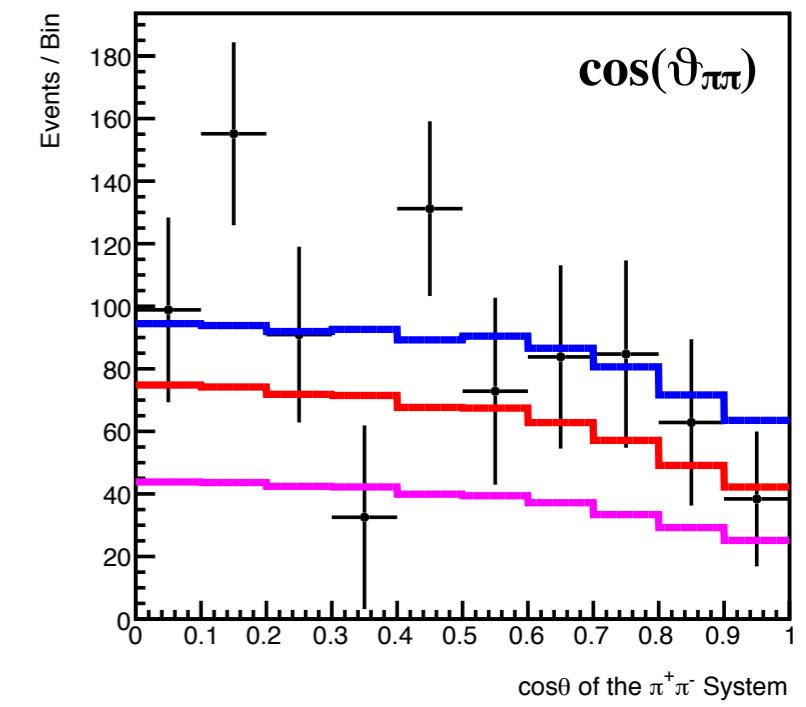
Data at  $E_{CM} = 4600$  MeV



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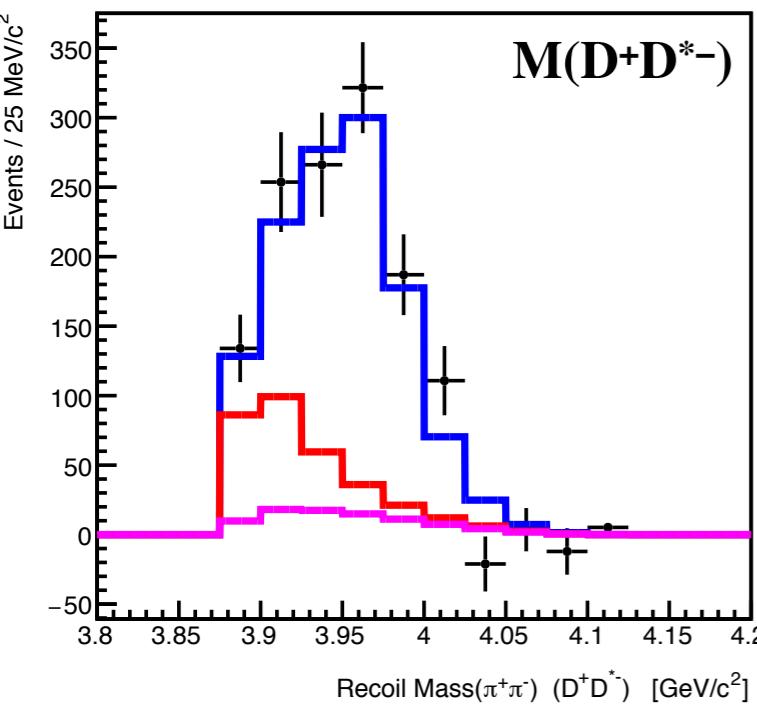


\* Use **Phase Space** and  **$D_1^+(2420)D^{*-}$**  and  **$h_c(2P)$**  (with parameters from theory).

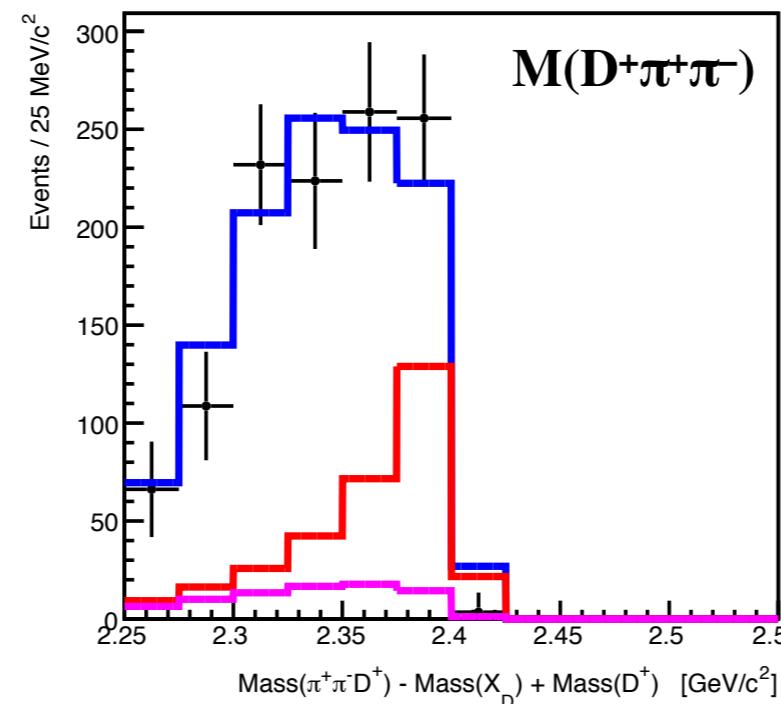
$$\chi^2 = 57.4$$

## II. Search for $\pi^+\pi^-h_c(2P)$ with $h_c(2P) \rightarrow D^+D^{*-}$

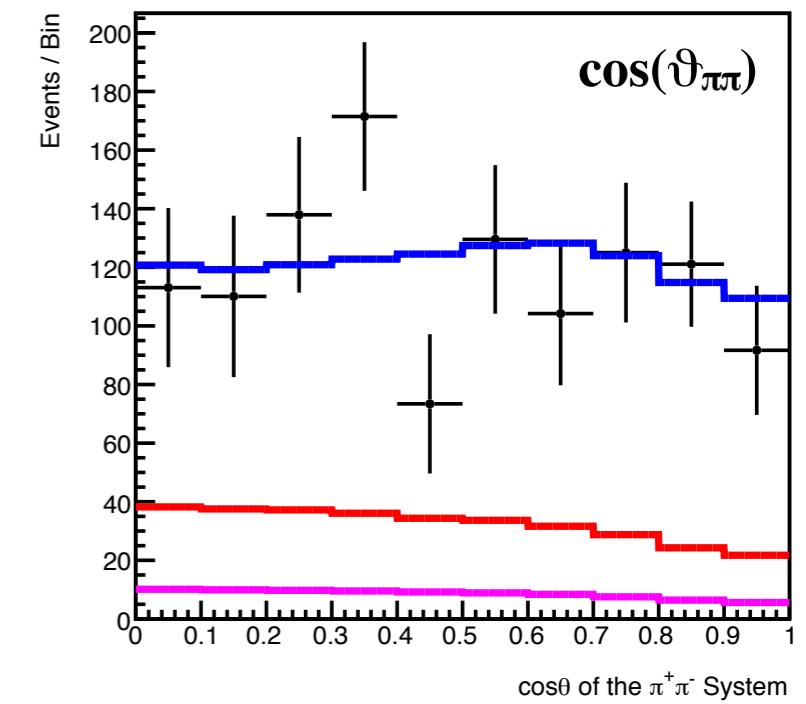
Data at  $E_{CM} = 4420$  MeV



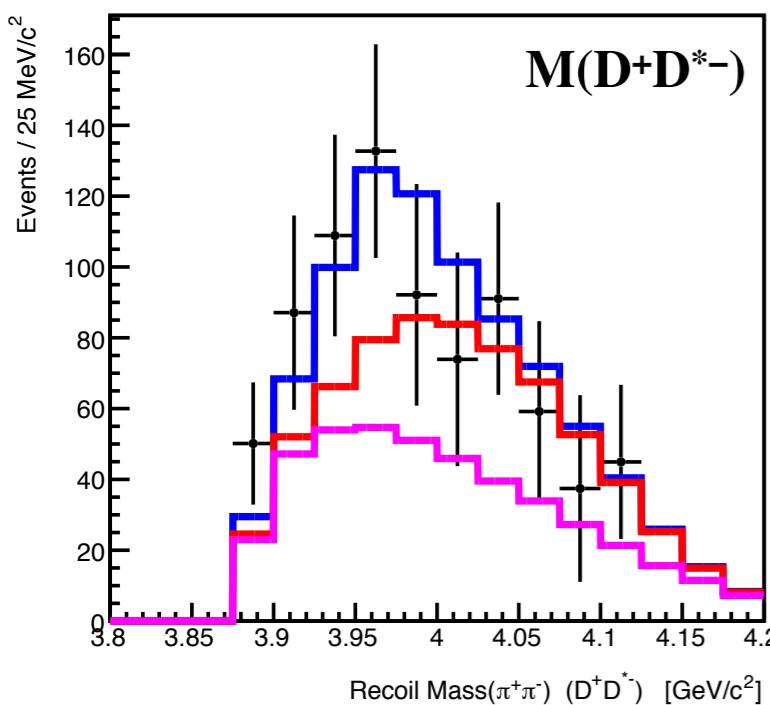
Data at  $E_{CM} = 4420$  MeV



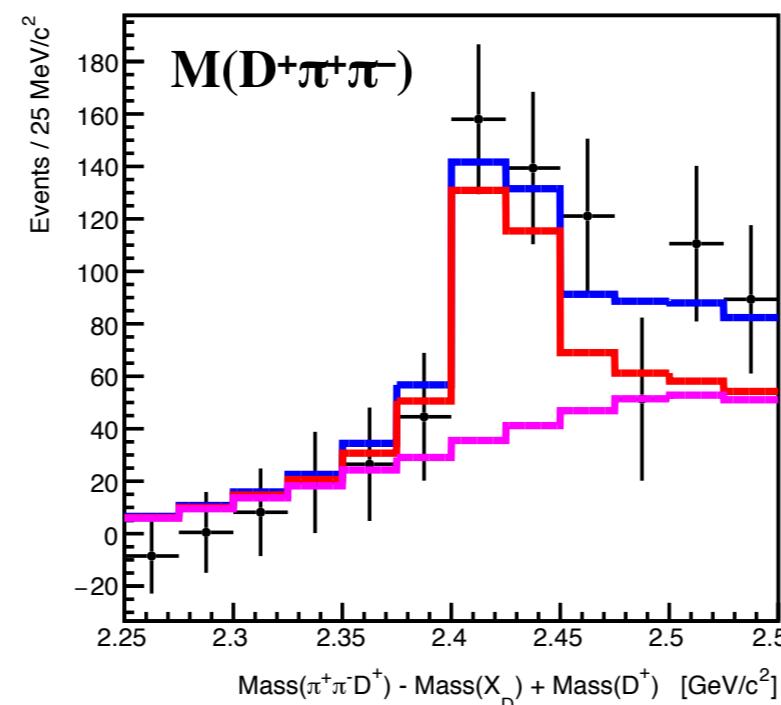
Data at  $E_{CM} = 4420$  MeV



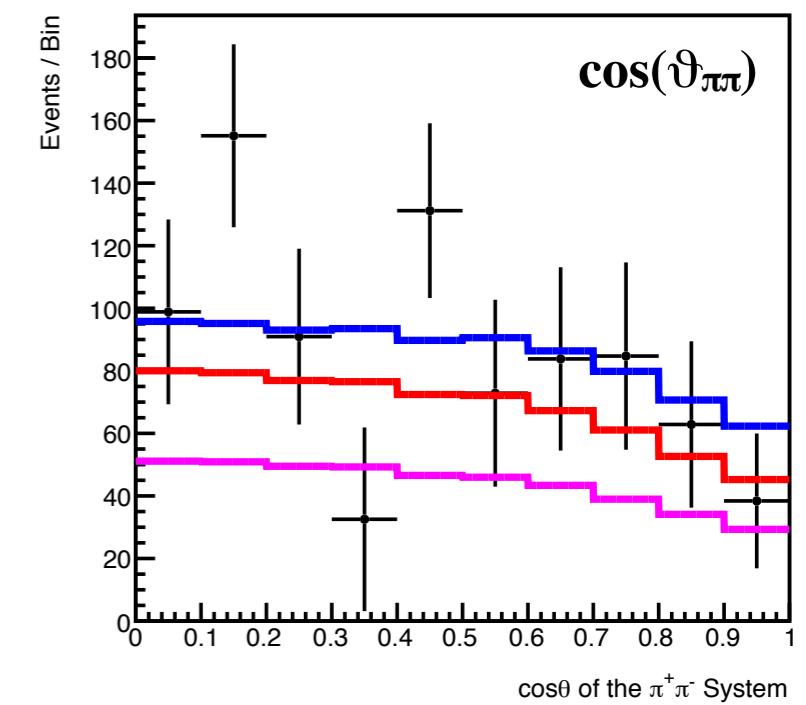
Data at  $E_{CM} = 4600$  MeV



Data at  $E_{CM} = 4600$  MeV



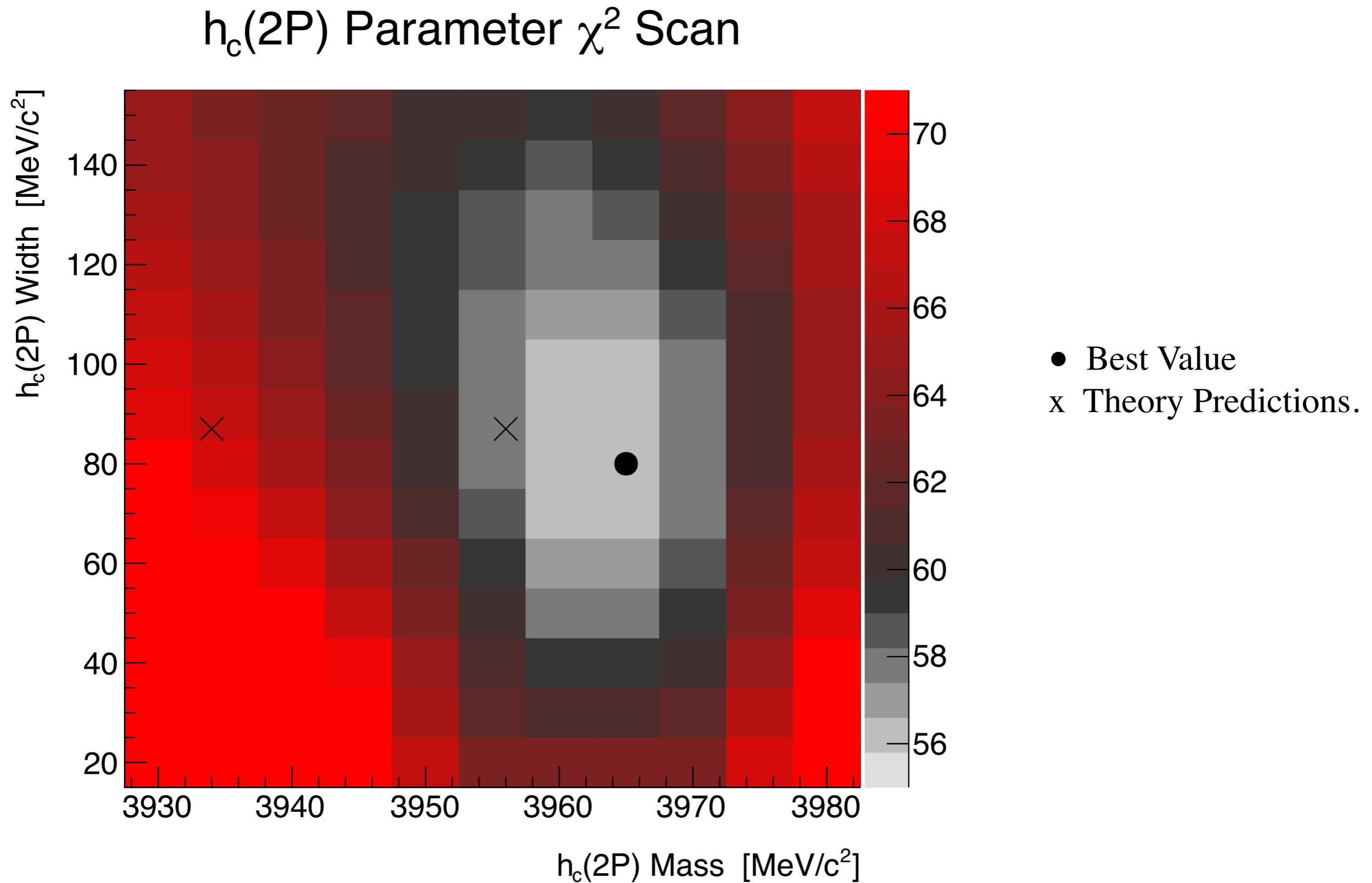
Data at  $E_{CM} = 4600$  MeV



\* Use **Phase Space** and **D<sub>1</sub><sup>+</sup>(2420)D<sup>\*-</sup>** and **h<sub>c</sub>(2P)** (with best parameters).

$$\chi^2 = 56.0$$

## II. Search for $\pi^+\pi^- h_c(2P)$ with $h_c(2P) \rightarrow D^+D^{*-}$



# Strategy

I. Measure the  $e^+e^- \rightarrow \pi^+\pi^- D^+D^{*-}$  cross section.

**The cross section is  $\sim 60$  pb, consistent with  $\pi^+\pi^-\psi(1S,2S)$  and  $\pi^+\pi^-h_c(2P)$ .**

*Systematic Errors: luminosity; tracking; fitting; ISR.*

II. Search for  $\pi^+\pi^-h_c(2P)$  with  $h_c(2P) \rightarrow D^+D^{*-}$ .

**Including an  $h_c(2P)$  signal describes data better than pure phase space and  $D_1D^*$ .**

*The statistical significance calculation requires more thought.*

**The mass and width are consistent with theoretical expectations.**

*Systematic Errors: fitting; mass calibration.*

III. Compare to  $e^+e^- \rightarrow \pi^-\pi^0 D^+\bar{D}^{*0}$ .

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$

#### Isospin Ratios

These ratios always hold:

$$\pi^+\pi^-D^+D^{*-} : \pi^+\pi^-D^0\bar{D}^{*0} = 1 : 1$$

$$\pi^-\pi^0D^+\bar{D}^{*0} : \pi^+\pi^0D^0D^{*-} = 1 : 1$$

$$\pi^0\pi^0D^+D^{*-} : \pi^0\pi^0D^0\bar{D}^{*0} = 1 : 1$$

For  $(\pi\pi)_{I=0}(D\bar{D}^*)_{I=0}$ :

$$\pi^+\pi^-D^+D^{*-} : \pi^-\pi^0D^+\bar{D}^{*0} : \pi^0\pi^0D^+D^{*-} = 2 : 0 : 1$$

For  $(\pi\pi)_{I=1}(D\bar{D}^*)_{I=1}$ :

$$\pi^+\pi^-D^+D^{*-} : \pi^-\pi^0D^+\bar{D}^{*0} : \pi^0\pi^0D^+D^{*-} = 1 : 2 : 0$$

For  $(D\pi)_{I=1/2}(\bar{D}^*\pi)_{I=1/2}$ :

$$\pi^+\pi^-D^+D^{*-} : \pi^-\pi^0D^+\bar{D}^{*0} : \pi^0\pi^0D^+D^{*-} = 4 : 4 : 1$$

**The ratio can tell us something about the isospin composition.**

$$\Rightarrow \frac{\sigma(\pi^-\pi^0D^+\bar{D}^{*0})}{\sigma(\pi^+\pi^-D^+D^{*-})} = 0$$

$$\Rightarrow \frac{\sigma(\pi^-\pi^0D^+\bar{D}^{*0})}{\sigma(\pi^+\pi^-D^+D^{*-})} = 2$$

$$\Rightarrow \frac{\sigma(\pi^-\pi^0D^+\bar{D}^{*0})}{\sigma(\pi^+\pi^-D^+D^{*-})} = 1$$

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$

Use almost the same method as before: Reconstruct  $\pi^-\pi^0D^+$  with  $D^+ \rightarrow K^-\pi^+\pi^+$

Isolate the reaction by finding the  $D^+$  in  $K^-\pi^+\pi^+$  and looking for the  $D^{*0}$  in the  $(K^-\pi^+\pi^+)\pi^-\pi^0$  missing mass. Use all combinations. Same track selections.

Perform a 1C fit for the  $\pi^0$  mass; require  $\chi^2 < 3$ .

**Use four classes of data:**

**SIGNAL MC:** Includes  $\pi^-\pi^0D^+D^{*0}$  and  $\pi^-\pi^0D^0D^{*+}$ .

*The latter is an irreducible background, since  $D^{*+} \rightarrow \pi^0D^+$ .*

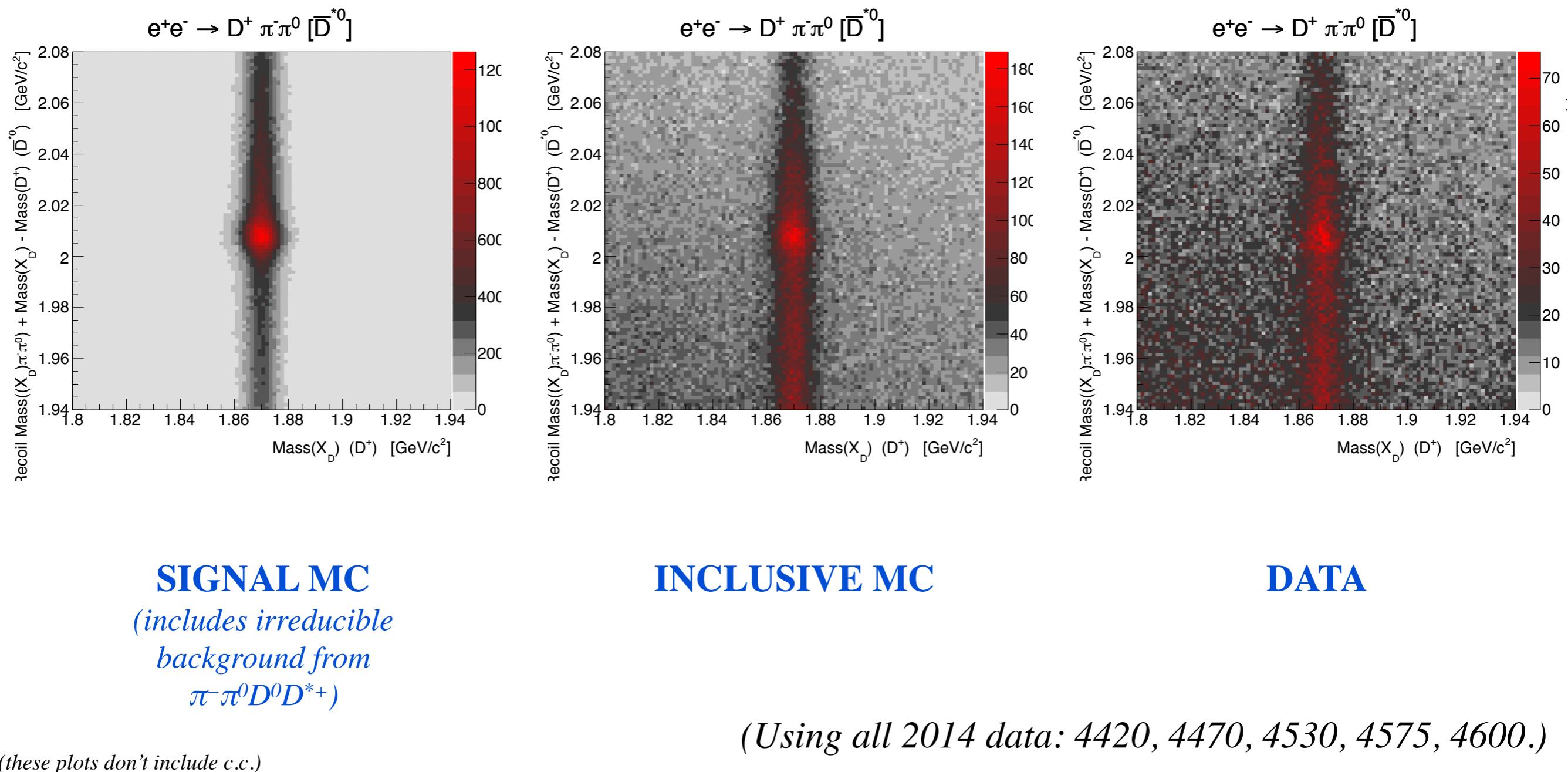
**$\pi D^* D^*$  MC:** Since this channel has peaking backgrounds, we generated a larger sample than what is in the D $\bar{D}$  MC. Charge combinations are fixed by isospin.

**INCLUSIVE MC:** (1) Includes full samples of inclusive D $\bar{D}$  MC at 4.42 and 4.60 GeV (*including important channels of the form  $\pi D^* D^*$* ).  
(2) We also add 200 pb each for all charge combinations of the form  $\pi\pi D D^*$  (*which includes signal as well as potential peaking backgrounds*).

**DATA:** Currently use all of the 2014 data: 4420, 4470, 4530, 4575, 4600 MeV.

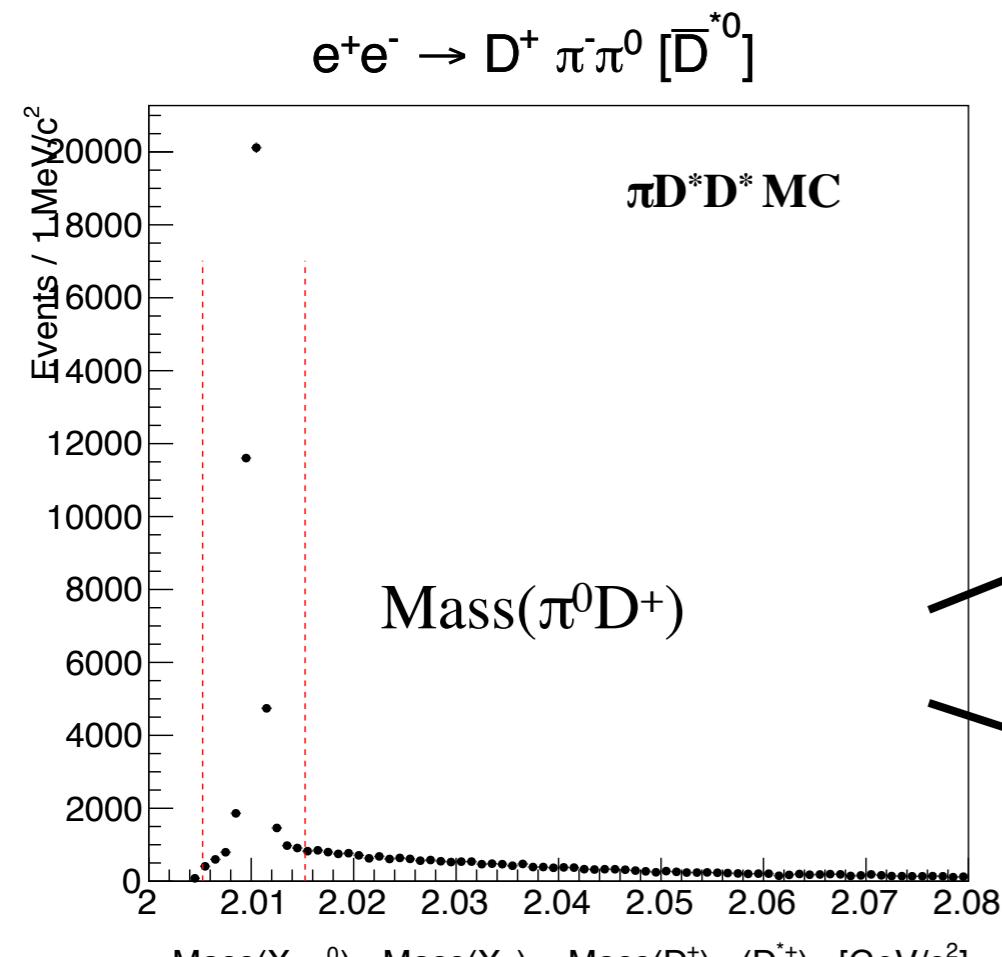
### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$

- \* Find the  $D^+$  using the  $D^+ \rightarrow K^-\pi^+\pi^+$  mass (*x-axis*).
- \* Find the  $D^{*0}$  using the  $D^+\pi^-\pi^0$  recoil mass [ $RM((K^-\pi^+\pi^+)\pi^-\pi^0) + M(K^-\pi^+\pi^+) - M(D^+)$ ] (*y-axis*).
- \* There are large peaking backgrounds from different combinations of  $\pi D^* D^*$ .



### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$

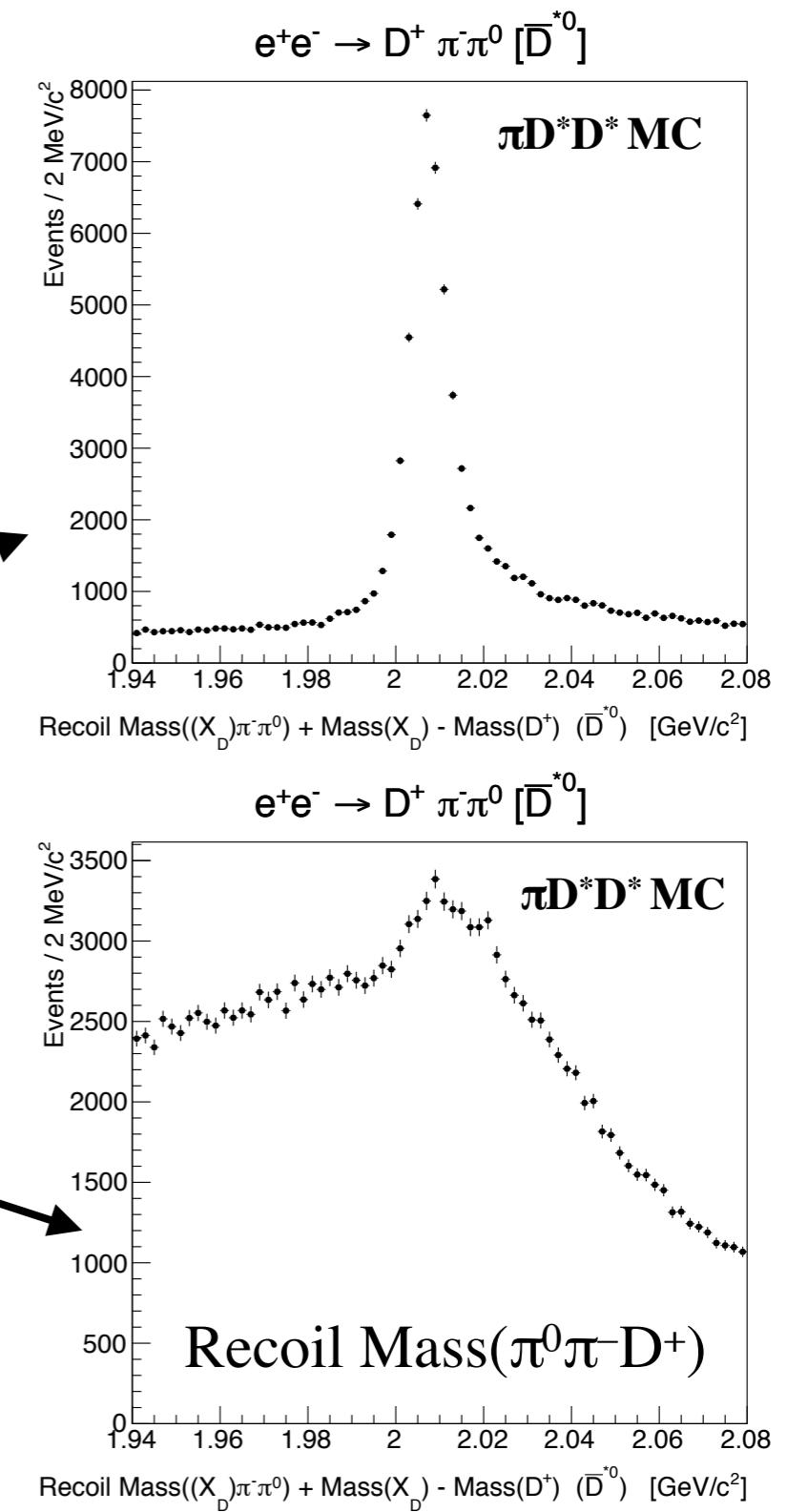
**Use the  $\pi D^* D^*$  MC to fix the peaking backgrounds.**



MC FOR  $\pi D^* D^*$

Select  $D^{*+} \rightarrow \pi^0 D^+$   
to find the other  $D^*$ .

Veto  $D^{*+} \rightarrow \pi^0 D^+$   
to find peaking  
background.



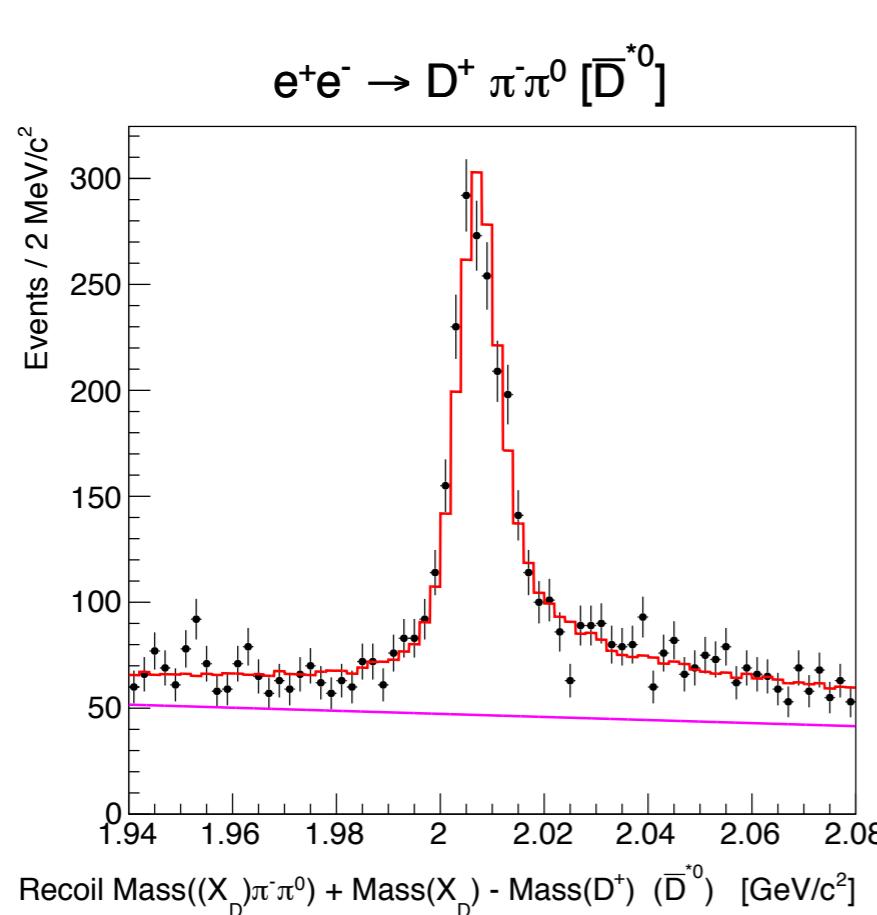
*Use the top to fit the data; then fix the size of the bottom...*

(these plots don't include c.c.)

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$

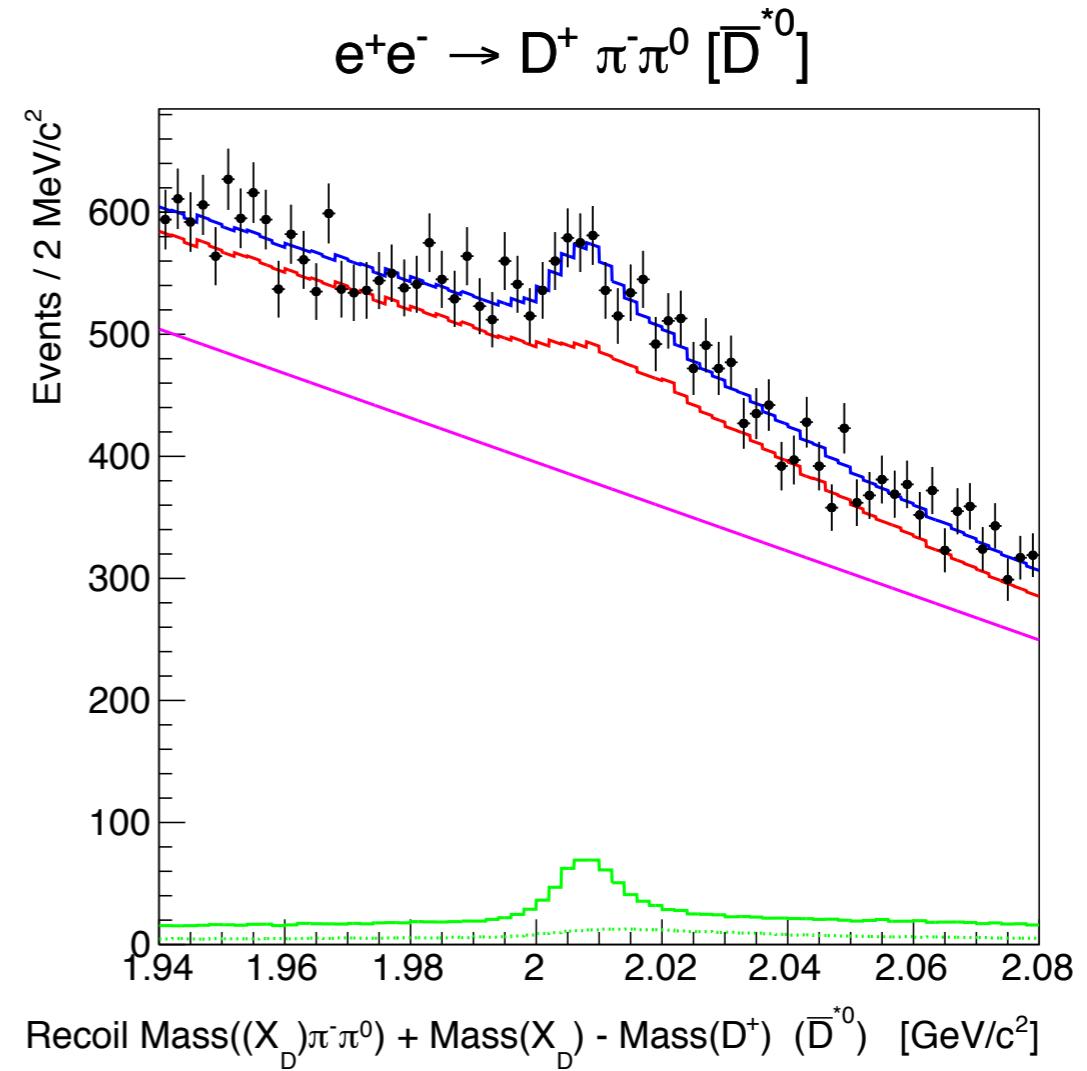
Fits (current technique), three free parameters:

- \* Get the  **$\pi D^* D^*$  background** shape from MC; fix its size using data.
- \* Use a **1st order polynomial** for non-peaking backgrounds.
- \* Take the **signal** shape from signal MC (*there are two components –  $\pi^-\pi^0D^0D^{*+}$  is an irreducible background*).



Select  $D^{*+} \rightarrow \pi^0D^+$  to fix  
the size of the  $\pi D^* D^*$  background.

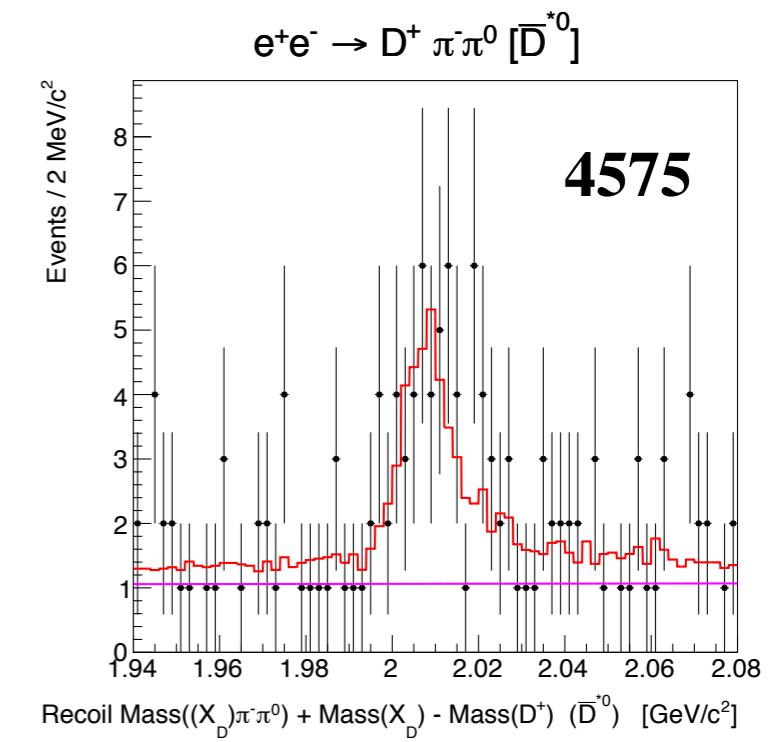
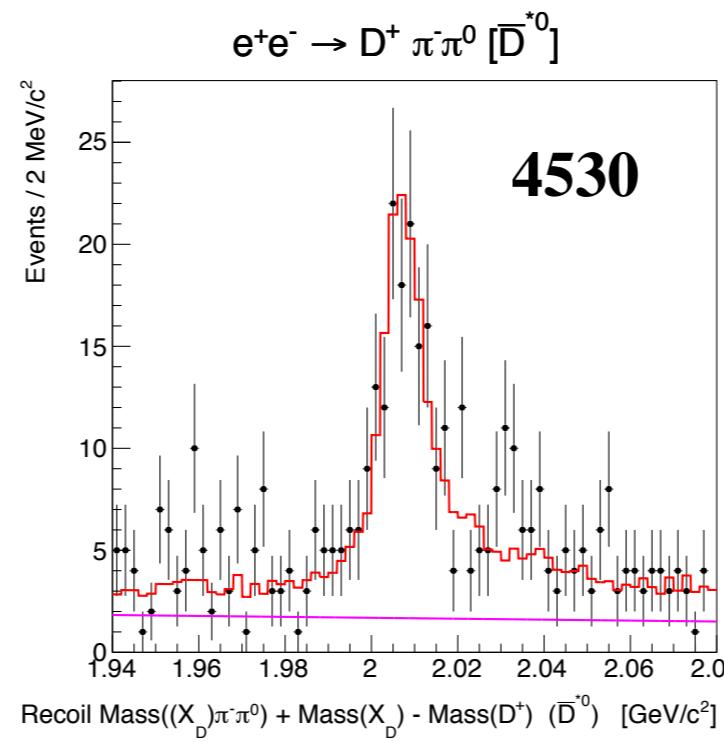
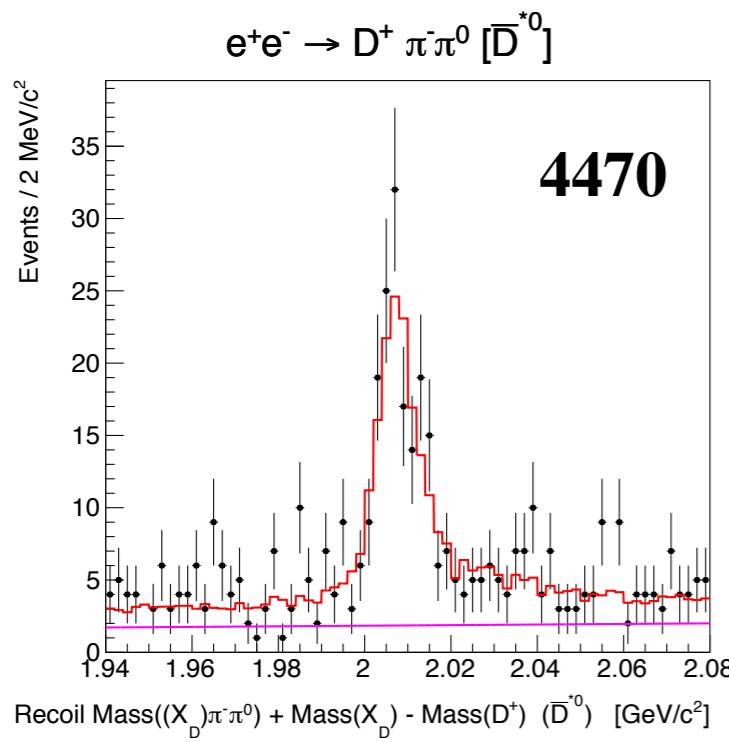
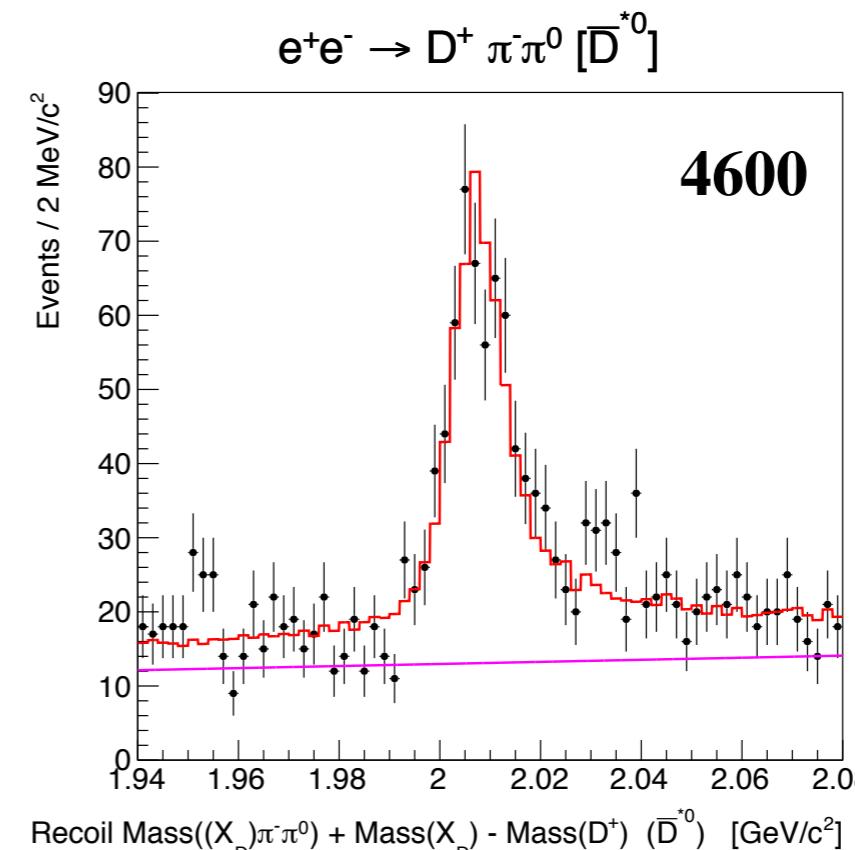
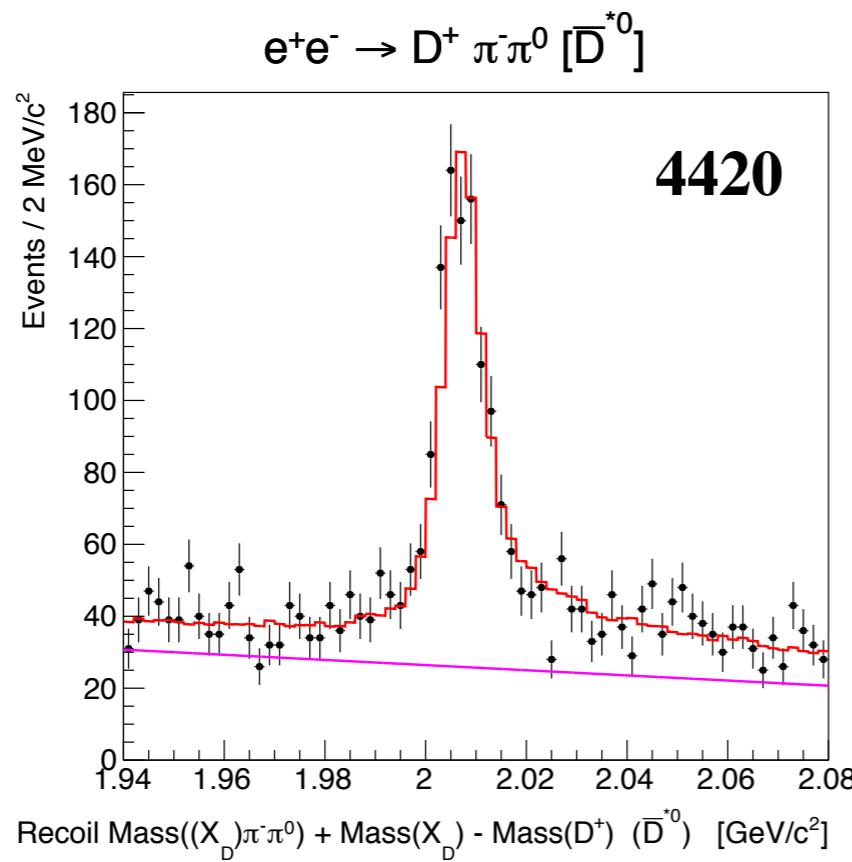
(these plots don't include c.c.)



Veto  $D^{*+} \rightarrow \pi^0D^+$  with the size of  $\pi D^* D^*$  fixed.

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0 D^+\bar{D}^{*0}$

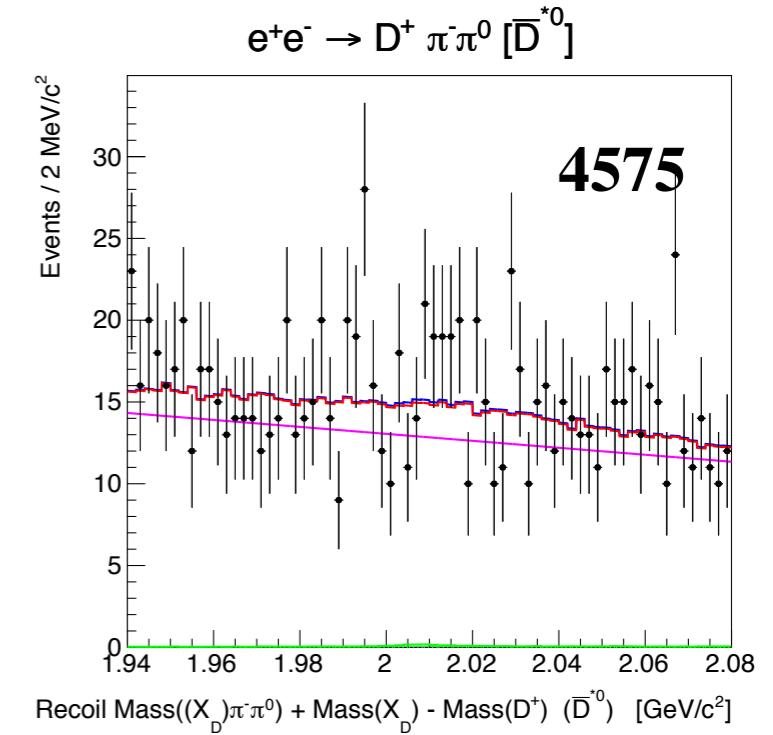
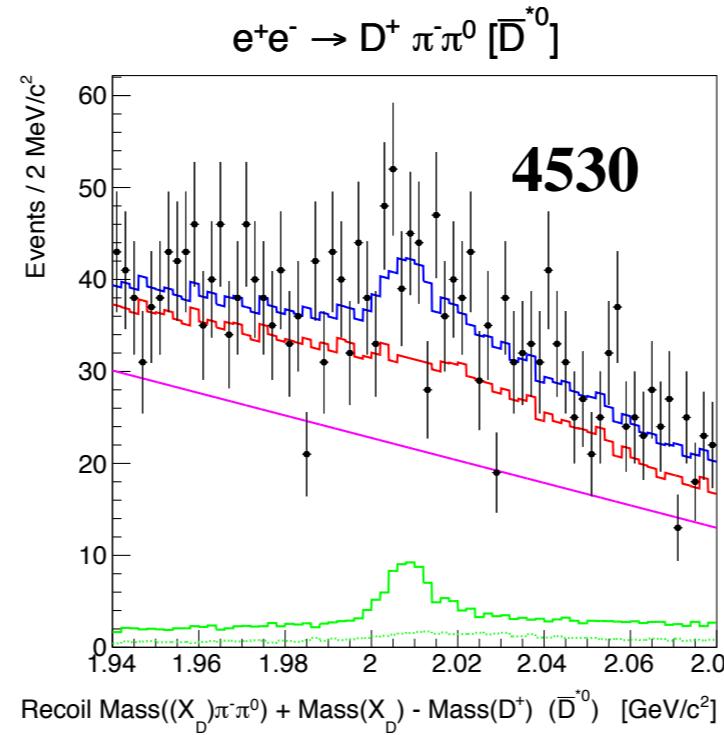
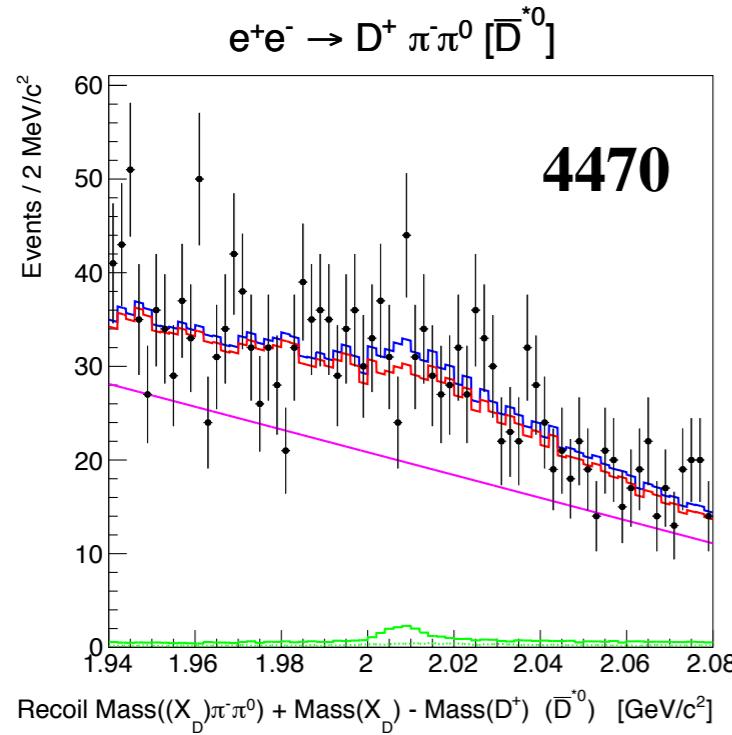
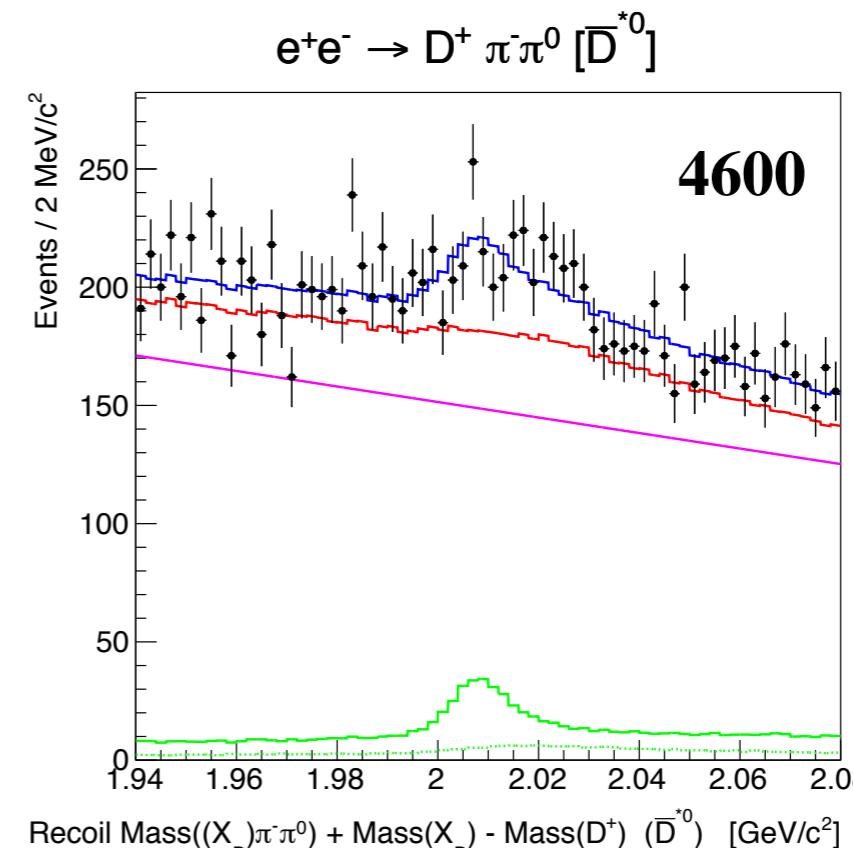
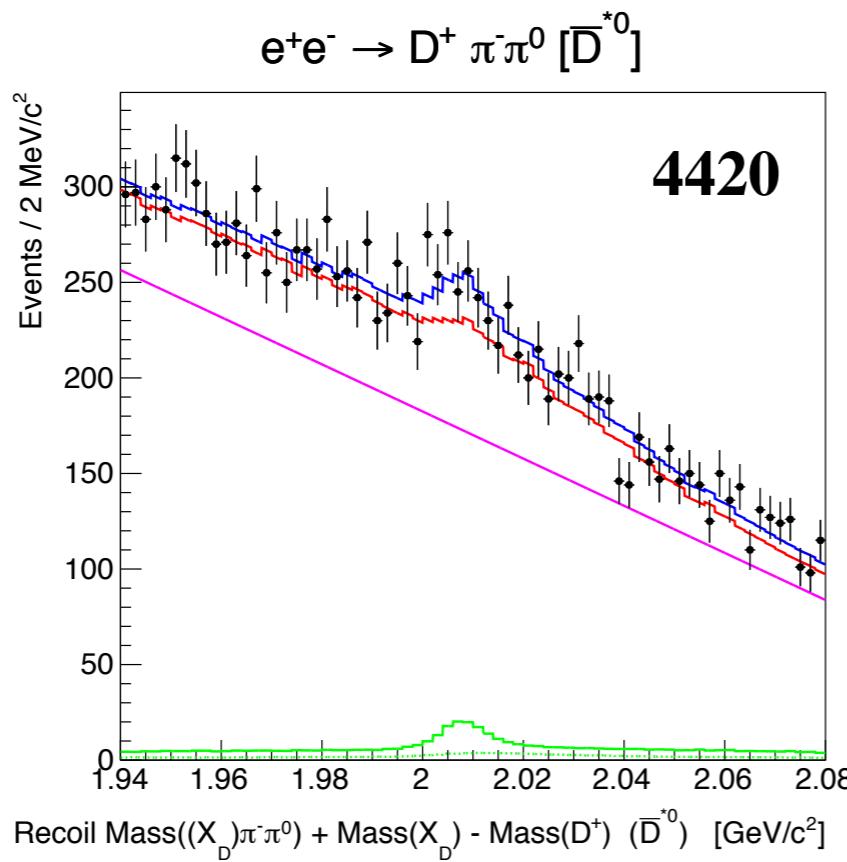
Select  
 $D^{*+} \rightarrow \pi^0 D^+$   
 to fix the  
 size of the  
 background.



(these plots don't include c.c.)

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0 D^+\bar{D}^{*0}$

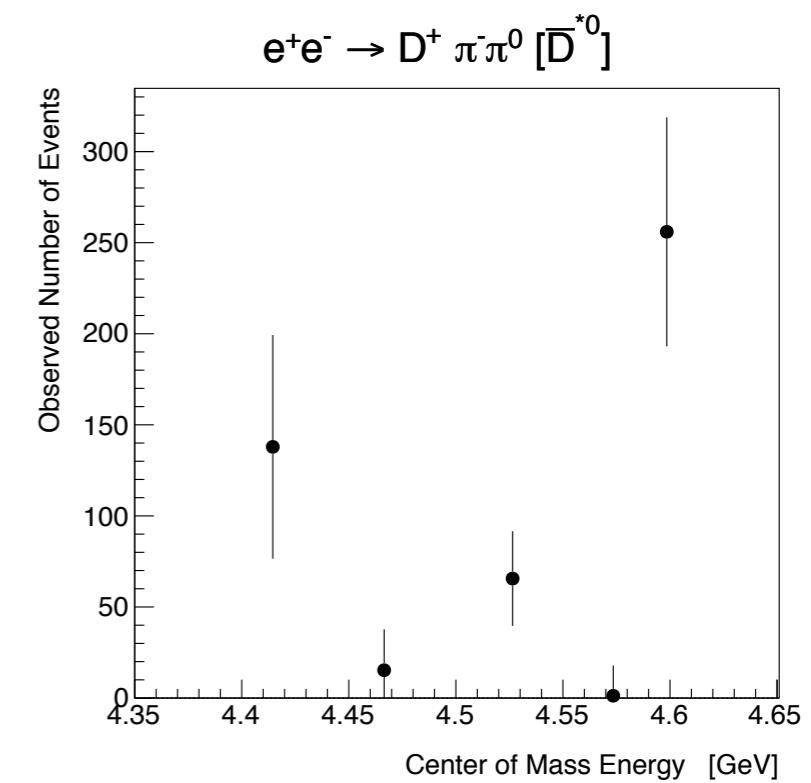
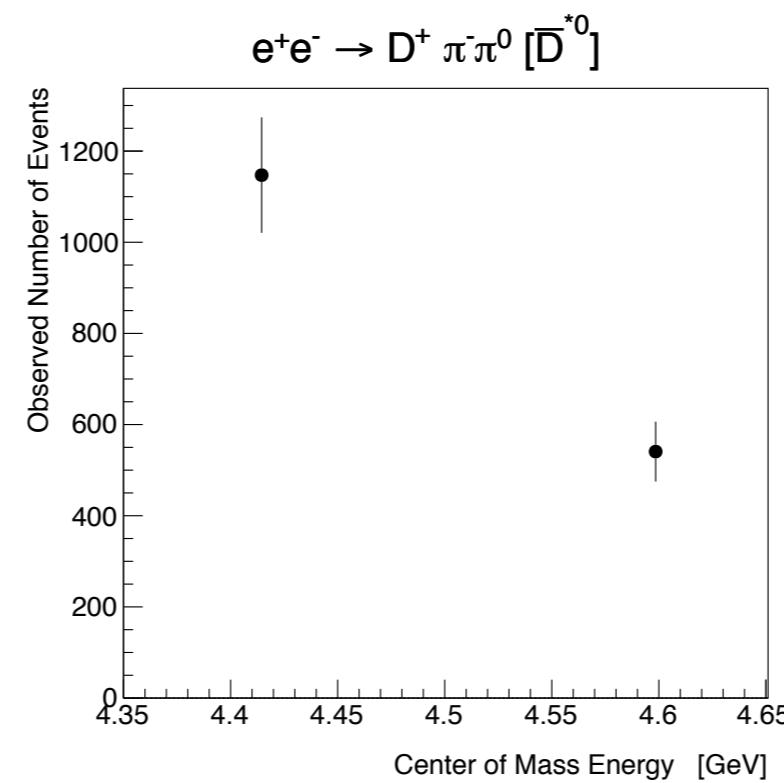
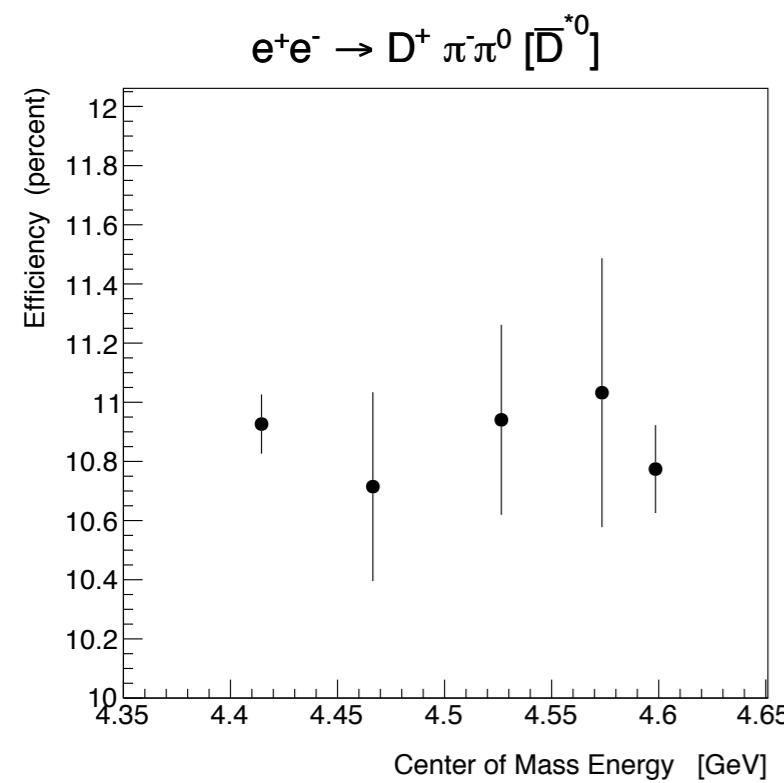
Veto  
 $D^{*+} \rightarrow \pi^0 D^+$   
 to get the  
 size of the  
 signal.



(these plots don't include c.c.)

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0 D^+\bar{D}^{*0}$

- \* Find the efficiency and number of observed events from the fits.



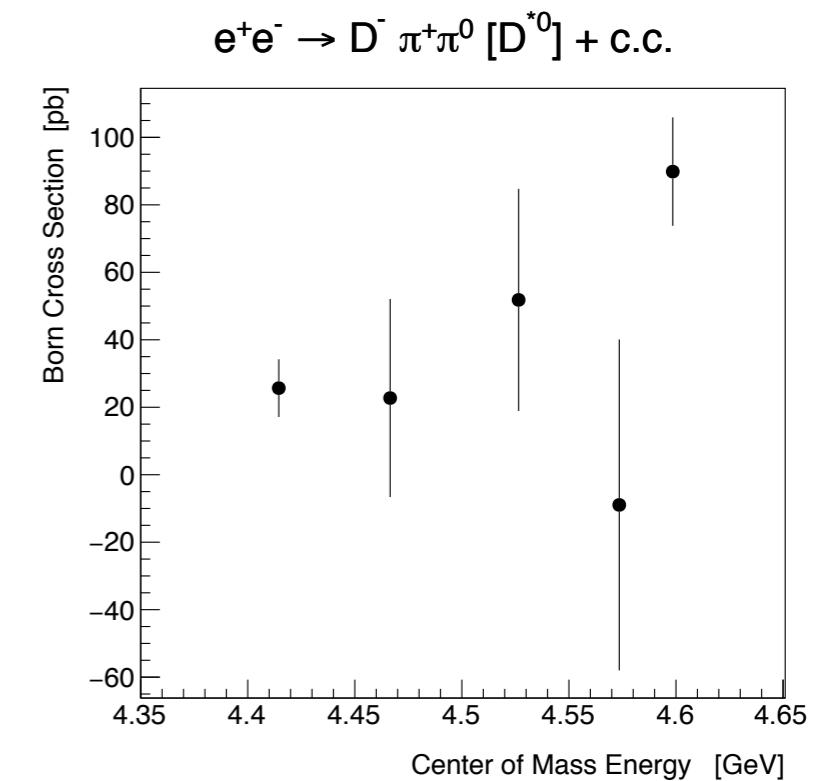
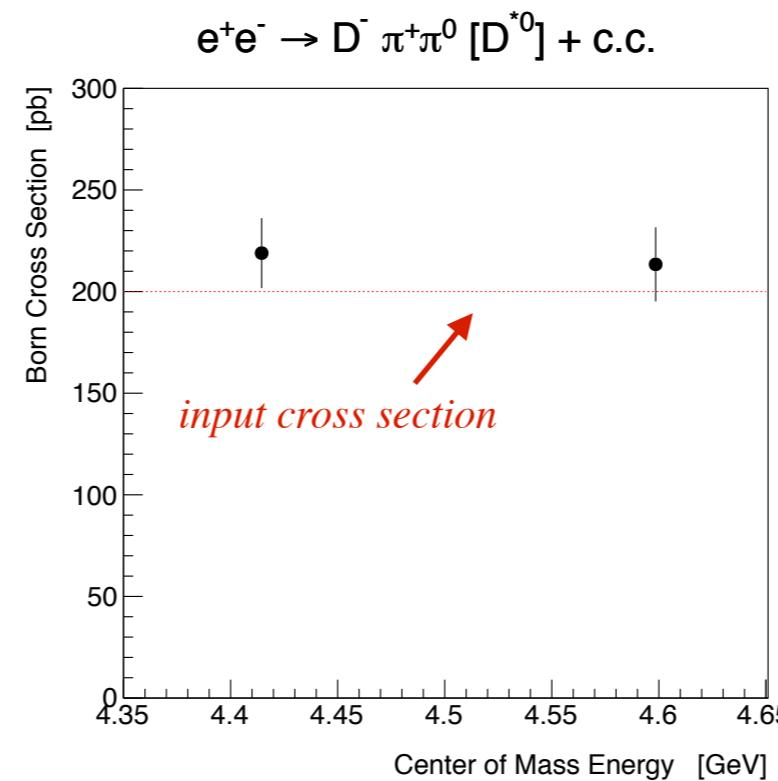
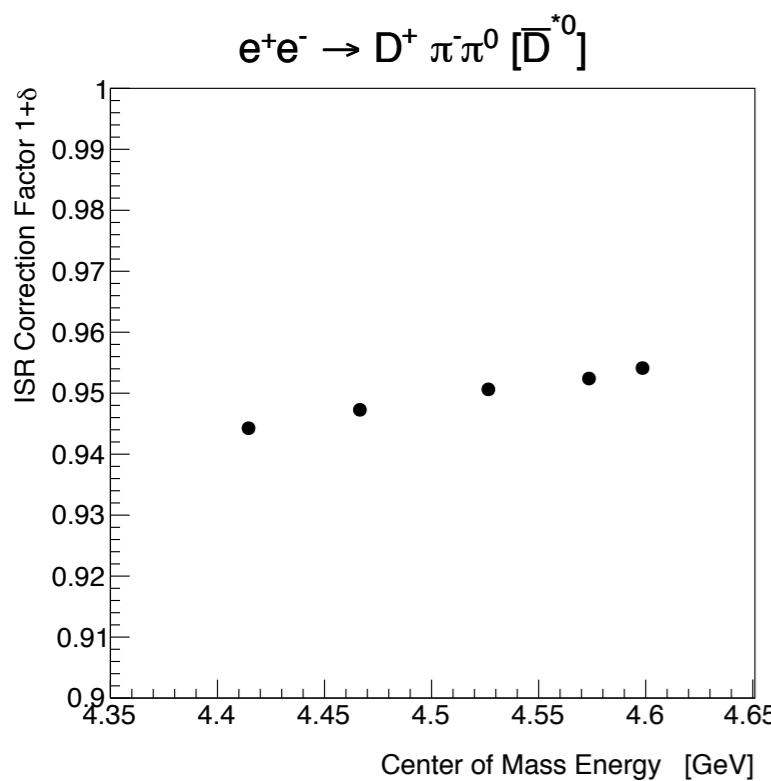
**SIGNAL MC**  
*(assuming flat cross section  
for ISR calculation)*  
  
*(these plots don't include c.c.)*

**INCLUSIVE MC**

**DATA**

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0 D^+\bar{D}^{*0}$

- \* Get the ISR correction factor from SIGNAL MC.
- \* Divide INCLUSIVE MC and DATA by the efficiency, luminosity, D branching fraction, and ISR correction factor to get the Born Cross Section. Add charge conjugate channels.

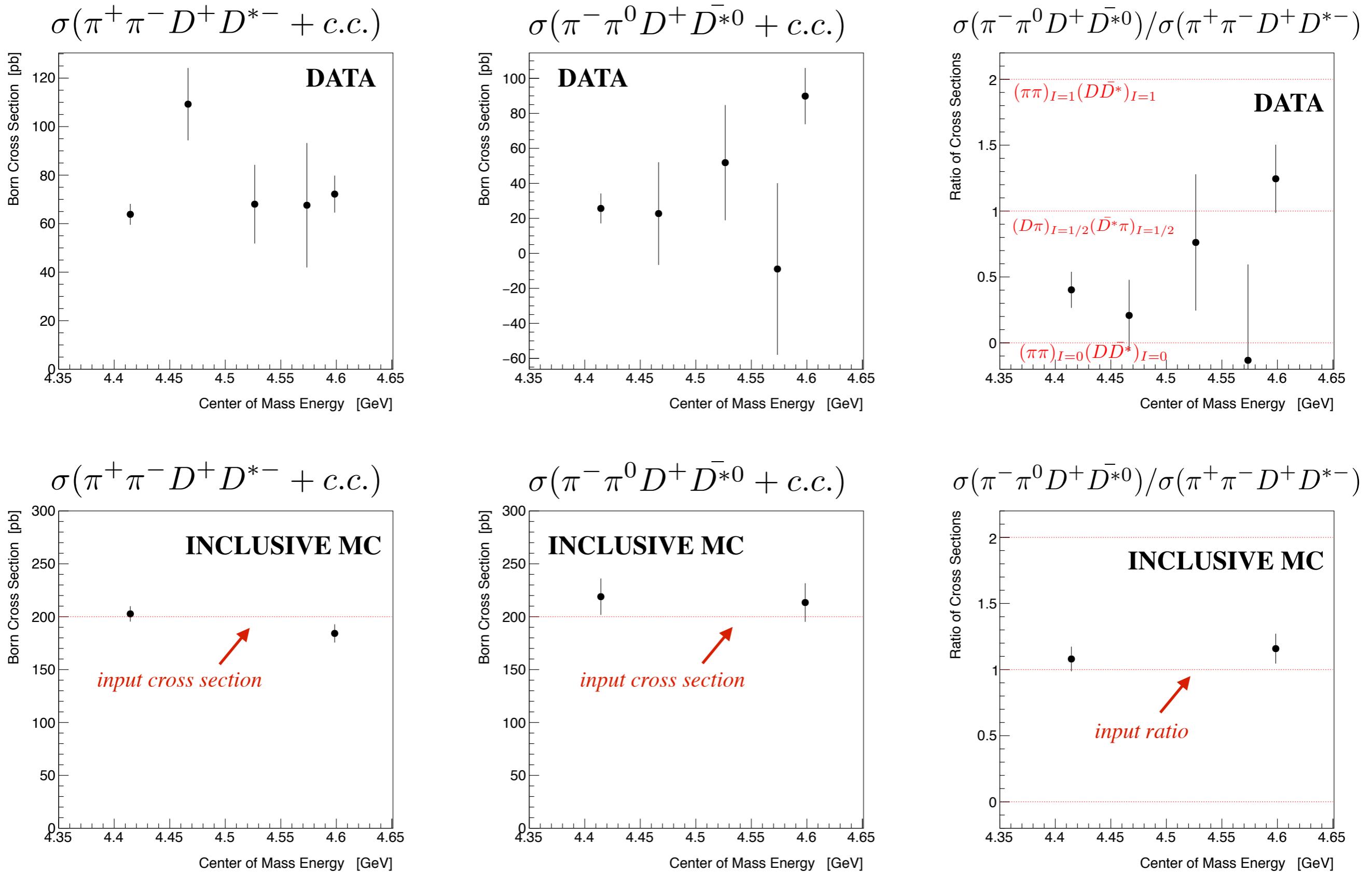


**SIGNAL MC**  
*(assuming flat cross section  
for ISR calculation;  
threshold = 4.2 GeV)*

**INCLUSIVE MC**

**DATA**

### III. Compare to $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$



# Strategy

I. Measure the  $e^+e^- \rightarrow \pi^+\pi^-D^+D^{*-}$  cross section.

The cross section is  $\sim 60$  pb, consistent with  $\pi^+\pi^-\psi(1S,2S)$  and  $\pi^+\pi^-h_c(2P)$ .

*Systematic Errors: luminosity; tracking; fitting; ISR.*

II. Search for  $\pi^+\pi^-h_c(2P)$  with  $h_c(2P) \rightarrow D^+D^{*-}$ .

Including an  $h_c(2P)$  signal describes data better than pure phase space and  $D_1D^*$ .

*The statistical significance calculation requires more thought.*

The mass and width are consistent with theoretical expectations.

*Systematic Errors: fitting; mass calibration.*

III. Compare to  $e^+e^- \rightarrow \pi^-\pi^0D^+\bar{D}^{*0}$ .

The cross section ratio appears to be consistent with predominantly isospin-0  $DD^*$  at 4420 MeV and a smaller fraction of isospin-0 at 4600 MeV.

*Systematic Errors: luminosity; tracking; fitting;  $\pi D^*D^*$  model; ISR.*

The  $h_c(2P)$  is suggestive! We are also exploring an alternate method. What else can we do??

# Backup: Background Channels (I)

1. $\pi^+ \pi^- D^+ D^{*-}$	1a. $\pi^+ \pi^- D^+(\pi^0 D^-)$	2a
	1b. $\pi^+ \pi^- D^+(\pi^- D^0)$	
2. $\pi^+ \pi^- D^- D^{*+}$	2a. $\pi^+ \pi^- D^-(\pi^0 D^+)$	1a
	2b. $\pi^+ \pi^- D^-(\pi^+ D^0)$	
3. $\pi^+ \pi^- D^0 D^{*0}$	3a. $\pi^+ \pi^- D^0(\pi^0 D^0)$	2b 4a 4b 6b 8b 13b 13d 14b 14d 15d
	3b. $\pi^+ \pi^- D^0(\gamma D^0)$	
4. $\pi^+ \pi^- \bar{D}^0 D^{*0}$	4a. $\pi^+ \pi^- \bar{D}^0(\pi^0 D^0)$	1b 3a 3b 6b 8b 13b 13d 14b 14d 15d
	4b. $\pi^+ \pi^- D^0(\gamma D^0)$	
5. $\pi^+ \pi^0 D^- D^{*0}$	5a. $\pi^+ \pi^0 D^-(\pi^0 D^0)$	1a 2a 6a 10b 13a 13c 15b
	5b. $\pi^+ \pi^0 D^-(\gamma D^0)$	
6. $\pi^+ \pi^0 D^0 D^{*-}$	6a. $\pi^+ \pi^0 D^0(\pi^0 D^-)$	3a 4a 5a 5b 8b 10b 13a 13b 13c 14b 15b 15d
	6b. $\pi^+ \pi^0 D^0(\pi^- D^0)$	
7. $\pi^- \pi^0 D^+ D^{*0}$	7a. $\pi^- \pi^0 D^+(\pi^0 D^0)$	1a 2a 8a 9b 14a 14c 15c
	7b. $\pi^- \pi^0 D^+(\gamma D^0)$	
8. $\pi^- \pi^0 \bar{D}^0 D^{*+}$	8a. $\pi^- \pi^0 \bar{D}^0(\pi^0 D^+)$	3a 4a 6b 7a 7b 9b 13b 14a 14b 14c 15c 15d
	8b. $\pi^- \pi^0 D^0(\pi^+ D^0)$	
9. $\pi^0 \pi^0 D^+ D^{*-}$	9a. $\pi^0 \pi^0 D^+(\pi^0 D^-)$	7a 8a 10a 14a 15a 15c
	9b. $\pi^0 \pi^0 D^+(\pi^- D^0)$	
10. $\pi^0 \pi^0 D^- D^{*+}$	10a. $\pi^0 \pi^0 D^-(\pi^0 D^+)$	5a 6a 9a 13a 15a 15b
	10b. $\pi^0 \pi^0 D^-(\pi^+ D^0)$	
11. $\pi^0 \pi^0 D^0 D^{*0}$	11a. $\pi^0 \pi^0 D^0(\pi^0 D^0)$	5a 6a 10b 12a 12b 13a 15b 16a 16b 16c
	11b. $\pi^0 \pi^0 D^0(\gamma D^0)$	
12. $\pi^0 \pi^0 D^0 D^{*0}$	12a. $\pi^0 \pi^0 D^0(\pi^0 D^0)$	7a 8a 9b 11a 11b 14a 15c 16a 16b 16c
	12b. $\pi^0 \pi^0 D^0(\gamma D^0)$	

# Backup: Background Channels (II)

13. $\pi^+ D^{*-} D^{*0}$	13a. $\pi^+(\pi^0 D^-)(\pi^0 D^0)$	
	13b. $\pi^+(\pi^- D^0)(\pi^0 D^0)$	
	13c. $\pi^+(\pi^0 D^-)(\gamma D^0)$	
	13d. $\pi^+(\pi^- D^0)(\gamma D^0)$	
14. $\pi^- D^{*+} D^{*0}$	14a. $\pi^-(\pi^0 D^+)(\pi^0 D^0)$	
	14b. $\pi^-(\pi^+ D^0)(\pi^0 D^0)$	
	14c. $\pi^-(\pi^0 D^+)(\gamma D^0)$	
	14d. $\pi^-(\pi^+ D^0)(\gamma D^0)$	
15. $\pi^0 D^{*+} D^{*-}$	15a. $\pi^0(\pi^0 D^+)(\pi^0 D^-)$	
	15b. $\pi^0(\pi^+ D^0)(\pi^0 D^-)$	
	15c. $\pi^0(\pi^0 D^+)(\pi^- D^0)$	
	15d. $\pi^0(\pi^+ D^0)(\pi^- D^0)$	
16. $\pi^0 D^{*0} D^{*0}$	16a. $\pi^0(\pi^0 D^0)(\pi^0 D^0)$	
	16b. $\pi^0(\gamma D^0)(\pi^0 D^0)$	
	16c. $\pi^0(\pi^0 D^0)(\gamma D^0)$	
	16d. $\pi^0(\gamma D^0)(\gamma D^0)$	