

Status of Measurement of R Value at BESIII

Wenbiao Yan

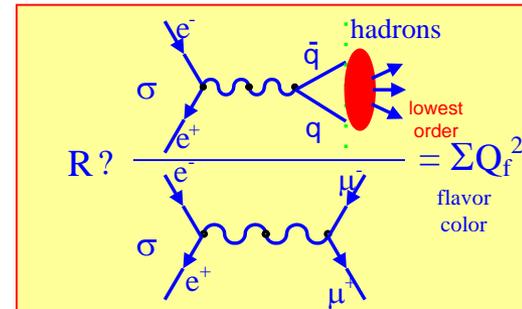
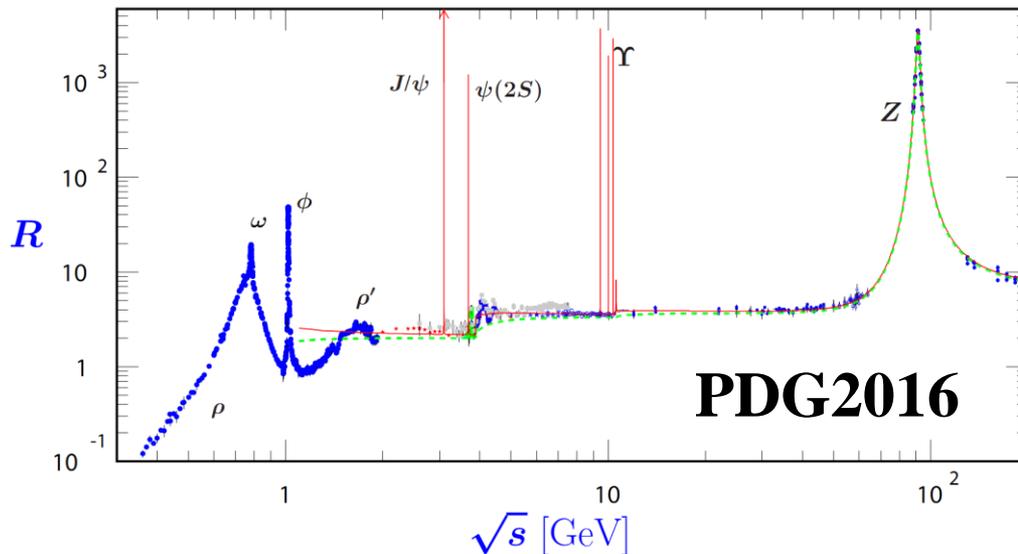
On behalf of BESIII Collaboration



R value

- The Born cross section of e^+e^- annihilation into hadrons normalized by theoretical $\mu^+\mu^-$ cross section

$$R = \frac{\sigma_{had}^0(e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons})}{\sigma_{\mu\mu}^0(e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-)}$$



- Precision !!!

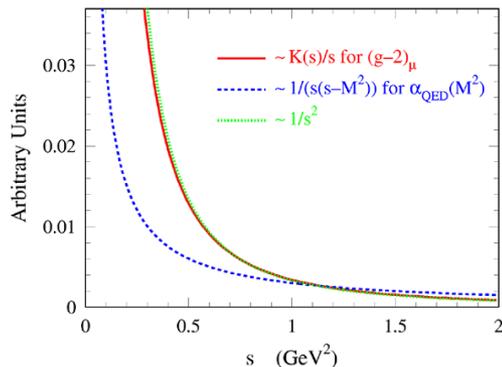
Muon magnetic moment $(g-2)_\mu$

- The Standard Model prediction for muon $a_\mu = (g_\mu - 2)/2$

$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{had,LO}} + a_\mu^{\text{had,HO}} + a_\mu^{\text{had,LBL}} + a_\mu^{\text{weak}}$$

$$a_\mu^{\text{Had}}[\text{LO}] = \frac{1}{3} \left(\frac{\alpha}{\pi} \right)^2 \int_{m_\pi^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

K(s): analytically known



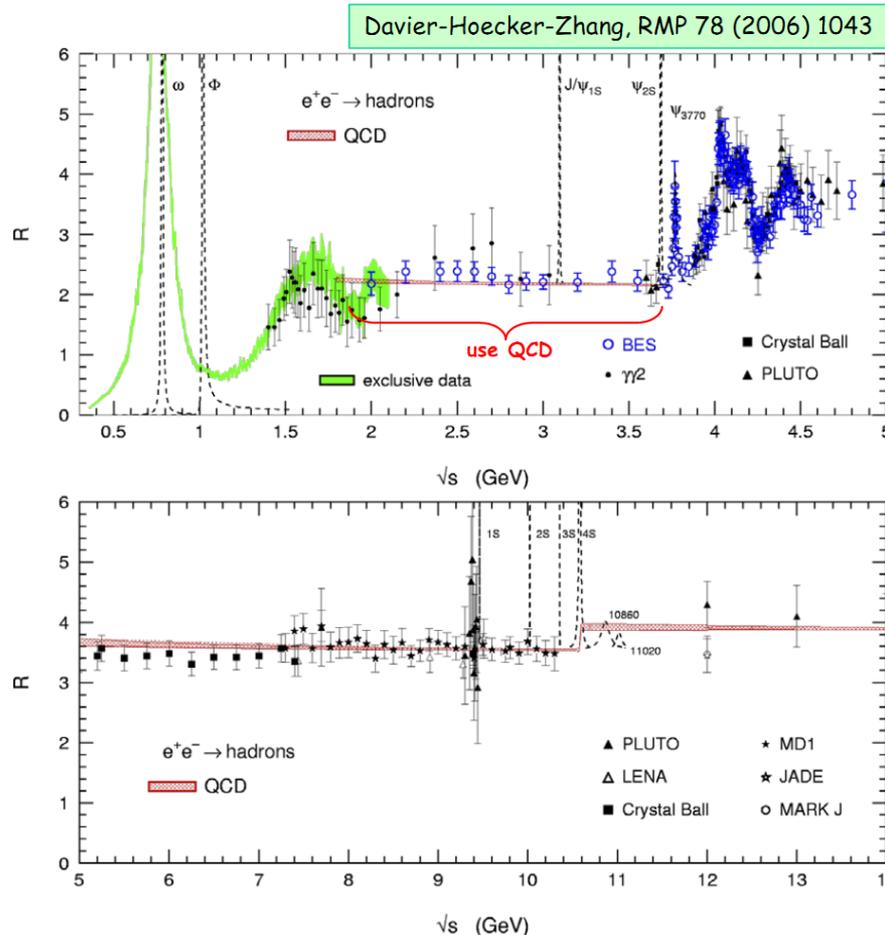
Prof. Michel Davier @ **Tau2016**

QED	11658471.885	+ - 0.004
EW	15.4	+ - 0.1
had LBL	10.5	+ - 2.6
had LO	692.8	+ - 3.3
had NLO	-9.87	+ - 0.09
had NNLO	1.24	+ - 0.01

prediction	11659181.9	+ - 4.2
exp BNL	11659208.9	+ - 6.3

Muon magnetic moment $(g-2)_\mu$

Prof. Michel Davier at Tau2016



- $[\pi^0\gamma-1.8\text{GeV}]$
 - sum about 22 \rightarrow 37 exclusive channels
 - estimate unmeasured channels using isospin relations

- $[1.8-3.7] \text{ GeV}$
 - good agreement between data and pQCD calculation; previous extensive QCD tests with τ data
 - \rightarrow use 4-loop pQCD
 - $J/\psi, \psi(2S)$: Breit-Wigner integrals

- $[3.7-5] \text{ GeV}$
 - charm particle thresholds
 - \rightarrow use data

- $>5\text{GeV}$
 - use 4-loop pQCD calculation

● BESIII: ISR and energy scan

EM fine structure constant

- The running of the electromagnetic fine structure constant is governed by the renormalized vacuum polarization function.

$$\alpha(s) = \frac{\alpha(0)}{1 - \Delta\alpha_{lep}(s) - \Delta\alpha_{top}(s) - \Delta\alpha_{had}^5(s)}$$

$$\Delta\alpha_{lep}(M_Z^2) = 0.03142$$

$$\Delta\alpha_{top}(M_Z^2) = 0.00007(1)$$

$$\Delta\alpha_{had}^5(M_Z^2) = 0.0280 \pm 0.0009$$

$$\Delta\alpha_{had}^5(M_Z^2) = -\frac{\alpha(0)M_Z^2}{3\pi} \operatorname{Re} \int_{4m_\pi^2}^{\infty} ds \frac{R(s)}{s(s - M_Z^2) - i\epsilon}$$

R value @ pQCD and charmonium

- Test pQCD prediction on R values

$$R = 3 \sum_f Q_f^2 \left[1 + \left(\frac{\alpha_s(s)}{\pi} \right) + 1.411 \left(\frac{\alpha_s(s)}{\pi} \right)^2 - 12.8 \left(\frac{\alpha_s(s)}{\pi} \right)^3 + \dots \right]$$

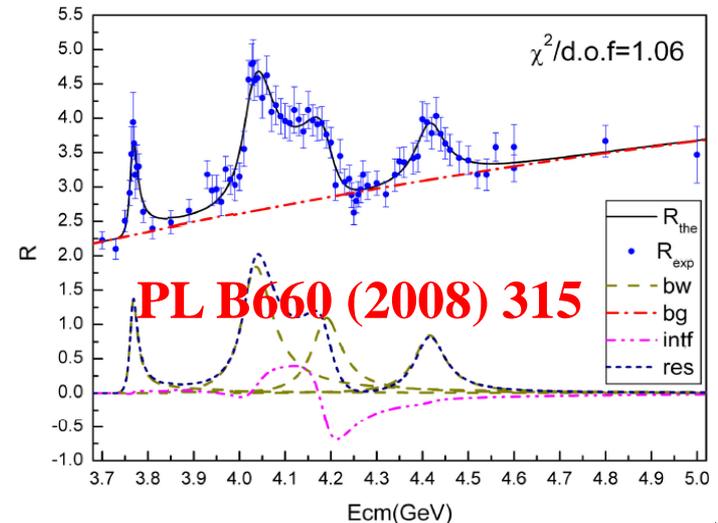
- Fitting to R values: resonance parameters of $\Psi(3770)$, $\Psi(4040)$, $\Psi(4160)$ and $\Psi(4410)$.

$\psi(4040)$	$I^{G(J^{PC})} = 0^-(1^{--})$
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$\psi(4040)$ MASS

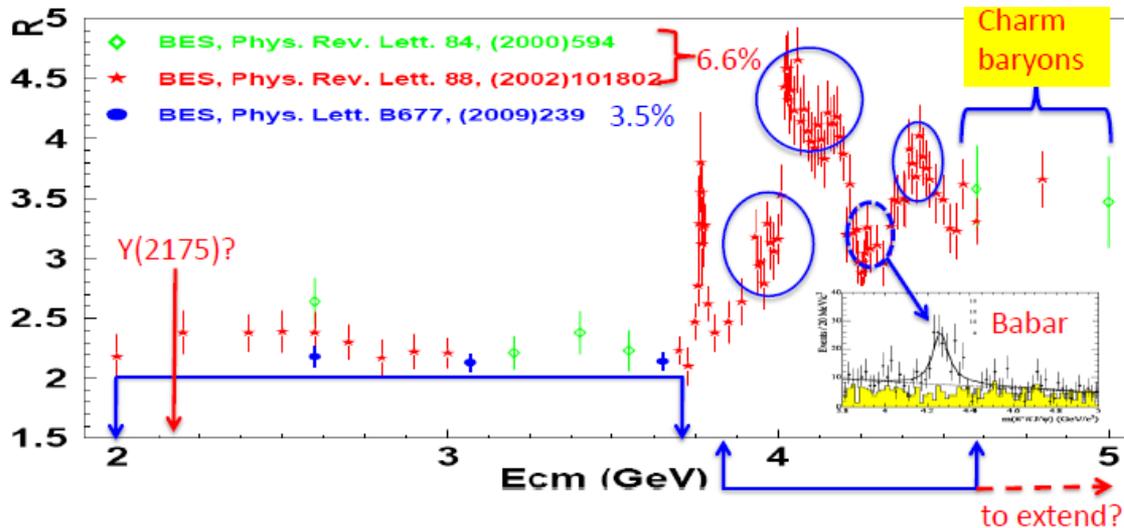
VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
4039 ± 1 OUR ESTIMATE			
4039.6 ± 4.3	1 ABLIKIM	08D BES2	$e^+e^- \rightarrow$ hadrons

4034 ± 6	2 MO	10 RVUE	$e^+e^- \rightarrow$ hadrons
4037 ± 2	3 SETH	05A RVUE	$e^+e^- \rightarrow$ hadrons
4040 ± 1	4 SETH	05A RVUE	$e^+e^- \rightarrow$ hadrons
4040 ± 10	BRANDELIK	78C DASP	e^+e^-



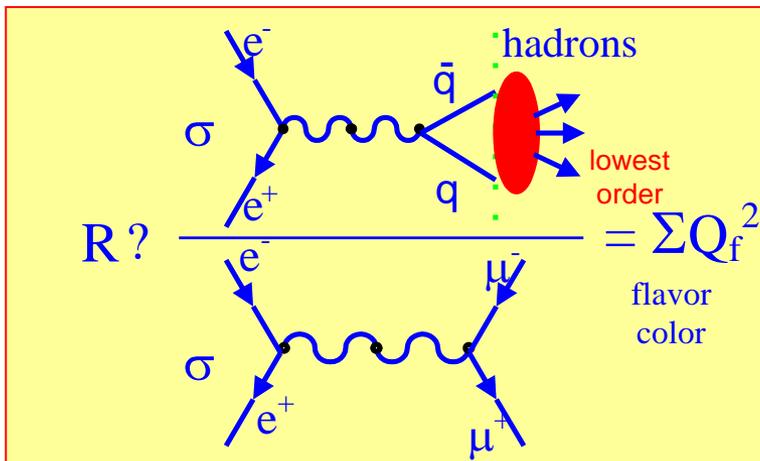
Data sets for R value

- Phase I: test run @ 2012
 - ✓ $E_{cm} = 2.232/2.400/2.800/3.400$ GeV, $\sim 12\text{pb}^{-1}$
- Phase II: fine scan for heavy charm resonant @ 2013-2014
 - ✓ $E_{cm} \in [3.800, 4.590]$ GeV, 104 energy points, $\sim 800\text{pb}^{-1}$
- Phase III: R & QCD scan @ 2015
 - ✓ $E_{cm} \in [2.000, 3.080]$ GeV, 21 energy points, $\sim 500\text{pb}^{-1}$



R value

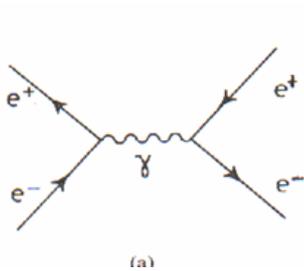
- R values are measured as



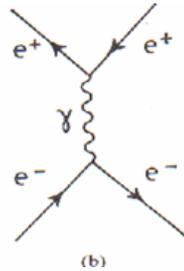
- L** integrated luminosity
- $1+\delta$** radiative correction factor
- N_{had}** observed hadronic events
- N_{bg}** from background events
- ϵ_{had}** selection efficiency
- $\sigma_{\mu\mu}$** Born cross section of μ pair production in QED

$$R = \frac{1}{\sigma_{\mu^+\mu^-}} \cdot \frac{N_{\text{had}} - N_{\text{bg}}}{L \cdot \epsilon_{\text{had}} \cdot (1 + \delta)}$$

Generators @ R analysis

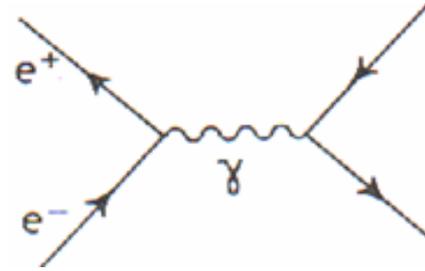


$e^+e^- \rightarrow (\gamma)e^+e^-$: **Babayaga**

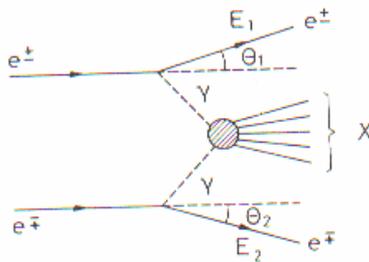


$e^+e^- \rightarrow (\gamma)\mu^+\mu^-$: **Babayaga**

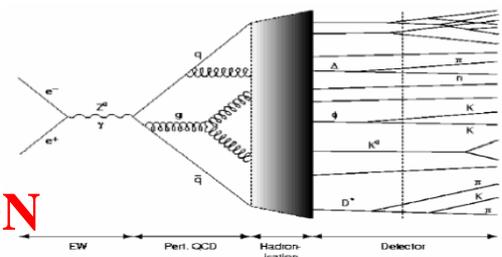
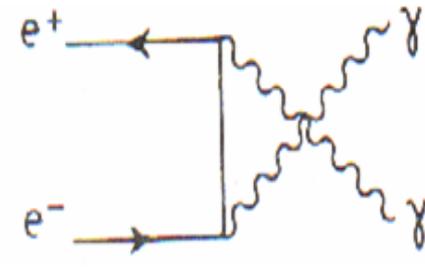
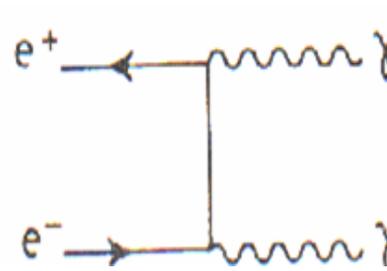
$e^+e^- \rightarrow (\gamma)\tau^+\tau^-$: **KKMC**



$e^+e^- \rightarrow (\gamma)\gamma\gamma$: **Babayaga**



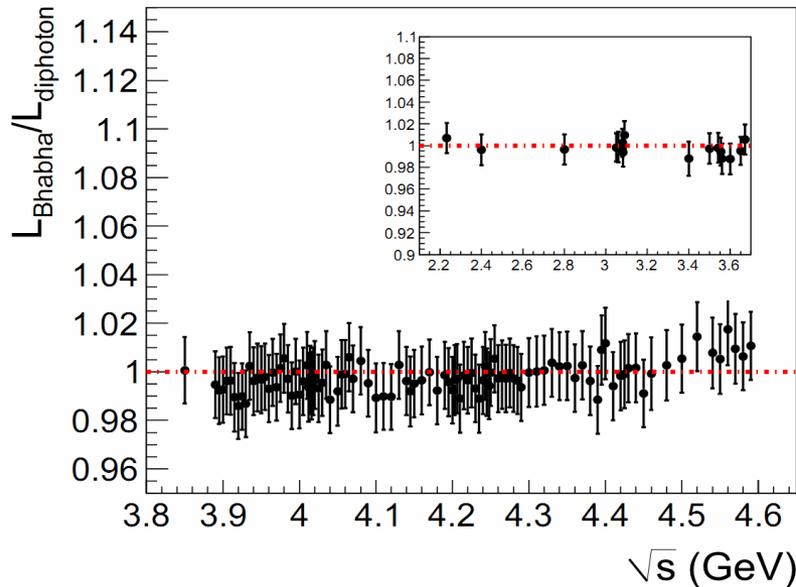
$e^+e^- \rightarrow e^+e^-X$: **TWOPHOTON**



$e^+e^- \rightarrow \text{hadrons}$:
ConExc & LUARLW

Luminosity

- Large-angle Bhabha $e^+e^- \rightarrow (\gamma)e^+e^-$ and diphoton $e^+e^- \rightarrow (\gamma)\gamma\gamma$:
about 0.8% uncertainty

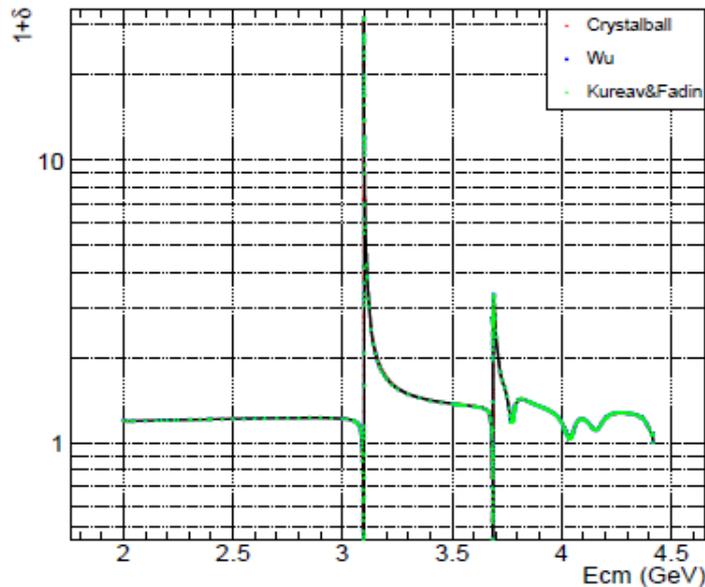


\sqrt{s}/GeV	$e^+e^- \rightarrow (\gamma)e^+e^-/\text{pb}^{-1}$	$e^+e^- \rightarrow (\gamma)\gamma\gamma/\text{pb}^{-1}$
2.2324	$2.645 \pm 0.006 \pm 0.020$	$2.627 \pm 0.009 \pm 0.028$
2.4000	$3.415 \pm 0.007 \pm 0.024$	$3.428 \pm 0.011 \pm 0.040$
2.8000	$3.753 \pm 0.008 \pm 0.026$	$3.766 \pm 0.014 \pm 0.042$
3.0500	$14.893 \pm 0.030 \pm 0.103$	$14.919 \pm 0.029 \pm 0.158$
3.0600	$15.040 \pm 0.030 \pm 0.131$	$15.060 \pm 0.029 \pm 0.158$
3.0800	$31.019 \pm 0.060 \pm 0.189$	$30.942 \pm 0.044 \pm 0.338$
3.0830	$4.740 \pm 0.011 \pm 0.029$	$4.769 \pm 0.017 \pm 0.052$
3.0900	$15.709 \pm 0.031 \pm 0.099$	$15.558 \pm 0.030 \pm 0.162$
3.0930	—	$14.910 \pm 0.030 \pm 0.157$
3.0943	—	$2.143 \pm 0.011 \pm 0.023$
3.0952	—	$1.816 \pm 0.010 \pm 0.019$
3.0958	—	$2.135 \pm 0.011 \pm 0.023$
3.0969	—	$2.069 \pm 0.011 \pm 0.024$
3.0982	—	$2.203 \pm 0.011 \pm 0.023$
3.0990	—	$0.756 \pm 0.007 \pm 0.008$

- Chinese Physics C41 (2017) 063001

Radiative correction factor ($1+\delta$)

- The Feynman diagrams scheme (CB) and structure function schemes (KF & WU) are used, results by there methods are consistent within **1.2%**.

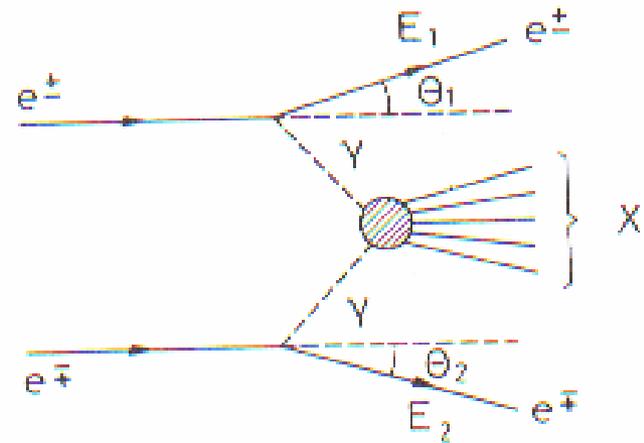


- **R value @ PDG2016 as input**

$$e^+e^- \rightarrow e^+e^- + X$$

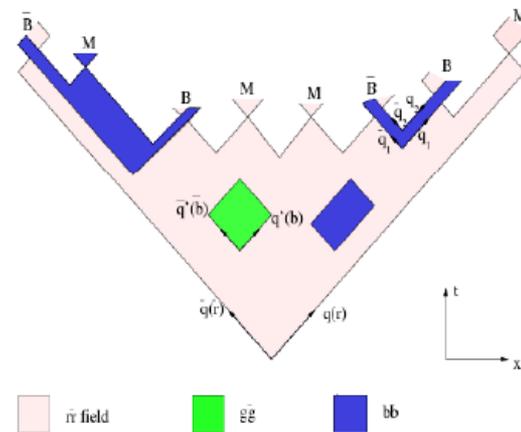
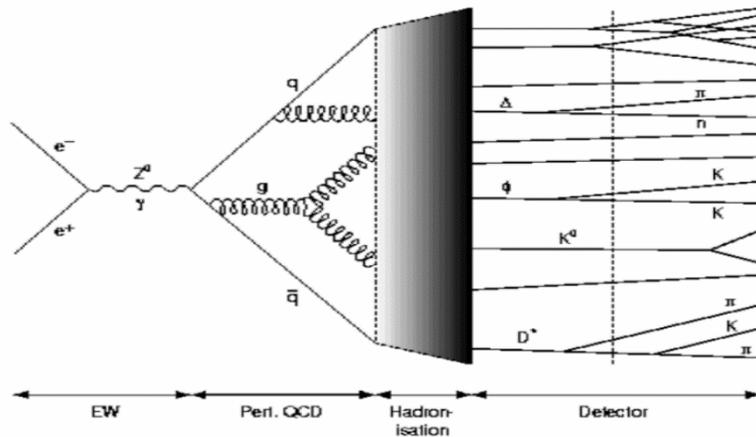
Measured quantity or reaction	Studied physical object or investigated problem	The $ee \rightarrow eeh$ cross section (cm ²) to be measured (at $\sqrt{s} \sim 5 - 10$ GeV)
$\gamma\gamma \rightarrow \pi^+\pi^-$ $\pi^0\pi^0$	Threshold theorems, Born term	10^{-33}
	PCAC, current algebra	$10^{-35} - 10^{-36}$
	Two-particle unitarity approximation (Range of validity)	$10^{-34} - 10^{-35}$
	The number of essential partial waves	
	$\pi\pi$ -phase and scattering lengths	$10^{-35} - 10^{-36}$
$\gamma\gamma \rightarrow K\bar{K}$	Going out of mass shell	$10^{-35} - 10^{-36}$
	The first Weinberg sum rule	$10^{-33} - 10^{-34}$
	f_1, S^*, ρ elasticity	
	Connection with the trace of energy-momentum tensor	
	FESR	
$\gamma\gamma \rightarrow n\pi; n > 2$	PCAC, chiral Lagrangians	$10^{-36} - 10^{-37}$
$\gamma\gamma \rightarrow \pi^0(\eta)$	π^0 -lifetime Triangle anomaly, q^2 -dependence	10^{-33}
$\gamma\gamma \rightarrow R$ (resonance)	Resonance parameters (ϵ, f, A_s , etc.)	$10^{-33} - 10^{-35}$
	Spin of X^0, E	$10^{-33} - 10^{-34}$
	FESR, symmetries	$\lesssim 10^{-35}$
	Parameters of A_1 , etc	

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- Background from two photon process
 - ✓ Underestimation by BesTwoGam MC
 - ✓ Use generator for (dominant) exclusive processes: $e^+e^-e^+e^-$; $e^+e^-\mu^+\mu^-$; $e^+e^-\pi^+\pi^-$; $e^+e^-K^+K^-$; $e^+e^-\eta$ and $e^+e^-\eta'$
- Other process: unclear but tiny

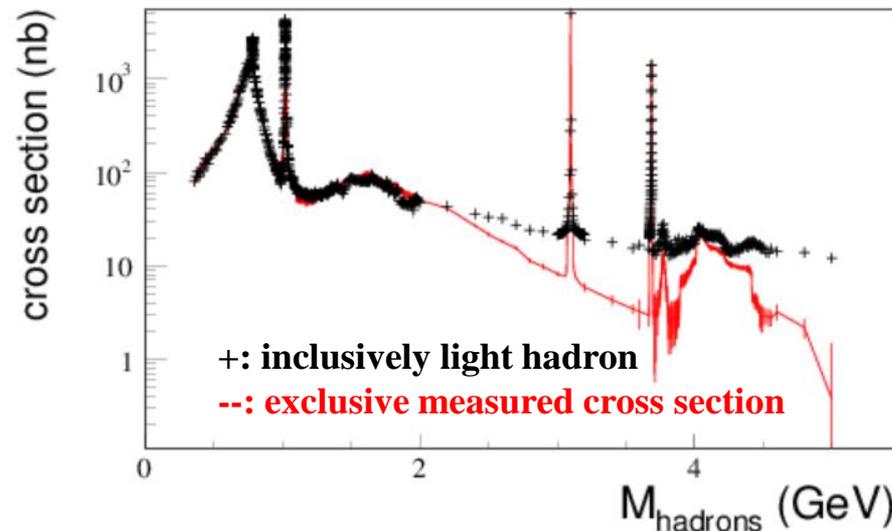
MC generator for $e^+e^- \rightarrow \text{hadrons}$



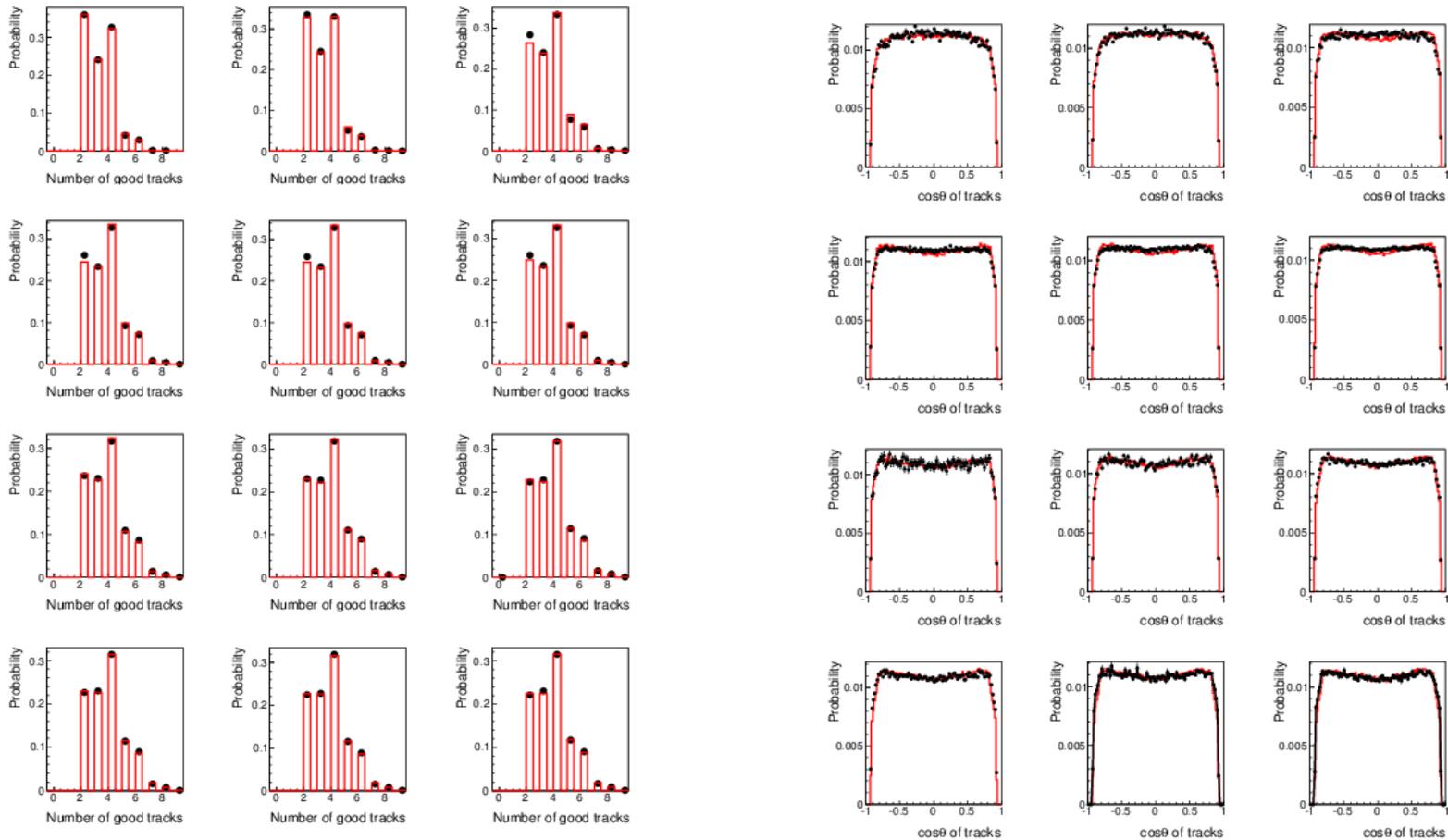
- **High energy e^+e^- collision: Herwig @ Cluster model; Jetset and Pythia @ String model**
- **Low energy e^+e^- collision: LUND Area Law, [hep-ph/9910285](https://arxiv.org/abs/hep-ph/9910285)**
 - ✓ **Simulate ISR inclusive continuous channels and $J^{PC}=1^-$ resonance between 2GeV and 5GeV. Need MC tuning**
 - ✓ **Left-right symmetry, NO**

MC generator for $e^+e^- \rightarrow \text{hadrons}$

- LUARLW: 100% by LUARLW
- ConExc generator:
 - ✓ ConExc + Phokhara + LUARLW
 - ✓ Phokhara deal with 10 exclusive processes
 - ✓ Others measured processes with ConExc
 - ✓ unknown by LUNDARLW

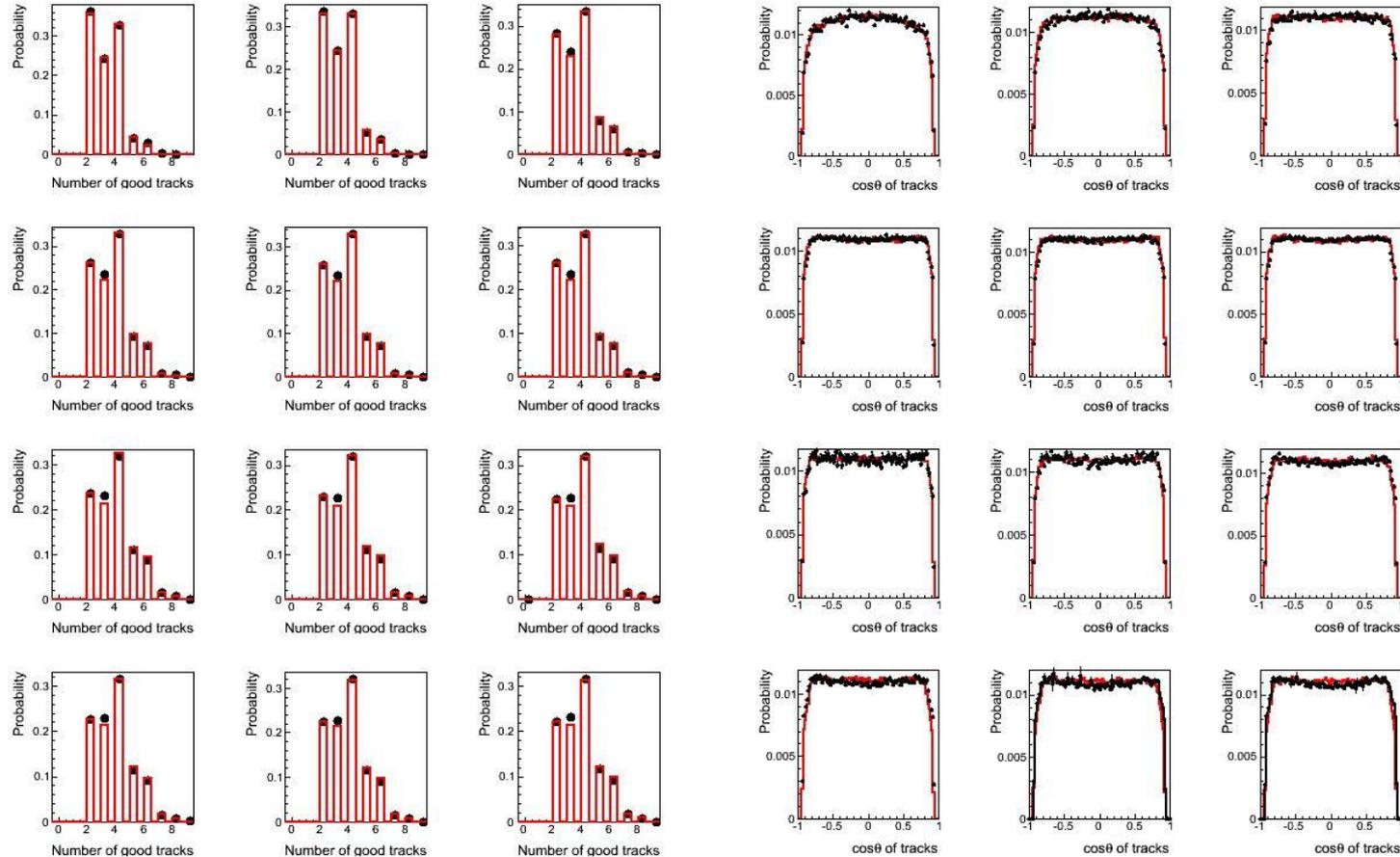


ConExc @ [2.232, 3.671]GeV



● ConExc could describe experimental data

LUARLW @ [2.232, 3.671] GeV



● LUARLW could describe experimental data

Status of R Measurement

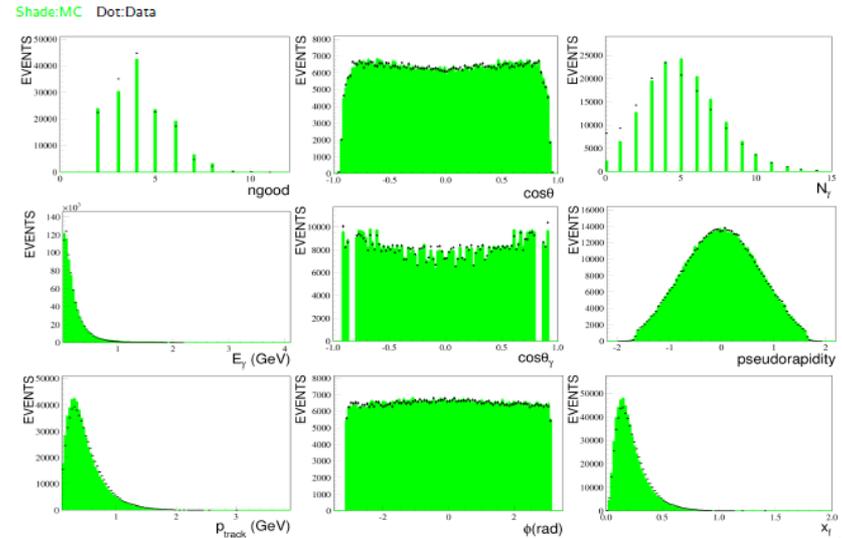
- BESIII memo at Convener's review

BESIII Analysis Memo

BAM-00XXX

June 13, 2017

The Measurements of R in e^+e^- Annihilation at Center-of-Mass Energy from 2.2324 to 3.6710 GeV at BESIII



- MC tuning at [3.800, 4.590]GeV

4.26GeV

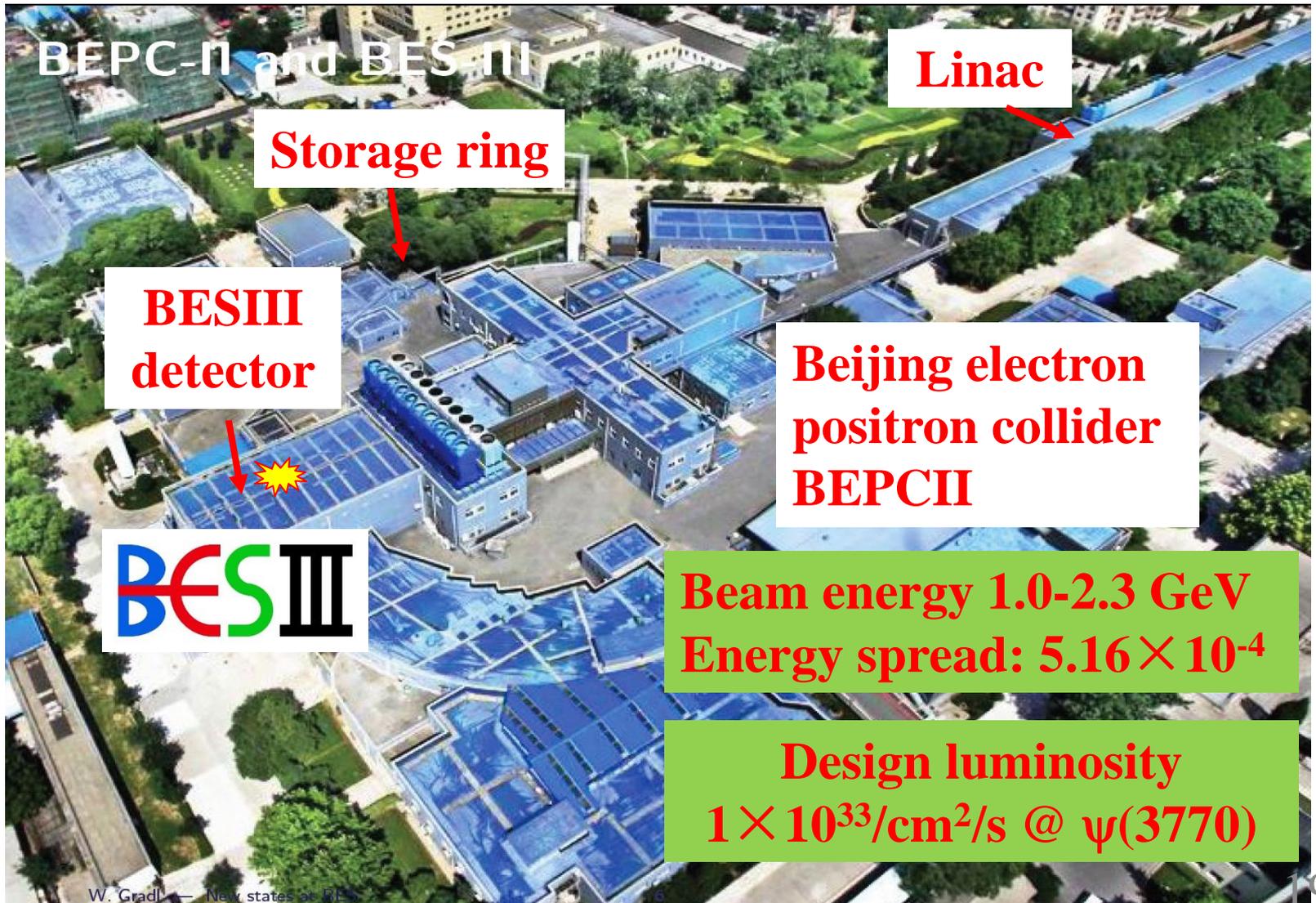
$$e^+e^- \Rightarrow \gamma^* \Rightarrow \begin{cases} \psi(4040) \Rightarrow D\bar{D}, D^*\bar{D}^*, D\bar{D}^*, \bar{D}D^*, D_s\bar{D}_s; \\ \psi(4160) \Rightarrow D\bar{D}, D^*\bar{D}^*, D\bar{D}^*, \bar{D}D^*, D_s\bar{D}_s, D_s\bar{D}_s^*; \\ \psi(4415) \Rightarrow D\bar{D}, D^*\bar{D}^*, D\bar{D}^*, \bar{D}D^*, D_s\bar{D}_s, D_s\bar{D}_s^*, D_s^*\bar{D}_s^*. \end{cases}$$

$$e^+e^- \Rightarrow \gamma^* \Rightarrow X(4160), X(4260) \dots \quad \text{with } J^{PC} = 1^{--}$$

Summary

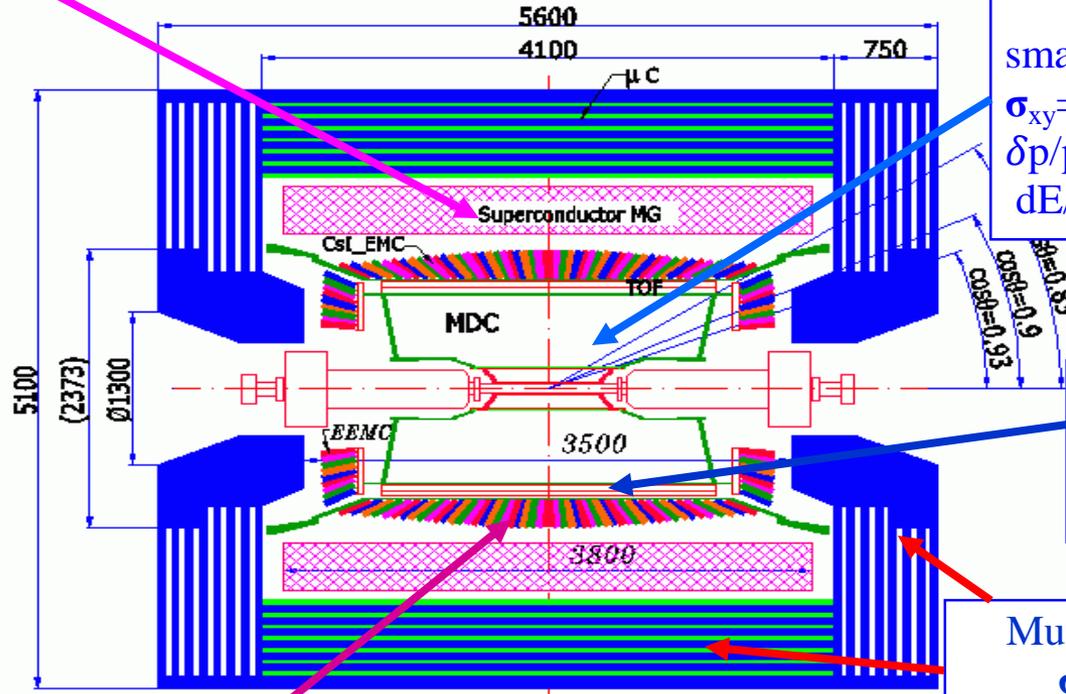
- **R values are important for $(g-2)_\mu$, $\alpha(M_Z)$, $\alpha_s(s)$, and test pQCD prediction, and resonance parameters of charmonium states**
- **BESIII have collected with R scan data @ [2.0, 4.6]GeV**
- **Data analysis @ [2.232, 3.671]GeV is finished**
 - ✓ **Integrated luminosity: about 0.8% uncertainty**
 - ✓ **Radiative correction factor ($1+\delta$): 1.2% uncertainty**
 - ✓ **MC generator: ConExc and LUARLW**
- **Data analysis @ [3.800, 4.590]GeV is in progress**

Bird's View of BEPCII & BESIII



BESIII Detector

Solenoid Magnet: 1 T Super conducting



**NIM A614
345 (2010)**

MDC
small cell & He gas
 $\sigma_{xy} = 130 \mu\text{m}$
 $\delta p/p = 0.5\% @ 1\text{GeV}$
 $dE/dx = 6\%$

TOF
 $\sigma_T = 90 \text{ ps}$ Barrel
110->80ps Endcap

Muon ID: 8~9 layer RPC
 $\sigma_{R\Phi} = 1.4 \text{ cm} \sim 1.7 \text{ cm}$

EMCAL: CsI crystal
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$
 $\sigma_{\phi,z} = 0.5 \sim 0.7 \text{ cm}/\sqrt{E}$

Data Acquisition:
Event rate = 3 kHz
Throughput ~ 50 MB/s

Trigger: Tracks & Showers
Pipelined; Latency = 6.4 μs

Hermetic spectrometer for neutral and charged particle with excellent resolution, PID, and large coverage