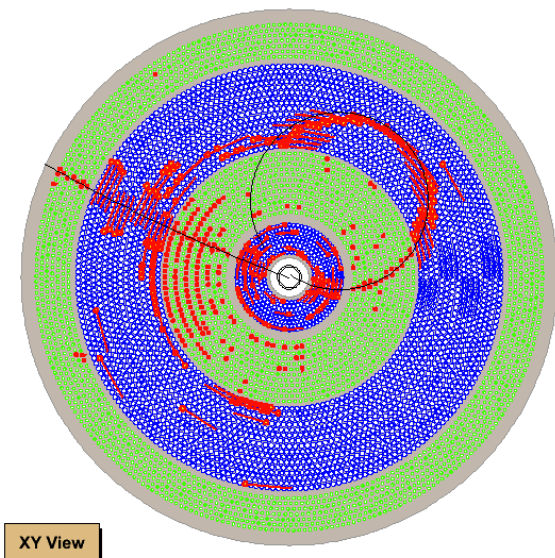


Hough Transform Based Track Finding for BESIII

Zhang Yao
June 5 2017

BESIII Drift Chamber (MDC)

- Design of MDC
 - **Axial** and **stereo** wires in grouped to super layers
 - Continuous axial/stereo layers
 - Big “gap” between axial & stereo layers
 - Max solid angle coverage is 0.93%
- MDC track finding algorithms
 - High pt tracks: Segment based finders
 - Curled tracks: Road hit searching method
- Requirement for a new tracking algorithm
 - Tracking efficiency can be improved for low Pt
 - Inner drift chamber will be replaced with a Cylindrical GEM detector

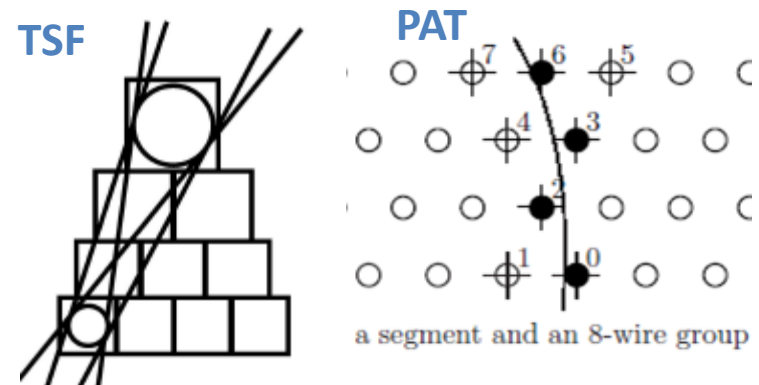
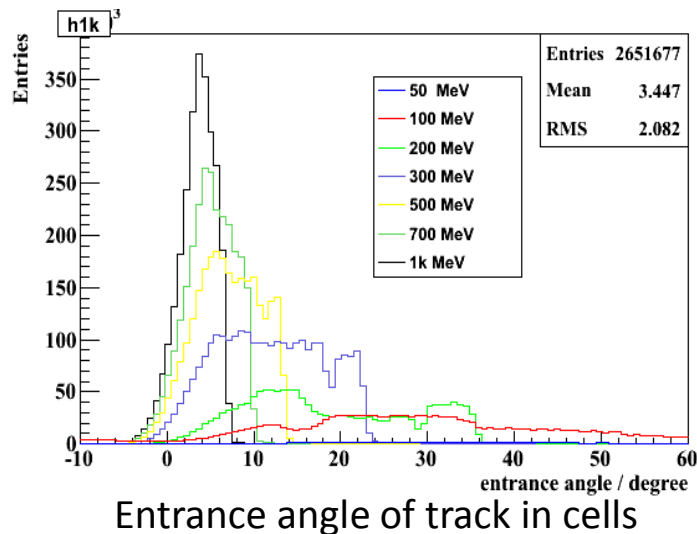


Why need a new tracking algorithm(1)

----Improve curling track efficiency

1. BESIII tracking Segment based finders :PAT & TSF

- Find **segment in super-layers** by template matching or hit searching in window area
- **group** segment to track



Track segment design in super layers

Angle coverage is limited by segment design

Sensitive to detector design, track Pt, hit inefficient and noise

Why need a new tracking algorithm(1)

----Improve curling track efficiency

2. Road method for curled track: CurlFinder

- **Select continuous hits** in same axial layer
- Pick up hits on road by hit neighbors
- **Effect by noise or background on the road**

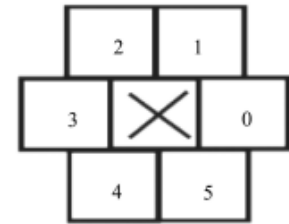
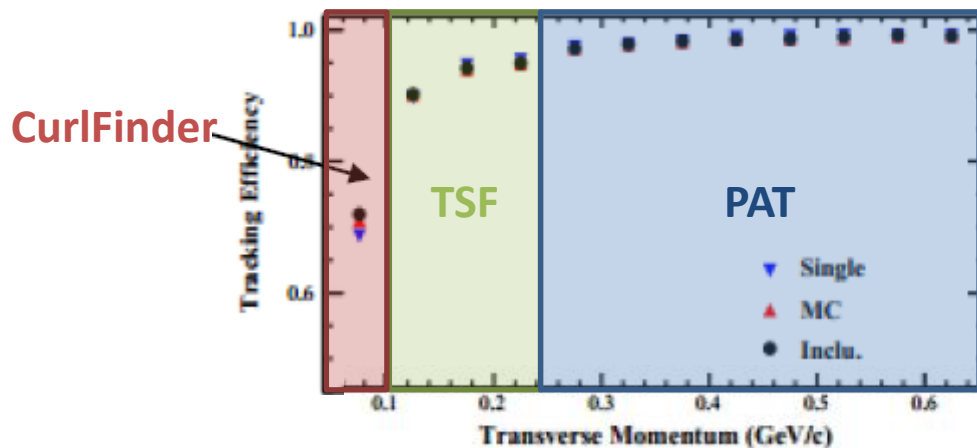


Fig. 2. The definition of neighbor: x represents one fired wire and 0-5 represent the sequentially numbered neighbor wires.



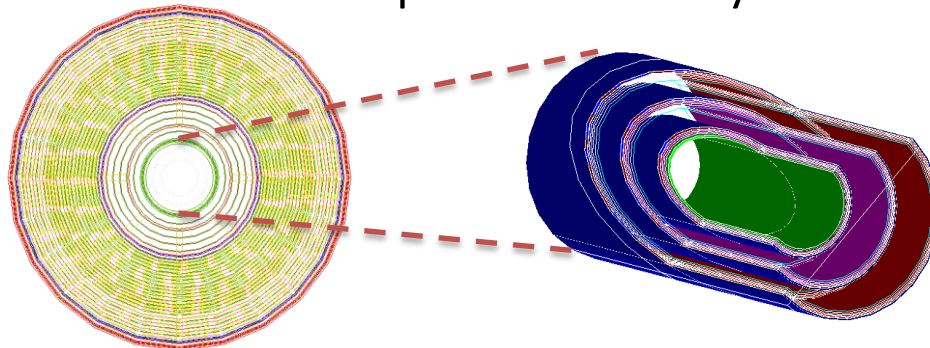
Tracking efficiency of π^- with P_T

Low p_T tracking can be improved

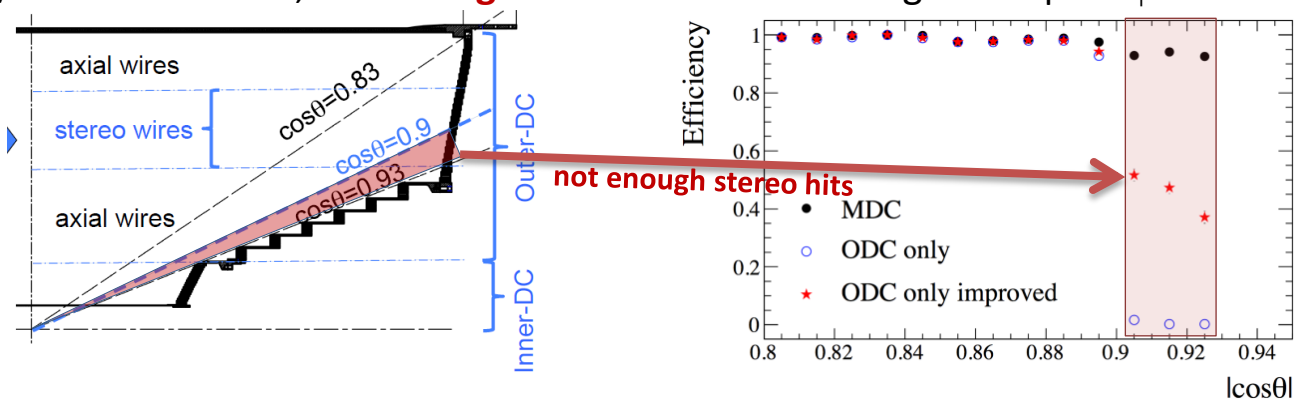
Why need a new tracking algorithm(2)

----Inner chamber upgrade

- Inner drift chamber will be replaced with a Cylindrical GEM detector



- Current tracking algorithms are limited by the geometrical acceptance
 - w/o inner chamber, **not enough stereo hits** for tracking when $|\cos\theta|>0.9$



The combine tracking of CGEM and ODC is needed

Introduction to Hough transform

- Global method
 - All hits are treated equally
- Mathematical
 - Transform of real space hits into a mathematical space in which the track candidates can be found more conveniently and insensitive to detector design
- Voting schemes
 - Let each feature vote for all the models that are compatible with it

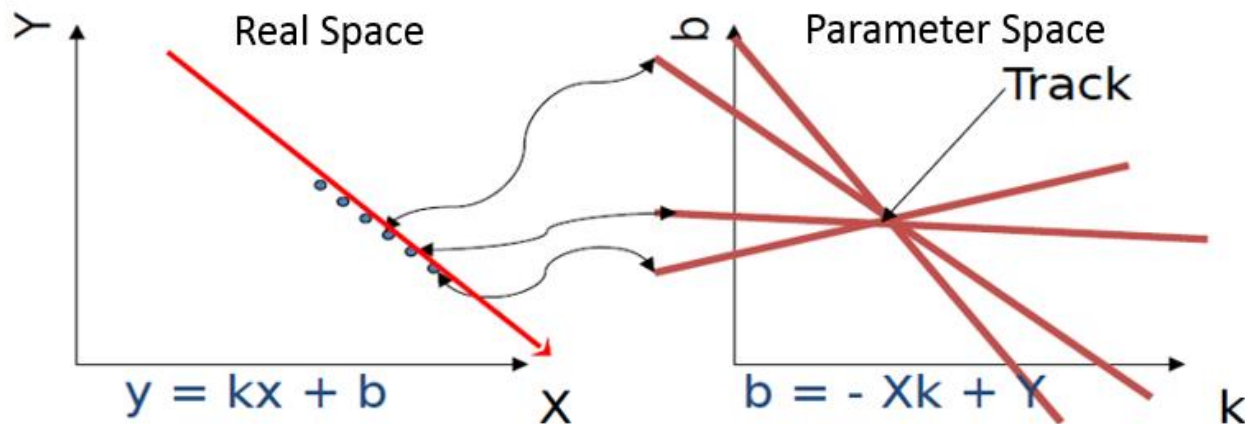
Advantages

- More hits can be included at first step
 - Find track using all axial/stereo layers or with axial and stereo layer simultaneously
- Noise resistant
 - Hopefully the noise features will not vote consistently for any single model
- Hit inefficient resistant
 - Missing data doesn't matter as long as there are enough features remaining to agree on a good model
- Quick

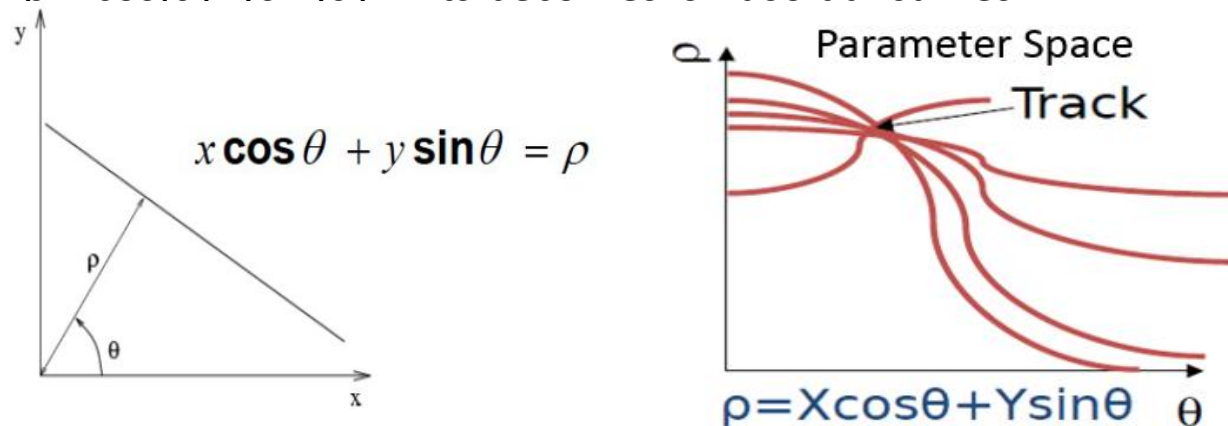
Introduction to Hough transform

Hough transform : a mathematical transformation

- Transform a point in real space to a line or a curve in parameter space
- Points rest on a line in real space \leftrightarrow lines or curves focus in Hough space



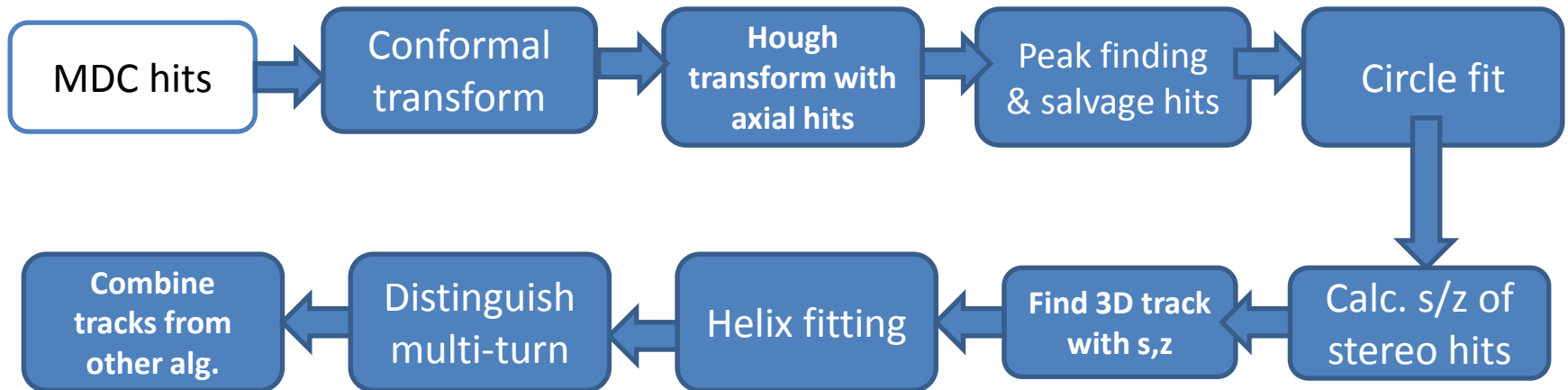
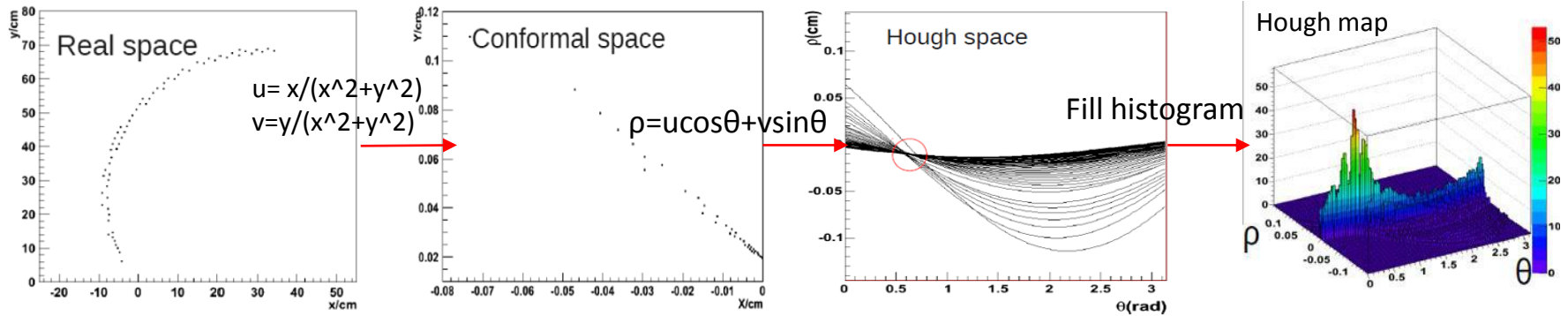
- $\rho = x \cos(\vartheta) + y \sin(\vartheta)$ hits becomes sinusoidal curves



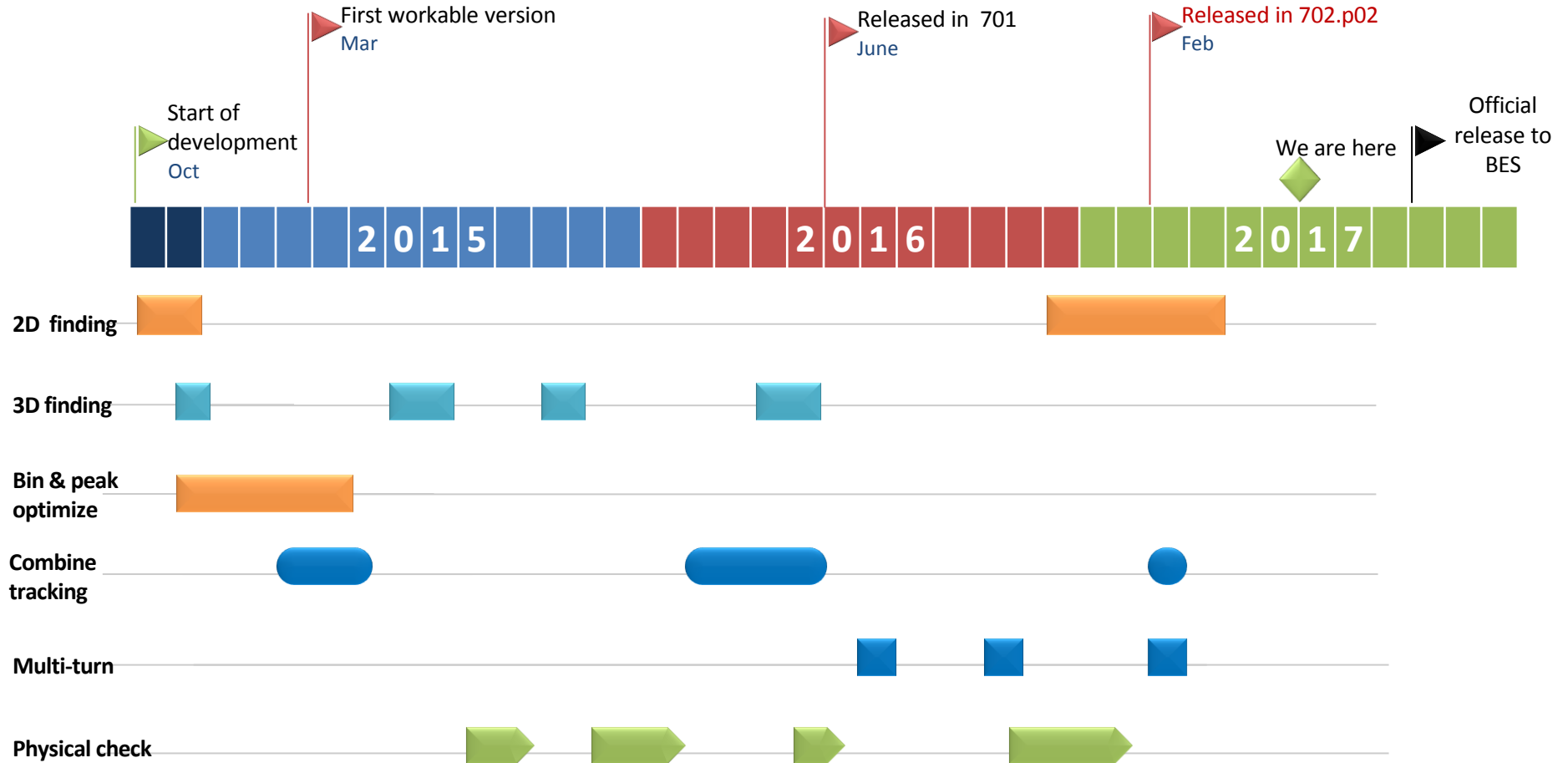
Overview of Hough tracking Development

- Manpower
 - Zhang Jin, Zhang Yao, Liu Huaimin (IHEP)
 - Zhang Xueyao (Shandong University)
 - Huang Zhen is work on CGEM-ODC tracking
- History and status
 - Coding all by ourselves, start from Oct. 2014
 - Now as a supplementary to PAT&TSF
 - Have been released for physical use @ BOSS 702.p02
 - CGEM-ODC tracking using Hough is under development

Implementation of Hough method

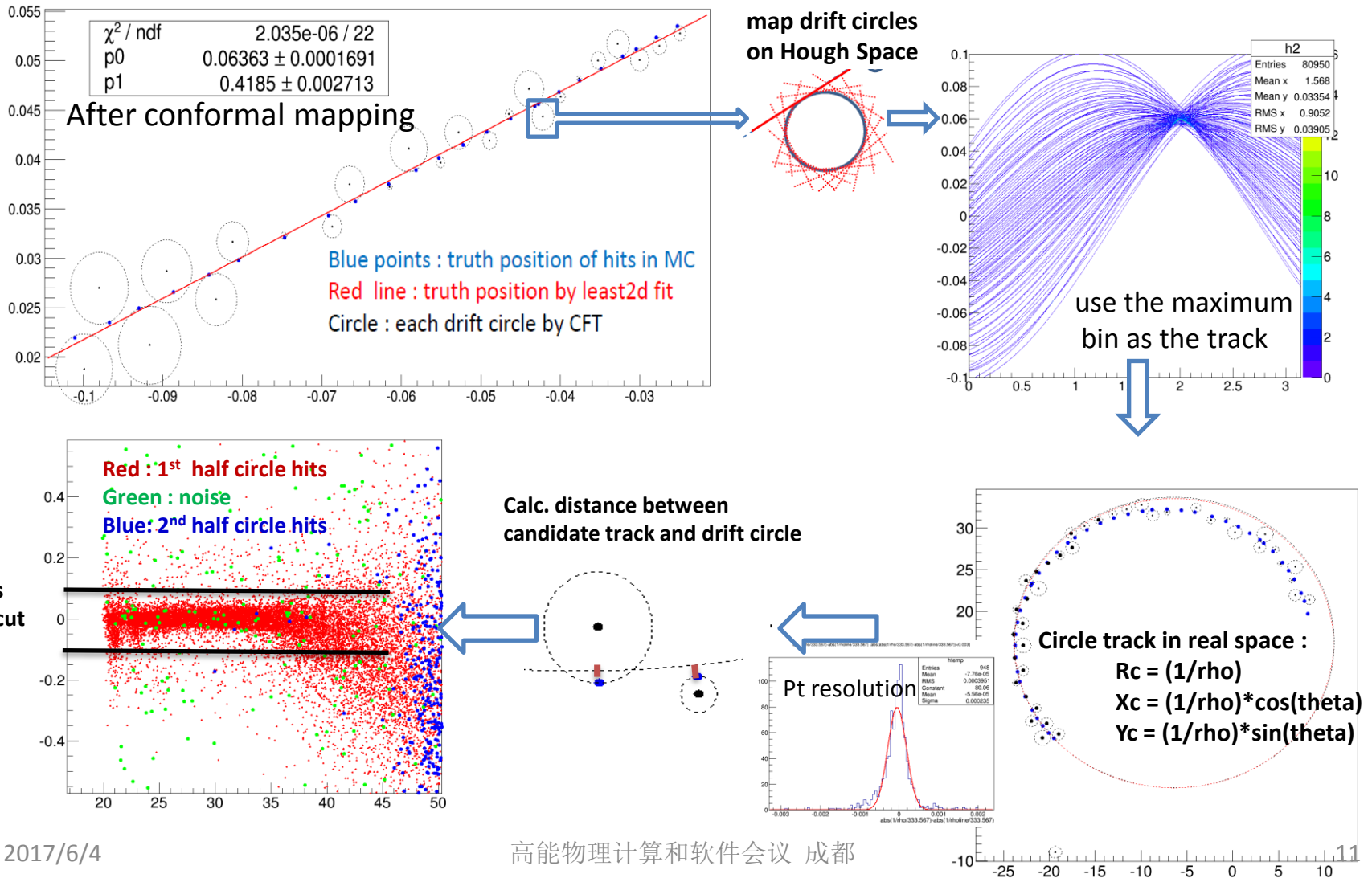


Timeline

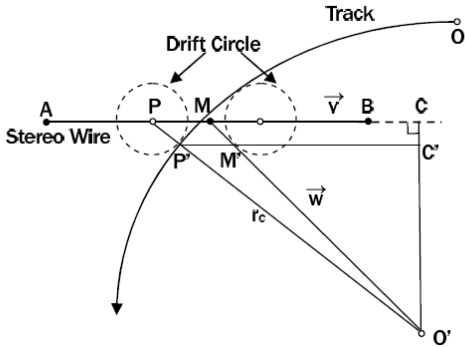


2D finding

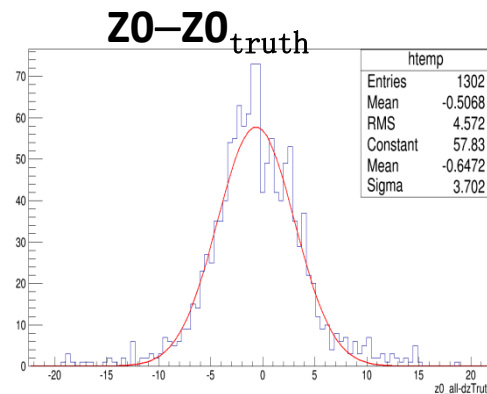
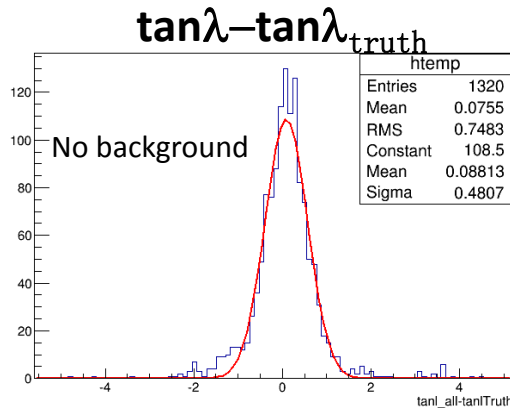
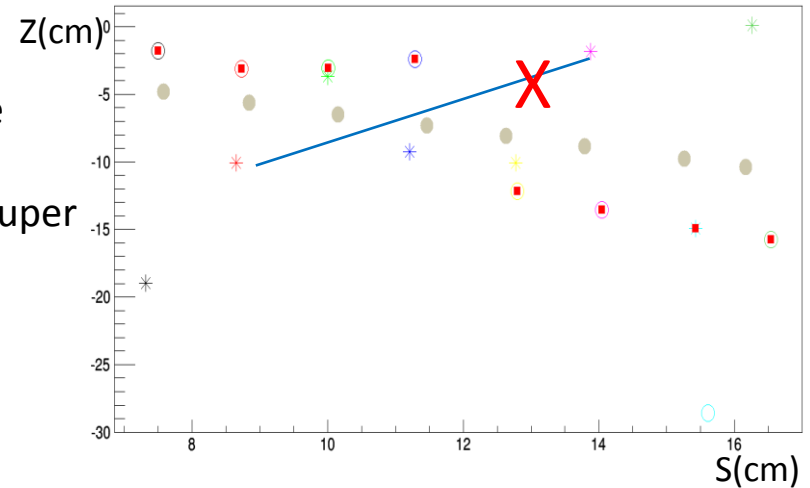
- From mapping wire position to use hit drift distance



3D finding

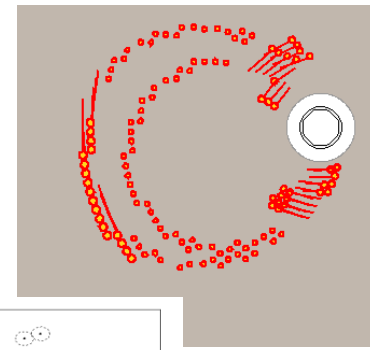


- Calculate z and flight length along track (S) by circle track and drift distance
- In S/Z plane calculate every line of points in same super layers
- Each two points add $(0,0)$ to fit a straight line
- Chi2 cut & z_0 cut & $\tan\lambda$ cut \rightarrow candidate line
- Fill candidate line in $(\tan\lambda, z_0)$ Hough space

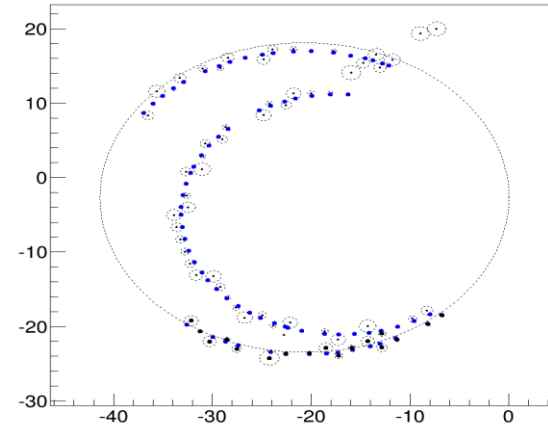
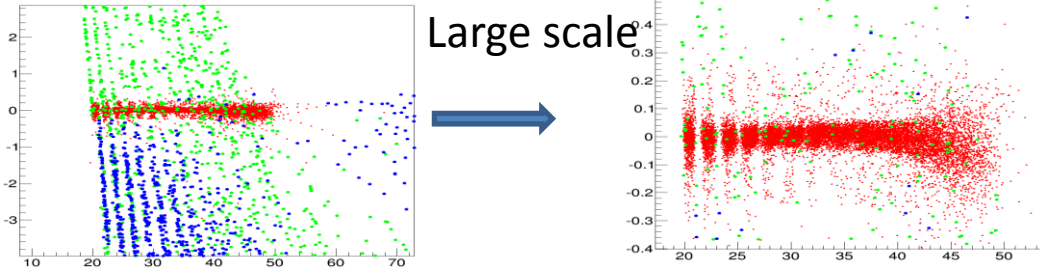


Resolution of $\tan\lambda$ and z_0 by s/z Hough transform is good

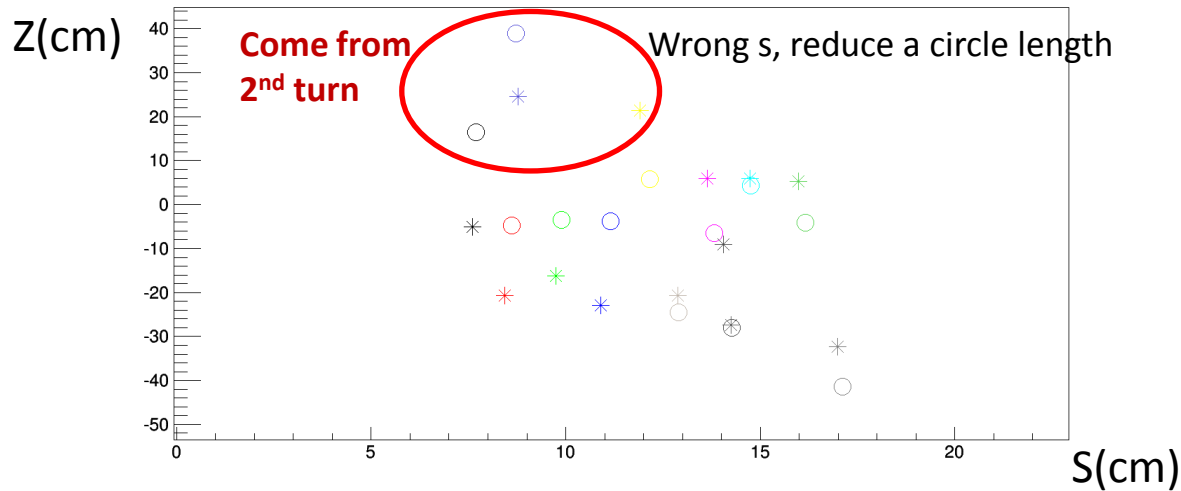
Multi turn tracks



70MeV : begin to make multi turn tracks



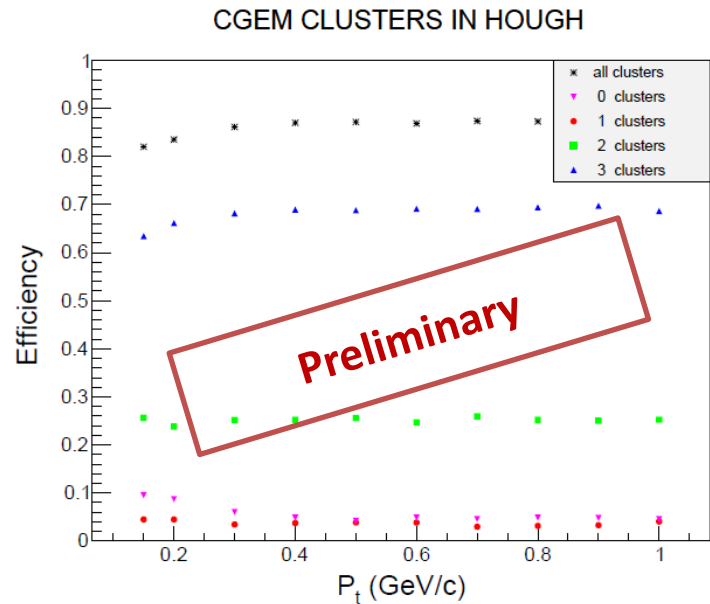
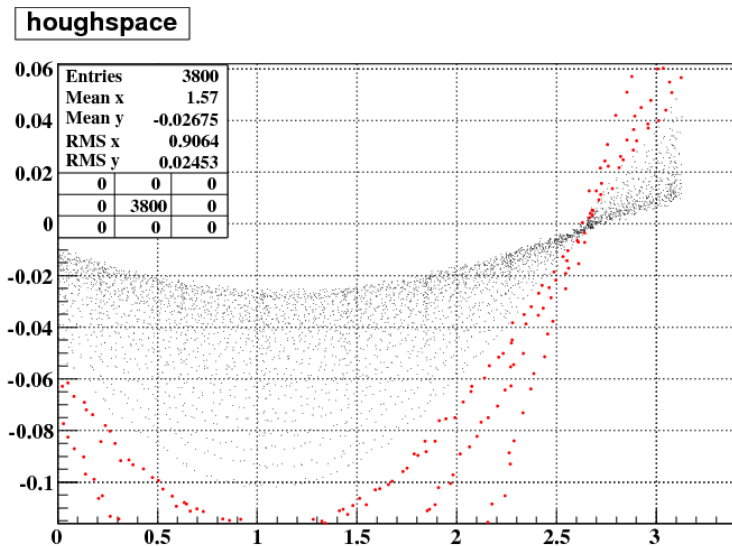
Hits can be tell from different turns in 70MeV



By S/Z Hough transform as first step , noise & hits from other turn may be reduced

CGEM+ODC tracking

- A preliminary CGEM+ODC tracking have been realized
 - CGEM cluster have been used for 2D track finding



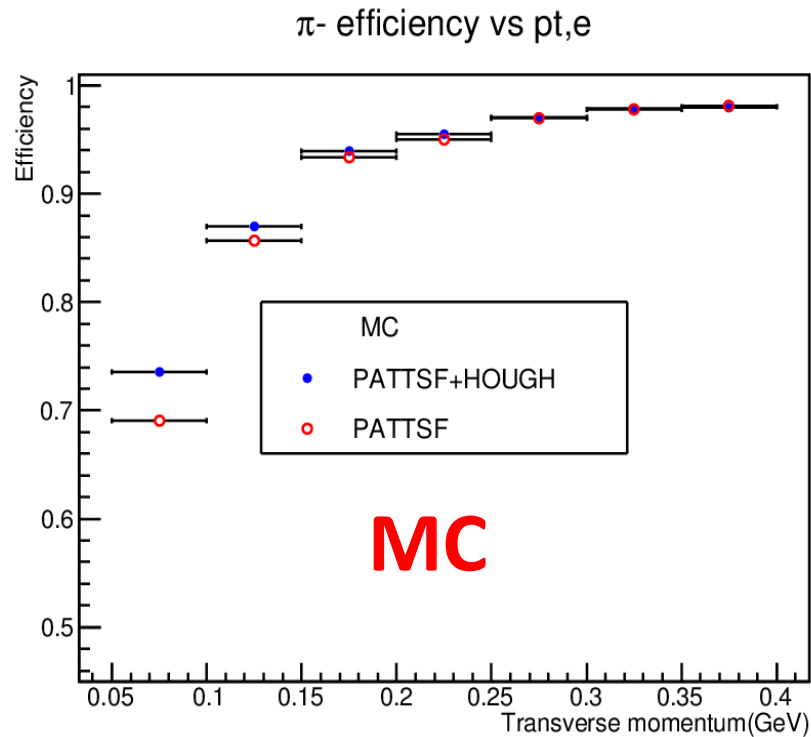
HOUGH tracking release

- Validation before release
 - Increments of computing time and memory are acceptable
 - No effect on original tracking
 - Improvement is consistent with previous study
- **HOUGH method have been released in BOSS 7.0.2.p02**
- **But not used in official release**
 - Won't influence the official tracking by default
- To use this package , modify the reconstruction job option file:
replace
`#include "$MDCXRECOROOT/share/jobOptions_MdcPatTsfRec.txt"`
with
`#include "$MDCHOUGHFINDERROOT/share/jobOptions_MdcPatTsfHoughRec.txt"`

Tracking efficiency check with MC

$$\Psi(2s) \rightarrow \pi^+ \pi^- J/\Psi, \quad J/\Psi \rightarrow l^+ l^-$$

Signal MC with background mixing, 500k events

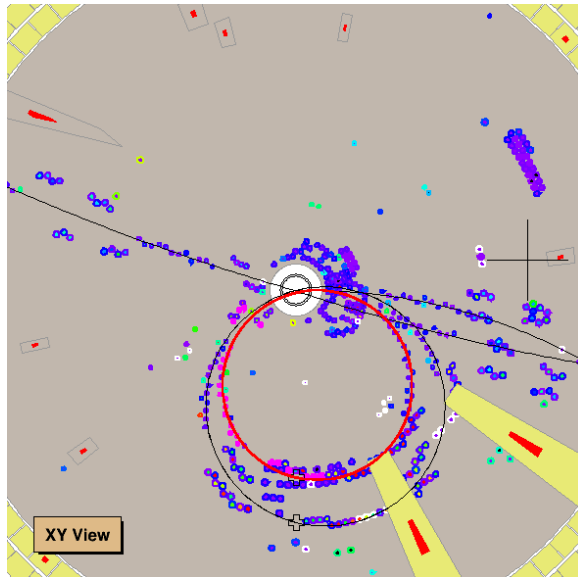


Tracking efficiency increased $\sim 4.5\%$ for $50\text{MeV} < pt < 100\text{MeV}$, relative increased $\sim 6.5\%$

Clone Track Rate

$$\Psi(2s) \rightarrow \pi^+\pi^-J/\Psi, J/\Psi \rightarrow l^+l^-$$

find 5 tracks passed tracking selection : a ghost track in this event



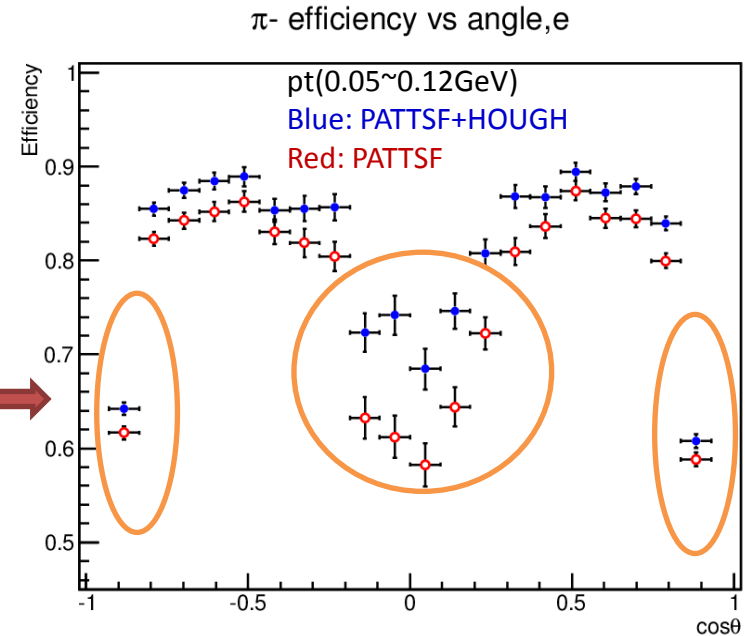
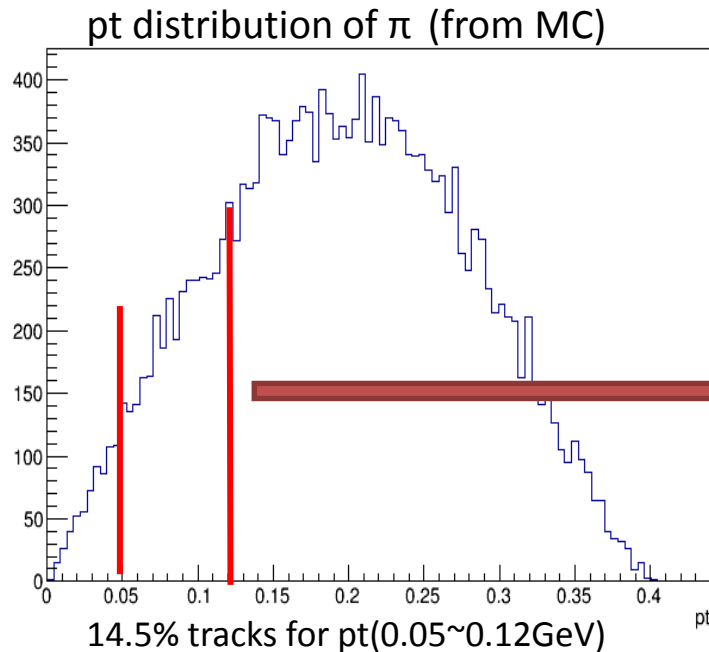
Most ghost tracks are from multi turn tracks

	N=3,4,5	N=4	N=5	N5/N(3,4,5)
PATTSF	207338	189847	240	1.16%
PATTSF+HOUGH	209211	193313	336	1.60%

clone track rate is acceptable

Tracking efficiency vs $\cos\theta$

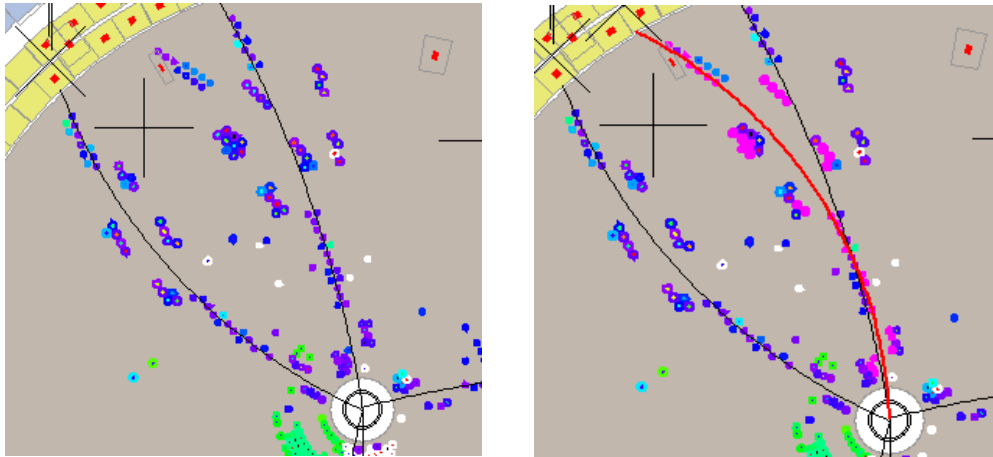
$$\Psi(2s) \rightarrow \pi^+ \pi^- J/\Psi, \quad J/\Psi \rightarrow |^+|^-$$



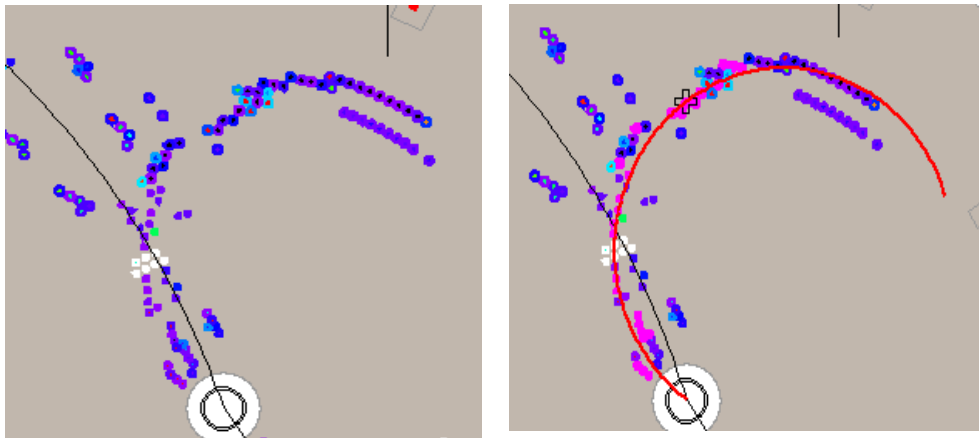
- Reason of low efficiency
 - small dip angle ($|\cos\theta| < 0.2$): bad vertex, hit overlap
 - large dip angle ($|\cos\theta| > 0.83$): hit overlap, noise, insufficient hits

Examples of salvaged tracks with HOUGH

Salvage high p_T track



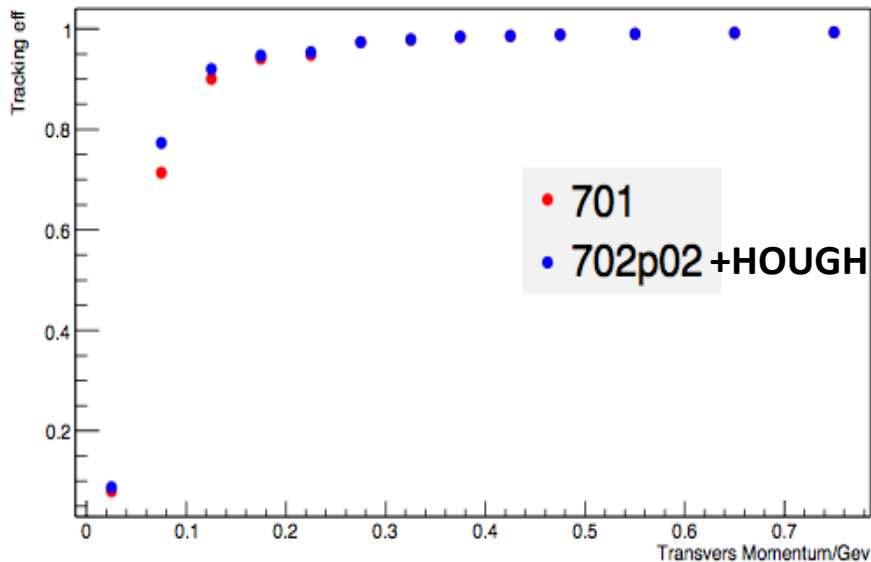
Salvage low p_T track



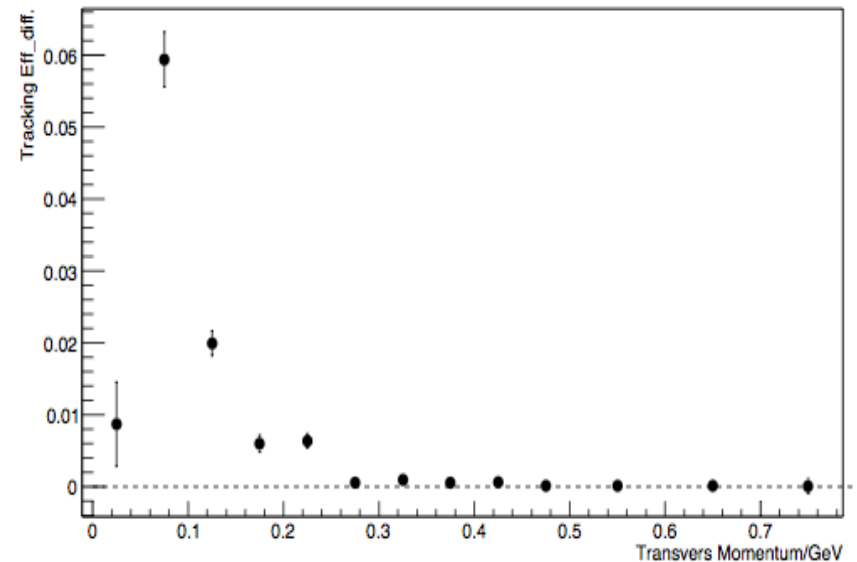
Tracking performance check with $J/\psi \rightarrow p\bar{p}\pi^+\pi^-$

Signal MC with 100,000 events

Tracking efficiency of π



Tracking efficiency difference after using HOUGH



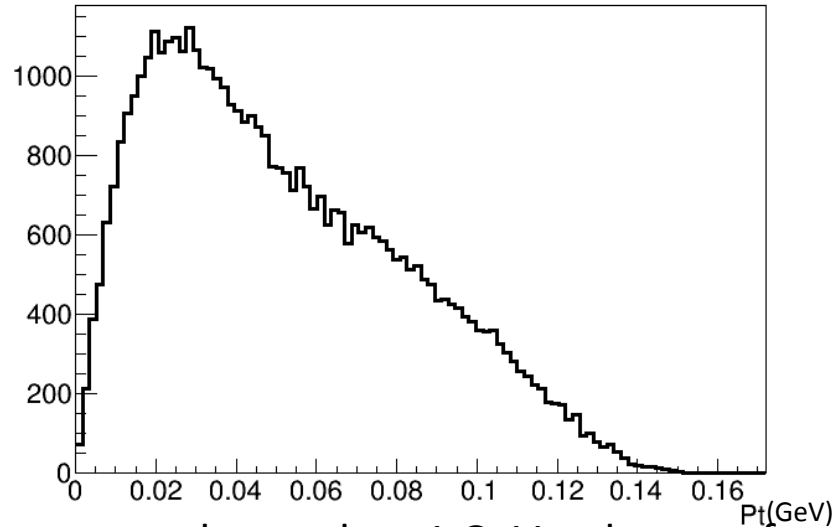
Tracking efficiency increased for barrel pion at $50\text{MeV} < p_T < 100\text{MeV}$
Detailed study is on going

Preliminary performance check by

$$\Psi' \rightarrow e^+ e^- \chi_{cJ}, \chi_{cJ} \rightarrow \Upsilon J/\Psi, J/\Psi \rightarrow l^+ l^-$$

Thanks to Zhang Jielei's help

Pt distribution of e (from MC)



Event Selection :

- 3 or 4 tracks
- define tracks with a momentum larger than 1 GeV as leptons from J/ Ψ
- one good photon
- 1C kinematic fit
 - $\chi^2 < 5$
 - $m(l^+ l^-) > 3.06 \text{ GeV}$ & $m(l^+ l^-)$
 - $m(\Upsilon / \Psi) > 3.49 \text{ GeV}$

$$\epsilon = \frac{n(n\text{Good} = 4)}{N(n\text{Good} = 3\text{or}4)}$$

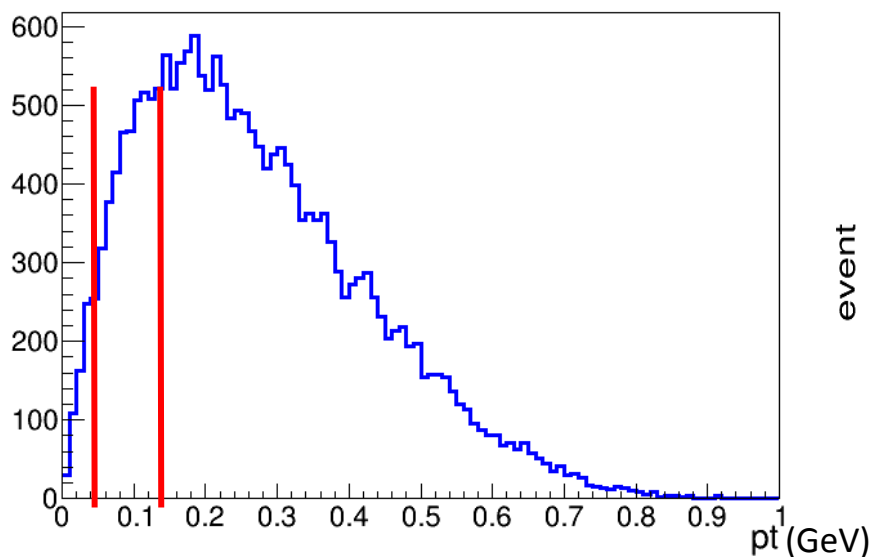
Tracking efficiency \uparrow 2.6% relatively \uparrow 5% with HOUGH

Preliminary performance check by

$$D_s^- \rightarrow K^- K_s \pi^0, K_s \rightarrow \pi^+ \pi^-$$

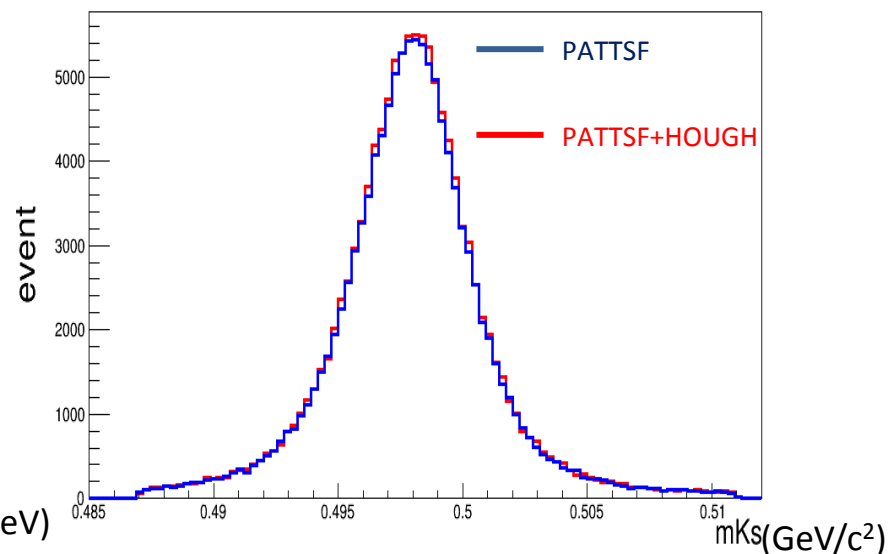
Thanks to Luyu's help

pt distribution of π (from MC)



14 % tracks for $pt(0.05 \sim 0.12) \text{ GeV}$

mass distribution of tagged D_s



number of tagged D_s \uparrow 1.87% after HOUGH in preliminary result

Ds Signal Yields

By H.L. Ma and S.F. Zhang

Check the Ds yields using 4180 data at run 45427 ~ 45855

- Version 702p01 : w/o HOUGH
- Version 702p02 + HOUGH

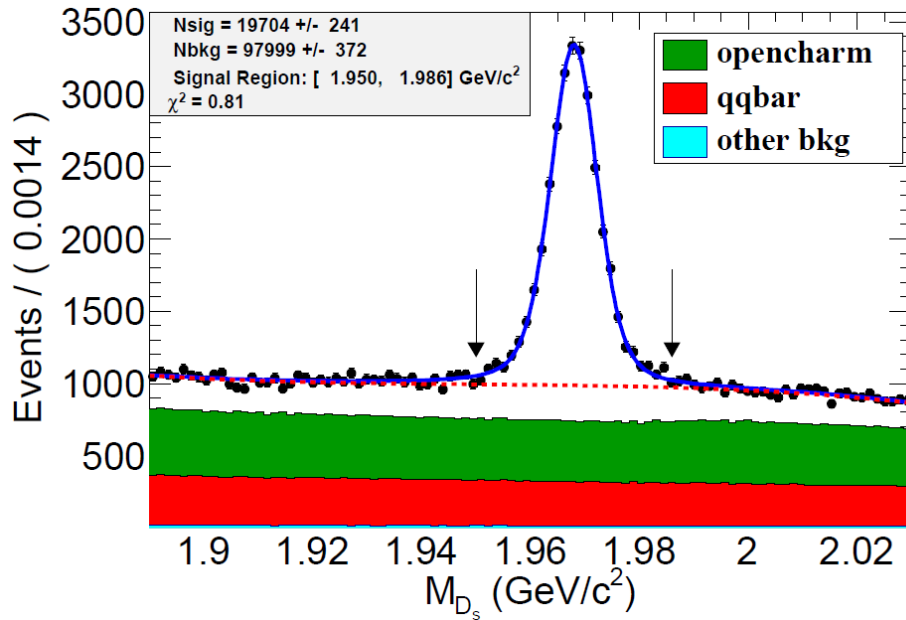
Tag Mode	$M_{D_s^+}$ window (GeV/c ²)	yields(702p01)	N_{bkg} (702p01)	yields(702p02)	N_{bkg} (702p02)
$K^+K^-\pi^+$	[1.950,1.986]	19704 ± 241	25336 ± 189	19746 ± 240	25132 ± 188
$K^+K^-\pi^+\pi^0$	[1.947,1.982]	5897 ± 438	32187 ± 290	5828 ± 267	32419 ± 226
$\pi^+\pi^+\pi^-$	[1.952,1.984]	5147 ± 353	44397 ± 271	5120 ± 354	45569 ± 274
$K_S^0K^+$	[1.948,1.991]	4706 ± 116	2700 ± 166	4701 ± 109	2638 ± 138
$K_S^0K^+\pi^0$	[1.946,1.987]	1670 ± 348	7836 ± 217	1725 ± 219	7780 ± 151
$K^+\pi^+\pi^-$	[1.953,1.983]	2384 ± 337	36090 ± 246	2415 ± 339	36473 ± 250
$K_S^0K_S^0\pi^+$	[1.951,1.986]	769 ± 62	1577 ± 49	815 ± 64	1635 ± 50
$K_S^0K^-\pi^+\pi^+$	[1.953,1.983]	1911 ± 92	3875 ± 74	1970 ± 95	3978 ± 75
$K_S^0K^+\pi^+\pi^-$	[1.958,1.980]	1002 ± 96	5344 ± 83	1055 ± 104	5486 ± 85
$\eta\gamma\gamma\pi^+$	[1.930,2.000]	2768 ± 173	8203 ± 149	2810 ± 175	8285 ± 151
$\eta_{\pi^+\pi^-\pi^0}\pi^+$	[1.941,1.990]	795 ± 62	1633 ± 52	820 ± 87	1689 ± 64
$\eta'_{\pi^+\pi^-\eta\gamma\gamma}\pi^+$	[1.940,1.996]	1380 ± 59	700 ± 39	1416 ± 60	766 ± 41
Total		48133 ± 825	169878 ± 608	48421 ± 703	171850 ± 557

$D_s \rightarrow K^+ K^- \pi^+$

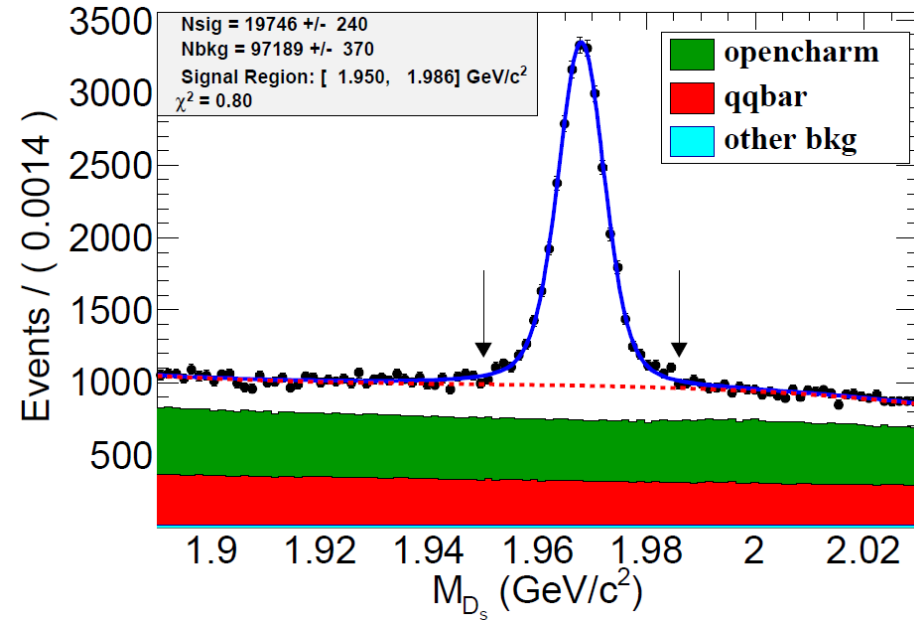
Ds mass window : [1.950,1.986]

Tag Mode	$M_{D_s^+}$ window (GeV/c ²)	yields(702p01)	N_{bkg} (702p01)	yields(702p02)	N_{bkg} (702p02)
$K^+ K^- \pi^+$	[1.950,1.986]	19704 ± 241	25336 ± 189	19746 ± 240	25132 ± 188

Version 702p01



Version 702p02 + HOUGH



Improvement can be seen after using HOUGH tracking

Summary and Outlook

- Hough tracking is released for physical test in BOSS 7.0.2.p02
 - Not yet been included in the default reconstruction flow
- Improvement can be seen at low p_T from physical channels
 - Efficiency have **3~4%** improvement in 50-120MeV
- More validations will be done using low p_T channels
- Outlook
 - Used for official data reconstruction at next released
 - Can be used on outer drift chamber + CGEM tracking