

LHC Single Beam DA: measurements vs simulations

Ewen H. Maclean

Studies in collaboration with R.Tomás, M.Giovanozzi, F.Schmidt, T.H.B.Persson & R.Appleby, with many thanks to the LHC optics measurement and correction team



Many thanks to the LHC@home volunteers!

Compensation & understanding of the nonlinear single-particle dynamics has begun to emerge as an operational constraint in LHC Run 2

7th Evian Workshop: [Nonlinear optics commissioning in the LHC](#)

Single beam DA is expected to be a significant challenge for the High-Luminosity LHC upgrade

[Optics Measurement and Correction Challenges for the HL-LHC, CERN-ACC-2017-0088](#)

→ Since 2011, a program of beam-based measurements has studied NL-dynamics throughout the LHC cycle

DA is a key observable & figure-of-merit for LHC. Examined via 3 methods:

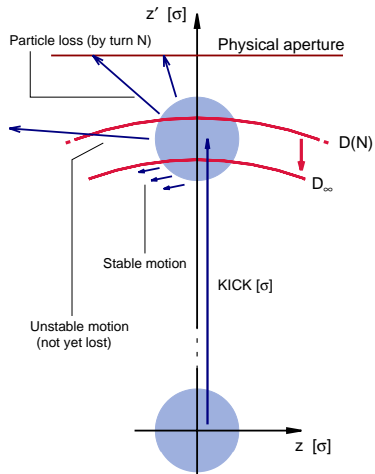
Long-term dynamic aperture (free oscillations):

- Conventional measurement via single kicks
- Measurement of long-term evolution of DA with heated beams

Short-term dynamic aperture:

- Short term DA of driven oscillations
(seen next talk by F.Carlier)

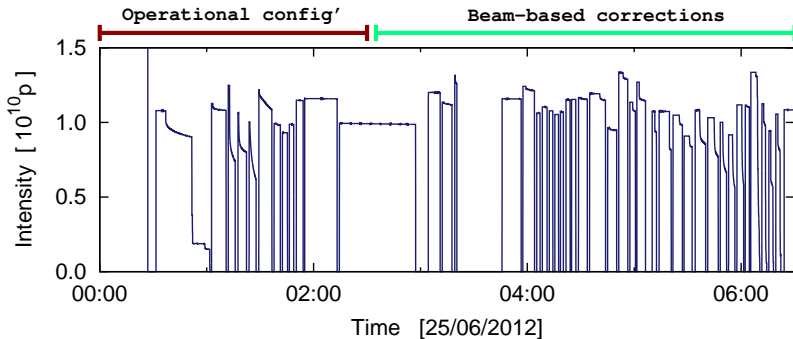
Measurement via single kicks



- LHC 'aperture kicker' dipole ramps up/down in $\sim 1/2$ turn
- Provide large amplitude displacement of pilot bunch ($\sim 10^{10} p$)
- Kick action determined from TbT BPM position data
 $\rightarrow (0.5 \times \text{Peak-to-Peak})^2 / \beta$
- Beam-loss following kick determines distance between kick and DA(N)

First detailed measurements performed in 2012 (LHCb2) to study DA and amplitude detuning

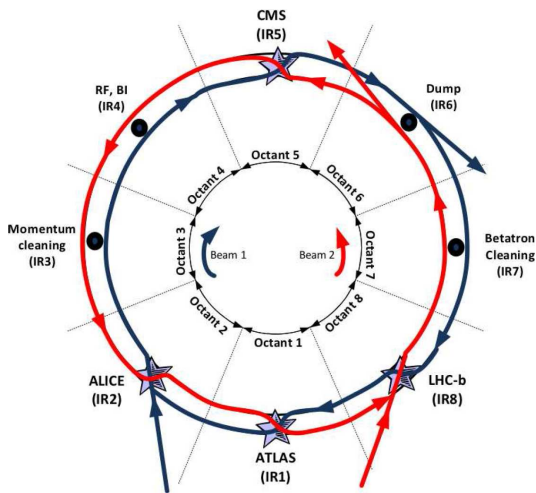
E.H. Maclean, R. Tomás, F. Schmidt, T.H.B. Persson, *Phys. Rev. ST Accel. Beams* 17 081002 (2014)



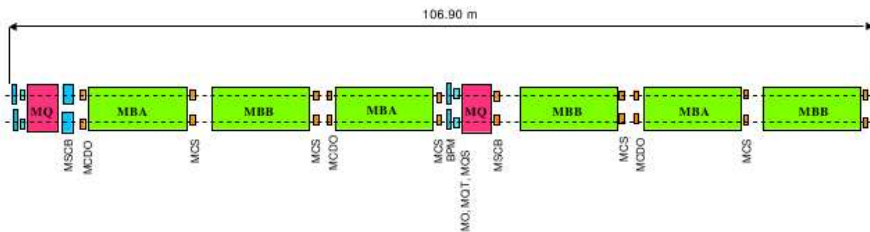
Two configurations examined at injection:

- **Operation configuration:** Landau octupoles (MO) for instability damping
→ Measurements in H & V planes
- **Corrected configuration:** MO off + beam-based correction for b_4 & b_5 errors
→ Measurement in H, V, & diagonal

NL-dynamics at injection dominated by sources in LHC arcs



NL-dynamics at injection dominated by sources in LHC arcs



MQT: trim quadrupole

MCS: spool piece sextupole

MQS: skew trim quadrupole

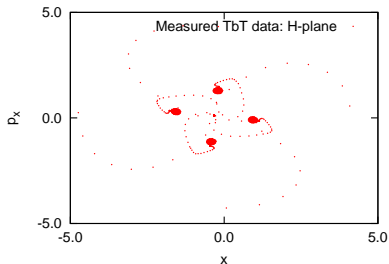
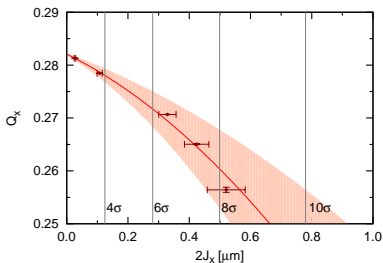
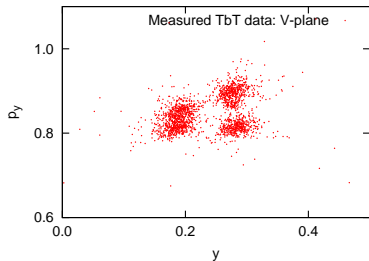
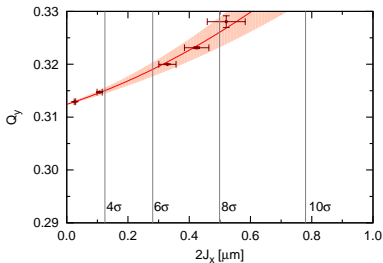
MCDO: spool piece octupole + decapole

MO: lattice octupole

MSCB: sextupole (skew sextupole) + orbit corrector

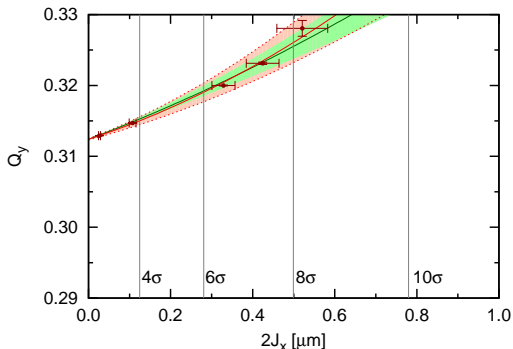
Operational config', H-plane:

- Observe large first and second order detuning-with-amplitude



- Simultaneously reach 3rd and 4th order resonances

- Compare measured detuning to best-knowledge model:
measured errors, measured alignments, octupole hysteresis



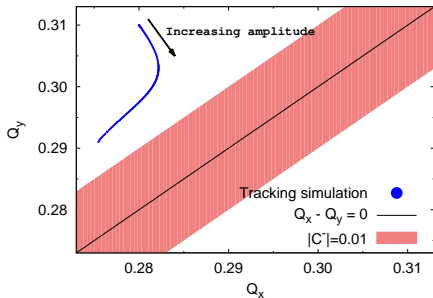
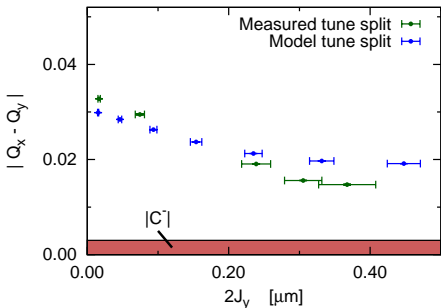
	[unit]	Meas' \pm err	Model \pm err
$\frac{\partial Q_x}{\partial \epsilon_x}$	$[10^3 \text{m}^{-1}]$	-29 7	-27 1
$\frac{\partial Q_y}{\partial \epsilon_x}$		19 3	21 2
$\frac{\partial Q_x}{\partial \epsilon_y}$		24 4	21 2
$\frac{\partial Q_y}{\partial \epsilon_y}$		-33 1	-31 1
$\frac{\partial^2 Q_x}{\partial \epsilon_x^2}$	$[10^9 \text{m}^{-2}]$	-60 30	-14 4
$\frac{\partial^2 Q_y}{\partial \epsilon_x^2}$		34 10	18 9

- Single biggest source of uncertainty in NL-model is linear coupling
(see [IPAC'17 WEPIK092](#) and reserve slides)

Operational configuration, V-plane:

Main feature observed is **Amplitude dependent closest tune approach**

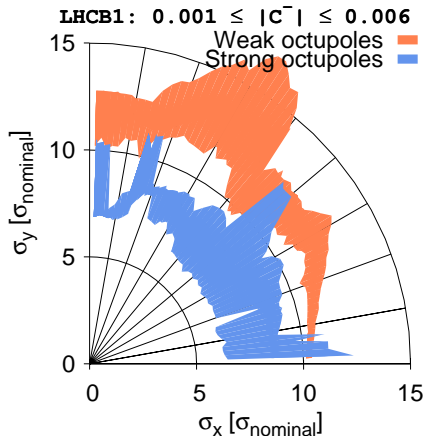
→ **Action dependent analogue of ΔQ_{min} from $|C^-|$** (PRSTAB 17 081002, IPAC'15 TUPTY042)



- Major source at 450 GeV is linear coupling + h_{1111} (cross-term detuning)
- Mechanism has been proposed: R.Tomás,T.Persson,E.Maclean, PRSTAB, 19, 071003 (2016)
- Predictions validated during 2016 LHC MD (to be published)

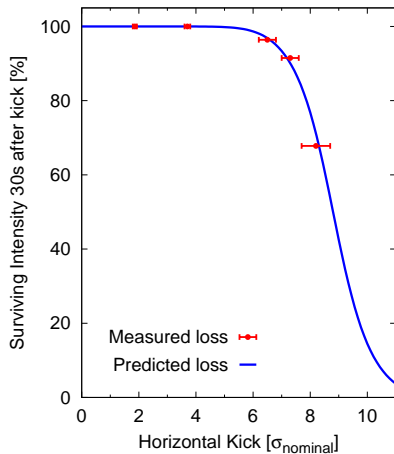
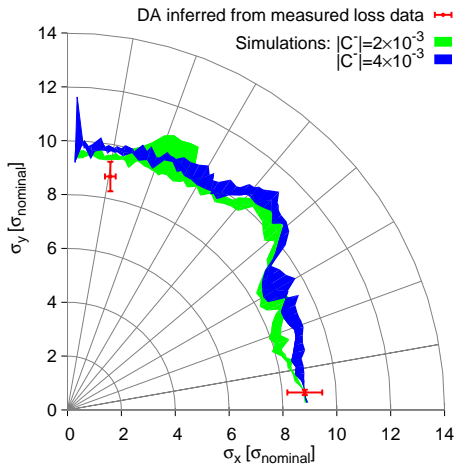
We believe we have a good understanding of the dynamics in H & V planes

- Linear coupling has a major influence on the observed behaviour
- This also translates into a large influence on dynamic aperture

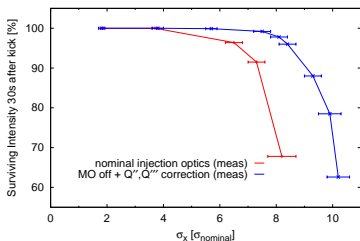
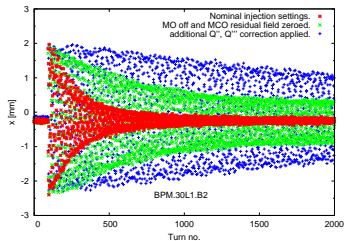
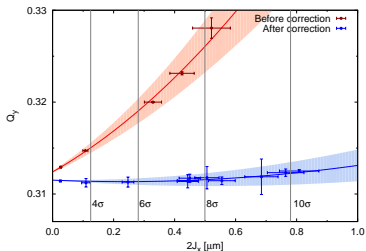
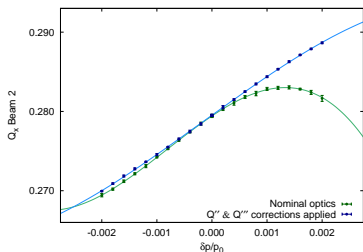


- Match coupling in DA simulations measured values, with spread reflecting coupling measurement quality

Compare DA 30s after kick to best-knowledge model in SIXTRACK



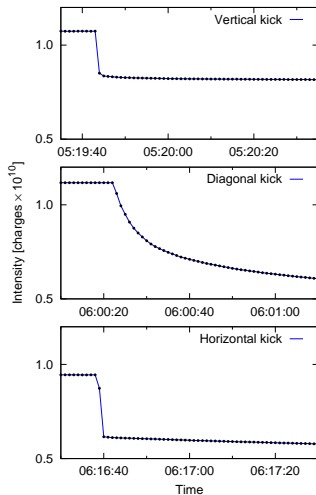
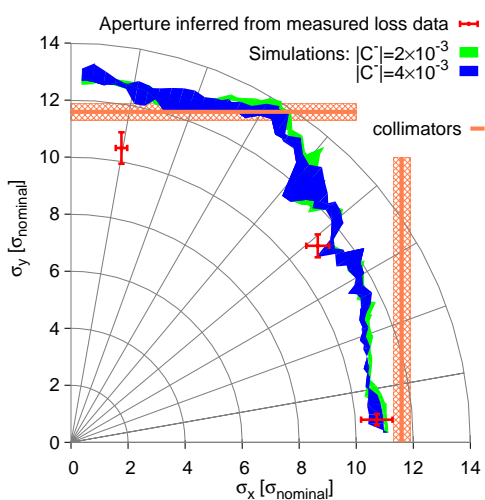
Corrected configuration, with beam-based minimization of Q'' & Q'''



- Improved decoherence, detuning, & DA
- Beam-based correction operational at injection since 2015

Compare DA 30s after kick to model in SIXTRACK

→ residual NL-chroma matched in NL-model



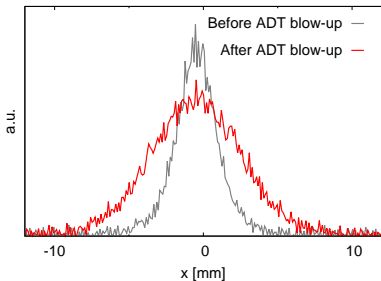
- Losses in H & V consistent with physical aperture

DA measured via single-kicks shows excellent agreement to model predictions at injection (within 10 %)

But single-kick method suffers from some limitations:

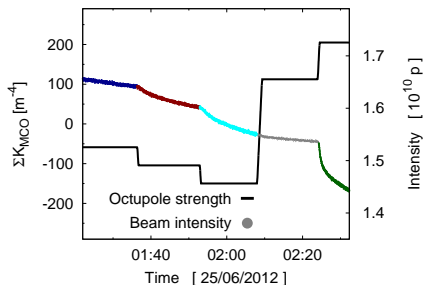
- Time consuming to measure full parameter space in σ_x/σ_y angles
- Only possible to measure at injection:
 - machine protection concerns
(large, rapid losses upon kick risk quench, or even damage!)
 - require fresh injection after every kick

Measurement of DA evolution using transverse damper



- **LHC transverse damper (ADT) used to blow-up bunch to large emittance**

- viable method @ 6.5 TeV
- slow heating limits quench risk
- blow-up in H+V so sample DA over entire parameter space



- **Examine intensity evolution upon changes in powering of NL-elements**

- **Change to fractional intensity related to an average DA after N turns**

$$\frac{I(N)}{I(1)} = 1 - \iint_{D(N)} \rho dA = 1 - e^{-\frac{D^2(N)}{2}}$$

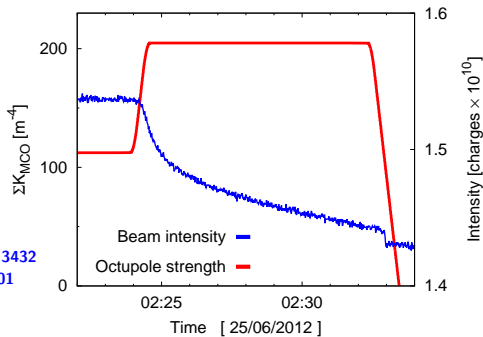
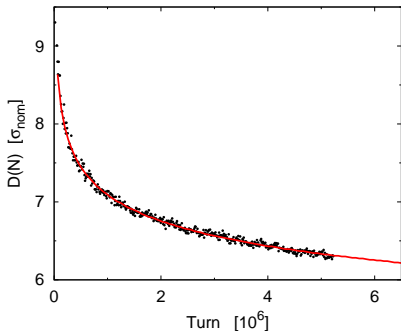
- **Normalize to standard DA units using synchrotron telescope profile data**

Aim not only to measure DA at given time, but also as function of turns

- Apply scaling law to measured/ simulated DA:

$$D(N) = D_{\infty} + \frac{b}{(\log N)^{\kappa}}$$

M.Giovanozzi, W.Scandale, E.Todesco, *Phys. Rev. E* 57 3432
 M.Giovanozzi, *Phys. Rev. ST Accel. Beams* 15, 024001



- Allows extrapolation of DA to operational timescales

→ 2.5 hours ≡ 10⁸ turns

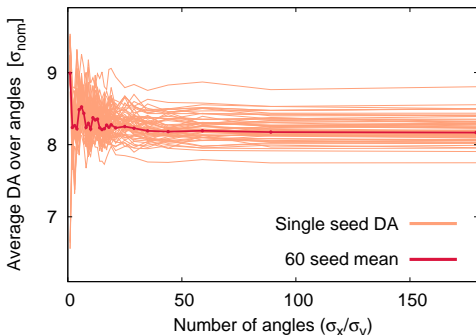
→ typical LHC simulation is 10⁵ - 10⁶ turns

- Provides more robust test for comparison of measurement to simulation

Basic model for comparison very similar to study with kicked beams on Beam 2:

- Measured normal/skew errors from 2-pole to 15-pole → 60 instances ('seeds') to account for measurement uncertainties
- Measured alignment errors
- Applied settings of octupole/decapole/skew-sextupole correctors
- Match $Q_{x,y}$ & $Q'_{x,y}$ with quadrupole/sextupole correctors
- Some beam-based input: octupole hysteresis, decapole feed-down

Ensure limits on model/measurement comparison come from machine knowledge rather than simulation parameters



Study DA saturation with simulation granularity

- e.g. Number of angles → use 60
- Large number of tracking simulations per configuration ($\sim 2e6$)!
- Volunteer computing essential to success

[LHC@home](#)

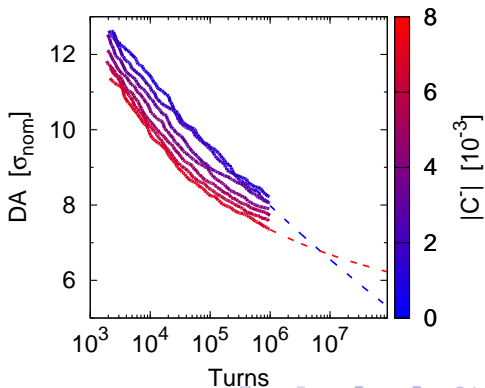
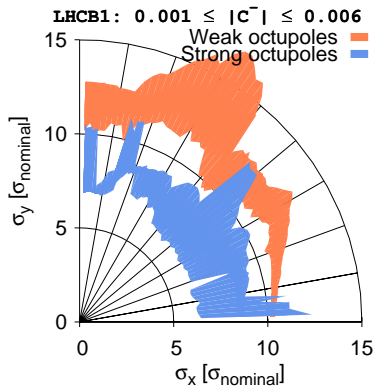
[N.Hoimyr et.al J.Phys.Conf.Ser. 396](#)

[032057](#)

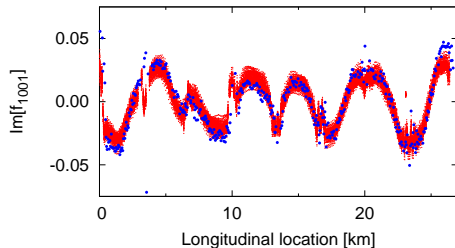
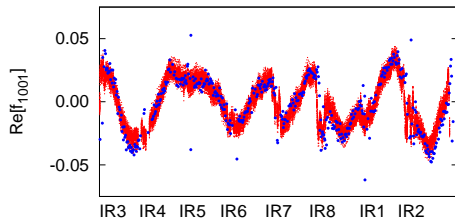
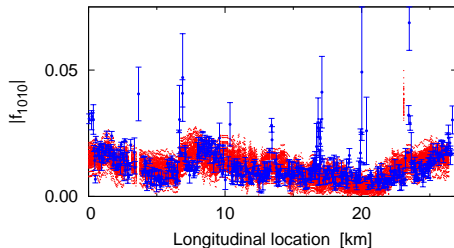
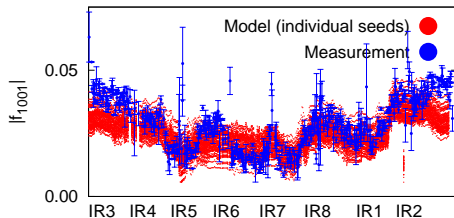
Closed orbit / beta-beat checked to have small impact on predicted DA evolution (see reserve slides)

Linear coupling can have a very large impact on LHC DA (IPAC'17 WEPIK092)

- Typical operational range of $|C^-|$ has larger effect than uncertainty on magnetic measurements
- Accurate coupling model is a priority for comparison to measurements



- Match amplitude/phase of linear coupling resonance driving terms to earlier studies with AC-dipole, & injection oscillations during DA measurements

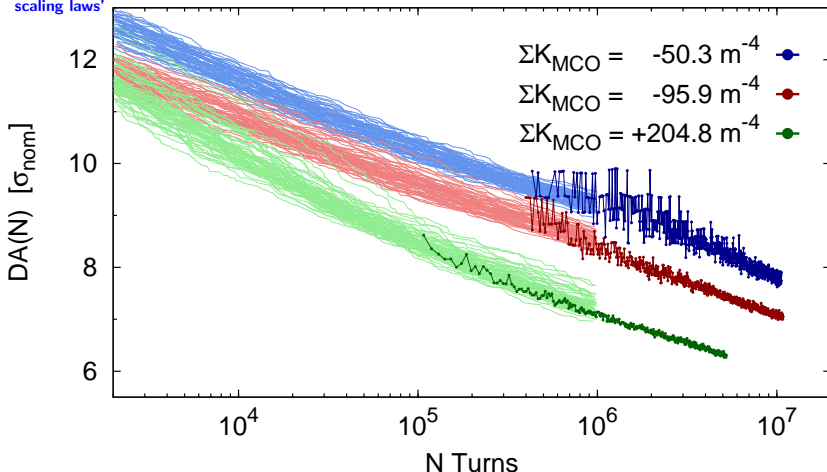


- For new measurements ensure coupling is well corrected & include witness bunch to monitor linear coupling RDTs

Comparison of modelled and measured DA

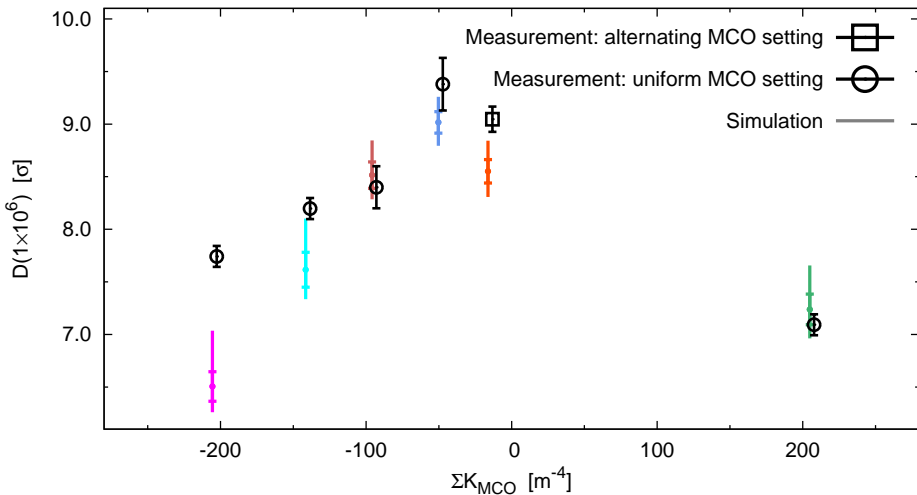
In preparation: E.H.Maclean, M.Giovanozzi & R.Appleby

'Novel method to measure the extent of the stable phase space region of proton synchrotrons using Nekoroshev-like scaling laws'

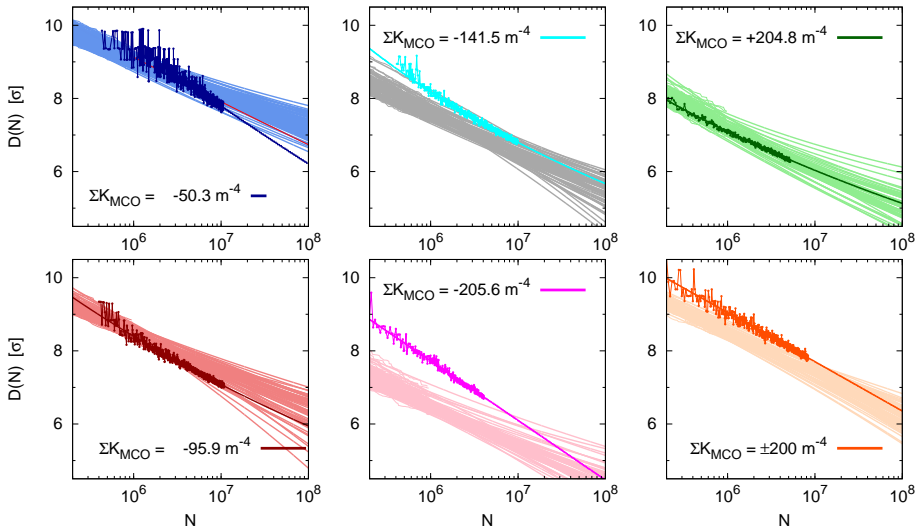


- Successful measurement of DA vs octupole strength via blow-up with transverse damper

Comparison of modelled and measured DA at 10^6 turns, for full range of octupole corrector strength



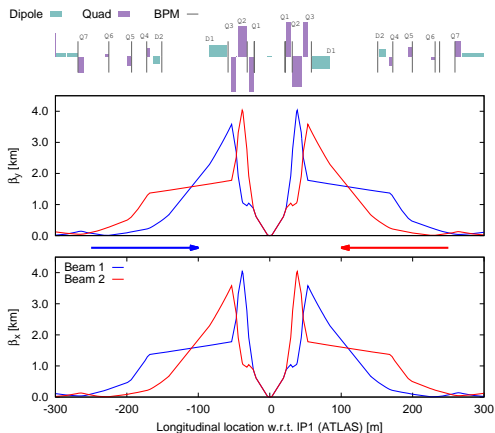
Extrapolation of measured & simulated DA via scaling law



- Measured and simulated dynamic aperture agree within 10%, over wide range of octupole strength

Correction of NL-errors in low- β^* IRs is a major motivation for DA studies in LHC

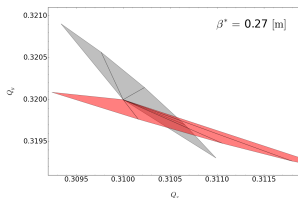
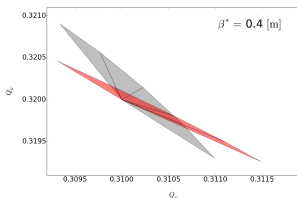
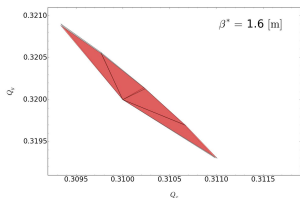
- Significant impact due to large $\beta_{x,y}$ in triplets and separation dipoles, e.g. IP1@0.6m



- High-Luminosity (HL)-LHC upgrade planned for 2025
→ increase β^* reach to ~ 0.15 cm

NL-errors in low- β^* IRs have potential to affect many key properties

- **Lifetime reduction** → single-beam DA is a serious concern for HL-LHC upgrade
- **Normal octupole errors distort Q-footprint during β^* -squeeze**
→ affects Landau damping of instabilities

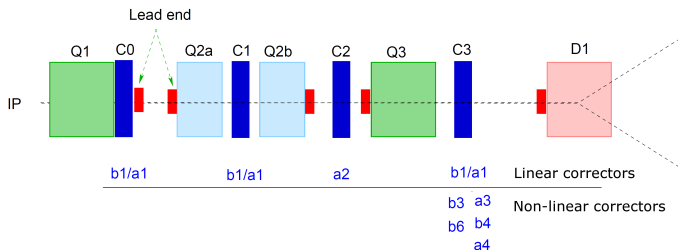


MO footprint, **MO+IR- b_4 footprint**

- **Observe/predict large feed-down to linear coupling from X'ing & sep bumps**
→ can distort footprint causing loss of Landau damping
- **Feed-down in IR also generates beta-beating**
→ detrimental to ATLAS/CMS luminosity imbalance
→ potential > 20% beta-beating due to sextupole feed-down in HL-LHC
→ Not just problem of machine optimization: machine protection!

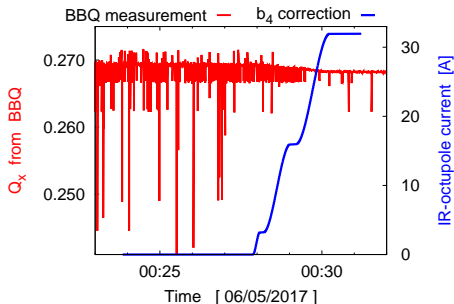
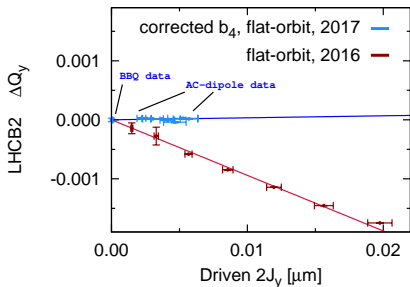
Dedicated nonlinear correctors for sextupole→dodecapole, located left/right of all experimental IRs

- **LHC:** b_3, a_3, b_4, a_4, b_6
- **HL-LHC:** $b_3, a_3, b_4, a_4, b_5, a_5, b_6, a_6$

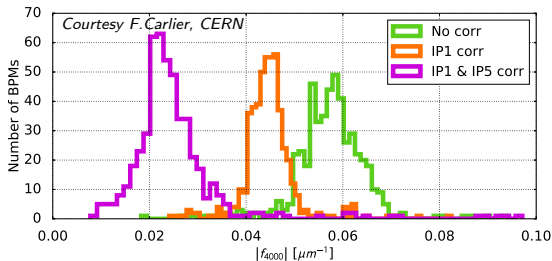


First commissioning of NL-corrections in LHC experimental IRs implemented in 2017

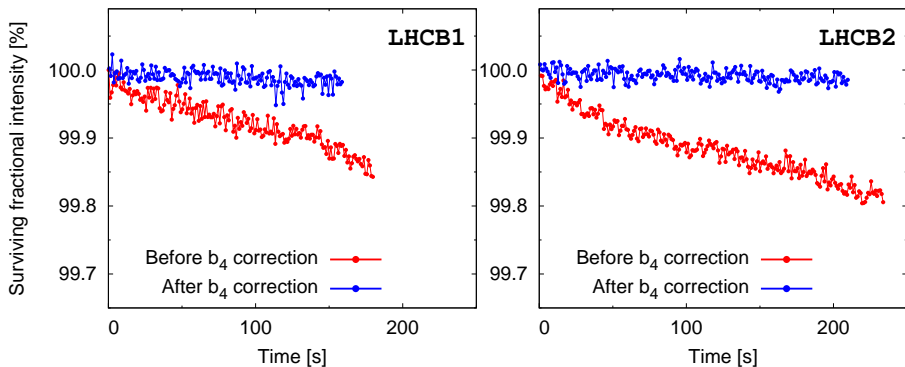
Normal octupole corrections determined to locally compensate amplitude-detuning generated in IR1 & IR5 at $\beta^* = 0.4$ m



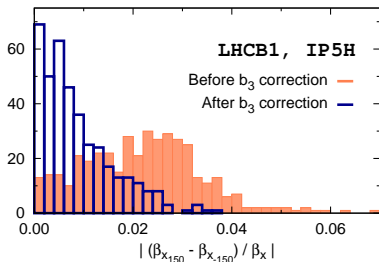
- Improved online tune & coupling measurement
- reduced strength of $4Q_x$ resonance



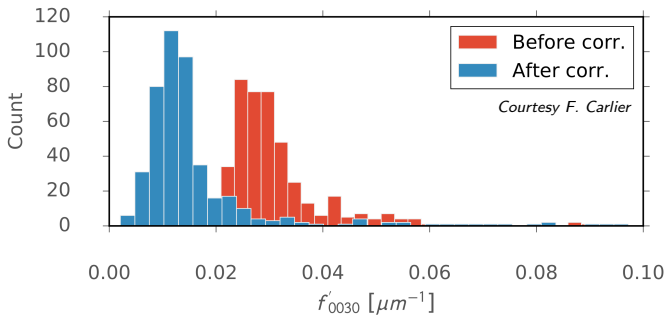
Normal octupole correction improved lifetime at $\beta^* = 0.14$ m
(machine development test to probe β^* reach of collider)



Normal/skew sextupole in IR5 & IR1 corrected by minimizing linear shift of tune with crossing angle



- Improved stability of linear optics with crossing-angle
- Reduced strength of $3Q_y$
- Skew octupole correction applied to minimize feed-down to coupling RDTs (see reserve slides)



Very high-order errors are hard to measure:

→ **direct DA compensation may be best method**

→ **First detailed measurements at 6.5 TeV several weeks ago ($\beta^* = 0.4\text{m}$)**

- **Biggest challenge was finding the DA!**

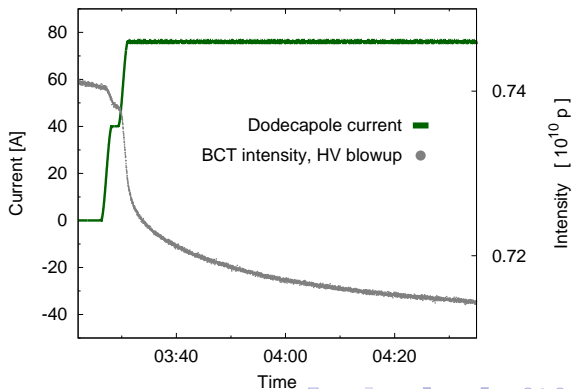
- No losses observed for operational powering of Landau octupoles

- Only saw significant losses with dodecapole correctors in experimental IRs powered to maximum strength

- **DA $> 10 \sigma_{\text{nom}}$ for operational configuration of octupoles**

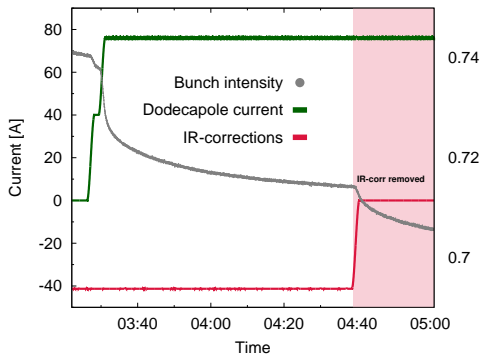
- **Max dodecapole powering reduced DA to $\sim 8 \sigma_{\text{nom}}$**

- dodecapole effects scale rapidly with $(\beta^*)^{-3}$



In 2017 LHC operated with local corrections for normal/skew sextupoles & normal/skew octupoles in low- β^* IRs

- **Clear practical benefits to operation:**
 - instrumentation & understanding/damping of instabilities
- **Does optimization of indirect observables (e.g. feed-down) improve DA?**
- **How important is DA in relation to other parameters influenced by IR-nonlinearities?**

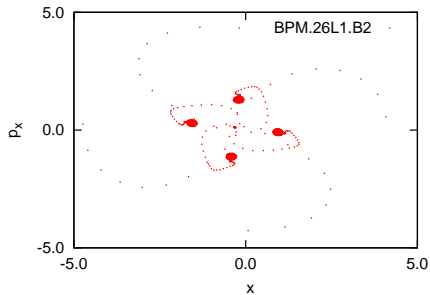
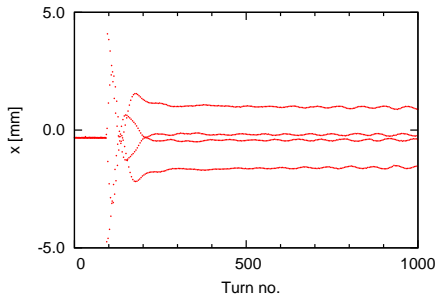
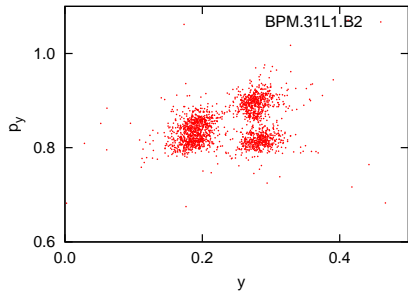
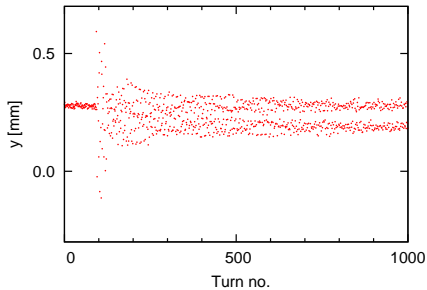


- **Slight improvement to Beam1 DA from to IR-corr**
- **Significant improvement to dynamic aperture of Beam 2**

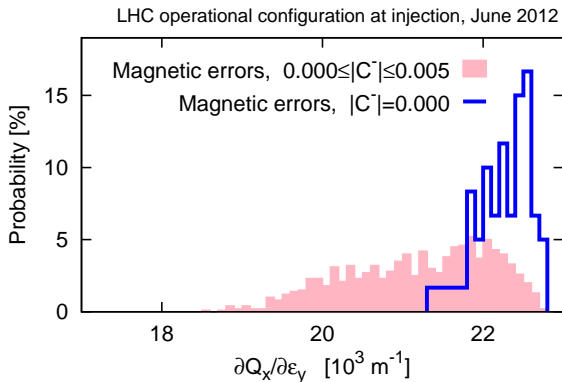
Conclusions

- Modelled & simulated DA at LHC injection agree within 10% via 2 techniques
- Technique based on slow blow-up of bunch with transverse damper validated at injection
- First beam-based commissioning for NL-errors at 6.5 TeV performed in 2017 with promising results
- Begun to apply DA measurement at 6.5 TeV as tool to study high-order NL-errors in experimental insertions

Reserve Slides

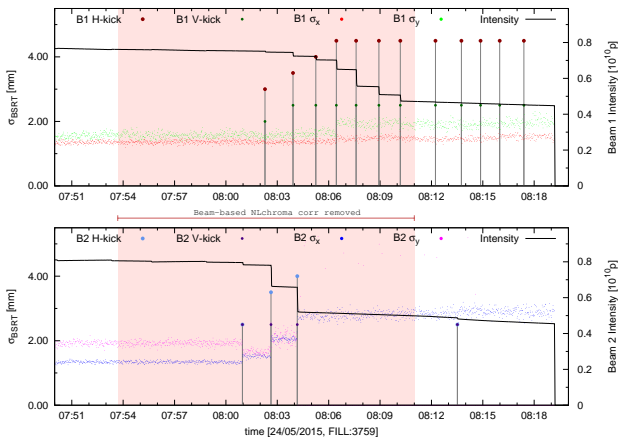


Uncertainty in predicted DA due to typical operational range of $|C^-|$, compared to uncertainty in magnetic measurements



Beam-based correction of Q''/Q''' implemented operationally in 2015

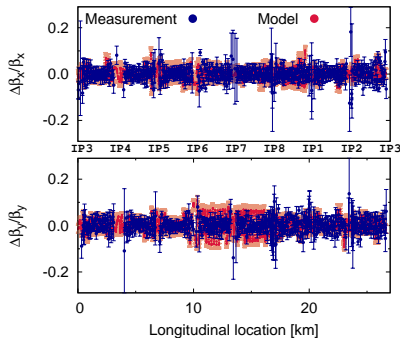
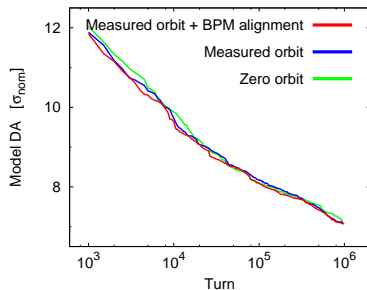
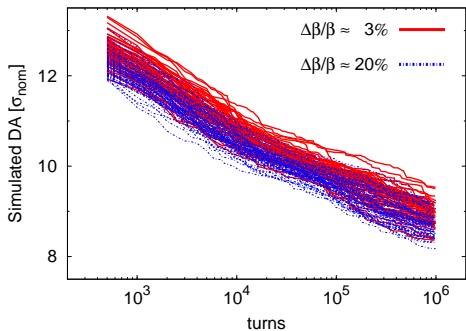
- Significantly improved beam-losses and blow-up upon AC-dipole excitation



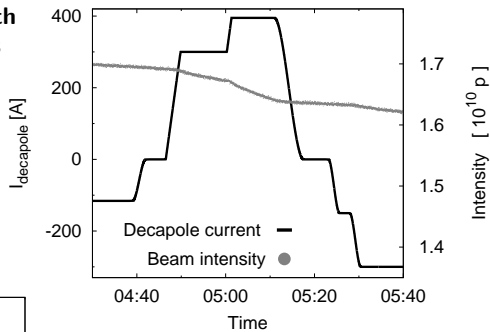
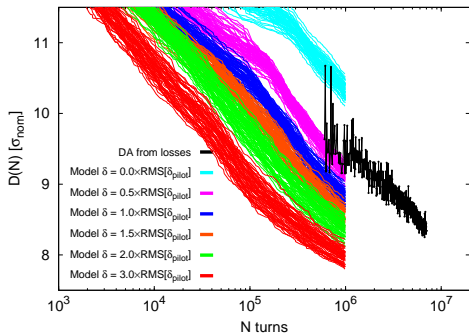
Detailed report found at: [\(CERN-ACC-Note-2016-0013\)](#)

■ Closed orbit and beta-beat have small impact on predicted DA

- replicate operational behaviour to create effective model
- avoids large number of virtual correctors, allowing simulations on LHC@home volunteer computing service

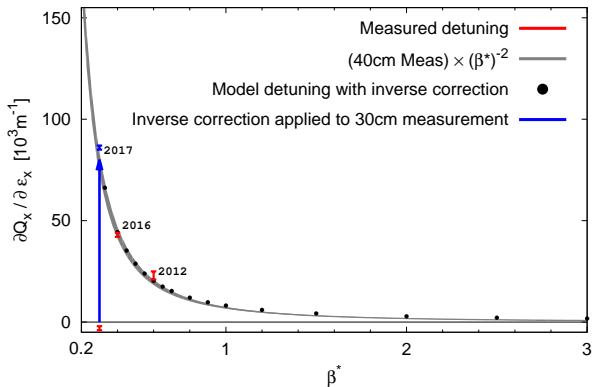


Measurements also performed with varying decapole strength in LHC arcs (450 GeV)



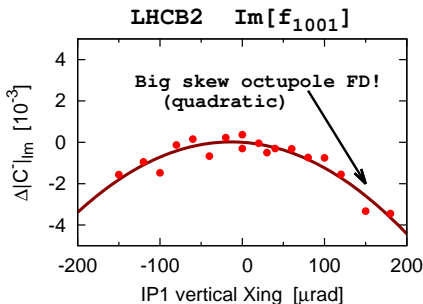
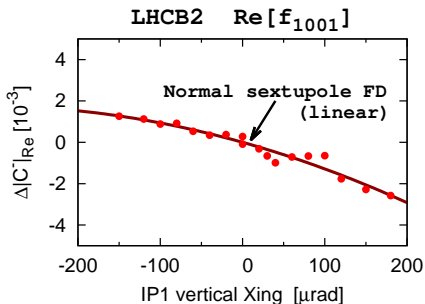
- DA variation with $\delta p/p$ was very small for octupole configurations at 450 GeV
- Strong decapole sources caused large momentum dependent DA in model

- Expect IR-tunespread to scale with $\sim (\beta^*)^{-2}$
- IR-tunespread appears consistent over extended period



Skew octupole compensation at $\beta^* = 0.4$ m

→ observe large feed-down to linear coupling



Difficult correction → a_4 corrector L1 dead

- Before correction: $\Delta|C^-|_{0 \rightarrow 150 \mu\text{rad}} = 5 \times 10^{-3}$
- After correction: $\Delta|C^-|_{0 \rightarrow 150 \mu\text{rad}} = 1.5 \times 10^{-3}$

Important for instabilities during crossing-angle levelling!