

半轻粲味介子衰变

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2. Semi-leptonic decays



Key point is to calculate form factors First try in the light-front quark model Wei Wang, Fu-Sheng Yu, Zhen-Xing Zhao

From Prof. Lu's slides







LHCb 物理理论与实验问题研讨会 Workshop on LHCb Physics 2016 Wuhan 2016年4月21-23日,中国武汉













Weak Decays of Doubly Heavy Baryon : $\Xi_{bc}^{0} \rightarrow pK^{-}$ and $\Xi_{cc}^{+} \rightarrow \Sigma_{++c}K^{-}$ *R.H. Li, C.D.Lu, W.Wang, F.S.Yu, Z.T. Zou*

Weak Decays of Doubly Heavy Baryon : the sequel

- Spectroscopy
- decay constant
- ➤ lifetime
- SU(3) Analysis
- > 1/2→1/2 case
- FCNC channels
- > 1/2→3/2 case
- Light quark decay



Observation of the doubly charmed baryon \varXi_{cc}^{++}

Phys.Rev.Lett. 119, 112001 (2017)

LHCb collaboration[†]

Abstract

A highly significant structure is observed in the $\Lambda_c^+ K^- \pi^+ \pi^+$ mass spectrum, where the Λ_c^+ baryon is reconstructed in the decay mode $pK^-\pi^+$. The structure is consistent with originating from a weakly decaying particle, identified as the doubly charmed baryon Ξ_{cc}^{++} . The mass, measured relative to that of the Λ_c^+ baryon, is found to be 3621.40 ± 0.72 (stat) ± 0.27 (syst) ± 0.14 (Λ_c^+) MeV/ c^2 , where the last uncertainty is due to the limited knowledge of the Λ_c^+ mass. The state is observed in a sample of proton-proton collision data collected by the LHCb experiment at a center-of-mass energy of 13 TeV, corresponding to an integrated luminosity of 1.7 fb⁻¹, and confirmed in an additional sample of data collected at 8 TeV.





Weak Decays of Doubly Heavy Baryon : $\Xi_{bc}^{0} \rightarrow pK^{-}$ and $\Xi_{cc}^{+} \rightarrow \Sigma_{++c}K^{-}$ *R.H. Li, C.D.Lu, W.Wang, F.S.Yu, Z.T. Zou*

Weak Decays of Doubly Heavy Baryons: the $1/2 \rightarrow 1/2$ case

Weak Decays of Doubly Heavy Baryons: the SU(3) Analysis

Weak Decays of Doubly Heavy Baryons: decay constant

Weak Decays of Doubly Heavy Baryons: lifetime

Weak Decays of Doubly Heavy Baryons: the FCNC channels

Weak Decays of Doubly Heavy Baryons: the $1/2 \rightarrow 3/2$ case





Quark-diquark picture

1707,02834,W.Wang, F.S.Yu, Z.X. Zhao



形状因子的计算



$$\langle B'(P', S'_{z})|(V - A)_{\mu}|B(P, S_{z})\rangle = \int \{d^{3}p_{2}\} \frac{\phi'^{*}(x', k'_{\perp})\phi(x, k_{\perp})}{2\sqrt{p_{1}^{+}p'_{1}^{+}(p_{1} \cdot \bar{P} + m_{1}M_{0})(p'_{1} \cdot \bar{P}' + m'_{1}M'_{0})}} \times \bar{u}(\bar{P}', S'_{z})\bar{\Gamma}'(p'_{1} + m'_{1})\gamma_{\mu}(1 - \gamma_{5})(p'_{1} + m_{1})\Gamma u(\bar{P}, S_{z})} \frac{1}{2}$$

 $[Q_2q](p_2)$



双粲重子的半轻衰变

 $\frac{\overline{K}^{0}}{\overline{K}^{0}} \frac{e^{+}}{\mu^{+}} \nu_{e}$

channels	$\Gamma/~{ m GeV}$	B	Γ_L/Γ_T
$\Xi_{cc}^{++} \to \Lambda_c^+ l^+ \nu_l$	1.08×10^{-14}	4.93×10^{-3}	8.50
$\Xi_{cc}^{++} \to \Sigma_c^+ l^+ \nu_l$	9.88×10^{-15}	4.50×10^{-3}	1.27
$\Xi_{cc}^{++} \to \Xi_c^+ l^+ \nu_l$	1.18×10^{-13}	5.39×10^{-2}	9.98
$\Xi_{cc}^{++}\to\Xi_c^{\prime+}l^+\nu_l$	1.32×10^{-13}	6.01×10^{-2}	1.41
$\Xi_{cc}^+ \to \Sigma_c^0 l^+ \nu_l$	1.97×10^{-14}	2.99×10^{-3}	1.27
$\Xi_{cc}^+ \to \Xi_c^0 l^+ \nu_l$	1.17×10^{-13}	1.77×10^{-2}	9.98
$\Xi_{cc}^+\to\Xi_c^{\prime 0}l^+\nu_l$	1.31×10^{-13}	1.99×10^{-2}	1.42
$\Omega_{cc}^+ \to \Xi_c^0 l^+ \nu_l$	5.42×10^{-15}	2.22×10^{-3}	9.14
$\Omega_{cc}^+ \to \Xi_c^{\prime 0} l^+ \nu_l$	6.07×10^{-15}	2.49×10^{-3}	1.34
$\Omega_{cc}^+ \to \Omega_c^0 l^+ \nu_l$	1.62×10^{-13}	6.65×10^{-2}	1.46

D⁺ DECAY MODES

(8.82±0.13) %	869
(8.74±0.19) %	865

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Weak Decays of Doubly Heavy Baryons: the SU(3) Analysis W. Wang, J. Xu, Z.P.Xing, 1707.06570









Decays into a light decuplet baryon and a charmed meson



SU(3)分析

宽度关系:

$$\begin{split} \Gamma(\Xi_{cc}^{++} \to \Lambda_c^+ \pi^+) &= \Gamma(\Xi_{cc}^{++} \to \Xi_c^+ K^+), \\ \Gamma(\Xi_{cc}^+ \to \Xi_c^+ K^0) &= \Gamma(\Omega_{cc}^+ \to \Lambda_c^+ \overline{K}^0), \\ \Gamma(\Omega_{cc}^+ \to \Xi_c^0 \pi^+) &= \Gamma(\Xi_{cc}^+ \to \Xi_c^0 K^+). \end{split}$$

$$\begin{split} \Gamma(\Xi_{cc}^{++} \to \Sigma_c^{++} \pi^0) &= \frac{1}{3} \Gamma(\Xi_{cc}^{++} \to \Sigma_c^{++} \eta), \\ \Gamma(\Xi_{cc}^{++} \to \Sigma_c^{+} \pi^+) &= \Gamma(\Xi_{cc}^{++} \to \Xi_c^{\prime+} K^+), \\ \Gamma(\Xi_{cc}^{+} \to \Sigma_c^{++} \pi^-) &= \Gamma(\Omega_{cc}^{+} \to \Sigma_c^{++} K^-), \\ \Gamma(\Xi_{cc}^{+} \to \Sigma_c^{0} \pi^+) &= \Gamma(\Omega_{cc}^{+} \to \Omega_c^{0} K^+), \\ \Gamma(\Xi_{cc}^{+} \to \Xi_c^{\prime+} K^0) &= \Gamma(\Omega_{cc}^{+} \to \Sigma_c^{+} \overline{K}^0), \\ \Gamma(\Omega_{cc}^{+} \to \Xi_c^{\prime0} \pi^+) &= \Gamma(\Xi_{cc}^{+} \to \Xi_c^{\prime0} K^+). \end{split}$$

Global fit in future?



双重重子寿命



literature	literature Ξ_{cc}^{++}		Ω_{cc}^+	
Karliner, Rosner, 2014	185	53		
Kiselev, Likhoded, 1998	430 ± 100	110 ± 10		
Kiselev, Likhoded,2002	460 ± 50	160 ± 50	270 ± 60	
Guberina, Melic, Stefancic, 1998	1550	220	250	
Chang, Li, Li, Wang, 2007	670	250	210	

 $\tau(\Xi_{cc}^{++}) \gg \tau(\Xi_{cc}^{+}) \sim \tau(\Omega_{cc})$





D-mesons

	$D^0 = (\bar{u}c)$	$D^+ = (\bar{d}c)$	$D_s^+ = (\bar{s}c)$
Mass (GeV)	1.86491(17)	1.8695(4)	1.9690(14)
Lifetime (ps)	0.4101(15)	1.040(7)	0.500(7)
$\tau(X)/\tau(D^0)$	1	2.536 ± 0.017	1.219 ± 0.017

$$\frac{\tau(D^+)}{\tau(D^0)}^{\text{HQE 2013}} = 2.2 \pm 0.4^{(\text{hadronic}) + 0.03(\text{scale})}_{-0.07} ,$$
$$\frac{\tau(D_s^+)}{\tau(D^0)}^{\text{HQE 2013}} = 1.19 \pm 0.12^{(\text{hadronic}) + 0.04(\text{scale})}_{-0.04}$$

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A. Lenz, T. Rauh, 1305.3588



双重重子寿命的计算

• 算符展开 $\hat{T} = T \left[i H_{eff}(x), H_{eff}(0) \right]$ $\Gamma(H_Q \to X) = \frac{1}{2m_{H_Q}} \operatorname{Im} \int d^4x \langle H_Q | \hat{T} | H_Q \rangle = \frac{1}{2m_{H_Q}} \langle H_Q | \hat{\Gamma} | H_Q \rangle,$ $\Gamma(H_Q \to X) = \frac{G_F^2 m_c^5}{192\pi^3} |V_{\rm CKM}|^2 \left(c_3 \frac{\langle H_c | \bar{c}c | H_c \rangle}{2m_{H_Q}} + c_5 \frac{\langle H_c | \bar{c}i\sigma_{\mu\nu}G^{\mu\nu}c | H_c \rangle}{2m_{H_Q}m_c^2} + c_6^i \frac{\langle H_c | (\bar{c}\Gamma_i q) (\bar{q}\Gamma_i c) | H_c \rangle}{2m_{H_Q}m_c^3} \right)$ $\Gamma_c = \frac{G_F^2 m_c^5}{102\pi^3} |V_{cs}|^2 c_{3,c}$ d.s С e⁺,μ⁺ v_e, v_μ



半轻D介子衰变



 \rightarrow D->P₁P₂|v

\blacktriangleright Why D->P₁P₂lv?

Theoretical Analysis



$D \rightarrow P \mid v \& D \rightarrow V \mid v$





• Hadronic current $(q^2 = (p_\ell + p_{\overline{\nu}_\ell})^2)$ in case of *D* decays to pseudoscalar meson $\langle P(p_\ell) | V^{\mu} | D(p_\ell) \rangle =$

- $f_+(q^2)$ and $f_0(q^2)$ are form factors
- neglecting the lepton mass only one form factor contributes

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cq}|^2 |p_P(q^2)|^3 f_+^P(q^2)$$

见刘朝峰报告

• Extract CKM matrix elements and test of LQCD calculations



$D \rightarrow P_1 P_2 Iv$

 $\overline{K}^0 e^+ \nu_e$ $\frac{\overline{K}^{0} \mu^{+} \nu_{\mu}}{\overline{K}^{-} \pi^{+} e^{+} \nu_{e}} \overline{K}^{*}(892)^{0} e^{+} \nu_{e}, \overline{K}^{*}(892)^{0} \rightarrow$ $\begin{array}{c} \kappa^{-}\pi^{+} \\ (\kappa^{-}\pi^{+})_{S-wave} e^{+}\nu_{e} \end{array}$ $\frac{\overline{K}^{*}(1410)^{0} e^{+} \nu_{e}}{\overline{K}^{*}(1410)^{0} \rightarrow K^{-} \pi^{+}}$ $\overline{K}_{2}^{*}(1430)^{0} e^{+} \nu_{e}$, $\overline{K}_2^*(1430)^0 \rightarrow K^- \pi^+$ $K^{-}\pi^{+}e^{+}\nu_{e}$ nonresonant $K^- \pi^+ \mu^+ \nu_\mu$ $\overline{K}^{*}(892)^{0'}\mu^{+}
u_{\mu}$, $\overline{K}^*(892)^0 \rightarrow K^- \pi^+$ $K^{-}\pi^{+}\mu^{+}\nu_{\mu}$ nonresonant $K^{-}\pi^{+}\pi^{0}\mu^{+}\nu_{\mu}$ $\pi^0 e^+ \nu_e$ $\eta e^+ \nu_e$ $\rho^0 e^+ \nu_e$ $\rho^0 \mu^+ \nu_\mu$ $\omega e^+ \nu_e$ $\eta'(958) e^+ \nu_e$ $\phi e^+ \nu_e$

($8.90\pm$	0.15) %		869
(9.3 \pm	0.7)%		865
($3.91\pm$	0.11) %		864
($3.68\pm$	0.10) %		722
	0.11) 10-3		
(2.20±	$(0.11) \times 10^{-3}$	e ,	_
< 6	$\times 10^{-3}$	CL=90%	_
< 5	$ imes 10^{-4}$	CL=90%	_
< 7	imes 10 ⁻³	CL=90%	864
($3.9 \pm$	0.4) %		851
($3.52\pm$	0.10) %		717
(2.1 \pm	0.5 $)\times10^{-3}$		851
< 1.6	imes 10 ⁻³	CL=90%	825
($4.05\pm$	$0.18) \times 10^{-3}$		930
($1.14\pm$	$0.10) \times 10^{-3}$		855
(2.18^+_{-})	$^{0.17}_{0.25})\times 10^{-3}$		774
(2.4 \pm	0.4) $\times10^{-3}$		770
($1.69\pm$	$0.11) \times 10^{-3}$		771
(2.2 \pm	0.5 $)\times10^{-4}$		689
< 1.3	imes 10 ⁻⁵	CL=90%	657



$$H = D.P.P.\lambda_p + D.\lambda_p \times \text{Tr}[P.P]$$

c->d: 16

c->s: 14



Scalar Mesons: Two nonets





标量粒子: 四夸克vs分子态



S





如何区分两、四夸克态?



Scalar Mesons: Two nonets

$$\begin{aligned} |f_0(600)\rangle &= \frac{1}{\sqrt{2}} (|\bar{u}u\rangle + |\bar{d}d\rangle) \equiv |\bar{n}n\rangle, \\ |f_0(980)\rangle &= |\bar{s}s\rangle, \qquad |a_0^0(980)\rangle = \frac{1}{\sqrt{2}} (|\bar{u}u\rangle - |\bar{d}d\rangle), \\ |a_0^-(980)\rangle &= |\bar{u}d\rangle, \qquad |a_0^+(980)\rangle = |\bar{d}u\rangle. \\ |f_0\rangle &= |\bar{s}s\rangle \cos\theta + |\bar{n}n\rangle \sin\theta, \\ |\sigma\rangle &= -|\bar{s}s\rangle \sin\theta + |\bar{n}n\rangle \cos\theta. \end{aligned}$$



Lu, WW, PRD82, 034016 (201

$$\hat{\mathcal{A}} \equiv \mathcal{A}(D^+ \to a_0^0 l^+ \nu). \qquad \qquad \mathcal{A}(D^+ \to f_0 l^+ \nu) = -\sin \theta \hat{\mathcal{A}}, \\ \mathcal{A}(D^+ \to \sigma l^+ \nu) = -\cos \theta \hat{\mathcal{A}},$$

$$\mathcal{B}(D^+ \to a_0^0 l^+ \nu) = \mathcal{B}(D^+ \to f_0 l^+ \nu) + \mathcal{B}(D^+ \to \sigma l^+ \nu)$$



Scalar Mesons: Two nonets

$$\begin{aligned} |\sigma\rangle &= \bar{u}u\bar{d}d, \quad |f_0\rangle = |\bar{n}n\bar{s}s\rangle, \\ |a_0^0\rangle &= \frac{1}{\sqrt{2}}(\bar{u}u - \bar{d}d)\bar{s}s, \\ |a_0^+\rangle &= |\bar{d}u\bar{s}s\rangle, \quad |a_0^-\rangle = |\bar{u}d\bar{s}s\rangle, \\ |\kappa^+\rangle &= |\bar{s}u\bar{d}d\rangle, \quad |\kappa^0\rangle = |\bar{s}d\bar{u}u\rangle, \\ |\bar{\kappa}^0\rangle &= |\bar{d}s\bar{u}u\rangle, \quad |\kappa^-\rangle = |\bar{u}s\bar{d}d\rangle. \end{aligned}$$

$$\begin{array}{ll} |f_0\rangle &=& |\bar{n}n\bar{s}s\rangle\cos\phi + |\bar{u}u\bar{d}d\rangle\sin\phi, \\ |\sigma\rangle &=& -|\bar{n}n\bar{s}s\rangle\sin\phi + |\bar{u}u\bar{d}d\rangle\cos\phi, \end{array}$$



$$\hat{\mathcal{A}}\equiv \mathcal{A}(D^+\to a_0^0 l^+\nu).$$

$$\mathcal{A}(D^+ \to f_0 l^+ \nu) = -(\cos \phi + \sqrt{2} \sin \phi) \hat{\mathcal{A}},$$

$$\mathcal{A}(D^+ \to \sigma l^+ \nu) = (\sin \phi - \sqrt{2} \cos \phi) \hat{\mathcal{A}},$$

$$\begin{split} \mathcal{B}(D^+ \to a_0^0 l^+ \nu) &= \frac{1}{3} [\mathcal{B}(D^+ \to f_0 l^+ \nu) + \mathcal{B}(D^+ \to \sigma l^+ \nu)]. \\ R &= \frac{\mathcal{B}(D^+ \to f_0 l^+ \nu) + \mathcal{B}(D^+ \to \sigma l^+ \nu)}{\mathcal{B}(D^+ \to a_0^0 l^+ \nu)}. = \begin{cases} 1 & \text{two quark} \\ 3 & \text{tetra-quark} \end{cases}. \end{split}$$

-



分子态: Scalar form factors in xPT









Red: P-wave Blue: S-wave Black: Total S

Y.J. Shi, WW, S. Zhao 1701.07571



如何区分标量粒子态: $D \rightarrow \pi^+\pi^-ev$



分子态模型: Red: P-wave Blue: S-wave Black: Total

The S-wave branching fraction for $2m_{\pi} < m_{\pi\pi} < 1.0$ GeV is given as

 $\mathcal{B}(D^- \to (\pi^+\pi^-)_S e^-\bar{\nu}) = (6.99 \pm 2.46) \times 10^{-4},$ $\mathcal{B}(D^- \to (\pi^+\pi^-)_S \mu^-\bar{\nu}) = (7.20 \pm 2.52) \times 10^{-4}.$

Y.J. Shi, WW, S. Zhao 1701.07571

$$R = \frac{\mathcal{B}(D^+ \to f_0 l^+ \nu) + \mathcal{B}(D^+ \to \sigma l^+ \nu)}{\mathcal{B}(D^+ \to a_0^0 l^+ \nu)} = \begin{cases} 1 & \text{two quark} \\ 3 & \text{tetra-quark} \end{cases}.$$

Lu, WW, PRD82, 034016 (2010)





 $d^{5}\Gamma = \frac{G_{F}^{2}||V_{cs}||^{2}}{(4\pi)^{6}m_{D}^{3}}X\beta I(m^{2}, q^{2}, \theta_{K}, \theta_{e}, \chi)$



$$\begin{aligned} \frac{d^{5}\Gamma}{dm_{K\pi}^{2}dq^{2}d\cos\theta_{K}d\cos\theta_{l}d\phi} &= \frac{3}{8} \Big[I_{1}(q^{2},m_{K\pi}^{2},\theta_{K}) \\ &+ I_{2}(q^{2},m_{K\pi}^{2},\theta_{K})\cos(2\theta_{l}) \\ &+ I_{3}(q^{2},m_{K\pi}^{2},\theta_{K})\sin^{2}\theta_{l}\cos(2\phi) \\ &+ I_{4}(q^{2},m_{K\pi}^{2},\theta_{K})\sin(2\theta_{l})\cos\phi \\ &+ I_{5}(q^{2},m_{K\pi}^{2},\theta_{K})\sin(\theta_{l})\cos\phi \\ &+ I_{6}(q^{2},m_{K\pi}^{2},\theta_{K})\cos\theta_{l} \\ &+ I_{7}(q^{2},m_{K\pi}^{2},\theta_{K})\sin(2\theta_{l})\sin\phi \\ &+ I_{8}(q^{2},m_{K\pi}^{2},\theta_{K})\sin(2\theta_{l})\sin\phi \end{aligned}$$

 $+I_9(q^2, m_{K\pi}^2, \theta_K) \sin^2 \theta_l \sin(2\phi) \Big],$

C. L. Y. Lee, M. Lu, and M. B. Wise, Phys. Rev. D 46, 5040 (1992).

 $\times dm^2 dq^2 d\cos(\theta_K) d\cos(\theta_e) d\chi.$

Meissner, WW, JHEP 1401 (2014) 107





$$\frac{d^{3}\Gamma}{dq^{2}dm_{K\pi}^{2}d\cos\theta_{K}} = \frac{1}{8} \left\{ (4+2\hat{m}_{l}^{2})|A_{0}^{0}|^{2} + 6\hat{m}_{l}^{2}|A_{t}^{0}|^{2} + \sqrt{3}(8+4\hat{m}_{l}^{2})\cos\theta_{K}\operatorname{Re}[A_{0}^{0}A_{0}^{1*}] + 12\sqrt{3}\hat{m}_{l}^{2}\cos\theta_{K}\operatorname{Re}[A_{t}^{0}A_{t}^{1*}] + (12+6\hat{m}_{l}^{2})|A_{0}^{1}|^{2}\cos^{2}\theta_{K} + 18\hat{m}_{l}^{2}\cos^{2}\theta_{K}|A_{t}^{1}|^{2} + (6+3\hat{m}_{l}^{2})\sin^{2}\theta_{K}(|A_{\perp}^{1}|^{2} + |A_{\parallel}^{1}|^{2}) \right\}.$$
(4.23)

$$A_{FB}^{K} \equiv \left[\int_{0}^{1} - \int_{-1}^{0} \right] d\cos\theta_{K} \frac{d^{3}\Gamma}{dq^{2}dm_{K\pi}^{2}d\cos\theta_{K}}$$
$$= \frac{\sqrt{3}}{2} (2 + \hat{m}_{l}^{2}) \operatorname{Re}[A_{0}^{0}A_{0}^{1*}] + \frac{3\sqrt{3}}{2} \hat{m}_{l}^{2} \operatorname{Re}[A_{t}^{0}A_{t}^{1*}]$$





FIG. 2 (color online). (a) Comparison between the S-wave phase measured in various experiments analyzing the $D^+ \rightarrow K^- \pi^+ \pi^+$ channel (E791 [6], FOCUS [7,8], and CLEO [9]) and a fit to LASS data (continuous line). The dashed line corresponds to the extrapolation of the fitted curve. Phase measurements from D^+ decays are shifted to be equal to zero at $m_{K\pi} = 0.67 \text{ GeV}/c^2$. (b) The S-wave amplitude measured in various experiments is compared with the elastic expression. Normalization is arbitrary between the various distributions.

BaBar:Phys.Rev. D83 (2011) 072001





Points with error bars by BESIII the solid line corresponds to LASS parameterization





BESIII, 1512.08627

Points with error bars by BESIII the solid line corresponds to LASS parameterization

Chiral PT: Doring, Meissner, WW,1307.0947





50:1





50:1

Expected data set increase and ~ increase in inst. Luminosity

50 _	LHCb Upgrade _	Belle II	BaBar + Belle	?
1	LHCb_today	$\overline{\text{BaBar} + \text{Belle}}$	CLEO –	BESIII

the energy increase from 7/8 TeV to 13 TeV at the LHC



Summary



□ 双粲重子

▶双粲重子弱衰变:续集

\square D->P₁P₂I v

▶ 检验标量粒子内部结构

▶ 测量散射相移

▶ 手征有效理论+QCD微扰理论





谢谢大家!

请批评指正!