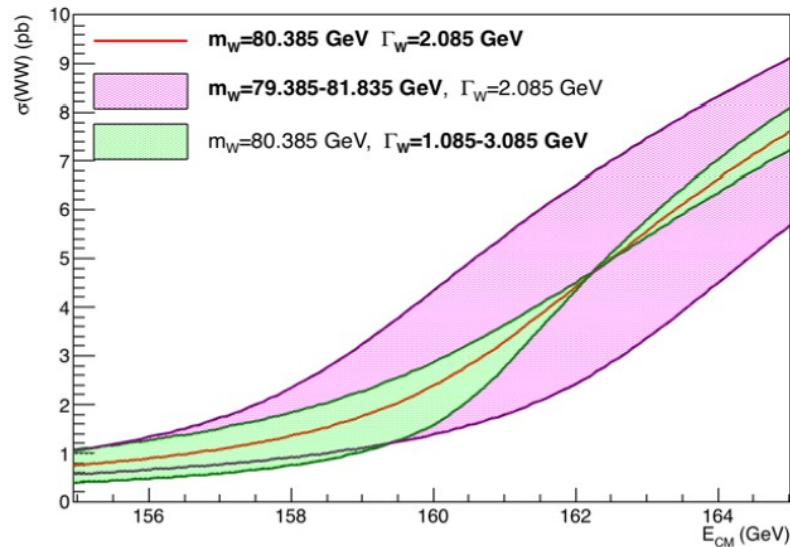


# Measurement of $m_W$ at threshold (thoughts)

- A few remarks about the post-LHC context
  - Last measurements and combination:
    - CDF :  $\delta m_W \sim 19$  MeV; D0 :  $\delta m_W \sim 23$  MeV (Tevatron average : 15 MeV)
    - ATLAS :  $\delta m_W \sim 19$  MeV
    - New average :  $\delta m_W \sim 11-13$  MeV, depending on uncertainty correlations
  - Foreseen sensitivity : 5-10 MeV, assuming measurements at roots = 5, 7, 8 and 13 TeV.
  - Further improvement might be possible with the upgraded LHC detectors, in the HLLHC era (using dedicated, low pile-up runs)
- To be interesting, the goal at CEPC should be well below 5 MeV

# Recent study : arXiv:1703.01626

- Studied the statistical precision on  $m_W$  from 1-point and 2-point cross section measurements



1-point example :  
At 162.3 GeV, the cross section is maximally sensitive to  $m_W$ , and insensitive to the width

Statistical uncertainty assuming  $15 \text{ ab}^{-1}$  (one FCC-ee year):  $\delta m_W \sim 0.25 \text{ MeV}$

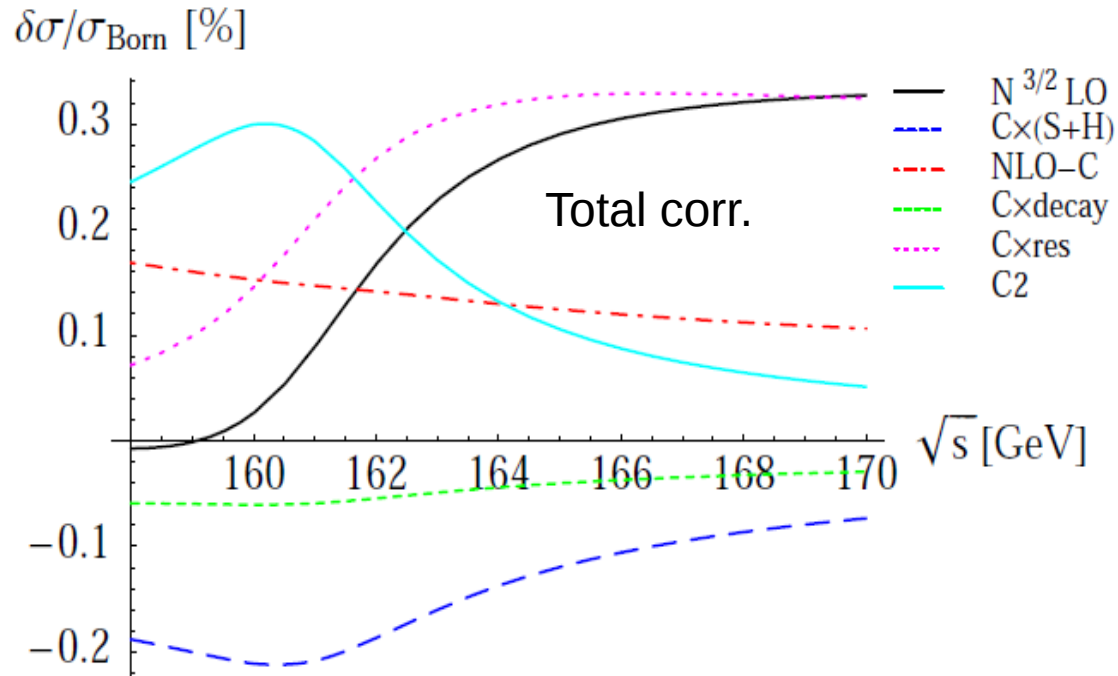
Requirements on systematic uncertainties:

Beam energy	$dE/E$	$< 3 \cdot 10^{-6}$	OK?
Luminosity	$dL/L$	$< 10^{-4}$	OK?
Cross section prediction	$d\sigma_{\text{th}}/\sigma_{\text{th}}$	$< 10^{-4}$	Limiting

With two-point measurement, achieve  $\delta m_W \sim 0.4 \text{ MeV}$ ,  $\delta \Gamma_W \sim 1 \text{ MeV}$

# Present theoretical uncertainties

- Contributions to the NNLO corrections (arXiv:0807.0102):



The authors estimate that the uncertainties from missing NNLO corrections amount to  $\delta m_W \sim 3$  MeV.  $\delta m_W \sim 1$  MeV is deemed achievable in the mid-term.

Note : the different terms have rather different energy dependence – the theoretical uncertainty is not reduced by measuring at different points

# Situation with $3.2 \text{ ab}^{-1}$

- Statistical uncertainty:  $\delta m_W \sim 0.6 \text{ MeV}$
- Requirements on systematic uncertainties:
  - Beam energy  $dE/E < 10^{-5}$  OK?
  - Luminosity  $dL/L < 2 \cdot 10^{-4}$  OK?
  - Cross section prediction  $d\sigma_{\text{th}}/\sigma_{\text{th}} < 2 \cdot 10^{-4}$  Still limiting
- Although the  $W$  width is not too important for BSM, measuring the cross section at at least two points allows to measure both  $m_W$  and  $\Gamma_W$ , making the mass measurement less model-dependent
- Brief summary : at present,  $3.2 \text{ ab}^{-1}$  is sufficient to make the statistical uncertainty sub-dominant, for a model-independent measurement at the  $\sim 2\text{-}3 \text{ MeV}$  level.

Further requirements are that

- Complete NNLO corrections become available for  $ee \rightarrow 4f$  ( $\rightarrow \delta m_W \sim 1 \text{ MeV}$ )
- The luminosity can be measured at the 0.02% level
- The beam energy can be measured with a precision of  $10^{-5}$

# Further studies

- Implement realistic running scenarios (ie cross section measurements at 1 / 2 / 5 points in energy, with a total luminosity budget of  $3.2 \text{ ab}^{-1}$ ), detector acceptance, luminosity uncertainties etc, to produce a complete uncertainty table.
- I would be happy to collaborate on these issues, please let me know.

## References (for my own record...)

- Beneke et al, arXiv:0707.0773v2, arXiv:0807.0102v1
- Snowmass 2013, arXiv:1310.6708v1
- Jadach et al, arXiv:hep-ph/0103163v3
- Dittmaier et al, arXiv:hep-ph/0505042v3
- FCC study, arXiv:1703.01626v1