#### A global analysis approach

A single parameter quantifies both Higgs Br precision and detector performance

P. Shen and G. Li

CEPC day, 2019-05-31, IHEP

# Outline

- Motivation
- Method
- Some numerical results with toy MC
- Summary & Plan

- Competition from both HL-LHC and FCC-ee
- FCC-ee
- ATLAS-CMS extrapolation range from 2 - 4%, with the exception of that on  $B^{\mu\mu}$  at 8% and on  $B^{Z\gamma}$  at 19%.



#### We possess what the LHC lacks (人无我有)

- Tagging method, absolute/model-independent
- All Higgs decays accessible except e and uds
- Multinomial distribution: statistical constraint













### **Detector design & Optimization**

Multi-purpose optimization: a bunch of benchmarks — A single parameter is favored, which means single-purpose optimization

Take the simplest case as an example -2 decay modes

### Efficiency matrix Based on MC, no dependence on Br's



A produced final state reconstructed as final state

Measurement is DEMODULATION All knowns on the right Goal: solve N and minimize its uncertainty



#### Two decays, neglect other background: p+q=1 — binomial distribution

Individual measurementsGlobal measurement
$$\sigma_{n_1} = \sqrt{N\epsilon_{11}}$$
 $\sigma_{n_1} = \sqrt{Np(1-p)\epsilon_{11}}$  $\sigma_{n_2} = \sqrt{N\epsilon_{22}}$  $\sum N_i = N$ 

Based on text book, or <u>https://en.wikipedia.org/wiki/Binomial\_distribution</u> https://en.wikipedia.org/wiki/Multinomial\_distribution

Decay – multinomial distributions

### Further the full covariance

$$V = egin{pmatrix} Npq & -Npq \ -Npq & Npq \end{pmatrix}$$

100% anti-correlated between the two decays! This can be used in data analysis to improve precisions.

#### **Successful examples**

- Precision measurement of the D<sup>\*0</sup> decay branching fractions by BESIII, Phys.Rev. D91 (2015) no.3, 031101
- Branching ratios of tau decays by ALEPH, Physics Reports 421 (2005) 191–284

### Let's see how it happens

$$ec{\sigma}_n = \left( egin{array}{c} ec{\sigma}_{n_1} \ ec{\sigma}_{n_2} \end{array} 
ight) ,$$

$$\sigma_{n_i}^2 = \vec{\sigma}_{n_i} \cdot \vec{\sigma}_{n_i}, \ \sigma_{n_{ij}} = \sigma_{n_{ji}} = \sigma_{n_1} \sigma_{n_2} \rho_{ij} = \vec{\sigma}_{n_i} \cdot \vec{\sigma}_{n_j},$$

$$\rho_{ij} = \frac{\vec{\sigma}_{n_i} \cdot \vec{\sigma}_{n_j}}{\sigma_{n_1} \sigma_{n_2}},$$

#### Matrix: compact and easy to expand to higher dimension

$$\Sigma^{n} = \vec{\sigma}_{n} \vec{\sigma}_{n}^{T} = \begin{pmatrix} \vec{\sigma}_{n_{1}} \\ \vec{\sigma}_{n_{2}} \end{pmatrix} \begin{pmatrix} \vec{\sigma}_{n_{1}} \\ \vec{\sigma}_{n_{2}} \end{pmatrix}^{T}$$
$$= \begin{pmatrix} \sigma_{n_{1}}^{2} & \sigma_{n_{12}} \\ \sigma_{n_{21}} & \sigma_{n_{2}}^{2} \end{pmatrix}$$

### Space transformation n—>N



 $ec{\sigma}_N = E^{-1}ec{\sigma}_n$ 

$$J_{Nn} = E^{-1} = rac{1}{|E|} egin{pmatrix} \epsilon_{22} & -\epsilon_{12} \ -\epsilon_{21} & \epsilon_{11} \end{pmatrix} \equiv rac{J_N}{|E|}$$

# Space transformation N—>B

$$J_{BN} = rac{1}{N^2}igg(egin{array}{cc} N_2 & -N_1 \ -N_2 & N_1 \ \end{pmatrix} = rac{J_B}{N^2}$$

• Features

 $\mathbf{V}$  Variance of B proportional to  $1/(N^4|\mathbf{E}|^2)$ 

**№** N<sup>4</sup> : statistical power

E|<sup>2</sup> proportional to the performance of Detector x Reconstruction x Analysis

Same uncertainties for both two Br's

$$ec{\sigma}_B \!= J_{BN} J_{Nn} ec{\sigma}_n \!= rac{igg( egin{array}{c} n_2 ec{\sigma}_1 \!-\! n_1 ec{\sigma}_2 \ -\! n_2 ec{\sigma}_1 \!+\! n_1 ec{\sigma}_2 igg) \ N^2 |E| \end{array}$$

$$egin{split} \Sigma_B &= rac{ec{\sigma}_B ec{\sigma}_B^T}{N^4 |E|^2} \ &= rac{[J_B J_N ec{\sigma}_n] [J_B J_N ec{\sigma}_n]^T}{N^4 |E|^2} \ &= rac{(n_2 \sigma_{n_1} + n_1 \sigma_{n_2})^2}{N^4 |E|^2} igg( egin{array}{c} 1 & -1 \ -1 & 1 \end{pmatrix} \end{split}$$

### Three or more decay modes



Similar features as N=2

Numerical results with toy MC

# On backgrounds

- Two type of backgrounds
  - Non-uuH backgrounds: subtracted by fitting, enlarging statistical uncertainty of n<sub>i</sub>
  - uuH backgrounds(cross talk): the efficiency matrix dealing with them

➢N and n<sub>i</sub>





- 9 Higgs decays accessible at CEPC
- Di-muon, Di-photon, and gamma Z are tiny: 0.02%, 0.23%, and 0.15%, respectively
- cc contaminated by bb due to large bb Br
- ZZ important for Higgs Width



#### Solve N<sub>i</sub> by minimizing the chi<sup>2</sup> with constraint

$$\chi^2 = \sum_i rac{(\sum \epsilon_{ij} N_j - n_i)^2}{\sigma_{n_i}^2} + rac{(\sum_l N_l - N)^2}{\sigma_N^2}$$

Higgs -> cc, bb, mm, tt, gg, aa, aZ, ZZ, WW 1 2 3 4 5 6 7 8 9

<i>,</i> ,		,									,
$\begin{pmatrix} n_1 \end{pmatrix}$		$\left( \epsilon_{11} \right)$	$\epsilon_{12}$	$\epsilon_{13}$	$\epsilon_{14}$	$\epsilon_{15}$	$\epsilon_{16}$	$\epsilon_{17}$	$\epsilon_{18}$	$\epsilon_{19}$	(N
$n_2$		$\epsilon_{21}$	$\epsilon_{22}$	$\epsilon_{23}$	$\epsilon_{24}$	$\epsilon_{25}$	$\epsilon_{26}$	$\epsilon_{27}$	$\epsilon_{28}$	$\epsilon_{29}$	N
$n_3$		$\epsilon_{31}$	$\epsilon_{32}$	$\epsilon_{23}$	$\epsilon_{34}$	$\epsilon_{35}$	$\epsilon_{36}$	$\epsilon_{37}$	$\epsilon_{38}$	$\epsilon_{39}$	N
$n_4$		$\epsilon_{41}$	$\epsilon_{42}$	$\epsilon_{33}$	$\epsilon_{44}$	$\epsilon_{45}$	$\epsilon_{46}$	$\epsilon_{47}$	$\epsilon_{48}$	$\epsilon_{49}$	N
$n_5$	=	$\epsilon_{51}$	$\epsilon_{52}$	$\epsilon_{43}$	$\epsilon_{54}$	$\epsilon_{55}$	$\epsilon_{56}$	$\epsilon_{57}$	$\epsilon_{58}$	$\epsilon_{59}$	N
$n_6$		$\epsilon_{61}$	$\epsilon_{62}$	$\epsilon_{53}$	$\epsilon_{64}$	$\epsilon_{65}$	$\epsilon_{66}$	$\epsilon_{67}$	$\epsilon_{68}$	$\epsilon_{69}$	N
$n_7$		$\epsilon_{71}$	$\epsilon_{72}$	$\epsilon_{63}$	$\epsilon_{74}$	$\epsilon_{75}$	$\epsilon_{76}$	$\epsilon_{77}$	$\epsilon_{78}$	$\epsilon_{79}$	N
$n_8$		$\epsilon_{81}$	$\epsilon_{82}$	$\epsilon_{73}$	$\epsilon_{84}$	$\epsilon_{85}$	$\epsilon_{86}$	$\epsilon_{87}$	$\epsilon_{88}$	$\epsilon_{89}$	N
$\left( \begin{array}{c} n_9 \end{array} \right)$		$\left( \epsilon_{91} \right)$	$\epsilon_{92}$	$\epsilon_{83}$	$\epsilon_{94}$	$\epsilon_{95}$	$\epsilon_{96}$	$\epsilon_{97}$	$\epsilon_{98}$	$\epsilon_{99}$ /	$\setminus N$

#### Neglect e and uds decays. Bear in mind: constraint

$$\sum_{i} N_i = N^{tag} \text{ or } \sum_{i} B_i = 1$$

$$B_i = rac{N_i}{N}$$

# Statistical limit

- ▶99% efficiency,
- ➡no cross talk,
- no other backgrounds
- eeH and qqH as good as mumuH

	0.99	0	0	0	0	0	0	0	0 \
	0	0.99	0	0	0	0	0	0	0
	0	0	0.99	0	0	0	0	0	0
	0	0	0	0.99	0	0	0	0	0
E =	0	0	0	0	0.99	0	0	0	0
	0	0	0	0	0	0.99	0	0	0
	0	0	0	0	0	0	0.99	0	0
	0	0	0	0	0	0	0	0.99	0
	0	0	0	0	0	0	0	0	0.99

 $N = L imes (\sigma_{\mu\mu H} + \sigma_{eeH} + \sigma_{qqH}) = 5600 imes (6.77 + 7.04 + 136.81) = 843,372$ 

#### Ideal case: eeH, qqh as good as uuH No background, no cross talk, multinomial uncertainties, and constraint





$$\sigma_{n_i} = \sqrt{Np(1-p)\epsilon_{ii}}$$

		MLT		POS
Bcc	2.713%	0.650% (	0.655%	0.664%)
Bbb	57.799%	0.086%	0.094%	0.144%)
Bmm	0.023%	7.190% 🔇	7.197%	7.198%)
Btt	6.319%	0.413% (	0.421%	0.435%)
Bgg	8.619%	0.347% (	0.356%	0.373%)
Baa	0.227%	2.294% (	2.296%	2.299%)
BaZ	0.150%	2.818% (	2.820%	2.822%)
BZZ	2.647%	0.658%	0.664%	0.673%)
BWW	21.496%	0.198%	0.209%	0.236%

#### More realistic: eeH, qqh as good as uuH 100% background, no cross talk, multinomial uncertainties, and constraint





$$\sigma_{n_i} = \sqrt{Np(1-p)\epsilon_{ii}}$$

		MLT		POS
Bcc	2.713%	0.773% (	0.779%	0.790%)
Bbb	57.799%	0.102% (	0.111%	0.171%)
Bmm	0.023%	8.547%	8.559%	8.560%)
Btt	6.319%	0.492%(	0.501%	0.518%)
Bgg	8.619%	0.413% (	0.424%	0.443%)
Baa	0.227%	2.728% (	2.731%	2.734%)
BaZ	0.150%	3.350% (	3.353%	3.356%)
BZZ	2.647%	0.783% (	0.789%	0.800%)
BWW	21.496%	0 235% (	0.249%	0 281%)

# Discussion

- qqH and eeH not good as uuH, but more statistics
- No full cross talk information in current analyses
- Degrading in real analysis and lots of compromises
- This approach can improve Higgs branching ratio measurement and set a statistical limit

# Efficiency matrix



#### Efficiency matrix

- Not necessary to know the branching ratios of Higgs decays
- Quantifies the detector/software/analysis performance with a single parameter det E
- It could be useful for detector optimization

#### A single purpose optimization instead of that of a bunch of benchmarks



Physics performance can be parameterized as a function of several parameters, or global precision of a set of benchmark processes or equivalent determinant of efficiency matrix [E]

Difficult



Now problem successfully becomes how to Maximize |E|<sup>2</sup>





- N=2, the maximum |E| : area of a square
- N=3, the maximum |E| : volume of a cube
- N>3, ...
- : volume of a HyperCube



Detector name: HC HyperCube or HiggsCube



# Summary and plan

- There should be at least one detector dedicated for Higgs study at CEPC
- Global analysis with extra constraint can improve precision of the Higgs decay branching ratios, but not significantly.
- Global analysis of e+e->u+u-H, H-> all 9 decay branching ratios as "benchmark" to optimize detector, software, and analysis, which has a unique parameter and is easy to quantify.
- Using fast simulation + global analysis + machine learning to maximize |E| is a new approach

• Including eeH and qqH could be better and difficult, but not impossible ...