

# Charm meson leptonic and semileptonic decays at BESIII

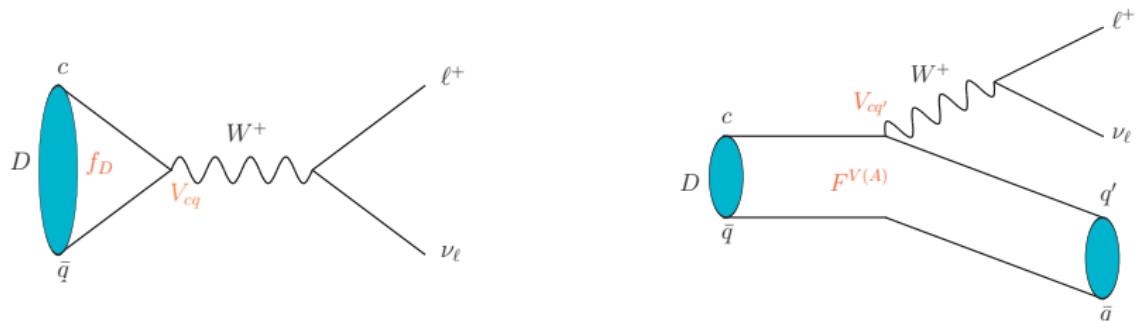
Sifan Zhang on behalf of the BESIII collaboration

NJU, IHEP

November 2, 2019

Joint Workshoop on Charmed Hadron Decays @ BESIII, BELLE, LHCb 2019  
Shanxi Normal University, Linfen

# Motivation



$$\mathcal{M} \propto |V_{cs(d)}| H^\mu L_\mu \quad q^\mu L_\mu \rightarrow 0 \text{ when } m_\ell \rightarrow 0$$

$$\langle P(p_2) | V^\mu | D(p_1) \rangle = f_+(q^2) [P^\mu - \frac{M_1^2 - M_2^2}{q^2} q^\mu] + f_0(q^2) \frac{M_1^2 - M_2^2}{q^2} q^\mu$$

$$\langle V(p_2, \epsilon_2) | V^\mu - A^\mu | D(p_1) \rangle =$$

$$-(M_1 + M_2) \epsilon_2^{*\mu} A_1(q^2) + \frac{\epsilon_2^{*q}}{M_1 + M_2} P^\mu A_2(q^2) +$$

$$2M_2 \frac{\epsilon_2^{*q}}{q^2} q^\mu [A_3(q^2) - A_0(q^2)] + \frac{2i\epsilon_{\mu\nu\rho\sigma}\epsilon^{*\nu} p_1^\rho p_2^\sigma}{M_1 + M_2} V(q^2)$$

$$r_V = \frac{V(0)}{A_1(0)}$$

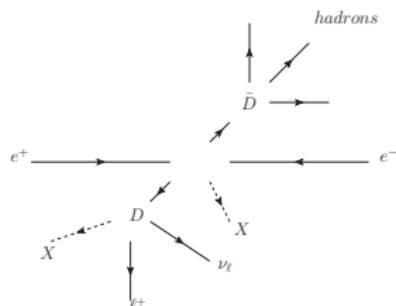
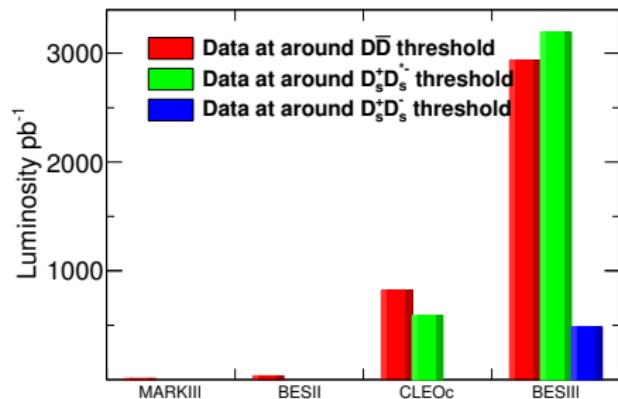
$$r_2 = \frac{A_2(0)}{A_1(0)}$$

$$H^\mu = f_D p_D^\mu$$

- test the unitarity of quark mixing matrix and search for new physics.
- test the theoretical calculation on decay constants and form factors, especially LQCD.
- test the lepton flavor universality.
- help to understand the internal structure of light scalar mesons.

# Experiments at the charm factory

Pair production at threshold, high efficiency and very low background.



With fully reconstructed tracks, neutrino information can be accessed via missing energy and momentum

$$N_{\text{ST}}^i = \frac{1}{2} N_{\text{miss}} \mathcal{B}_{\text{ST}}^i \epsilon_{\text{ST}}^i$$

$$N_{\text{DT}}^i = \frac{1}{2} N_{\text{miss}} \mathcal{B}_{\text{DT}}^i \mathcal{B}_{\text{sig}} \epsilon_{\text{DT}}^i$$

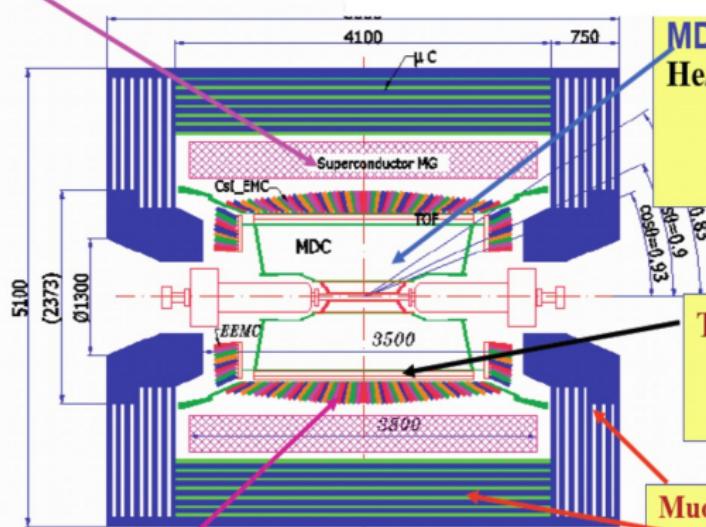
$$U_{\text{miss}} = E_{\text{miss}} - |\vec{p}|_{\text{miss}}$$

$$M_{\text{miss}}^2 = E_{\text{miss}}^2 - |\vec{p}|_{\text{miss}}^2$$

# BESIII

Magnet: 1 T Super conducting

Nucl. Instr. Meth. A614, 345 (2010)



EMC: CsI crystal, 28 cm  
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$   
 $\sigma_z = 0.6 \text{ cm}/\sqrt{E}$

Data Acquisition:  
Event rate = 4 kHz  
Total data volume ~ 50 MB/s

MDC: small cell & Gas:  
He/C<sub>3</sub>H<sub>8</sub> (60/40), 43 layers  
 $\sigma_{xy} = 130 \mu\text{m}$   
 $\sigma_p/p = 0.5\% @ 1 \text{ GeV}$   
 $dE/dx = 6\%$

TOF:  
 $\sigma_t = 100 \text{ ps}$  Barrel  
 $110 \text{ ps}$  Endcap

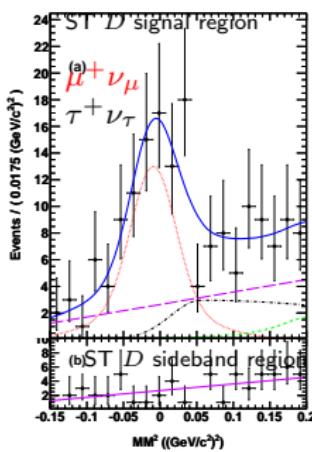
Muon ID: 9 layers RPC  
8 layers for endcap

60 ps for ETOF after  
upgraded in 2015

# $D_s^+$ leptonic decays

BESIII PRD94(2016)072004

BESIII@4.009



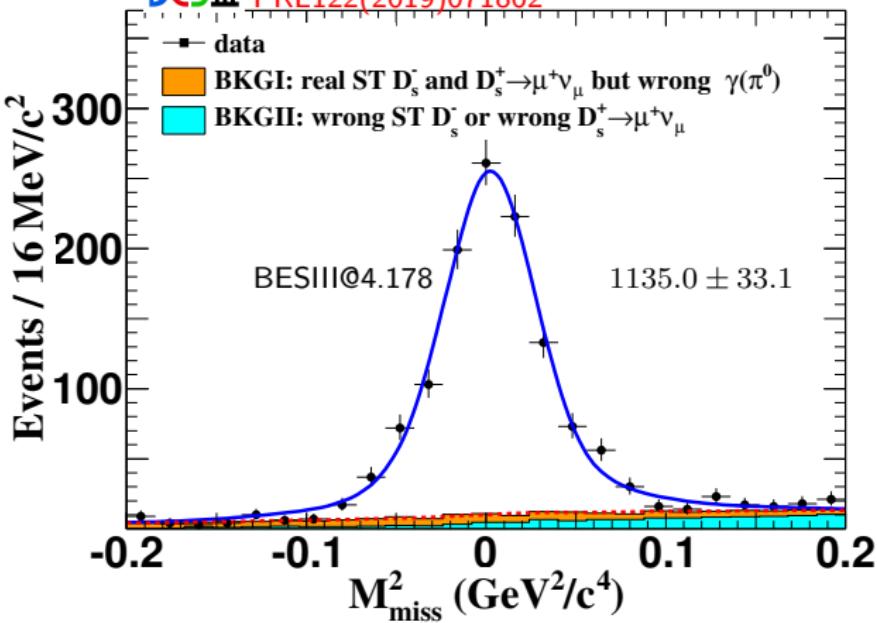
$$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (5.17 \pm 0.75 \pm 0.21) \times 10^{-3}$$

$$\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (3.28 \pm 1.83 \pm 0.37) \%$$

$$f_{D_s^+} |V_{cs}| = 239 \pm 17 \pm 5 \text{ MeV with } \mu^+ \nu_\mu$$

$$f_{D_s^+} |V_{cs}| = 193 \pm 54 \pm 11 \text{ MeV with } \tau^+ \nu_\tau$$

BESIII PRL122(2019)071802

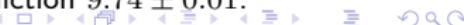


$$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (5.49 \pm 0.16 \pm 0.15) \times 10^{-3}$$

$$f_{D_s^+} |V_{cs}| = 246.2 \pm 3.6 \pm 3.5$$

$$R_{D_s^+} = \frac{\Gamma(D_s^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D_s^+ \rightarrow \mu^+ \nu_\mu)} = 10.19 \pm 0.52$$

$$\text{SM prediction } 9.74 \pm 0.01.$$



# Comparison of $|V_{cs}|$ and $f_{D_s^+}$

Inputs:

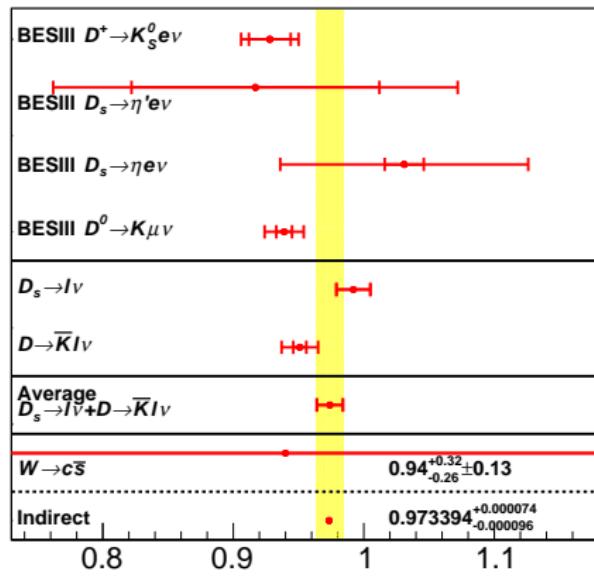
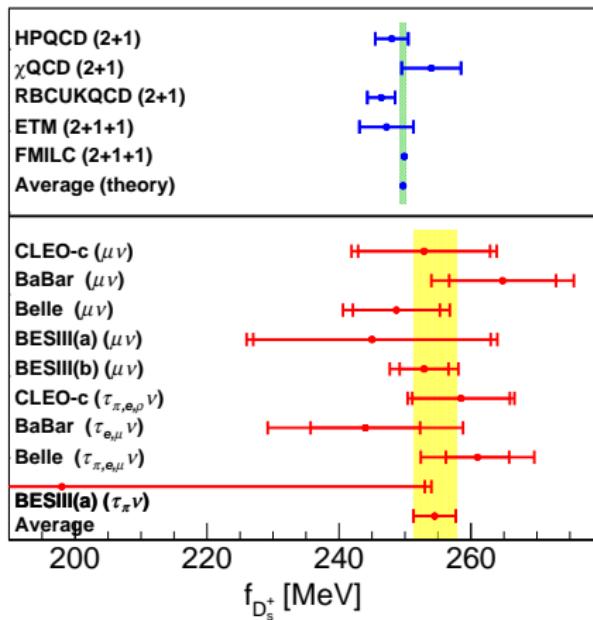
PDG2018 from CKM unitarity:

$$|V_{cs}| = 0.97359^{+0.00010}_{-0.00011}$$

LQCD average:

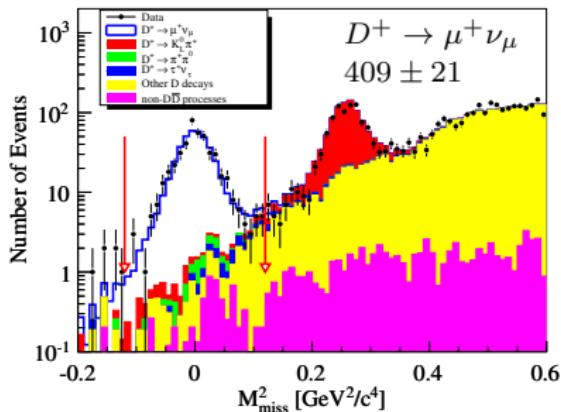
$$f_{D_s^+}^{\text{LQCD}} = 249.7 \pm 0.4 \text{ MeV}$$

$$f_+^{D \rightarrow K}(0)^{\text{LQCD}} = 0.760 \pm 0.011$$



# $D^+$ leptonic decays

BESIII PRD89(2014)051104

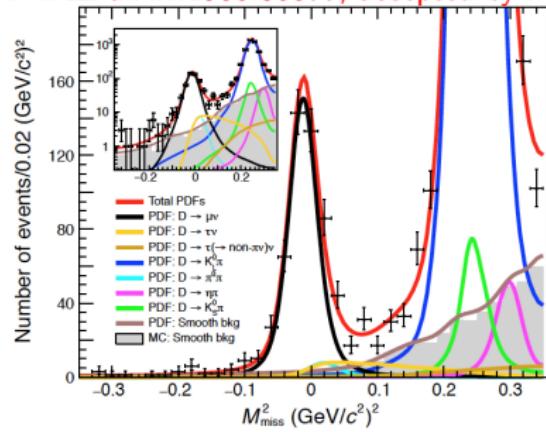


$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu_\mu) = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} |V_{cd}| = 46.7 \pm 1.2 \pm 0.4 \text{ MeV}$$

$$R_{D^+} = \frac{\Gamma(D^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D^+ \rightarrow \mu^+ \nu_\mu)} = 3.21 \pm 0.64 \pm 0.43$$

BESIII arXiv:1908.08877, accepted by PRL



$$\mathcal{B}(D^+ \rightarrow \tau^+ \nu_\tau) = (1.20 \pm 0.24 \pm 0.12) \times 10^{-3}$$

$$f_{D^+} |V_{cd}| = 50.4 \pm 5.1 \pm 2.5 \text{ MeV}$$

First observation with  $5.1\sigma$  signal significance.

SM prediction  $2.67 \pm 0.01$ .

# Comparison of $|V_{cd}|$ and $f_{D^+}$

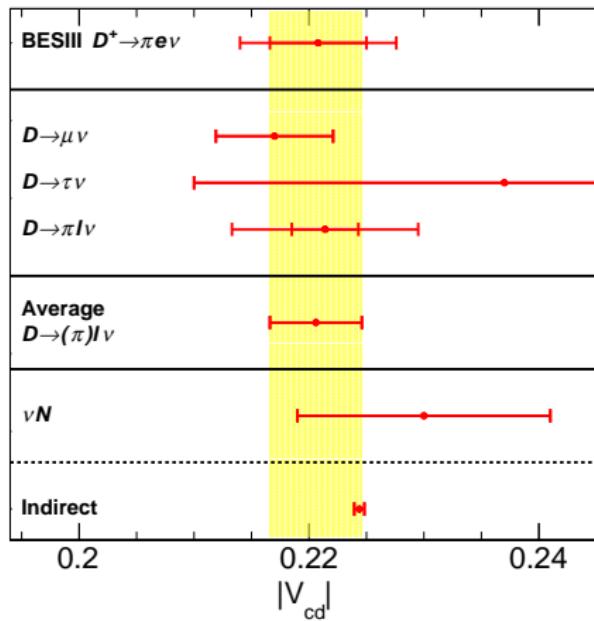
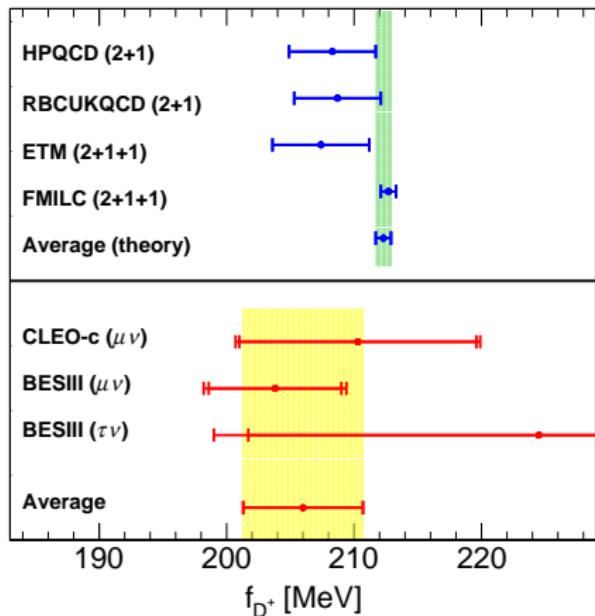
Inputs:

PDG2018 from CKM unitarity:

$$|V_{cd}| = 0.22438 \pm 0.00044$$

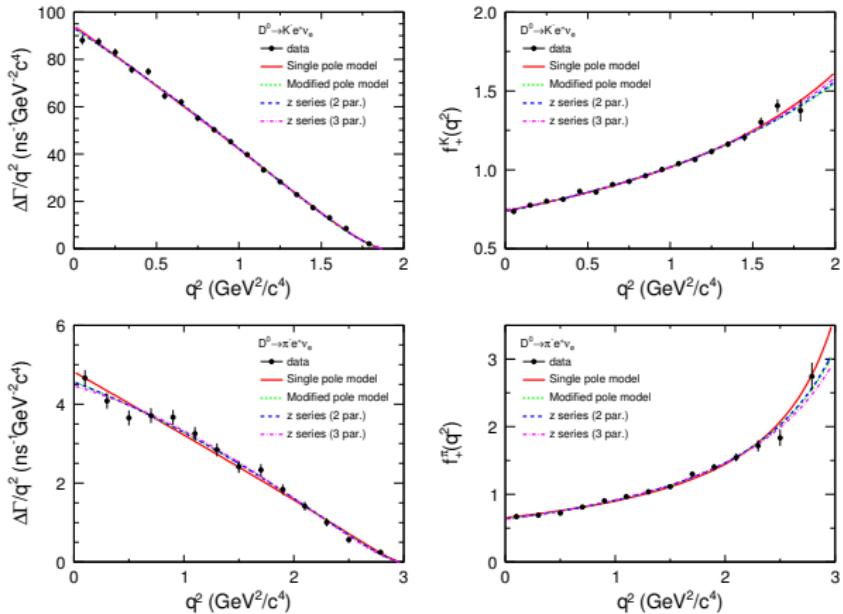
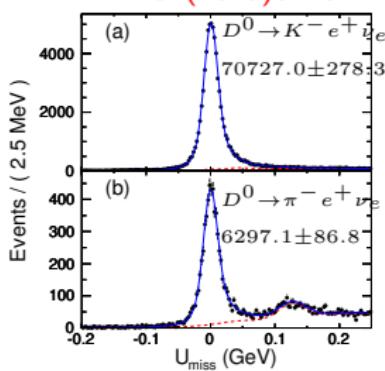
LQCD average:

$$f_{D^+}^{\text{LQCD}} = 212.3 \pm 0.6 \text{ MeV}$$
$$f_+^{D \rightarrow \pi}(0)^{\text{LQCD}} = 0.634 \pm 0.015$$



$$D^0 \rightarrow K^-(\pi^-)e^+\nu_e$$

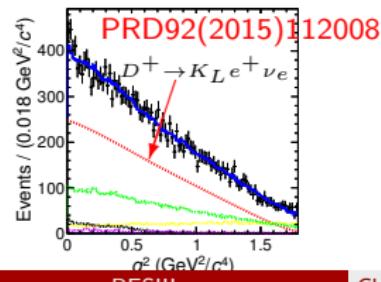
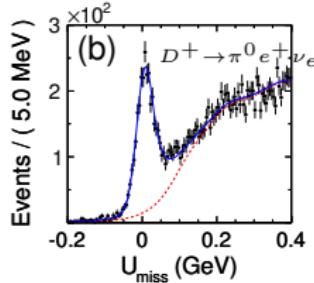
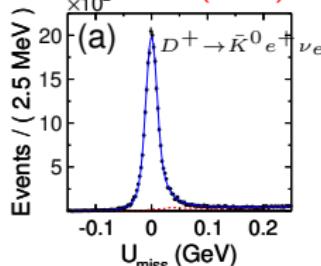
**BESIII** PRD92(2015)072012



$\mathcal{B}(D^0 \rightarrow K^- e^+ \bar{\nu}_e)$	$(3.505 \pm 0.014 \pm 0.033)\%$	$f_+^{D \rightarrow K}(0) V_{cs} $	$0.7172 \pm 0.0025 \pm 0.0035$
$\mathcal{B}(D^0 \rightarrow \pi^- e^+ \bar{\nu}_e)$	$(0.295 \pm 0.004 \pm 0.003)\%$	$f_+^{D \rightarrow \pi}(0) V_{cd} $	$0.1435 \pm 0.0018 \pm 0.0009$

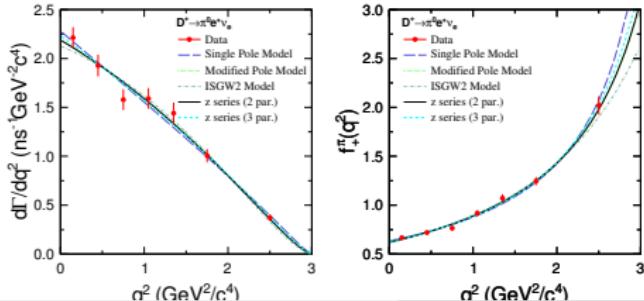
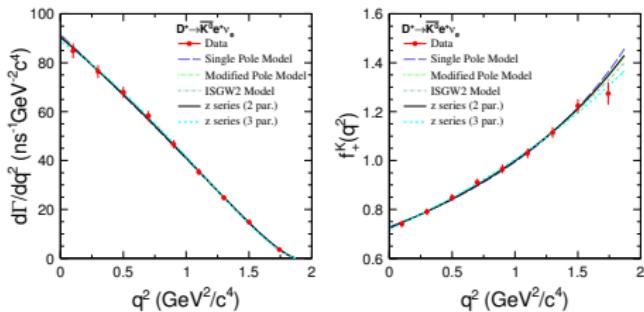
$$D^+ \rightarrow \bar{K}^0(\pi^0)e^+\nu_e$$

**BESIII** PRD96(2017)012002



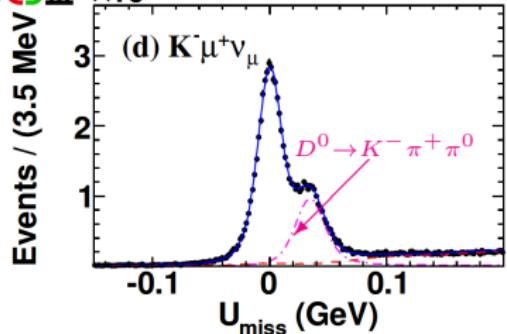
BESIII

$\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)$ (via $K_S^0$ )	$(8.60 \pm 0.06 \pm 0.15)\%$
$f_+^{D \rightarrow K(0) V_{cs} }$	$0.7053 \pm 0.0040 \pm 0.0112$
$\mathcal{B}(D^+ \rightarrow \bar{\pi}^0 e^+ \nu_e)$	$(0.363 \pm 0.008 \pm 0.005)\%$
$f_+^{D \rightarrow \pi(0) V_{cd} }$	$0.1400 \pm 0.0026 \pm 0.0007$
$\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)$ (via $K_L^0$ )	$(8.962 \pm 0.054 \pm 0.206)\%$
$f_+^{D \rightarrow K(0) V_{cs} }$	$0.728 \pm 0.006 \pm 0.011$

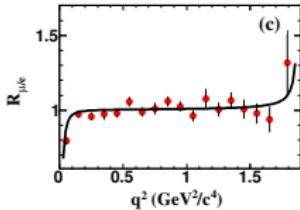
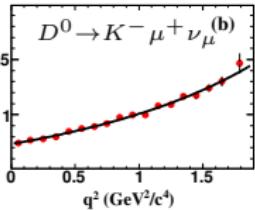
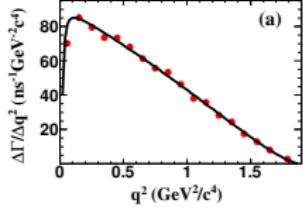
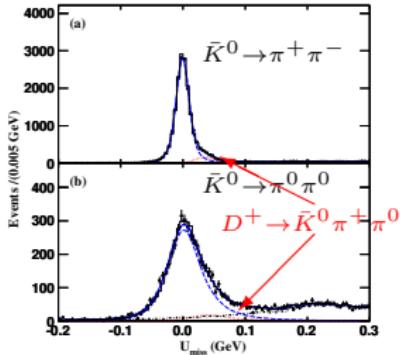


$$D \rightarrow \bar{K} \mu^+ \nu_\mu$$

BESIII  $\times 10^3$  PRL122(2019)011804



BESIII EPJC76(2016)369



$$\frac{\Gamma(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}$$

$$0.974 \pm 0.014$$

$$\frac{\Gamma(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)}$$

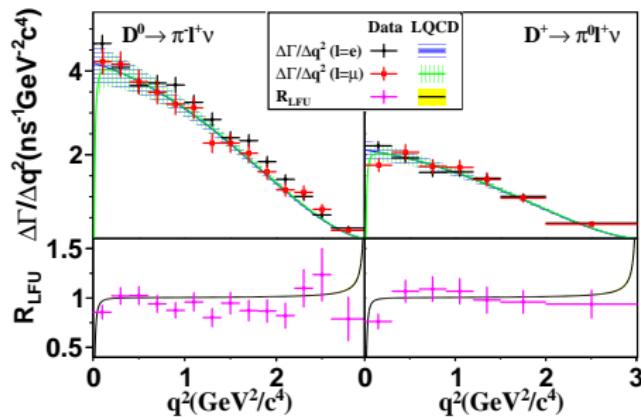
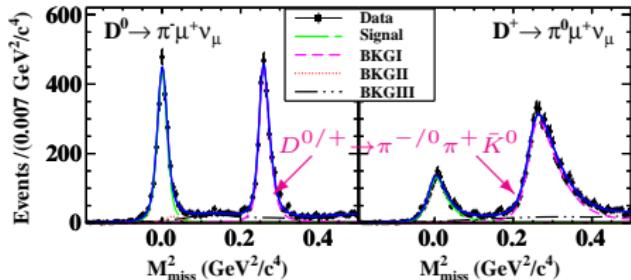
$$0.988 \pm 0.033$$

Expected:  
 $0.975 \pm 0.001$

$\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu)$	$(3.431 \pm 0.019 \pm 0.035)\%$
$f_+^{D \rightarrow K}(0) V_{cs} $	$0.7133 \pm 0.0038 \pm 0.0030$
$\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)$	$(8.72 \pm 0.07 \pm 0.18)\%$

$$D \rightarrow \pi \mu^+ \nu_\mu$$

BESIII PRL121(2018)171803



$$\mathcal{B}(D^0 \rightarrow \pi^- \mu^+ \nu_\mu) = (0.272 \pm 0.008 \pm 0.006)\%$$

$$\mathcal{B}(D^+ \rightarrow \pi^0 \mu^+ \nu_\mu) = (0.350 \pm 0.011 \pm 0.010)\%$$

$$\frac{\Gamma(D^0 \rightarrow \pi^- \mu^+ \nu_\mu)}{\Gamma(D^0 \rightarrow \pi^- e^+ \nu_e)} = 0.922 \pm 0.037$$

$$\frac{\Gamma(D^+ \rightarrow \pi^0 \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \pi^0 e^+ \nu_e)} = 0.964 \pm 0.045$$

The LQCD calculations are taken from ETM's results published in PRD96(2017)054514, with

$$\frac{\Gamma(D \rightarrow \pi \mu^+ \nu_\mu)}{\Gamma(D \rightarrow \pi e^+ \nu_e)} = 0.985 \pm 0.002$$

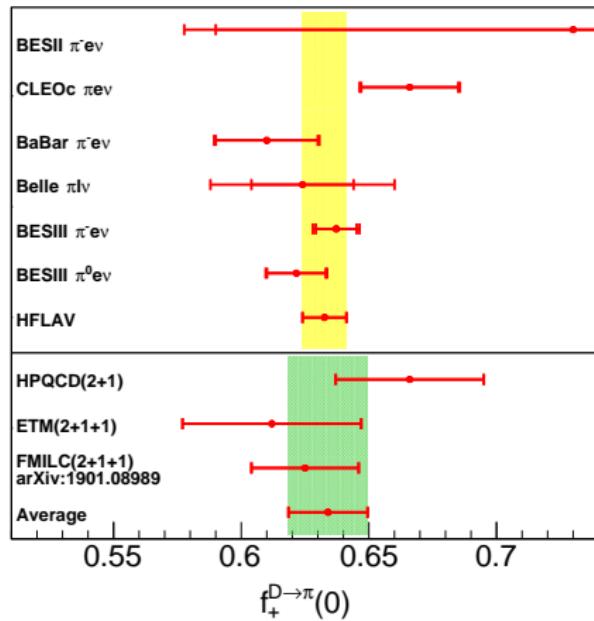
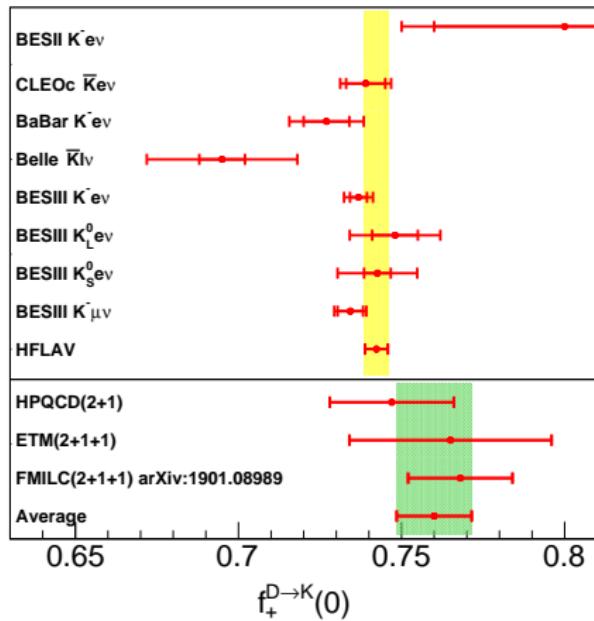
# Comparison of $f_+^{D \rightarrow K}(0)$ and $f_+^{D \rightarrow \pi}(0)$

Inputs:

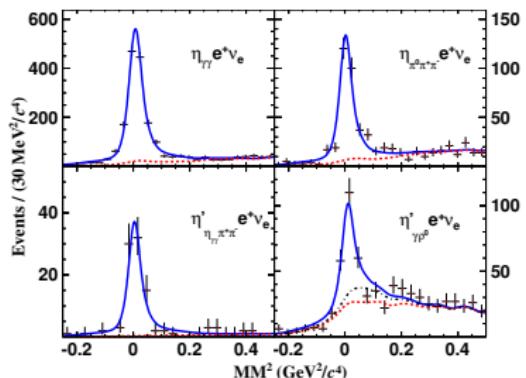
PDG2018 from CKM unitarity:

$$|V_{cs}| = 0.97359^{+0.00010}_{-0.00011}$$

$$|V_{cd}| = 0.22438 \pm 0.00044$$

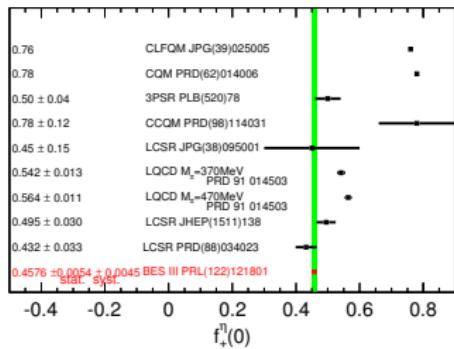


$$D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$$

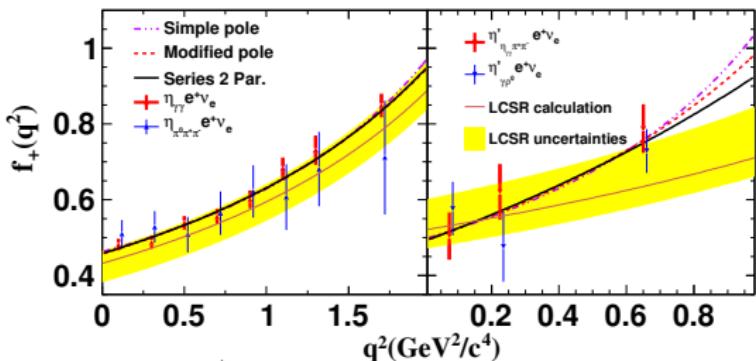


$$\mathcal{B}(D_s^+ \rightarrow \eta e^+ \nu_e) = (2.323 \pm 0.063 \pm 0.063)\%$$

$$\mathcal{B}(D_s^+ \rightarrow \eta' e^+ \nu_e) = (0.824 \pm 0.073 \pm 0.027)\%$$

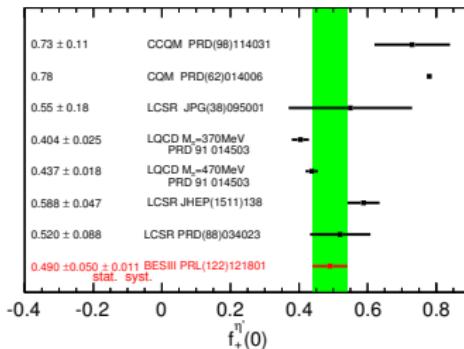


**BESIII** PRL122(2019)121801



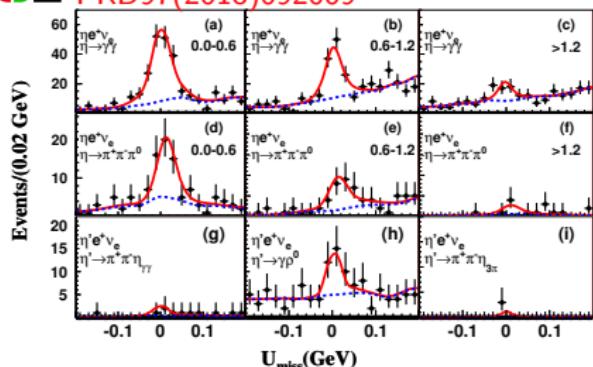
$$f_+^{D_s^+ \rightarrow \eta}(0)|V_{cs}| = 0.4455 \pm 0.0053 \pm 0.0044$$

$$f_+^{D_s^+ \rightarrow \eta'}(0)|V_{cs}| = 0.477 \pm 0.049 \pm 0.011$$



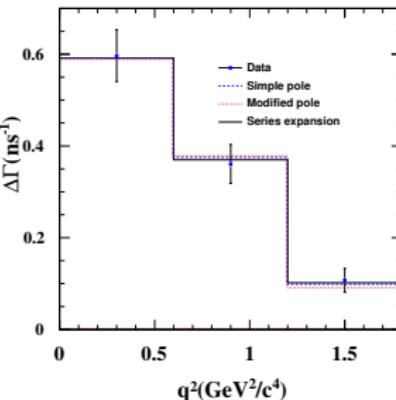
$$D^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$$

**BESIII** PRD97(2018)092009

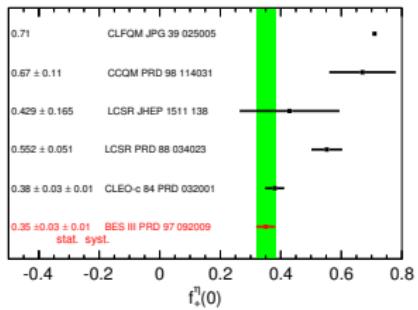


$$\mathcal{B}(D^+ \rightarrow \eta e^+ \nu_e) = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$$

$$\mathcal{B}(D^+ \rightarrow \eta' e^+ \nu_e) = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$$



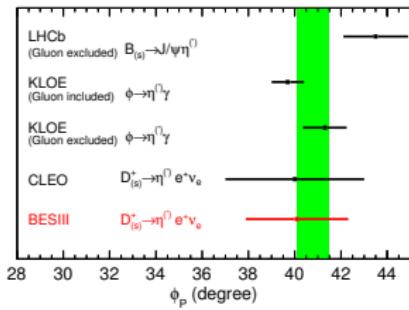
$$f_+^{D^+ \rightarrow \eta}(0)|V_{cd}| = (7.86 \pm 0.64 \pm 0.21) \times 10^{-2}$$



Model independent  
determination of  $\eta - \eta'$   
mixing angle.

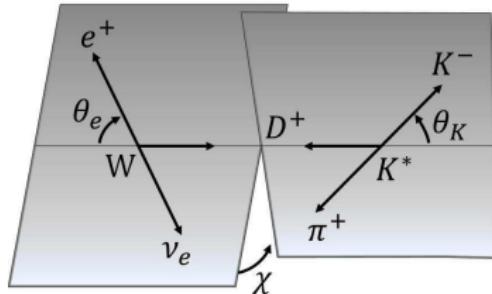
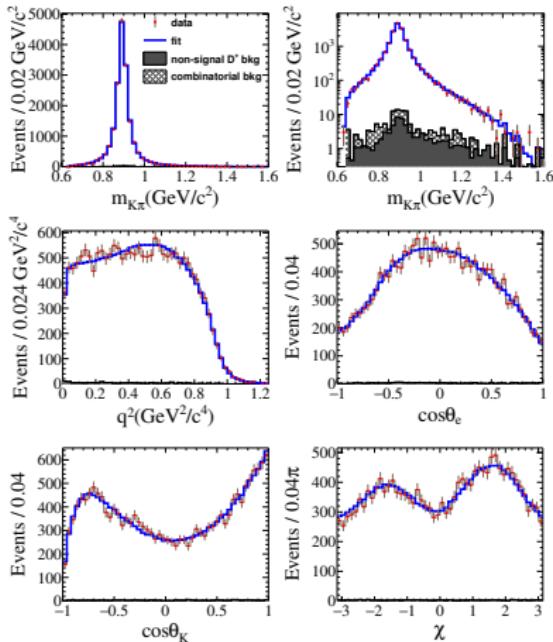
$$\frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu_e)/\Gamma(D_s^+ \rightarrow \eta e^+ \nu_e)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu_e)/\Gamma(D^+ \rightarrow \eta e^+ \nu_e)} \simeq \cot^4 \Phi_P$$

$$\Phi_P = (40.1 \pm 2.1 \pm 0.7)^\circ$$



$$D^+ \rightarrow K^- \pi^+ e^+ \nu_e$$

**BESIII** PRD94(2016)032001



$$r_V = V(0)/A_1(0) = 1.411 \pm 0.058 \pm 0.007$$

$$r_2 = A_2(0)/A_1(0) = 0.788 \pm 0.042 \pm 0.008$$

$$A_1(0) = 0.589 \pm 0.010 \pm 0.012$$

Not included in the nominal fit:

$\mathcal{B}(D^+ \rightarrow \bar{K}^*(1410)^0 e^+ \nu_e)$	$(0 \pm 0.009 \pm 0.008)\%$
	$< 0.028\% \text{ (90\% C.L.)}$
$\mathcal{B}(D^+ \rightarrow \bar{K}_2^*(1430)^0 e^+ \nu_e)$	$(0.011 \pm 0.003 \pm 0.007)\%$
	$< 0.023\% \text{ (90\% C.L.)}$

$$\mathcal{P}(\bar{K}^*(892)^0)$$

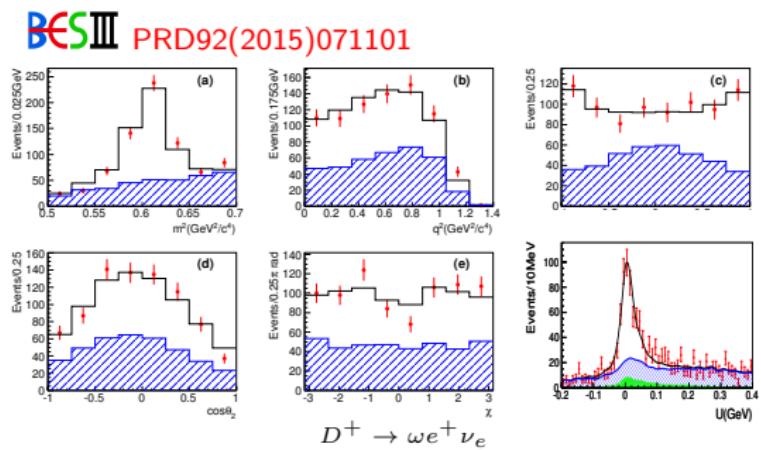
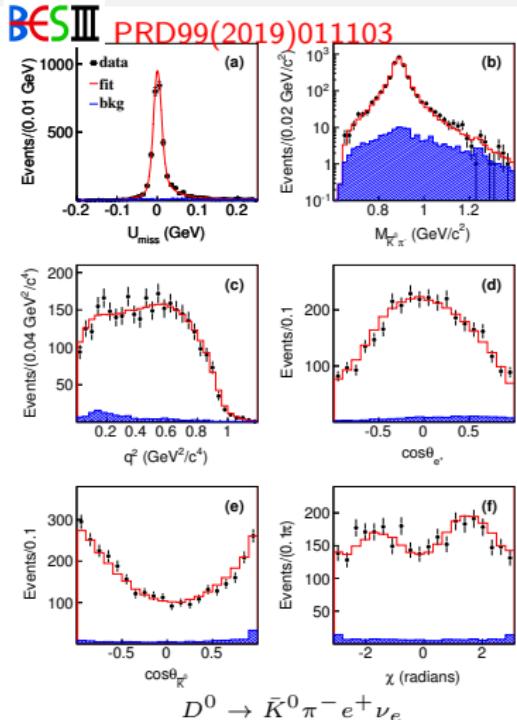
Simple Pole plus  
BW with mass-dependent width  
LASS plus  
BW with mass-dependent width

$$(3.54 \pm 0.03 \pm 0.08)\%$$

$$S(\bar{K}_0^*(1430)^0 \text{ and non-resonant part})$$

$$(0.228 \pm 0.008 \pm 0.008)\%$$

$D^0 \rightarrow \bar{K}^0 \pi^- e^+ \nu_e$  and  $D^+ \rightarrow \omega e^+ \nu_e$



$\mathcal{B}(D^+ \rightarrow \omega e^+ \nu_e)$	$(1.63 \pm 0.11 \pm 0.08) \times 10^{-3}$
$r_V$	$1.24 \pm 0.09 \pm 0.06$
$r_2$	$1.06 \pm 0.15 \pm 0.05$

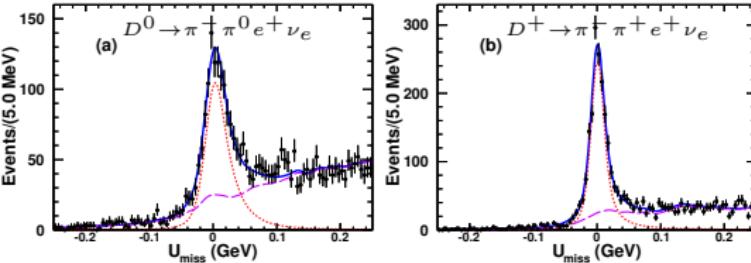
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$S(\bar{K}^0 \pi)_{S\text{-wave}}$	$(7.90 \pm 1.40 \pm 0.91) \times 10^{-4}$	$P(K^*(892)^-)$	$(1.355 \pm 0.031 \pm 0.032)\%$
$r_V$	$1.46 \pm 0.07 \pm 0.02$	$r_2$	$0.67 \pm 0.06 \pm 0.01$

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$D \rightarrow \pi\pi e^+ \nu_e$

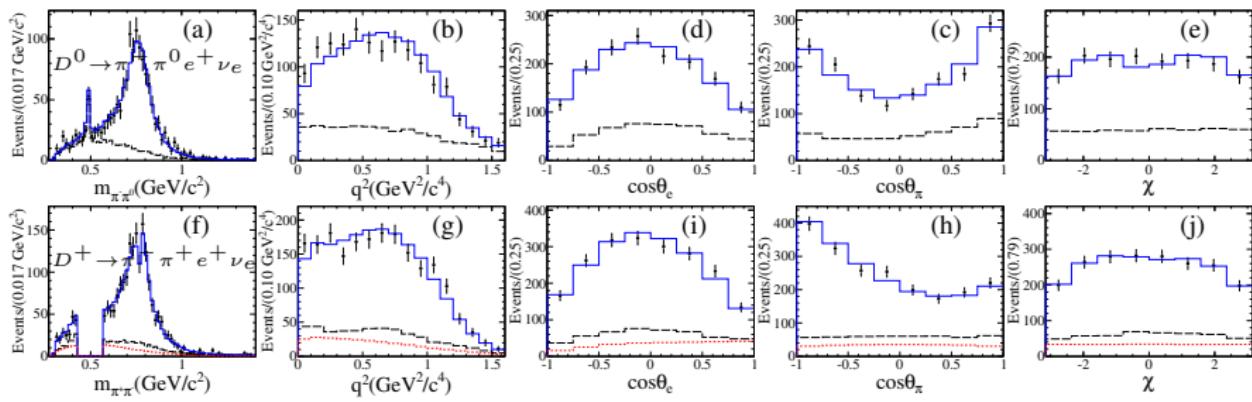
BESIII PRL122(2019)062001



Signal mode	BF ( $\times 10^{-3}$ )
$D^0 \rightarrow \pi^- \pi^0 e^+ \nu_e$	$1.445 \pm 0.058 \pm 0.039$
$D^0 \rightarrow \rho^- e^+ \nu_e$	$1.445 \pm 0.048 \pm 0.039$
$D^+ \rightarrow \pi^- \pi^+ e^+ \nu_e$	$2.449 \pm 0.074 \pm 0.073$
$D^+ \rightarrow \rho^0 e^+ \nu_e$	$1.860 \pm 0.070 \pm 0.061$
$D^+ \rightarrow \omega e^+ \nu_e$	$2.05 \pm 0.66 \pm 0.30$
$D^+ \rightarrow f_0(500) e^+ \nu_e$	$0.630 \pm 0.043 \pm 0.032$
$f_0(500) \rightarrow \pi^+ \pi^-$	
$D^+ \rightarrow f_0(980) e^+ \nu_e$	$< 0.028$
$f_0(980) \rightarrow \pi^+ \pi^-$	

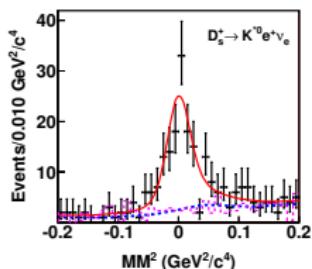
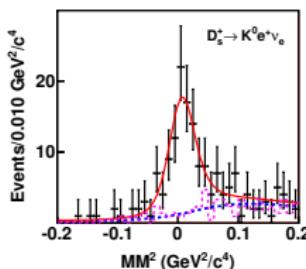
$$r_V = 1.695 \pm 0.083 \pm 0.051$$

$$r_2 = 0.845 \pm 0.056 \pm 0.039$$



$$D_s^+ \rightarrow K^{(*)0} e^+ \nu_e$$

BESIII PRL122(2019)061801



$$\mathcal{B}(D_s^+ \rightarrow K^0 e^+ \nu_e) = (3.25 \pm 0.38 \pm 0.16) \times 10^{-3}$$

$$f_+^{D_s^+ \rightarrow K^0}(0) |V_{cd}| = 0.162 \pm 0.019 \pm 0.003$$

$$\mathcal{B}(D_s^+ \rightarrow K^0 e^+ \nu_e) = (2.37 \pm 0.26 \pm 0.20) \times 10^{-3}$$

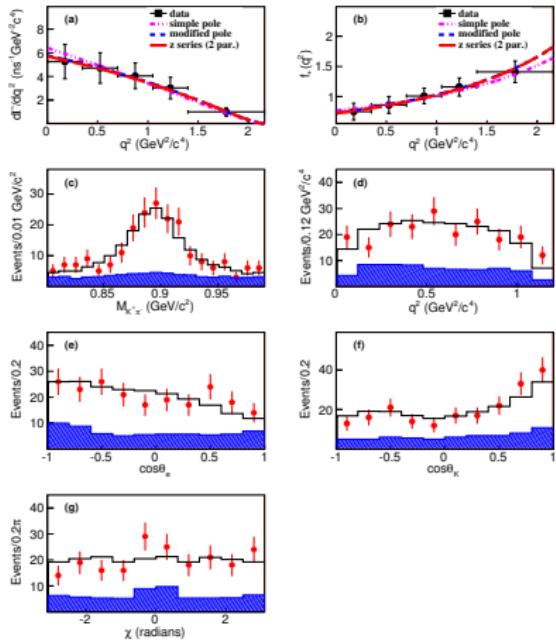
$$r_V = 1.67 \pm 0.34 \pm 0.16$$

$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

$$f_+^{D_s^+ \rightarrow K^0}(0) / f_+^{D^+ \rightarrow \pi^0}(0) = 1.16 \pm 0.14 \pm 0.02$$

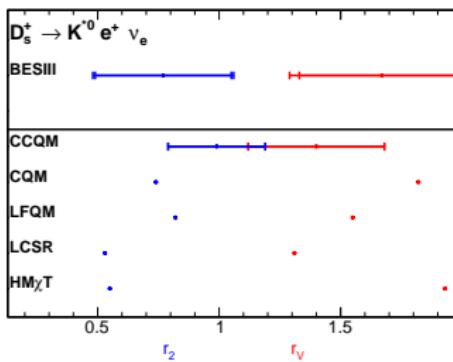
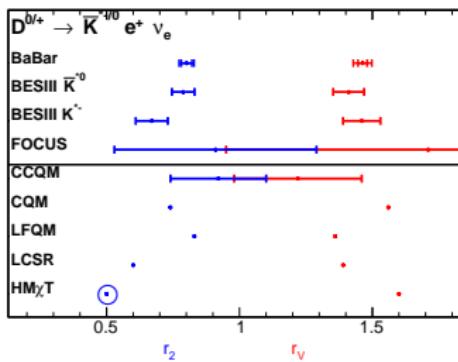
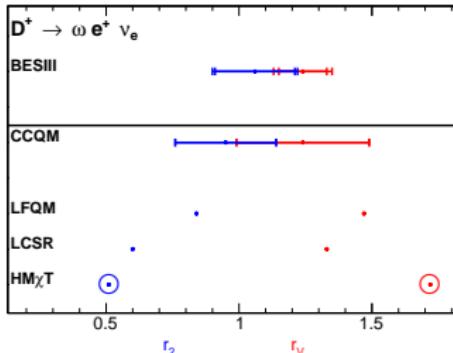
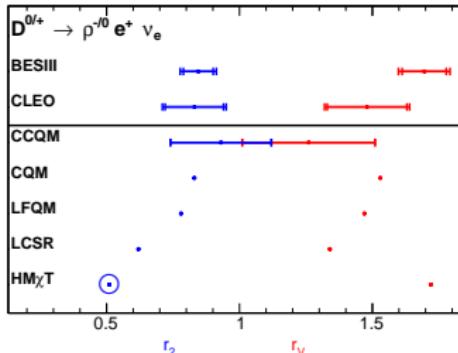
$$r_V^{D_s^+ \rightarrow K^{*0}} / r_V^{D^+ \rightarrow \rho^0} = 1.13 \pm 0.26 \pm 0.11$$

$$r_2^{D_s^+ \rightarrow K^{*0}} / r_2^{D^+ \rightarrow \rho^0} = 0.93 \pm 0.36 \pm 0.10$$



Agrees with U-spin ( $d \leftrightarrow s$ ) symmetry.

# Comparison of $r_V$ and $r_2$ with theoretical calculations



CCQM  
LFQM  
HM $_{\chi}$ T

arXiv:1904.07740  
JPG39(2012)025005  
PRD72(2005)034029

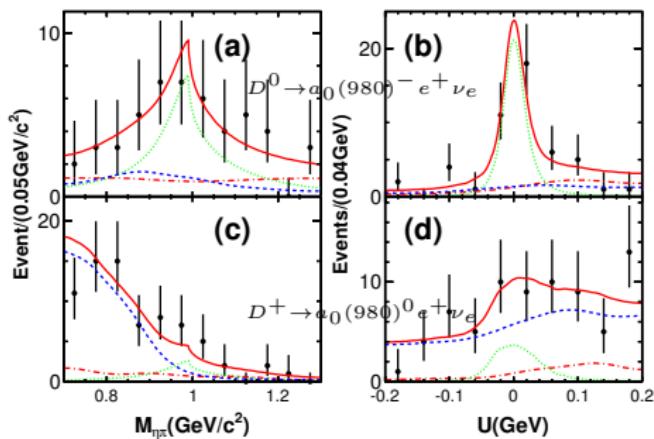
CQM  
LCSR  
(not applicable?)

PRD62(2000)014006

Int. J. Mod. Phys. A 21(2006)6125

$$D \rightarrow a_0(980)e^+\nu_e$$

**BESIII** PRL121(2018)081802



A model-independent way to study the nature of light scalar mesons proposed by PRD82(2016)034016

$$R = \frac{\mathcal{B}(D^+ \rightarrow f_0(980)e^+\nu_e) + \mathcal{B}(D^+ \rightarrow f_0(500)e^+\nu_e)}{\mathcal{B}(D^+ \rightarrow a_0(980)^0e^+\nu_e)}$$

$R = 1.0 \pm 0.3$  for two-quark description;  
 $R = 3.0 \pm 0.9$  for tetraquark description.

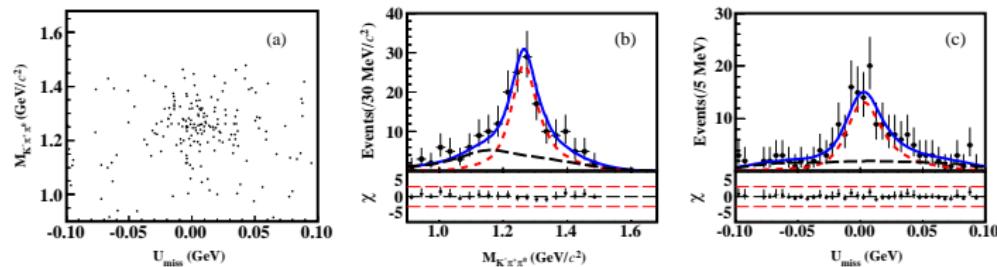
We have  $R > 2.7$  @90% C.L. at BESIII  
 Which favors the tetraquark description.

Decay	BF ( $\times 10^{-4}$ )	Significance
$D^0 \rightarrow a_0(980)^- e^+\nu_e, a_0(980)^- \rightarrow \eta\pi^-$	$1.33^{+0.33}_{-0.29} \pm 0.09$	$6.4\sigma$
$D^+ \rightarrow a_0(980)^0 e^+\nu_e, a_0(980)^0 \rightarrow \eta\pi^0$	$1.66^{+0.81}_{-0.66} \pm 0.11$ $< 3.0$ (90% C.L.)	$2.9\sigma$

# $D^+ \rightarrow \bar{K}_1(1270)^0 e^+ \nu_e$

- First observation of  $D$  meson semileptonic decay into axial-vector mesons.
- Provide insight into the mixing angle of  ${}^1P_1$  and  ${}^3P_1$  states  $\theta_{K_1}$ .
- Test various theoretical calculations.
- Provide important input to study the photon polarisation in  $B \rightarrow K_1 \gamma$  by measuring the ratio of up-down asymmetries of  $\theta_K$  and  $\theta_l$  (more statistics needed). (See Dr. Zhen-Xing Zhao's talk)

**BESIII** arXiv:1907.11370, accepted by PRL

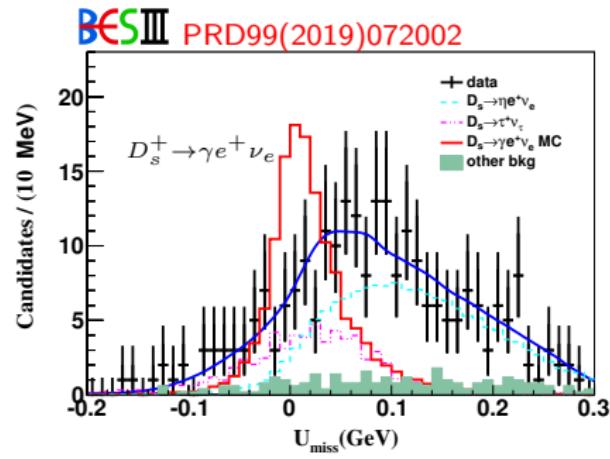
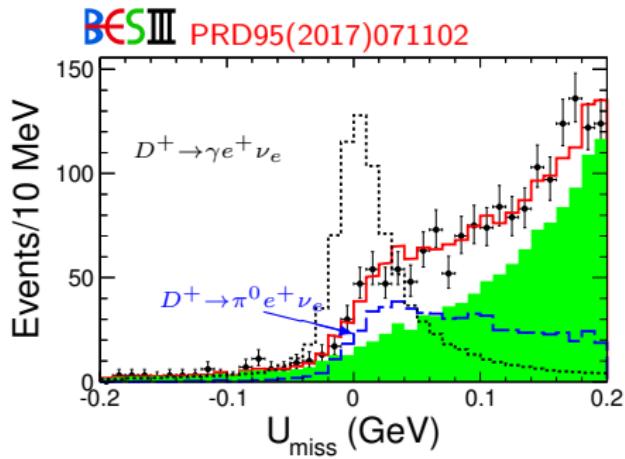
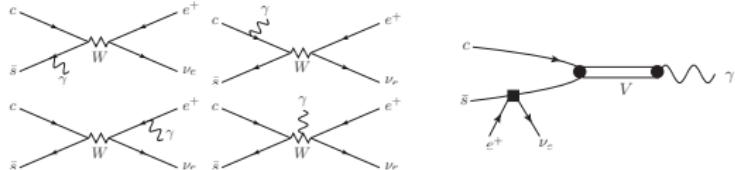


$$\mathcal{B}(D^+ \rightarrow \bar{K}_1(1270)^0 e^+ \nu_e) = (2.30 \pm 0.26 \pm 0.18 \pm 0.25) \times 10^{-3}$$

The measured BF agrees with CLFQM and LCSR predictions when  $\theta_{K_1} \sim 33^\circ$  or  $57^\circ$  and clearly rules out the case when setting  $\theta_{K_1}$  negative.

$$D \rightarrow \gamma e^+ \nu_e$$

Not subject to helicity suppression.  
Only photon energy larger than 10 MeV are considered.  
The BFs are predicated to be  $10^{-5} \rightarrow 10^{-3}$  in various models.



$$\mathcal{B}(D^+ \rightarrow \gamma e^+ \nu_e) < 3.0 \times 10^{-5} \text{ @90% C.L.}$$

$$\mathcal{B}(D_s^+ \rightarrow \gamma e^+ \nu_e) < 1.3 \times 10^{-4} \text{ @90% C.L.}$$

# Summary

- Precise measurement of decay constants, form factors and quark mixing matrix elements → precision improved with BESIII measurement.
- Lepton flavor universality test → no evidence of violation found in the charm sector at the precision of 1.5% for CF decays and 4% for SCS decays..
- Study the nature of light scalar mesons → tetraquark description favored with BESIII's results.
- First observation of  $D$  meson semileptonic decay to axias vector meson at BESIII.

Thanks for your attention!