

Charmed Meson Hadronic decays at BESIII

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(On behalf of the BESIII collaboration)

Outline

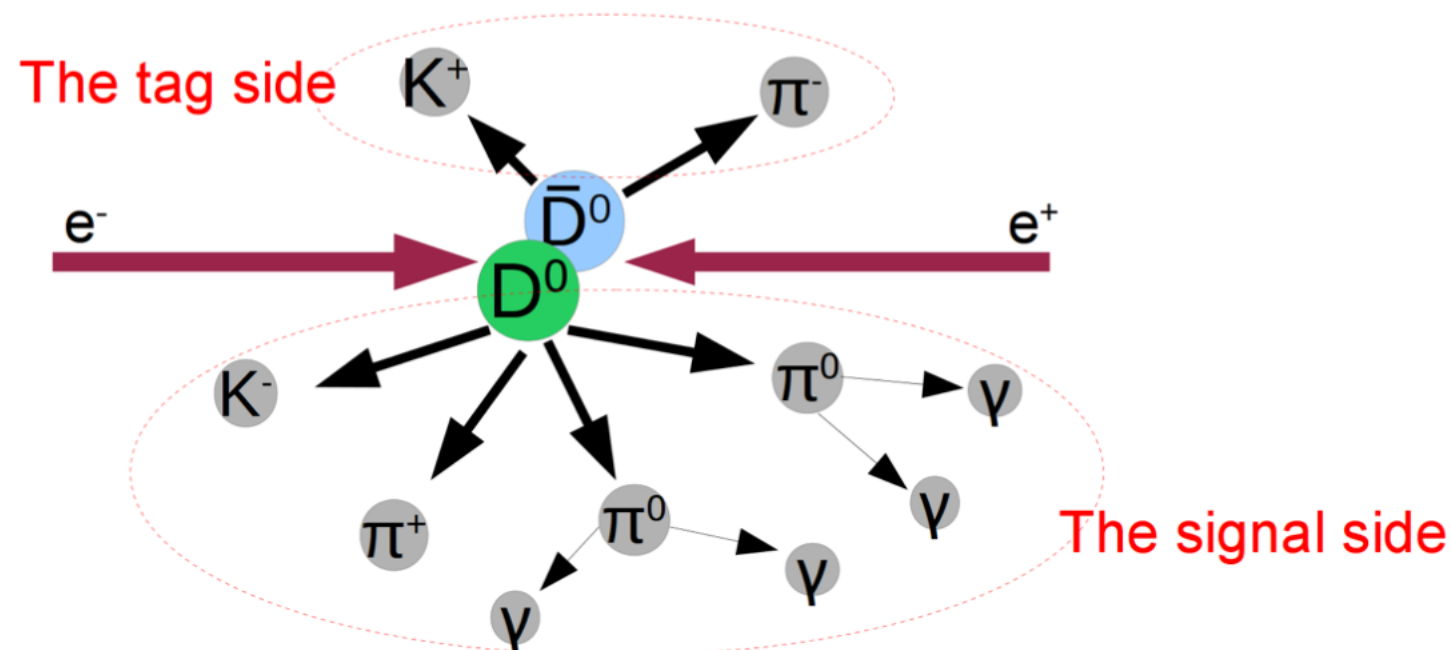
- Introduction
 - D^0 , D^+ , and D_s dataset
 - DTag and branching fraction
- Branching fraction measurement of D hadronic decays
- Amplitude analysis
 - $K^-\pi^+\pi^+\pi^-$, $K_S\pi^+\pi^+\pi^-$, $K^-\pi^+\pi^0\pi^0$, $\pi^+\pi^0\eta$ etc.
- Summary

BESIII Data Taken near DD^{bar} Threshold

- BEPCII collider: $e^+e^- \rightarrow \psi(3770) \rightarrow DD^{\text{bar}}$
- 2.9 fb^{-1} dataset at $\psi(3770)$ resonance ($\sim 3.6\times$ larger than CLEO's)
 $M_{D^0} = 1864.84 \text{ MeV}$ $M_{D^+} = 1869.62 \text{ MeV}$
 $2M_{D^0} = 3729.68 \text{ MeV}$ $2M_{D^+} = 3739.24 \text{ MeV}$
- 3.19 fb^{-1} dataset at $E_{\text{cm}} 4.178 \text{ GeV}$ ($\sim 5.3\times$ larger than CLEO's)
 - D_s are produced mostly via $e^+e^- \rightarrow D_s D_s^*$
 - more energy points are ready (4.190, 4.200, 4.210, 4.220, 4.230 GeV. Total are about $0.8\times$ of 4.178 data.)
- Advantages of DD^{bar} pair production near threshold
 - The DD^{bar} events are clean; not enough energy for even one additional pion
 - Tagging reduces background from light-quark “continuum” and other charm final states
 - Double tag technique can provide access to absolute BFs
 - Many systematic uncertainties cancel with tagging technique

DTag Technique

- There are two types of samples used in the Dtag technique: single tag (ST) and double tag (DT).
- Single tag: only one D meson is reconstructed through a chosen hadronic decay.
- Double tag: both D and $\bar{D}$ are reconstructed,
- the D reconstructed through the studied hadronic decay is called “the signal side”.
- the $\bar{D}$ reconstructed through well-known and clean hadronic decay modes is called “the tag side”.
- (Charge-conjugate states are implied throughout this talk.)



Observation of the Singly Cabibbo-Suppressed Decay $D^+ \rightarrow \omega \pi^+$ and Evidence for $D^0 \rightarrow \omega \pi^0$

Chose six (five) decay modes for $D^{+(0)}$.

In order to have a better solution for $D^{+(0)} \rightarrow \pi^+ \pi^- \pi^0 \pi^{+(0)}$ background, DT samples $D^{+(0)} \rightarrow \pi^+ \pi^- \pi^0 \pi^{+(0)}$ vs. tag modes are reconstructed first. Then fits to $\pi^+ \pi^- \pi^0$ mass are performed.

Note that we are searching for $\omega \rightarrow \pi^+ \pi^- \pi^0$.

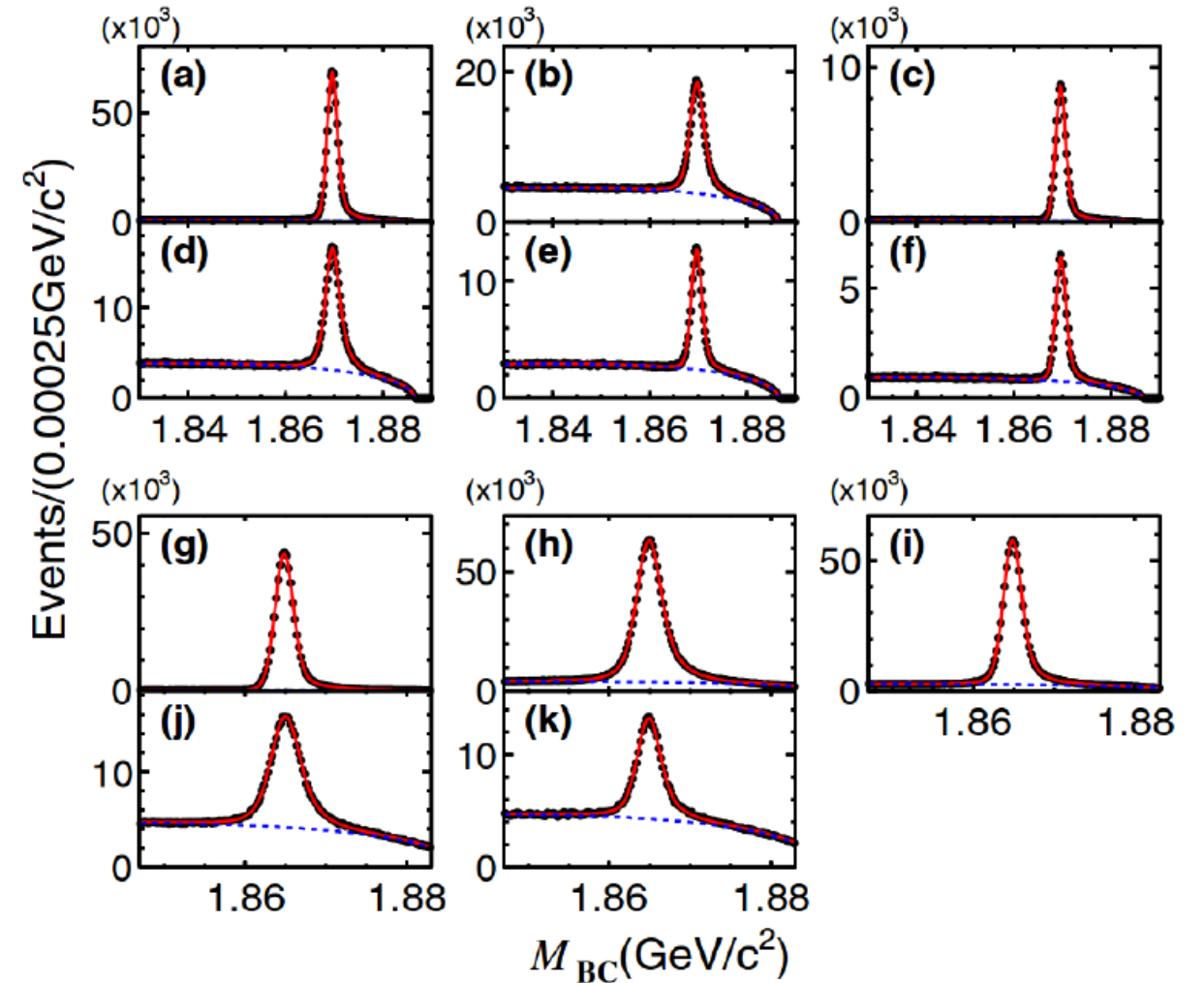


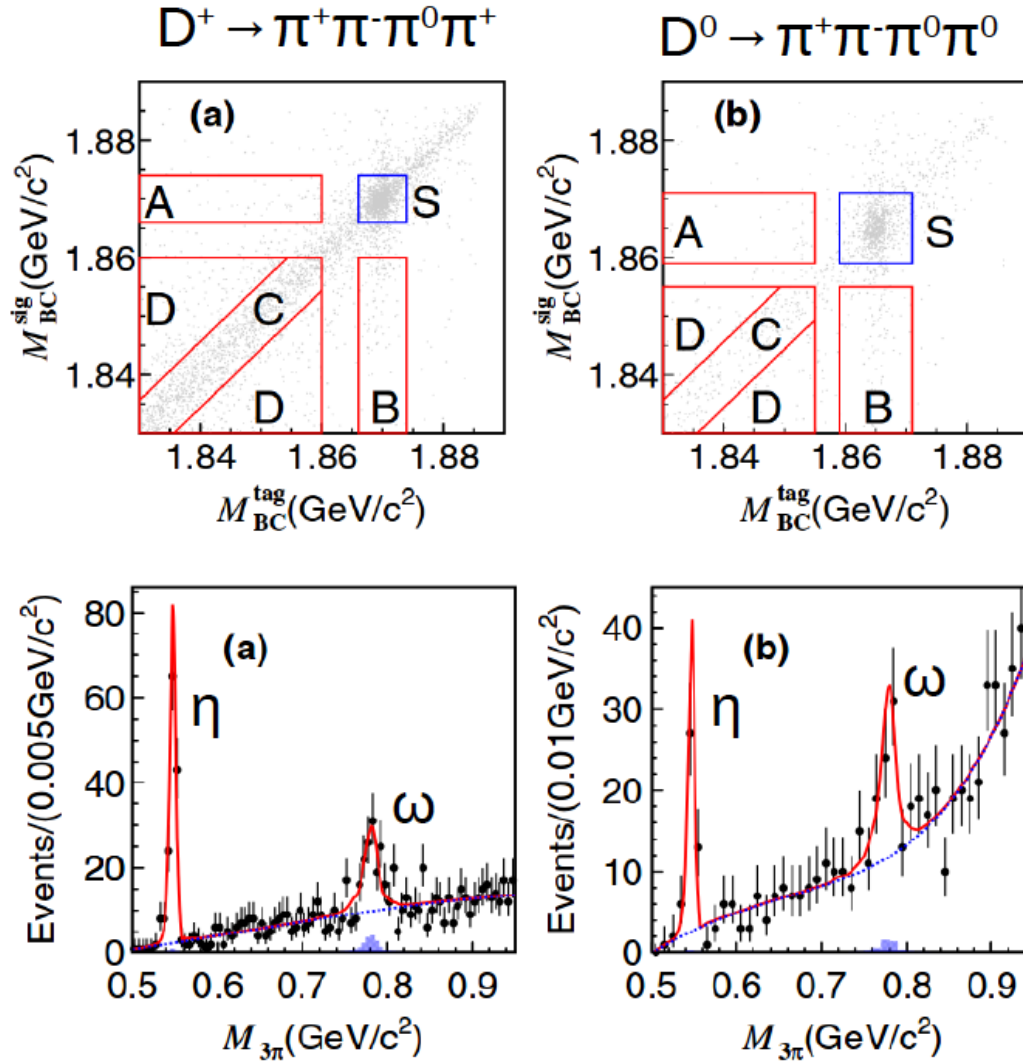
FIG. 1. M_{BC} distributions of ST samples for different tag modes. The first two rows show charged D decays: (a) $K^+ \pi^- \pi^-$, (b) $K^+ \pi^- \pi^- \pi^0$, (c) $K_S^0 \pi^-$, (d) $K_S^0 \pi^- \pi^0$, (e) $K_S^0 \pi^+ \pi^- \pi^-$, (f) $K^+ K^- \pi^-$, the latter two rows show neutral D decays: (g) $K^+ \pi^-$, (h) $K^+ \pi^- \pi^0$, (i) $K^+ \pi^- \pi^+ \pi^-$, (j) $K^+ \pi^- \pi^0 \pi^0$, (k) $K^+ \pi^- \pi^+ \pi^- \pi^0$. Data are shown as points, the (red) solid lines are the total fits and the (blue) dashed lines are the background shapes. D and $\bar{D}$ candidates are combined.

$$\mathcal{B}_{\text{sig}} = \frac{\sum_{\alpha} N_{\text{sig}}^{\text{obs}, \alpha}}{\sum_{\alpha} N_{\text{tag}}^{\text{obs}, \alpha} \epsilon_{\text{tag, sig}}^{\alpha} / \epsilon_{\text{tag}}^{\alpha}}$$

DT $D^{+(0)} \rightarrow \pi^+\pi^-\pi^0\pi^{+(0)}$ vs. tag modes

Fits to $M_{3\pi}$ distributions of signal and sideband regions to obtain the signal and peaking background yields, respectively.

Events counts in sidebands are projected into the signal region with scale factors.



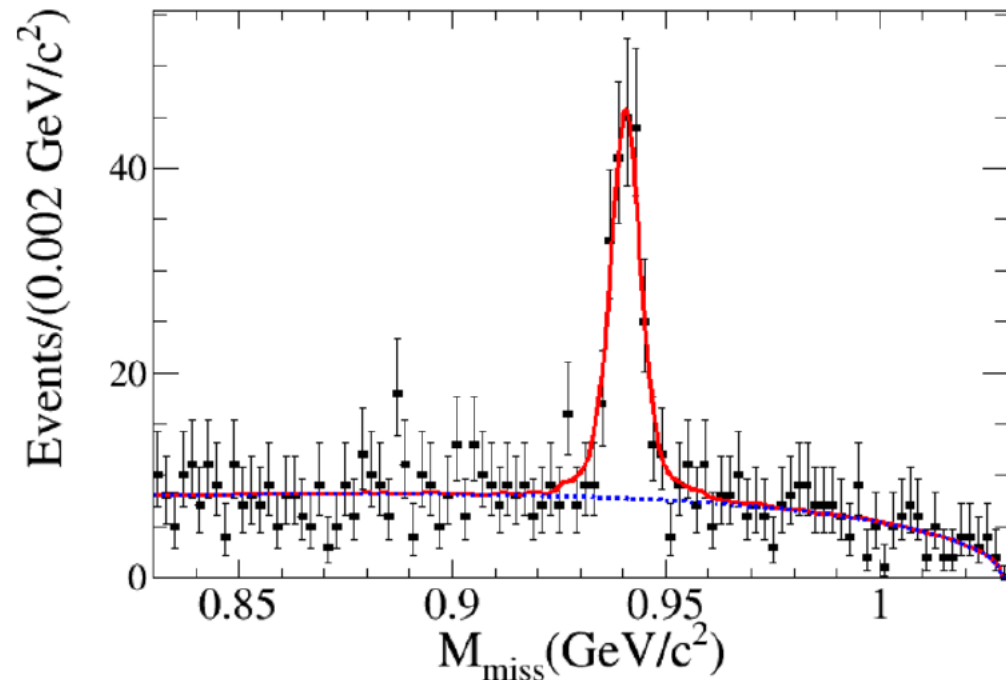
Red line: total fit
Blue line: background
Hatched histogram:
peaking background
From sidebands

ModeH	$N_{\omega(\eta)}$	$N_{\omega(\eta)}^{\text{bkg}}$	$N_{\text{sig}}^{\text{obs}}$
$D^+ \rightarrow \omega\pi^+$	100 ± 16	21 ± 4	79 ± 16
$D^0 \rightarrow \omega\pi^0$	50 ± 12	5 ± 5	45 ± 13
$D^+ \rightarrow \eta\pi^+$	264 ± 17	6 ± 2	258 ± 18
$D^0 \rightarrow \eta\pi^0$	78 ± 10	3 ± 2	75 ± 10

Mode	This work	Previous measurements
$D^+ \rightarrow \omega\pi^+$	$(2.79 \pm 0.57 \pm 0.16) \times 10^{-4}$	$< 3.4 \times 10^{-4}$ at 90% C.L.
$D^0 \rightarrow \omega\pi^0$	$(1.17 \pm 0.34 \pm 0.07) \times 10^{-4}$	$< 2.6 \times 10^{-4}$ at 90% C.L.
$D^+ \rightarrow \eta\pi^+$	$(3.07 \pm 0.22 \pm 0.13) \times 10^{-3}$	$(3.53 \pm 0.21) \times 10^{-3}$
$D^0 \rightarrow \eta\pi^0$	$(0.65 \pm 0.09 \pm 0.04) \times 10^{-3}$	$(0.68 \pm 0.07) \times 10^{-3}$

PRL **116**, 082001 (2016)

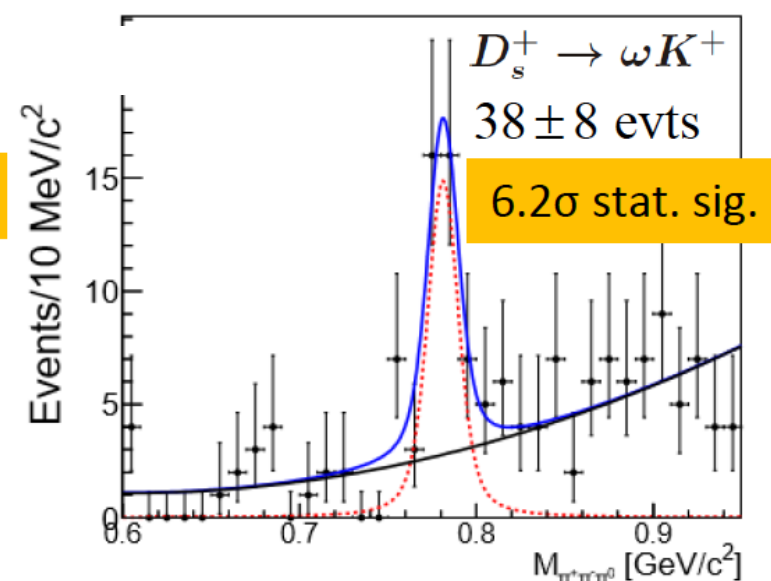
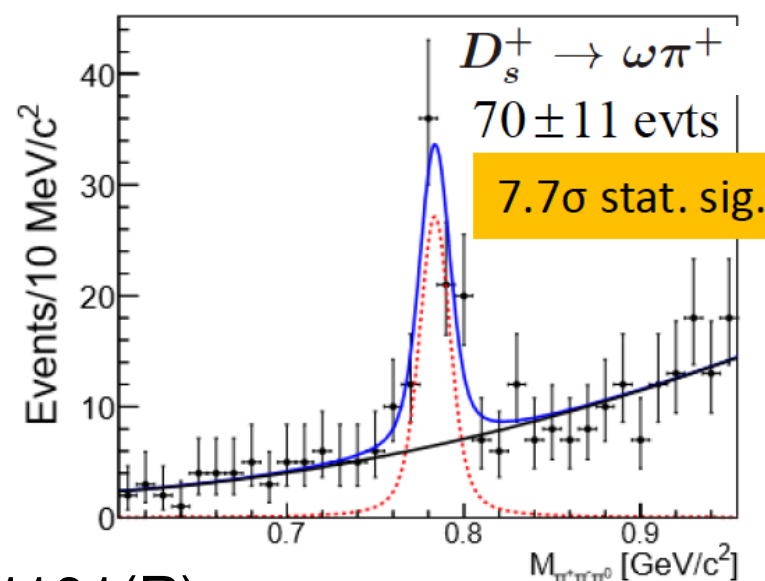
Measurements of pure W-annihilation decays in D_s^+



$$\mathcal{B}_{D_s^+ \rightarrow p\bar{n}} = (1.22 \pm 0.10) \times 10^{-3}$$

Consistent with long-distance expectation

Phys. Rev. D **99**, 031101(R)



Phys. Rev. D **99**, 091101(R)

Consistent with CLEO's measurement, but more precise.

$$\mathcal{B}(D_s^+ \rightarrow \omega\pi^+) = (1.85 \pm 0.30_{stat.} \pm 0.19_{sys.}) \times 10^{-3}$$

$$\mathcal{B}(D_s^+ \rightarrow \omega K^+) = (1.13 \pm 0.24_{stat.} \pm 0.14_{sys.}) \times 10^{-3}$$

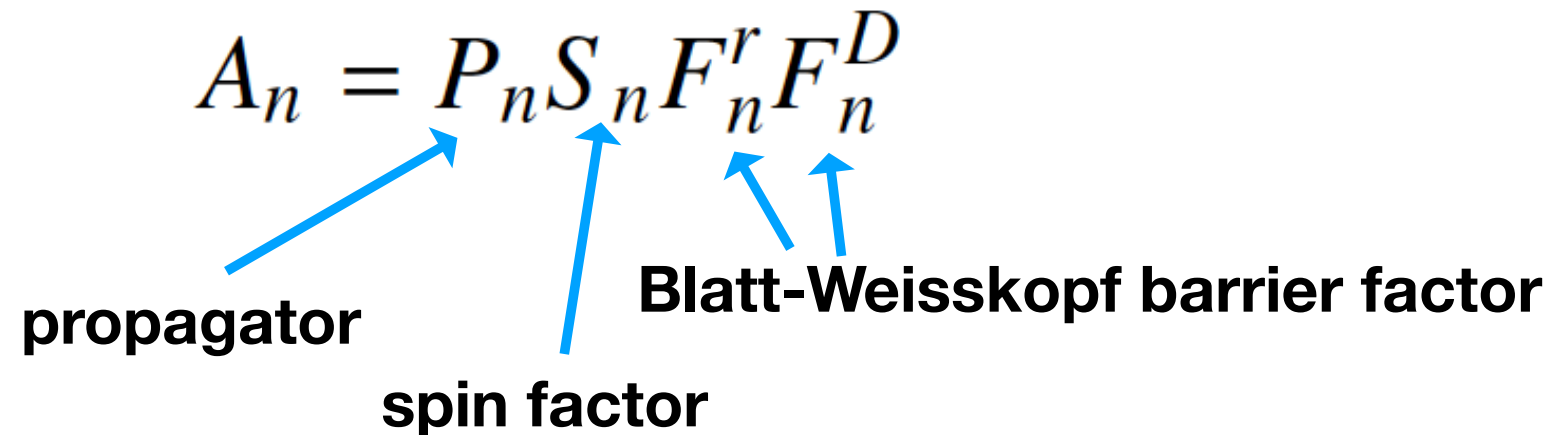
First observation !

This measurement implies the ρ - ω mixing is negligible.

Amplitude Analysis of $D_{(s)}$ three- and four-body decays

The amplitude of the n^{th} intermediate state

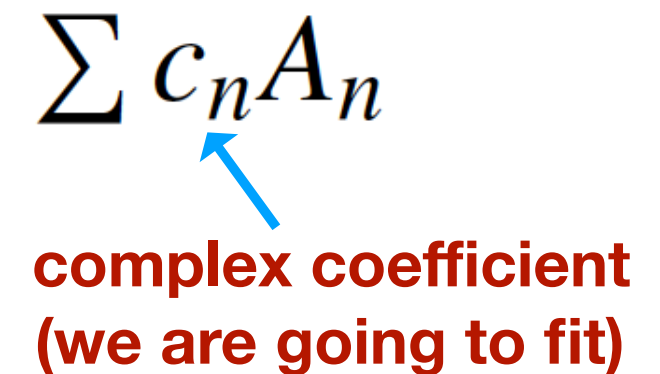
$$A_n = P_n S_n F_n^r F_n^D$$



propagator spin factor Blatt-Weisskopf barrier factor

The total amplitude M

$$\sum c_n A_n$$



complex coefficient
(we are going to fit)

The signal probability density function (PDF)

$$f_S(p_j) = \frac{\epsilon(p_j) |M(p_j)|^2 R_3(p_j)}{\int \epsilon(p_j) |M(p_j)|^2 R_3(p_j) dp_j}$$

Likelihood

$$\ln L = \sum_k^{N_{data}} \ln f_S(p_j^k)$$

The normalization is determined by MC integration

$$\int \epsilon(p_j) |M(p_j)|^2 R_3(p_j) dp_j \approx \frac{1}{N_{MC}} \sum_{k_{MC}}^{N_{MC}} \frac{|M(p_j^{k_{MC}})|^2}{|M^{gen}(p_j^{k_{MC}})|^2}$$

Propagator

$K^*(892)$, $K^*(1680)$: RBW

$$P = \frac{1}{(m_0^2 - s_a) - i m_0 \Gamma(m)}$$

a_0 : two-channel-coupled Flatté formula

$$1 / [(m_0^2 - s_a) - i (g_{\eta\pi}^2 \rho_{\eta\pi} + g_{K\bar{K}}^2 \rho_{K\bar{K}})]$$

Phys. Rev. D 95, no. 3, 032002 (2017)

Amplitude Analysis of $K\pi\pi\pi$

- There are seven $D \rightarrow K\pi\pi\pi$ modes:

- $D^0 \rightarrow K^-\pi^+\pi^+\pi^-$ (published on PRD)

- $D^0 \rightarrow K^-\pi^+\pi^0\pi^0$ (published on PRD)

- $D^0 \rightarrow K_S\pi^0\pi^0\pi^0$

- $D^0 \rightarrow K_S\pi^+\pi^-\pi^0$ (on-going)

- $D^+ \rightarrow K^-\pi^+\pi^+\pi^0$ (on-going)

- $D^+ \rightarrow K_S\pi^+\pi^0\pi^0$ (on-going)

- $D^+ \rightarrow K_S\pi^+\pi^+\pi^-$ (published on PRD)

- Four-body decays are in five-dimensions

- We have

- Partial Wave Analysis Tools based on CPU and GPU kernel

- Great Electro-Magnetic Calorimeter (EMC) with CsI

- superior resolution and efficiency of π^0

- Largest dataset at $\psi(3770)$ resonance

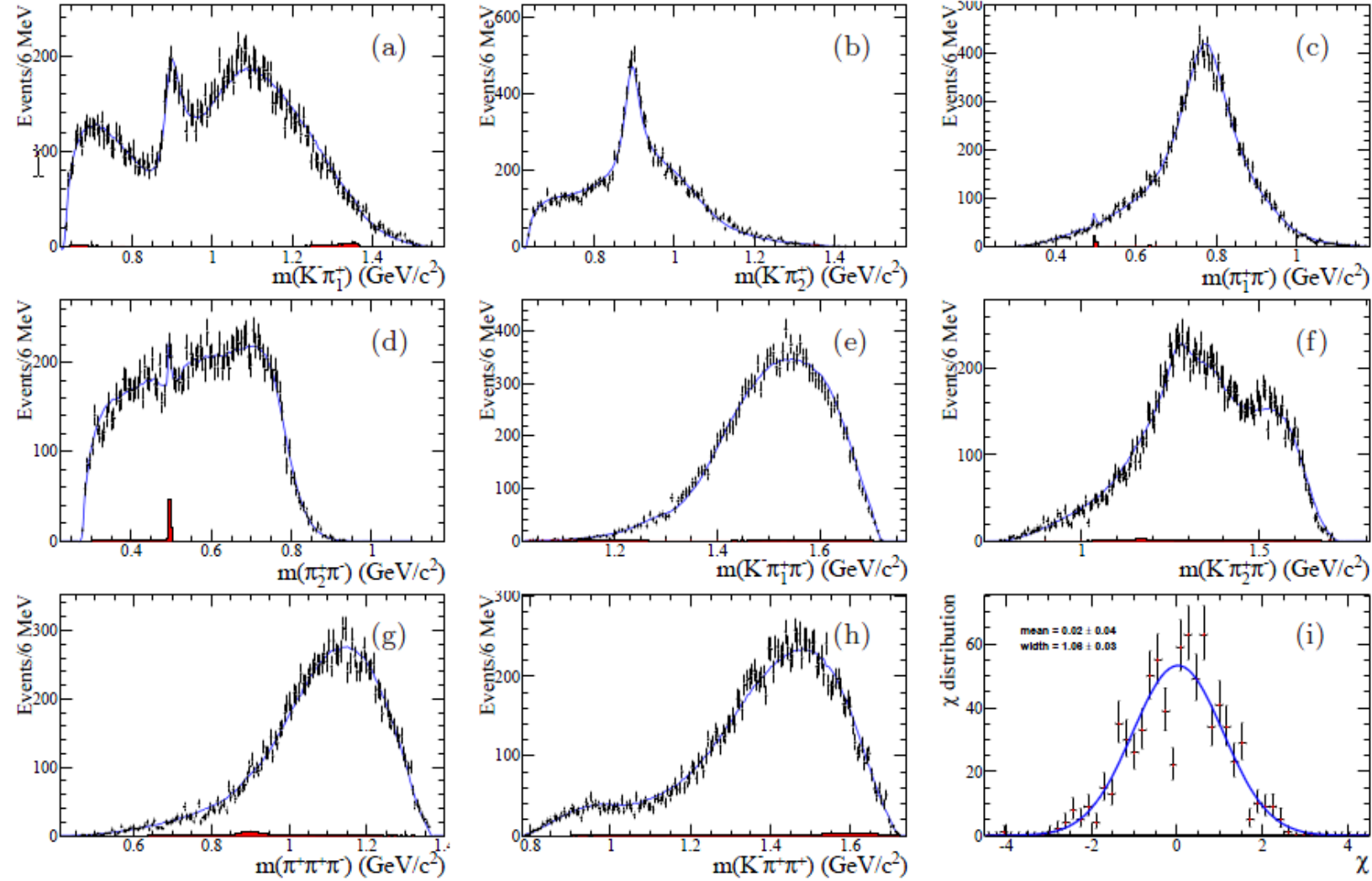
- small statistical errors and clean background

Amplitude Analysis Results of $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$

Double tag $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ vs. $D^0 \rightarrow K^+ \pi^-$

Amplitude	ϕ_i	Fit fraction (%)
$D^0[S] \rightarrow \bar{K}^* \rho^0$	$2.35 \pm 0.06 \pm 0.18$	$6.5 \pm 0.5 \pm 0.8$
$D^0[P] \rightarrow \bar{K}^* \rho^0$	$-2.25 \pm 0.08 \pm 0.15$	$2.3 \pm 0.2 \pm 0.1$
$D^0[D] \rightarrow \bar{K}^* \rho^0$	$2.49 \pm 0.06 \pm 0.11$	$7.9 \pm 0.4 \pm 0.7$
$D^0 \rightarrow K^- a_1^+(1260), a_1^+(1260)[S] \rightarrow \rho^0 \pi^+$	0(fixed)	$53.2 \pm 2.8 \pm 4.0$
$D^0 \rightarrow K^- a_1^+(1260), a_1^+(1260)[D] \rightarrow \rho^0 \pi^+$	$-2.11 \pm 0.15 \pm 0.21$	$0.3 \pm 0.1 \pm 0.1$
$D^0 \rightarrow K_1^-(1270) \pi^+, K_1^-(1270)[S] \rightarrow \bar{K}^{*0} \pi^-$	$1.48 \pm 0.21 \pm 0.24$	$0.1 \pm 0.1 \pm 0.1$
$D^0 \rightarrow K_1^-(1270) \pi^+, K_1^-(1270)[D] \rightarrow \bar{K}^{*0} \pi^-$	$3.00 \pm 0.09 \pm 0.15$	$0.7 \pm 0.2 \pm 0.2$
$D^0 \rightarrow K_1^-(1270) \pi^+, K_1^-(1270) \rightarrow K^- \rho^0$	$-2.46 \pm 0.06 \pm 0.21$	$3.4 \pm 0.3 \pm 0.5$
$D^0 \rightarrow (\rho^0 K^-)_A \pi^+, (\rho^0 K^-)_A[D] \rightarrow K^- \rho^0$	$-0.43 \pm 0.09 \pm 0.12$	$1.1 \pm 0.2 \pm 0.3$
$D^0 \rightarrow (K^- \rho^0)_P \pi^+$	$-0.14 \pm 0.11 \pm 0.10$	$7.4 \pm 1.6 \pm 5.7$
$D^0 \rightarrow (K^- \pi^+)_S \rho^0$	$-2.45 \pm 0.19 \pm 0.47$	$2.0 \pm 0.7 \pm 1.9$
$D^0 \rightarrow (K^- \rho^0)_V \pi^+$	$-1.34 \pm 0.12 \pm 0.09$	$0.4 \pm 0.1 \pm 0.1$
$D^0 \rightarrow (\bar{K}^{*0} \pi^-)_P \pi^+$	$-2.09 \pm 0.12 \pm 0.22$	$2.4 \pm 0.5 \pm 0.5$
$D^0 \rightarrow \bar{K}^{*0} (\pi^+ \pi^-)_S$	$-0.17 \pm 0.11 \pm 0.12$	$2.6 \pm 0.6 \pm 0.6$
$D^0 \rightarrow (\bar{K}^{*0} \pi^-)_V \pi^+$	$-2.13 \pm 0.10 \pm 0.11$	$0.8 \pm 0.1 \pm 0.1$
$D^0 \rightarrow ((K^- \pi^+)_S \pi^-)_A \pi^+$	$-1.36 \pm 0.08 \pm 0.37$	$5.6 \pm 0.9 \pm 2.7$
$D^0 \rightarrow K^- ((\pi^+ \pi^-)_S \pi^+)_A$	$-2.23 \pm 0.08 \pm 0.22$	$13.1 \pm 1.9 \pm 2.2$
$D^0 \rightarrow (K^- \pi^+)_S (\pi^+ \pi^-)_S$	$-1.40 \pm 0.04 \pm 0.22$	$16.3 \pm 0.5 \pm 0.6$
$D^0[S] \rightarrow (K^- \pi^+)_V (\pi^+ \pi^-)_V$	$1.59 \pm 0.13 \pm 0.41$	$5.4 \pm 1.2 \pm 1.9$
$D^0 \rightarrow (K^- \pi^+)_S (\pi^+ \pi^-)_V$	$-0.16 \pm 0.17 \pm 0.43$	$1.9 \pm 0.6 \pm 1.2$
$D^0 \rightarrow (K^- \pi^+)_V (\pi^+ \pi^-)_S$	$2.58 \pm 0.08 \pm 0.25$	$2.9 \pm 0.5 \pm 1.7$
$D^0 \rightarrow (K^- \pi^+)_T (\pi^+ \pi^-)_S$	$-2.92 \pm 0.14 \pm 0.12$	$0.3 \pm 0.1 \pm 0.1$
$D^0 \rightarrow (K^- \pi^+)_S (\pi^+ \pi^-)_T$	$2.45 \pm 0.12 \pm 0.37$	$0.5 \pm 0.1 \pm 0.1$

Amplitude Analysis Results of $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$



Component	Fit fraction (%)
$D^0 \rightarrow \bar{K}^{*0} \rho^0$	$12.3 \pm 0.4 \pm 0.5$
$D^0 \rightarrow K^- a_1^+(1260) (\rho^0 \pi^+)$	$54.6 \pm 2.8 \pm 3.7$
$D^0 \rightarrow K_1^-(1270) (\bar{K}^{*0} \pi^-) \pi^+$	$0.8 \pm 0.2 \pm 0.2$
$D^0 \rightarrow K_1^-(1270) (K^- \rho^0) \pi^+$	$3.4 \pm 0.3 \pm 0.2$
$D^0 \rightarrow K^- \pi^+ \rho^0$	$8.4 \pm 1.1 \pm 2.2$
$D^0 \rightarrow \bar{K}^{*0} \pi^+ \pi^-$	$7.0 \pm 0.4 \pm 0.3$
$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	$21.9 \pm 0.6 \pm 0.6$

Published in PRD 95, 072010

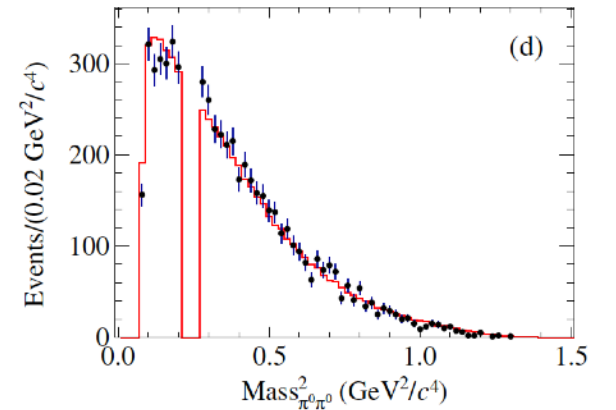
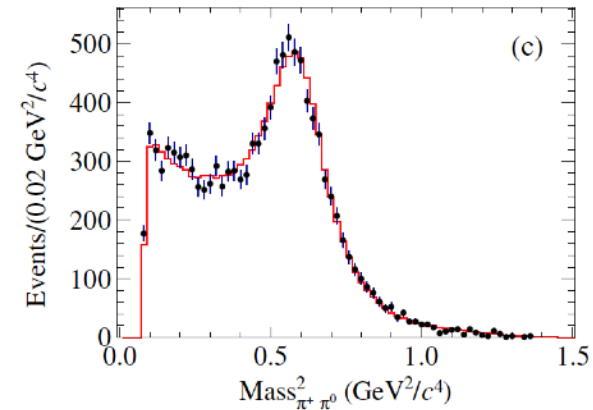
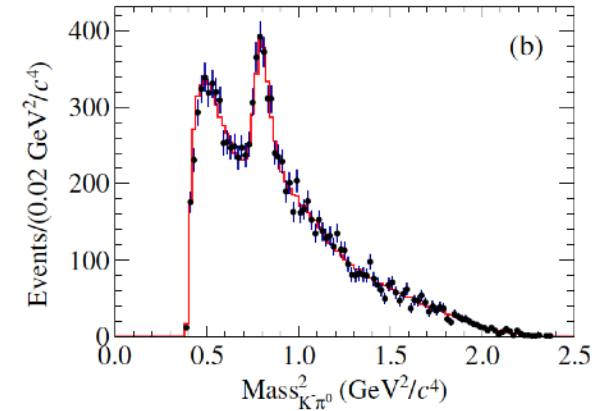
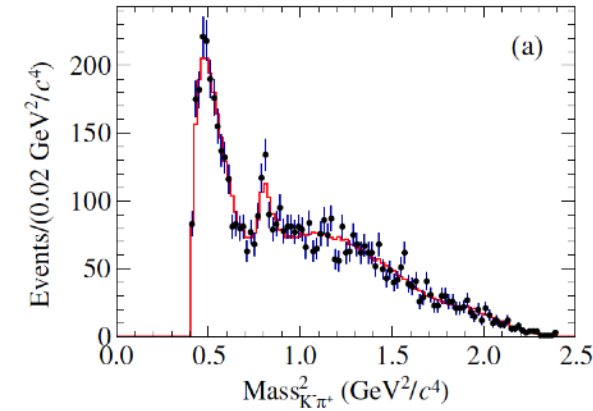
Amplitude Analysis Results of $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$

Double tag: $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$ (signal) vs. $\bar{D}^0 \rightarrow K^+ \pi^-$ (tag)

The number of event selected is 5950 with a purity of $\sim 99\%$

The data can be described with 26 amplitudes:

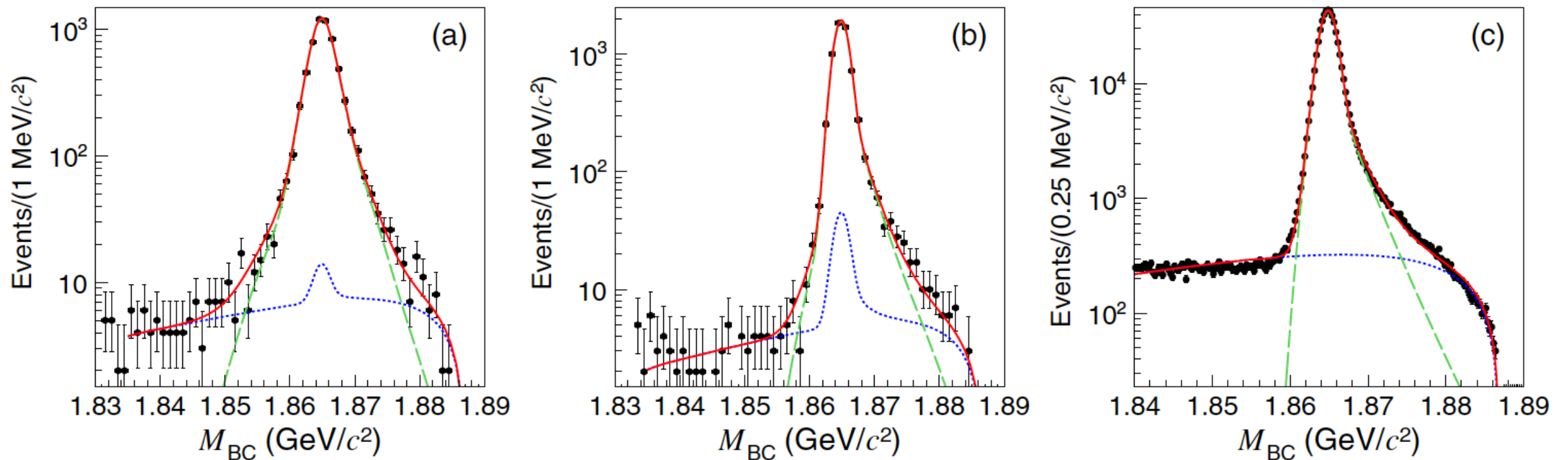
Amplitude mode	FF(%)	Phase (ϕ)
$D \rightarrow SS$		
$D \rightarrow (K^- \pi^+)_{S\text{-wave}} (\pi^0 \pi^0)_S$	$6.92 \pm 1.44 \pm 2.86$	$-0.75 \pm 0.15 \pm 0.47$
$D \rightarrow (K^- \pi^0)_{S\text{-wave}} (\pi^+ \pi^0)_S$	$4.18 \pm 1.02 \pm 1.77$	$-2.90 \pm 0.19 \pm 0.47$
$D \rightarrow AP, A \rightarrow VP$		
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0[S]$	$28.36 \pm 2.50 \pm 3.53$	0 (fixed)
$D \rightarrow K^- a_1(1260)^+, \rho^+ \pi^0[D]$	$0.68 \pm 0.29 \pm 0.30$	$-2.05 \pm 0.17 \pm 0.25$
$D \rightarrow K_1(1270)^- \pi^+, K^{*-} \pi^0[S]$	$0.15 \pm 0.09 \pm 0.18$	$1.84 \pm 0.34 \pm 0.43$
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0[S]$	$0.39 \pm 0.18 \pm 0.30$	$-1.55 \pm 0.20 \pm 0.26$
$D \rightarrow K_1(1270)^0 \pi^0, K^{*0} \pi^0[D]$	$0.11 \pm 0.11 \pm 0.13$	$-1.35 \pm 0.43 \pm 0.48$
$D \rightarrow K_1(1270)^0 \pi^0, K^- \rho^+[S]$	$2.71 \pm 0.38 \pm 0.29$	$-2.07 \pm 0.09 \pm 0.20$
$D \rightarrow (K^{*-} \pi^0)_A \pi^+, K^{*-} \pi^0[S]$	$1.85 \pm 0.62 \pm 1.11$	$1.93 \pm 0.10 \pm 0.15$
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0[S]$	$3.13 \pm 0.45 \pm 0.58$	$0.44 \pm 0.12 \pm 0.21$
$D \rightarrow (K^{*0} \pi^0)_A \pi^0, K^{*0} \pi^0[D]$	$0.46 \pm 0.17 \pm 0.29$	$-1.84 \pm 0.26 \pm 0.42$
$D \rightarrow (\rho^+ K^-)_A \pi^0, K^- \rho^+[D]$	$0.75 \pm 0.40 \pm 0.60$	$0.64 \pm 0.36 \pm 0.53$
$D \rightarrow AP, A \rightarrow SP$		
$D \rightarrow ((K^- \pi^+)_{S\text{-wave}} \pi^0)_A \pi^0$	$1.99 \pm 1.08 \pm 1.55$	$-0.02 \pm 0.25 \pm 0.53$
$D \rightarrow VS$		
$D \rightarrow (K^- \pi^0)_{S\text{-wave}} \rho^+$	$14.63 \pm 1.70 \pm 2.41$	$-2.39 \pm 0.11 \pm 0.35$
$D \rightarrow K^{*-} (\pi^+ \pi^0)_S$	$0.80 \pm 0.38 \pm 0.26$	$1.59 \pm 0.19 \pm 0.24$
$D \rightarrow K^{*0} (\pi^0 \pi^0)_S$	$0.12 \pm 0.27 \pm 0.27$	$1.45 \pm 0.48 \pm 0.51$
$D \rightarrow VP, V \rightarrow VP$		
$D \rightarrow (K^{*-} \pi^+)_V \pi^0$	$2.25 \pm 0.43 \pm 0.45$	$0.52 \pm 0.12 \pm 0.17$
$D \rightarrow VV$		
$D[S] \rightarrow K^{*-} \rho^+$	$5.15 \pm 0.75 \pm 1.28$	$1.24 \pm 0.11 \pm 0.23$
$D[P] \rightarrow K^{*-} \rho^+$	$3.25 \pm 0.55 \pm 0.41$	$-2.89 \pm 0.10 \pm 0.18$
$D[D] \rightarrow K^{*-} \rho^+$	$10.90 \pm 1.53 \pm 2.36$	$2.41 \pm 0.08 \pm 0.16$
$D[P] \rightarrow (K^- \pi^0)_V \rho^+$	$0.36 \pm 0.19 \pm 0.27$	$-0.94 \pm 0.19 \pm 0.28$
$D[D] \rightarrow (K^- \pi^0)_V \rho^+$	$2.13 \pm 0.56 \pm 0.92$	$-1.93 \pm 0.22 \pm 0.25$
$D[D] \rightarrow K^{*-} (\pi^+ \pi^0)_V$	$1.66 \pm 0.52 \pm 0.61$	$-1.17 \pm 0.20 \pm 0.39$
$D[S] \rightarrow (K^- \pi^0)_V (\pi^+ \pi^0)_V$	$5.17 \pm 1.91 \pm 1.82$	$-1.74 \pm 0.20 \pm 0.31$
$D \rightarrow TS$		
$D \rightarrow (K^- \pi^+)_{S\text{-wave}} (\pi^0 \pi^0)_T$	$0.30 \pm 0.21 \pm 0.32$	$-2.93 \pm 0.31 \pm 0.82$
$D \rightarrow (K^- \pi^0)_{S\text{-wave}} (\pi^+ \pi^0)_T$	$0.14 \pm 0.12 \pm 0.10$	$2.23 \pm 0.38 \pm 0.65$



Branching Fraction Results of $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$

Double tag(DT) $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$ vs. $\bar{D}^0 \rightarrow K^+ \pi^-$
Single tag(ST) $\bar{D}^0 \rightarrow K^+ \pi^-$

$$\mathcal{B}_{\text{sig}} = \frac{N_{\text{tag,sig}}^{\text{DT}}}{N_{\text{tag}}^{\text{ST}}} \frac{\varepsilon_{\text{tag}}}{\varepsilon_{\text{tag,sig}}}$$



The amplitude analysis result is used to determine the detection efficiency, where the DT efficiency is 8.39%

The branching fraction is determined to be

$$(8.86 \pm 0.13(\text{stat}) \pm 0.19(\text{syst}))\%$$

Amplitude Analysis of $D^+ \rightarrow K_S \pi^+ \pi^+ \pi^-$

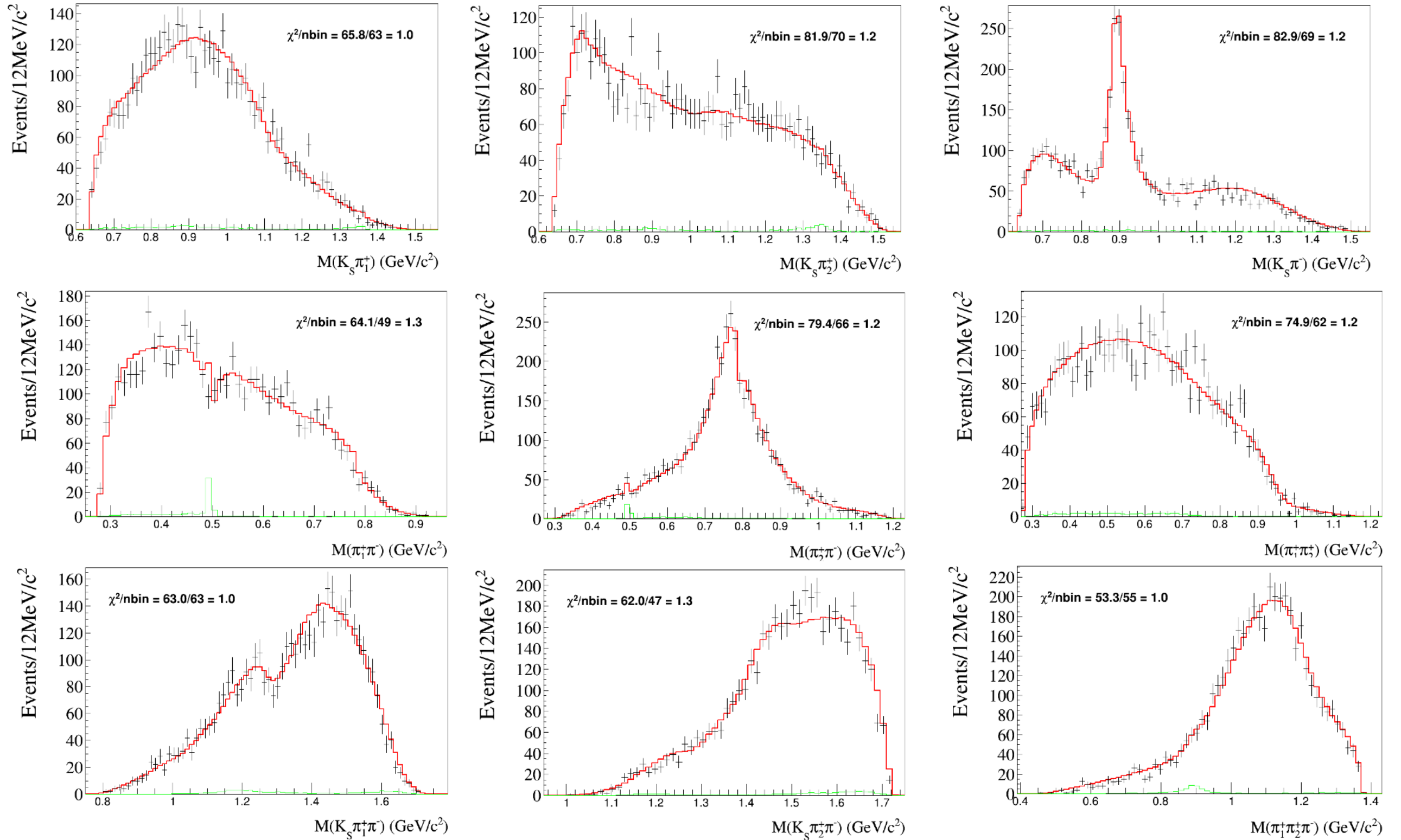
Double tag $D^+ \rightarrow K_S \pi^+ \pi^+ \pi^-$ vs. $D^- \rightarrow K^+ \pi^- \pi^-$

The number of event selected is 4559 with a purity of ~99%

The data can be described with 12 amplitudes:

Amplitude	ϕ	fit fraction
$D^+ \rightarrow K_S^0 a_1(1260)^+, a_1(1260)^+ \rightarrow \rho^0 \pi^+[S]$	0.000(fixed)	$0.567 \pm 0.020 \pm 0.044$
$D^+ \rightarrow K_S^0 a_1(1260)^+, a_1(1260)^+ \rightarrow f_0(500) \pi^+$	$-2.023 \pm 0.068 \pm 0.113$	$0.050 \pm 0.006 \pm 0.007$
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+, \bar{K}_1(1400)^0 \rightarrow K^{*-} \pi^+[S]$	$-2.714 \pm 0.038 \pm 0.051$	$0.380 \pm 0.013 \pm 0.014$
$D^+ \rightarrow \bar{K}_1(1400)^0 \pi^+, \bar{K}_1(1400)^0 \rightarrow K^{*-} \pi^+[D]$	$3.431 \pm 0.137 \pm 0.117$	$0.015 \pm 0.004 \pm 0.005$
$D^+ \rightarrow \bar{K}_1(1270)^0 \pi^+, \bar{K}_1(1270)^0 \rightarrow K_S^0 \rho^0[S]$	$-0.418 \pm 0.070 \pm 0.087$	$0.036 \pm 0.004 \pm 0.002$
$D^+ \rightarrow K(1460)^0 \pi^+, K(1460)^0 \rightarrow K_S^0 \rho^0$	$-1.850 \pm 0.120 \pm 0.223$	$0.014 \pm 0.004 \pm 0.003$
$D^+ \rightarrow (K_S^0 \rho^0)_A[D] \pi^+$	$2.328 \pm 0.097 \pm 0.068$	$0.011 \pm 0.003 \pm 0.002$
$D^+ \rightarrow K_S^0 (\rho^0 \pi^+)_P$	$1.656 \pm 0.083 \pm 0.056$	$0.031 \pm 0.004 \pm 0.010$
$D^+ \rightarrow (K^{*-} \pi^+)_A[S] \pi^+$	$-4.321 \pm 0.047 \pm 0.073$	$0.132 \pm 0.011 \pm 0.011$
$D^+ \rightarrow (K^{*-} \pi^+)_A[D] \pi^+$	$0.989 \pm 0.158 \pm 0.229$	$0.013 \pm 0.004 \pm 0.004$
$D^+ \rightarrow (K_S^0 (\pi^+ \pi^-)_S)_A \pi^+$	$-2.935 \pm 0.060 \pm 0.125$	$0.051 \pm 0.004 \pm 0.003$
$D^+ \rightarrow ((K_S^0 \pi^-)_S \pi^+)_P \pi^+$	$1.864 \pm 0.069 \pm 0.288$	$0.022 \pm 0.003 \pm 0.003$

Amplitude Analysis of $D^+ \rightarrow K_S \pi^+ \pi^+ \pi^-$



Amplitude Analysis of $D^+ \rightarrow K_S \pi^+ \pi^+ \pi^-$

The preliminary results of branching fractions for different components :

Component	Branching fraction (%)
$D^+ \rightarrow K_S^0 a_1(1260)^+ (\rho^0 \pi^+)$	$1.684 \pm 0.059 \pm 0.131 \pm 0.062$
$D^+ \rightarrow K_S^0 a_1(1260)^+ (f_0(500) \pi^+)$	$0.149 \pm 0.018 \pm 0.021 \pm 0.006$
$D^+ \rightarrow \bar{K}_1(1400)^0 (K^{*-} \pi^+) \pi^+$	$1.105 \pm 0.045 \pm 0.048 \pm 0.041$
$D^+ \rightarrow \bar{K}_1(1270)^0 (K_S^0 \rho^0) \pi^+$	$0.107 \pm 0.012 \pm 0.006 \pm 0.004$
$D^+ \rightarrow \bar{K}(1460)^0 (K_S^0 \rho^0) \pi^+$	$0.042 \pm 0.012 \pm 0.009 \pm 0.002$
$D^+ \rightarrow K_S^0 \pi^+ \rho^0$	$0.131 \pm 0.015 \pm 0.015 \pm 0.005$
$D^+ \rightarrow K^{*-} \pi^+ \pi^+$	$0.413 \pm 0.036 \pm 0.059 \pm 0.015$
$D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$	$0.220 \pm 0.015 \pm 0.024 \pm 0.008$

stat. uncertainty from FF

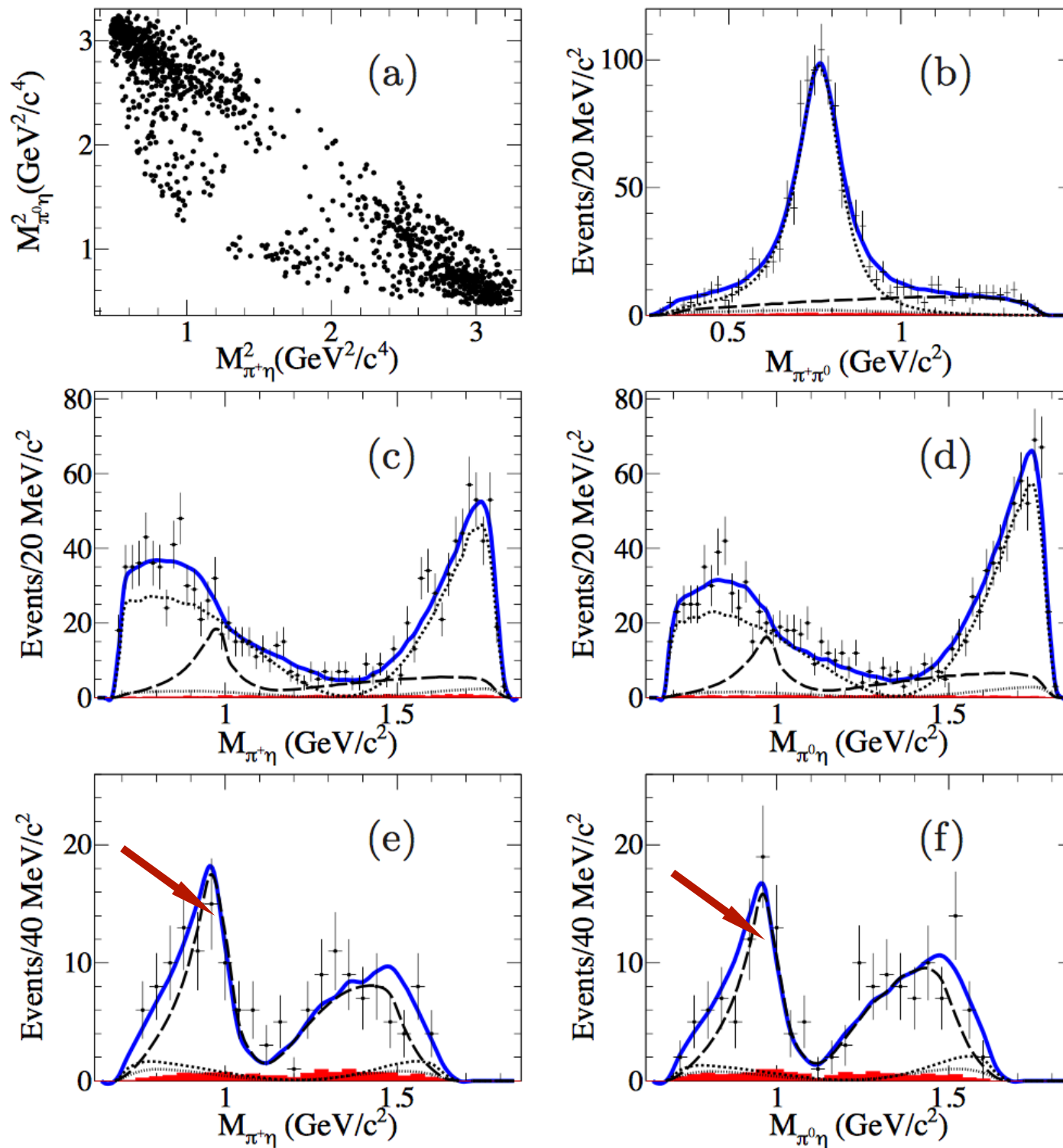
sys. uncertainty from FF

uncertainties related to $\text{BF}(D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-)$ in PDG

The measurements of the decays with $K1(1270)$ and $K1(1400)$ involved provide some experimental information in understanding the mixture of the two excited Kaons.

Amplitude Analysis of $D_s^+ \rightarrow \pi^+ \pi^0 \eta$

Observation of $D_s^+ \rightarrow a_0(980) \pi^0 + \pi^+$

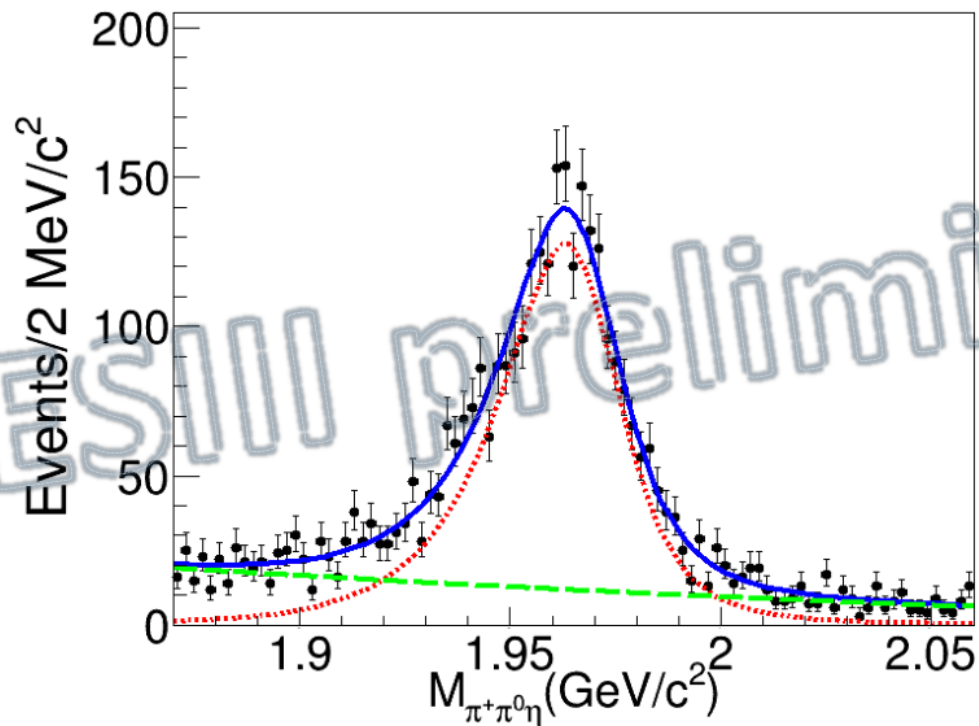


Dots with error bar: data
Solid line: total fit
Dashed line: rho+ eta
Long-dashed line: $a_0(980)\pi$

The phase difference between $a_0(980)^0\pi^+$ and $a_0(980)^+\pi^0$ is found to agree with 180°

Amplitude Analysis of $D_s^+ \rightarrow \pi^+ \pi^0 \eta$

Fit to signal mode



Total Tag yield: 255895 ± 1358 .

DT yield: 2626 ± 77 .

Efficiency is determined with the amplitude analysis result.

- Dots with error bars: data.
- Total fit.
- Signal: MC shape convoluted with a Gaussian.
- Background: second-order Chebychev.

$$BF(D_s^+ \rightarrow \pi^+ \pi^0 \eta) = (9.50 \pm 0.28_{stat.} \pm 0.41_{sys.})\%$$

Branching fraction (%)
$\mathcal{B}(D_s^+ \rightarrow \rho^+ \eta) = 7.44 \pm 0.48_{stat.} \pm 0.44_{sys.}$
$\mathcal{B}(D_s^+ \rightarrow a_0(980)\pi)^* = 2.20 \pm 0.22_{stat.} \pm 0.34_{sys.}$
$\mathcal{B}(D_s^+ \rightarrow a_0(980)^+ \pi^0)^* = 1.46 \pm 0.15_{stat.} \pm 0.22_{sys.}$
$\mathcal{B}(D_s^+ \rightarrow a_0(980)^0 \pi^+)^* = 1.46 \pm 0.15_{stat.} \pm 0.22_{sys.}$

$$BF(\text{sub-mode } n) = \mathcal{B}(D_s^+ \rightarrow \pi^+ \pi^0 \eta) FF(n)$$

First observation

The measured $\mathcal{B}(D_s^+ \rightarrow a_0(980)^+ \pi^0)$ is larger than other measured pure W -annihilation decays ($D_s^+ \rightarrow p\eta$, $D_s^+ \rightarrow \omega \pi^+$) by one order.

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Summary

- DTag and DD^{bar} threshold data allows us to perform inclusive and exclusive branching fraction measurement
- Double tag provides clean samples for amplitude analysis
- Many D^0 and D^+ studies have been published, including strong phase and y_{cp} measurements, and more related measurements are on-going
- Excellent D_s studies are published based on our 3.19 fb^{-1} data at $E_{\text{cm}} = 4.178 \text{ GeV}$ (and at $4.190\text{-}4.230 \text{ GeV}$)
 - “Many” D_s amplitude analyses of three- and four-body decays are expected to be published in the next year.