



Probing dark matter at e^+e^- colliders

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Zuowei Liu, **Yu Zhang**, 1808.00983, PRD

Zuowei Liu, Yong-Heng Xu, **Yu Zhang**, 1903.12114, JHEP

Jinhan Liang, Zuowei Liu, Yue Ma, **Yu Zhang**, 1909.06847

Yu Zhang, et. al., 1907.07046, PRD

第三届北京师范大学暗物质研讨会

珠海 2019年12月8日



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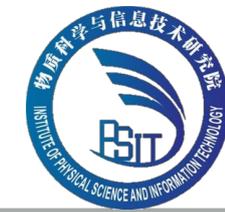
珠海 2019年12月8日



Outline

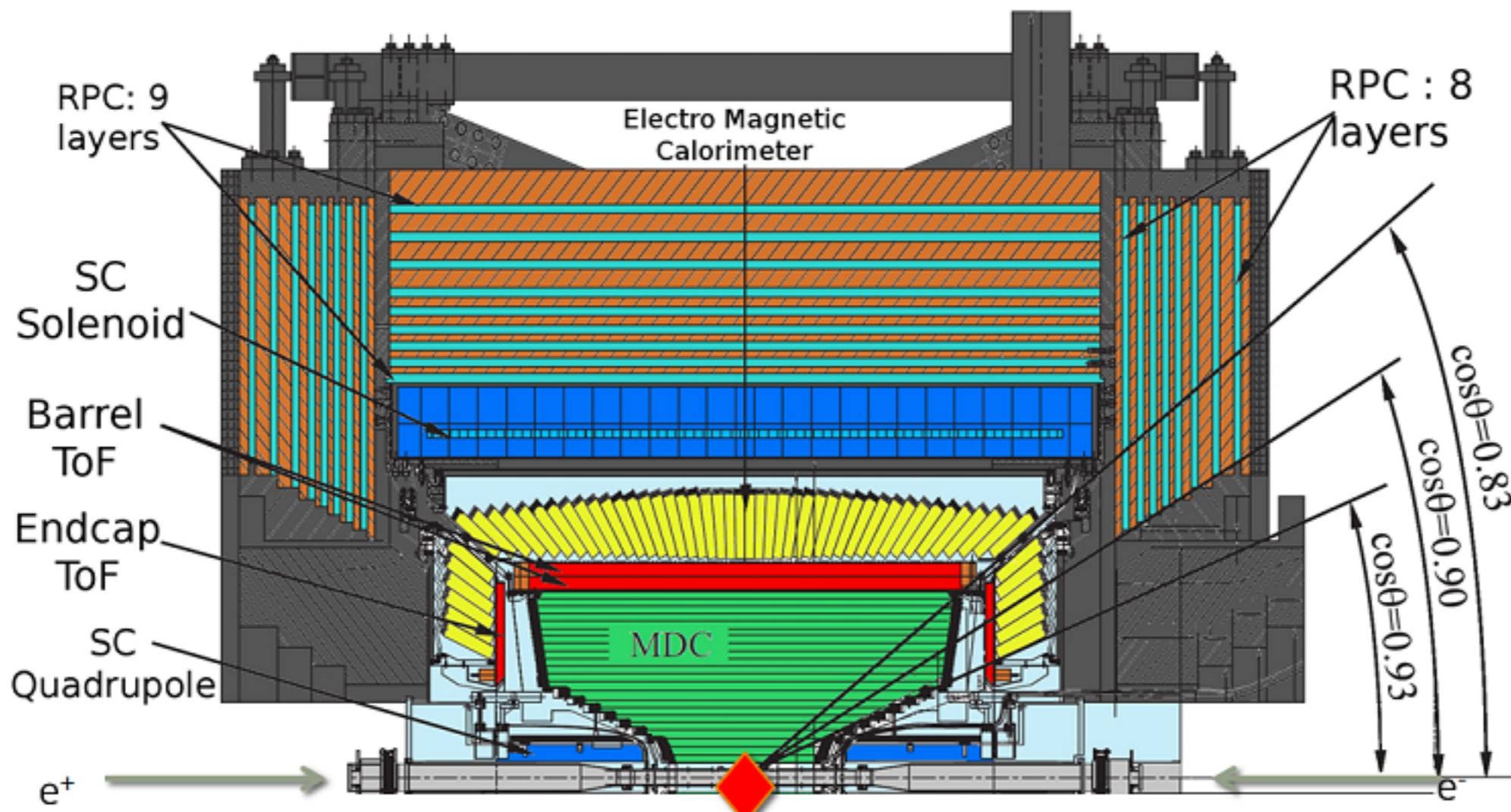


- e^+e^- colliders
- Millicharge DM models at BESIII/STCF/Belle2/Babar/CEPC
- Z' DM models at CEPC
- DM effective operators at CEPC
- Dark photon invisible decay at BESIII/STCF
- Summary



e^+e^- colliders





主漂移室 (MDC) : $|\cos \theta| < 0.93$

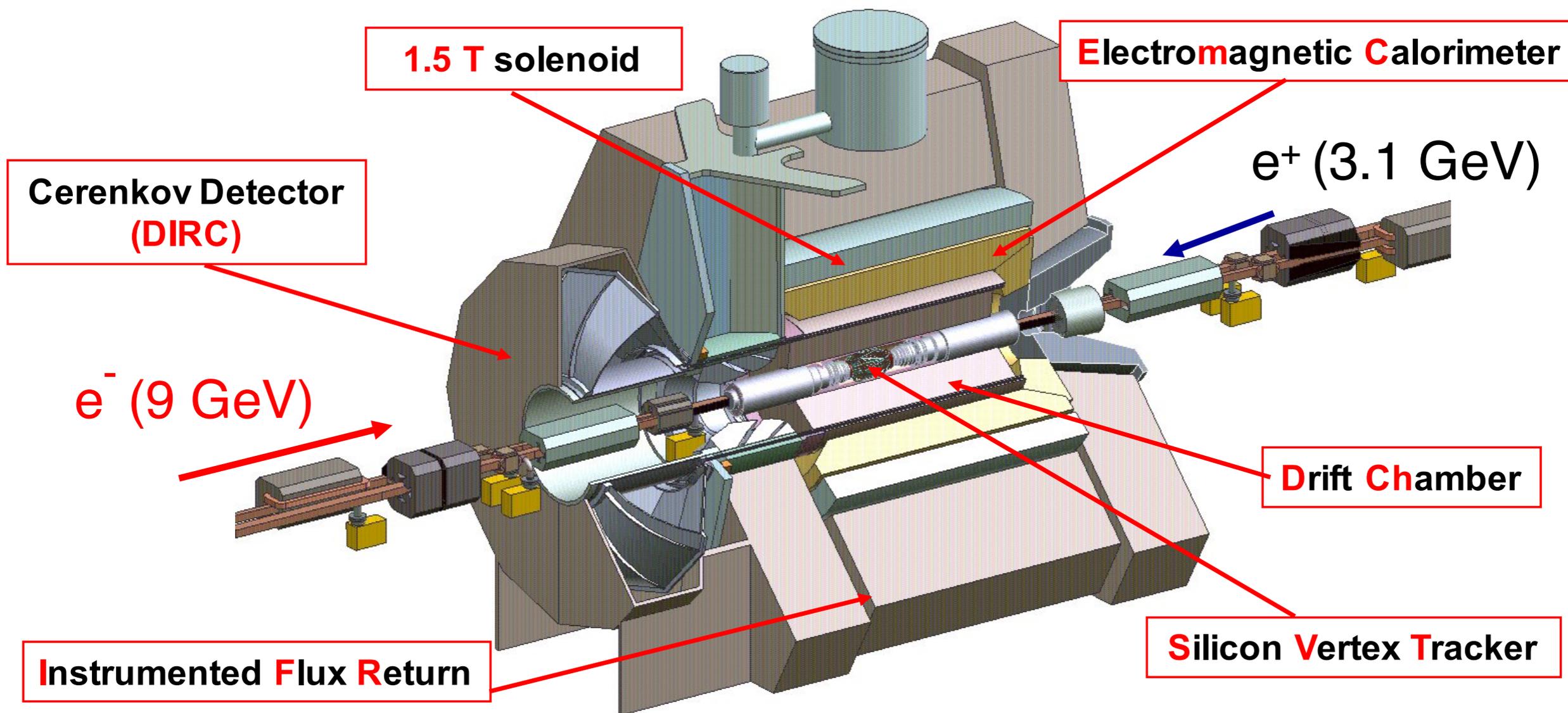
飞行时间计数器 (TOF) : $|\cos \theta| < 0.83$ $0.85 < |\cos \theta| < 0.95$

电磁量能器 (EMC) : $|\cos \theta| < 0.83$ $0.85 < |\cos \theta| < 0.93$

Super Tau-Charm Facility (STCF)

- Peak luminosity $0.5-1 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ at **4 GeV**
- Energy range $E_{\text{cm}} = \mathbf{2-7\text{GeV}}$
- **Polarization** available on electron beam (Phase II)
- Basic **Features** of machine :
 - **Symmetric** machine with **dual-ring**
 - **Large Piwinski angle** collision + **crabbed waist** solution for the IR
 - **Siberia snake** for polarization
 - **Total cost 4B RMB**

From H. Peng @CHARM18



The BaBar detector was built at [SLAC](#) to study the millions of B mesons produced by the [PEP-II](#) storage ring.



PEP-II/BaBar



PEP-II Records

Last update:
April 8, 2008

Peak Luminosity

$12.069 \times 10^{33} \text{ cm}^{-2} \text{ sec}^{-1}$

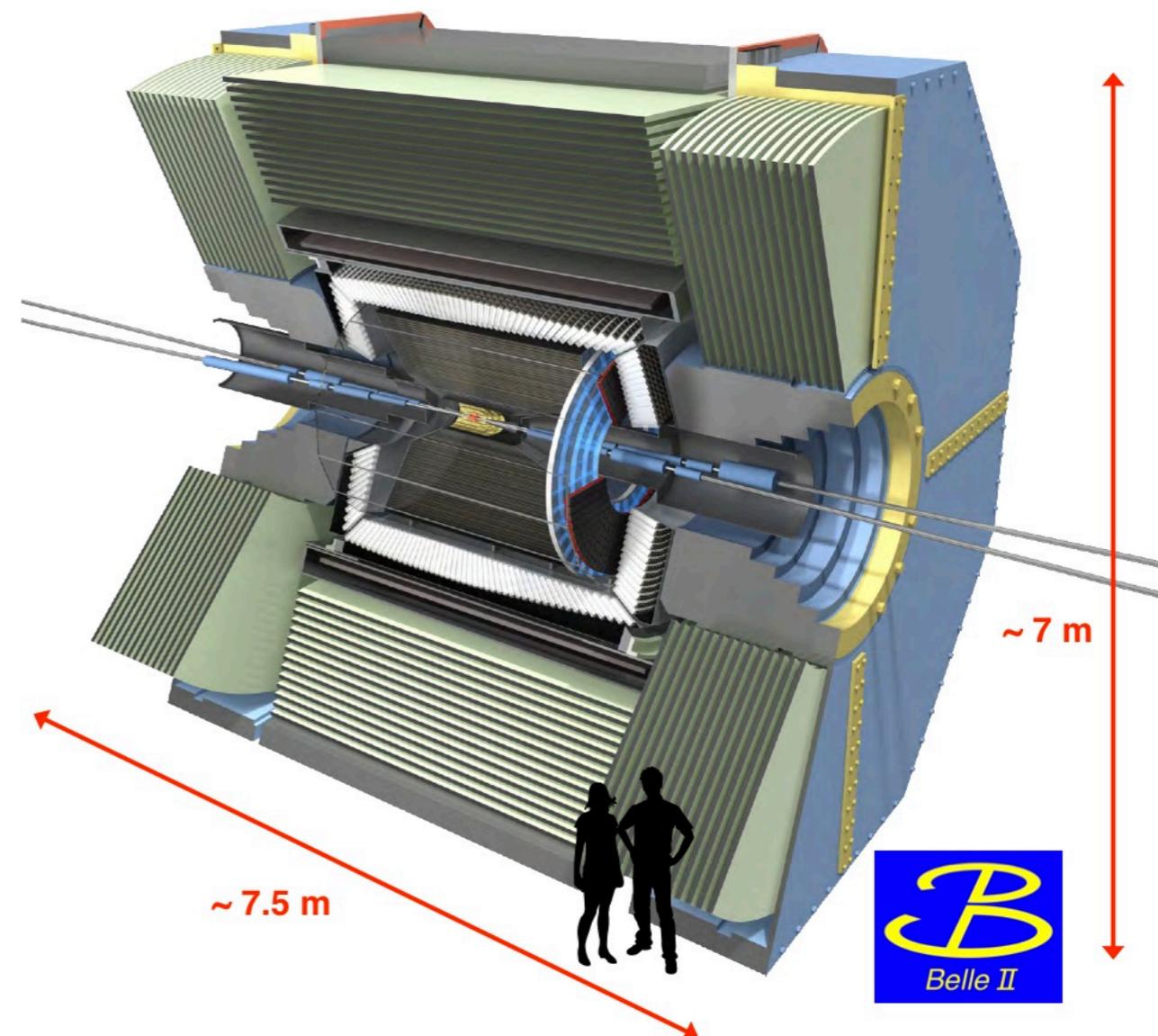
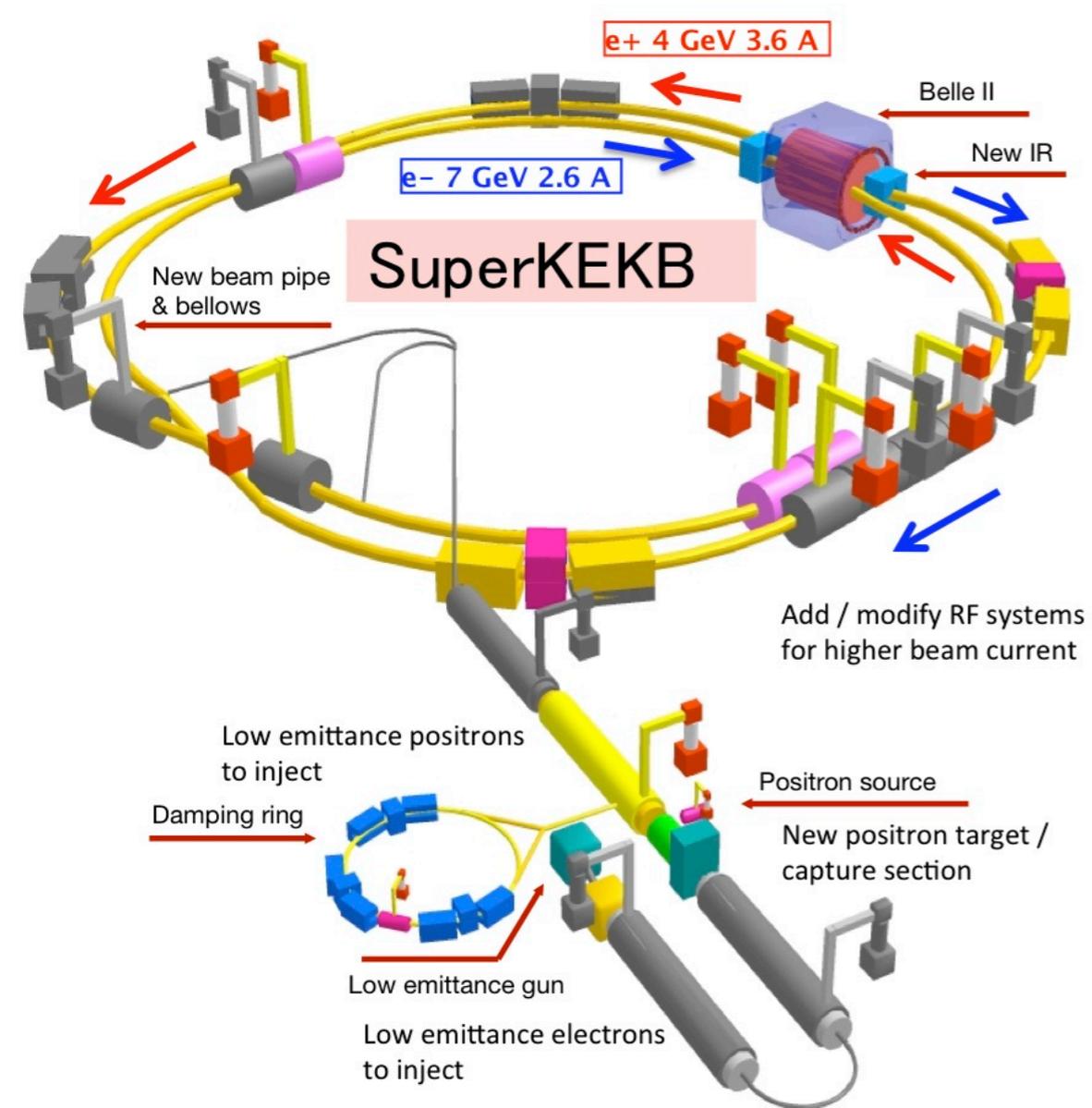
1722 bunches 2900 mA LER 1875 mA HER

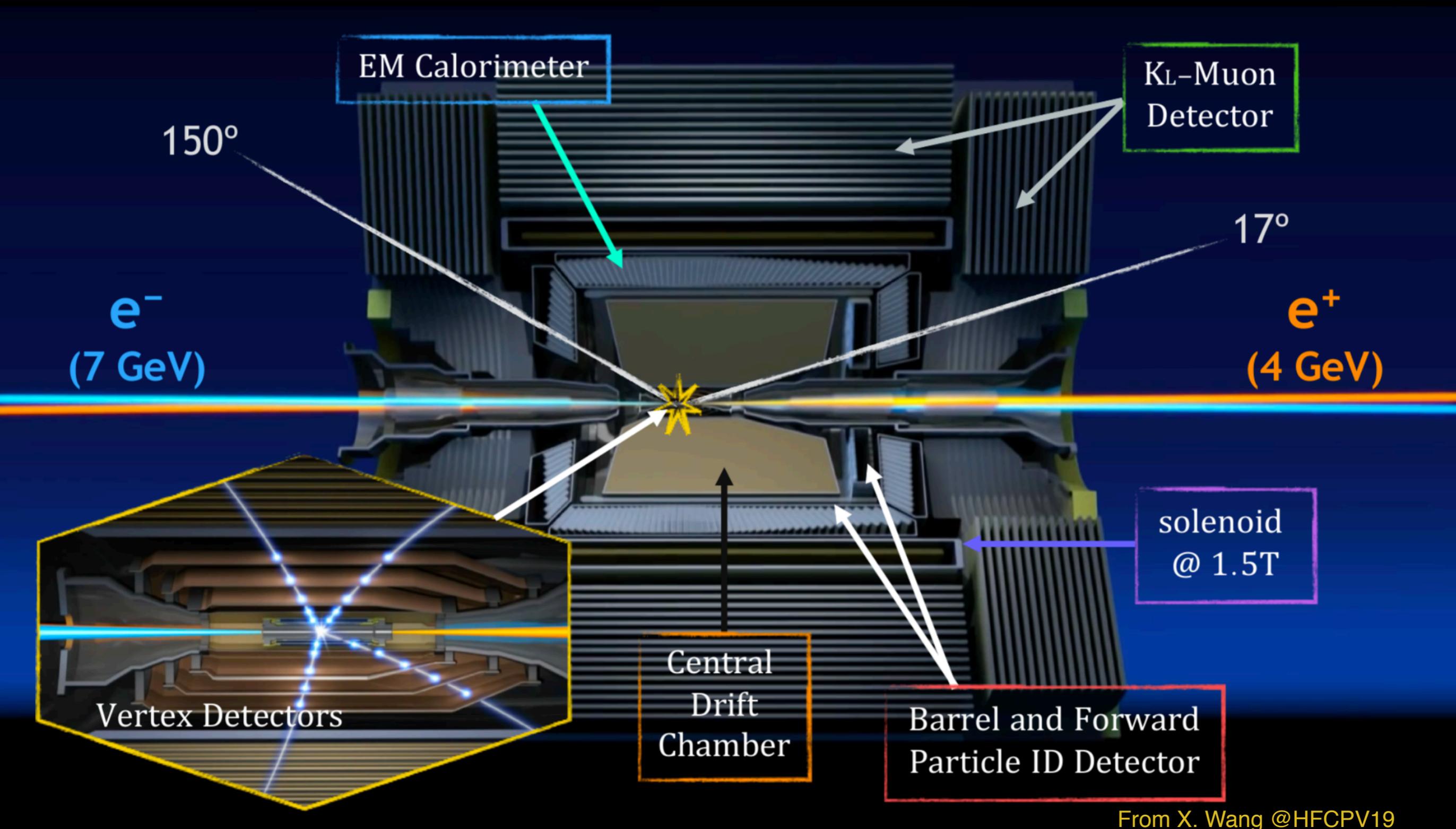
August 16, 2006

Integration records of delivered luminosity

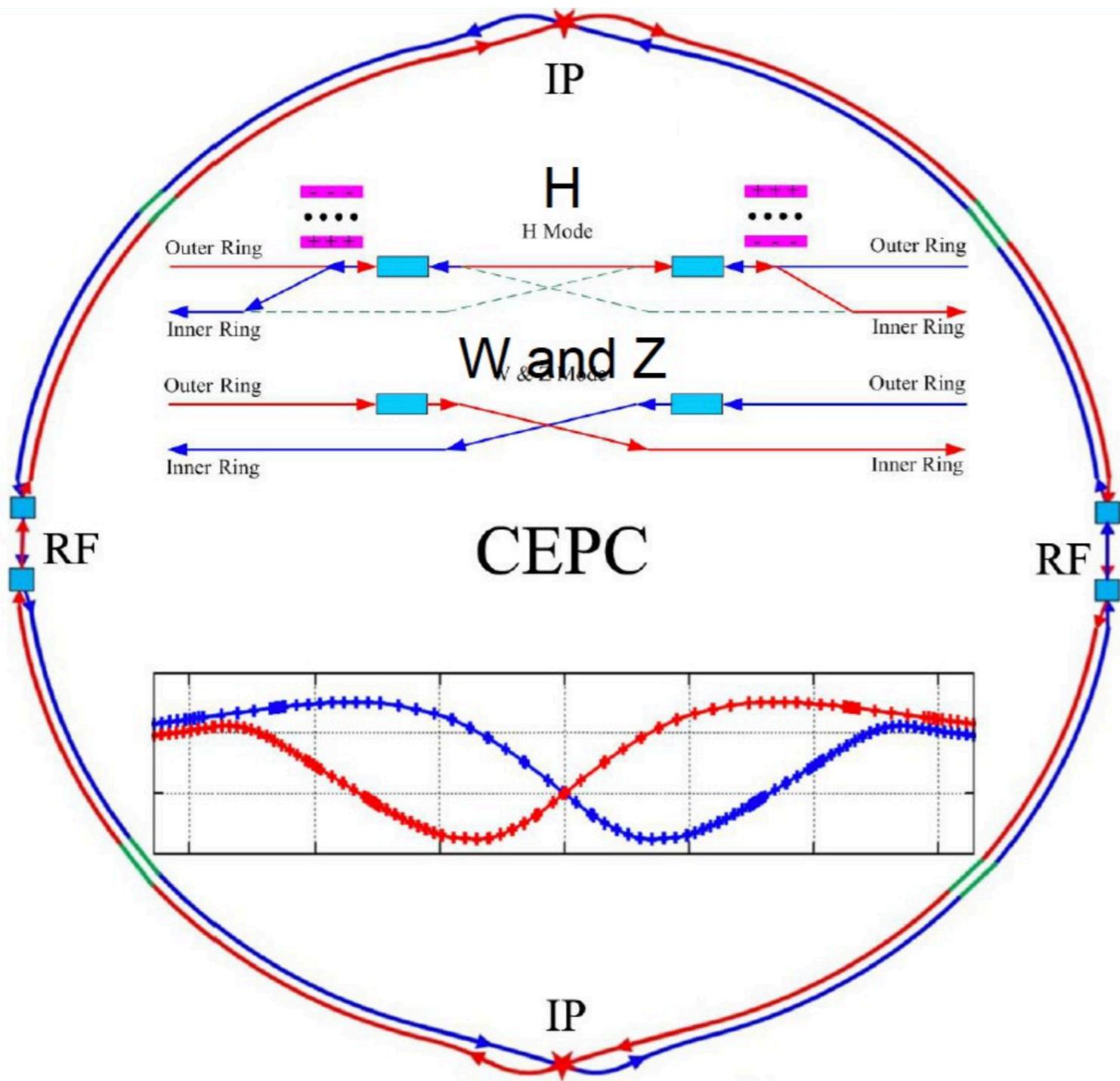
Best shift (8 hrs, 0:00, 08:00, 16:00)	339.0 pb ⁻¹	Aug 16, 2006
Best 3 shifts in a row	910.7 pb ⁻¹	Jul 2-3, 2006
Best day	858.4 pb ⁻¹	Aug 19, 2007
Best 7 days (0:00 to 24:00)	5.411 fb ⁻¹	Aug 14-Aug 20, 2007
Best week (Sun 0:00 to Sat 24:00)	5.137 fb ⁻¹	Aug 12-Aug 18, 2007
Peak HER current	2069 mA	Feb 29, 2008
Peak LER current	3213 mA	Apr 7, 2008
Best 30 days	19.776 fb ⁻¹	Aug 5 – Sep 3, 2007
Best month	19.732 fb ⁻¹	August 2007
Total delivered	557 fb ⁻¹	

PEP-II turned off April 7, 2008





From X. Wang @HFPCV19

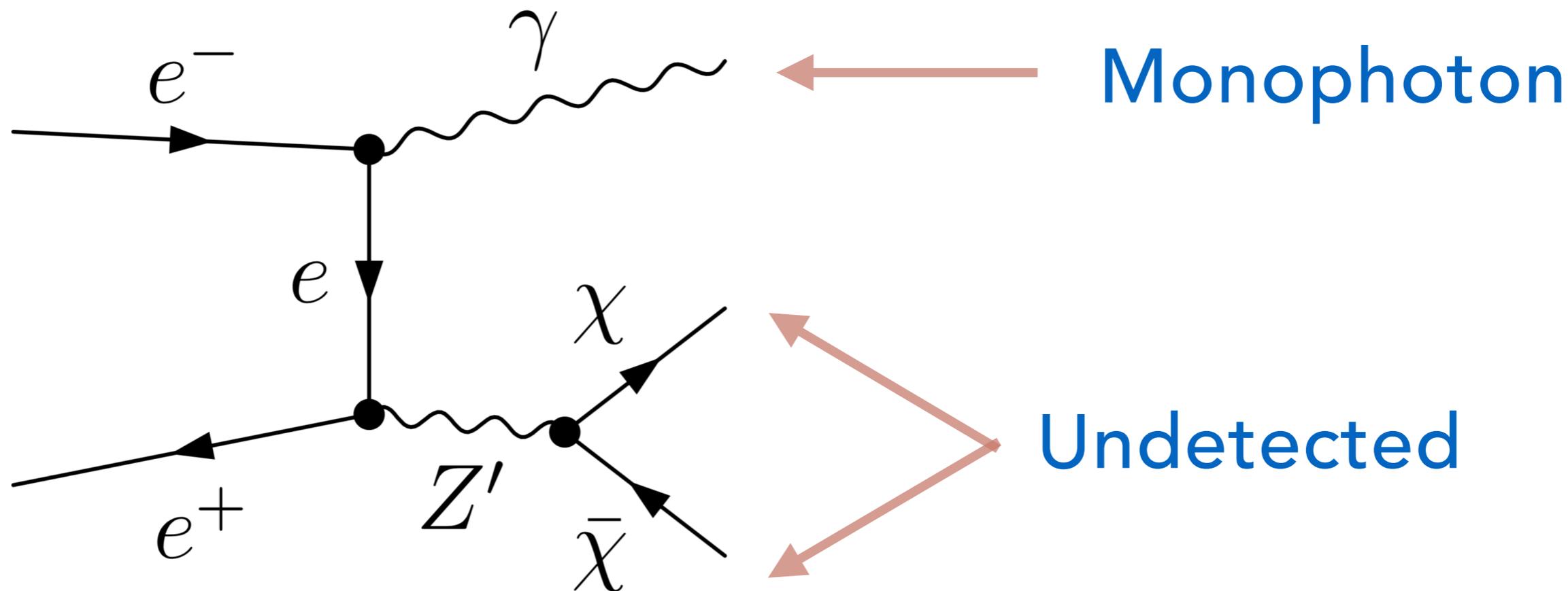


CEPC collider ring (100km)

H Mode: $e^+e^- \rightarrow ZH$
 $\sqrt{s} = 240 \text{ GeV}$
 $L = 5.6 \text{ ab}^{-1}$

Z Mode: $e^+e^- \rightarrow Z$
 $\sqrt{s} = 91.2 \text{ GeV}$
 $L = 16 \text{ ab}^{-1}$

W Mode: $e^+e^- \rightarrow W^+W^-$
 $\sqrt{s} = 158 \sim 172 \text{ GeV}$
 $L = 2.6 \text{ ab}^{-1}$





Millicharge DM models

Zuowei Liu, **Yu Zhang**, 1808.00983, PRD

Zuowei Liu, Yong-Heng Xu, **Yu Zhang**, 1903.12114, JHEP

Jinhan Liang, Zuowei Liu, Yue Ma, **Yu Zhang**, 1909.06847

mass →	≈2.3 MeV/c ²	≈1.275 GeV/c ²	≈173.07 GeV/c ²	0	≈126 GeV/c ²
charge →	2/3	2/3	2/3	0	0
spin →	1/2	1/2	1/2	1	0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS					
	≈4.8 MeV/c ²	≈95 MeV/c ²	≈4.18 GeV/c ²	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	d down	s strange	b bottom	γ photon	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	91.2 GeV/c ²	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS				GAUGE BOSONS	
	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²	80.4 GeV/c ²	
	0	0	0	±1	
	1/2	1/2	1/2	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

$$Q_e = -1$$

$$Q_u = 2/3$$

$$Q_d = -1/3$$

$$Q_W = \pm 1$$

- In general, electric charge can be of any value
- $\mathcal{L}_{int} = \varepsilon e A_\mu \bar{\chi} \gamma^\mu \chi$
- $\varepsilon \ll 1$, χ is millicharged
- Stringent constraints on millicharge of SM particles

$$Q_p - Q_e < (0.8 \pm 0.8) \times 10^{-21} e$$

Marinelli et al. 1984

$$Q_n < (-0.1 \pm 1.1) \times 10^{-21} e$$

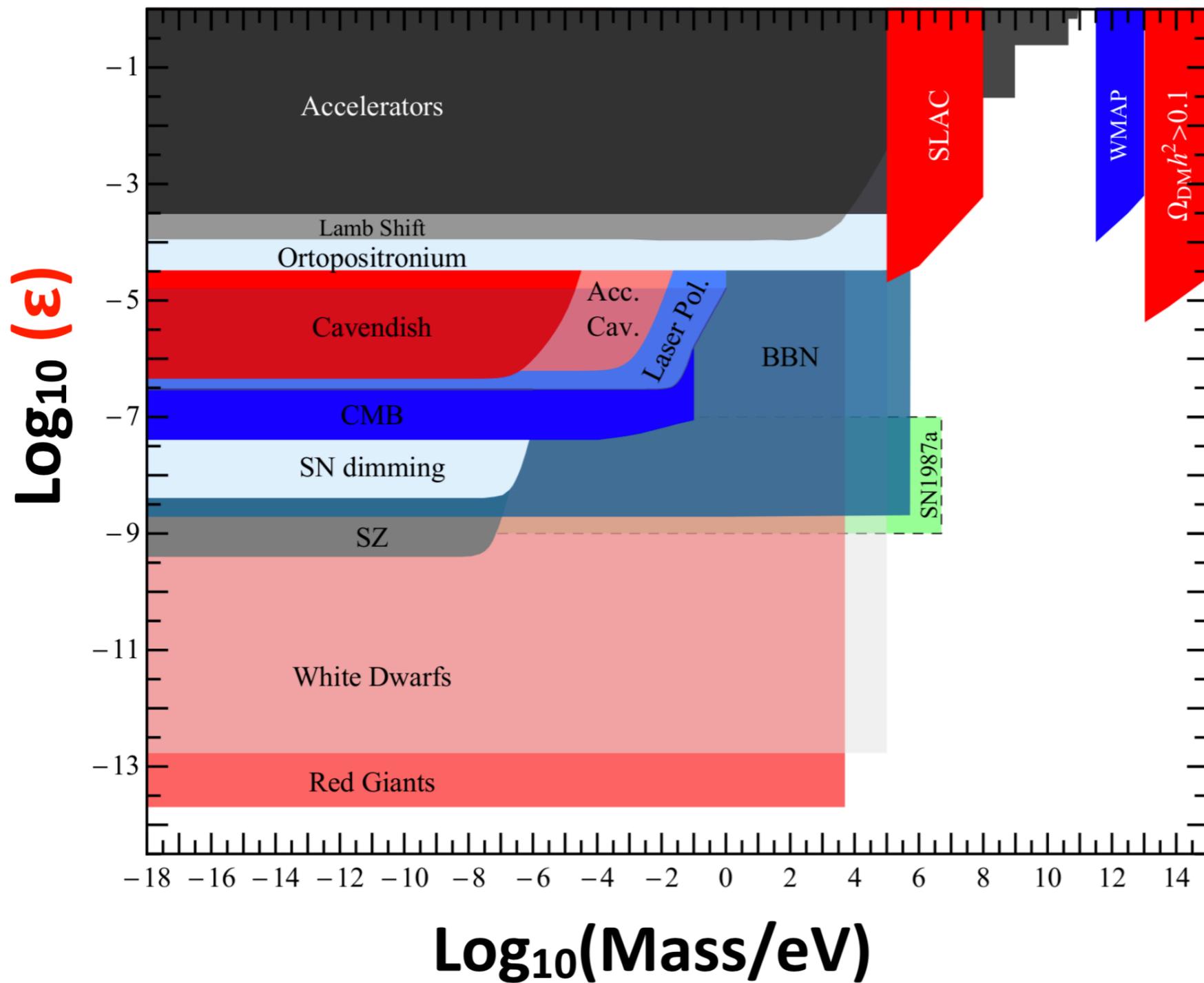
Bressi et al. 2011

$$Q_n < (-0.4 \pm 1.1) \times 10^{-21} e$$

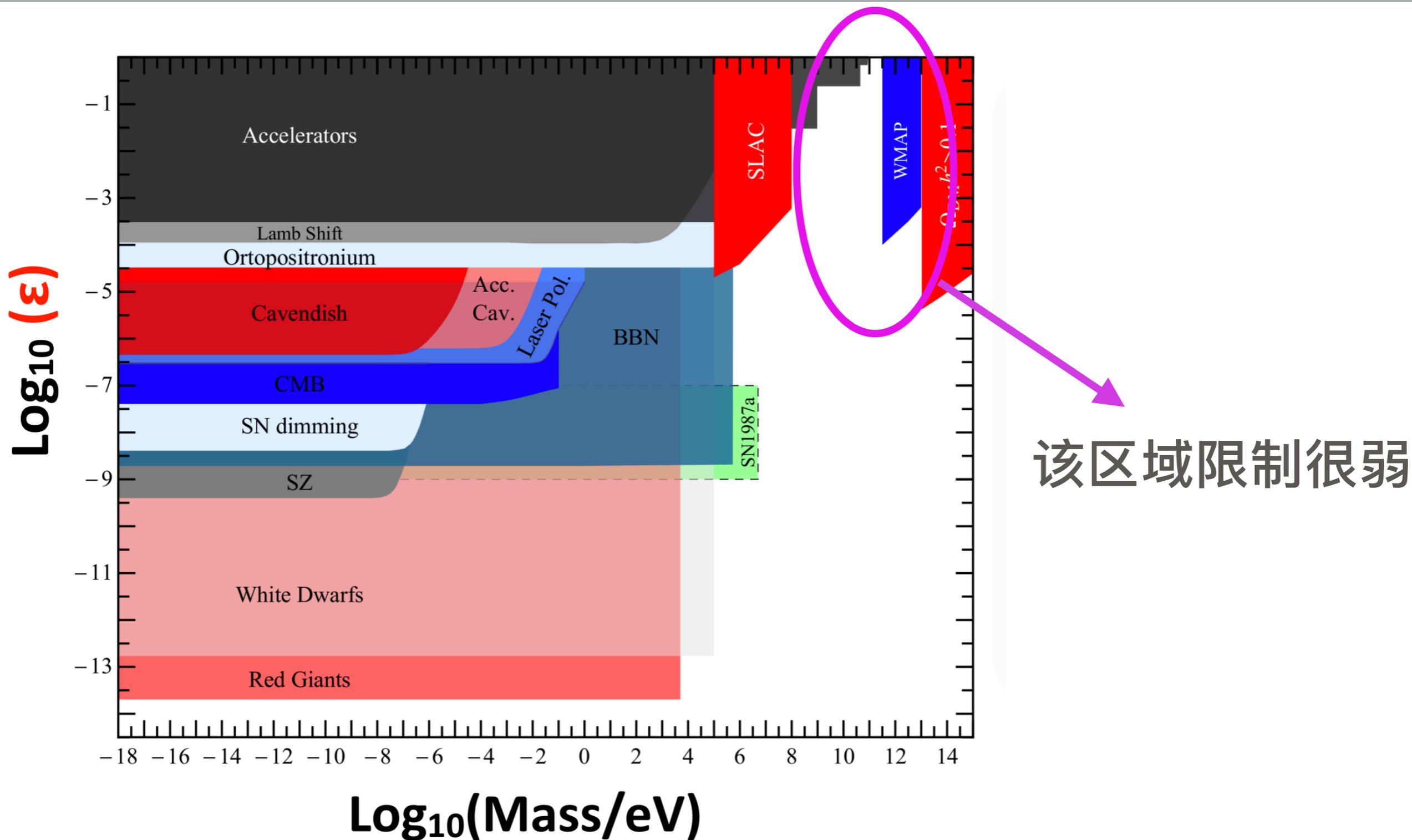
Baumann et al. 1988

$$Q_\nu < 10^{-17} e$$

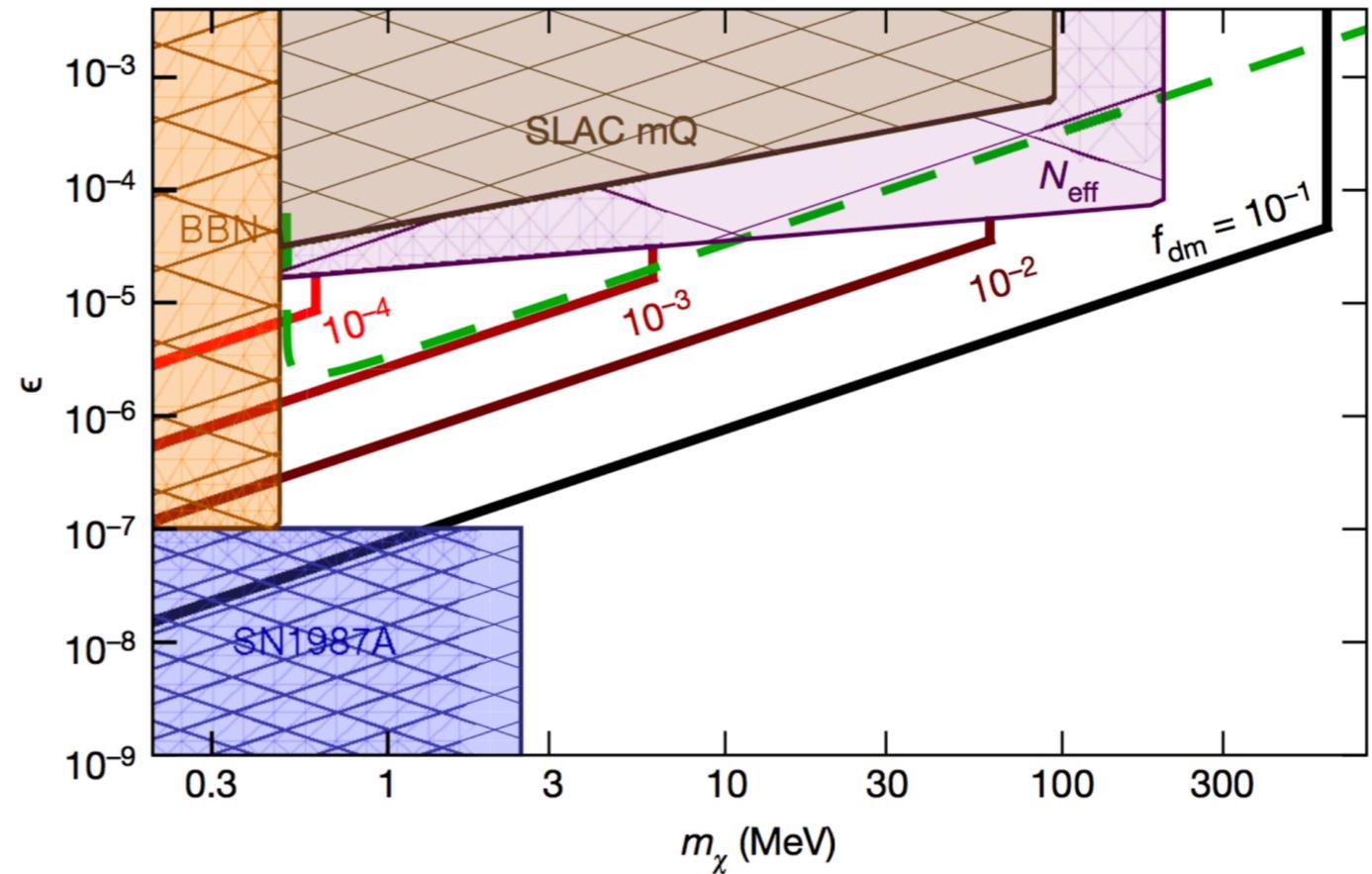
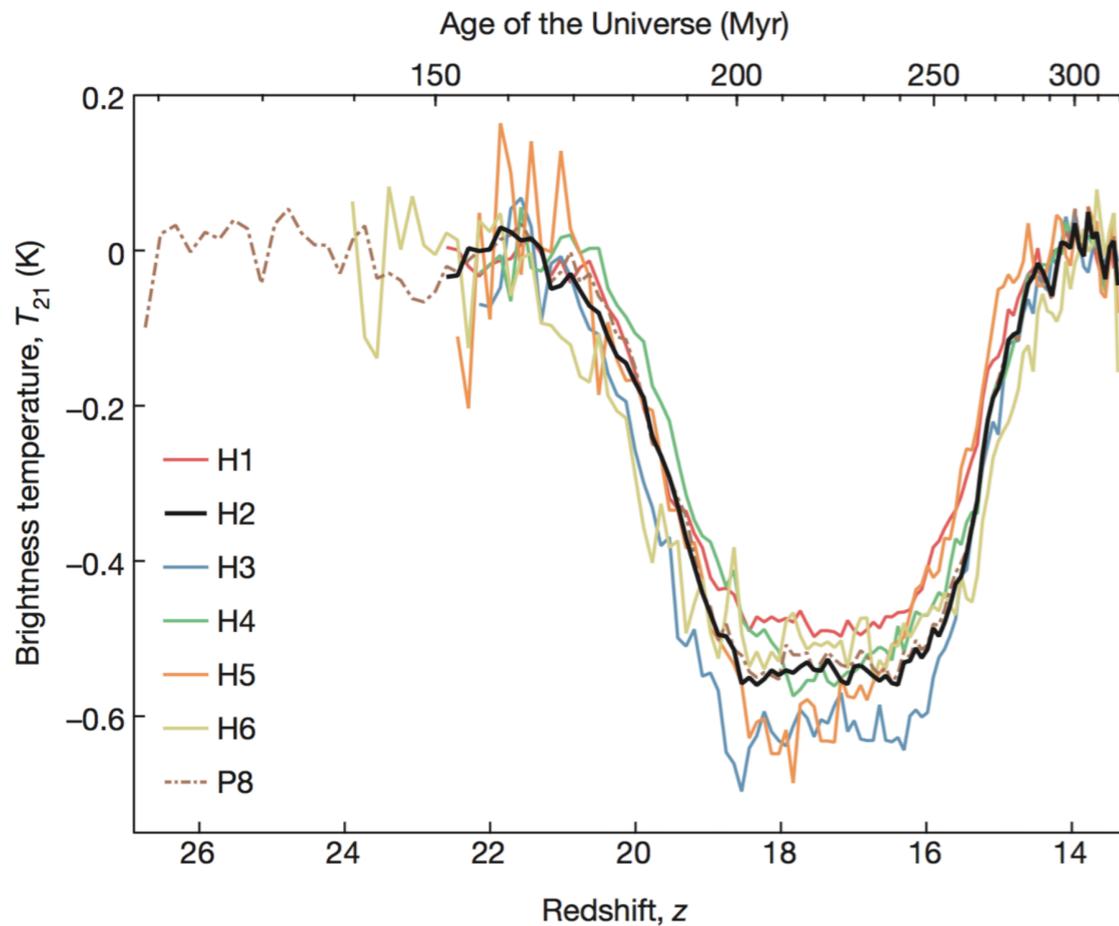
Barbiellini et al. 1987



Jaeckel, Ringwald, 1002.0329



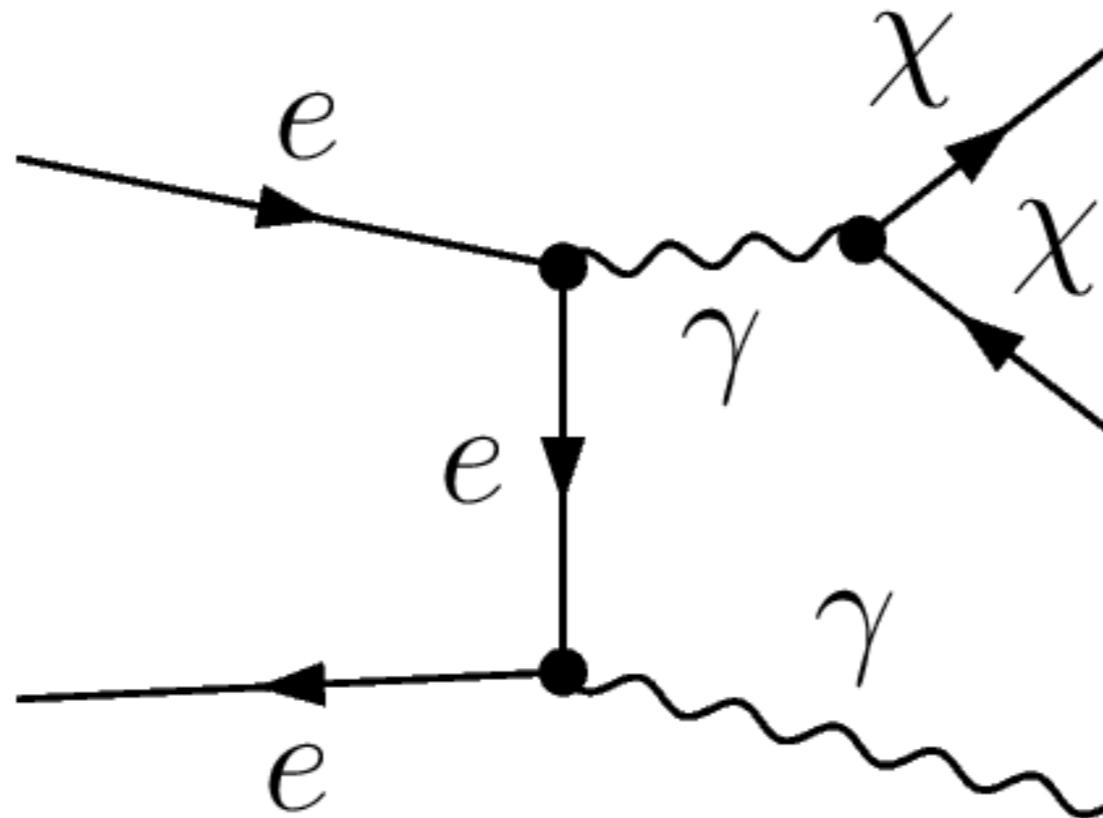
Jaeckel, Ringwald, 1002.0329



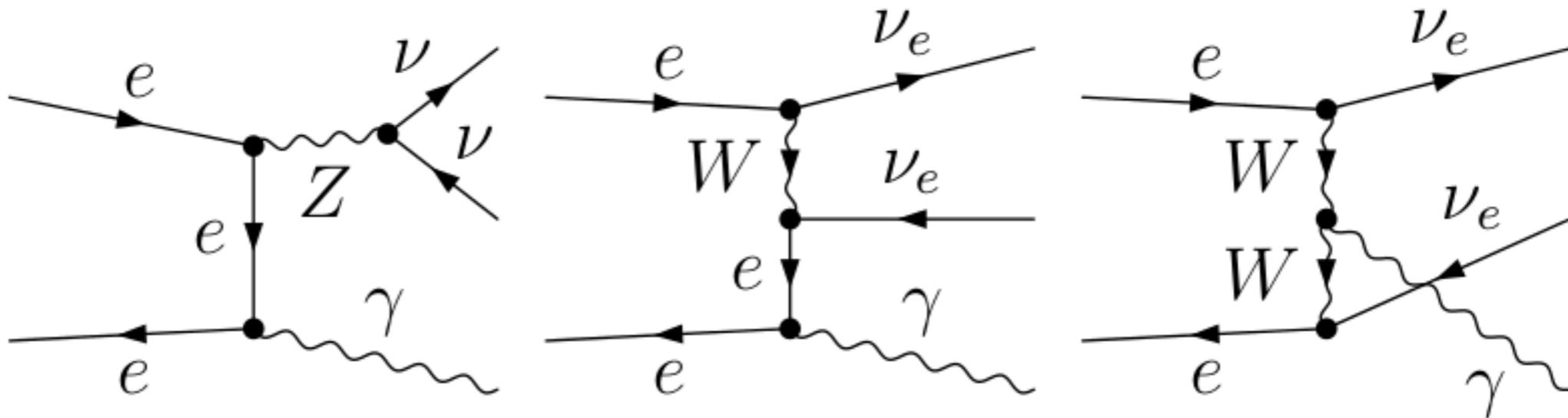
Bowman et al., Nature 25792 (2018); Barkana, Nature 25791 (2018); Munoz, Loeb, Nature 557 (2018) no.7707, 684; + others

$$e^+e^- \rightarrow \chi\bar{\chi}\gamma$$

$$\mathcal{L}_{int} = \varepsilon e A_\mu \bar{\chi} \gamma^\mu \chi$$



$$e^+e^- \rightarrow \nu\bar{\nu}\gamma$$



BESIII & STCF: BESIII, 1707.05178

- EMC桶部(barrel):

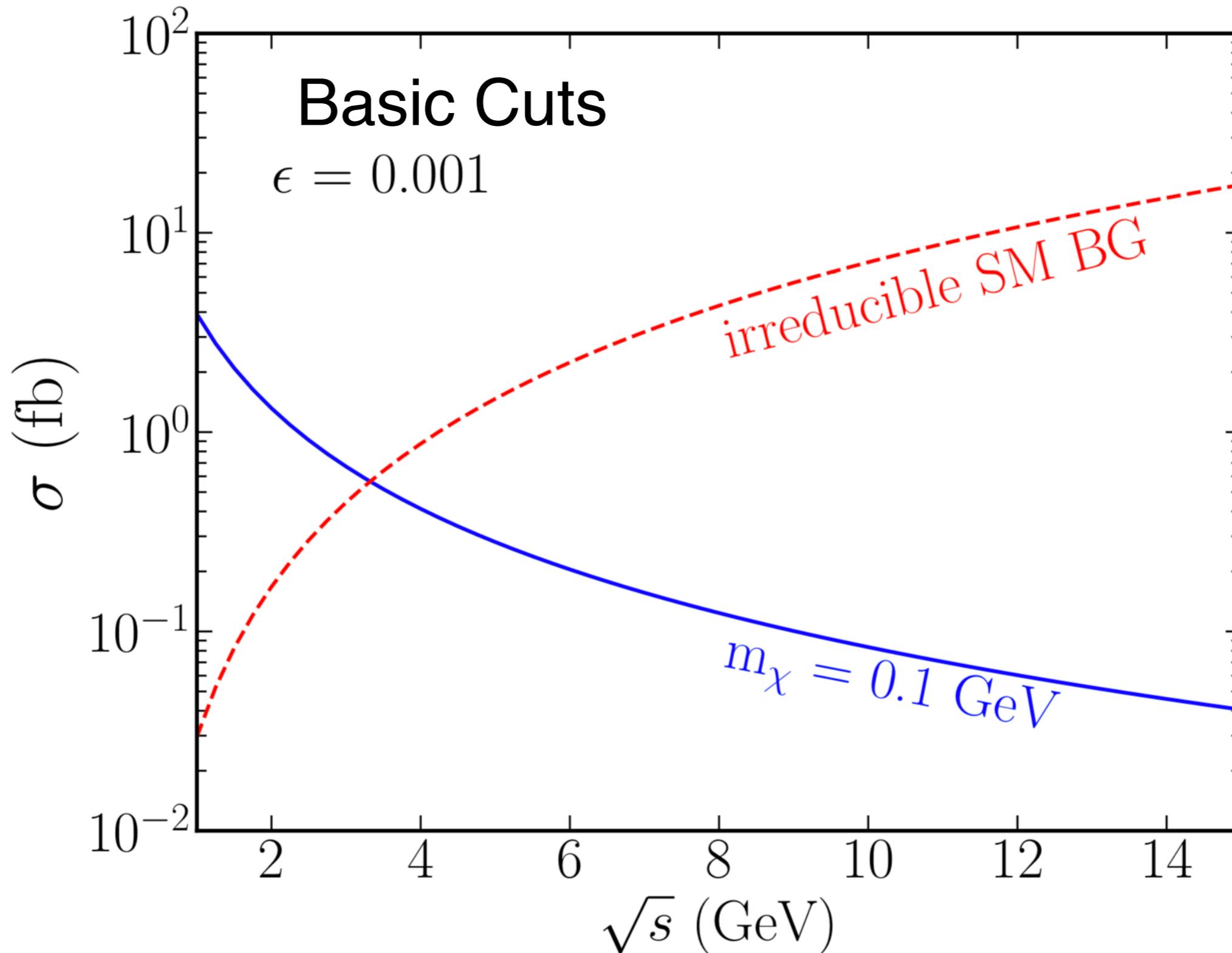
$$E_\gamma > 25 \text{ MeV} \ \& \ |\cos \theta_\gamma| < 0.8$$

- EMC端盖(end-caps):

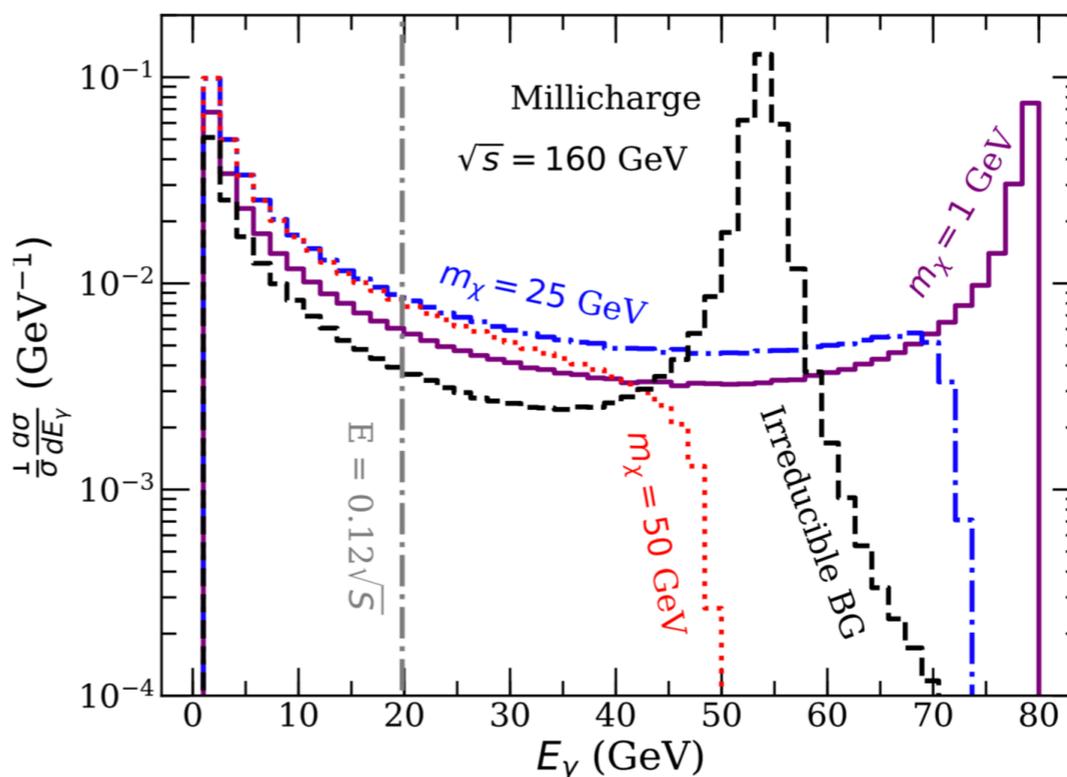
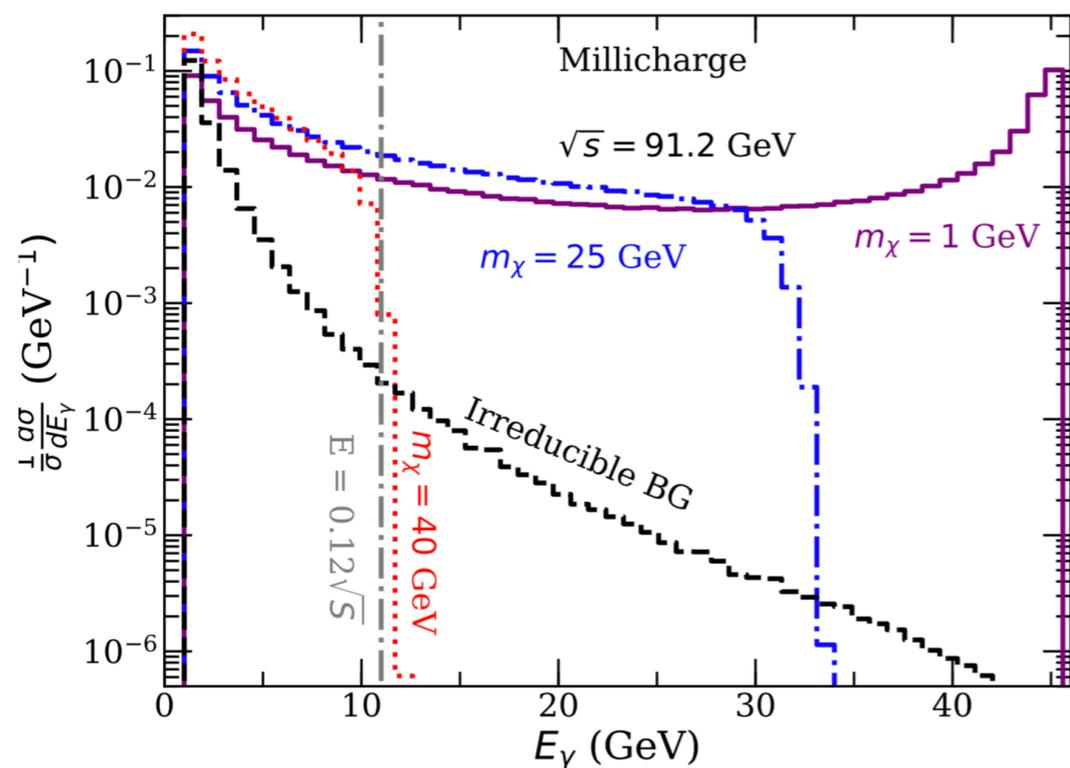
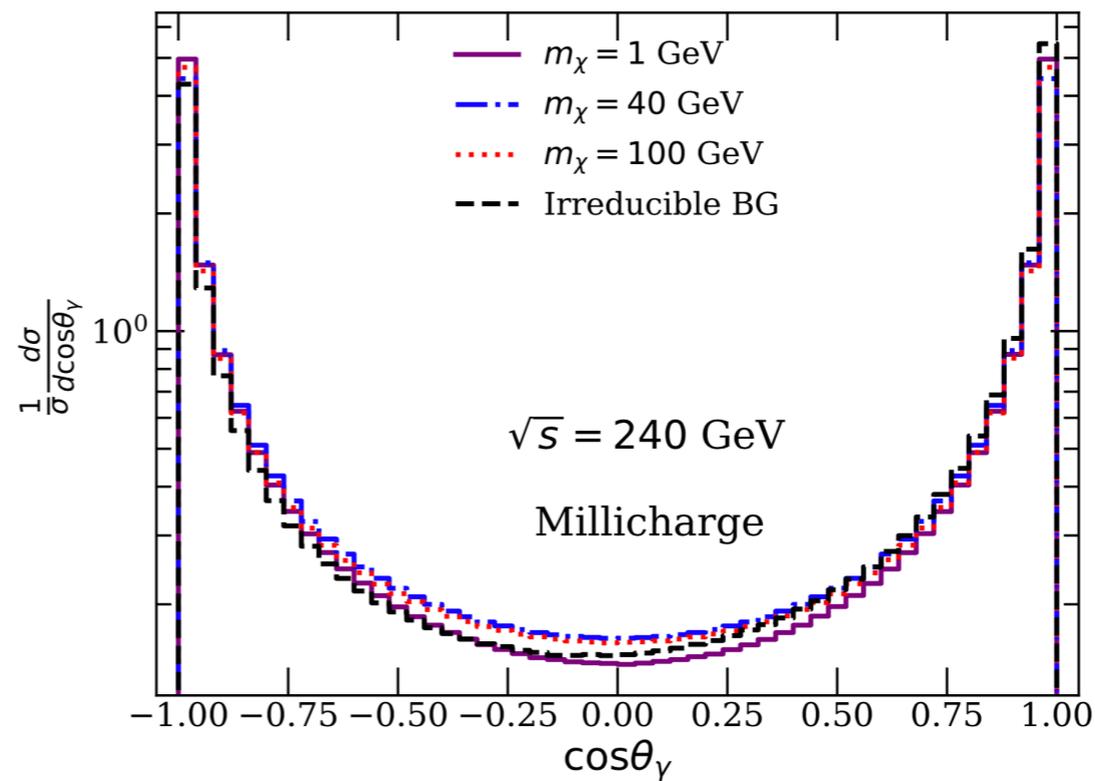
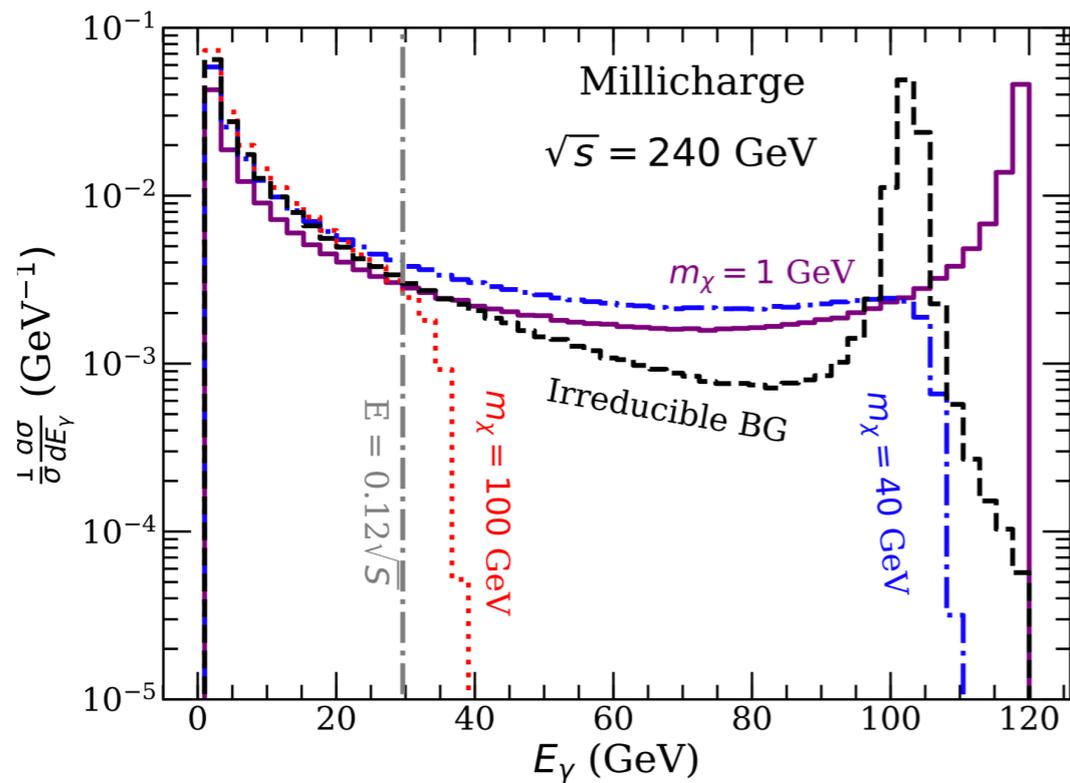
$$E_\gamma > 50 \text{ MeV} \ \& \ 0.86 < |\cos \theta_\gamma| < 0.92$$

CEPC: CEPC, 1811.10545

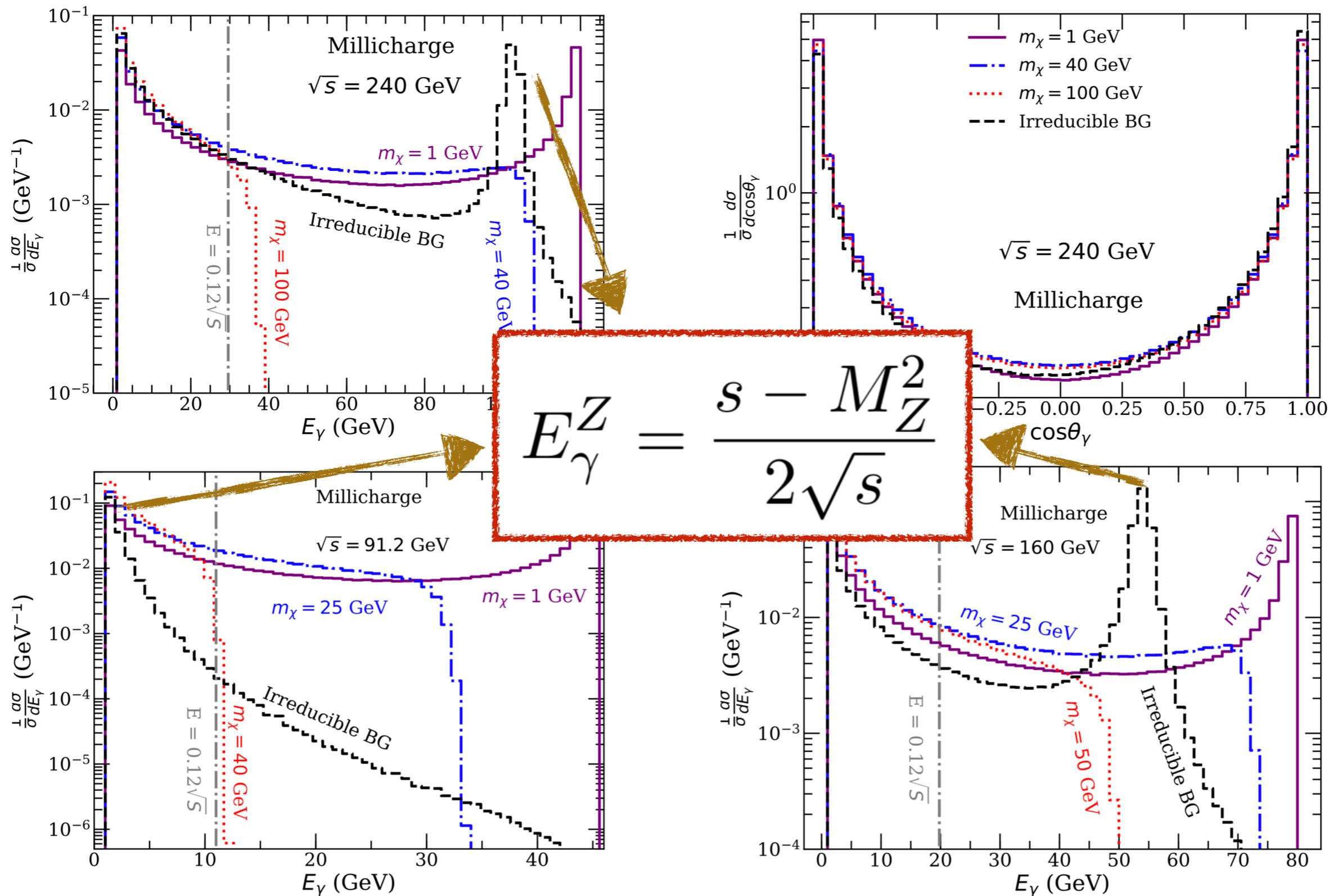
- $E_\gamma > 0.1 \text{ GeV} \ \& \ |\cos \theta_\gamma| < 0.99$



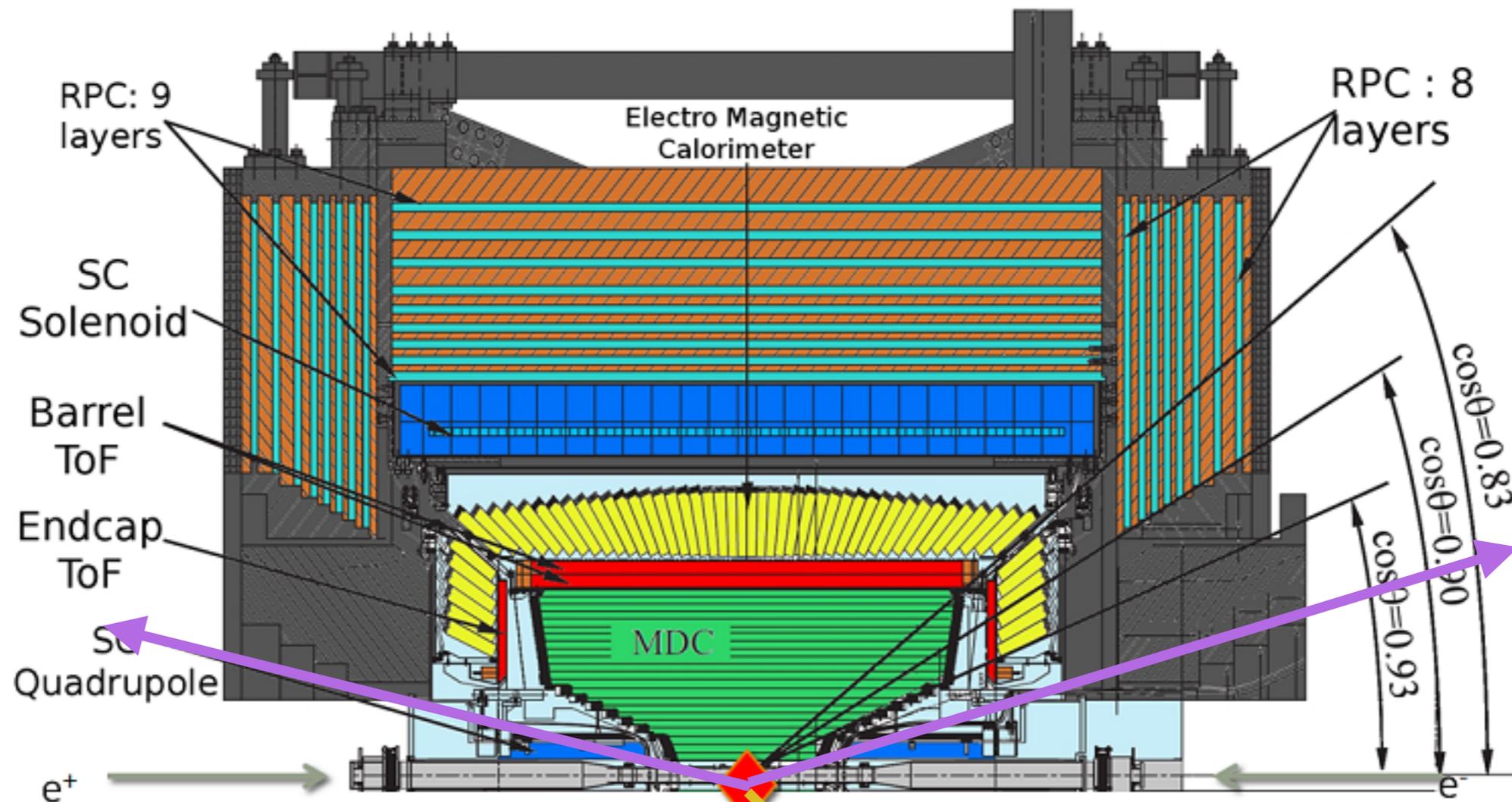
Smaller colliding energy has better sensitivity !



After Basic Cuts



After Basic Cuts



主漂移室 (MDC) : $|\cos\theta| < 0.93$

飞行时间计数器 (TOF) : $|\cos\theta| < 0.83$ $0.85 < |\cos\theta| < 0.95$

电磁量能器 (EMC) : $|\cos\theta| < 0.83$ $0.85 < |\cos\theta| < 0.93$

1. 共振态衰变 (比如 $J/\psi \rightarrow \gamma X$)

① $J/\psi \rightarrow \gamma \nu \nu$ 可忽略的不可约背景,

$$\text{Br} = 0.7 \times 10^{-10} \quad \text{Gao 1408.4552}$$

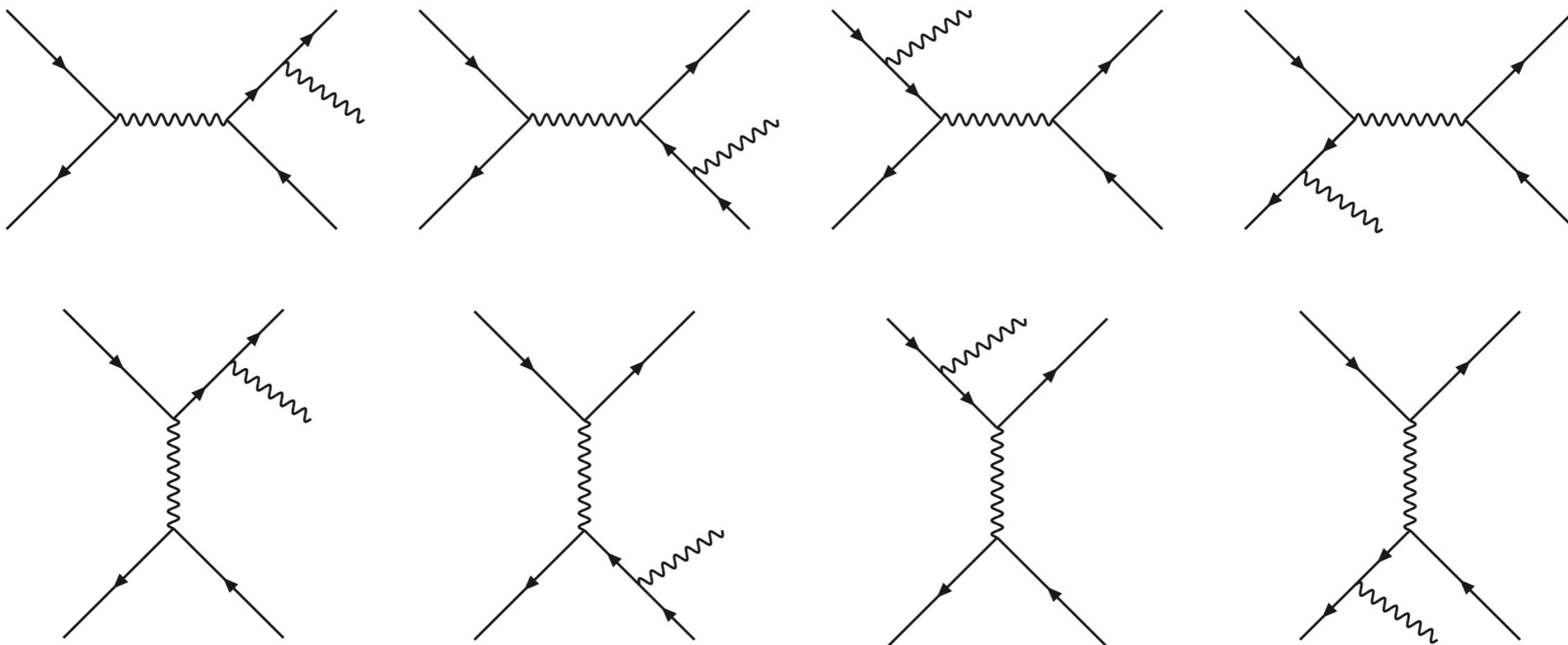
② $J/\psi \rightarrow \gamma X$ 末态X探测不到

2. 过程 $e^+ e^- \rightarrow e^+ e^- \gamma$ 末态电子探测不到

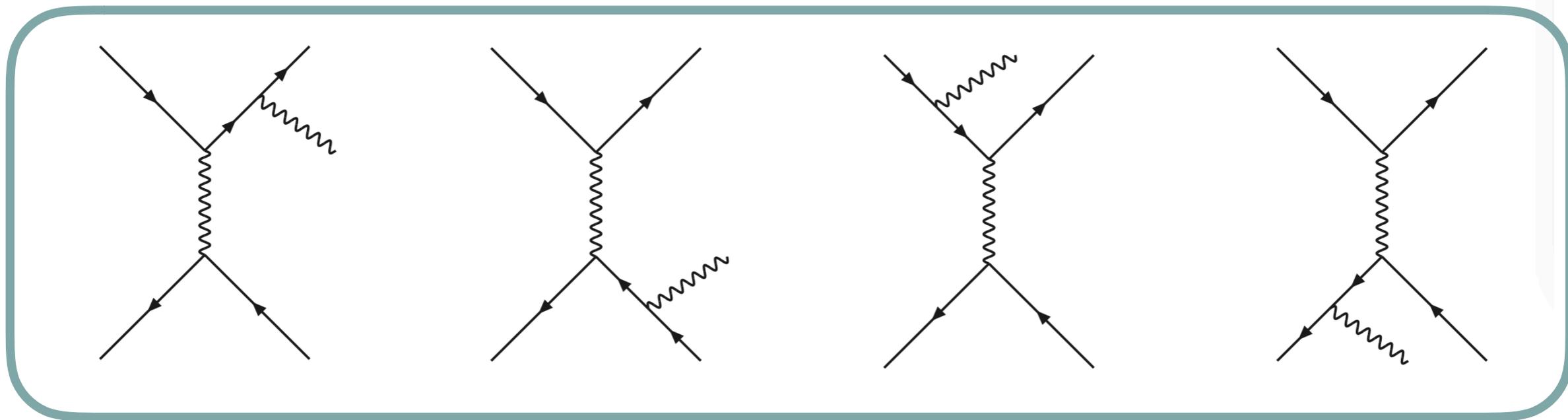
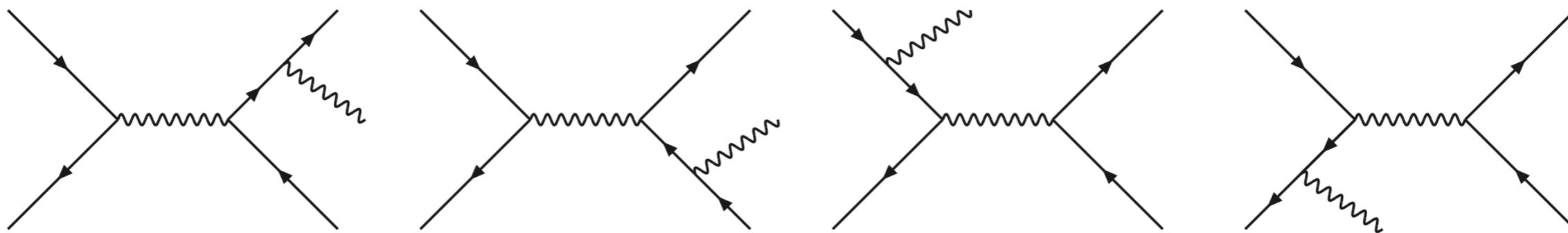
3. 过程 $e^+ e^- \rightarrow f f \gamma$ 末态ff探测不到

4. 过程 $e^+ e^- \rightarrow \gamma \gamma \gamma$ 末态只能探测到一个光子

AcMs, Mastrolia, Ossola, 0909.1750



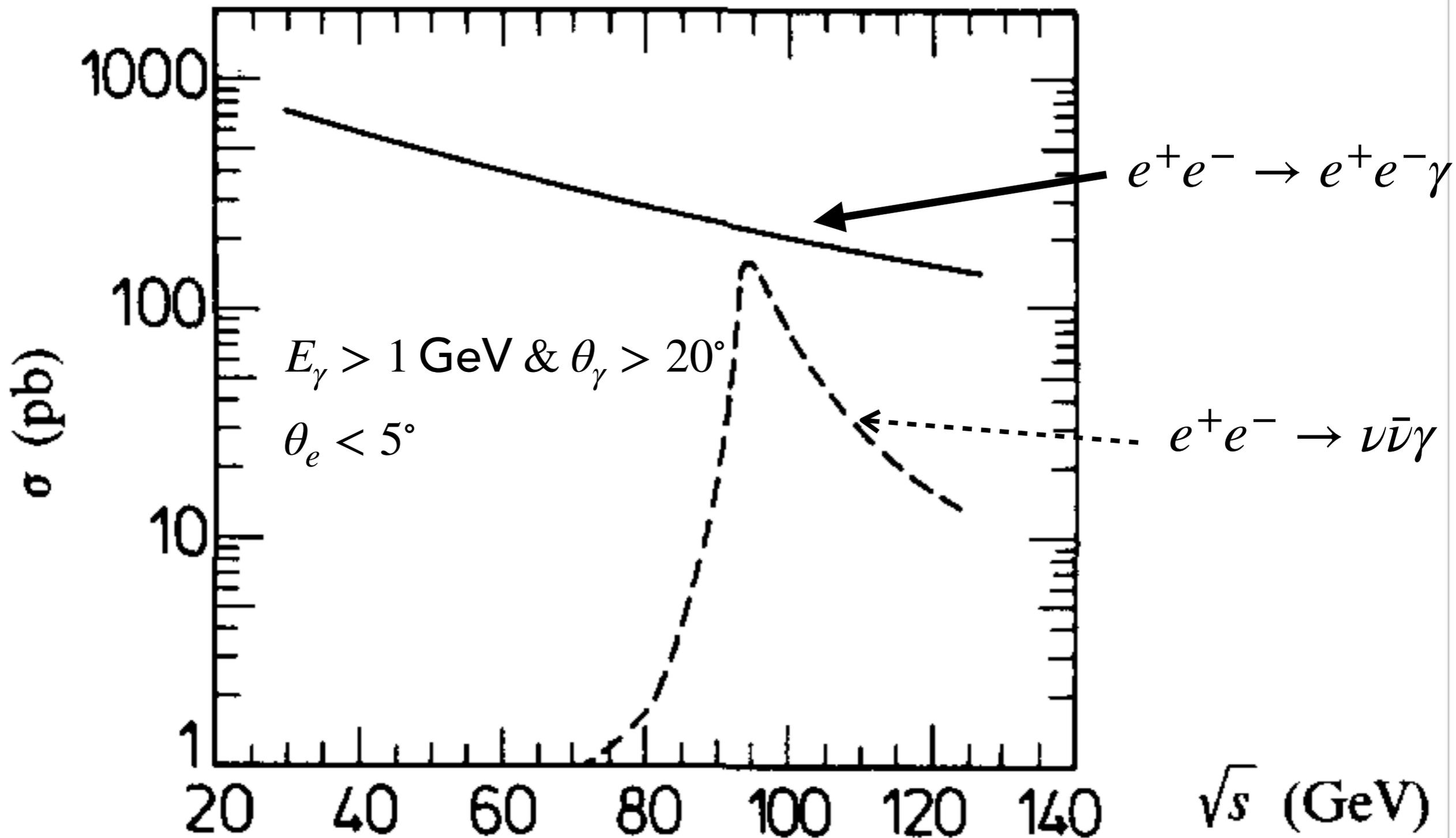
AcMs, Mastrolia, Ossola, 0909.1750

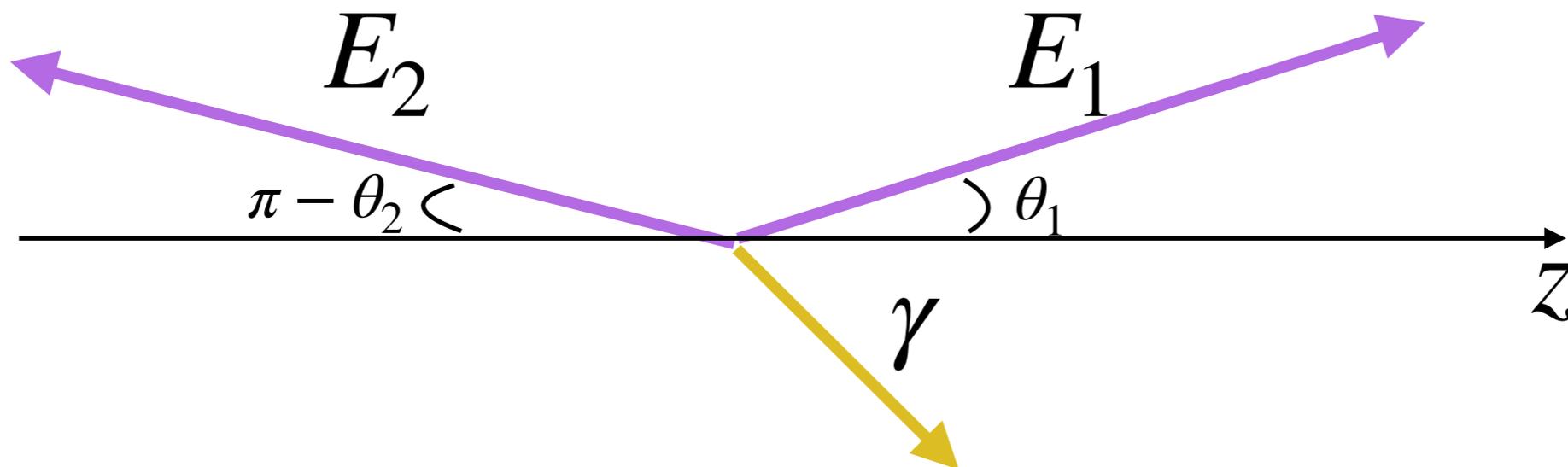


collinear singularity in the t-channel

$$|\overline{\mathcal{M}}|^2 \propto \frac{1}{t_{13}t_{24}} \sim \frac{1}{\theta_{13}^2 t_{24}} \text{ for } \theta_{13} \ll 1 \text{ \& } m_e \rightarrow 0$$

Mana, MarMnez, NPB 1987





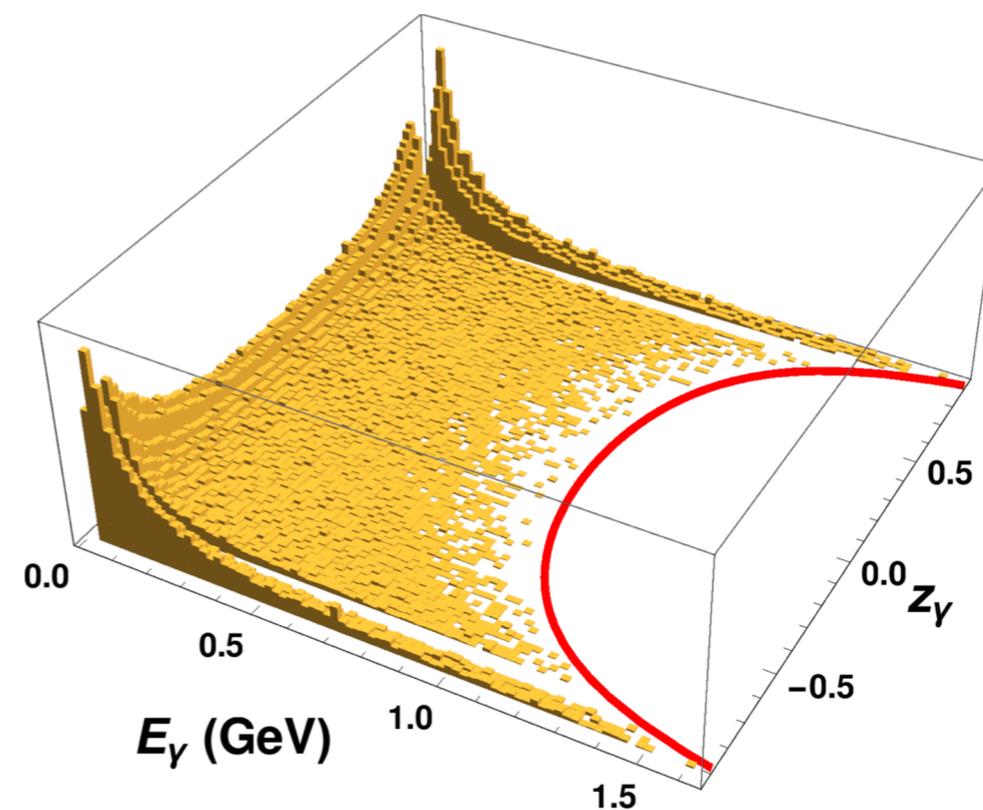
$$\begin{cases} E_\gamma^m \sin \theta_\gamma - E_1 \sin \theta_1 - E_2 \sin \theta_2 = 0 \\ E_\gamma^m \cos \theta_\gamma + E_1 \cos \theta_1 + E_2 \cos \theta_2 = 0 \\ E_\gamma^m + E_1 + E_2 = \sqrt{s}, \end{cases}$$

$$E_\gamma^m(\theta_\gamma) = \frac{\sqrt{s}(A \cos \theta_1 - \sin \theta_1)}{A(\cos \theta_1 - \cos \theta_\gamma) - (\sin \theta_\gamma + \sin \theta_1)}$$

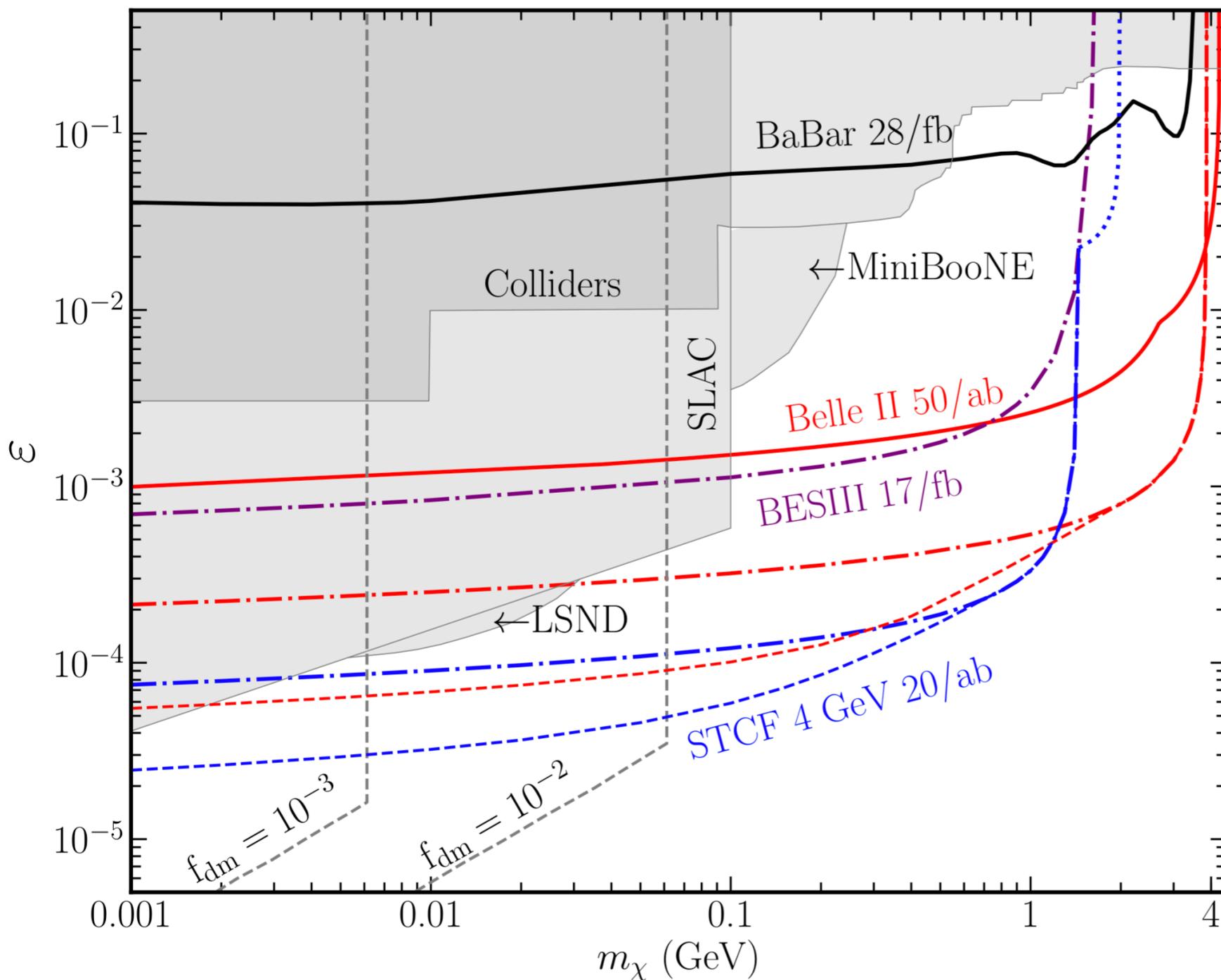
$$A = (\sin \theta_1 - \sin \theta_2) / (\cos \theta_1 - \cos \theta_2)$$

$$\sin \theta_1 = \sin \theta_2 = \sin \theta_b$$

$$E_\gamma^m(\theta_\gamma) = \sqrt{s} \left(1 + \frac{\sin \theta_\gamma}{\sin \theta_b} \right)^{-1}$$



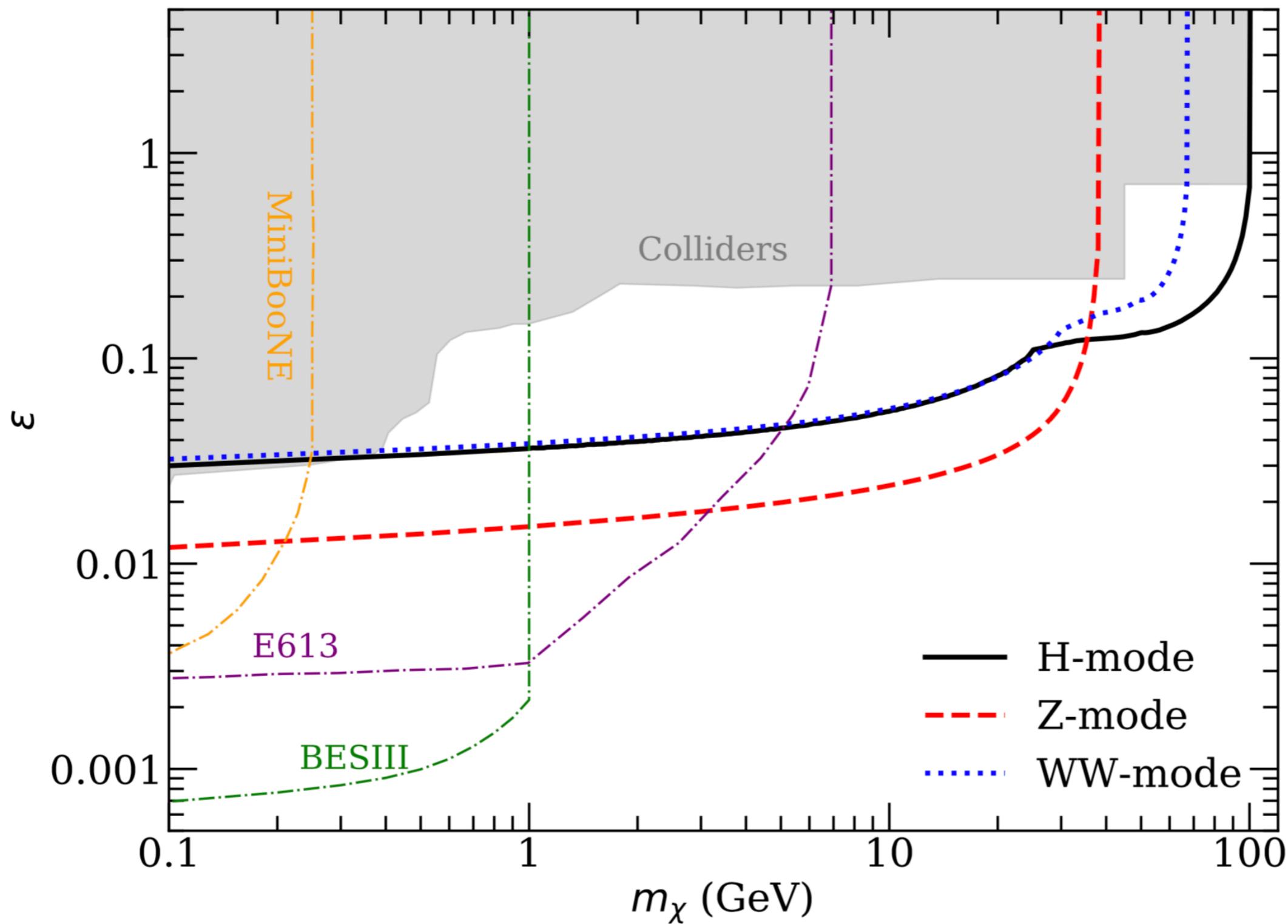
$$e^+e^- \rightarrow e^+e^-\gamma, |\cos \theta_{e^\pm}| > 0.95$$

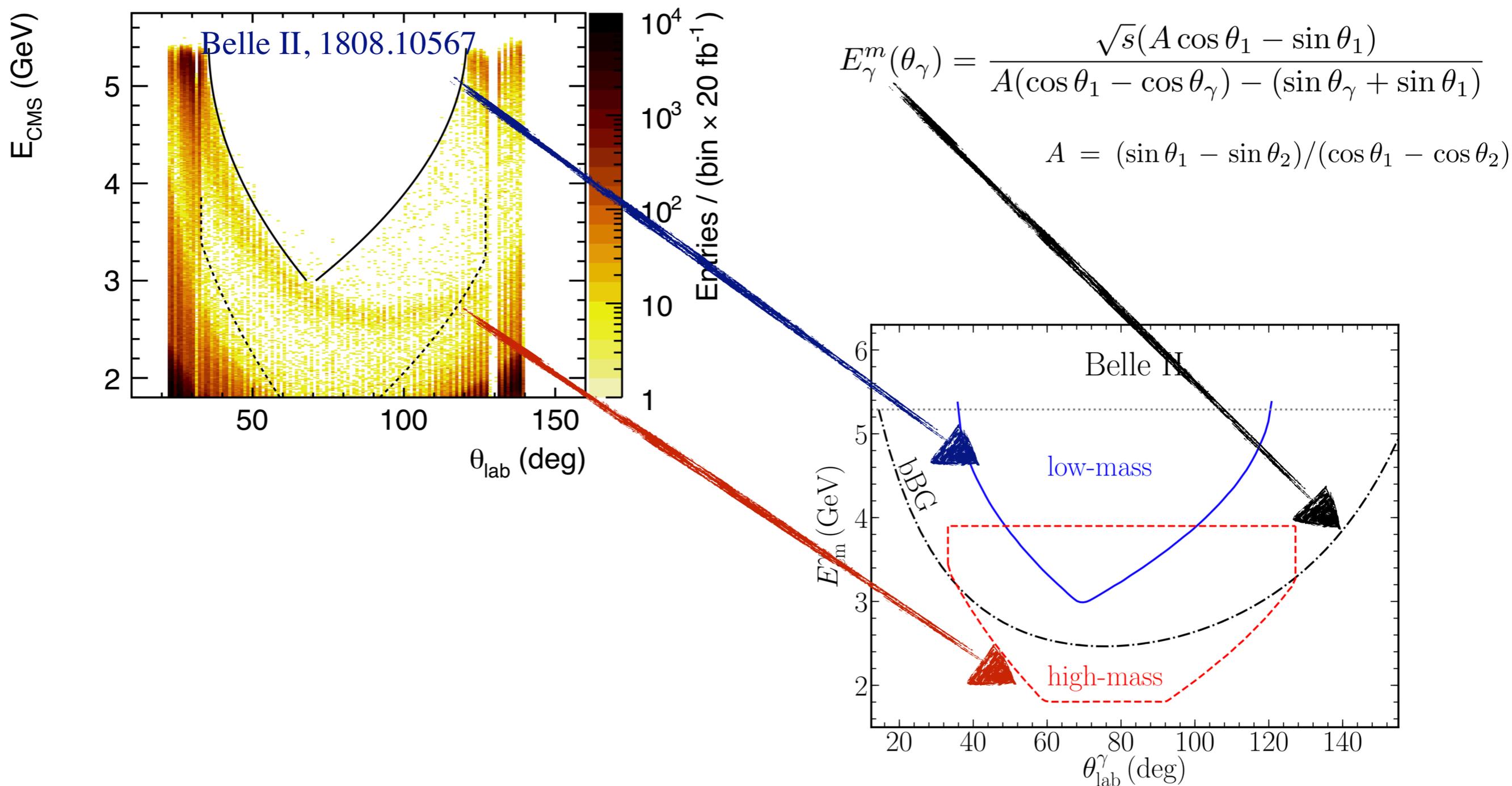


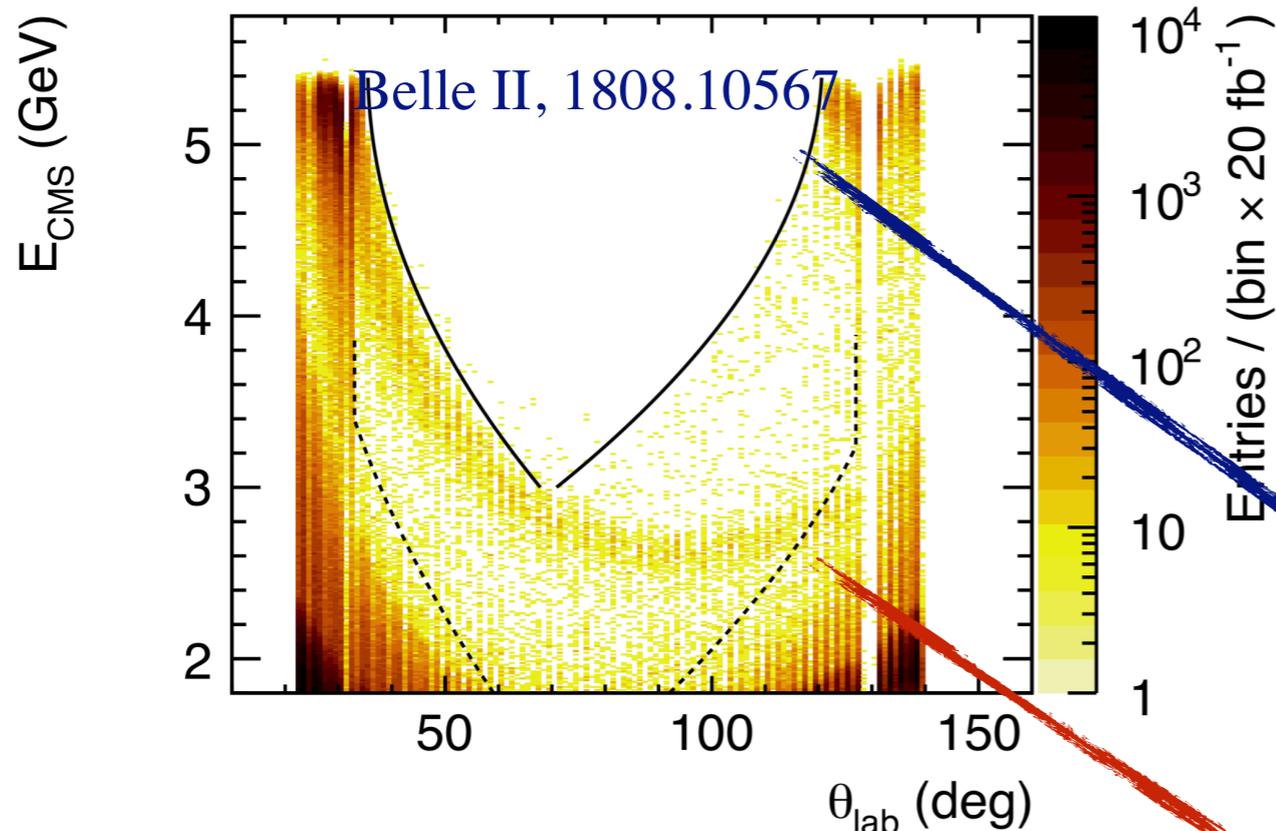
$$\chi_i^2(\epsilon) \equiv \frac{S_i^2}{S_i + B_i}$$

$$\chi_{\text{tot}}^2(\epsilon) = \sum_i \chi_i^2(\epsilon)$$

$$\chi_{\text{tot}}^2(\epsilon_{95}) = \chi^2(0) + 2.71$$

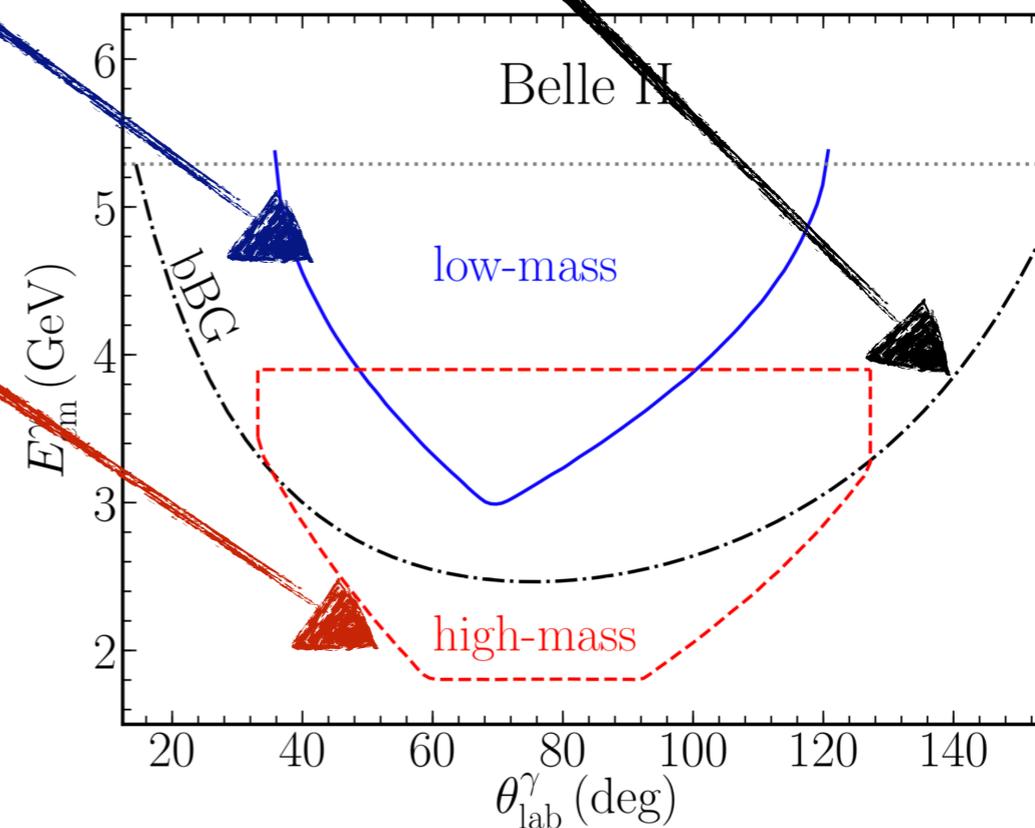
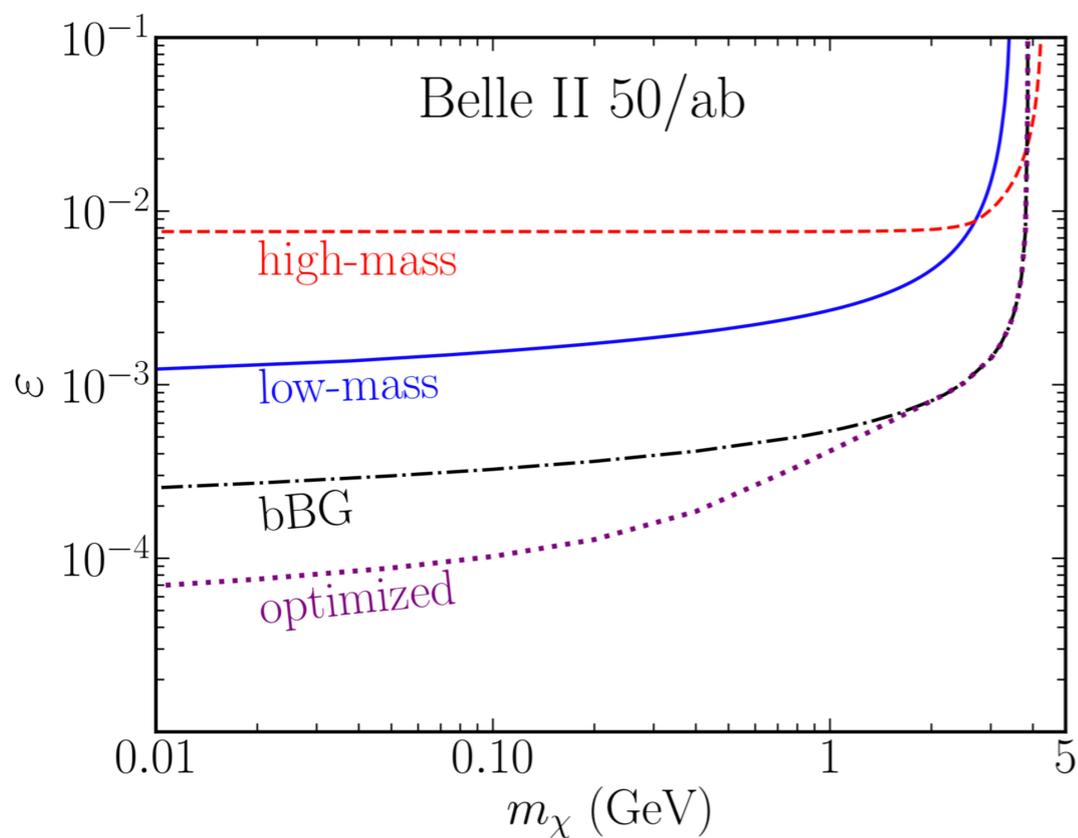


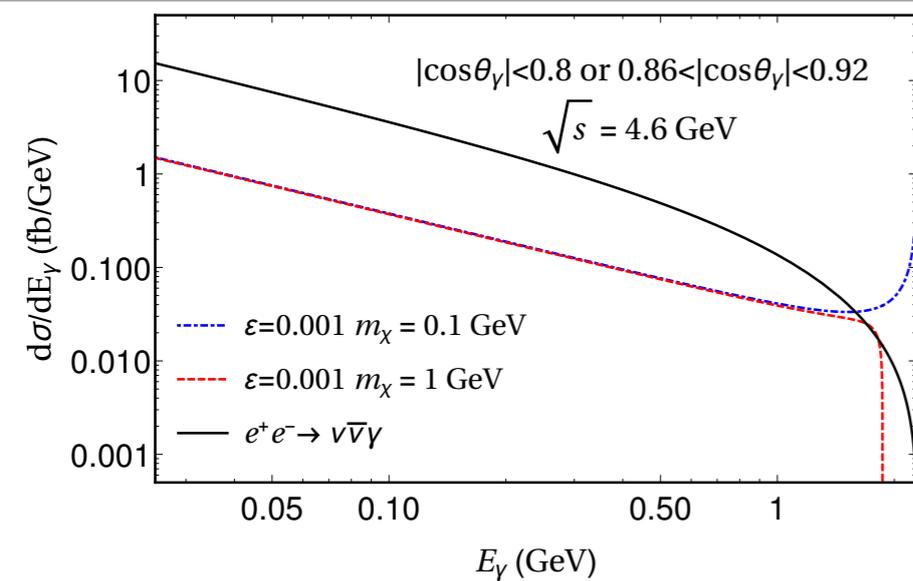




$$E_{\gamma}^m(\theta_{\gamma}) = \frac{\sqrt{s}(A \cos \theta_1 - \sin \theta_1)}{A(\cos \theta_1 - \cos \theta_{\gamma}) - (\sin \theta_{\gamma} + \sin \theta_1)}$$

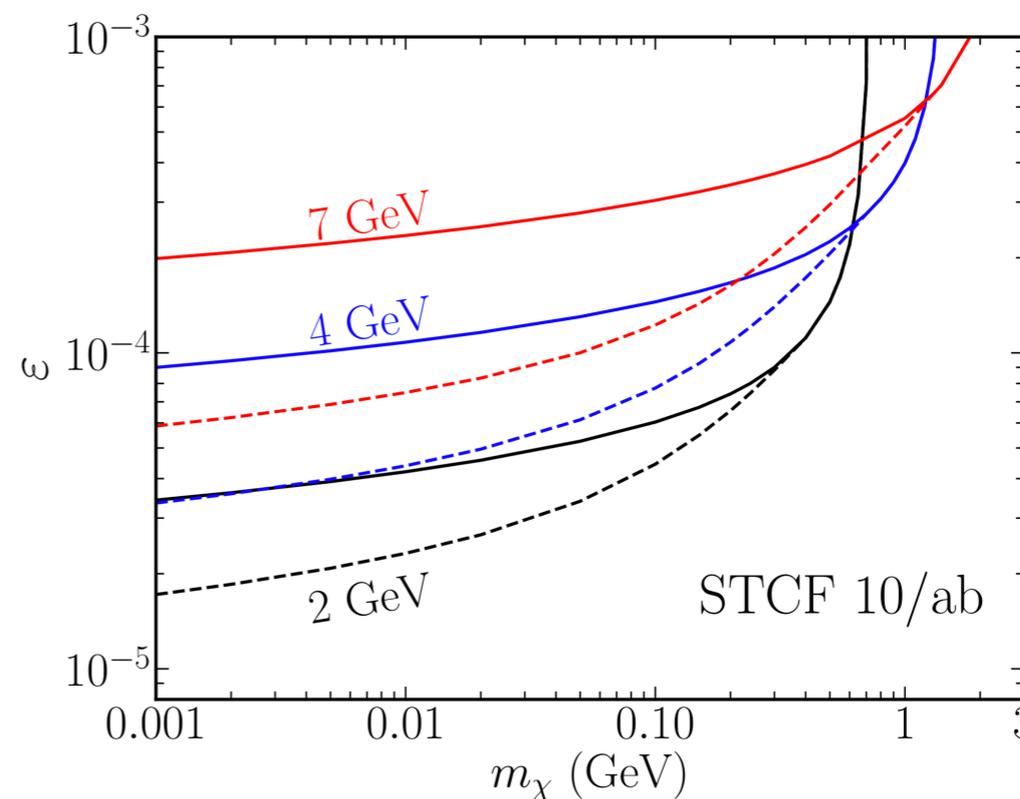
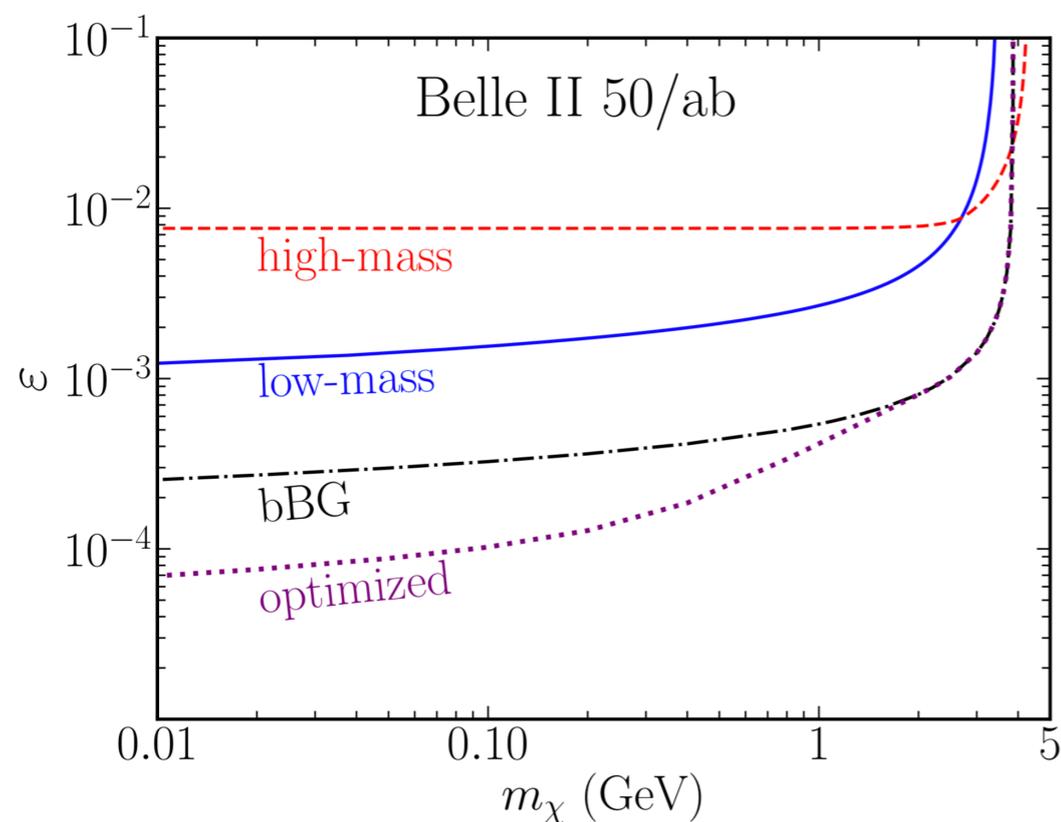
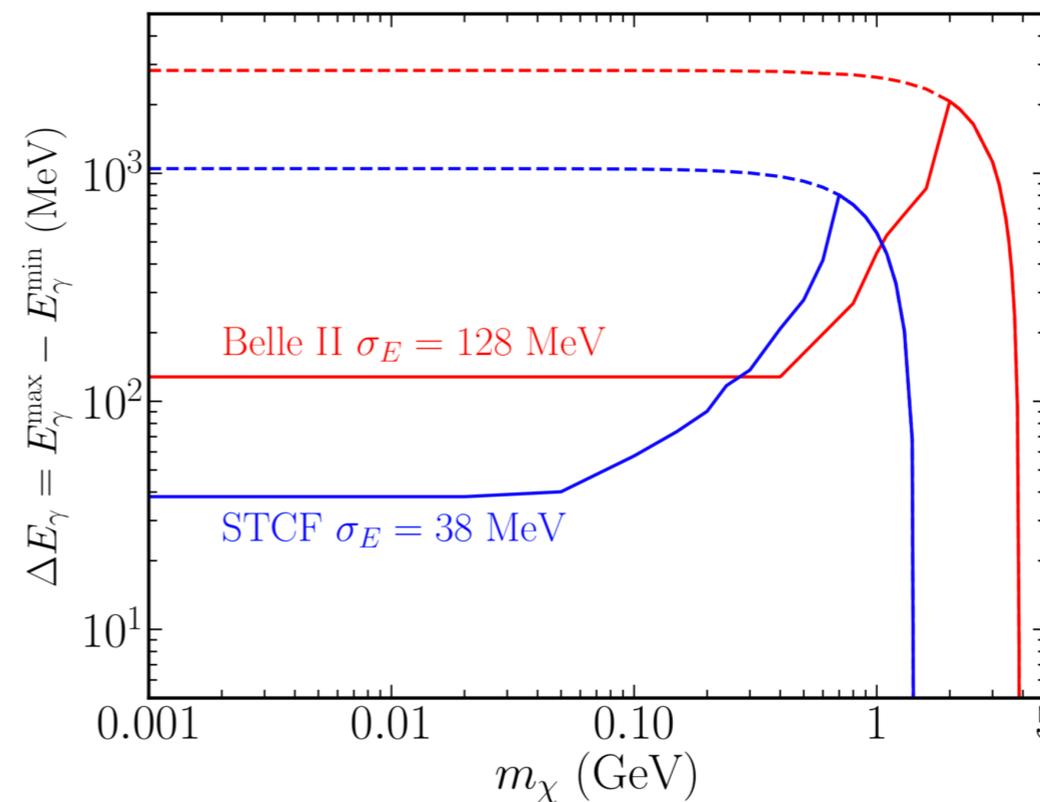
$$A = (\sin \theta_1 - \sin \theta_2) / (\cos \theta_1 - \cos \theta_2)$$





$$E_{\gamma}^{\min} < E_{\gamma} < E_{\gamma}^{\max} \quad E_{\gamma}^{\max} = (s - 4m_{\chi}^2)/(2\sqrt{s})$$

$$\Delta E_{\gamma} \equiv E_{\gamma}^{\max} - E_{\gamma}^{\min}$$

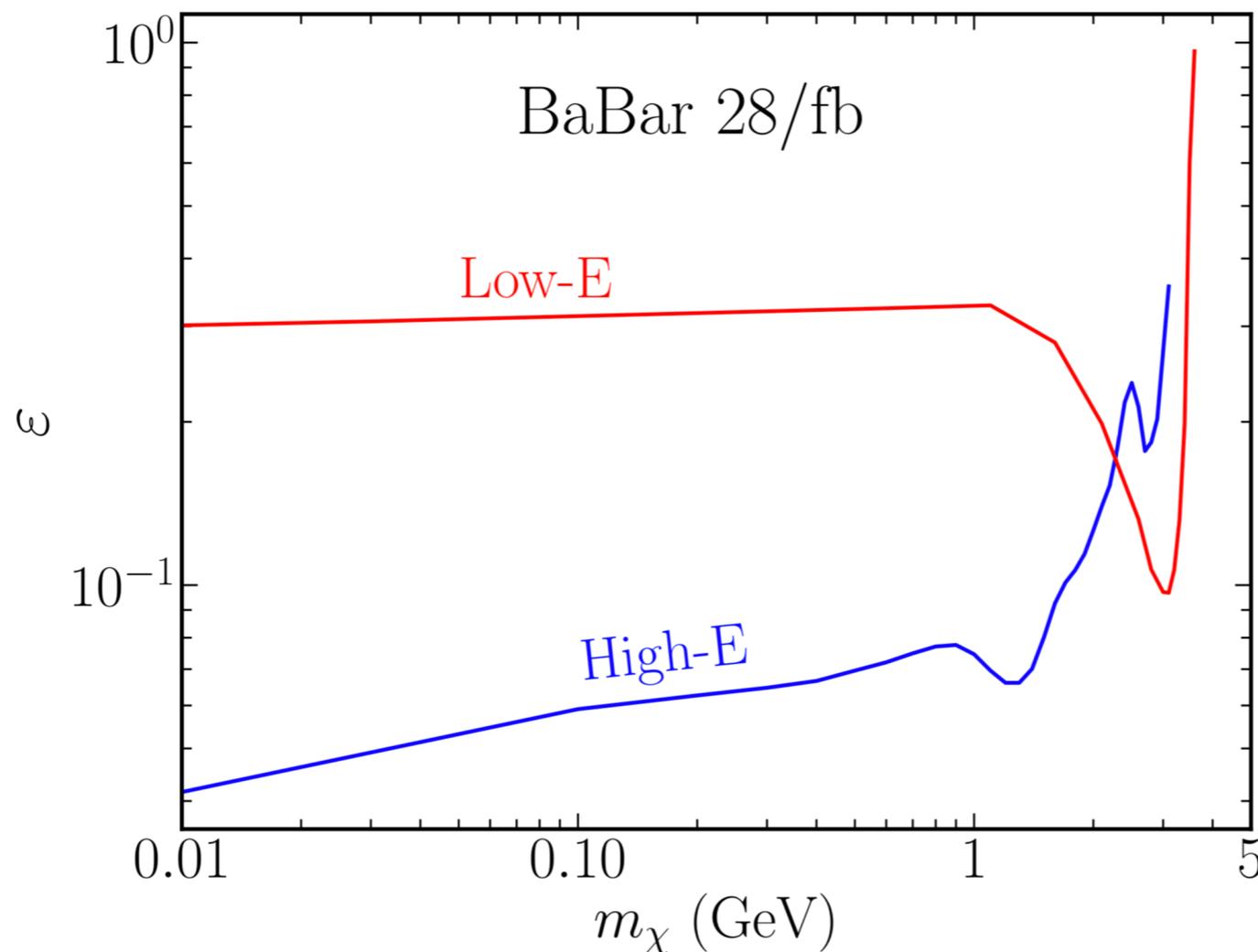


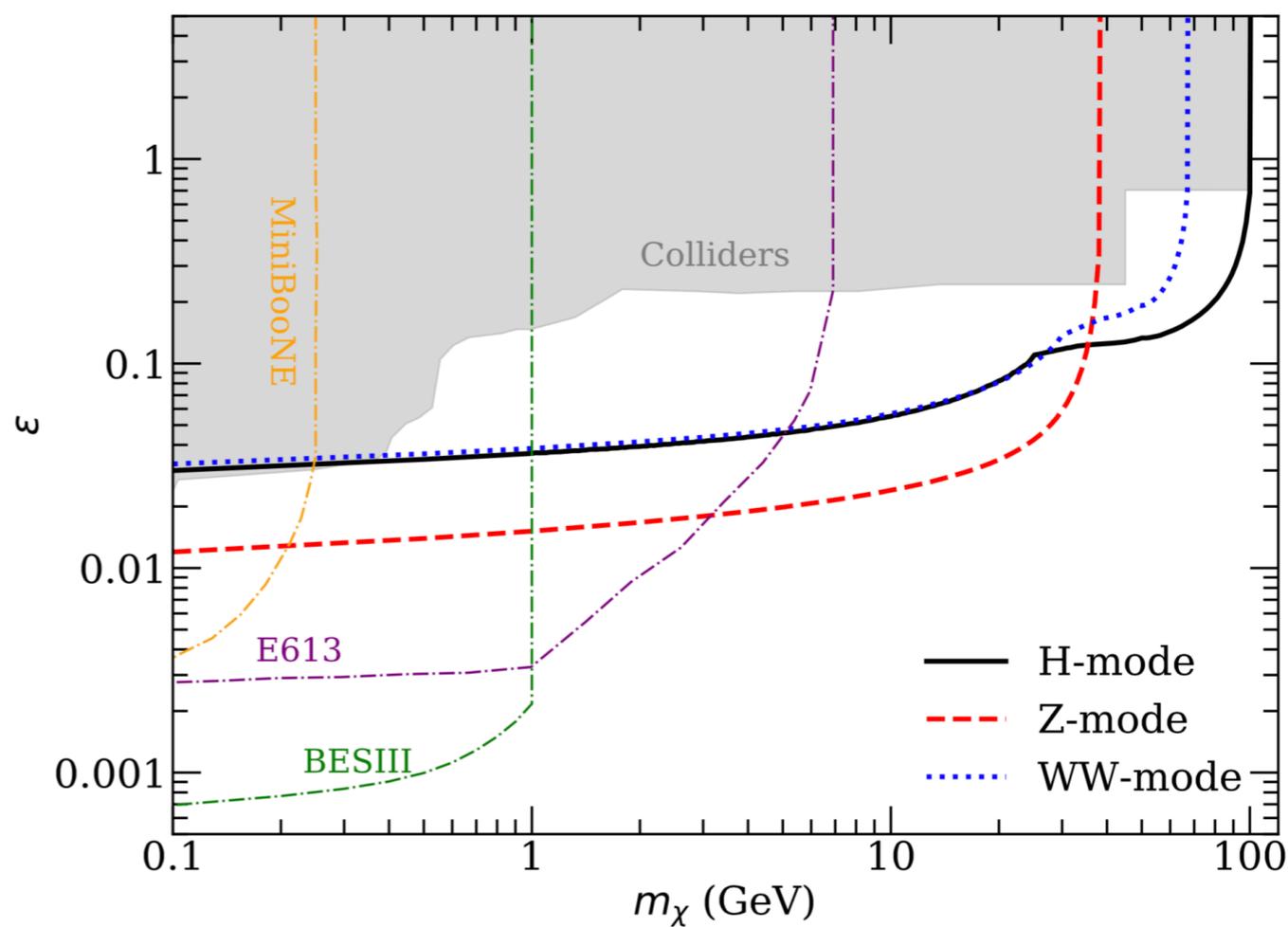
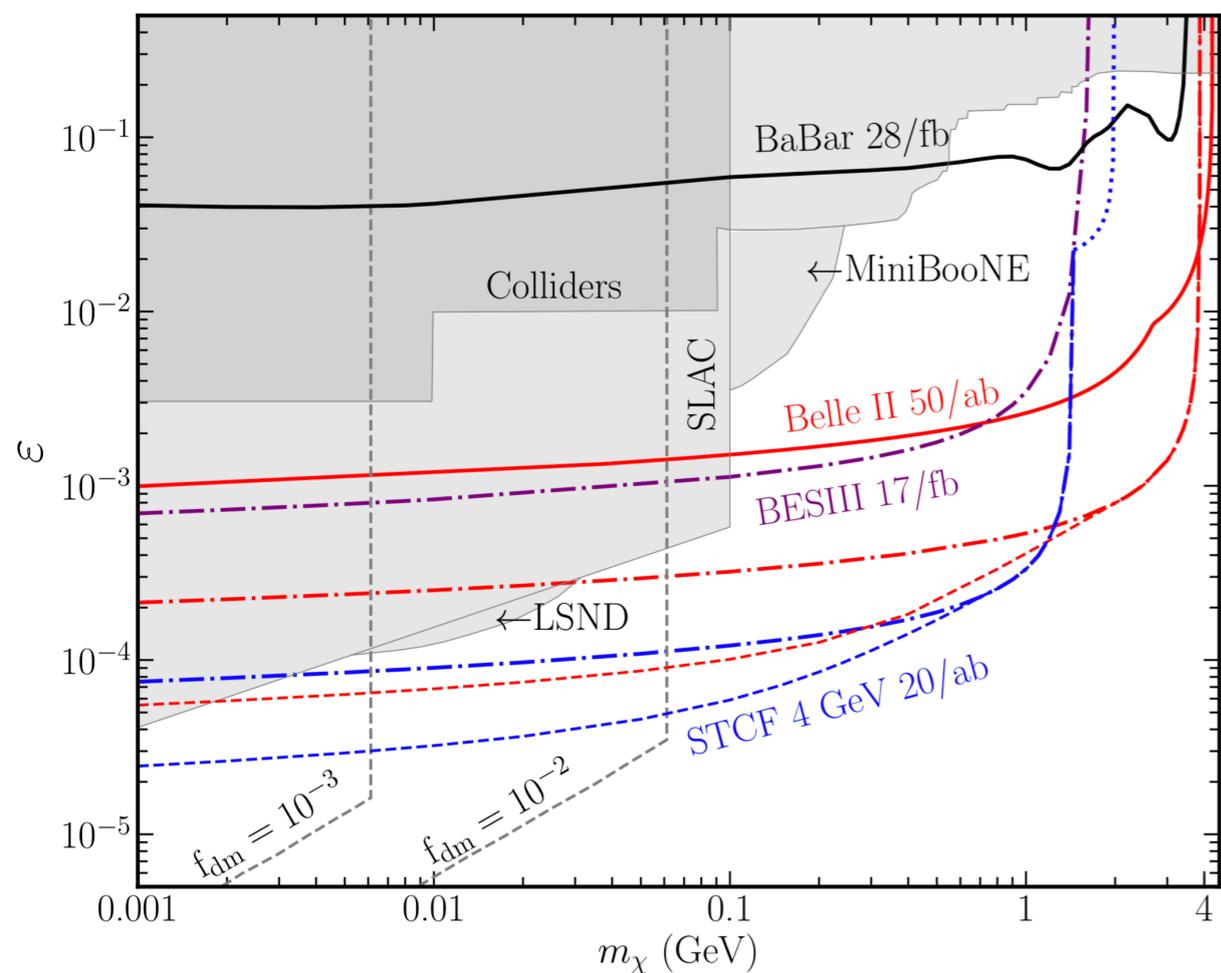
$$e^+e^- \rightarrow \Upsilon(3S) \rightarrow \gamma A^0$$

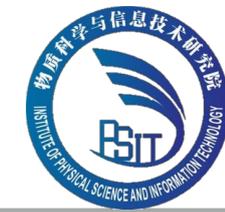
BaBar, 0808.0017

High-E (28/fb): $3.2 \text{ GeV} < E_{\text{cm}}^\gamma < 5.5 \text{ GeV}$, $-0.31 < \cos(\theta_{\text{cm}}^\gamma) < 0.6$

Low-E (19/fb): $2.2 \text{ GeV} < E_{\text{cm}}^\gamma < 3.7 \text{ GeV}$, $-0.46 < \cos(\theta_{\text{cm}}^\gamma) < 0.46$

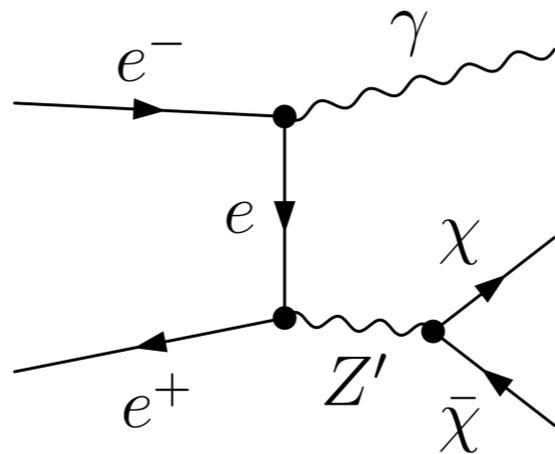






Z' DM models

Zuowei Liu, Yong-Heng Xu, **Yu Zhang**, 1903.12114, JHEP

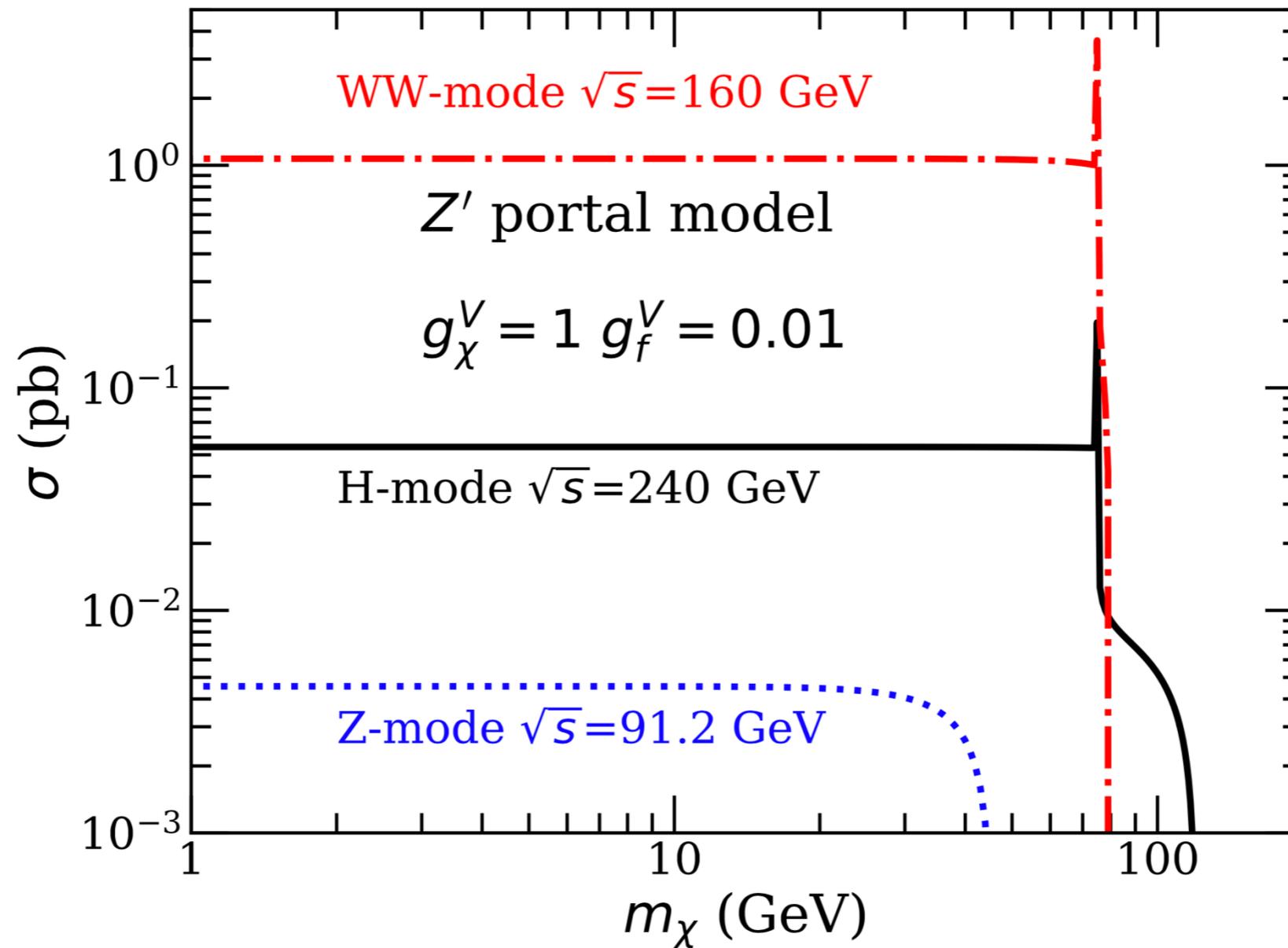


$$\mathcal{L} = Z'_\mu \bar{\chi} \gamma^\mu (g_V^\chi - g_A^\chi \gamma_5) \chi + Z'_\mu \bar{f} \gamma^\mu (g_V^f - g_A^f \gamma_5) f$$

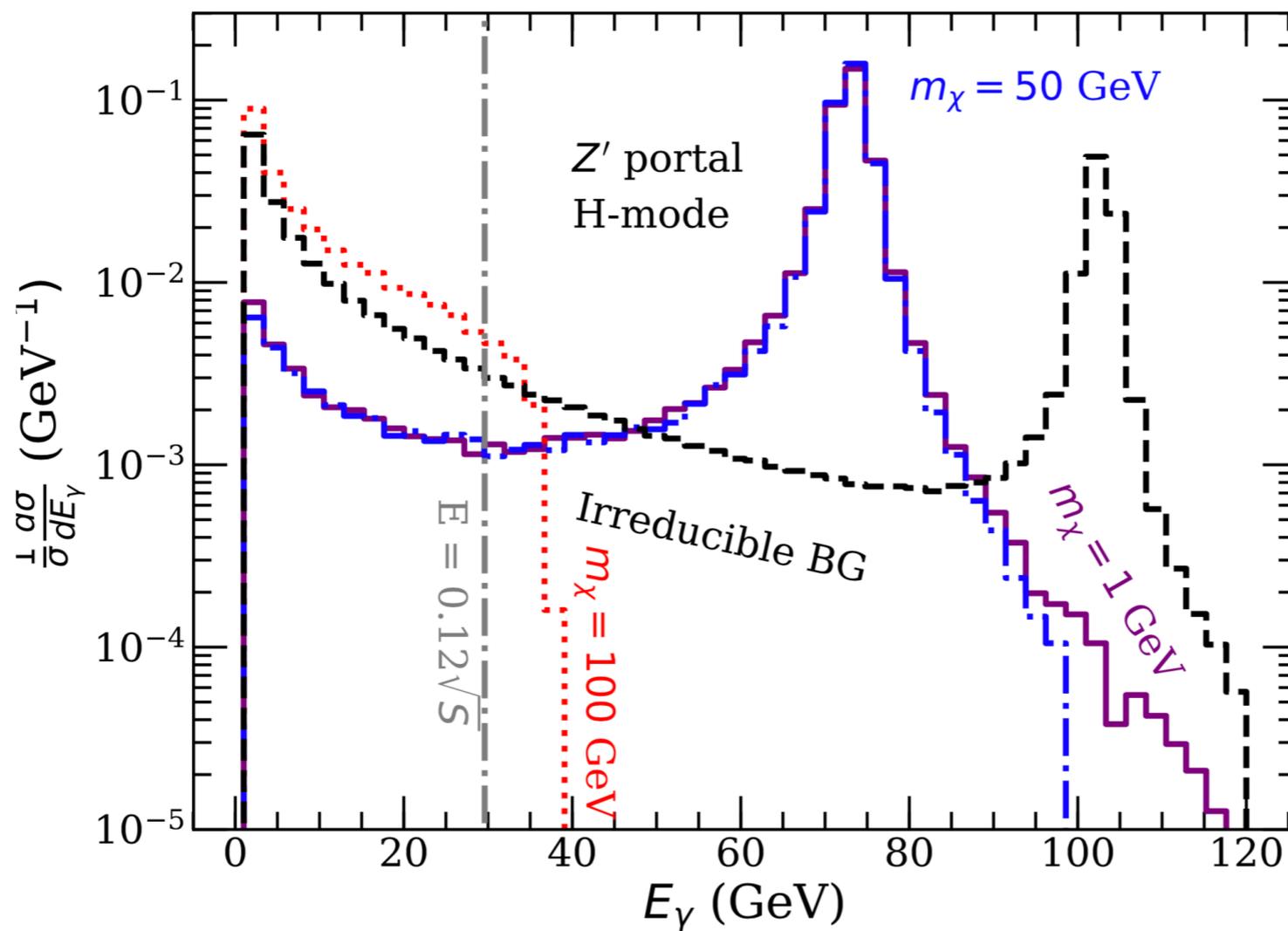
$$\frac{d\sigma}{dE_\gamma dz_\gamma} = \frac{\alpha [(g_V^f)^2 + (g_A^f)^2] [(g_V^\chi)^2 (1 + 2y) + (g_A^\chi)^2 (1 - 4y)] s_\gamma^2 \beta_\chi \left[\frac{1 + x(1 + z_\gamma^2)}{1 - z_\gamma^2} \right]}{6\pi^2 s E_\gamma [(s_\gamma - M_{Z'}^2)^2 + M_{Z'}^2 \Gamma_{Z'}^2]}$$

$$\Gamma_{Z'} = \Gamma(Z' \rightarrow \chi \bar{\chi}) + \sum_f \Gamma(Z' \rightarrow f \bar{f})$$

$$\Gamma(Z' \rightarrow \chi \bar{\chi}) = \frac{M_{Z'}}{12\pi} \sqrt{1 - 4 \frac{m_\chi^2}{M_{Z'}^2}} \left[(g_V^\chi)^2 \left(1 + 2 \frac{m_\chi^2}{M_{Z'}^2} \right) + (g_A^\chi)^2 \left(1 - 4 \frac{m_\chi^2}{M_{Z'}^2} \right) \right]$$



$$M'_Z = 150 \text{ GeV}$$

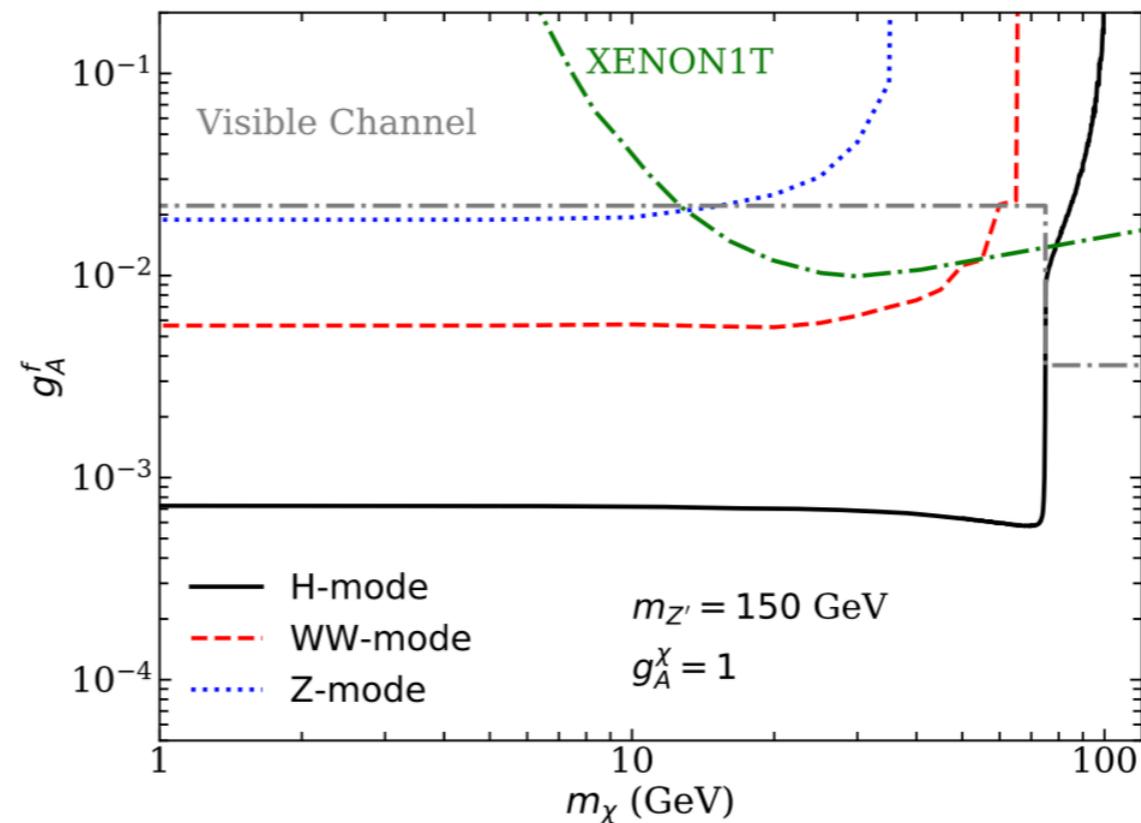
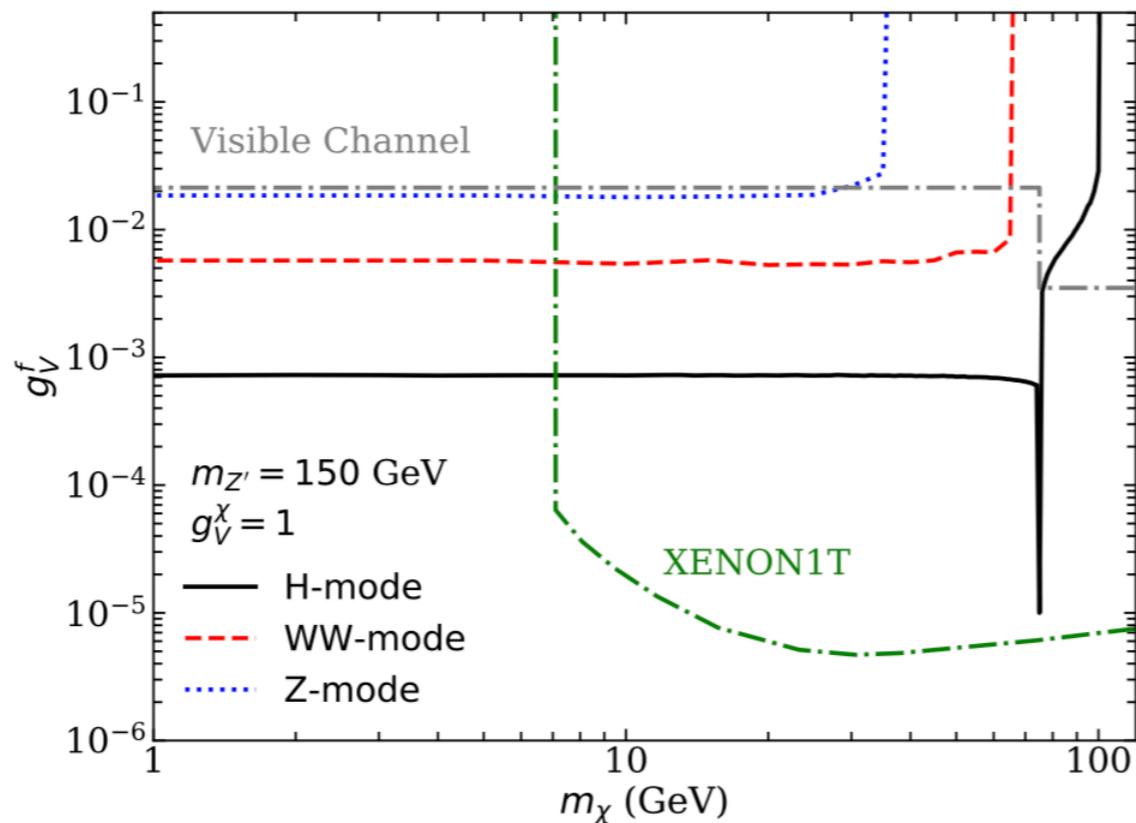


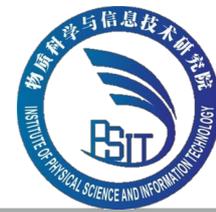
- (1) $E_\gamma > 0.1 \text{ GeV}$,
- (2) $|\cos \theta_\gamma| < |\cos \theta_b| = 0.99$,
- (3) $E_\gamma < E_\chi^m = (s - 4m_\chi^2)/(2\sqrt{s})$,
- (4) veto $E_\gamma \in (E_\gamma^Z \pm 5\Gamma_\gamma^Z)$,
- (5) $E_\gamma(\theta_\gamma) > E_B^m(\theta_\gamma) = \sqrt{s}(1 + \sin \theta_\gamma / \sin \theta_b)^{-1}$

In the H mode: (for $m < 75 \text{ GeV}$)

$$147 \text{ GeV} < M_\gamma < 153 \text{ GeV}$$

$$M_\gamma = \sqrt{s - 2\sqrt{s}E_\gamma}$$





DM effective operators

Zuowei Liu, Yong-Heng Xu, **Yu Zhang**, 1903.12114, JHEP

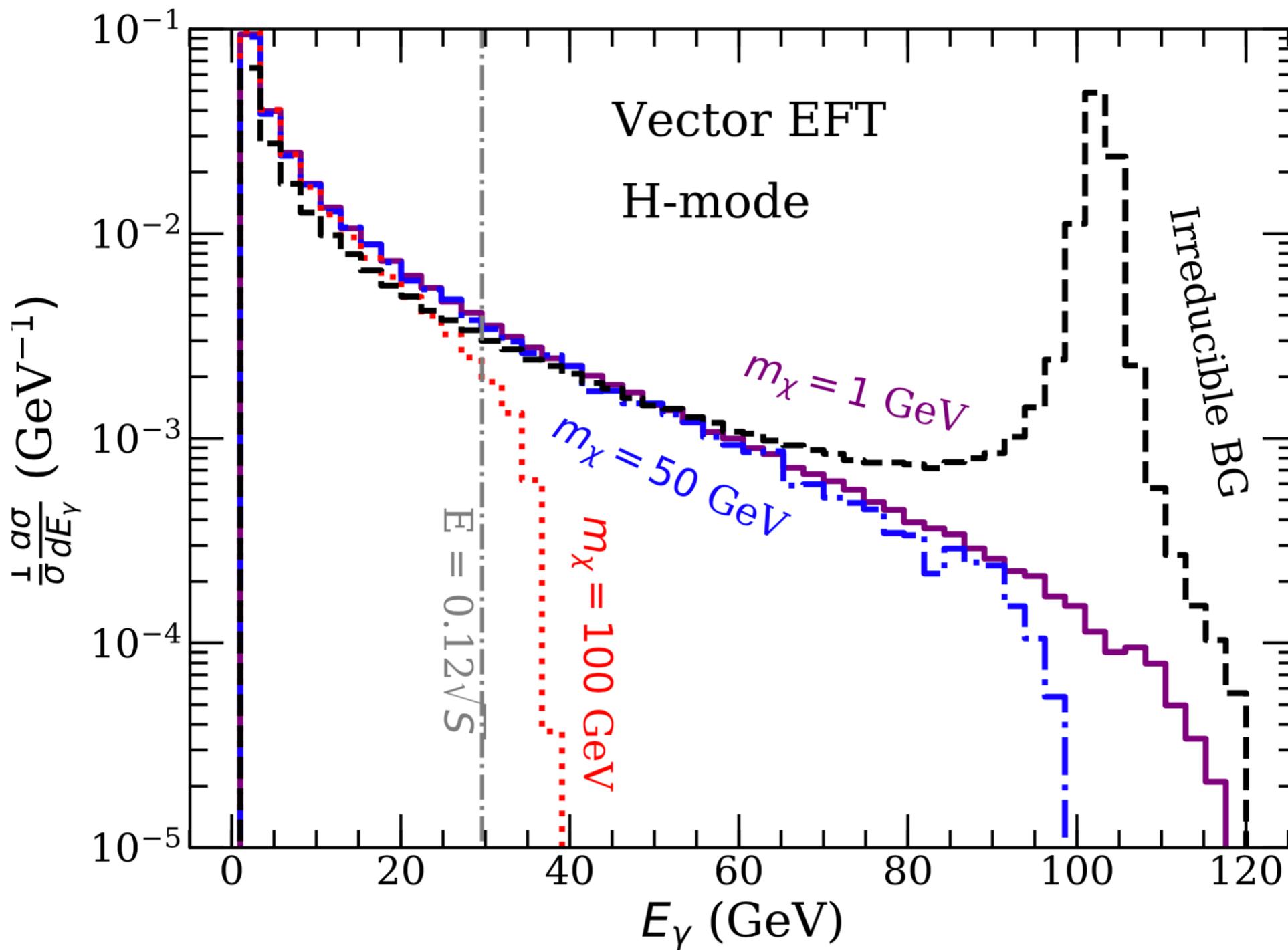
Vector: $\mathcal{L} = \frac{1}{\Lambda_V^2} \bar{\chi} \gamma_\mu \chi \bar{\ell} \gamma^\mu \ell,$

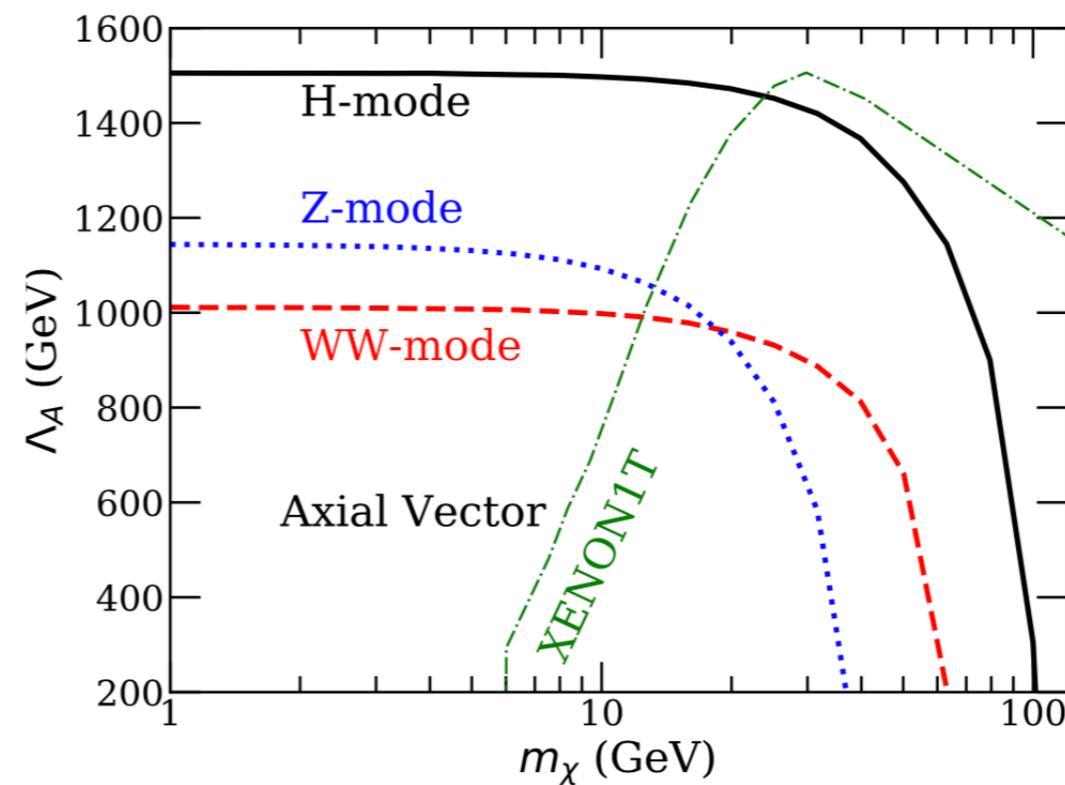
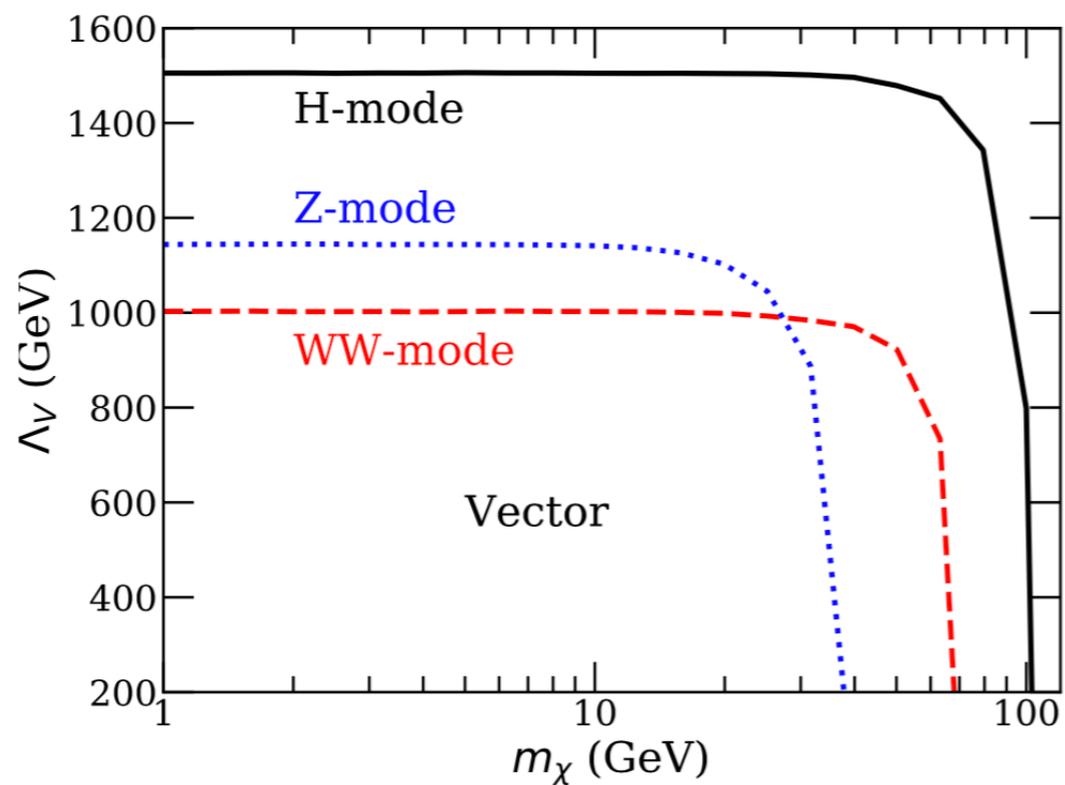
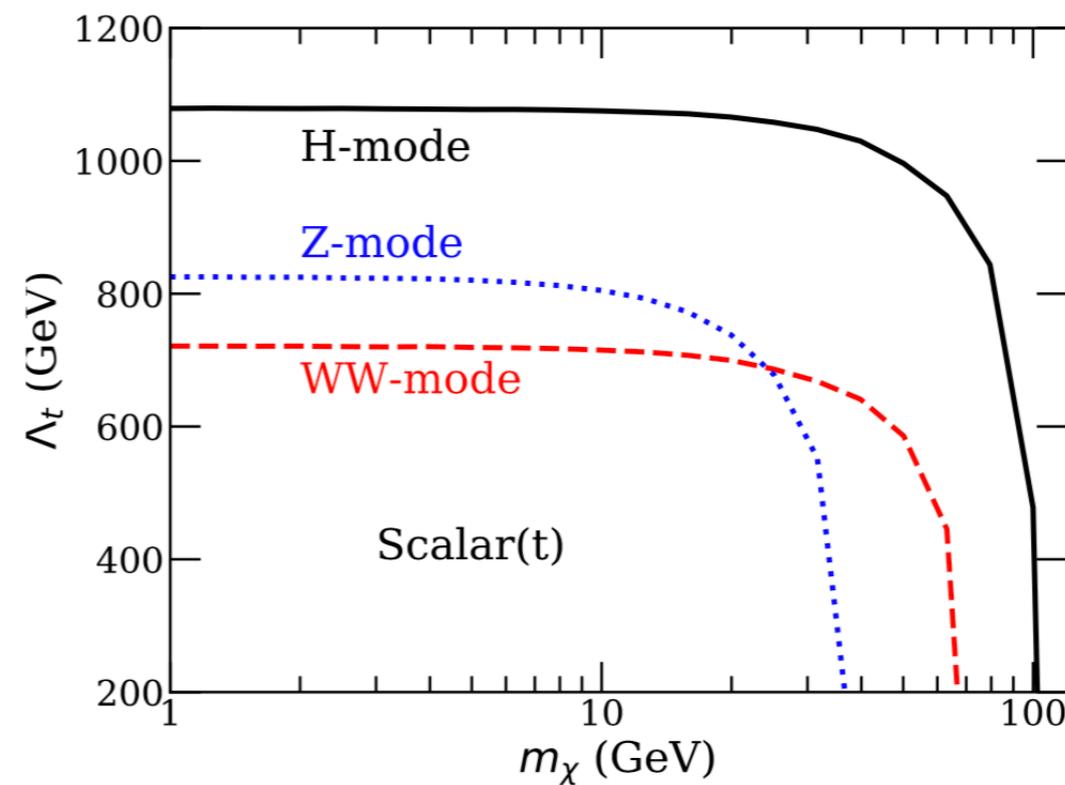
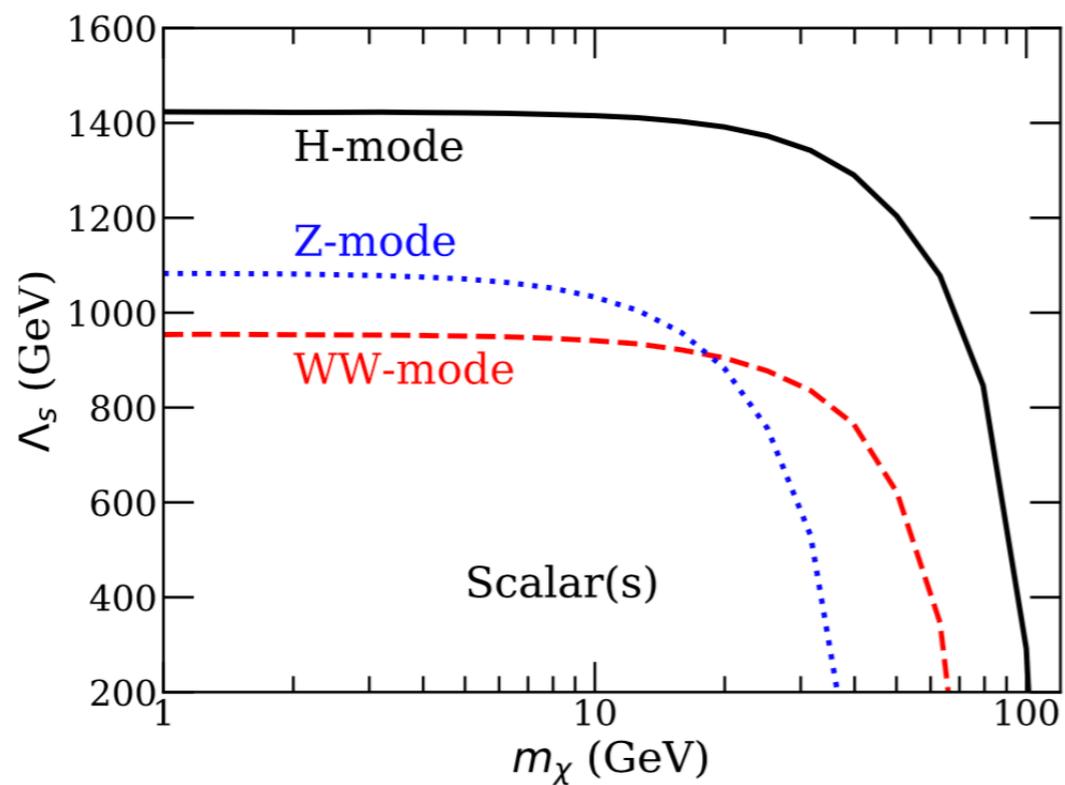
Scalar(s): $\mathcal{L} = \frac{1}{\Lambda_s^2} \bar{\chi} \chi \bar{\ell} \ell,$

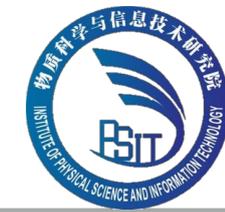
Axial vector: $\mathcal{L} = \frac{1}{\Lambda_A^2} \bar{\chi} \gamma_\mu \gamma_5 \chi \bar{\ell} \gamma^\mu \gamma_5 \ell,$

Scalar(t): $\mathcal{L} = \frac{1}{\Lambda_t^2} \bar{\chi} \ell \bar{\ell} \chi$

Distributions



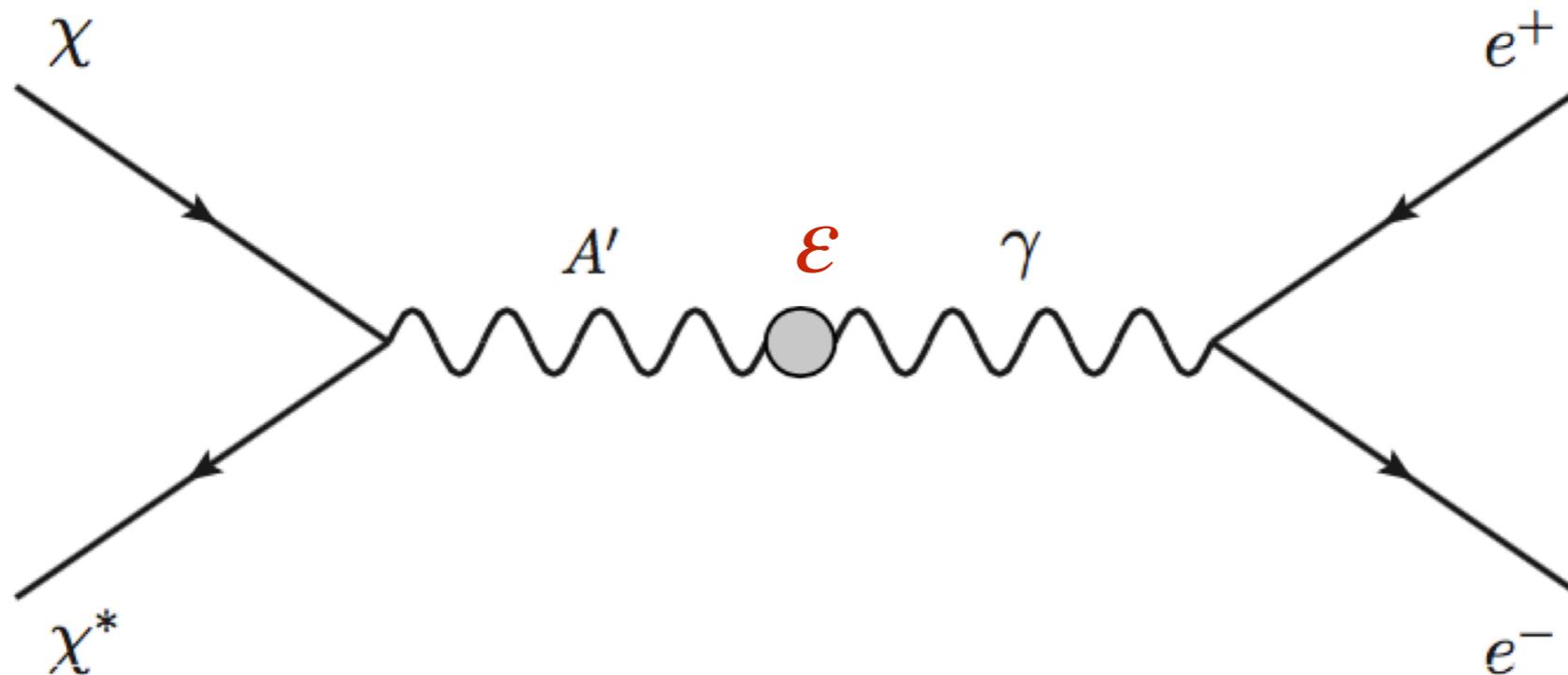




Dark photon invisible decay at BESIII/STCF

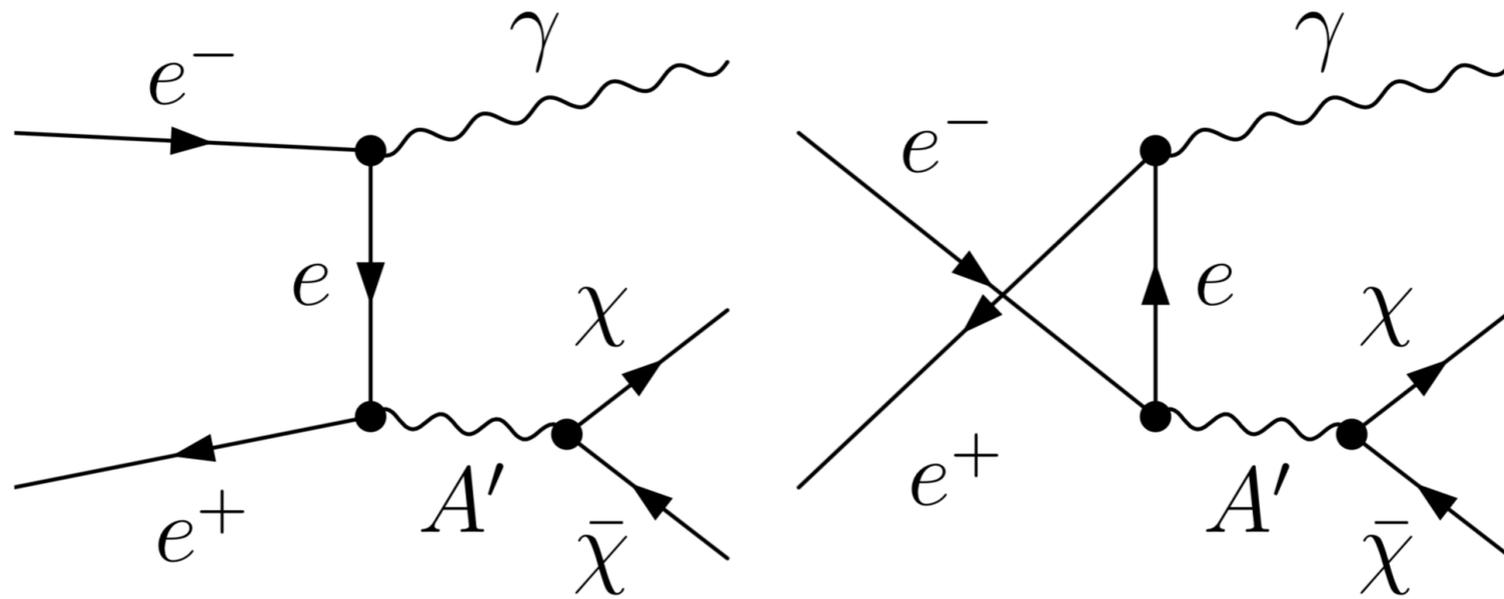
Yu Zhang, et. al., 1907.07046, PRD

Dark photon



$$\mathcal{L}_{\text{kinetic mixing}} = -\frac{\epsilon}{2} F'_{\mu\nu} F^{\mu\nu}$$

$$\epsilon Q_f A' \bar{f} \gamma^\mu f$$

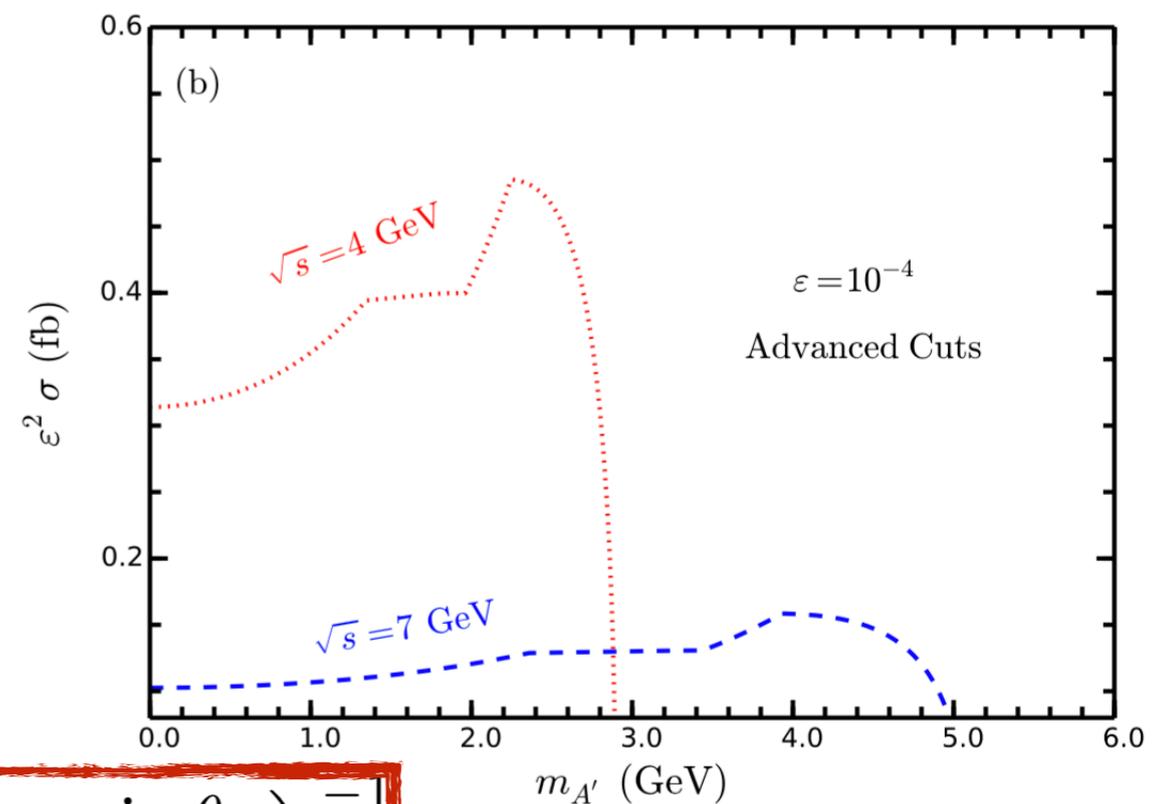
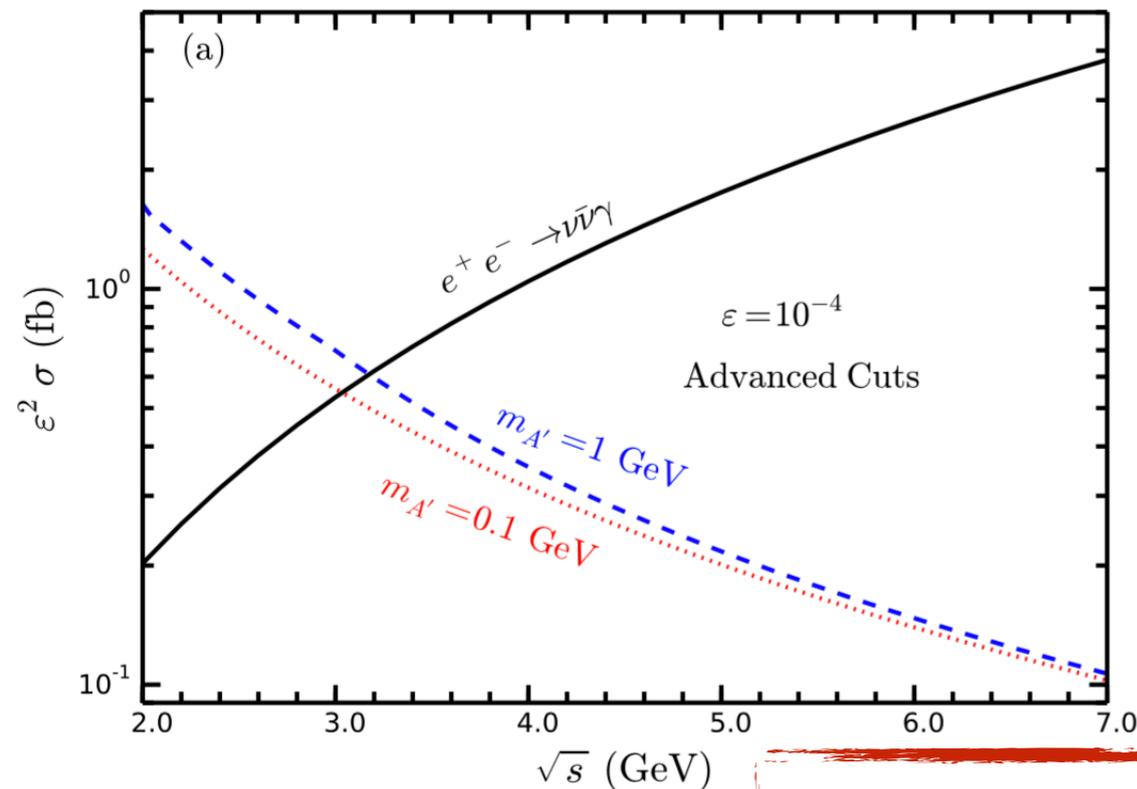
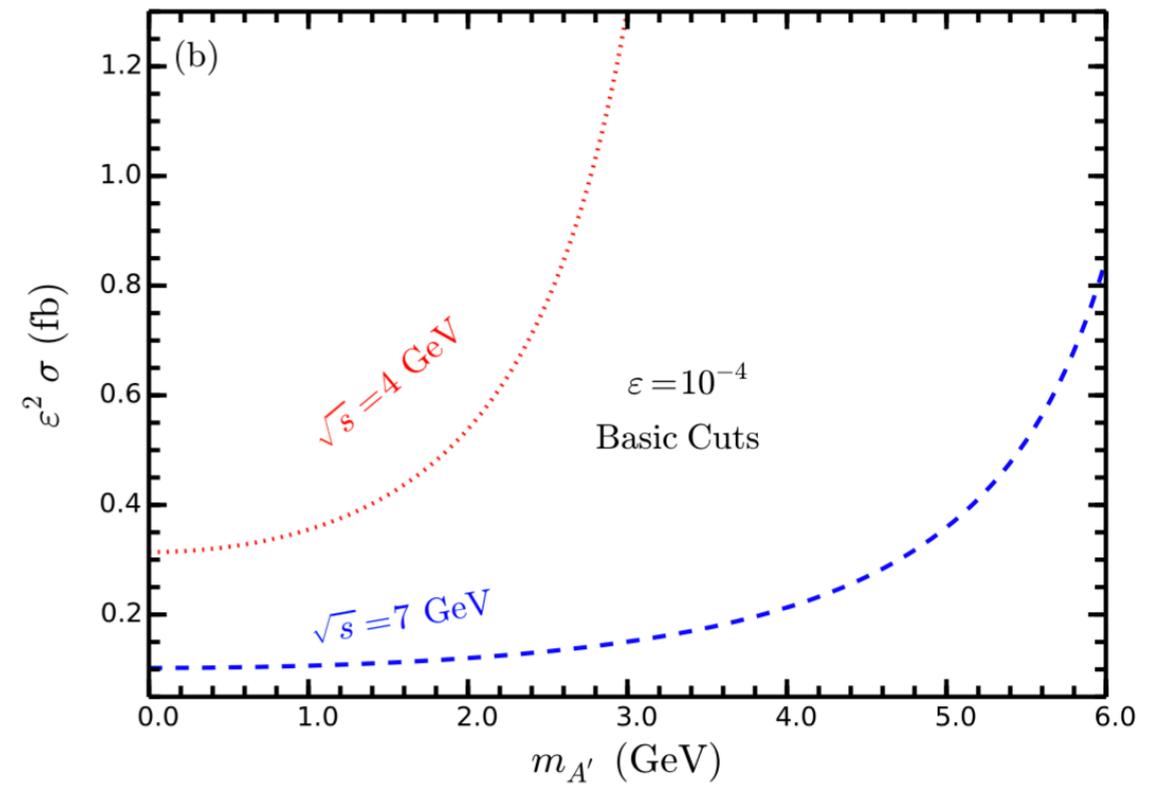
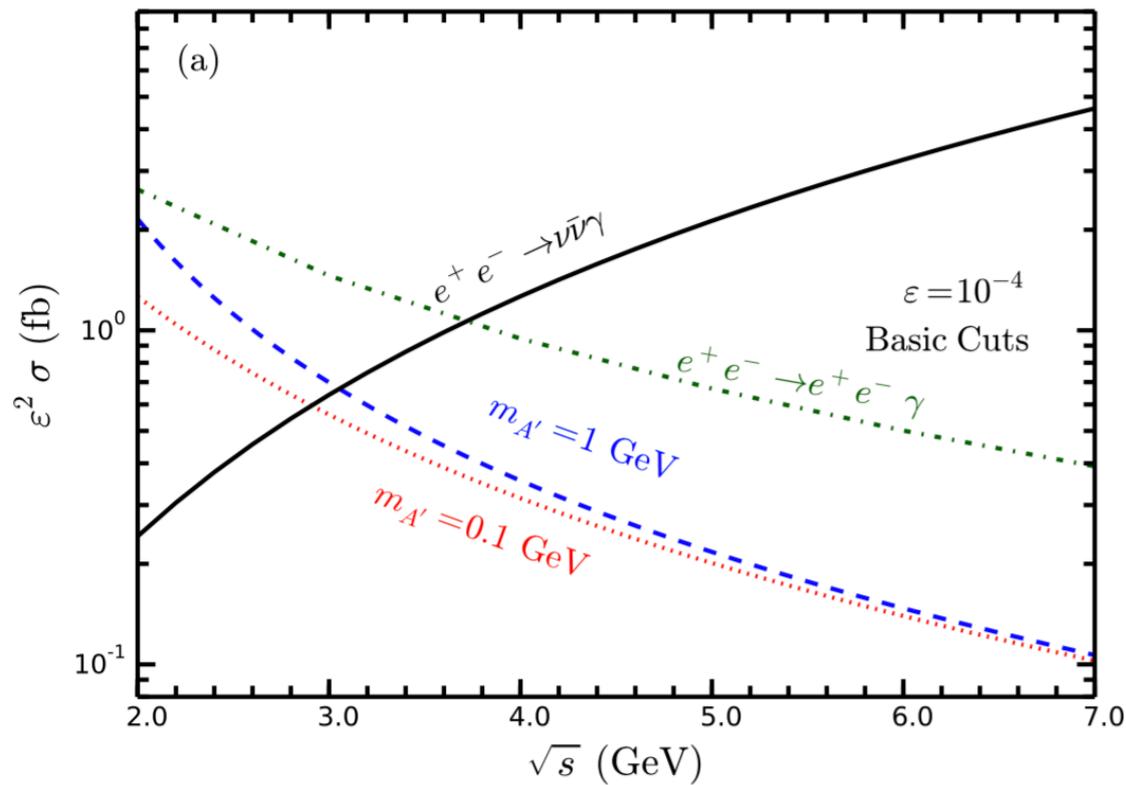


$$E_\gamma = \frac{s - m_{A'}^2}{2\sqrt{s}}$$

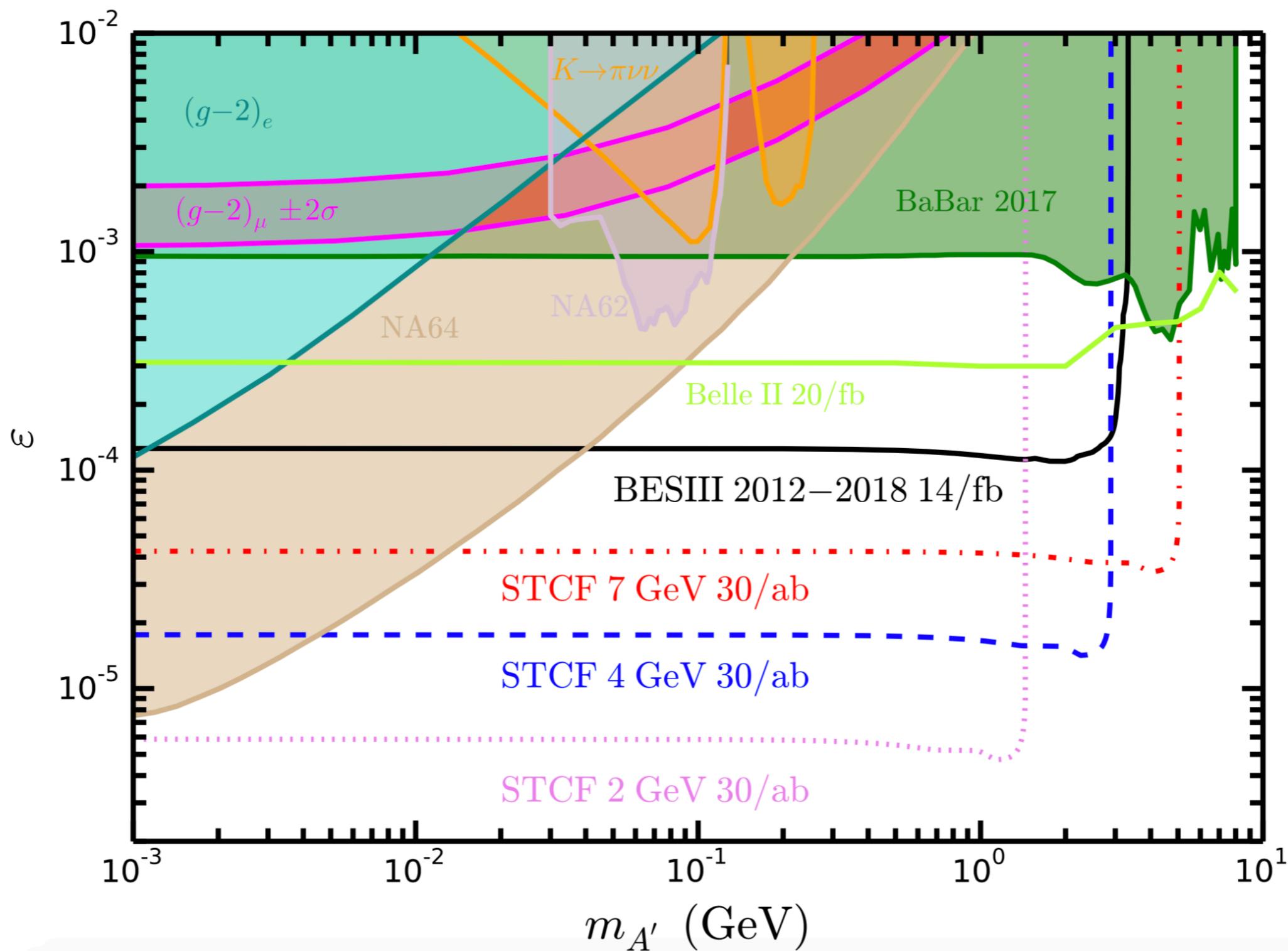
$$\frac{d\sigma_{\gamma A'}}{dz_\gamma} = \frac{2\pi\epsilon^2\alpha^2}{s} \left(1 - \frac{m_{A'}^2}{s}\right) \frac{1 + z_\gamma^2 + \frac{4sm_{A'}^2}{(s - m_{A'}^2)^2}}{(1 + z_\gamma)(1 - z_\gamma)}$$

$$\sigma_{\gamma A'} = \frac{2\pi\epsilon^2\alpha^2}{s} \left(1 - \frac{m_{A'}^2}{s}\right) \left[\left(1 + \frac{2sm_{A'}^2}{(s - m_{A'}^2)^2}\right) \mathcal{Z} - z_\gamma^{\max} + z_\gamma^{\min} \right]$$

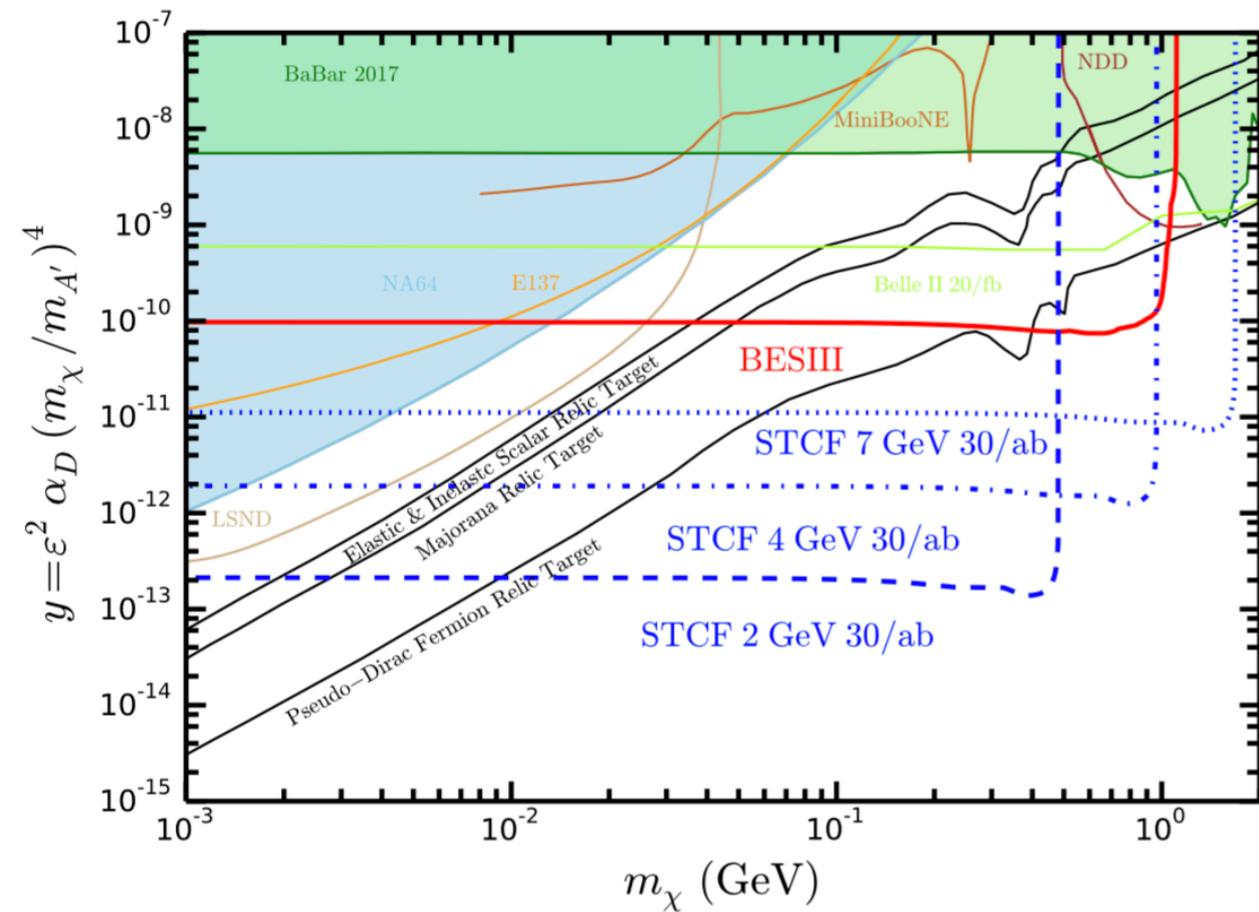
$$\mathcal{Z} = \ln \frac{(1 + z_\gamma^{\max})(1 - z_\gamma^{\min})}{(1 - z_\gamma^{\max})(1 + z_\gamma^{\min})}$$



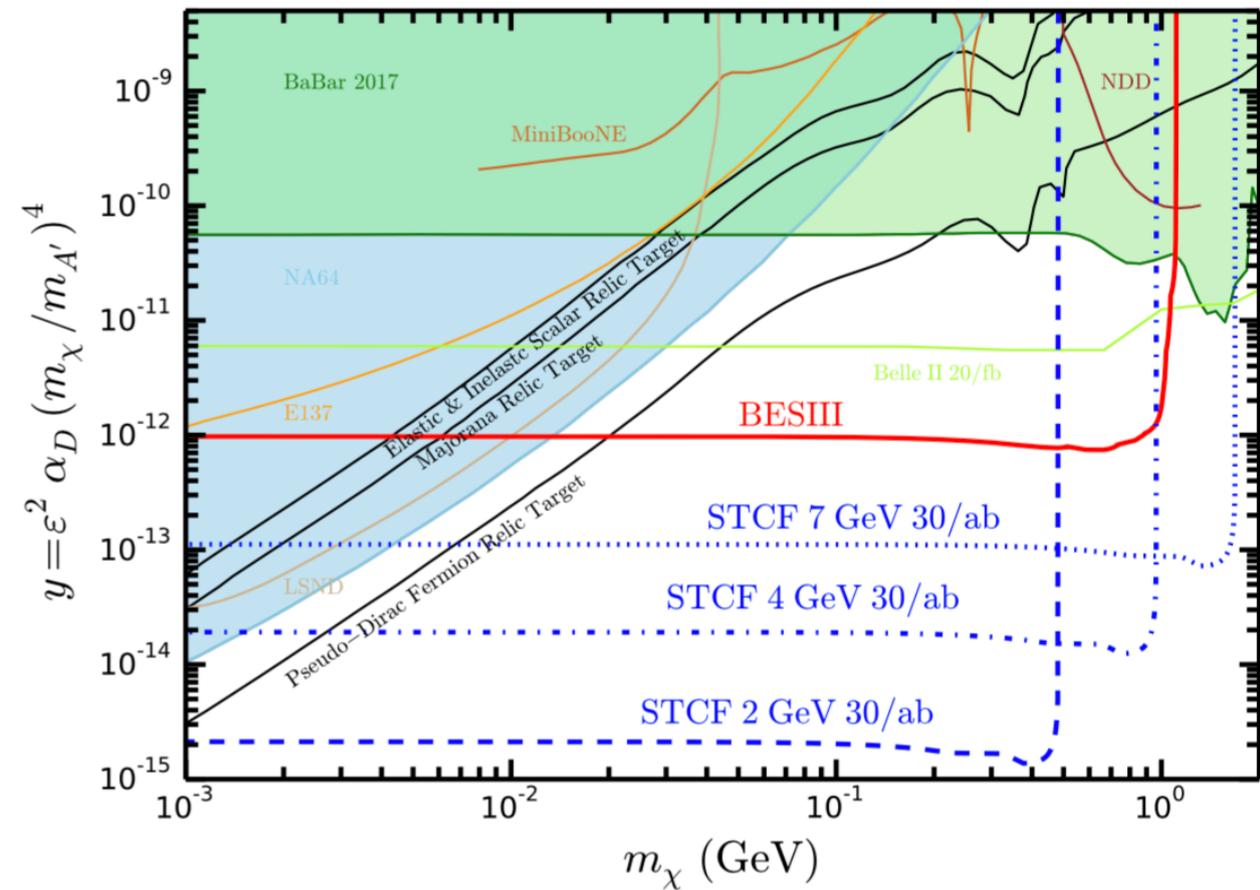
$$E_{\gamma}^m(\theta_{\gamma}) = \sqrt{s} \left(1 + \frac{\sin \theta_{\gamma}}{\sin \theta_b} \right)^{-1}$$



$$y = \varepsilon^2 \alpha_D (m_\chi / m_{A'})^4$$



$$m_{A'} = 3m_\chi, \quad \alpha_D = 0.5$$



$$m_{A'} = 3m_\chi, \quad \alpha_D = 0.005$$



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