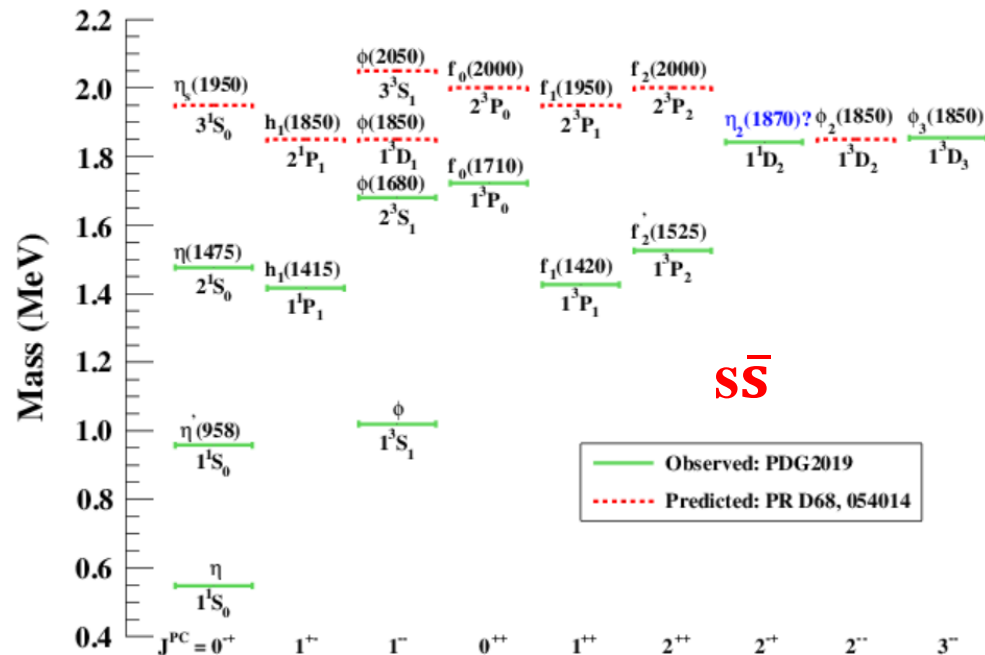


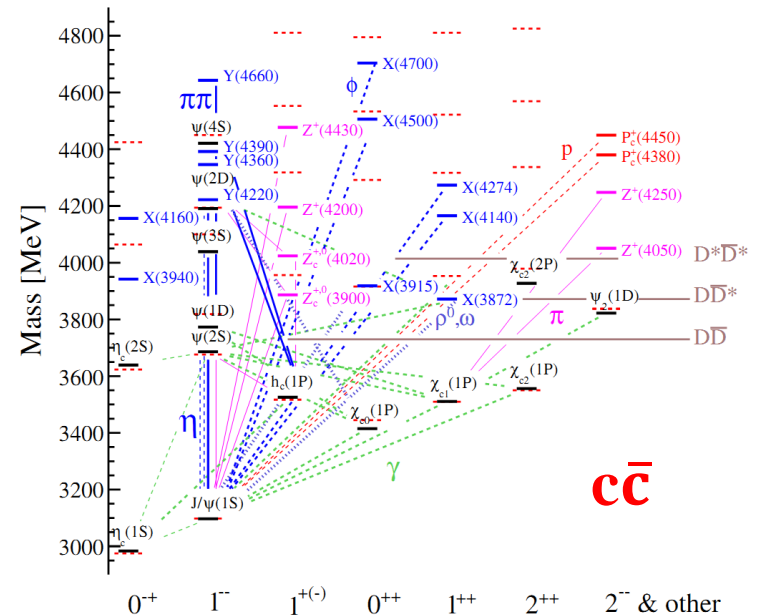
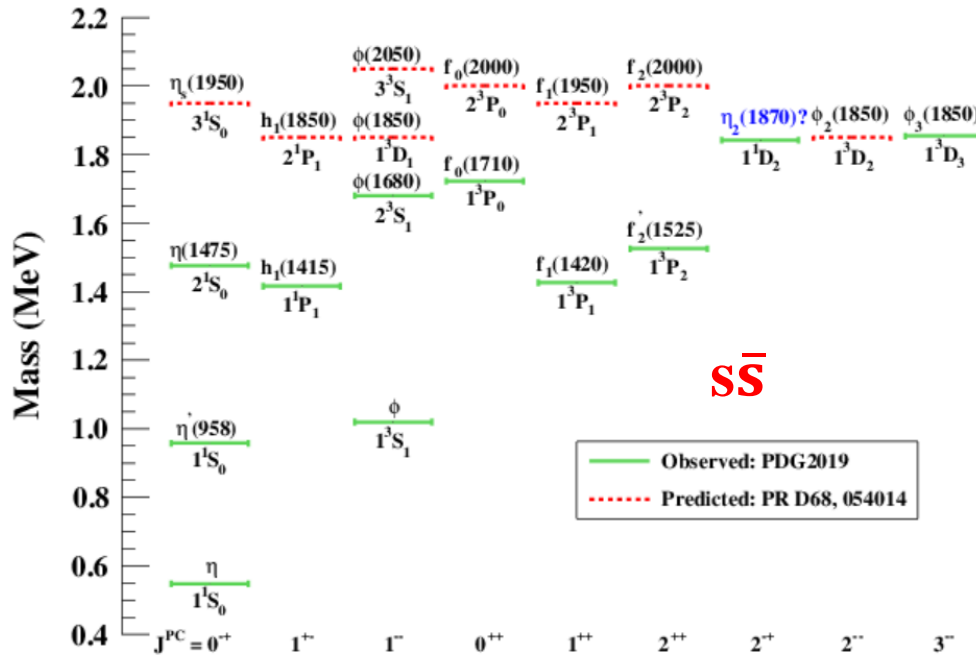
# Recent results on $\phi(2170)$ at BESIII

鄢文标 (中国科学技术大学)



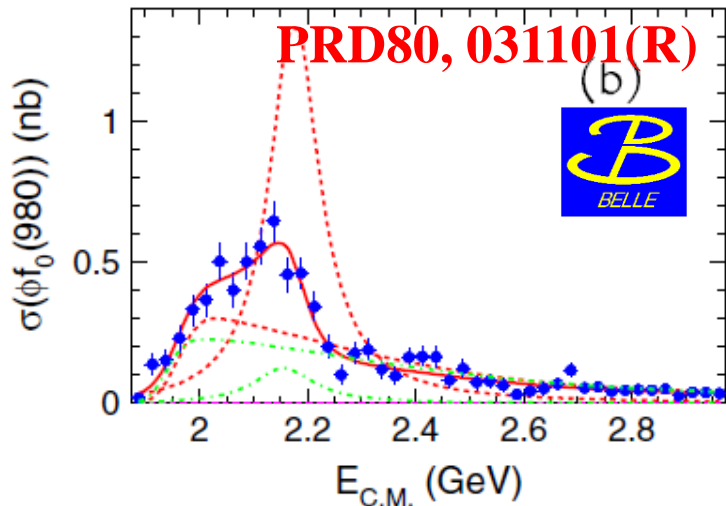
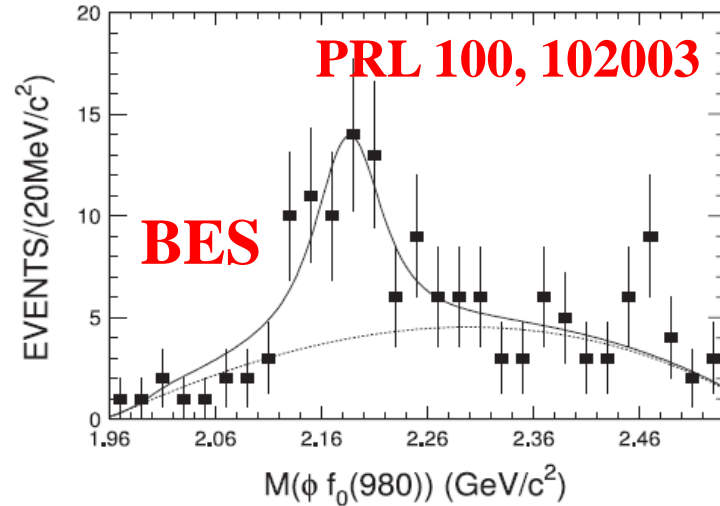
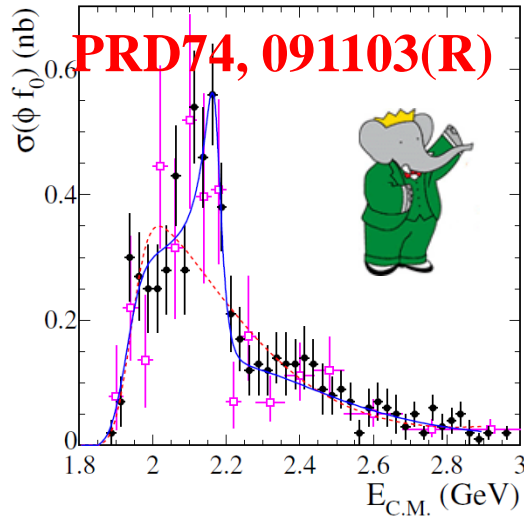
“6<sup>th</sup> workshop on the XYZ particles”, 2020.01.20, 上海

# Strange quarkonium



- Compared with  $c\bar{c}$  and  $b\bar{b}$ ,  $s\bar{s}$  is a terra incognita.
- There are XYZ particles with charm & bottom quark, how about strange quark ?
- The strange quark has intermediate mass,  $s\bar{s}$  serves as bridge between light and heavy quark.

# $\phi(2170)/Y(2175)$

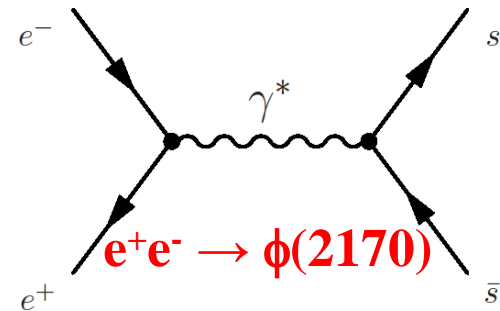
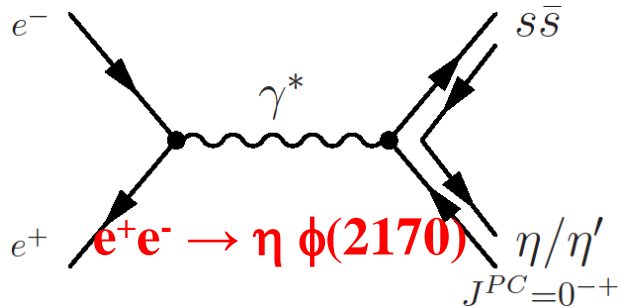
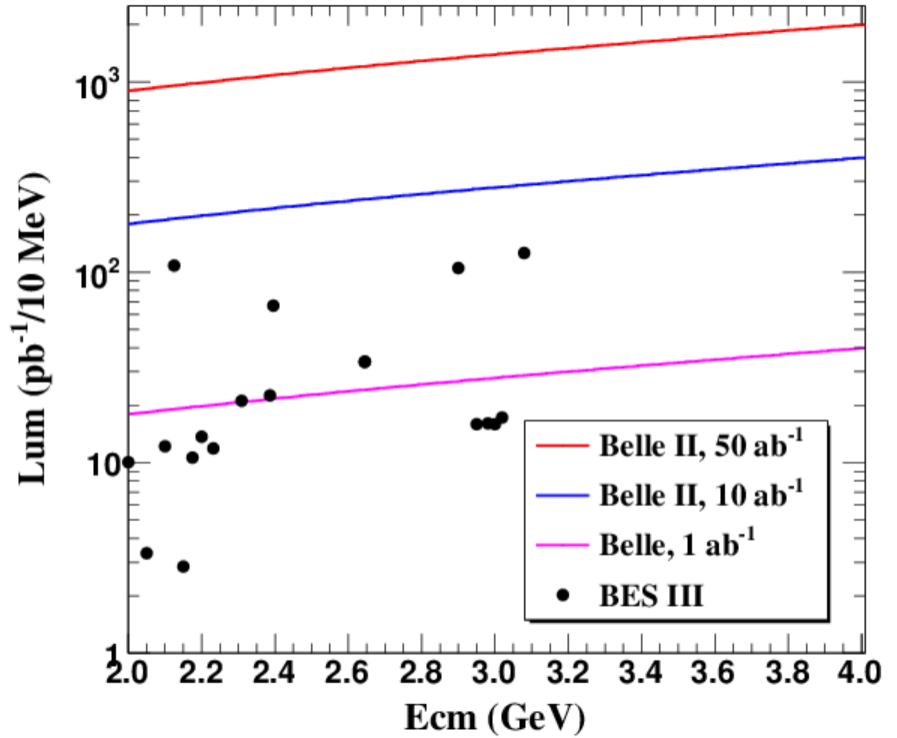
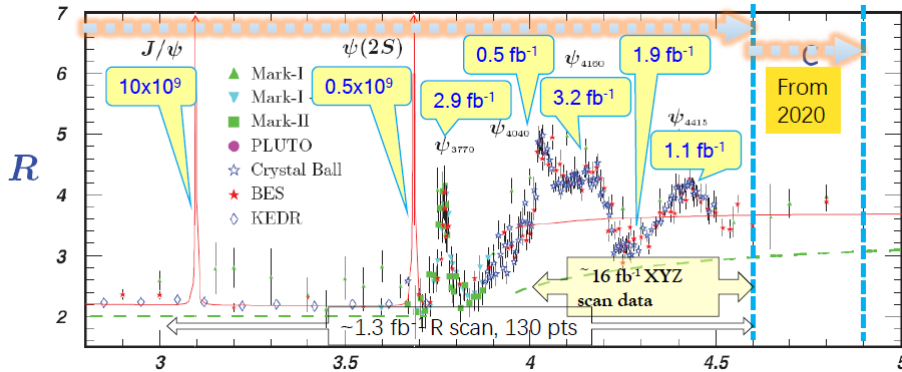
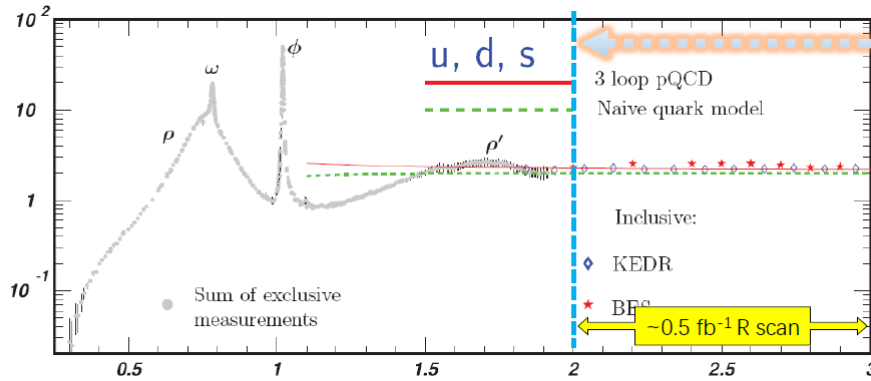


**Eur. Phys. J. C72, 2008**

$$e^+e^- \Rightarrow \begin{cases} Y(2175) \rightarrow \phi(1020)\pi^+\pi^- & \text{strange,} \\ Y(4260) \rightarrow J/\psi\pi^+\pi^- & \text{charm,} \\ \Upsilon(10860) \rightarrow \Upsilon(1S, 2S)\pi^+\pi^- & \text{bottom,} \end{cases}$$

$\phi(2170)$  as strange analogue of  $Y(4220)$

# $J^{PC} = 1^{-} \phi(2170) @ \text{BESIII}$

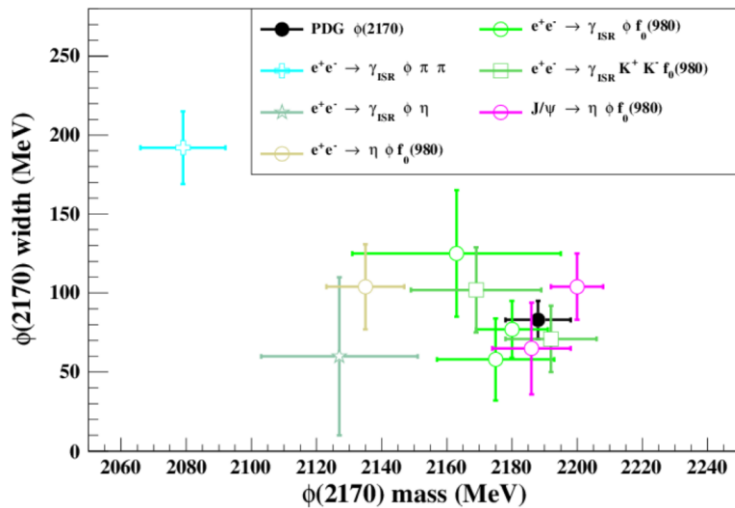


# $\phi(2170)$

PDG

$\phi(2170)$  DECAY MODES

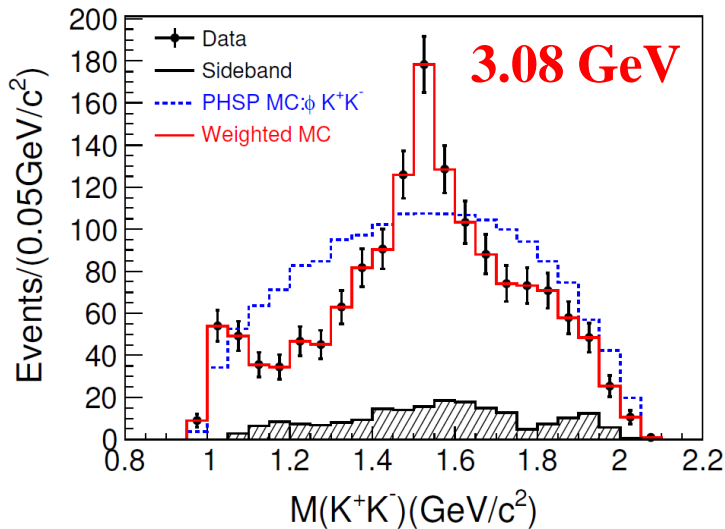
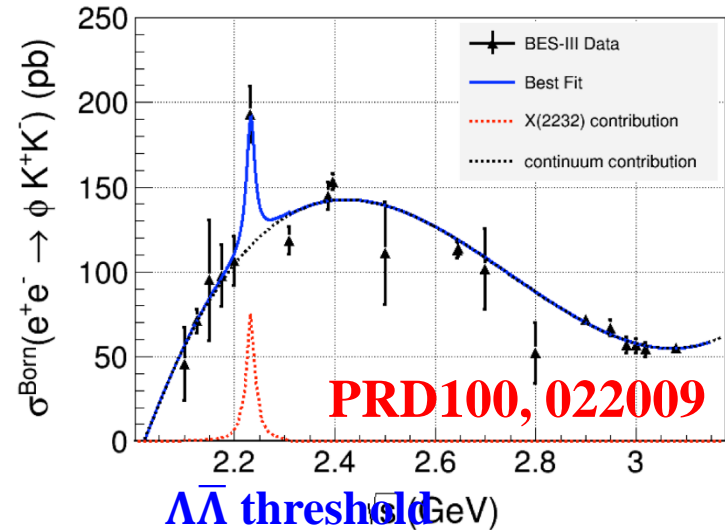
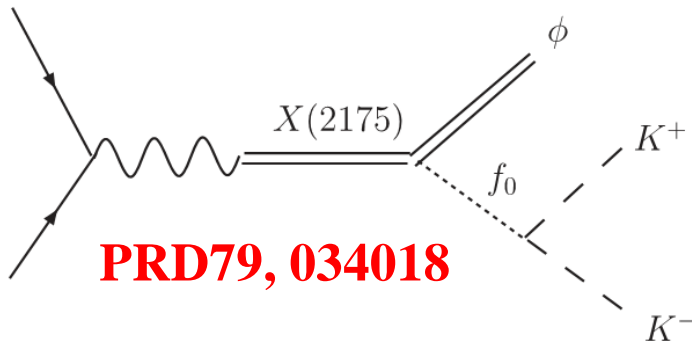
Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1$ $e^+ e^-$	seen
$\Gamma_2$ $\phi \eta$	
$\Gamma_3$ $\phi \pi \pi$	
$\Gamma_4$ $\phi f_0(980)$	seen
$\Gamma_5$ $K^+ K^- \pi^+ \pi^-$	
$\Gamma_6$ $K^+ K^- f_0(980) \rightarrow K^+ K^- \pi^+ \pi^-$	seen
$\Gamma_7$ $K^+ K^- \pi^0 \pi^0$	
$\Gamma_8$ $K^+ K^- f_0(980) \rightarrow K^+ K^- \pi^0 \pi^0$	seen
$\Gamma_9$ $K^{*0} K^\pm \pi^\mp$	not seen
$\Gamma_{10}$ $K^*(892)^0 \bar{K}^*(892)^0$	not seen



- Published experimental information
  - ✓ Limited decay modes
  - ✓ Inconsistence on mass & width
- Theorists explain  $\phi(2170)$  as
  - ✓  $s\bar{s}g$  hybrid
  - ✓  $2^3D_1$  or  $3^3S_1 s\bar{s}$
  - ✓ tetraquark
  - ✓ Molecular state  $\Lambda\bar{\Lambda}$
  - ✓  $\phi f_0(980)$  resonance with FSI
  - ✓ Three body system  $\phi KK$
  - ✓ **Estimated or ruled out: not yet**
- aspects of  $\phi(2170)$  are still not fully understood.

$$e^+ e^- \rightarrow \phi K^+ K^-$$

- $\phi(2170)$ : resonant of  $\phi K K$

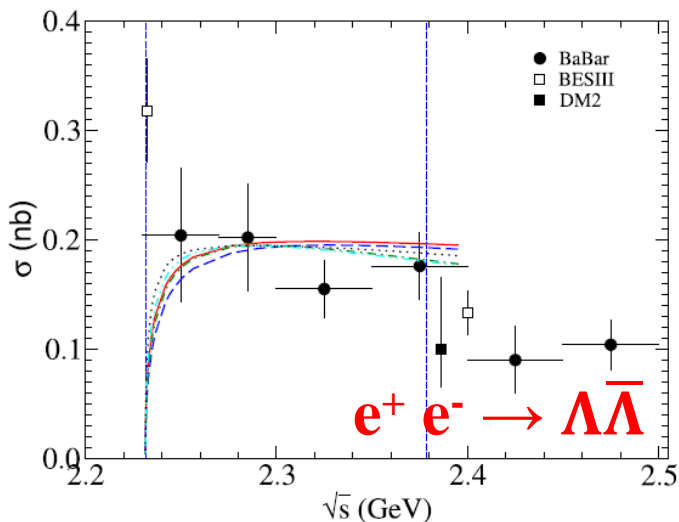
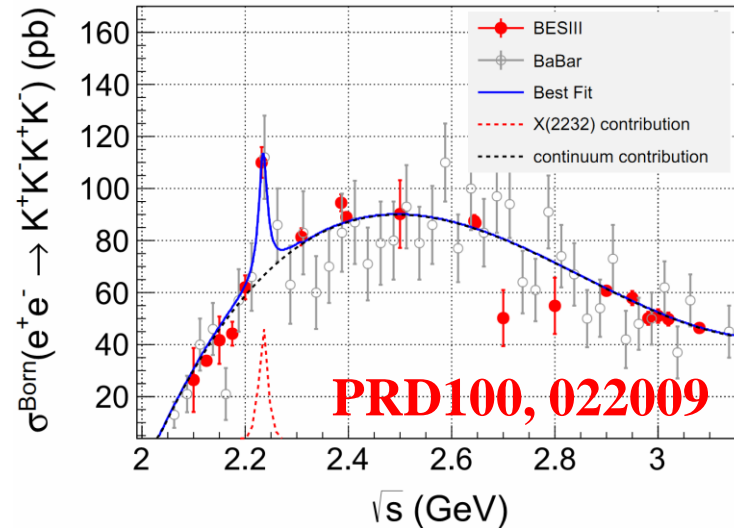
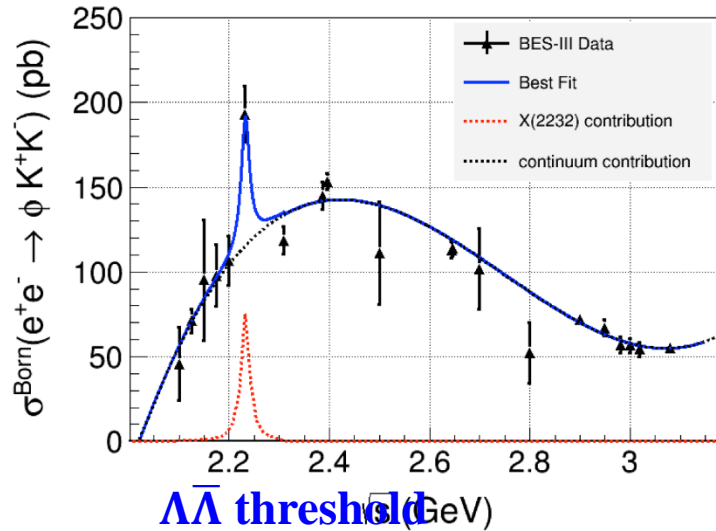


- A hint for a resonance around  $\Lambda\bar{\Lambda}$  threshold

- ✓ Mass =  $2232 \pm 3.5 \text{ MeV}$ ;
- ✓ Width  $< 20 \text{ MeV}$

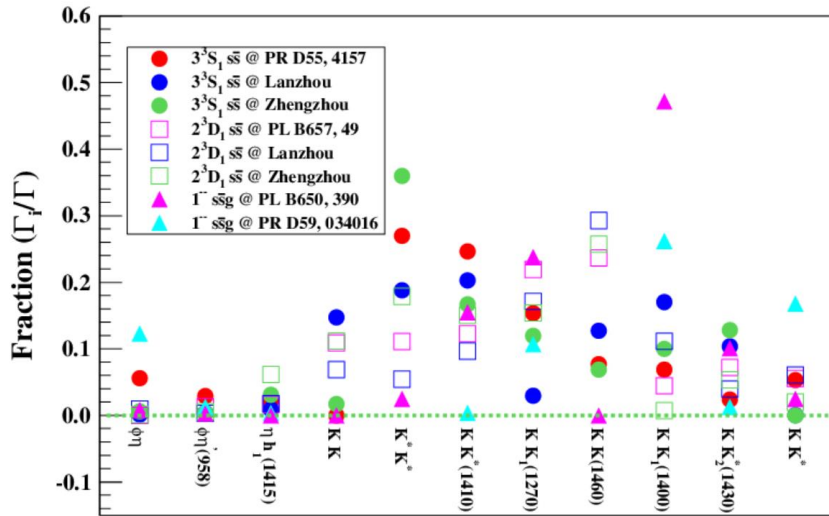
- Three body system  $\phi K K$ : ?

# $e^+ e^- \rightarrow 2(K^+ K^-)$



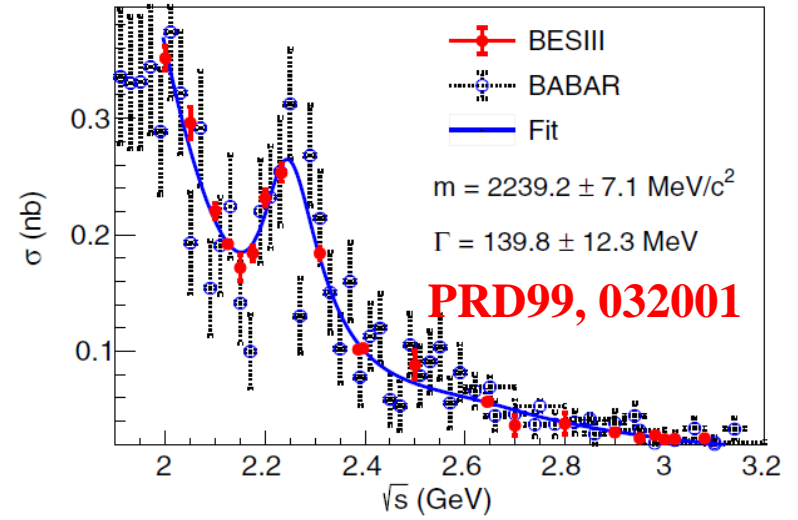
- $\phi K^+K^-$  and  $2(K^+K^-)$  have similar enhancement around 2.2324 GeV
- $\Lambda\bar{\Lambda}$  threshold ?
- More ideas ?

# $e^+ e^- \rightarrow K^+ K^-$



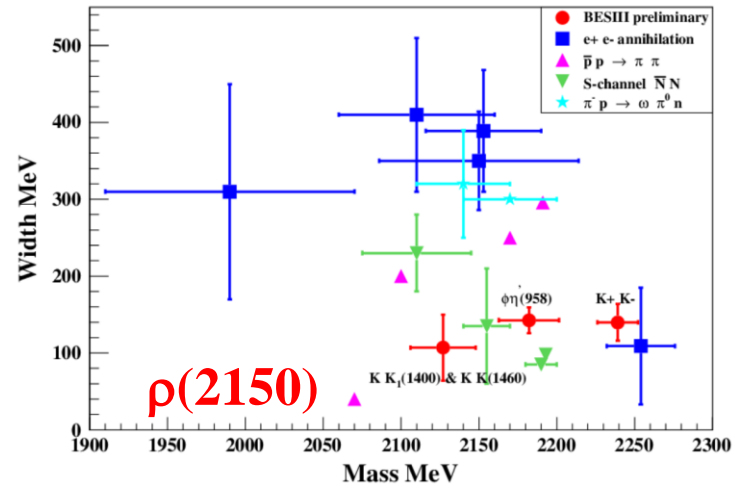
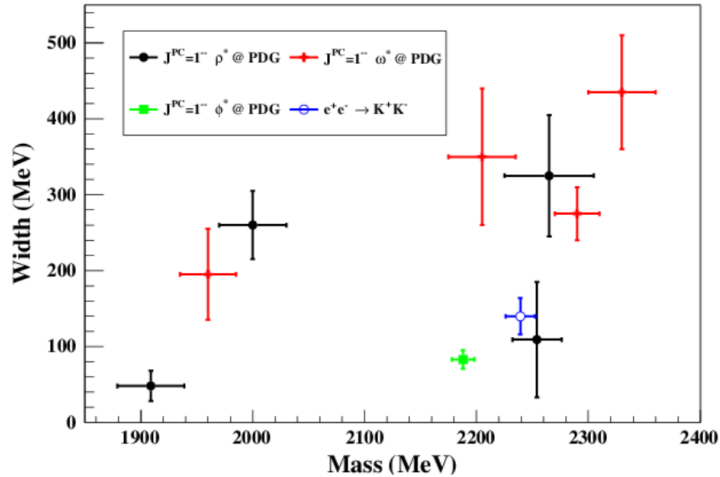
- $K^+K^-$  @  $\phi(2170)$ 
  - ✓ Obvious discrepancy between different theory models
  - ✓ isoscalar:  $\omega^*/\phi^*$ ; isovector:  $\rho^*$
- $\sigma(e^+e^- \rightarrow K^+K^-)$  @ [2.0-3.08]GeV

$\phi(2170)$ decay	This work	$^3P_0$ model	Data [5]
	<b><math>3^3S_1 \Lambda\bar{\Lambda}</math></b>	within $s\bar{s}$ [10]	
$KK$	73.8–87.7	...	...
$\phi f_0(980)$	0.25–0.3	< 10	Seen
$\omega\sigma$	4.2–4.9		
$K^*K_0^*(800)$	1.8–2.1	<b>PRD96, 074027</b>	...
Total	80.1–95		$83 \pm 12$

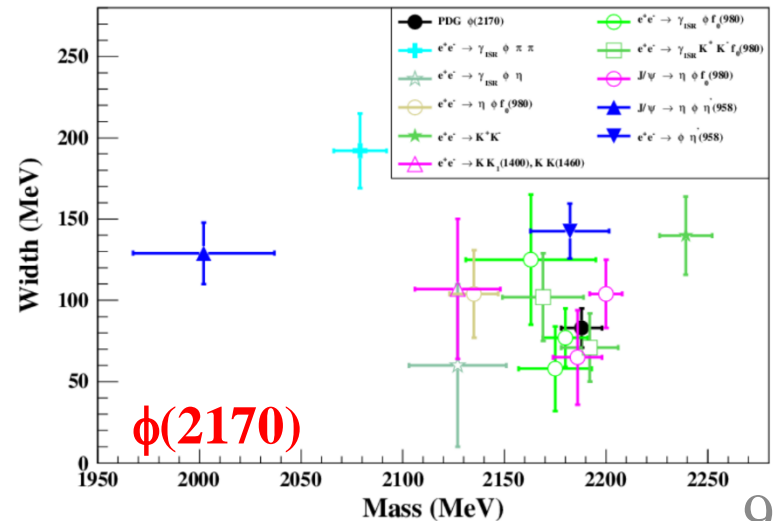




$$e^+ e^- \rightarrow K^+ K^-$$

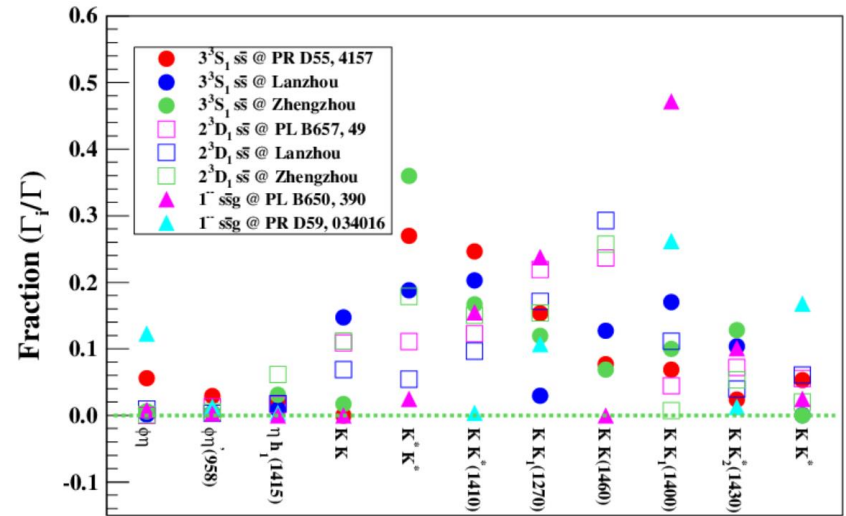
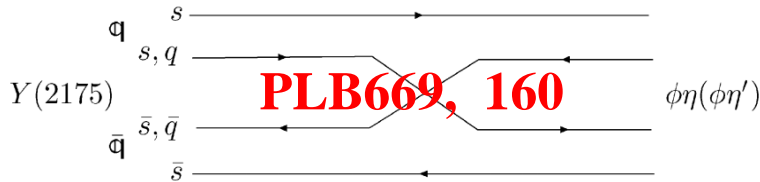


- Compare  $K^+K^-$  resonance
  - ✓  $J^{PC}=1^-$  vector:  $\omega^*/\phi^*/\rho^*$
  - ✓  $\rho(2150)$  @ PDG
  - ✓  $\phi(2150)$  experimental results
- $K^+K^-$  resonance:  $\rho(2150)$  ?



# $e^+ e^- \rightarrow \phi\eta$ and $\phi\eta'$

- $\phi\eta$  and  $\phi\eta'$  modes: isoscalar
  - ✓  $\phi^*$  and  $\omega^*$  (OZI suppressed)
  - ✓ useful to measure parameters
- Tetraquark favorites  $\phi\eta$  and  $\phi\eta'$

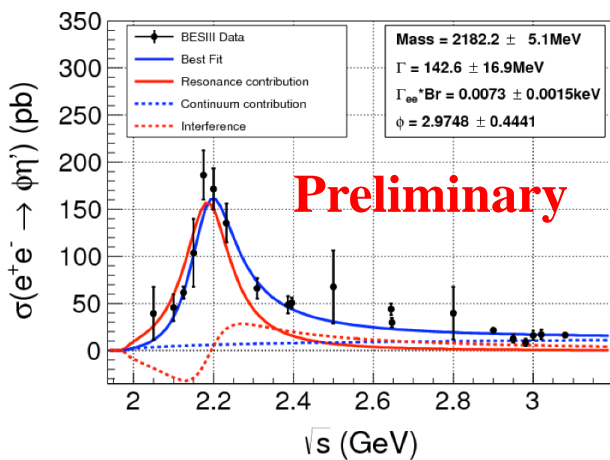
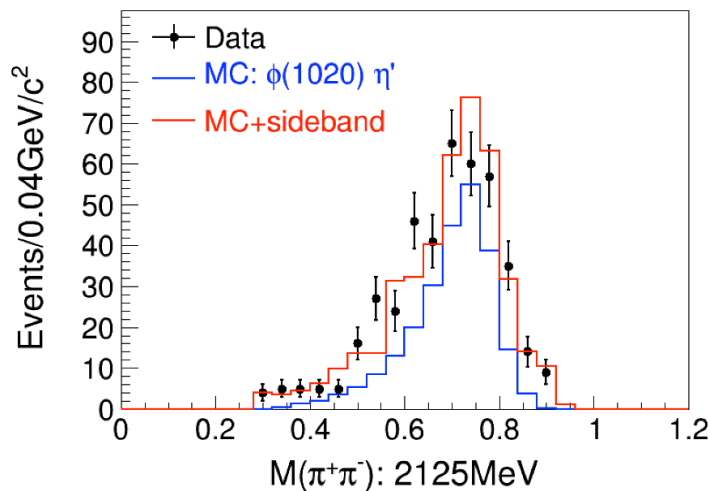
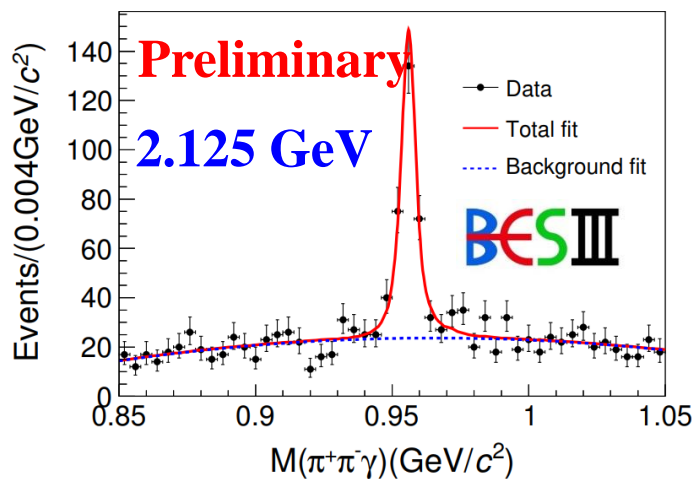


- $1^- \bar{s}s g$  hybrid has large  $\Gamma_{\phi\eta}$  and smaller  $\Gamma_{\phi\eta'}$

$1^- \bar{s}s g$	alt	2.2GeV	standard	IKP	Ding
	PRD59, 034016				PLB650,390
$\phi\eta$	2	19	11	3	1.2
$\phi\eta'$	0.01	2	0.1	0.02	0.4
$\text{Br}(\phi\eta)/\text{Br}(\phi\eta')$	200	9.5	110	150	3

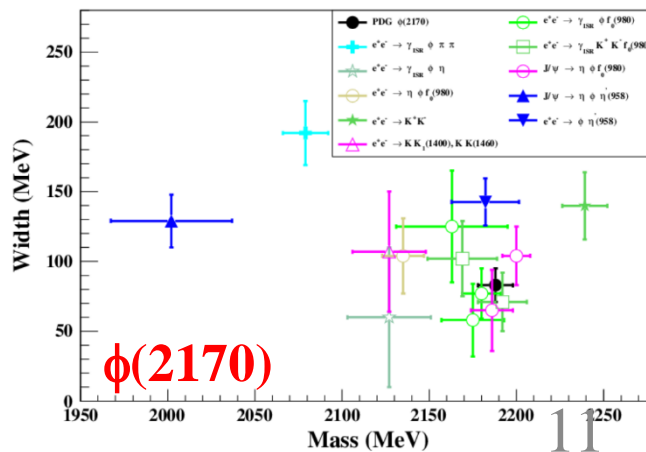
# $e^+ e^- \rightarrow \phi \eta'$

## ● BESIII: $e^+ e^- \rightarrow \phi \eta'$ with $\eta' \rightarrow \gamma \pi^+ \pi^-$



$$\frac{M_R}{\sqrt{s}} \sqrt{\frac{12\pi\Gamma_{e^+e^-}^R \mathcal{B}_{\mathcal{R}}(\phi \eta') \Gamma_{tot}^R}{s - M_R^2 + iM_R\Gamma_{tot}^R}} \cdot \sqrt{\frac{\Phi(\sqrt{s})}{\Phi(M_R)}}$$

## ● $\phi(2170)$ @ $\phi \eta'$ ?



# $\phi\eta$ and $\phi\eta'$

- $e^+ e^- \rightarrow \phi\eta$  and  $\phi\eta'$ 
  - ✓ **BarBar  $\phi\eta$ :  $1.7 \pm 0.7 \pm 1.3 \text{eV}$**

$$\frac{Br[\phi(2170) \rightarrow \phi\eta] \Gamma_{ee}}{Br[\phi(2170) \rightarrow \phi\eta'] \Gamma_{ee}} = \mathbf{0.23 \pm 0.11}$$

- **If we observed  $\phi(2150)$  in  $e^+ e^- \rightarrow \phi\eta'$ ,  $\phi(2150)$  as an  $1^- s\bar{s}g$  ?**

$1^- s\bar{s}g$	alt	2.2GeV	standard	IKP	Ding
	PRD59, 034016				PLB650,390
$\phi\eta$	2	19	11	3	1.2
$\phi\eta'$	0.01	2	0.1	0.02	0.4
$Br(\phi\eta)/Br(\phi\eta')$	200	9.5	110	150	3

# $\eta$ - $\eta'$ mixing

- SU(3) quark model, SU(3) singlet state  $\eta_0$  and octet state  $\eta_8$ ,  $\eta_q = \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})$  and  $\eta_s = s\bar{s}$ .  $\theta = -11.7^\circ$ .

$$\begin{pmatrix} \eta \\ \eta' \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \eta_8 \\ \eta_0 \end{pmatrix} \quad \begin{pmatrix} \eta_8 \\ \eta_0 \end{pmatrix} = \begin{pmatrix} \sqrt{\frac{1}{3}} & -\sqrt{\frac{2}{3}} \\ \sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} \end{pmatrix} \begin{pmatrix} \eta_q \\ \eta_s \end{pmatrix}$$

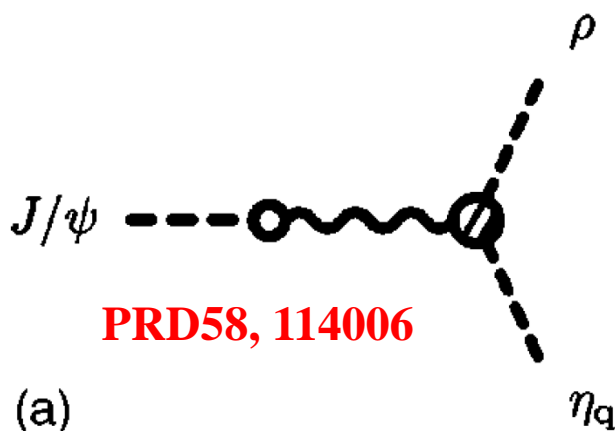
- Resonances decay

$$\frac{\Gamma[J/\psi \rightarrow \eta' \rho]}{\Gamma[J/\psi \rightarrow \eta \rho]} = \tan^2 \phi \left( \frac{k_{\eta' \rho}}{k_{\eta \rho}} \right)^3$$

$$\rho\eta': (0.81 \pm 0.08) < \rho\eta: (1.93 \pm 0.23) \times 10^{-4}$$

- $\phi(2170) \rightarrow \phi\eta$  and  $\phi\eta'$ : normal ?

$$\frac{Br[\phi(2170) \rightarrow \phi\eta] \Gamma_{ee}}{Br[\phi(2170) \rightarrow \phi\eta'] \Gamma_{ee}} = \mathbf{0.23 \pm 0.11}$$



PRD58, 114006

# $e^+ e^- \rightarrow K K \pi \pi$

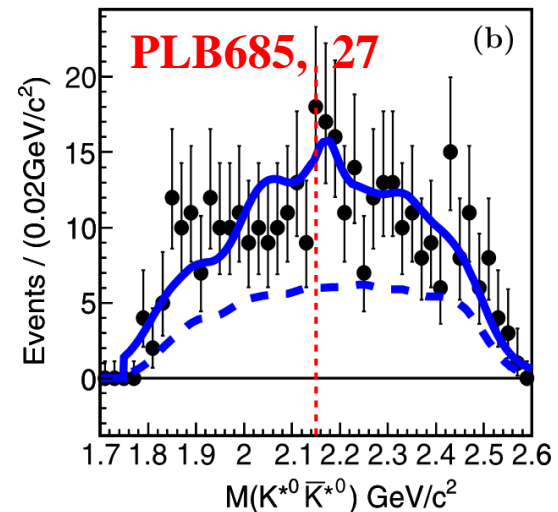
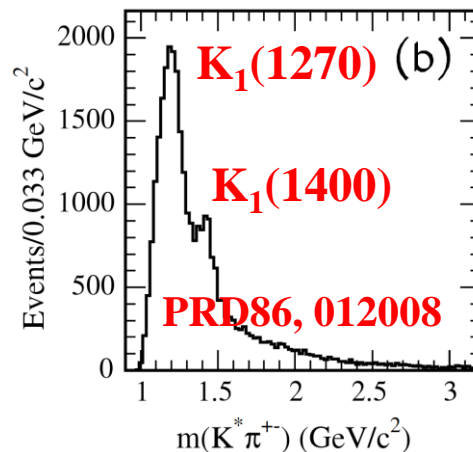
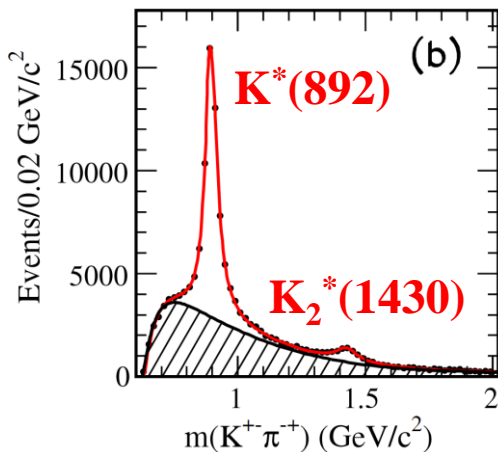
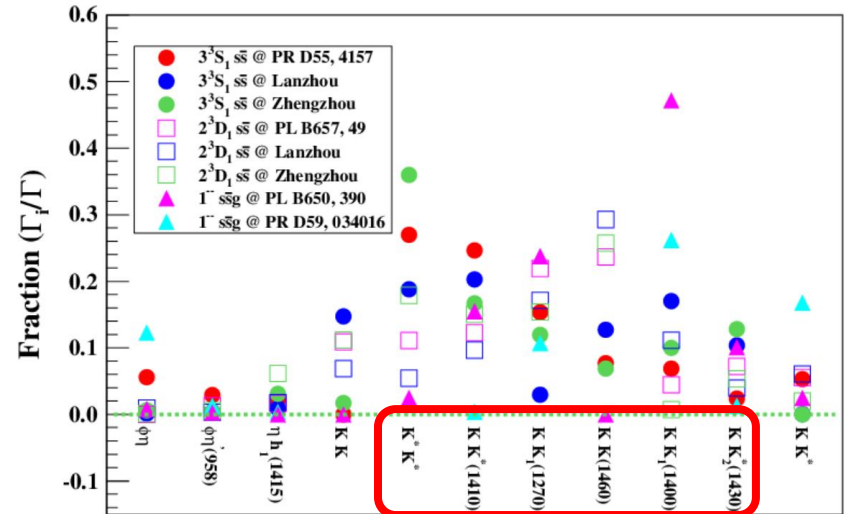
●  $e^+e^- \rightarrow KK\pi\pi$ : important to distinguish  $\phi(2170)$  theory models

- ✓  $K^*K^*$ :  $s\bar{s}g$  (unfavored),  $3^3S_1$  (favored)
- ✓  $KK_1(1400)$ :  $s\bar{s}g$  (favored)
- ✓  $KK(1460)$ :  $s\bar{s}g$  (unfavored),  $2^3D_1$  (favored)

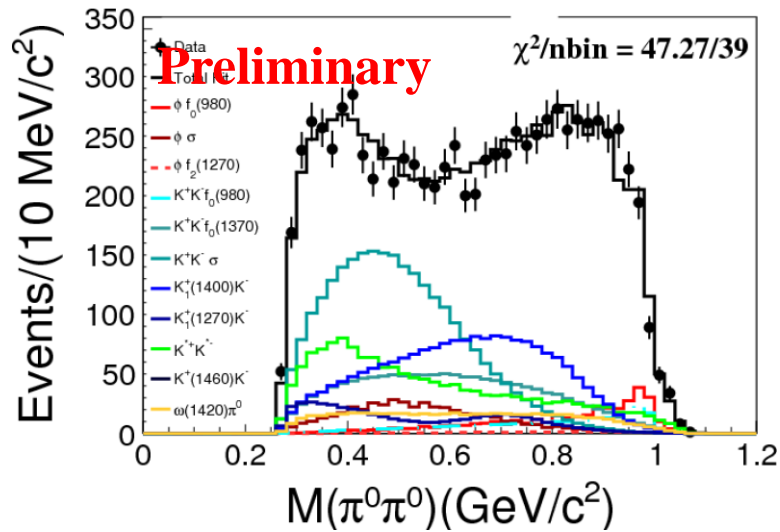
● BaBar:  $K^*(892)$ ,  $K_2^*(1430)$ ,  $K_1(1270)$  and  $K_1(1400)$

●  $J/\psi \rightarrow \eta\phi(2170) \rightarrow \eta K^*K^*$

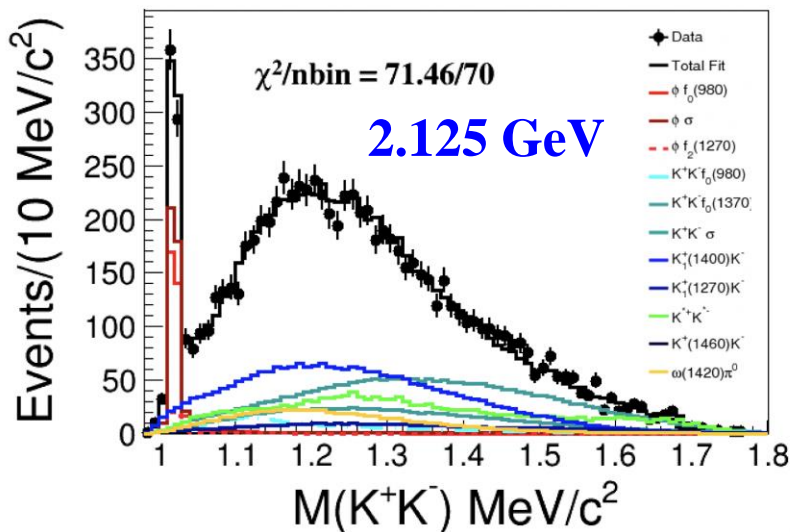
- ✓ BES: 58M  $J/\psi$ , a upper limit



$$e^+ e^- \rightarrow K^+ K^- \pi^0 \pi^0$$



process	Significance (2.1250 GeV)	Significance (2.3960 GeV)
$\phi f_0(980)$	$>8.0 \sigma$	$>8.0 \sigma$
$\phi \sigma$	$>8.0 \sigma$	–
$\phi f_2(1270)$	$5.0 \sigma$	–
$\phi f_0(1370)$	–	$6.9 \sigma$
$K^{*+}(892)K^{*-}(892)$	$>8.0 \sigma$	$>8.0 \sigma$
$K^+(1460)K^-$	$>8.0 \sigma$	$6.4 \sigma$
$K_0^{*+}(1430)K^{*-}(892)$	$>8.0 \sigma$	$7.5 \sigma$
$K_2^{*+}(1430)K^{*-}(892)$	–	$6.4 \sigma$
$K_1^+(1400)K^-$	$>8.0 \sigma$	$>8.0 \sigma$
$K_1^+(1270)K^-$	$>8.0 \sigma$	$>8.0 \sigma$
$K^{*+}(892)K^- \pi^0$	–	$5.4 \sigma$
$K^+ K^- f_0(980)$	$6.2 \sigma$	$>8.0 \sigma$
$K^+ K^- \sigma$	$>8.0 \sigma$	$>8.0 \sigma$
$K^+ K^- f_0(1370)$	$>8.0 \sigma$	$7.4 \sigma$
$\omega(1420)\pi^0$	$>8.0 \sigma$	$5.2 \sigma$



- A PWA for multi-energy points @ [2.0, 2.644]GeV
- There is **no significant signal of  $e^+e^- \rightarrow KK^*(1410)$** .
- Extract Born cross section of intermediate states.

# $e^+ e^- \rightarrow K^+ K^- \pi^0 \pi^0$

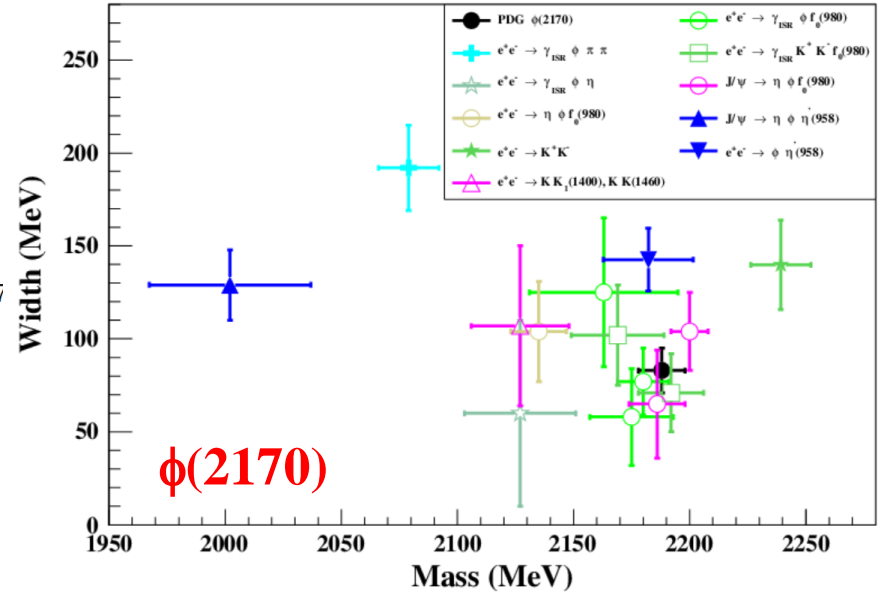
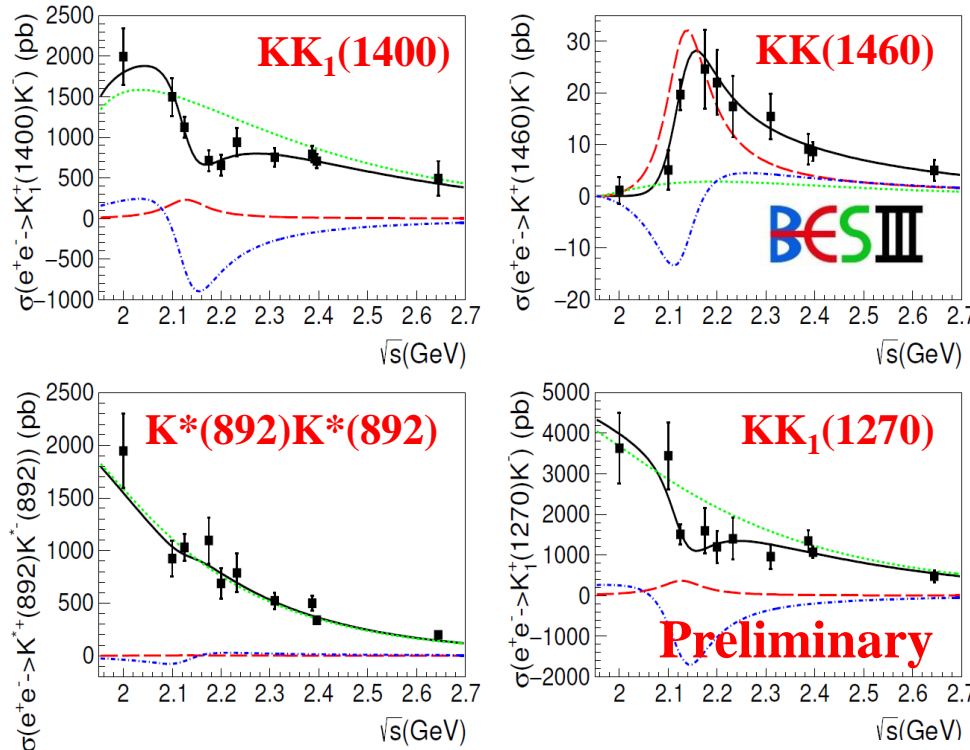


Table 22: Fitting parameters.

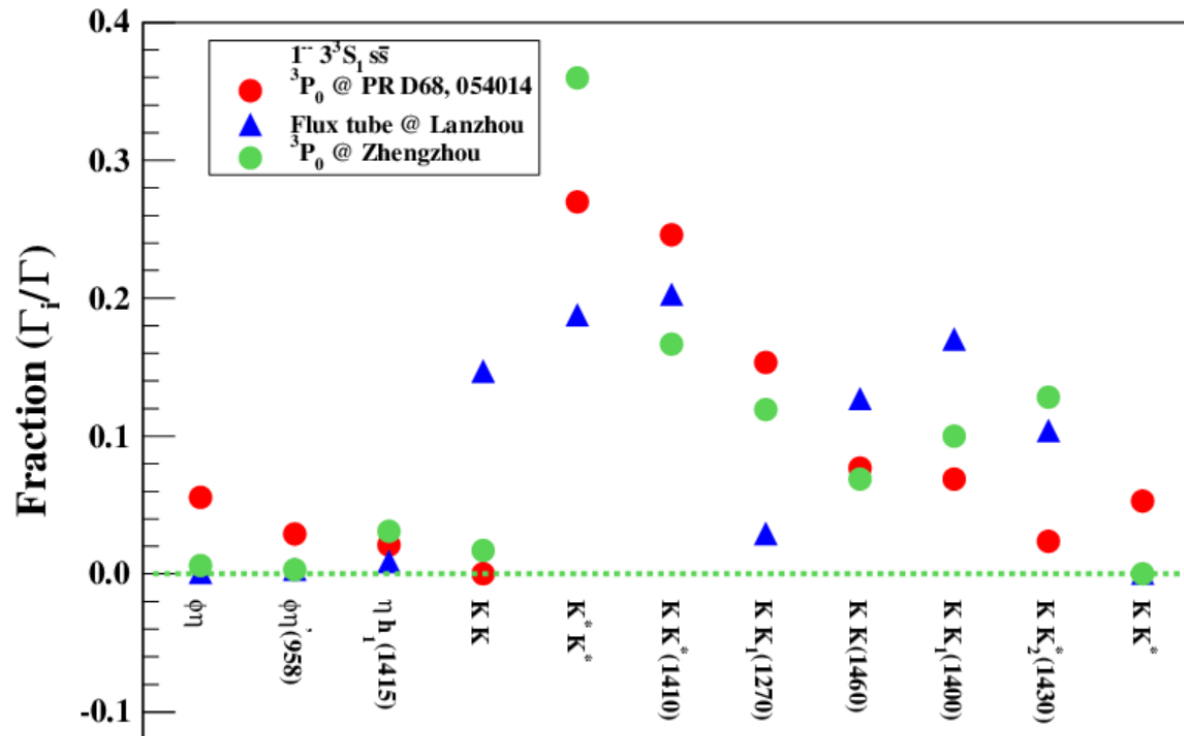
channel	$e^+e^- \rightarrow K_1^+(1400)K^-$	$e^+e^- \rightarrow K^+(1460)K^-$	$e^+e^- \rightarrow K_1^+(1270)K^-$	$e^+e^- \rightarrow K^{*+}K^{*-}$
Mass (MeV/c <sup>2</sup> )	2126.5 ± 16.8			
Width (MeV)	106.9 ± 32.1			
	Solution1	Solution2	Solution1	Solution2
$\mathcal{B}_R \Gamma^{e^+e^-}$ (eV)	7.6 ± 3.7	152.6 ± 14.2	4.7 ± 3.3	98.8 ± 7.8
$\phi$ (rad)	3.7 ± 0.4	4.5 ± 0.3	4.0 ± 0.2	4.5 ± 0.1
Significance( $\sigma$ )	4.8		1.4	
			1.2	

- ✓ Dots: BESIII data
- ✓ Black curves: fit results
- ✓ Red long-dashed:  $\phi(2170)$
- ✓ Green shot-dashed:  $1/s^n$
- ✓ Blue dash-dotted: interference

●  $\phi(2170) \rightarrow K K_1(1400)$  and  $K K(1460)$ : **Yes ?**



# $1^- 3^3S_1 s\bar{s}$



- Fraction  $\Gamma_i/\Gamma$ : weakly model & input parameters dependent
- Dominant decay modes:  **$KK^*(1410)$  &  $K^*K^*$**
- **$KK$ : sharp distinction ?**

# $\phi(2170)$ as pure $3^3S_1 s\bar{s}$

Decay modes	$3^3S_1 s\bar{s}$	
	$^3P_0$ model	Lanzhou
KK	0	35.8
$K^*K^*$	102	45.7
KK(1460)	29	30.9
$KK^*(1410)$	93	49.3
$KK_1(1270)$	58	7.1
$KK_1(1400)$	26	41.4
$KK_2^*(1430)$	9.0	25.2
$\phi\eta$	21	0.3
$\phi\eta'$	11	0.8

- Reduction to Absurdity
  - ✓  $3^3S_1 s\bar{s}$ :  $\Gamma_{K^*K^*} > \Gamma_{KK_1(1400)}$
  - ✓ Exp.  $\phi(2170)$  @  $KK_1(1400)$
  - ✓ Exp. no  $\phi(2170)$  @  $K^*K^*$
  - ✓ Exp. similar  $\epsilon_{\text{eff}}$
  - ✓  $\phi(2170)$  as pure  $3^3S_1 s\bar{s}$  ???
- Similar check for several modes
  - ✓  $KK^*(1410)$ : No  $\phi(2170)$
  - ✓  $KK(1460)$ : Yes  $\phi(2170)$
- $\phi(2170)$  as pure  $3^3S_1 s\bar{s}$ : ???

# $1^- s\bar{s}g$

Decay modes	$1^- s\bar{s}g$				$\phi(2170)$
	Ding	IKP	standard	2.2GeV	BESIII
KK	0				NO
$K^*K^*$	0				NO
KK(1460)	0				Yes
$KK^*(1410)$	23	9	11	55	NO
$KK_1(1270)$	35.3	26	18.1	16.6	?
$KK_1(1400)$	70.1	63.7	32.04	40.6	Yes
$KK_2^*(1430)$	15.0	2	0.07	2	Not yet
$\phi\eta$	1.2	3	11	19	Not yet
$\phi\eta'$	0.4	0.02	0.1	2	Yes

- No  $\phi(2170)$  at  $KK^*(1410)$
- Yes  $\phi(2170)$  at  $KK(1460)$  line-shape
- Small  $\Gamma(\phi\eta)/\Gamma(\phi\eta')$  at BESIII

# Summary and outlook

- Compared with  $c\bar{c}$  and  $b\bar{b}$ ,  $s\bar{s}$  is a terra incognita
- Aspects of  $\phi(2170)$  are still not fully understood
- Using BESIII R scan data, we are extensively studying  $\phi(2170)$ 
  - ✓  $\phi(2170)$  as pure  $3^3S_1 s\bar{s}$ : ???
  - ✓  $\phi(2170)$  as pure  $2^3D_1 s\bar{s}$ : ???
  - ✓  $\phi(2170)$  as molecular state  $\Lambda\bar{\Lambda}$ : ???
  - ✓  $\phi(2170)$  as three body system  $\phi KK$ : ???
  - ✓  $\phi(2170)$  as  $1^- s\bar{s}g$  hybrid: ???
  - ✓  $\phi(2170)$  as tetraquark: ???
  - ✓  $\phi(2170)$  as mixing state: ???
- Theorists revisited  $\phi(2170)$  decay again, please

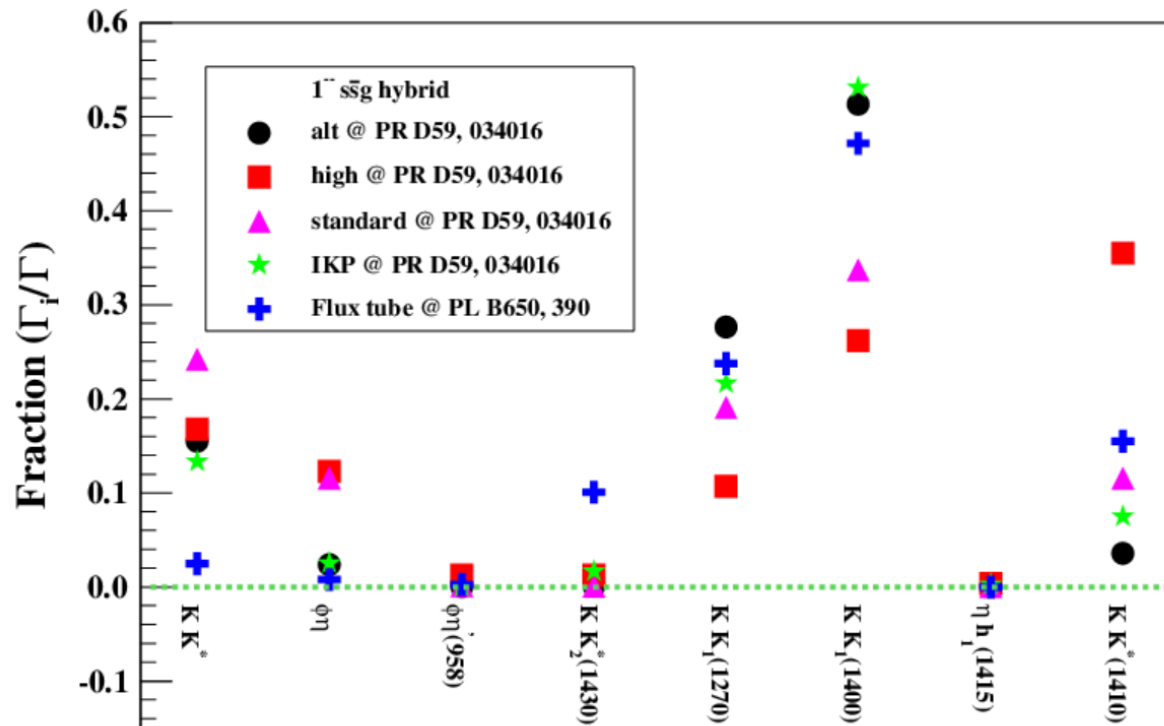


# $1^- s\bar{s}g$ hybrid

$1^- s\bar{s}g$	alt	2.2GeV	standard	IKP	Ding
	PRD59, 034016				PLB650,390
$K^*K$	13	26	<b>23</b>	16	3.7
$\phi\eta$	2	19	11	3	1.2
$\phi\eta'$	0.01	2	0.1	0.02	0.4
$KK_2^*(1430)$	0.1	2	0.07	2	15
$KK_1(1270)$	<b>23.2</b>	16.6	18.1	<b>26</b>	<b>35.3</b>
$KK_1(1400)$	<b>43.1</b>	<b>40.6</b>	<b>32.04</b>	<b>63.7</b>	<b>70.1</b>
$h_1(1415)\eta$	0.07	0.6	0.04	0.3	0
$KK^*(1410)$	3	<b>55</b>	11	9	23
Width(MeV)	<b>84</b>	<b>155</b>	<b>95</b>	<b>120</b>	<b>148.7</b>

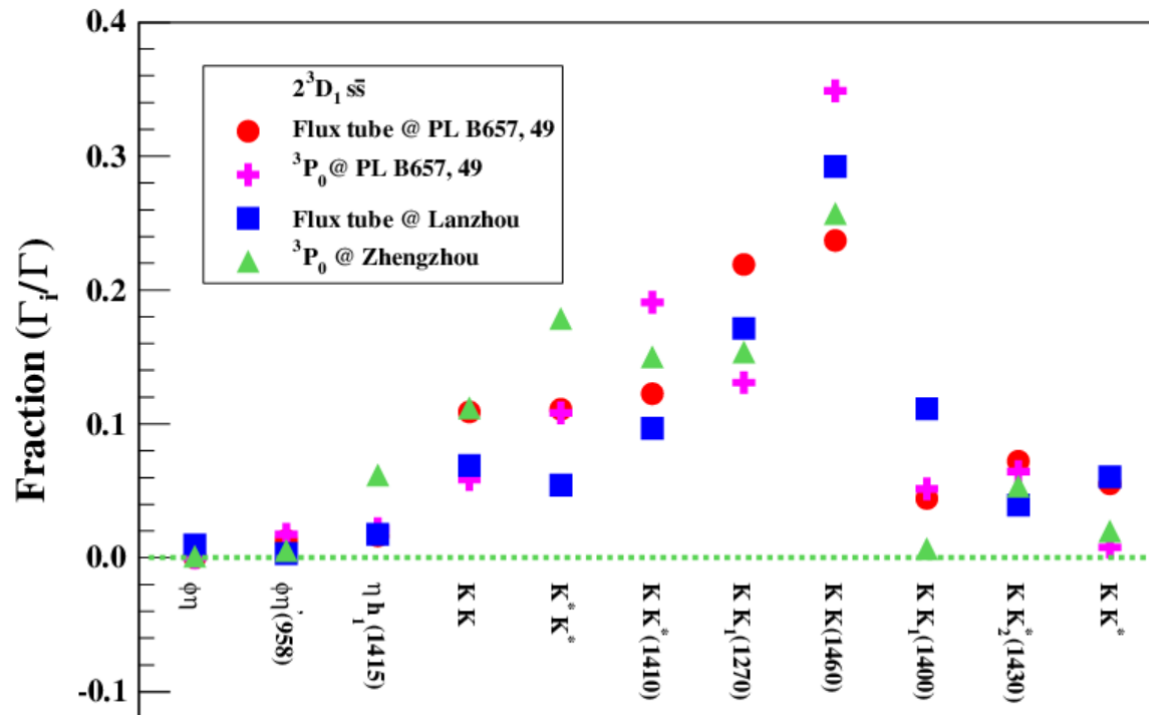
- Theory prediction: model & input parameters dependent

# $1^-$ $s\bar{s}g$ hybrid



- Fraction  $\Gamma_i/\Gamma$ : weakly model & input parameters dependent
- Dominant decay modes:  **$KK_1(1400)$  &  $KK_1(1270)$**

# $1-2^3D_1 s\bar{s}$



- Fraction  $\Gamma_i/\Gamma$ : weakly model & input parameters dependent
- Dominant decay modes: **KK(1460) &  $KK_1(1270)$**

# $\phi(2170): 2^3D_1 s\bar{s}$

Decay modes	$2^3D_1 s\bar{s}$			$\phi(2170)$
	$^3P_0$ model	Flux tube	Lanzhou	BESIII
KK	9.8	23.1	40.8	NO
$K^*K^*$	18.11	23.5	32.2	NO
$KK(1460)$	58.3	50.2	173.5	YES
$KK^*(1410)$	31.9	26.0	57.3	NO
$KK_1(1270)$	21.9	46.4	101.5	?
$KK_1(1400)$	8.6	9.4	65.9	Yes
$KK_2^*(1430)$	10.8	15.3	23.3	Not yet
$\phi\eta$	0	0	5.7	Not yet
$\phi\eta'$	2.9	2.8	1.8	Yes

- No  $\phi(2170)$  at  $KK$ ,  $K^*K^*$  and  $KK_1(1270)$  line-shape
- Yes  $\phi(2170)$  at  $KK_1(1400)$



# $\phi(2170)$ @ $\phi f_0(980)$

$\phi f_0(980)$	Mass (MeV)	Width (MeV)	Events
BaBar (2006)	$2175 \pm 10 \pm 15$	$58 \pm 16 \pm 20$	271
BES (2008)	$2186 \pm 10 \pm 6$	$65 \pm 23 \pm 17$	52
Belle (2009)	$2163 \pm 32$	$125 \pm 40$	4.8K
BaBar (2012)	$2172 \pm 10 \pm 8$	$96 \pm 19 \pm 12$	
BESIII (2015)	$2200 \pm 6 \pm 5$	$104 \pm 15 \pm 15$	471
BESIII (2019)	$2135 \pm 8 \pm 9$	$104 \pm 24 \pm 12$	95
PDG2018	$2188 \pm 10$	$83 \pm 12$	

- $\phi(2170)$  @ PDG2019: NO PDG estimated value