

Some remarks on Y(4260)

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中国物理学会

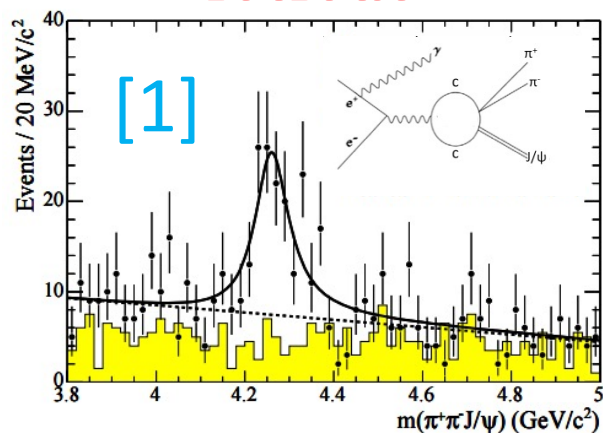
Chinese Physical Society

中国物理学会高能物理分会第十三届全国粒子物理学术会议

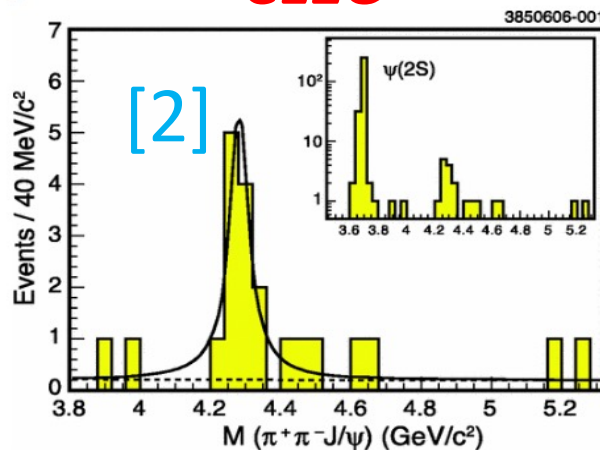
August 16 - 20, 2021

Discovery of $Y(4260)$ in $e^+e^- \rightarrow \gamma_{ISR} \pi^+ \pi^- J/\psi$

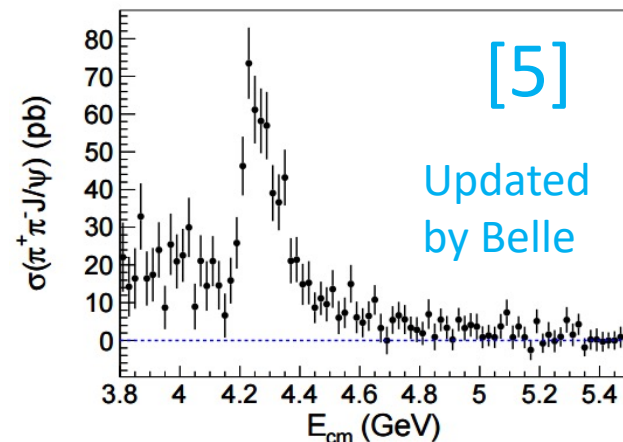
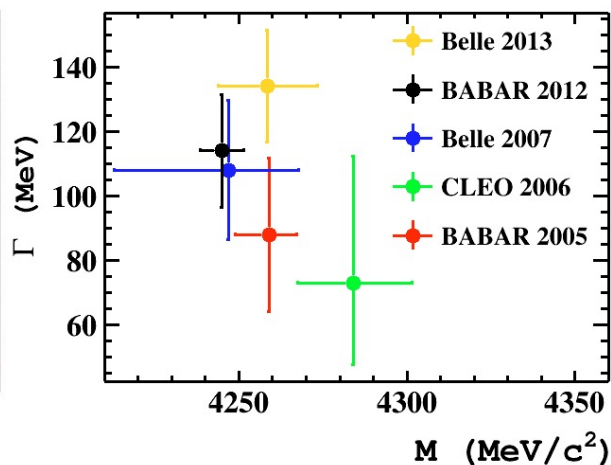
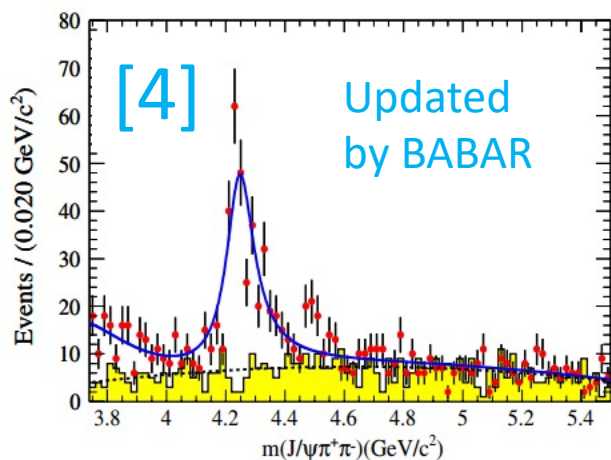
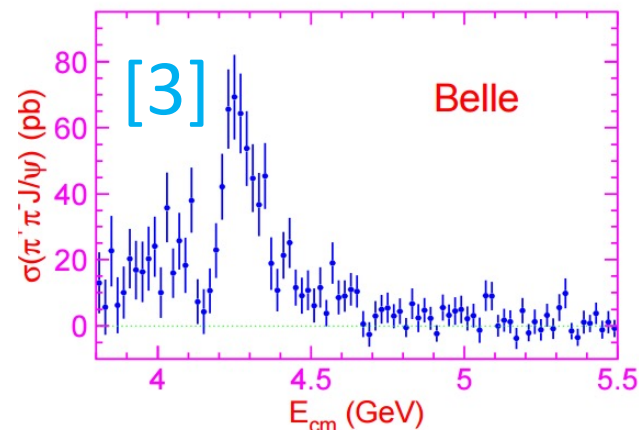
BABAR



CLEO



Belle



[1] PRL 95, 142001 (2005).

[2] PRD 74, 091104(R) (2006).

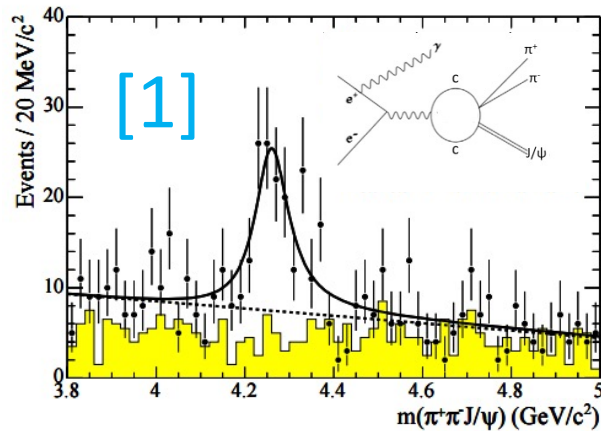
[3] PRL 99, 182004 (2007).

[4] PRD 86, 051102(R) (2012).

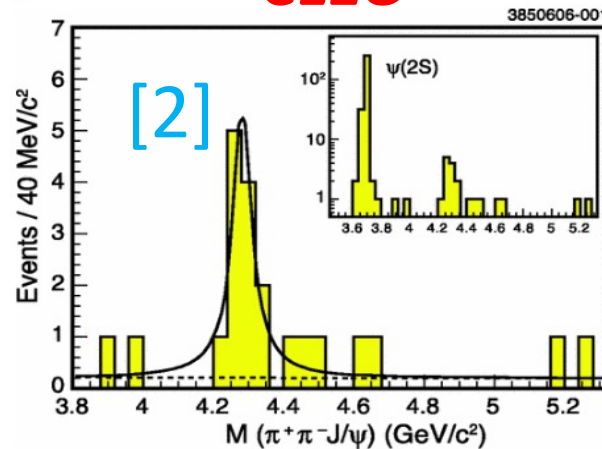
[5] PRL 110, 252002 (2013).

Discovery of $Y(4260) \rightarrow \pi^+ \pi^- J/\psi$

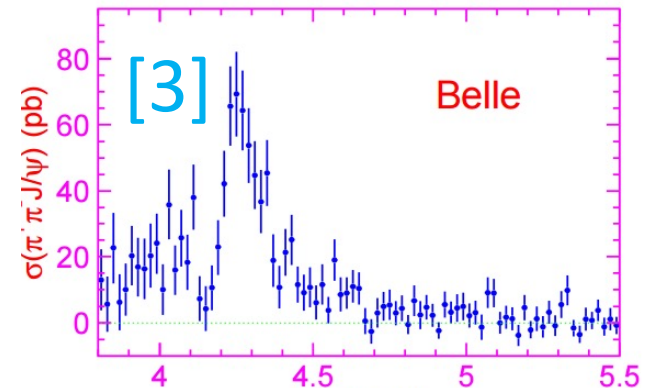
BABAR



CLEO

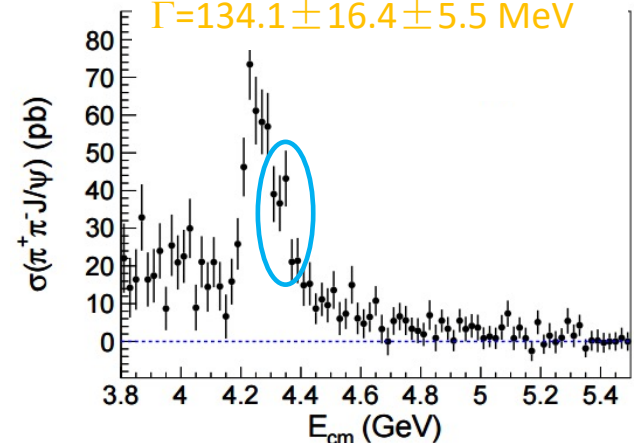
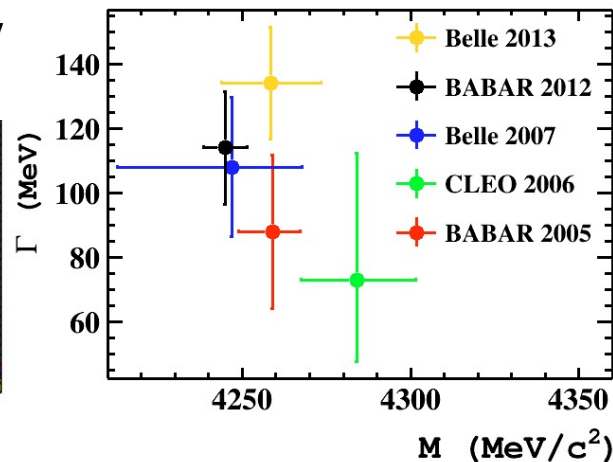
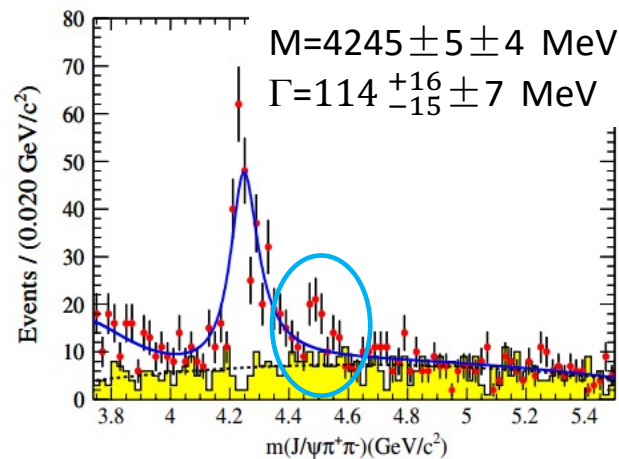


Belle



$$M = 4258.6 \pm 8.3 \pm 12.1 \text{ MeV}$$

$$\Gamma = 134.1 \pm 16.4 \pm 5.5 \text{ MeV}$$



■ Average [PDG 2014] : $M = 4251 \pm 9 \text{ MeV}$, $\Gamma = 120 \pm 12 \text{ MeV}$

■ There seem a few bumps in the updated BABAR and Belle data ! Improved measurements are needed.

Intriguing $Y(4260)$

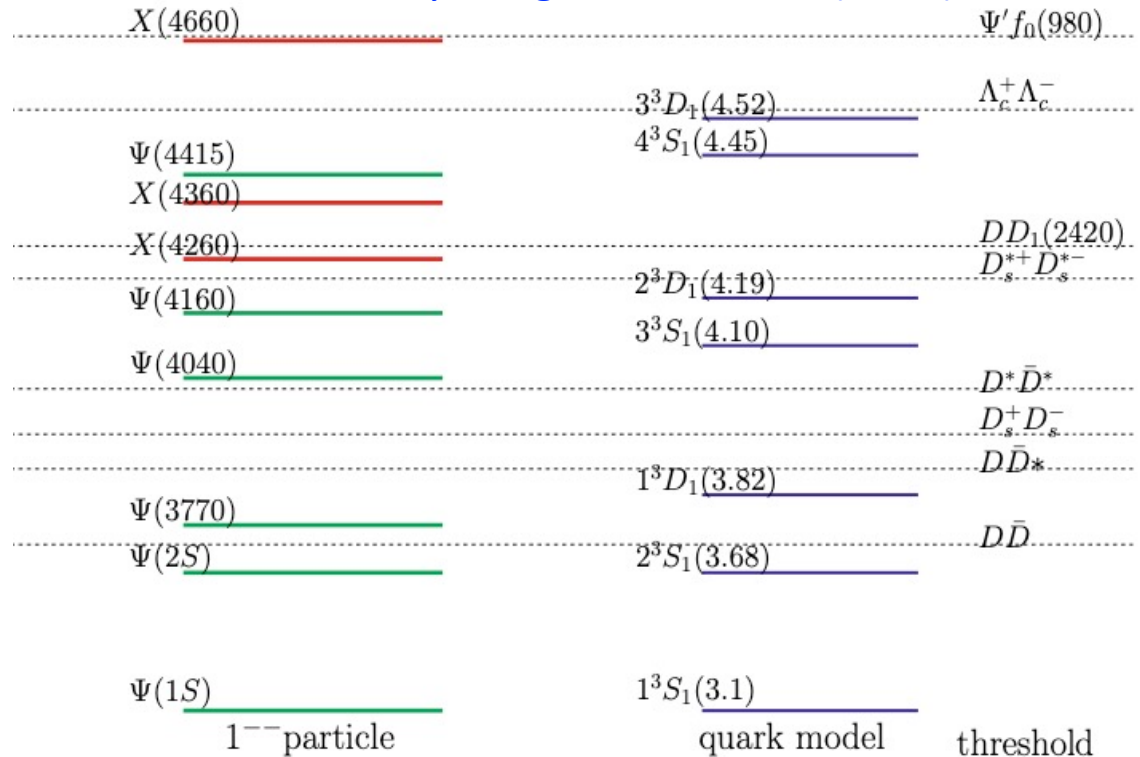
Have attracted considerable attention!

 Mass

- Such 1^{--} states expected up to 4.4 GeV are generally well-established $1S$, $2S$, $1D$, $3S$, $2D$ and $4S$.

- No enough unassigned vector states for $Y(4260)$ in charmonium spectrum

Godfrey & Isgur, PRD32,189(1985)



Green: predicted and discovered

Red: unpredicted but discovered

Intriguing $Y(4260)$

 Mass

 OZI rule

- No open charm process is significantly observed (before 2017).
- If taking $Y(4260)$ as a charmonium state, it violates OZI rule.

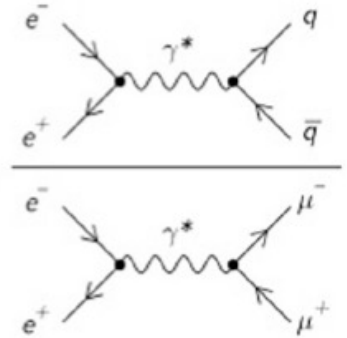
Intriguing Y(4260)

X Mass

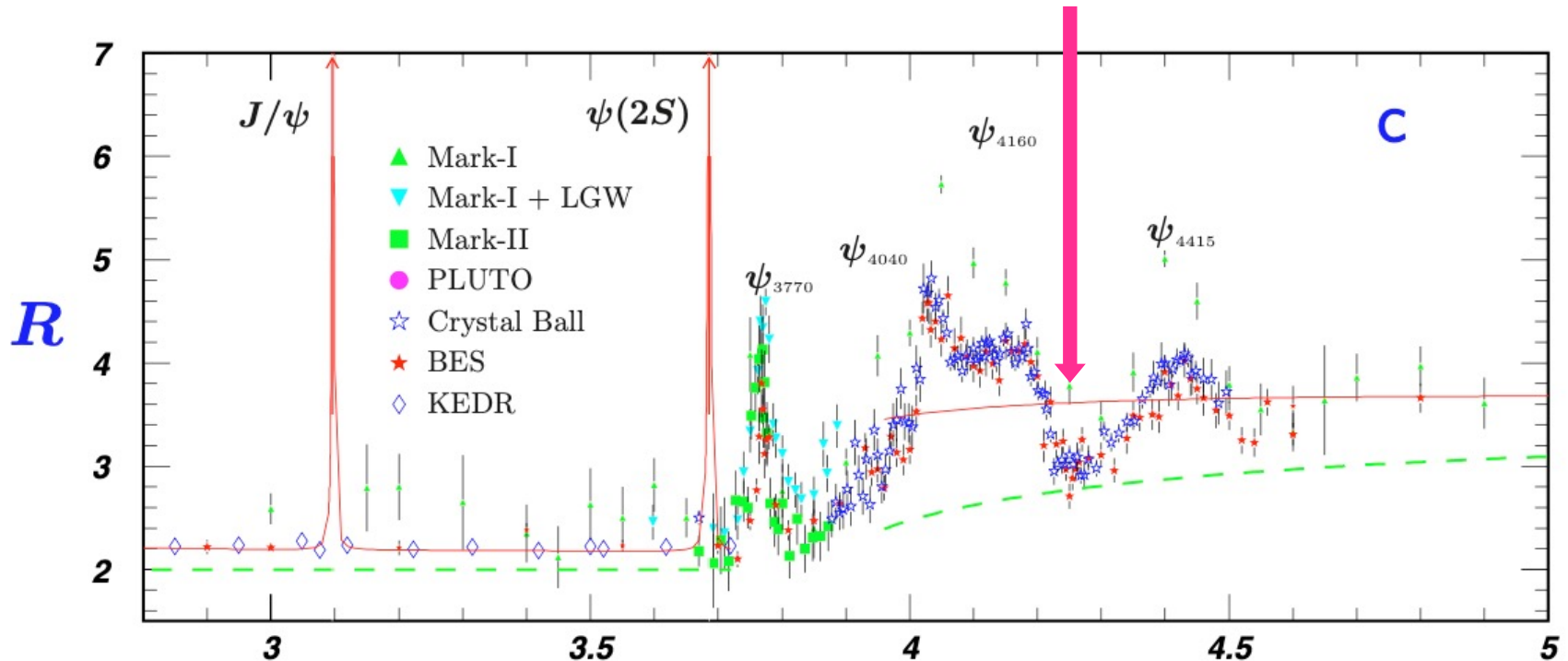
X OZI rule

X Non in R scan

$$R = \frac{\sigma(e^-e^+ \rightarrow \text{hadrons})}{\sigma(e^-e^+ \rightarrow \mu^-\mu^+)} \approx$$



● No obvious peak around 4.26 GeV in the R distribution is discovered.



Intriguing Y(4260)

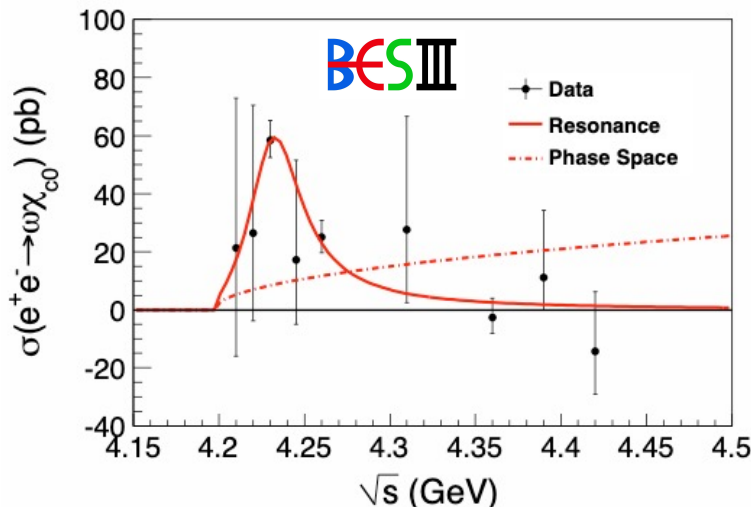
✗ Mass

✗ OZI rule

✗ Non in R scan

● In 2012, Ref[1] predicted that Y(4260) has a sizable coupling to $\omega\chi_{c0}$, and is taken as a $c\bar{c}$ state. Meanwhile, they gave out $\Gamma_{e^+e^-} = 23.30 \pm 3.55$ eV.

● It is as expected that BESIII observed a resonant structure ($>9\sigma$) in $M(\omega\chi_{c0})$, with mass of $4230 \pm 8 \pm 6$ MeV and width of $38 \pm 12 \pm 2$ MeV [2].



Incompatible!

Average [PDG 2014] : $M = 4251 \pm 9$ MeV,
 $\Gamma = 120 \pm 12$ MeV

[1] arXiv:1206.6911, PRD 92, 014020 (2015)

[2] PRL114, 092003 (2015)

Intriguing Y(4260)

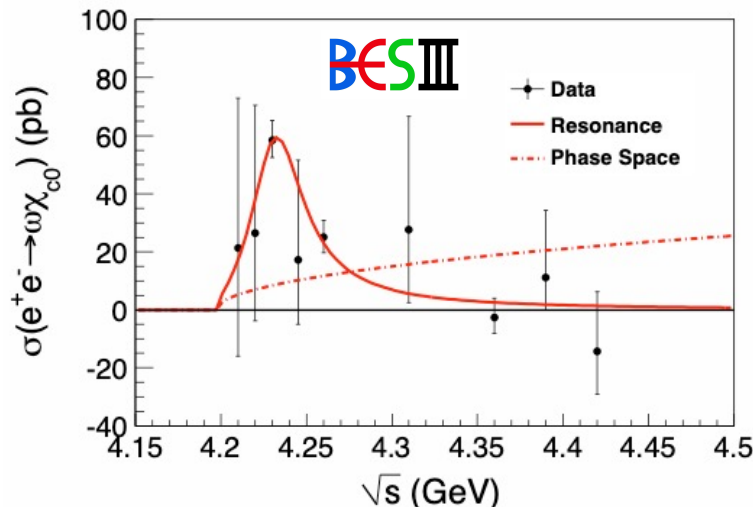
✗ Mass (and width)

✗ OZI rule

✗ Non in R scan

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Intriguing $Y(4260)$



Mass (and width)



OZI rule



Non in R scan



$\psi(4^3S_1)$

More refined potential models
has been growing !

- The screened potential model [1] recalculated the charmonium spectra. The $\psi(4^3S_1)$'s mass is reduced from ~ 4415 to 4273 MeV, which reconciles to some extent the contradiction in "mass" but doesn't explain why $Y(4260)$ in $M(\omega\chi_{c0})$ is so narrow.

In units of MeV

State	NR[2]	GI[2]	SC[1]	Exp [PDG 2014]
$\psi(3^3S_1)$	4072	4100	4022	4039 ± 1
$\psi(2^3D_1)$	4142	4194	4089	4191 ± 5
$\psi(4^3S_1)$	4406	4450	4273	4251 ± 9
$\psi(3^3D_1)$			4317	

[1] PRD 79, 094004 (2009)

[2] PRD 72, 054026 (2005)

NR: nonrelativistic potential model, GI: Godfrey-Isgur model, SC: screened potential model.

Intriguing Y(4260)

? Mass (and width)

✗ OZI rule

✗ Non in R scan

✗ Leptonic width

- The screened potential model [1] also calculated the leptonic widths of charmonia included $\psi(4^3S_1)$ state.

- However, Ref[2] gave out $\Gamma_{e^+e^-}[Y(4260)] = 23.30 \pm 3.55 \text{ eV}$, in which the coupling $Y(4260) \rightarrow \omega\chi_{c0}$ has been successfully predicted, and they also take Y(4260) as a $c\bar{c}$ state.

state	Γ_{ee}^0	Γ_{ee}	$\Gamma_{ee}^{\text{expt}}$
$1^3S_1(3097)$	11.8	6.60	$5.55 \pm 0.14 \pm 0.02$
$2^3S_1(3686)$	4.29	2.40	2.33 ± 0.07
$3^3S_1(4039)$	2.53	1.42	0.86 ± 0.07
$4^3S_1(4263)$	1.73	0.97	
$5^3S_1(4421)$	1.25	0.70	0.58 ± 0.07
$6^3S_1(4664)$	0.88	0.49	
$1^3D_1(3775)$	0.055	0.031	0.259 ± 0.016
$2^3D_1(4153)$	0.066	0.037	0.83 ± 0.07
$3^3D_1(4361)$	0.079	0.044	

[1] PRD 79, 094004 (2009)
[2] PRD 92, 014020 (2015),
arXiv:1206.6911

Γ_{ee}^0 and Γ_{ee} are without and with QCD corrections, respectively (in unit of keV).

Intriguing $Y(4260)$

? Mass (and width)

✗ OZI rule

✗ Non in R scan

✗ Leptonic width

- The more refined relativistic potential model [1] also calculated the leptonic widths of charmonia included $\psi(4^3S_1)$ state.

- However, Ref[2] gave out $\Gamma_{e^+e^-}[Y(4260)] = 23.30 \pm 3.55 \text{ eV}$, in which the coupling $Y(4260) \rightarrow \omega\chi_{c0}$ has been successfully predicted, and they also take $Y(4260)$ as a $c\bar{c}$ state.

$\Gamma_{e\bar{e}}$ (keV)	Pert	Nonpert
$\psi(1S)$	4.28	1.89
$\psi(2S)$	2.25	1.04
$\psi(3S)$	1.66	0.77
$\psi(4S)$	1.33	0.65
$\psi(1D)$	0.09	0.23
$\psi(2D)$	0.16	0.45

[1] PRD 75, 074031 (2007)

[2] PRD 92, 014020 (2015),
arXiv:1206.6911

Pert and NonPert are short for perturbative and Non-perturbative, respectively.

Theoretical interpretations for $Y(4260) \rightarrow \pi\pi J/\psi$

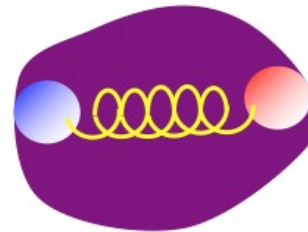
- Excited charmonium
- Compact tetraquark
- $c\bar{c}$ -gluon hybrid
- Meson-meson molecule
- Threshold effect
- et al.



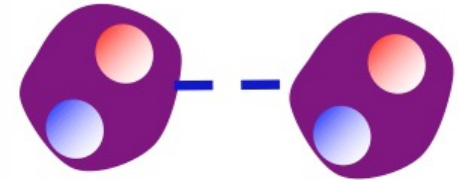
meson



tetraquark



hybrid



molecule

* Main references are moved into backup.

* These pictures come from Shuangshi Fang's talk.

Theoretical interpretations for $Y(4260) \rightarrow \pi\pi J/\psi$

- Exited $c\bar{c}$ state

 Mass	 OZI rule	 Non R scan	 $\Gamma_{e^+e^-}$
--	--	--	---

- Tetraquark

 Mass	 OZI rule	 Non R scan	 $\Gamma_{e^+e^-}$
--	--	--	---

- $c\bar{c}$ -gluon hybrid

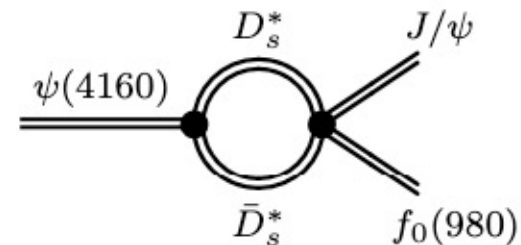
 Mass	 OZI rule	 Non R scan	 $\Gamma_{e^+e^-}$
--	--	--	---

- $D_1\bar{D}$ molecule

 Mass	 OZI rule	 Non R scan	 $\Gamma_{e^+e^-}$
--	--	--	---

- Kinematic effect Loop-driven decay [1]

It can well explain why $Y(4260)$ is not seen in OZI-allowed decays experimentally.



[1] Acta Phys. Pol. B. 51(8),1713 (2020)

* Other references are moved into backup.

Theoretical interpretations for $Y(4260) \rightarrow \pi\pi J/\psi$

● Exited $c\bar{c}$ state	? Mass	✗ OZI rule	✗ Non R scan	✗ $\Gamma_{e^+e^-}$
● Tetraquark	? Mass	✓ OZI rule	✗ Non R scan	? $\Gamma_{e^+e^-}$
● $c\bar{c}$ -gluon hybrid	? Mass	✓ OZI rule	✗ Non R scan	? $\Gamma_{e^+e^-}$
● $D_1\bar{D}$ molecule	✓ Mass	✓ OZI rule	✗ Non R scan	? $\Gamma_{e^+e^-}$
● Kinematic effect	✓ Mass	✓ OZI rule	✓ Non R scan	
● et al.				



- All of resonant interpretations for $Y(4260)$ is failed in R-scan distribution, instead, the interpretation of non-resonance enhancement can match the experiments (before 2017). **Is that the truth ?**

* Main references are moved into backup.

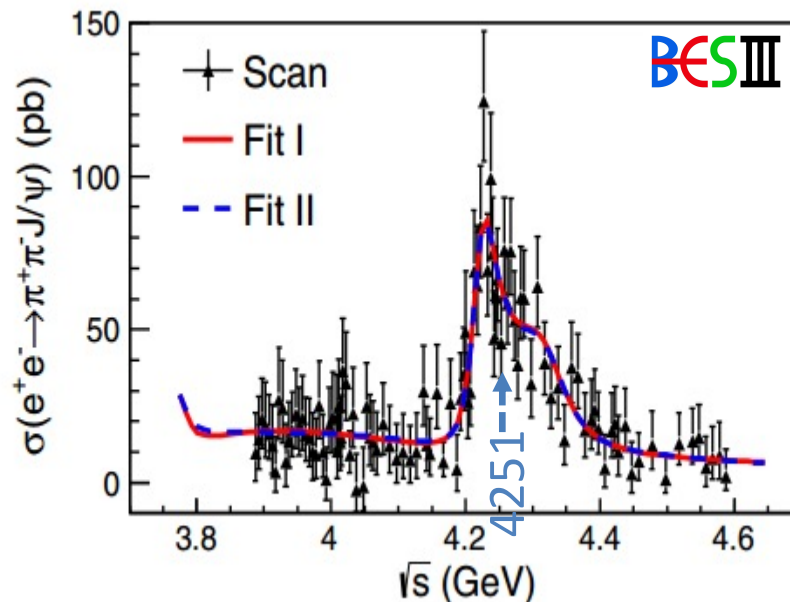
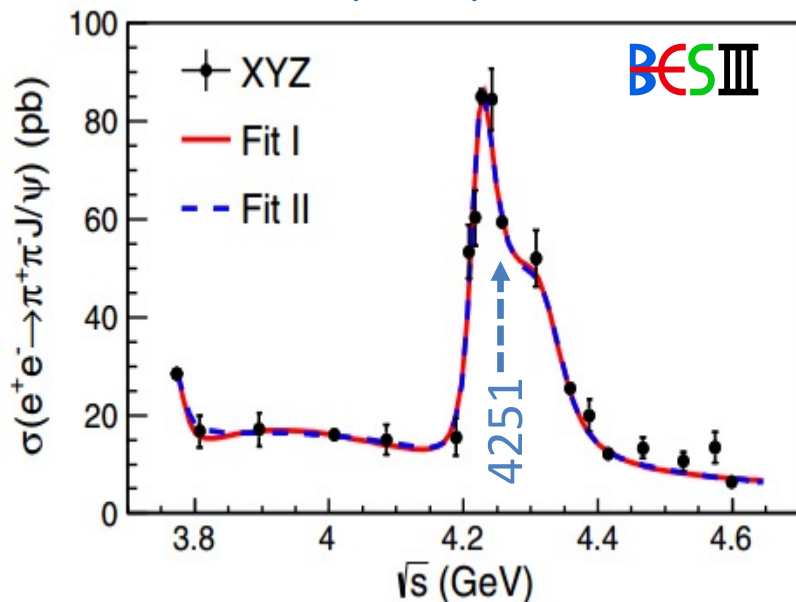
November revolution for $Y(4260)$?

2017

- In spring of 2017, BESIII published a **precise** measurement of $e^+e^- \rightarrow \pi^+\pi^-J/\psi$ cross sections at c.m. energies from 3.77 to 4.60 GeV using data samples with an integrated luminosity of 9 fb^{-1} .
- The **mass and width** of lower state, called $Y(4220)$, are well consistent with those observed in $M(\omega\chi_{c0})$.

$$Y(4260) = Y(4220) + Y(4320)$$

PRL 118, 092001 (2017)

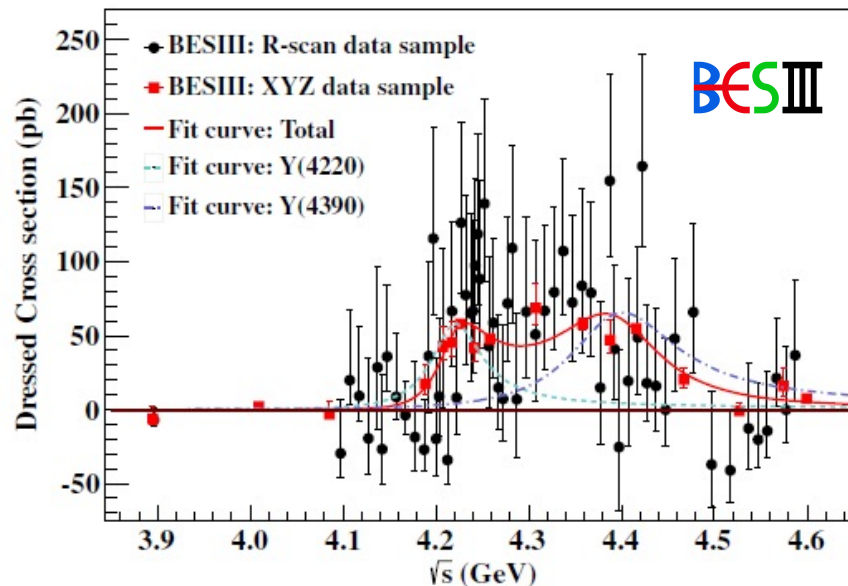


$$M = (4222.0 \pm 3.1 \pm 1.4) \text{ MeV}, \Gamma = (44.1 \pm 4.3 \pm 2.0) \text{ MeV}$$

November revolution for $Y(4260)$?

2017

- In spring of 2017, BESIII also published a **updated** measurement of $e^+e^- \rightarrow \pi^+\pi^-h_c$ cross sections at c.m. energies with improved significance with two resonant structures.
- The **mass and width** of the lower state are well consistent with those observed in $M(\omega\chi_{c0})$.



$Y(4220) + Y(4390)$

PRL 118, 092002 (2017)

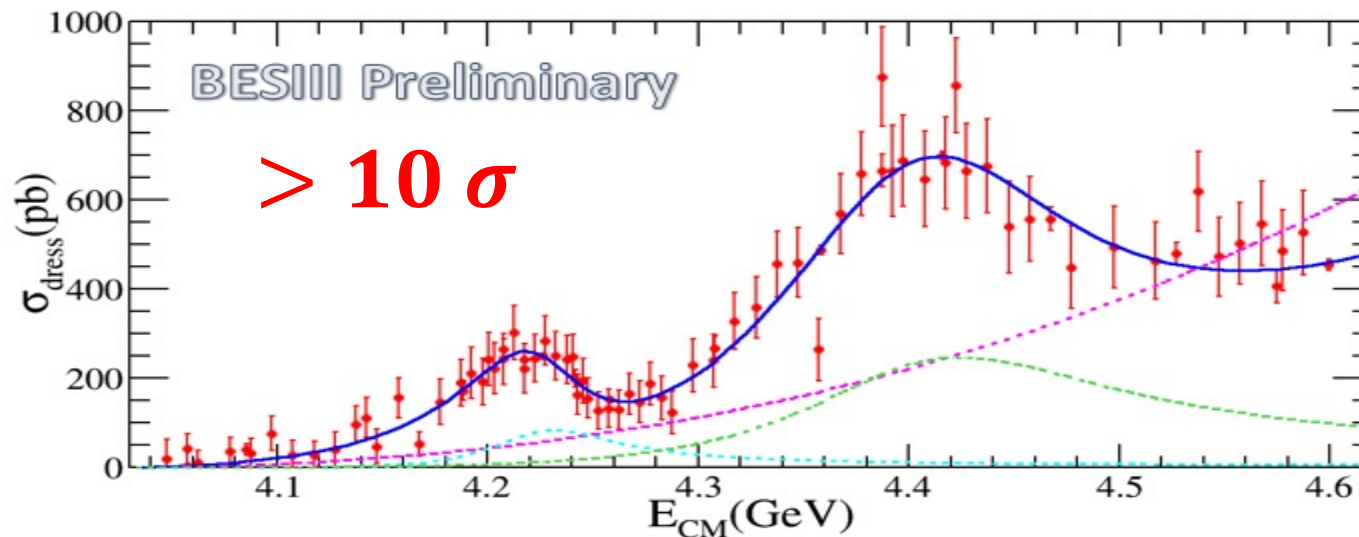
$$M = (4218.4_{-4.5}^{+5.5} \pm 0.9) \text{ MeV}, \Gamma = (66.0_{-8.3}^{+12.3} \pm 0.4) \text{ MeV}$$

November revolution for $Y(4260)$?

2017

- What's more, the first open charm decays of $Y(4260)$ is found !
- In 10th workshop of the France China Particle Physics Laboratory in spring of 2017, BESIII announced the heavy news. The results published afterwards in PRL 122, 102002 (2019)
- The **mass and width** of the lower state are well consistent with those observed in $M(\omega\chi_{c0})$.

$$e^+e^- \rightarrow \pi^+ D^0 D^{*-}$$



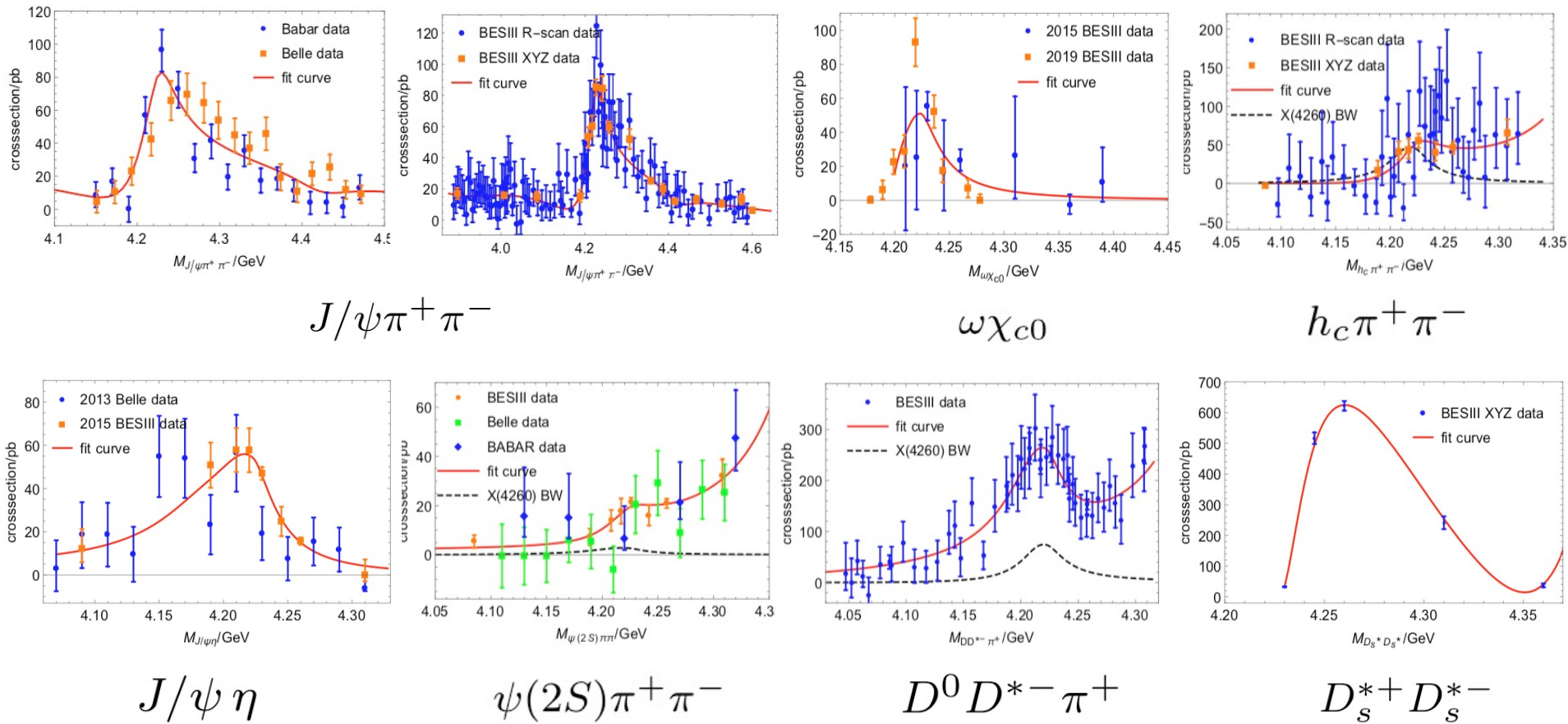
$$M = (4228.6 \pm 4.1 \pm 6.3) \text{ MeV}, \Gamma = (77.0 \pm 6.8 \pm 6.3) \text{ MeV}$$

November revolution for $Y(4260)$?

2017

- Since the narrow $Y(4220)$ and the broad $Y(4260)$ observed in the same process, i.e. $e^+e^- \rightarrow (\gamma_{ISR})\pi^+\pi^-J/\psi$, all of experiments should see the same scenario. It is reasonable to infer that the broad $Y(4260)$ observed by BABAR, Belle, and CLEO is the combination of $Y(4220)$ and $Y(43xx)$.
- Perhaps for historical reasons, the new $Y(4220)$ with lower mass and narrower width is also called $Y(4260)$. Therefore, the label “ $Y(4260)$ ” indicated the narrow $Y(4220)$ in the following slides.
- In recent years, BESIII observed and/or searched for a number of $Y(4260)$ decays, which is crucial to probe the nature of $Y(4260)$. Because of this, Stephen & Tomasz & Daria called BESIII as “ $Y(4260)$ factory” [Rev.Mod.Phys. 90 (2018)1, 015003].

Observation of main Y(4260) decays



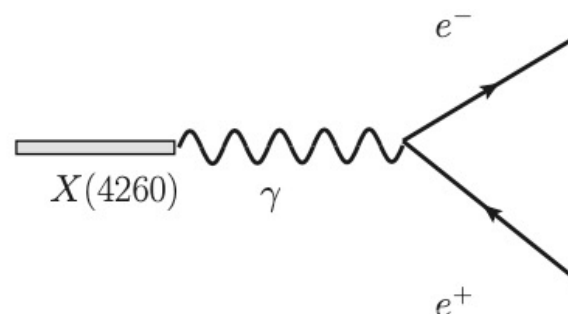
$\sigma(e^+e^- \rightarrow \text{final states}) > 10 \text{ pb}^{-1}$ (up to 2020)

* Figures are from EPJC81(2021)83, and the reference for each measurement can also be seen in EPJC81(2021)83.

On leptonic width of $X(4260)$

- The leptonic decay width

$$\mathcal{L}_{\gamma X} = \frac{g_0}{M_X} X_{\mu\nu} F^{\mu\nu} \implies \Gamma_{e^+e^-} = \frac{4\alpha}{3} \frac{g_0^2}{M_X}$$



- The cross section for each decay

$$\sigma_{e^+e^- \rightarrow X(4260) \rightarrow f} = \frac{3\pi}{k^2} \frac{\sqrt{s\Gamma_{ee}\Gamma_f}}{s - M_X^2 + i\sqrt{s}\Gamma_{tot}(s)} + \sum_i \frac{c_i e^{i\phi_i}}{s - M_i^2 + i\sqrt{s}\Gamma_i} + \tilde{c}^2$$

$X(4260) \rightarrow f$

Bkg for $\psi \rightarrow f$

Non-Resonance bkg

On leptonic width of $X(4260)$

● The propagator of $X(4260) \rightarrow f$

$$\frac{1}{D_X(s)} = \frac{1}{s - M_X^2 + i\sqrt{s}\Gamma_{tot}(s)}$$

$$\Gamma_{tot}(s) = \Gamma_{J/\psi\pi\pi}(s) + \Gamma_{h_c\pi\pi}(s) + \Gamma_{D\bar{D}^*\pi}(s) + \Gamma_{\psi(2S)\pi\pi}(s) + \Gamma_{\omega\chi_{c0}}(s) \\
+ \Gamma_{J/\psi\eta}(s) + \Gamma_{D_s^*\bar{D}_s^*}(s) + \Gamma_{D\bar{D}}(s) + \Gamma_{D\bar{D}^*}(s) + \Gamma_{D^*\bar{D}^*}(s) + \Gamma_0$$

unknown decay width

- two body decay width

$$\Gamma_{\omega\chi_{c0}}(s) = g_{\omega\chi_{c0}} k_{\omega\chi_{c0}}, \quad \Gamma_{J/\psi\eta}(s) = g_{J/\psi\eta} k_{J/\psi\eta}^3, \quad \Gamma_{D_s^*\bar{D}_s^*}(s) = g_{D_s^*\bar{D}_s^*} k_{D_s^*\bar{D}_s^*}^3,$$

$$\Gamma_{D^+D^-}(s) = g_{D^+D^-} k_{D^+D^-}^3, \quad \Gamma_{D^+D^{*-}}(s) = g_{D^+D^{*-}} k_{D^+D^{*-}}^3,$$

$$\Gamma_{D^{*+}D^{*-}}(s) = g_{D^{*+}D^{*-}} k_{D^{*+}D^{*-}}^3.$$

Flatte parameterization

- Three-body decay width [PDG]

$$d\Gamma_f = \frac{1}{(2\pi)^5} \frac{1}{16M_X^2} |\mathcal{M}|^2 |p_1^*| |p_3| dm_{12} d\Omega_1^* d\Omega_3,$$

On leptonic width of $X(4260)$

- Considering the isospin symmetry and heavy quark spin symmetry

$$\begin{aligned}\Gamma_{J/\psi\pi\pi}(s) &= \frac{3}{2}\Gamma_{J/\psi\pi^+\pi^-}(s), \Gamma_{h_c\pi\pi}(s) = \frac{3}{2}\Gamma_{h_c\pi^+\pi^-}(s), \Gamma_{\psi(2S)\pi\pi}(s) \\ &= \frac{3}{2}\Gamma_{\psi(2S)\pi^+\pi^-}(s), \Gamma_{D\bar{D}^*\pi}(s) = 3\Gamma_{D^0D^{*-}\pi^+}(s), \Gamma_{D\bar{D}}(s) = 2\Gamma_{D^+D^-}(s), \\ \Gamma_{D\bar{D}^*}(s) &= 2\Gamma_{D^+D^{*-}+c.c.}(s), \Gamma_{D^*\bar{D}^*}(s) = 2\Gamma_{D^{*+}D^{*-}}(s),\end{aligned}$$

$$g_{D^+D^-}:g_{D^+D^{*-}}:g_{D^{*+}D^{*-}} = 1:4:7 \text{ [1]}$$

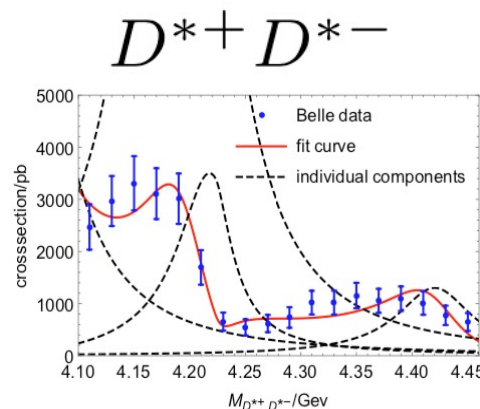
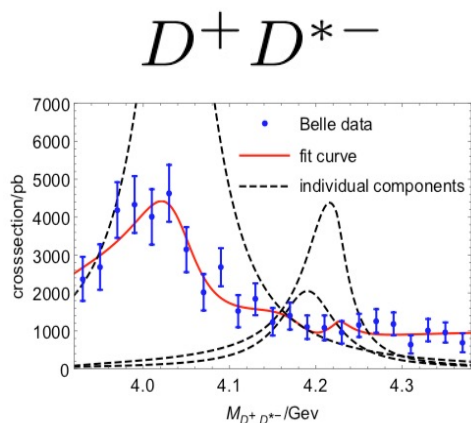
- Combined fit

parameters	value
$g_0(\text{MeV})$	23.865 ± 0.602
$M_X(\text{GeV})$	4.219 ± 0.001
$\Gamma_0(\text{GeV})$	0.005 ± 0.002
$\Gamma_{e^+e^-}(\text{keV})$	0.3~1.3
$\chi^2/d.o.f.$	$292.84/(357-43) = 0.93$

Due to interfered multiplicity and different bkg. shapes, we only gave out the leptonic width range, which is consistent with that of $\psi(4^3S_1)$ (or mixed with a small $\psi(2^3D_1/3^3D_1)$) in the refined potential models.

[1] M.B. Voloshin, Phys. Rev. D **85**, 034024 (2012)

An interpretation of non-peak in $M(D^{(*)}\bar{D}^{(*)})$ @4220 MeV



Other fit
 projections see
 Slide 20 for details.

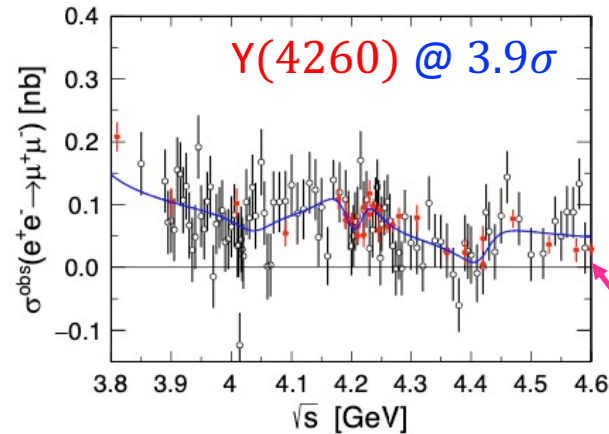
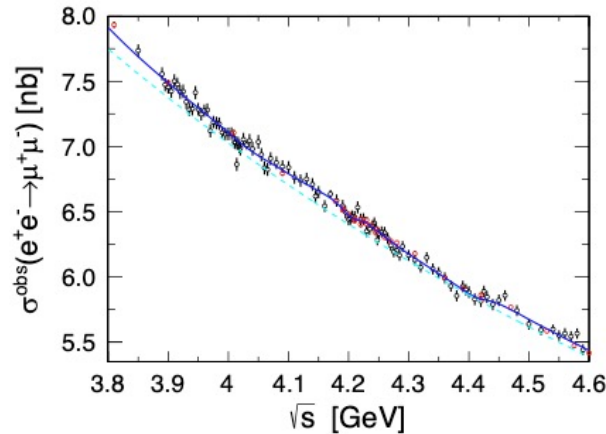
$$\psi(4040)_{fixed} + \psi(4160)_{fixed} + Y(4260) + \psi(4415)_{fixed}$$

- Interference among multiple ψ states can describe $M(D^{(*)}\bar{D}^{(*)})$ very well.
- Certainly, **more improved** measurements of $e^+e^- \rightarrow D^{(*)}\bar{D}^{(*)}$ is necessary to further confirmed if non-peak around 4220 MeV is caused by destructive interference.

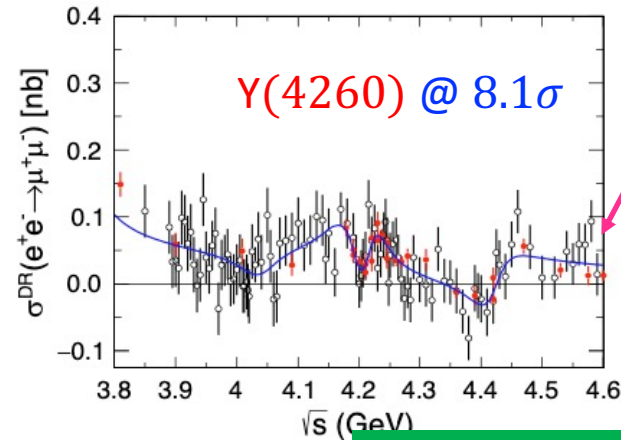
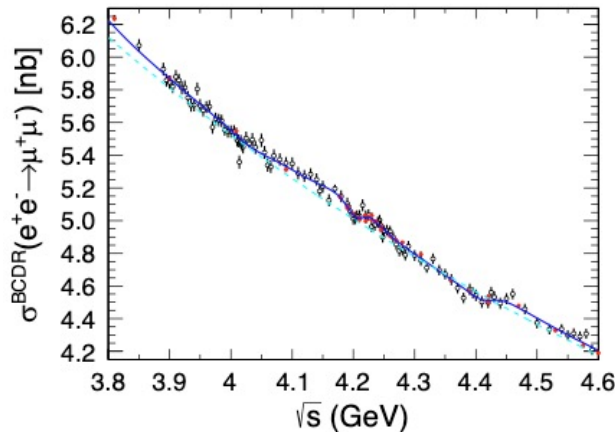
Good news from BESIII



Without ISR
correction



With ISR
correction



Subtracted both
the continuum and
 $\psi(2S) \rightarrow \mu^+ \mu^-$
contributions

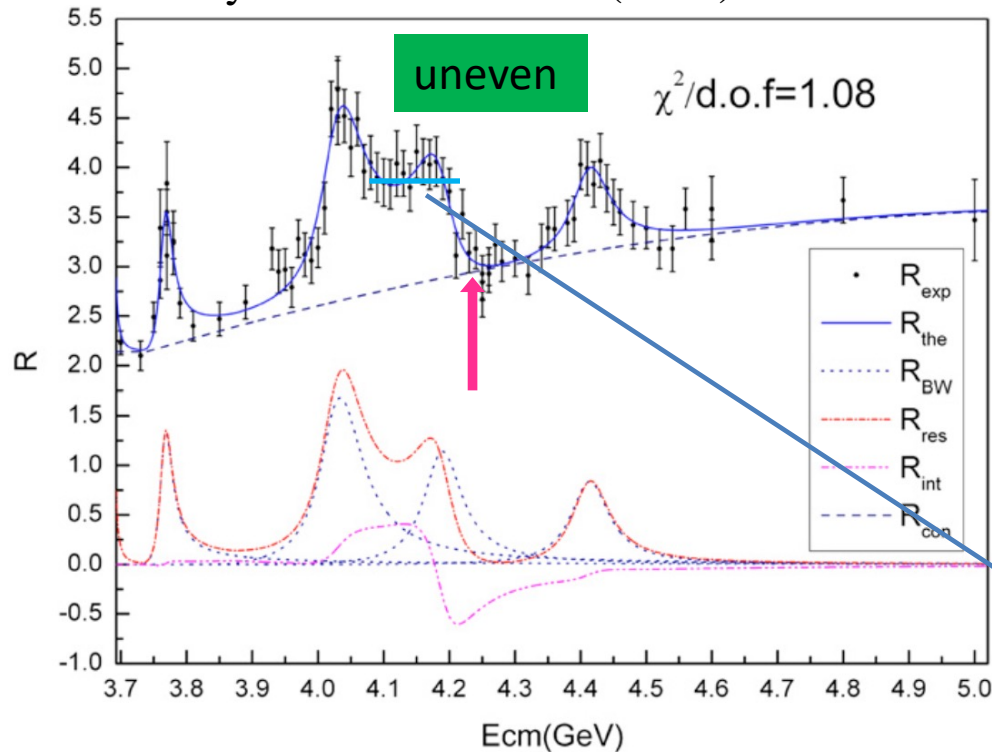
$$M_{S(4220)} = 4216.7 \pm 8.9 \pm 4.1 \text{ MeV}, \quad \Gamma_{\mu^+ \mu^-}: 1.09 \sim 1.53 \text{ keV}$$

$$\Gamma_{S(4220)}^{\text{tot}} = 47.2 \pm 22.8 \pm 10.5 \text{ MeV}$$

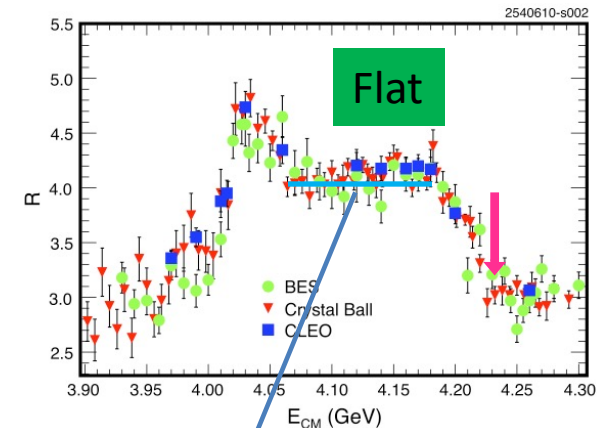
Consistent well with the combined
fit to multiple hadron channels as
well as refined potential models !

Investigation of non-peak in R scan @4220 MeV

Physics Letters B 660 (2008) 315



Eur. Phys. J. C (2011) 71: 1534



The fit seems not consistent well with all data. Might another charmonium state be required.

- At present, the $\psi(4040)$ and $\psi(4160)$'s parameters in PDG mainly derives from the BESII fit to the R-scan distribution. We believe that it is time to update the experimental data as well as the fit.

$Y(4260)$ is $\psi(4S)$?

If this law of mass gap relation still holds for states with $n = 3, 4$ in J/ψ and Υ families, the mass of $\psi(4S)$ should be located at 4,264~4290 MeV rather than 4415 MeV, which is compatible with the screened potential model prediction[PRD 79, 094004 (2009)].

Eur. Phys. J. C 74, 3208 (2014)

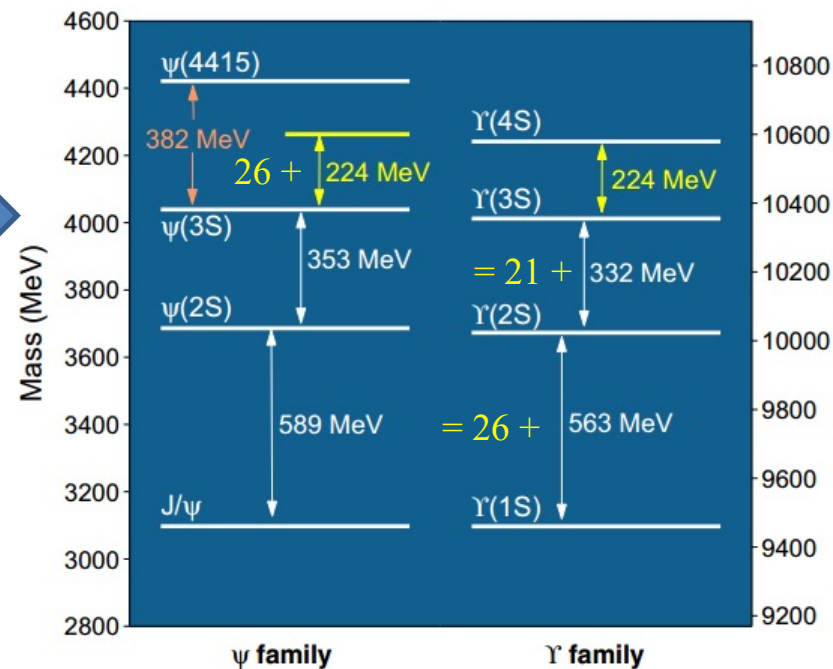
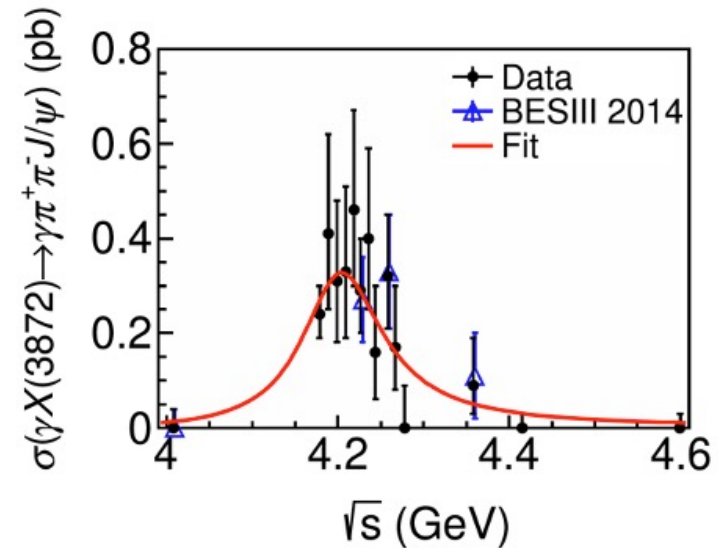


Fig. 1 A comparison between the J/ψ and Υ families

Radiative decay of $Y(4260)$

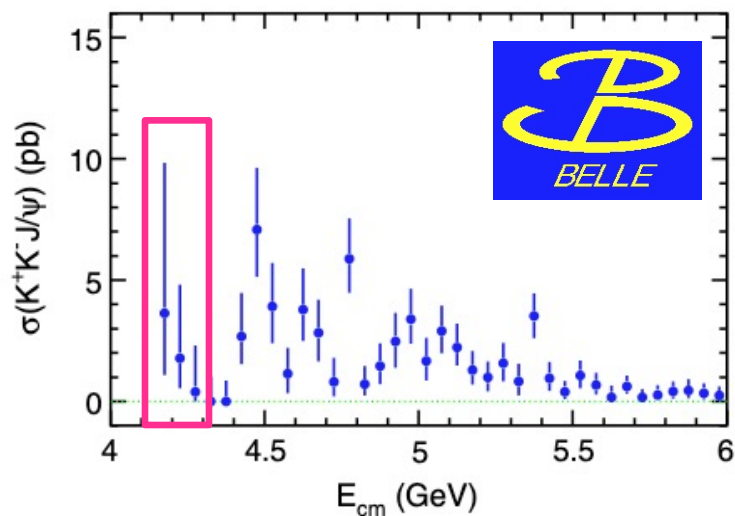
BESIII

PRL 122, 232002 (2019)



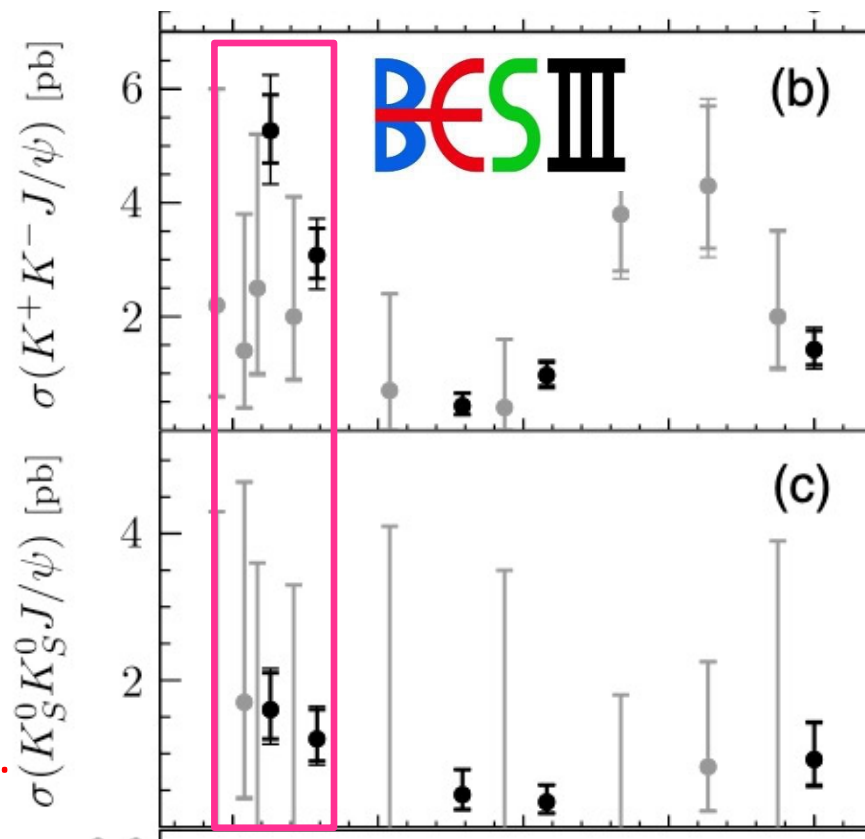
- The product of the cross section and Br. around 4220 MeV is ~ 0.3 pb. Exploiting Br($X(3872) \rightarrow \pi^+ \pi^- J/\psi$) = 4.1% measured by BABAR[1], $\sigma_{top}(e^+ e^- \rightarrow \gamma X(3872)) = 7.3$ pb, which is about one tenth of $\sigma_{top}(e^+ e^- \rightarrow \pi^+ \pi^- J/\psi)$.
- According to Ref [2], Br($Y(4260) \rightarrow \pi^+ \pi^- J/\psi$) is $\mathcal{O}(10^{-4})$ and $\Gamma_{tot}(Y(4260)) \sim 50$ MeV, and we can do an analogy to gain $\Gamma(Y(4260) \rightarrow X(3872)) = 5 \times \mathcal{O}(10^{-1})$ keV. assuming $X(3872)$ as the $\chi_{c1}(2P)$ state, $\Gamma(4^3S_1 \rightarrow 2^3P_1) = 5 \times \mathcal{O}(10^{-1})$ keV.
- The radiative widths $\Gamma(4^3S_1 \rightarrow 2^3P_1)$ [3] used GI and non-relativistic models are calculated to be 0.49 and 0.92 keV, which is consistent with the above rough estimation and suggests $Y(4260)$ is the $\psi(4^3S_1)$ candidate.

$Y(4260) \rightarrow K\bar{K}J/\psi$?



PRD 89, 072015 (2014)

- If $Y(4260)$ is a charmonium state, it should be observed in the $K\bar{K}J/\psi$ system.
- There are some hints for this decay, and it would be confirmed in the near future.



PRD 97, 071101(R) (2018)



Summary of $\psi(4260)$

- Excited $c\bar{c}$ state

✓ Mass

✓ OZI rule

? Non R scan

✓ $\Gamma_{e^+e^-}$

✓ Γ_γ

- Tetraquark

? Mass

✓ OZI rule

? Non R scan

? $\Gamma_{e^+e^-}$

? Γ_γ

- $c\bar{c}$ -gluon hybrid

? Mass

✓ OZI rule

? Non R scan

? $\Gamma_{e^+e^-}$

? Γ_γ

- $D_1\bar{D}$ molecule

✓ Mass

✓ OZI rule

? Non R scan

? $\Gamma_{e^+e^-}$

? Γ_γ

- $D_s^{*+}D_s^{*-}$ effect

✓ Mass

✓ OZI rule

✓ Non R scan

- et al.

Open charm channels significantly!

As mentioned above, $\psi(4260)$ might interpreted as a mixture of 4^3S_1 (or mixed with a 4^1S_0) and 4^3P_0 states.

More information is needed to confirm the nature of $\psi(4260)$.

Thank you!

Backup

Theoretical interpretations

- **Excited charmonium:** PRD 99, 114003 (2019), EPJC 79, 613 (2019), EPJC **78**, 136 (2018), PRD**79**,094004(2009), PRD72,031503(2005)
- **Compact tetraquark:** PRD 89, 114010 (2014), EPJC 71, 1534
- **$c\bar{c}$ -gluon hybrid:** Phys. Lett. B 628, 215. Phys. Lett. B 631, 164. Phys. Lett. B 625, 212.
- **Meson-meson molecule:** PRL 111, 132003, PRD 94, 054035 (2016), PRD 79, 014001, PRL**102**, 242003 (2009),
- **Threshold effect:** Acta Phys.Pol.B.**51**(8),1713–1737(2020)
- **et al.**