

FIMP Dark Matter from Leptogenesis in Fast Expanding Universe

Zhi-Long Han

School of Physics and Technology, University of Jinan

August 17, 2021

Based on JCAP06(2021)006, arXiv:2104.02364

Introduction

- Beyond standard model evidences —
neutrino mass, baryon asymmetry, dark matter
- Common origin for BSM —
 ν MSM, Scotogenic Model, **sterile neutrino portal model ...**
- Model Structure —
 - Sterile neutrinos N with the type-I seesaw mechanism
 - Baryon asymmetry is generated via the thermal leptogenesis
 - Dark sector: scalar singlet ϕ , fermion singlet χ under Z_2 symmetry
- The relevant Yukawa interactions and mass terms are

$$-\mathcal{L} = y \bar{L} \tilde{H} N + \lambda \bar{\chi} \phi N + \frac{1}{2} \overline{N^C} m_N N + m_\chi \bar{\chi} \chi + \text{h.c..} \quad (1)$$

Introduction

- About the dark scalar ϕ —
 - For m_ϕ below electroweak scale, the dominant decay is $\phi \rightarrow \chi \nu$

$$\Gamma_{\phi \rightarrow \chi \nu} = \frac{\lambda^2}{16\pi} \frac{m_\nu}{m_N} m_\phi \left(1 - \frac{m_\chi^2}{m_\phi^2}\right)^2. \quad (2)$$

- Decaying DM when its lifetime is larger than the age of Universe.
- A scalar singlet S with the condition $m_\phi \sim m_S/2$
- In the standard cosmology the Universe is radiation dominant after inflation until Big Bang Nucleosynthesis.
- Scalar field φ with energy density red-shifts as $\rho_\varphi \propto a^{-(4+n)}$
- Lead to a fast expanding Universe (FEU) when $n > 0$
- The period of FIMP DM generation from leptogenesis is right between inflation and BBN

A Fast Expanding Universe

In SC, radiation is the dominant component before BBN

$$\rho_r(T) = \frac{\pi^2}{30} g_*(T) T^4, \quad (3)$$

The Hubble parameter, is related to the radiation as

$$H_r(T) = \sqrt{\frac{8\pi G \rho_r(T)}{3}} = 1.66 \sqrt{g_*(T)} \frac{T^2}{M_p}, \quad (4)$$

In a FEU, scalar component φ coexists with the radiation

$$\rho_\varphi \sim a^{-(4+n)}, n > 0. \quad (5)$$

Assuming entropy conservation $S = sa^3$ and using the relation $\rho_r(T) \propto g_*(T)T^4$ in Eqn. (3), we can have

$$\rho_\varphi(T) = \rho_r(T) \frac{g_*(T_r)}{g_*(T)} \left(\frac{g_{*s}(T)}{g_{*s}(T_r)} \right)^{\frac{4+n}{3}} \left(\frac{T}{T_r} \right)^n. \quad (6)$$

A Fast Expanding Universe

Therefore, the total energy density can be expressed as

$$\rho(T) = \rho_r(T) + \rho_\varphi(T) = \rho_r(T) \left[1 + \frac{g_*(T_r)}{g_*(T)} \left(\frac{g_{*s}(T)}{g_{*s}(T_r)} \right)^{\frac{4+n}{3}} \left(\frac{T}{T_r} \right)^n \right]. \quad (7)$$

The typical temperature for leptogenesis $T \sim M_N \gtrsim 10^9$ GeV, $g_*(T) = g_{*s}(T) = 106.75$ as a constant. Then

$$\rho(T) = \rho_r(T) \left[1 + \left(\frac{T}{T_r} \right)^n \right]. \quad (8)$$

The Hubble parameter in a fast expanding Universe is modified by

$$H(T) = 1.66\sqrt{g_*} \frac{T^2}{M_p} \left[1 + \left(\frac{T}{T_r} \right)^n \right]^{\frac{1}{2}} = H_r(T) \left[1 + \left(\frac{T}{T_r} \right)^n \right]^{\frac{1}{2}}. \quad (9)$$

FIMP DM from Leptogenesis in SC

The CP asymmetry is generated by out-of-equilibrium CP-violating decays of Majorana neutrino.

$$\varepsilon = -\frac{3}{16\pi(y^\dagger y)_{11}} \sum_{j=2,3} \text{Im} \left[\left(y^\dagger y \right)_{1j}^2 \right] \frac{M_1}{M_j}. \quad (10)$$

Casas-Ibarra parametrization of Yukawa coupling

$$y = \frac{\sqrt{2}}{v} U_{\text{PMNS}} \hat{m}_\nu^{1/2} R(\hat{m}_N)^{1/2}, \quad (11)$$

Davidson-Ibarra bound on ε can be derived

$$|\varepsilon| \lesssim \frac{3}{16\pi} \frac{M_1 m_3}{v}. \quad (12)$$

FIMP DM from Leptogenesis in SC

The evolution of abundance Y_{N_1} , Y_χ and lepton asymmetry Y_L is described by the Boltzmann equations

$$\frac{dY_{N_1}}{dz} = -D_r(Y_{N_1} - Y_{N_1}^{eq}), \quad (13)$$

$$\frac{dY_L}{dz} = -\varepsilon D_r(Y_{N_1} - Y_{N_1}^{eq}) - W_r Y_L, \quad (14)$$

$$\frac{dY_\chi}{dz} = D_r Y_{N_1} \text{BR}_\chi, \quad (15)$$

The decay and washout terms are

$$D_r(z) = K z \frac{\mathcal{K}_1(z)}{\mathcal{K}_2(z)}, \quad W_r(z) = \frac{1}{4} K z^3 \mathcal{K}_1(z), \quad (16)$$

The decay parameter K is defined as

$$K = \frac{\Gamma_1}{H_r(z=1)}, \quad (17)$$

FIMP DM from Leptogenesis in FEU

Boltzmann equations have the same form as the standard cosmology

$$\frac{dY_{N_1}}{dz} = -D(Y_{N_1} - Y_{N_1}^{eq}), \quad (18)$$

$$\frac{dY_L}{dz} = -\varepsilon D(Y_{N_1} - Y_{N_1}^{eq}) - WY_L, \quad (19)$$

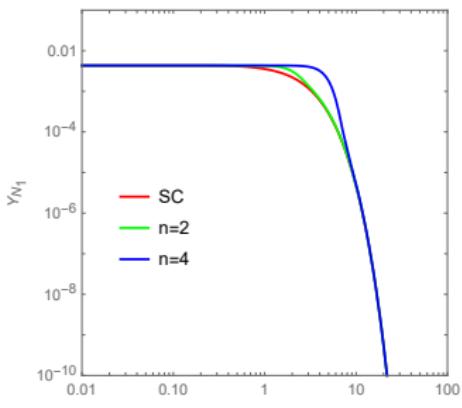
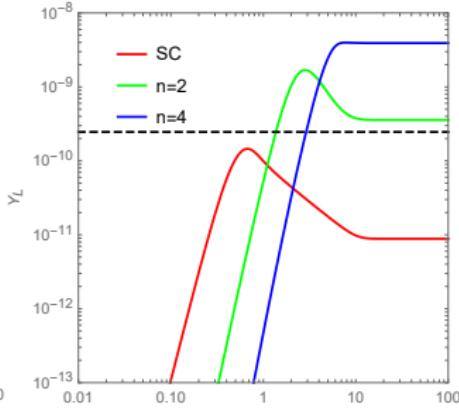
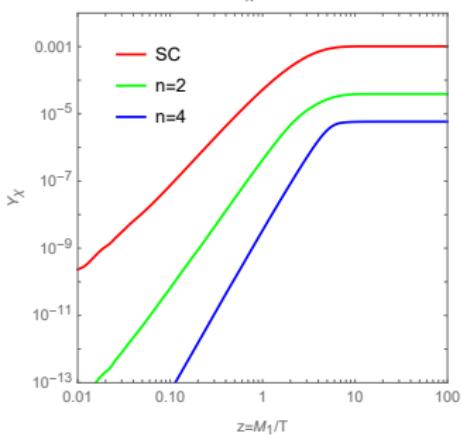
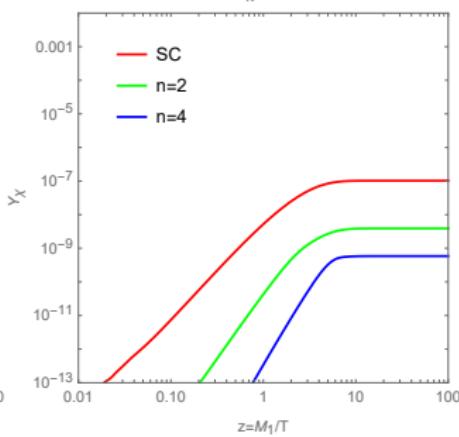
$$\frac{dY_\chi}{dz} = D Y_{N_1} \text{BR}_\chi, \quad (20)$$

but the decay and washout terms are modified as

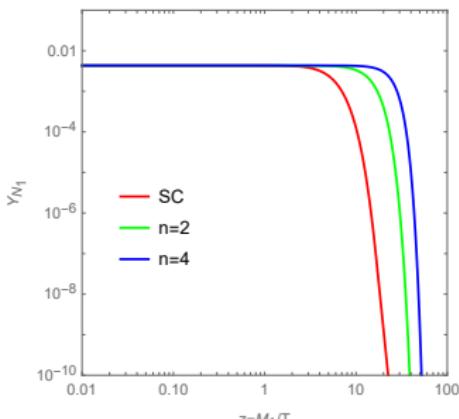
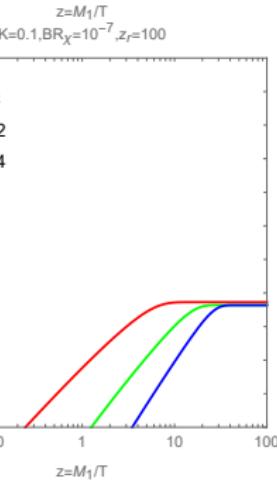
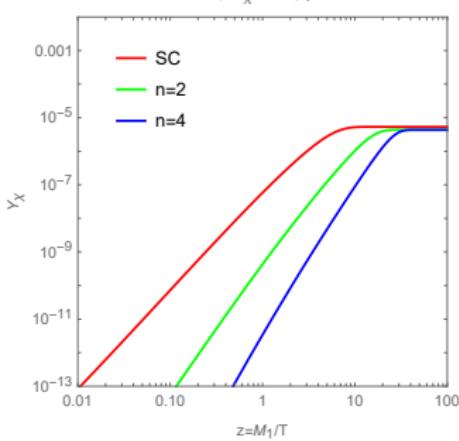
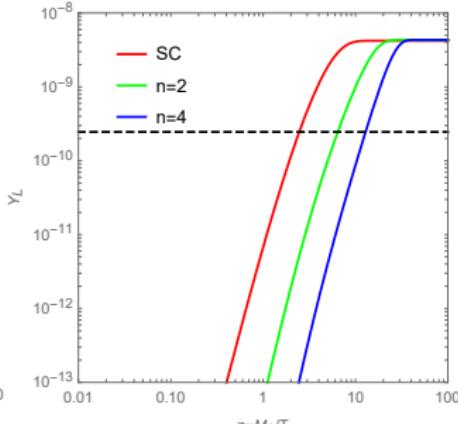
$$D(z) = Kz \frac{\mathcal{K}_1(z)}{\mathcal{K}_2(z)} \left[1 + \left(\frac{z_r}{z} \right)^n \right]^{-1/2}, \quad W(z) = \frac{1}{4} K z^3 \mathcal{K}_1(z) \left[1 + \left(\frac{z_r}{z} \right)^n \right]^{-1/2},$$

The lepton asymmetry is converted into the baryon asymmetry via the sphaleron processes

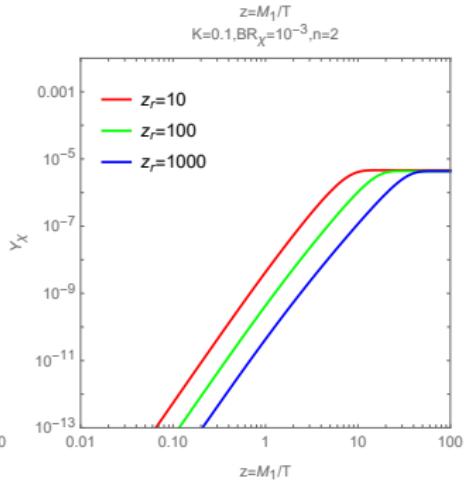
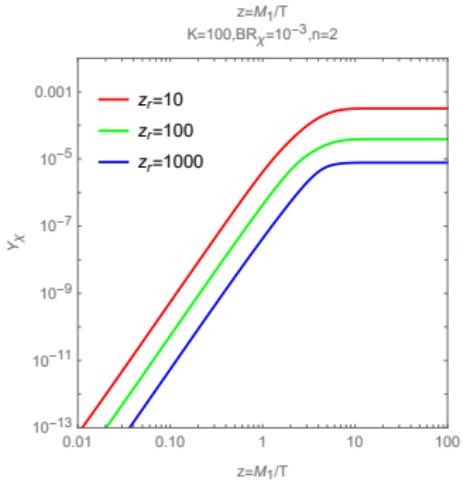
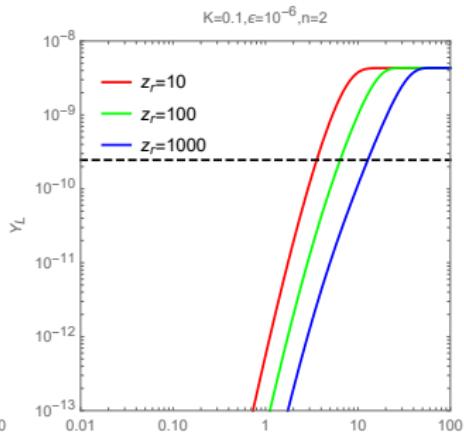
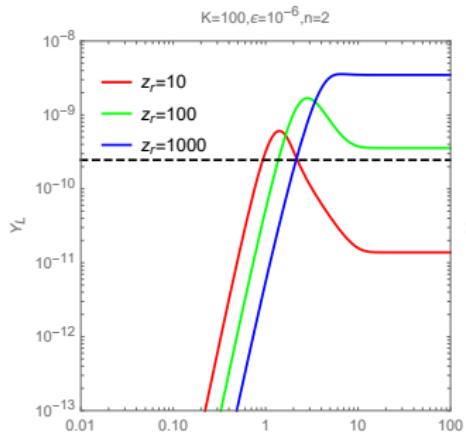
$$Y_B = \frac{28}{79} Y_L, \quad (21)$$

$K=100, \epsilon=10^{-6}, z_f=100$  $K=100, \epsilon=10^{-6}, z_f=100$  $K=100, BR_{\chi}=10^{-3}, z_f=100$  $K=100, BR_{\chi}=10^{-7}, z_f=100$ 

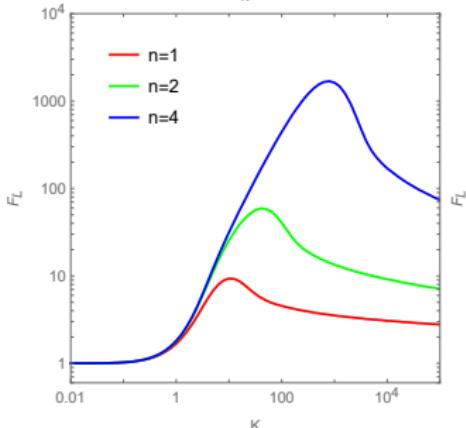
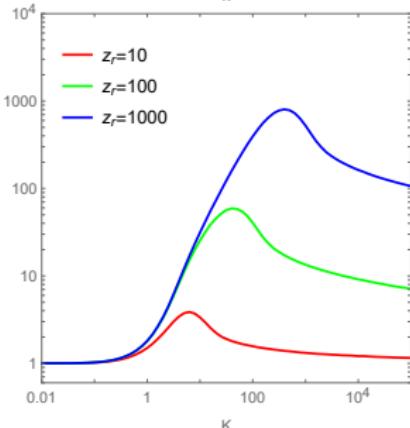
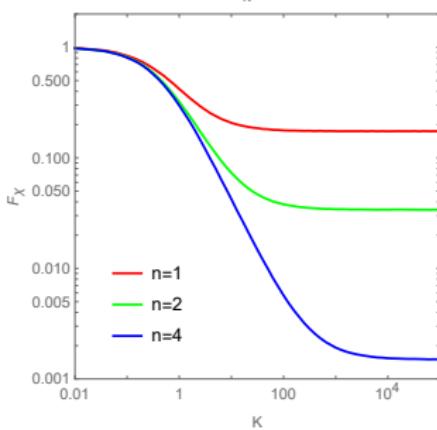
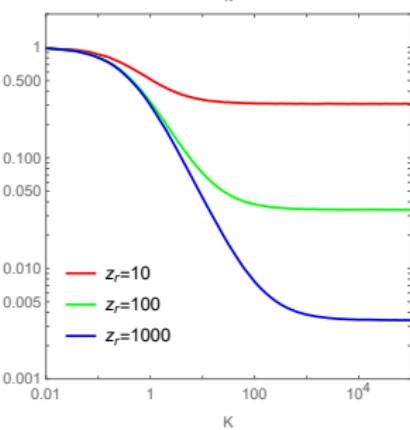
- Impact of parameter n for strong washout.
- Y_L increases as the parameter n increases
- Y_χ decreases as the parameter n increases

$K=0.1, \epsilon=10^{-6}, z_f=100$  $K=0.1, \epsilon=10^{-6}, z_f=100$ 

- Impact of parameter n for weak washout.
- Production of Y_L and Y_χ are postponed. But the final lepton asymmetry and DM abundance are of the same order for different n .



- Impact of parameter z_r .
- In the strong washout case, modifications of z_r will have a great impact on the evolution of Y_L and Y_χ .
- In the weak washout case, the impact is small.

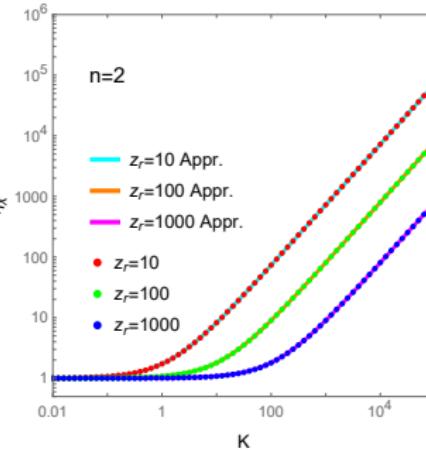
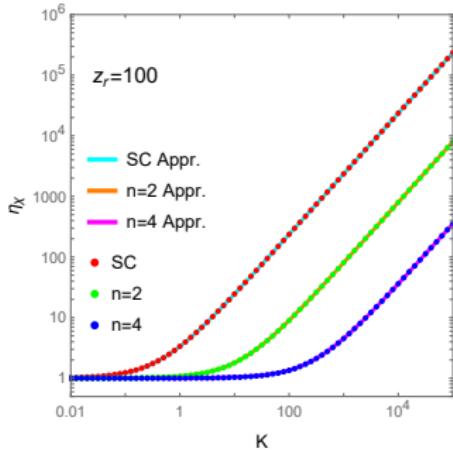
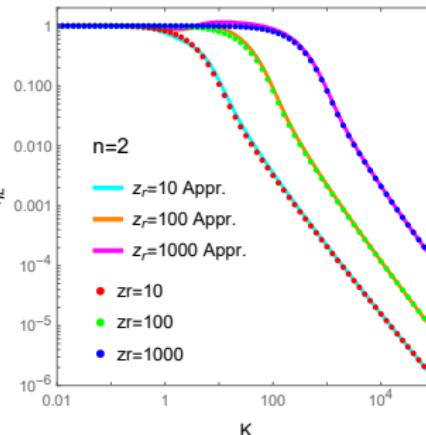
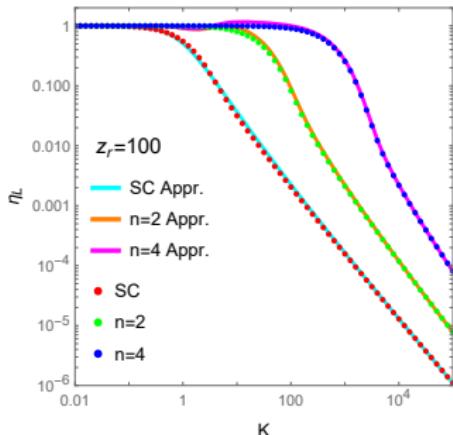
$\epsilon=10^{-6}, BR_\chi=10^{-3}, z_r=100$  $\epsilon=10^{-6}, BR_\chi=10^{-3}, n=2$  $\epsilon=10^{-6}, BR_\chi=10^{-3}, z_r=100$  $\epsilon=10^{-6}, BR_\chi=10^{-3}, n=2$ 

- The scale factors F_L and F_χ as a function of K .

$$F_L = \frac{Y_L^{\text{FEU}}(\infty)}{Y_L^{\text{SC}}(\infty)},$$

$$F_\chi = \frac{Y_\chi^{\text{FEU}}(\infty)}{Y_\chi^{\text{SC}}(\infty)}.$$

- The efficiency factors η_L and η_χ as a function of K

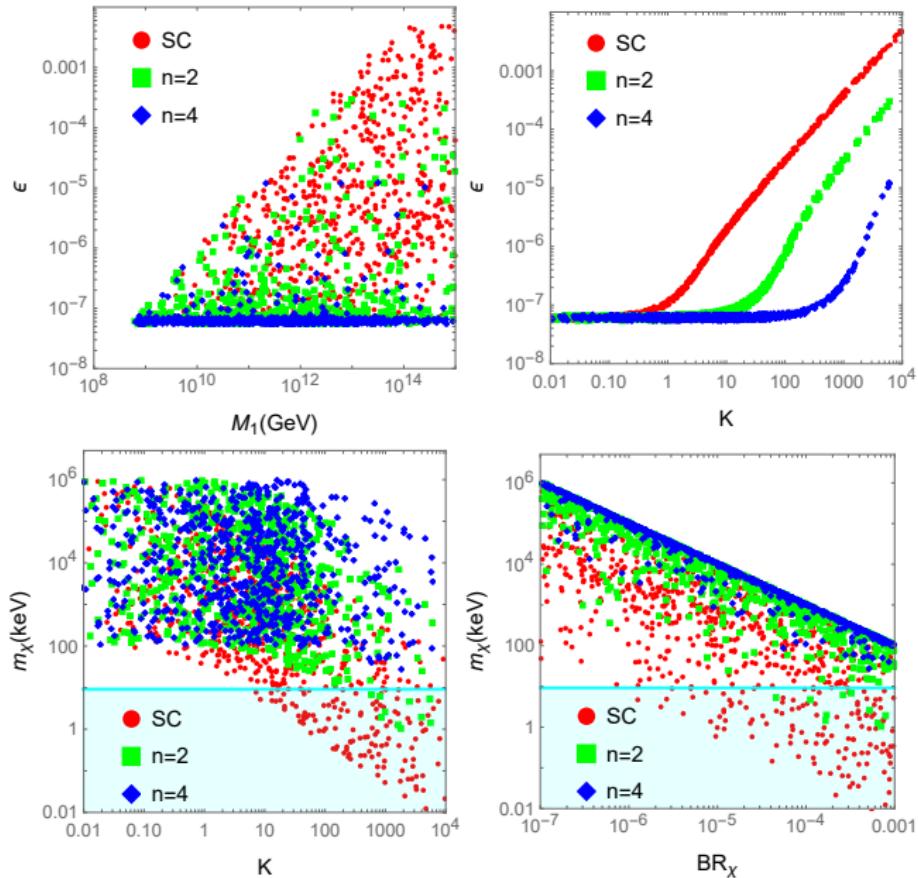


$$\eta_L^{\text{SC}} \simeq \frac{1}{1 + 1.3K \ln(1 + K)}$$

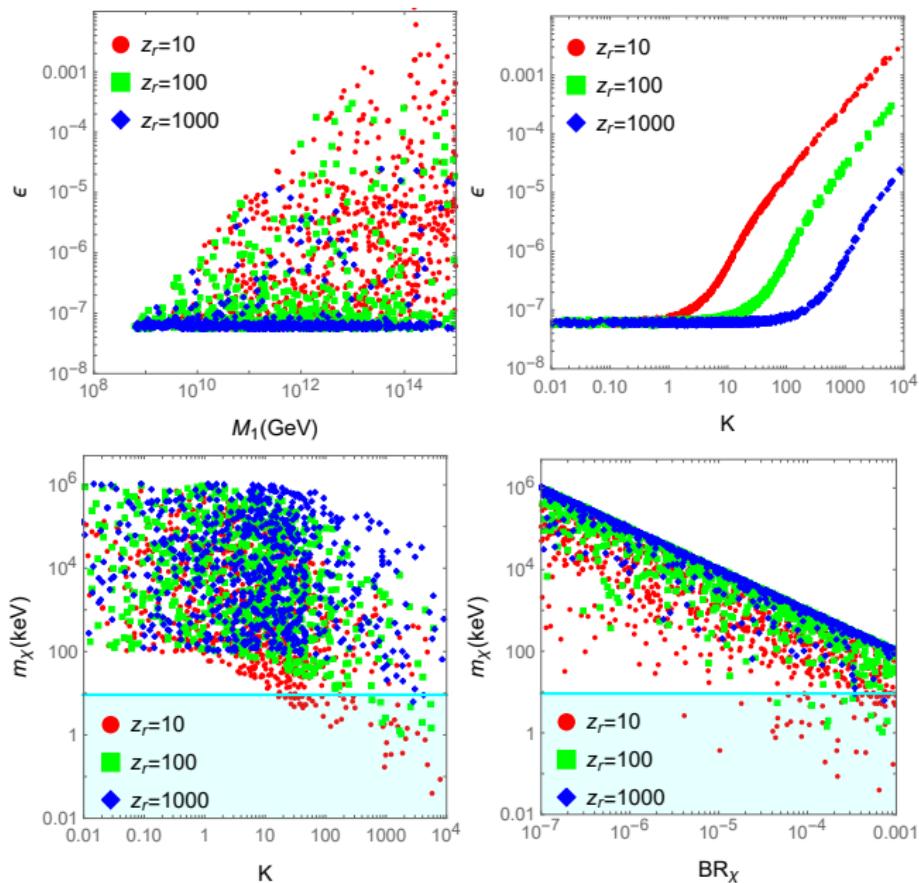
$$\eta_\chi^{\text{SC}} \simeq 1 + \frac{3\pi}{4}K.$$

$$\eta_L^{\text{FEU}} = \eta_L^{\text{SC}} F_L^{\text{FEU}},$$

$$\eta_\chi^{\text{FEU}} = \eta_\chi^{\text{SC}} F_\chi^{\text{FEU}}.$$



- Scanned results for SC and FEU with $n=2, 4$. For FEU, we take $z_r = 100$ to illustrate.
- For the FIMP DM χ , it is required $m_\chi > 9.2$ keV to satisfy all limits.



- Scanned results for FEU with $z_r = 10, 100, 1000$. Here, we take $n = 2$ to illustrate.

Conclusion

- Sterile neutrino portal model provides a common origin for neutrino mass, baryon asymmetry and DM.
- For weak washout scenario $K \lesssim 1$, modifications of final lepton asymmetry Y_L and DM abundance Y_χ are relatively small in FEU.
- But for strong washout case $K \gtrsim 1$, the final $Y_L(Y_\chi)$ could be increased (suppressed) by several orders of magnitudes.
- However, it seems hard to figure out explicit values of the two parameters n and z_r when only considering the results of FIMP DM from leptogenesis.