

CPV in baryonic decays

Yu-Kuo Hsiao 萧佑国

Shanxi Normal University

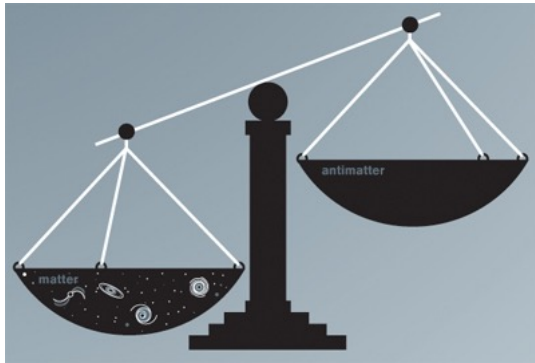
第一届 LHCb 前沿物理研讨会

2019.12.14

Outline:

1. Introduction
2. Formalism
3. Results
4. Summary

Introduction



- To explain the matter-antimatter asymmetry, CPV is needed. (one of Sakharov conditions)
- In SM, the CKM matrix elements provide the unique source, explaining CPV in the K, B and D systems.
- Baryonic CPV for baryonic universe.

Two-body $B \rightarrow MM$ decays

- To explain $\mathcal{A}_{CP}(\bar{B}^0 \rightarrow K^- \pi^+) = -0.082 \pm 0.006$, one needs the penguin annihilation amp to flip the naive results based on the factorization.

**Y.Y. Keum, H.n. Li, A.I. Sanda, PRD63, 054008 (2001);
H.Y. Cheng, C.K. Chua, PRD80, 074031 (2009).**

- The naive result of $\mathcal{A}_{CP}(\bar{B}^0 \rightarrow K^- \pi^+) \simeq \mathcal{A}_{CP}(B^- \rightarrow K^- \pi^0)$ NOT approved by the data of $\mathcal{A}_{CP}(B^- \rightarrow K^- \pi^0) = 0.037 \pm 0.021$.

One needs the color-suppressed tree amp to flip the sign again.

**H.Y. Cheng, C.K. Chua, PRD80, 074031 (2009);
H.n. Li, S. Mishima, PRD83, 034023 (2011).**

- **Direct CPA in B_b decays:**

$$\mathcal{A}_{CP}(\mathbf{B}_b \rightarrow f) = \frac{\Gamma(\mathbf{B}_b \rightarrow f) - \Gamma(\bar{\mathbf{B}}_b \rightarrow \bar{f})}{\Gamma(\mathbf{B}_b \rightarrow f) + \Gamma(\bar{\mathbf{B}}_b \rightarrow \bar{f})}$$

$$\mathcal{A}(\mathbf{B}_b \rightarrow f) = ae^{i\delta_w} + be^{i\delta_s}$$

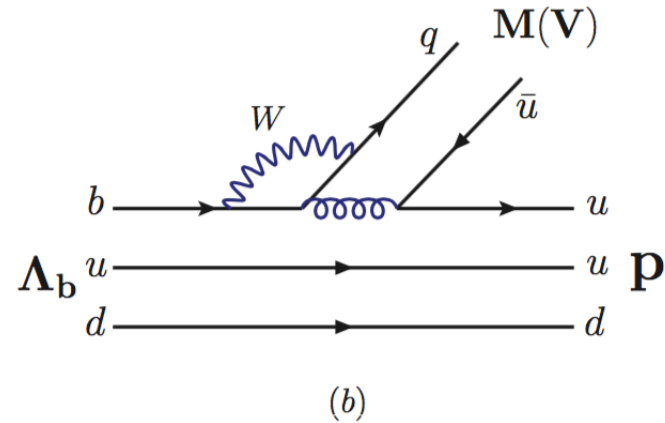
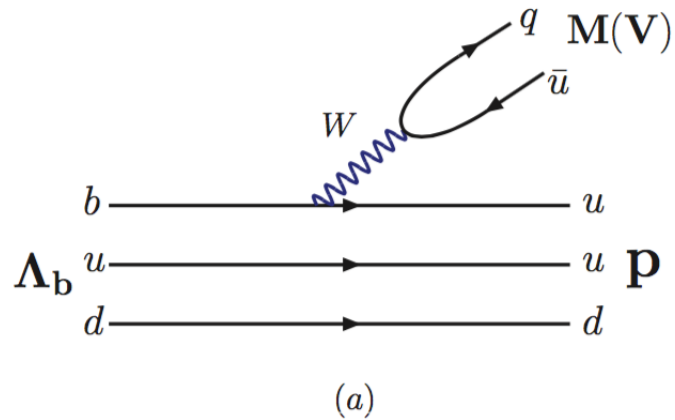
$$\mathcal{A}(\bar{\mathbf{B}}_b \rightarrow \bar{f}) = ae^{-i\delta_w} + be^{i\delta_s}$$

$$\Gamma(\mathbf{B}_b \rightarrow f) \neq \Gamma(\bar{\mathbf{B}}_b \rightarrow \bar{f})$$

$$\delta_w: V_{ub} = A\lambda^3(\rho - i\eta)$$

δ_s : effective Wilson coefficients (quark rescattering)

• Factorization



• Amplitudes

$$\mathcal{A}(\Lambda_b \rightarrow pM) = i \frac{G_F}{\sqrt{2}} m_b f_M \left[\alpha_M \langle p | \bar{u} b | \Lambda_b \rangle + \beta_M \langle p | \bar{u} \gamma_5 b | \Lambda_b \rangle \right]$$

$$\mathcal{A}(\Lambda_b \rightarrow pV) = \frac{G_F}{\sqrt{2}} m_V f_V \varepsilon^{\mu*} \alpha_V \langle p | \bar{u} \gamma_\mu (1 - \gamma_5) b | \Lambda_b \rangle$$

- $\Lambda_b \rightarrow p$ transition form factors

$$\langle \mathcal{B} | \bar{q} \gamma_\mu b | \mathcal{B}_b \rangle = \bar{u}_{\mathcal{B}} \left[f_1 \gamma_\mu + \frac{f_2}{m_{\mathcal{B}_b}} i \sigma_{\mu\nu} q^\nu + \frac{f_3}{m_{\mathcal{B}_b}} q_\mu \right] u_{\mathcal{B}_b}$$

$$\langle \mathcal{B} | \bar{q} \gamma_\mu \gamma_5 b | \mathcal{B}_b \rangle = \bar{u}_{\mathcal{B}} \left[g_1 \gamma_\mu + \frac{g_2}{m_{\mathcal{B}_b}} i \sigma_{\mu\nu} q^\nu + \frac{g_3}{m_{\mathcal{B}_b}} q_\mu \right] \gamma_5 u_{\mathcal{B}_b}$$

$$\langle \mathcal{B} | \bar{q} b | \mathcal{B}_b \rangle = f_S \bar{u}_{\mathcal{B}} u_{\mathcal{B}_b}, \quad \langle \mathcal{B} | \bar{q} \gamma_5 b | \mathcal{B}_b \rangle = f_P \bar{u}_{\mathcal{B}} \gamma_5 u_{\mathcal{B}_b}$$

In equation of motion:

$$f_S = \frac{m_{\mathcal{B}_b} - m_{\mathcal{B}}}{m_b - m_q} f_1, \quad f_P = \frac{m_{\mathcal{B}_b} + m_{\mathcal{B}}}{m_b + m_q} g_1.$$

$$f_1 = g_1 \text{ and } f_{2,3} = g_{2,3} = 0$$

$$f_1(q^2) = \frac{C_F}{(1 - q^2/m_{\mathcal{B}_b}^2)^2}, \quad g_1(q^2) = \frac{C_F}{(1 - q^2/m_{\mathcal{B}_b}^2)^2}$$

$$C_F = 0.14 \pm 0.03$$

from the light-cone sum rules

JHEP 1109, 106 (2011); JHEP 1112, 067 (2011)

$$\mathcal{B}(\Lambda_b \rightarrow pK^-) = (5.1_{-2.0}^{+2.4}) \times 10^{-6}$$

$$\mathcal{B}(\Lambda_b \rightarrow p\pi^-) = (4.4_{-1.7}^{+2.1}) \times 10^{-6}$$

- We fit C_F to reduce the uncertainty.

$$C_F = 0.136 \pm 0.009$$

$$\mathcal{B}(\Lambda_b \rightarrow pK^-) = (4.8 \pm 0.7 \pm 0.1 \pm 0.3) \times 10^{-6}$$

$$\mathcal{B}(\Lambda_b \rightarrow p\pi^-) = (4.2 \pm 0.6 \pm 0.4 \pm 0.2) \times 10^{-6}$$

- $\mathcal{R}_{\pi K} \equiv \frac{\mathcal{B}(\Lambda_b \rightarrow p\pi^-)}{\mathcal{B}(\Lambda_b \rightarrow pK^-)} = 0.84 \pm 0.22$ (CDF and LHCb)

$$\mathcal{A}(\Lambda_b \rightarrow pM) = i\frac{G_F}{\sqrt{2}}m_b f_M \left[\alpha_M \langle p|\bar{u}b|\Lambda_b\rangle + \beta_M \langle p|\bar{u}\gamma_5 b|\Lambda_b\rangle \right]$$

$$\mathcal{R}_{\pi K} = \frac{f_\pi^2}{f_K^2} \frac{|\alpha_\pi|^2 + |\alpha_{\bar{\pi}}|^2}{|\alpha_K|^2 + |\alpha_{\bar{K}}|^2} \frac{1 + \xi_\pi^+}{1 + \xi_K^+}$$

$$\alpha_M(\beta_M) = V_{ub}V_{uq}^* a_1 - V_{tb}V_{tq}^*(a_4 \pm r_M a_6)$$

$$\xi_M^\pm \equiv \left(\frac{|\beta_M|^2 \pm |\beta_{\bar{M}}|^2}{|\alpha_M|^2 + |\alpha_{\bar{M}}|^2} \right) R_{\Lambda_b \rightarrow p}$$

$$R_{\Lambda_b \rightarrow p} = |\langle p|\bar{u}\gamma_5 b|\Lambda_b\rangle|^2 / |\langle p|\bar{u}b|\Lambda_b\rangle|^2 = 1.008$$

$$(\xi_\pi^+, \xi_K^+) = (1.03 \pm 0.04 \pm 0.00, 0.11 \pm 0.01 \pm 0.02)$$

$$\mathcal{R}_{\pi K} \simeq 2 \frac{f_\pi^2}{f_K^2} \frac{|\alpha_\pi|^2 + |\alpha_{\bar{\pi}}|^2}{|\alpha_K|^2 + |\alpha_{\bar{K}}|^2}, \text{ nearly model-indepent}$$

$$\mathcal{R}_{\pi K} = 0.84 \pm 0.09 \pm 0.00.$$

• The direct CP asymmetry: $\mathcal{A}_{CP} = \frac{\Gamma_{M(V)} - \Gamma_{\bar{M}(\bar{V})}}{\Gamma_{M(V)} + \Gamma_{\bar{M}(\bar{V})}}$

$$\mathcal{A}_{CP}(\Lambda_b \rightarrow pM) = \left(\frac{|\alpha_M|^2 - |\alpha_{\bar{M}}|^2}{|\alpha_M|^2 + |\alpha_{\bar{M}}|^2} + \xi_M^- \right) \frac{1}{1 + \xi_M^+}$$

$$(\xi_\pi^+, \xi_K^+) = (1.03 \pm 0.04 \pm 0.00, 0.11 \pm 0.01 \pm 0.02)$$

$$(\xi_\pi^-, \xi_K^-) = (-4.0 \pm 0.3 \pm 0.0, -4.0 \pm 0.2 \pm 0.3) \times 10^{-3}$$

$$\mathcal{A}_{CP}(\Lambda_b \rightarrow pK^-) = (5.8 \pm 0.2 \pm 0.1)\%$$

$$\mathcal{A}_{CP}(\Lambda_b \rightarrow p\pi^-) = (-3.9 \pm 0.2 \pm 0.0)\%$$

- The vector mode:

$$\mathcal{A}(\Lambda_b \rightarrow pV) = \frac{G_F}{\sqrt{2}} m_V f_V \varepsilon^{\mu*} \alpha_V \langle p | \bar{u} \gamma_\mu (1 - \gamma_5) b | \Lambda_b \rangle$$

$$\alpha_V = V_{ub} V_{uq}^* a_1 - V_{tb} V_{tq}^* a_4$$

$$\mathcal{R}_{\rho K^*} \equiv \frac{\mathcal{B}(\Lambda_b \rightarrow p\rho^-)}{\mathcal{B}(\Lambda_b \rightarrow pK^{*-})} = \frac{f_\rho^2}{f_{K^*}^2} \frac{|\alpha_\rho|^2 + |\alpha_{\bar{\rho}}|^2}{|\alpha_{K^*}|^2 + |\alpha_{\bar{K}^*}|^2}$$

$$\mathcal{A}_{CP}(\Lambda_b \rightarrow pV) = \frac{|\alpha_V|^2 - |\alpha_{\bar{V}}|^2}{|\alpha_V|^2 + |\alpha_{\bar{V}}|^2}$$

$$\mathcal{B}(\Lambda_b \rightarrow pK^{*-}) = (2.5 \pm 0.5) \times 10^{-6}$$

$$\mathcal{B}(\Lambda_b \rightarrow p\rho^-) = (11.4 \pm 2.1) \times 10^{-6}$$

$$\mathcal{R}_{\rho K^*} = 4.6 \pm 0.5$$

$$\mathcal{A}_{CP}(\Lambda_b \rightarrow pK^{*-}) = (19.6 \pm 1.6)\%$$

$$\mathcal{A}_{CP}(\Lambda_b \rightarrow p\rho^-) = (-3.7 \pm 0.3)\%$$

• Summary:

	our result	pQCD ¹	data
$10^6 \mathcal{B}(\Lambda_b \rightarrow pK^-)$	$4.8 \pm 0.7 \pm 0.1 \pm 0.3$	$2.0_{-1.3}^{+1.0}$	4.9 ± 0.9^2
$10^6 \mathcal{B}(\Lambda_b \rightarrow p\pi^-)$	$4.2 \pm 0.6 \pm 0.4 \pm 0.2$	$5.2_{-1.9}^{+2.5}$	4.1 ± 0.8^2
$10^6 \mathcal{B}(\Lambda_b \rightarrow pK^{*-})$	$2.5 \pm 0.3 \pm 0.2 \pm 0.3$	—	—
$10^6 \mathcal{B}(\Lambda_b \rightarrow p\rho^-)$	$11.4 \pm 1.6 \pm 1.2 \pm 0.6$	—	—
$10^2 \mathcal{A}_{CP}(\Lambda_b \rightarrow pK^-)$	$5.8 \pm 0.2 \pm 0.1$	-5_{-5}^{+26}	$-10 \pm 8 \pm 4^3$ ($-2.0 \pm 1.3 \pm 1.9^4$)
$10^2 \mathcal{A}_{CP}(\Lambda_b \rightarrow p\pi^-)$	$-3.9 \pm 0.2 \pm 0.0$	-31_{-1}^{+43}	$6 \pm 7 \pm 3^3$ ($-3.5 \pm 1.7 \pm 2.0^4$)
$10^2 \mathcal{A}_{CP}(\Lambda_b \rightarrow pK^{*-})$	$19.6 \pm 1.3 \pm 1.0$	—	—
$10^2 \mathcal{A}_{CP}(\Lambda_b \rightarrow p\rho^-)$	$-3.7 \pm 0.3 \pm 0.0$	—	—

¹ PRD80, 034011 (2009).

² PDG (2014)

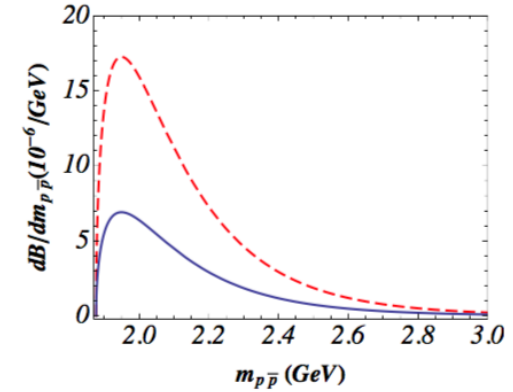
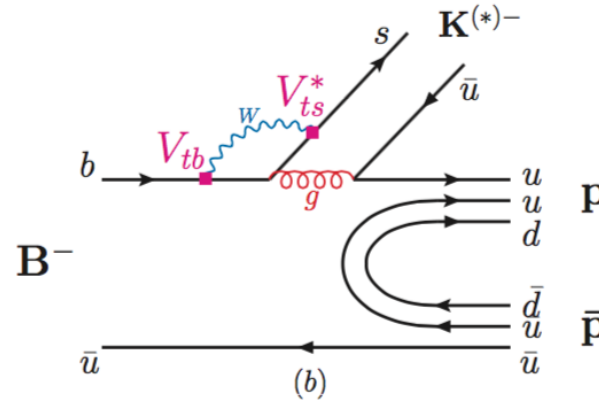
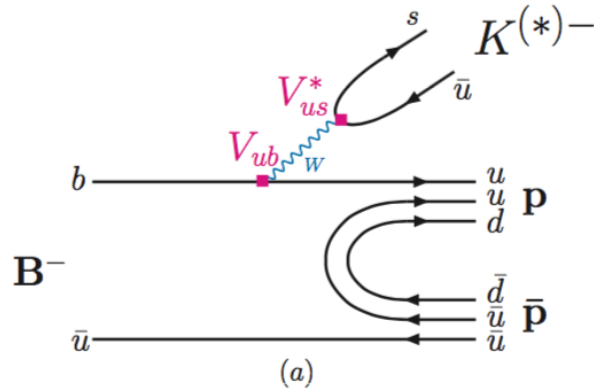
³ CDF, PRL106, 181802 (2011); 113, 242001 (2014).

⁴ LHCb, PLB787, 124 (2018).

$$A_{CP}^{pK^-} - A_{CP}^{p\pi^-} = 0.014 \pm 0.022 \pm 0.010,$$

$$A_{CP}(\Lambda_b^0 \rightarrow \bar{K}^0 p\pi^-) = 0.22 \pm 0.13 \text{ (stat)} \pm 0.03 \text{ (syst)}. \text{ LHCb JHEP 1404 (2014) 087}$$

$$B^- \rightarrow p\bar{p}K^{(*)-}$$



$$\mathcal{A}_K = i \frac{G_F}{\sqrt{2}} m_b f_K [\alpha_K \langle p\bar{p} | \bar{u}b | B^- \rangle + \beta_K \langle p\bar{p} | \bar{u}\gamma_5 b | B^- \rangle]$$

$$\mathcal{A}_{K^*} = \frac{G_F}{\sqrt{2}} m_{K^*} f_{K^*} \varepsilon^\mu \alpha_{K^*} \langle p\bar{p} | \bar{u}\gamma_\mu (1 - \gamma_5) b | B^- \rangle$$

$$\mathcal{B}(B^- \rightarrow p\bar{p}(K^-, K^{*-})) = (5.8 \pm 1.7, 2.2 \pm 0.6) \times 10^{-6}$$

Threshold effect:

Sharply raising peak around $m_{p\bar{p}} \simeq m_p + m_{\bar{p}}$

$$A_{CP}(M) = \frac{\Gamma(B^- \rightarrow p\bar{p}M^-) - \Gamma(B^+ \rightarrow p\bar{p}M^+)}{\Gamma(B^- \rightarrow p\bar{p}M^-) + \Gamma(B^+ \rightarrow p\bar{p}M^+)}$$

$$A_{CP}(K) \simeq \frac{|\alpha_K|^2 - |\bar{\alpha}_K|^2}{|\alpha_K|^2 + |\bar{\alpha}_K|^2} \quad (\alpha_K \gg \beta_K)$$

$$A_{CP}(K^*) = \frac{|\alpha_{K^*}|^2 - |\bar{\alpha}_{K^*}|^2}{|\alpha_{K^*}|^2 + |\bar{\alpha}_{K^*}|^2}$$

Hadronic uncertainties eliminated!

- Direct CP violation in $B \rightarrow p\bar{p}M$

Geng, Hsiao, Ng, PRL98, 011801 (2007)

$A_{CP}(M)$	$A_{CP}(K^{*\pm})$	$A_{CP}(K^\pm)$	$A_{CP}(\pi^\pm)$
Our result (2007)	0.22 ± 0.04	0.06 ± 0.01	-0.06
BELLE (2004)	—	-0.05 ± 0.11	—
BABAR (2005)	—	-0.16 ± 0.09	—
BABAR (2007)	0.32 ± 0.14	—	0.04 ± 0.07
BELLE (2008)	-0.01 ± 0.20	-0.02 ± 0.05	-0.17 ± 0.11
PDG (2014)	0.21 ± 0.16	-0.16 ± 0.07	0 ± 0.04
LHCb* (2014)	—	0.021 ± 0.020	-0.041 ± 0.039

* PRL113, 141801 (2014)

$\mathcal{B}_b \rightarrow \mathcal{B}_n M$	$\mathcal{B} \times 10^6$	$\mathcal{A}_{CP} \times 10^2$
$\Lambda_b \rightarrow p\pi^-$	$4.25_{-0.48}^{+1.04} \pm 0.74 \pm 0.56$	$-3.9_{-0.0}^{+0.0} \pm 0.4$
$\Lambda_b \rightarrow pK^-$	$4.49_{-0.39}^{+0.84} \pm 0.26 \pm 0.59$	$6.7_{-0.2}^{+0.3} \pm 0.3$
$\Lambda_b \rightarrow n\pi^0$	$0.10_{-0.03}^{+0.03} \pm 0.01 \pm 0.01$	$8.0_{-1.4}^{+1.2} \pm 0.3$
$\Lambda_b \rightarrow n\bar{K}^0$	$4.61_{-0.58}^{+1.31} \pm 0.31 \pm 0.61$	$1.1_{-0.0}^{+0.0} \pm 0.0$
$\Lambda_b \rightarrow \Lambda\pi^0$	$(3.4_{-0.4}^{+0.8} \pm 0.1 \pm 0.4) \times 10^{-2}$	$0.0_{-0.0}^{+0.0} \pm 0.0$
$\Lambda_b \rightarrow \Lambda K^0$	$(9.4_{-3.8}^{+2.3} \pm 0.4 \pm 1.3) \times 10^{-3}$	$0.2_{-0.0}^{+0.1} \pm 0.0$

$$\mathcal{A} = T e^{i\delta_W} + P e^{i\delta_S}$$

$$R = P/T$$

$$\mathcal{A}_{CP} = \frac{2R \sin \delta_W \sin \delta_S}{1 + 2R \cos \delta_W \cos \delta_S + R^2}$$

$\mathcal{B}_b \rightarrow \mathcal{B}_n M$	$\mathcal{B} \times 10^6$	$\mathcal{A}_{CP} \times 10^2$
$\Lambda_b \rightarrow p\rho^-$	$11.03_{-1.25}^{+2.72} \pm 1.97 \pm 1.46$	$-3.8_{-0.0}^{+0.0} \pm 0.4$
$\Lambda_b \rightarrow pK^{*-}$	$2.86_{-0.29}^{+0.62} \pm 0.11 \pm 0.51$	$19.7_{-0.3}^{+0.4} \pm 1.4$
$\Lambda_b \rightarrow n\rho^0$	$0.18_{-0.09}^{+0.09} \pm 0.02 \pm 0.02$	$14.0_{-1.8}^{+1.8} \pm 1.0$
$\Lambda_b \rightarrow n\omega$	$0.22_{-0.10}^{+0.16} \pm 0.03 \pm 0.03$	$-18.2_{-4.2}^{+24.4} \pm 1.6$
$\Lambda_b \rightarrow n\phi$	$0.02_{-0.02}^{+0.17} \pm 0.00 \pm 0.00$	$-8.8_{-5.1}^{+7.4} \pm 0.3$
$\Lambda_b \rightarrow n\bar{K}^{*0}$	$3.09_{-0.67}^{+1.57} \pm 0.21 \pm 0.41$	$1.3_{-0.1}^{+0.1} \pm 0.0$
$\Lambda_b \rightarrow \Lambda\rho^0$	$(9.5_{-1.3}^{+3.0} \pm 0.4 \pm 1.3) \times 10^{-2}$	$2.3_{-0.8}^{+0.7} \pm 0.2$
$\Lambda_b \rightarrow \Lambda\omega$	$0.71_{-0.70}^{+1.59} \pm 0.04 \pm 0.09$	$3.6_{-4.0}^{+4.8} \pm 0.2$
$\Lambda_b \rightarrow \Lambda\phi$	$1.77_{-1.68}^{+1.65} \pm 0.12 \pm 0.23$	$1.4_{-0.1}^{+0.7} \pm 0.1$
$\Lambda_b \rightarrow \Lambda K^{*0}$	$(9.2_{-2.0}^{+4.7} \pm 0.4 \pm 1.2) \times 10^{-2}$	$1.3_{-0.1}^{+0.1} \pm 0.0$
$\Lambda_b \rightarrow n\eta$	$(6.9_{-2.4}^{+2.7} \pm 0.9 \pm 0.9) \times 10^{-2}$	$-16.8_{-2.1}^{+2.1} \pm 1.3$
$\Lambda_b \rightarrow n\eta'$	$(4.2_{-1.8}^{+1.8} \pm 0.6 \pm 0.6) \times 10^{-2}$	$-15.7_{-5.6}^{+4.0} \pm 1.3$
$\Lambda_b \rightarrow \Lambda\eta$	$1.59_{-0.17}^{+0.38} \pm 0.11 \pm 0.21$	$0.4_{-0.2}^{+0.2} \pm 0.0$
$\Lambda_b \rightarrow \Lambda\eta'$	$1.90_{-0.23}^{+0.68} \pm 0.13 \pm 0.25$	$1.6_{-0.1}^{+0.1} \pm 0.1$

CPV in internal W-emission dominated baryonic B decays

$$A = Te^{i\delta_W} + Pe^{i\delta_S}$$

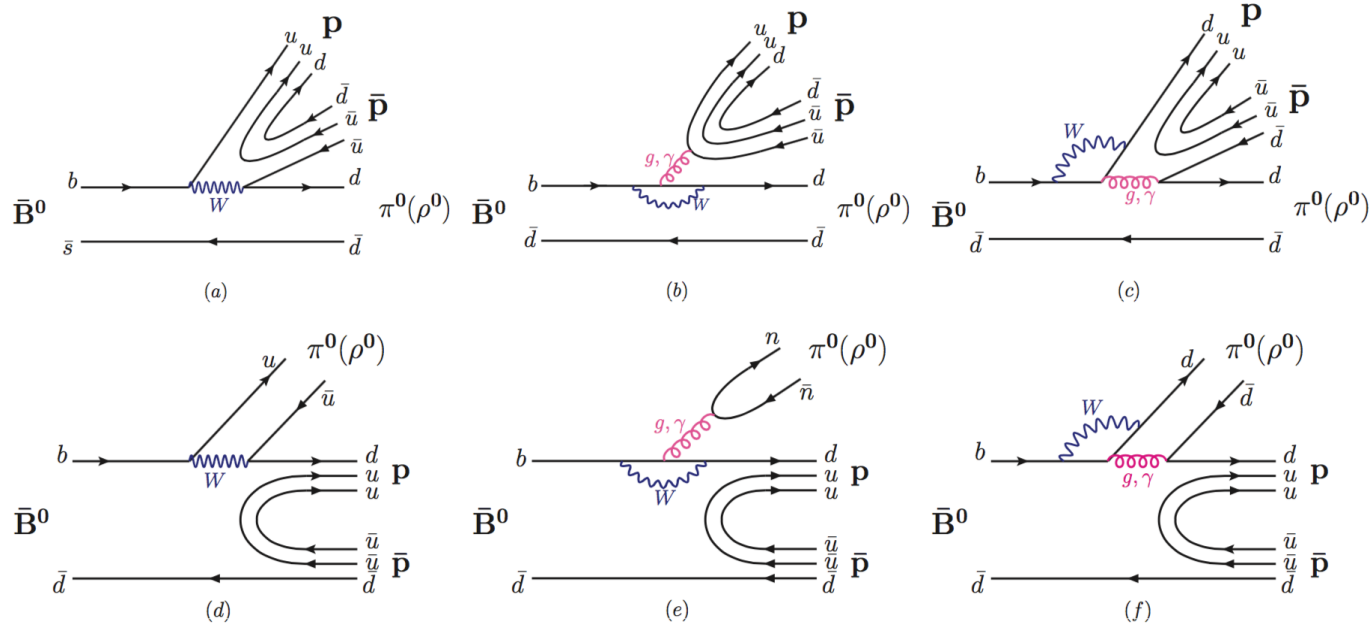
$$R = P/T$$

$$A_{CP} = \frac{2R \sin \delta_W \sin \delta_S}{1 + 2R \cos \delta_W \cos \delta_S + R^2}$$

$$\mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\pi^0) = (5.0 \pm 1.8 \pm 0.6) \times 10^{-7},$$

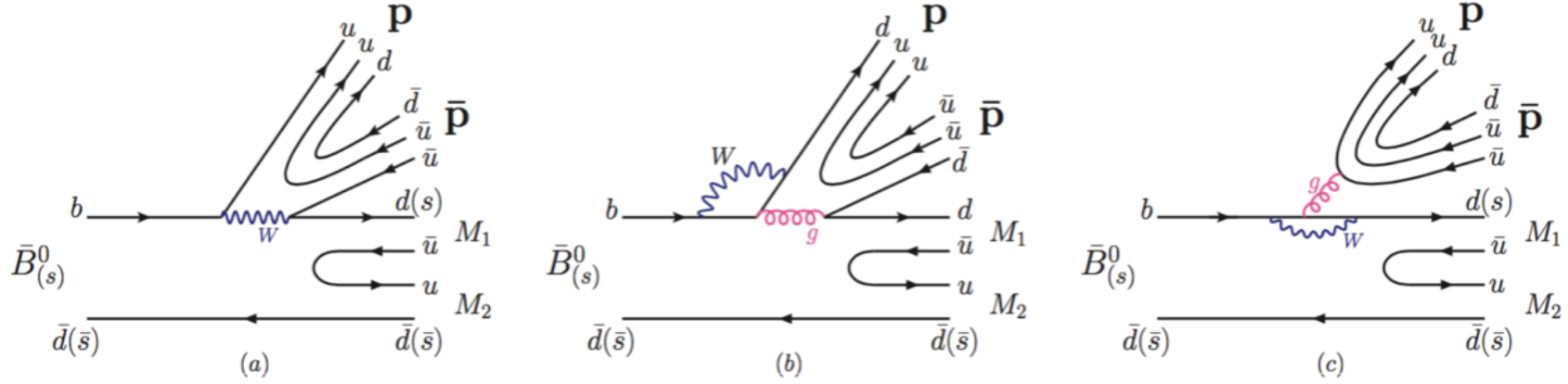
$$\mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\pi^+\pi^-) = (2.7 \pm 0.1 \pm 0.1 \pm 0.2) \times 10^{-6},$$

$$\mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\pi^0) = (5.0 \pm 1.8 \pm 0.6) \times 10^{-7}$$



$$\begin{aligned} \mathcal{A}_1(X_M) &= \frac{G_F}{\sqrt{2}} \left\{ \left[\langle p\bar{p} | \bar{u} \gamma^\mu (\alpha_2^+ - \alpha_2^- \gamma_5) u | 0 \rangle + \langle p\bar{p} | \bar{d} \gamma^\mu (\alpha_3^+ - \alpha_3^- \gamma_5) d | 0 \rangle \right] \right. \\ &\quad \left. \times \langle X_M | \bar{d} \gamma_\mu (1 - \gamma_5) b | \bar{B}^0 \rangle + \alpha_6 \langle p\bar{p} | \bar{d} (1 + \gamma_5) d | 0 \rangle \langle X_M | \bar{d} (1 - \gamma_5) b | \bar{B}^0 \rangle \right\}, \\ \mathcal{A}_2(X_M) &= \frac{G_F}{\sqrt{2}} \left\{ \left[\langle X_M | \bar{u} \gamma^\mu (\alpha_2^+ - \alpha_2^- \gamma_5) u | 0 \rangle + \langle X_M | \bar{d} \gamma^\mu (\alpha_3^+ - \alpha_3^- \gamma_5) d | 0 \rangle \right] \right. \\ &\quad \left. \times \langle p\bar{p} | \bar{d} \gamma_\mu (1 - \gamma_5) b | \bar{B}^0 \rangle + \alpha_6 \langle X_M | \bar{d} (1 + \gamma_5) d | 0 \rangle \langle p\bar{p} | \bar{d} (1 - \gamma_5) b | \bar{B}^0 \rangle \right\}, \end{aligned}$$

$$\mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\pi^+\pi^-) = (2.7 \pm 0.1 \pm 0.1 \pm 0.2) \times 10^{-6}$$



$$\begin{aligned} \mathcal{A}_1(\bar{B}^0_{(s)} \rightarrow p\bar{p}M_1M_2) = & \frac{G_F}{\sqrt{2}} \left\{ \left[\langle p\bar{p} | \alpha_+^q (\bar{u}u)_V - \alpha_-^q (\bar{u}u)_A | 0 \rangle + \langle p\bar{p} | \beta_+^q (\bar{d}d)_V - \beta_-^q (\bar{d}d)_A | 0 \rangle \right. \right. \\ & \left. \left. + (\alpha_4^q - \alpha_{10}^q/2) \langle p\bar{p} | (\bar{q}q)_{V-A} | 0 \rangle \right] \langle M_1M_2 | (\bar{q}b)_{V-A} | \bar{B}^0_{(s)} \rangle \right. \\ & \left. + \alpha_6^q \langle p\bar{p} | (\bar{q}q)_{S+P} | 0 \rangle \langle M_1M_2 | (\bar{q}b)_{S-P} | \bar{B}^0_{(s)} \rangle \right\}, \end{aligned}$$

- $B \rightarrow M_1 M_2$ transition form factors

$$\langle M_1 M_2 | \bar{q}_1 \gamma_\mu (1 - \gamma_5) b | B \rangle =$$

$$h \epsilon_{\mu\nu\alpha\beta} p_B^\nu p^\alpha (p_{M_2} - p_{M_1})^\beta + i r q_\mu + i w_+ p_\mu + i w_- (p_{M_2} - p_{M_1})$$

$$h = \frac{C_h}{t^2}, \quad w_- = \frac{D_{w_-}}{t^2}$$

Chua, Hou, Shiau and Tsai,

“Evidence for factorization in three-body anti- $B \rightarrow D^{(*)} K^- K^0$ decays,”

PRD67, 034012 (2003); EPJC33, S253 (2004).

$$(C_h, C_{w_-})|_{B \rightarrow \pi\pi} = (3.6 \pm 0.3, 0.7 \pm 0.2) \text{ GeV}^3$$

$$(C_h, C_{w_-})|_{B \rightarrow KK(K\pi)} = (-38.9 \pm 3.3, 14.2 \pm 2.3) \text{ GeV}^3$$

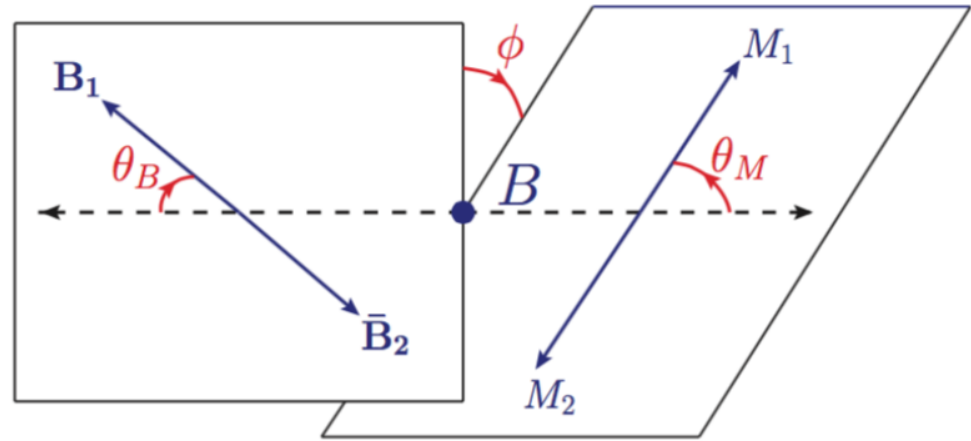
phase space

$$d\Gamma = \frac{|\bar{\mathcal{A}}|^2}{4(4\pi)^6 m_B^3} X \alpha_{\mathbf{B}} \alpha_{\mathbf{M}} ds dt d\cos\theta_{\mathbf{B}} d\cos\theta_{\mathbf{M}} d\phi$$

$$X = \left[\frac{1}{4} (m_B^2 - s - t)^2 - st \right]^{1/2},$$

$$\alpha_{\mathbf{B}} = \frac{1}{t} \lambda^{1/2}(t, m_{\mathbf{B}_1}^2, m_{\bar{\mathbf{B}}_2}^2),$$

$$\alpha_{\mathbf{M}} = \frac{1}{s} \lambda^{1/2}(s, m_{M_1}^2, m_{M_2}^2),$$



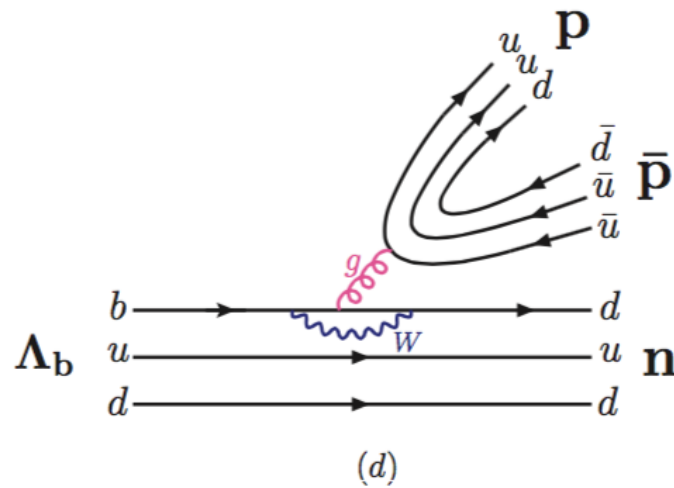
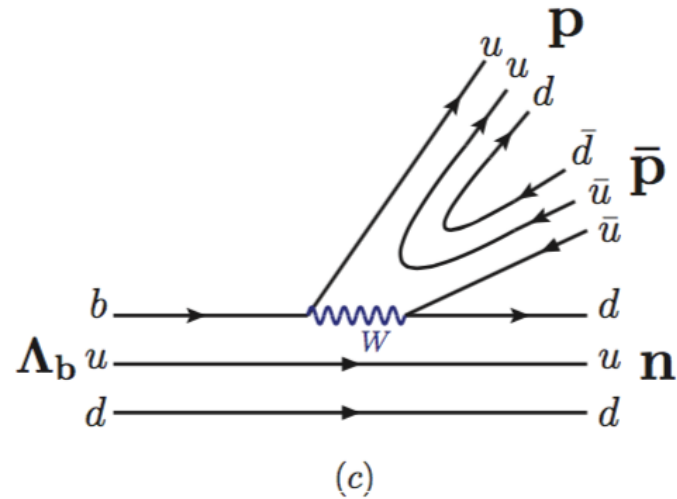
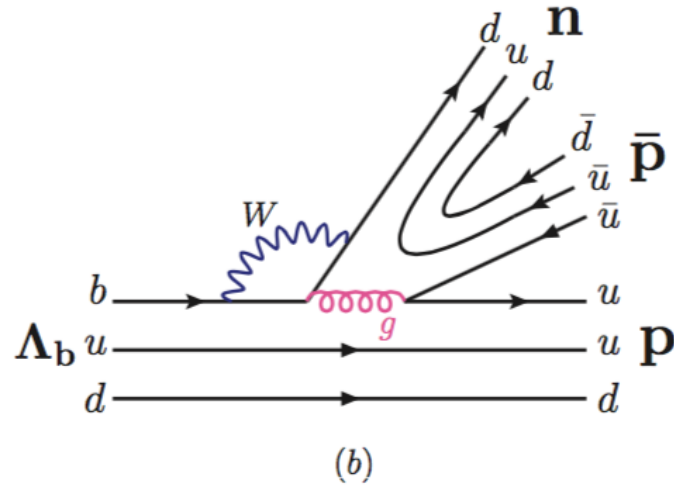
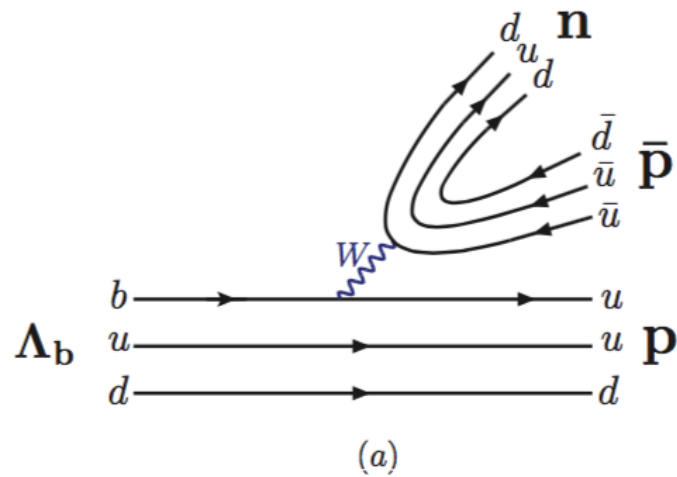
$$\lambda(a, b, c) = a^2 + b^2 + c^2 - 2ab - 2bc - 2ca,$$

$$(m_{M_1} + m_{M_2})^2 \leq s \leq (m_B - \sqrt{t})^2, \quad (m_{\mathbf{B}_1} + m_{\bar{\mathbf{B}}_2})^2 \leq t \leq (m_B - m_{M_1} - m_{M_2})^2,$$

$$0 \leq \theta_{\mathbf{B}}, \theta_{\mathbf{M}} \leq \pi, \quad 0 \leq \phi \leq 2\pi.$$

	our result	data
$10^7 \mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\pi^0)$	$5.5 \pm 0.3 \pm 1.0$	5.0 ± 1.9 [23]
$10^7 \mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\rho^0)$	$1.9 \pm 0.1 \pm 0.4$	—
$10^6 \mathcal{B}(\bar{B}^0 \rightarrow p\bar{p}\pi^+\pi^-)$	$2.7 \pm 0.2 \pm 0.7$	2.7 ± 0.2 [18]
$\mathcal{A}_{CP}(\bar{B}^0 \rightarrow p\bar{p}\pi^0)$	$(-16.0 \pm 1.6 \pm 1.7)\%$	—
$\mathcal{A}_{CP}(\bar{B}^0 \rightarrow p\bar{p}\rho^0)$	$(-12.2 \pm 1.2 \pm 1.7)\%$	—
$\mathcal{A}_{CP}(\bar{B}^0 \rightarrow p\bar{p}\pi^+\pi^-)$	$(-11.5 \pm 1.2 \pm 1.4)\%$	—

The $\Lambda_b^0 \rightarrow p\bar{p}n$ decay



$$\mathcal{A}(\Lambda_b^0 \rightarrow p\bar{p}n) \simeq \frac{G_F}{\sqrt{2}} V_{ub} V_{ud}^* a_1 \langle n\bar{p} | (\bar{d}u)_{V-A} | 0 \rangle \langle p | (\bar{u}b)_{V-A} | \Lambda_b^0 \rangle$$

$$\mathcal{A}(\Lambda_b^0 \rightarrow p\bar{p}n) \simeq \frac{G_F}{\sqrt{2}} V_{ub} V_{ud}^* a_1 \langle n\bar{p} | (\bar{d}u)_{V-A} | 0 \rangle \langle p | (\bar{u}b)_{V-A} | \Lambda_b^0 \rangle$$

Theoretical tools, well developed!

$$\langle n\bar{p} | \bar{d}\gamma_\mu(1 - \gamma_5)u | 0 \rangle = \bar{u}_n [F_1\gamma_\mu - (g_A\gamma_\mu + \frac{h_A}{m_n+m_{\bar{p}}}q_\mu)\gamma_5] v_{\bar{p}}$$

$$\langle p | \bar{u}\gamma_\mu(1 - \gamma_5)b | \Lambda_b \rangle = \bar{u}_p [f_1\gamma_\mu - g_1\gamma_\mu\gamma_5] u_{\Lambda_b}$$

$$F_1(g_A) = C_{F_1(g_A)}/t^2 [\ln(t/\Lambda_0^2)]^{-\gamma}$$

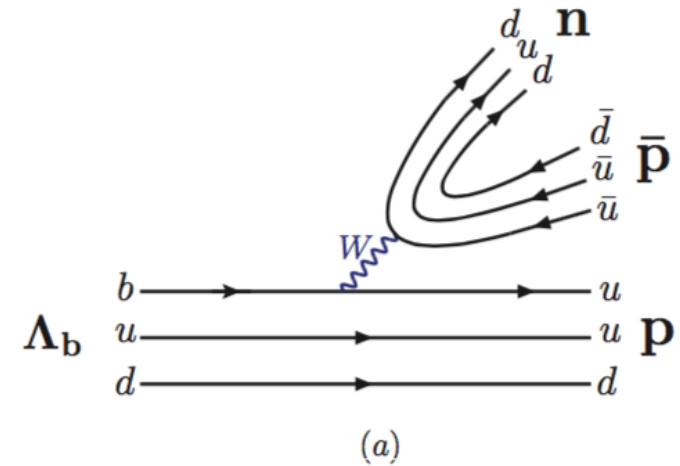
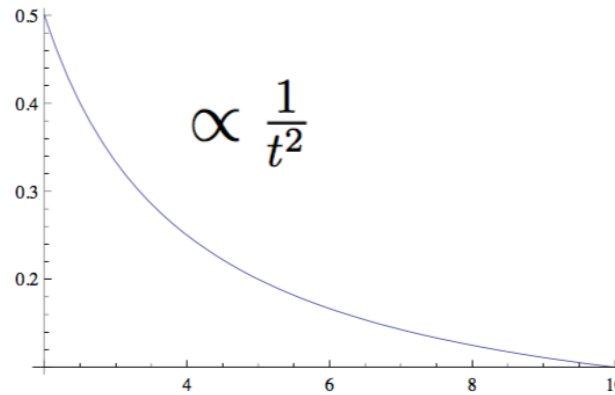
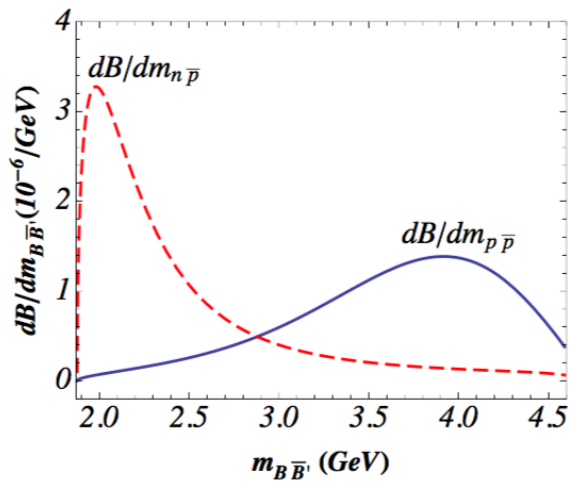
$$h_A = C_{h_A}/t^2, \gamma = 2.148, \Lambda_0 = 0.3 \text{ GeV and } t \equiv q^2$$

$$f_1(g_1) = C_{f_1(g_1)}/(1 - t/m_{\Lambda_b}^2)^2$$

Numerical results

$$\mathcal{B}(\Lambda_b^0 \rightarrow p\bar{p}n) = (2.0_{-0.2}^{+0.3} \pm 0.1 \pm 0.1) \times 10^{-6}$$

\mathcal{A}_{CP} and \mathcal{A}_T estimated to be around -4%, undetectable due to n.



$d\mathcal{B}/dm_{n\bar{p}}$, threshold effect:

sharply raising peak around $m_{n\bar{p}} \simeq m_n + m_{\bar{p}}$

for the $n\bar{p}$ production: $F_1(g_A) \propto \frac{1}{t^2} = 1/(p_n + p_{\bar{p}})^2$

reshape the phase space

$p\bar{p}$ and $n\bar{n}$ not produced in pairs: NO threshold effect

CPV in $\mathbf{B}_c \rightarrow \mathbf{B}M$

- Abundant measurements for $\Lambda_c^+ \rightarrow \mathbf{B}M$ at BESIII.

More data coming.

Theoretical study should be renewed also;

besides, giving predictions.

- Non-factorizable effects, significant in \mathbf{B}_c decays.
- The search for CP violation.

$$\begin{aligned}\Delta\mathcal{A}_{CP} &\equiv \mathcal{A}_{CP}(D^0 \rightarrow K^+K^-) - \mathcal{A}_{CP}(D^0 \rightarrow \pi^+\pi^-) \\ &= (-15.4 \pm 2.9) \times 10^{-4} \text{ (LHCb)}.\end{aligned}$$

Future studies

- $\Lambda_b^0 \rightarrow p\bar{p}\Lambda$, $\Lambda_b^0 \rightarrow \Lambda\bar{p}\Lambda$, $\Lambda_b^0 \rightarrow \Lambda\bar{\Lambda}\Lambda$, $\Xi_b^{+,0} \rightarrow \mathbf{B}_1\bar{\mathbf{B}}_2\mathbf{B}_3$

- DCPA in $\mathbf{B}_b \rightarrow \mathbf{B}_1\bar{\mathbf{B}}_2\mathbf{B}_3$

- Time reversal violating asymmetries

via triple product correlations (rich baryon spins)

- DCPA in $\mathbf{B}_c \rightarrow \mathbf{B}M$

Thank You