

Global and local spin polarization in heavy-ion collisions

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at [HENPIC](#) online seminar, 2021-06-02

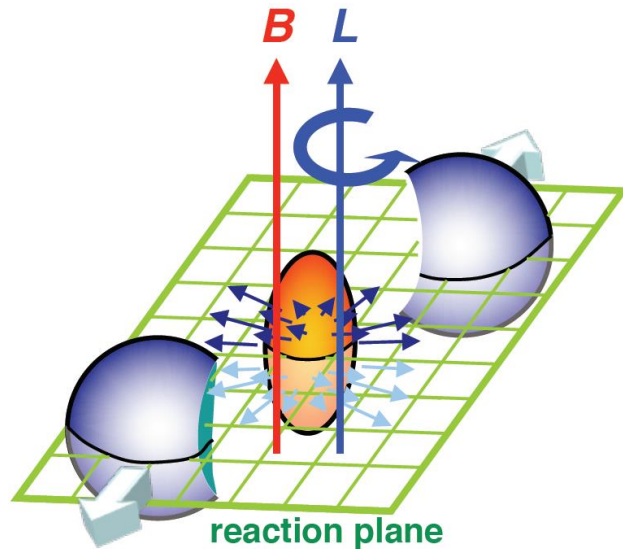
- Introduction
- Polarization from thermal vorticity
 - Global polarization
 - Local polarization puzzle
- Shear induced polarization

Introduction: spin polarization

Global Angular Momentum & Global Polarization

Orbital Angular Momentum

Large angular momentum and magnetic field in non-central heavy ion collisions



RHIC: $L = 10^5 \hbar$ @ 200 GeV & 7 fm
LHC: $L = 10^7 \hbar$ @ 2760 GeV & 7 fm

X. Xia's henpic talk

Early works on polarization

Global polarization of Λ and spin alignment of vector mesons from spin-orbital coupling

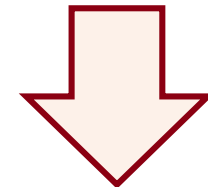
Z. T. Liang, X. N. Wang,
Phys.Rev.Lett. 94 (2005) 102301, *Phys.Lett.B* 629 (2005) 20-26

Secondary particles can be polarized in un-polarized high energy collisions

S. Voloshin [nucl-th/0410089](https://arxiv.org/abs/nucl-th/0410089)

$$\langle \vec{S}_{\vec{\omega}}; \text{hadrons} \rangle \parallel \vec{L}_{\text{QGP}}$$

Global quark polarization

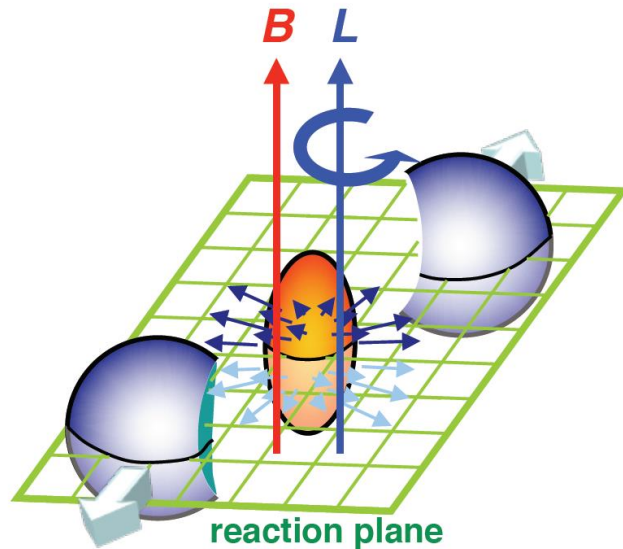


Global Λ polarization
(recombination/fragmentation)

Global Angular Momentum & Global Polarization

Orbital Angular Momentum

Large angular momentum and magnetic field in non-central heavy ion collisions



RHIC: $L = 10^5 \hbar$ @ 200 GeV
 LHC: $L = 10^7 \hbar$ @ 2760 GeV

Motivate spin polarization measurements in experiments!

X. Xia's hepnc talk

Early works on polarization

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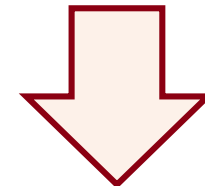
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Secondary particles can be polarized in un-polarized high energy collisions

S. Voloshin nucl-th/0410089

$$\langle \vec{S}_{\vec{\omega}}; \text{hadrons} \rangle \parallel \vec{L}_{\text{QGP}}$$

Global quark polarization



Global Λ polarization
 (recombination/fragmentation)

Polarization Measurement

'self-analyzing' of hyperon

Daughter baryon is preferentially emitted in the direction of hyperon's spin (opposite for anti-particle)

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha_H \mathbf{P}_H \cdot \mathbf{p}_p^*)$$

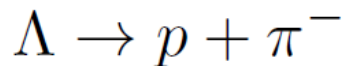
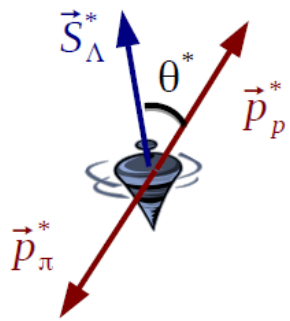
P_H : Λ polarization

\mathbf{p}_p^* : proton momentum in the Λ rest frame

α_H : Λ decay parameter

$$\alpha_\Lambda = 0.642 \pm 0.013 \rightarrow \alpha_\Lambda = 0.732 \pm 0.014$$

P.A. Zyla et al. (PDG), PTEP2020.083C01

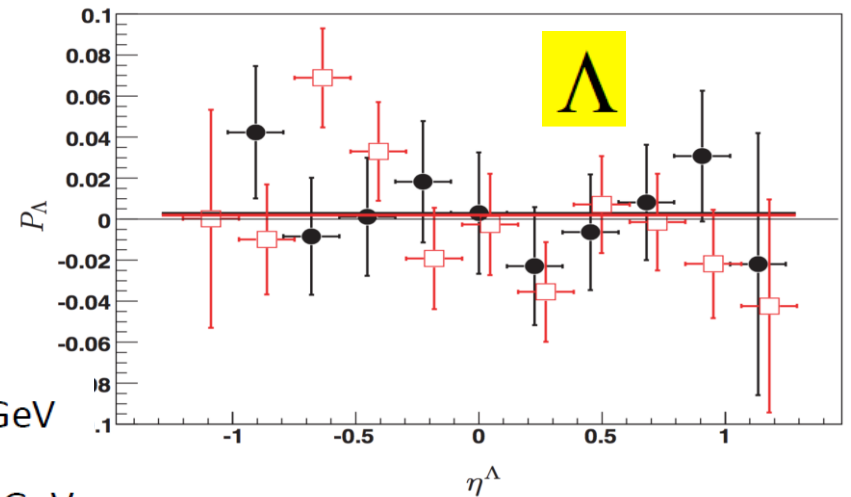


(BR: 63.9%, $c\tau \sim 7.9$ cm)

S. Voloshin and T. Niida, PRC 94.021904 (2016)

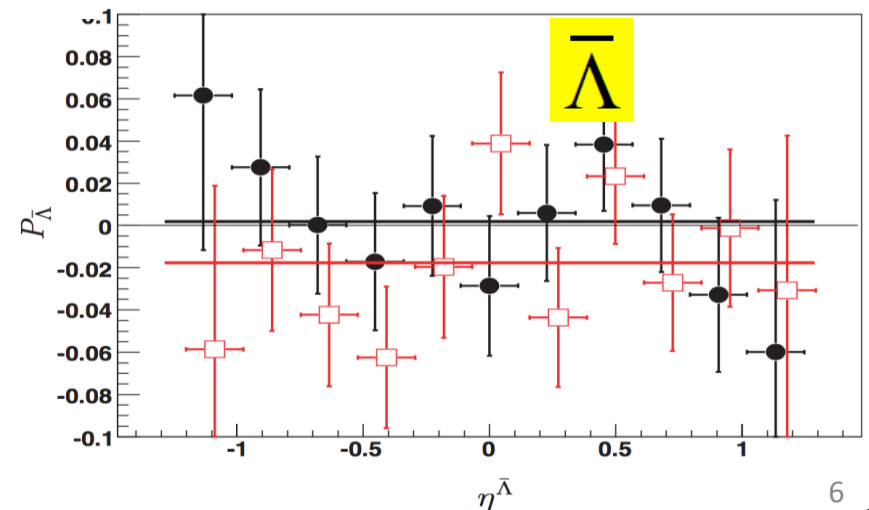
No signal at high energy

Phys. Rev. C 76, 024915 (2007)



● 200 GeV

□ 62.4 GeV



Polarization Measurement

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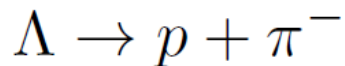
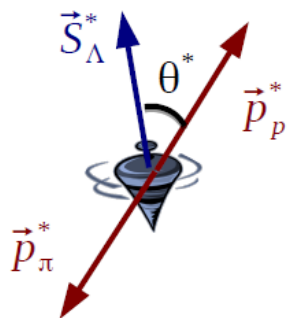
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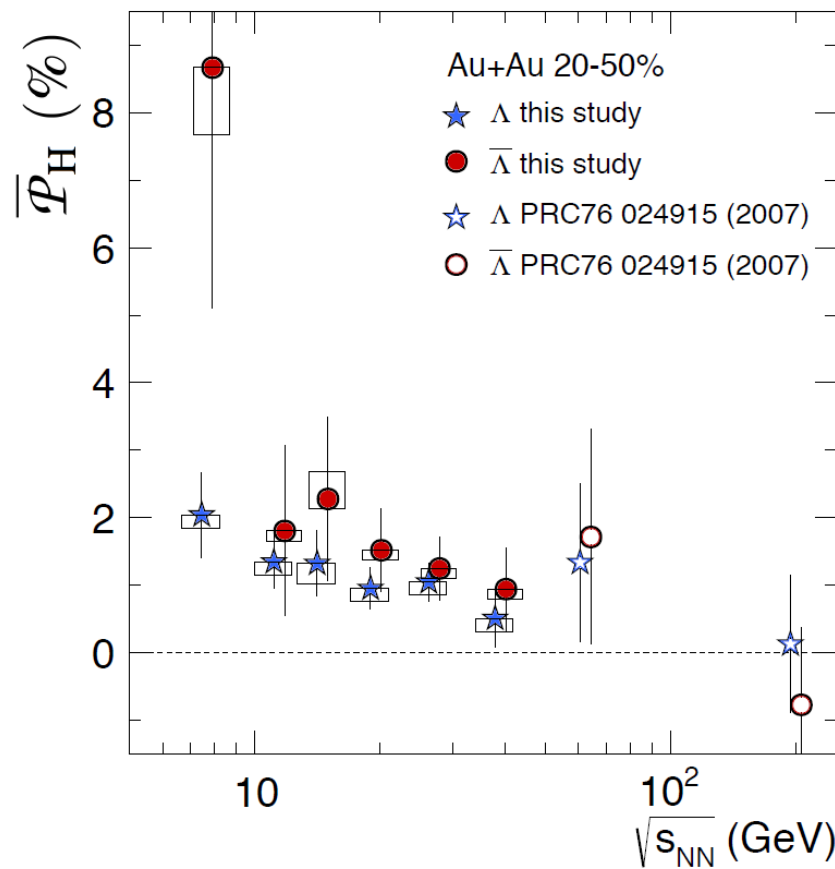


(BR: 63.9%, $c\tau \sim 7.9$ cm)

S. Voloshin and T. Niida, PRC 94.021904 (2016)

Most vortical fluid!

STAR Collaboration, Nature 548, 62 (2017)



$$\omega = (P_\Lambda + P_{\bar{\Lambda}}) k_B T / \hbar \sim 10^{22} \text{ s}^{-1}$$

Spin-orbital coupling in Condensed Matter

Gradient of spin voltage \rightarrow spin current

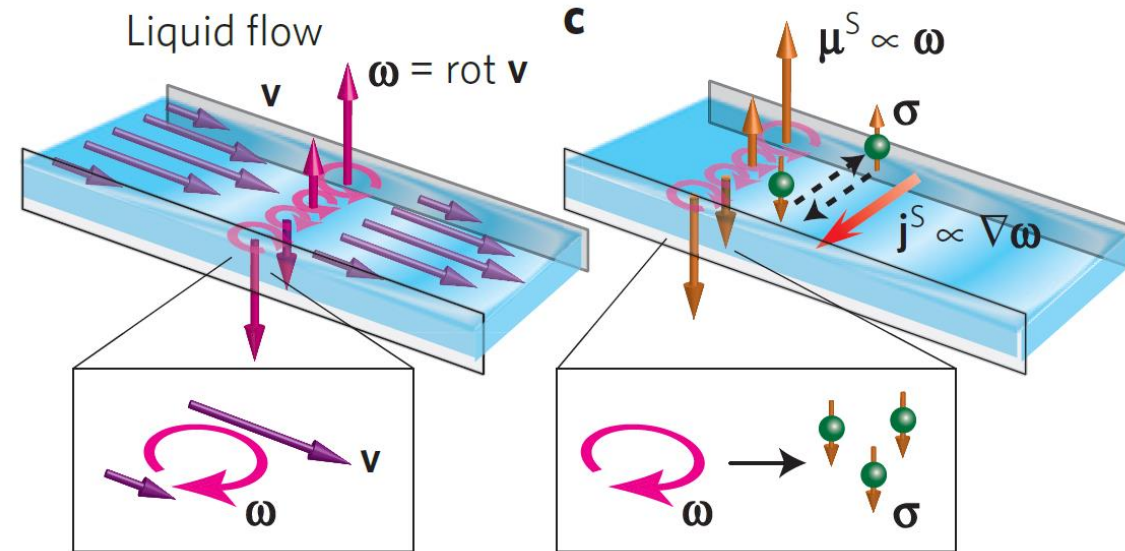
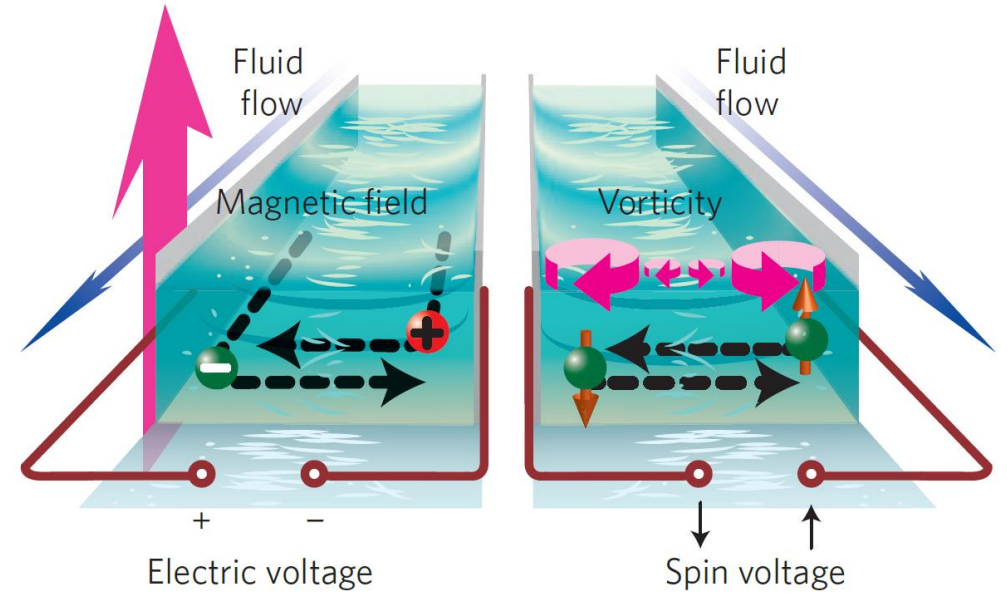
Spin voltage from Electrochemical potential:

$$\mu^S \equiv \mu_{\uparrow} - \mu_{\downarrow}$$

Diffusion equation:

$$\nabla^2 \boldsymbol{\mu}^S = \frac{1}{\lambda^2} \boldsymbol{\mu}^S - \frac{4e^2}{\sigma_0 \hbar} \xi \boldsymbol{\omega}$$

The spin current is detected by inverse spin Hall effect (ISHE)



Theoretical frameworks

Theories for spin-vorticity coupling

Early works: Polarization from global orbital angular momentum

Z. T. Liang, X. N. Wang, Phys.Rev.Lett. 94 (2005) 102301, Voloshin nucl-th/0410089

- In non-central heavy-ion collisions, L_y induce global quark polarization

$$P_q = -\pi\mu p/2E(E + m_q).$$

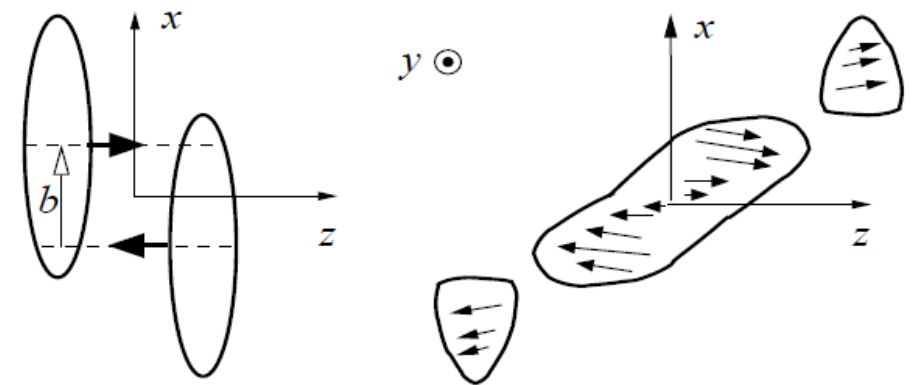
- Quark polarization transfer to final hyperon polarization via recombination (or fragmentation)

$$P_\Lambda = P_s, R_\Lambda = 3(1 - P_q^2);$$

$$P_\Sigma = (4P_q - P_s - 3P_sP_q^2)/R_\Sigma, R_\Sigma = 3 - 4P_qP_s + P_q^2;$$

$$P_\Xi = (4P_s - P_q - 3P_qP_s^2)/R_\Xi, R_\Xi = 3 - 4P_qP_s + P_s^2;$$

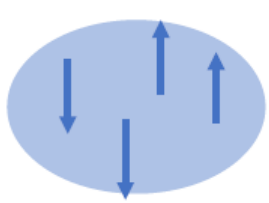
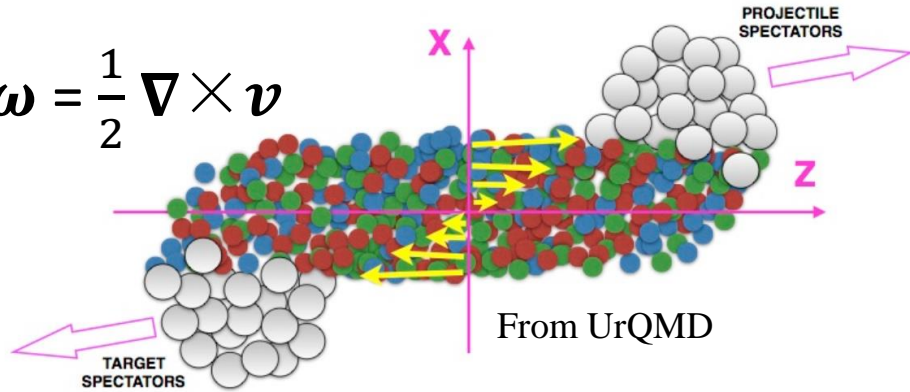
$$P_\Omega = 2P_s(5 + P_s^2)/R_\Omega, R_\Omega = 6(1 + P_s^2).$$



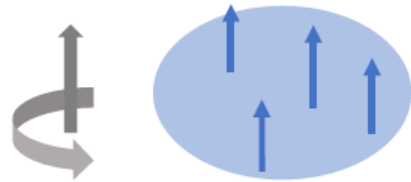
Vorticity from hydro/transport pic

Averaged vorticity $\langle \omega_y \rangle$

$$\boldsymbol{\omega} = \frac{1}{2} \nabla \times \boldsymbol{v}$$



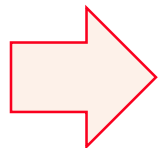
$$H = H_0 - \boldsymbol{\omega} \cdot \boldsymbol{S}$$



$$\frac{dN}{dp} \sim e^{-(H_0 - \boldsymbol{\omega} \cdot \boldsymbol{S})/T}$$

Landau & Lifshitz, Statistical Physics

$$\langle \vec{\omega}_{\text{QGP}} \rangle \parallel \vec{L}_{\text{QGP}}$$

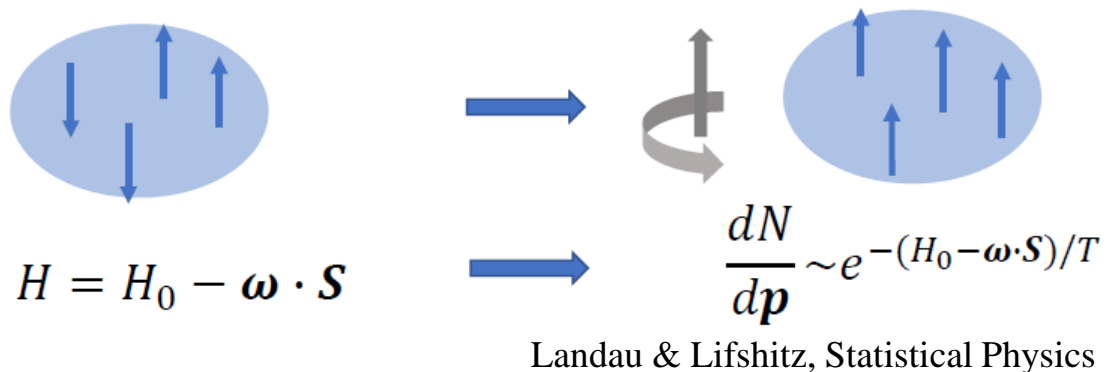
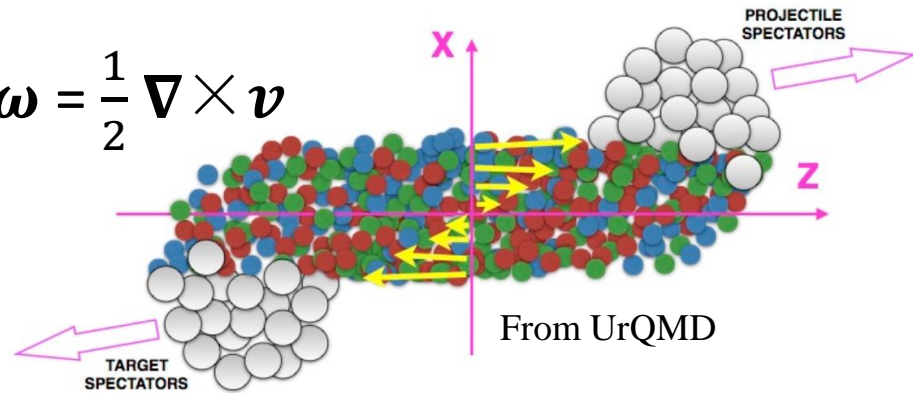


$$\langle \vec{S}_{\vec{\omega}}; \text{hadrons} \rangle \parallel \vec{L}_{\text{QGP}}$$

Vorticity from hydro/transport pic

Averaged vorticity $\langle \omega_y \rangle$

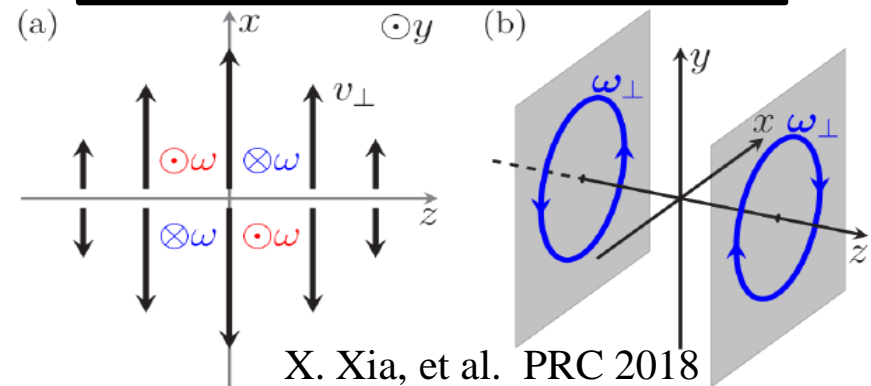
$$\boldsymbol{\omega} = \frac{1}{2} \nabla \times \mathbf{v}$$



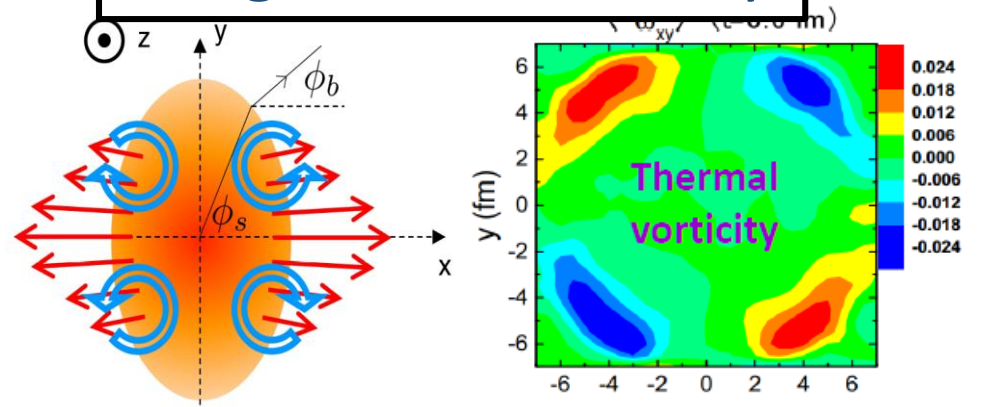
$$\langle \vec{\omega}_{\text{QGP}} \rangle \parallel \vec{L}_{\text{QGP}} \quad \longrightarrow \quad \langle \vec{S}_{\vec{\omega}}; \text{hadrons} \rangle \parallel \vec{L}_{\text{QGP}}$$

inhomogeneous expansion

Transverse vorticity



Longitudinal vorticity



Thermal vorticity induced polarization

thermal vorticity & Polarization

- Valid at global equilibrium.
- Always extrapolated to local equilibrium.

$$S^\mu(x, p) = -\frac{1}{2m} \frac{S(S+1)}{3} [1 - f(x, p)] \epsilon^{\mu\nu\rho\sigma} p_\sigma \varpi_{\nu\rho}$$

F. Becattini, et al. *Annals Phys.* 338 32 (2013)

Thermal vorticity:

$$\varpi_{\mu\nu} = -\frac{1}{2} (\partial_\mu \beta_\nu - \partial_\nu \beta_\mu)$$

$$\beta_\mu = u_\mu / T$$

See also: R. Fang, L. Pang, Q. Wang, X. Wang, *PRC* 2016

Y. Liu, K. Mameda, X. Huang, *CPC* 2020

'Spin Cooper-Frye' formula

- Integration on freeze-out hyper surface

$$S^\mu(p) = \frac{\int d\Sigma_\lambda p^\lambda f(x, p) \langle S(x, p) \rangle}{\int d\Sigma_\lambda p^\lambda f(x, p)}$$

- Boost to particle rest frame

$$S^* = S - \frac{\mathbf{p} \cdot \mathbf{S}}{E(E+m)} \mathbf{p}$$

- Normalized spin polarization

$$P^\mu(p) = \frac{1}{S} S^\mu(p)$$

Numerical simulation

thermal vorticity & Polarization

- Valid at global equilibrium.
- Always extrapolated to local equilibrium.

$$S^\mu(x, p) = -\frac{1}{2m} \frac{S(S+1)}{3} [1 - f(x, p)] \epsilon^{\mu\nu\rho\sigma} p_\sigma \overline{\omega}_{\nu\rho}$$

'Spin Cooper-Frye' formula

- Integration on freeze-out hyper surface

$$S^\mu(p) = \frac{\int d\Sigma_\lambda p^\lambda f(x, p) \langle S(x, p) \rangle}{\int d\Sigma_\lambda p^\lambda f(x, p)}$$

- Boost to particle rest frame

- Most of the calculations on market are built as:

1) hydrodynamic calculations

Hydrodynamic evolution

Freeze-out

Formula from above

2) Microscopic(transport, cascade) model calculations

Parton/hadron cascade

Coarse-graining

Formula from above

Hydrodynamic/transport models

Hydrodynamic models

PICR: Y.L. Xie, D.J. Wang, L.P. Csernai, Phys.Rev.C 95 (2017) 3, 031901, Eur.Phys.J.C 80 (2020) 1, 39

ECHO-QGP: F. Becattini, G. Inghirami, et al., Eur.Phys.J.C 75 (2015) 9, 406

AMPT + CLVisc: L.-G Pang, H. Elfner, Q. Wang and X.-N. Wang , Phys.Rev.Lett. 117 (2016) 192301

AMPT + MUSIC: BF, K. Xu, X-G, Huang, H. Song, Phys.Rev.C 103 (2021) 2, 024903

UrQMD/Glauber + vHLL: Iu. Karpenko, F. Becattini , Eur.Phys.J.C 77 (2017) 4, 213, Phys.Rev.Lett. 120 (2018) 012302

3FD (3-fluid dynamics): Yu. Ivanov, A. Soldatov, Phys. Rev. C 97, 024908 (2018)

Transport models

AMPT: Y. Jiang, J. Liao, Z. Lin, Phys.Rev.C 94 (2016) 4, 044910

D. Wei, W. Deng and X-G. Huang, Phys.Rev. C99 (2019) 014905

H. Li, L. Pang, Q. Wang and X. Xia, Phys.Rev. C96 (2017) 054908

UrQMD: O. Vitiuk, L. Bravina and E. Zabrodin, Phys.Lett.B 803 (2020) 135298

X-G. Deng, X-G. Huang, Y-G. Ma and S. Zhang, Phys.Rev.C 101 (2020) 6, 064908

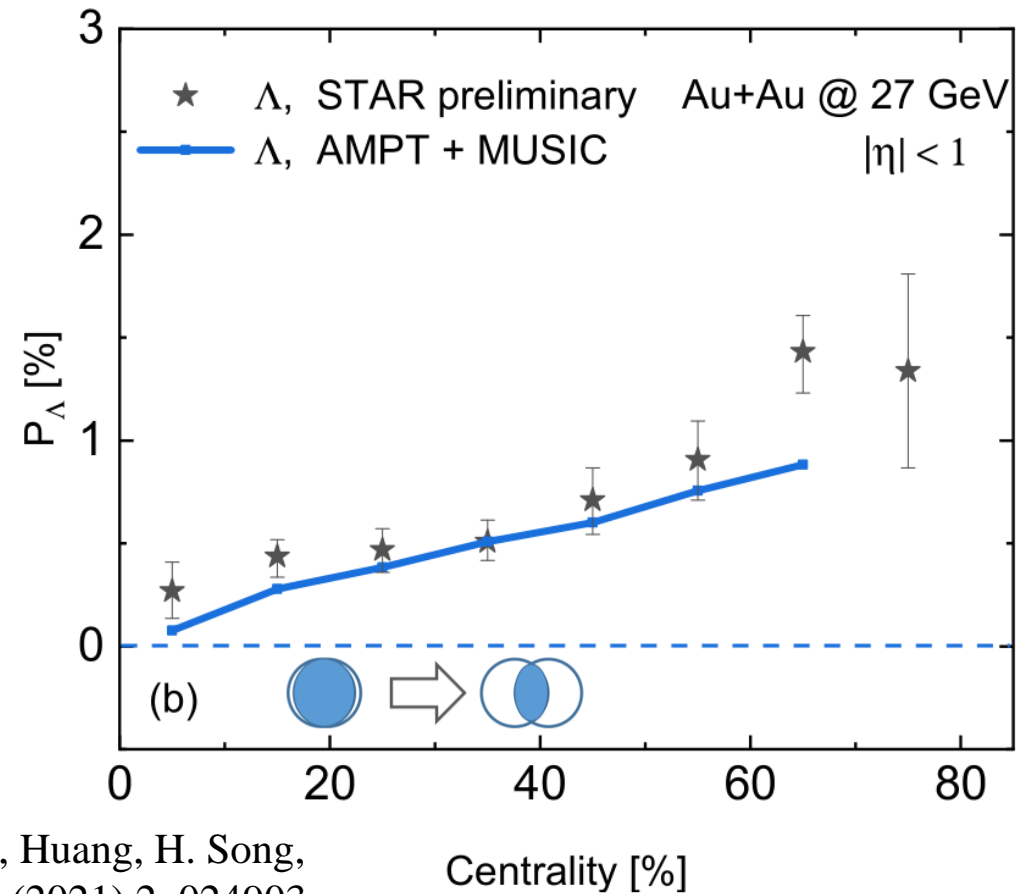
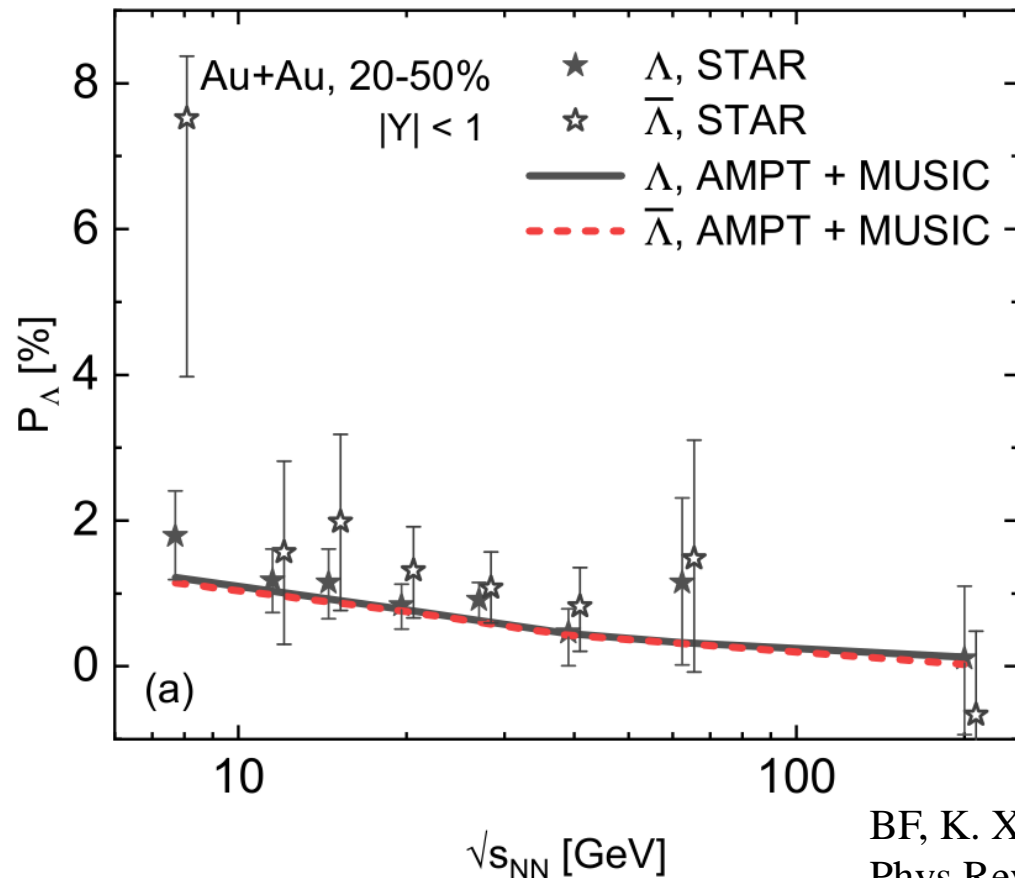
...

Global polarization

Global polarization

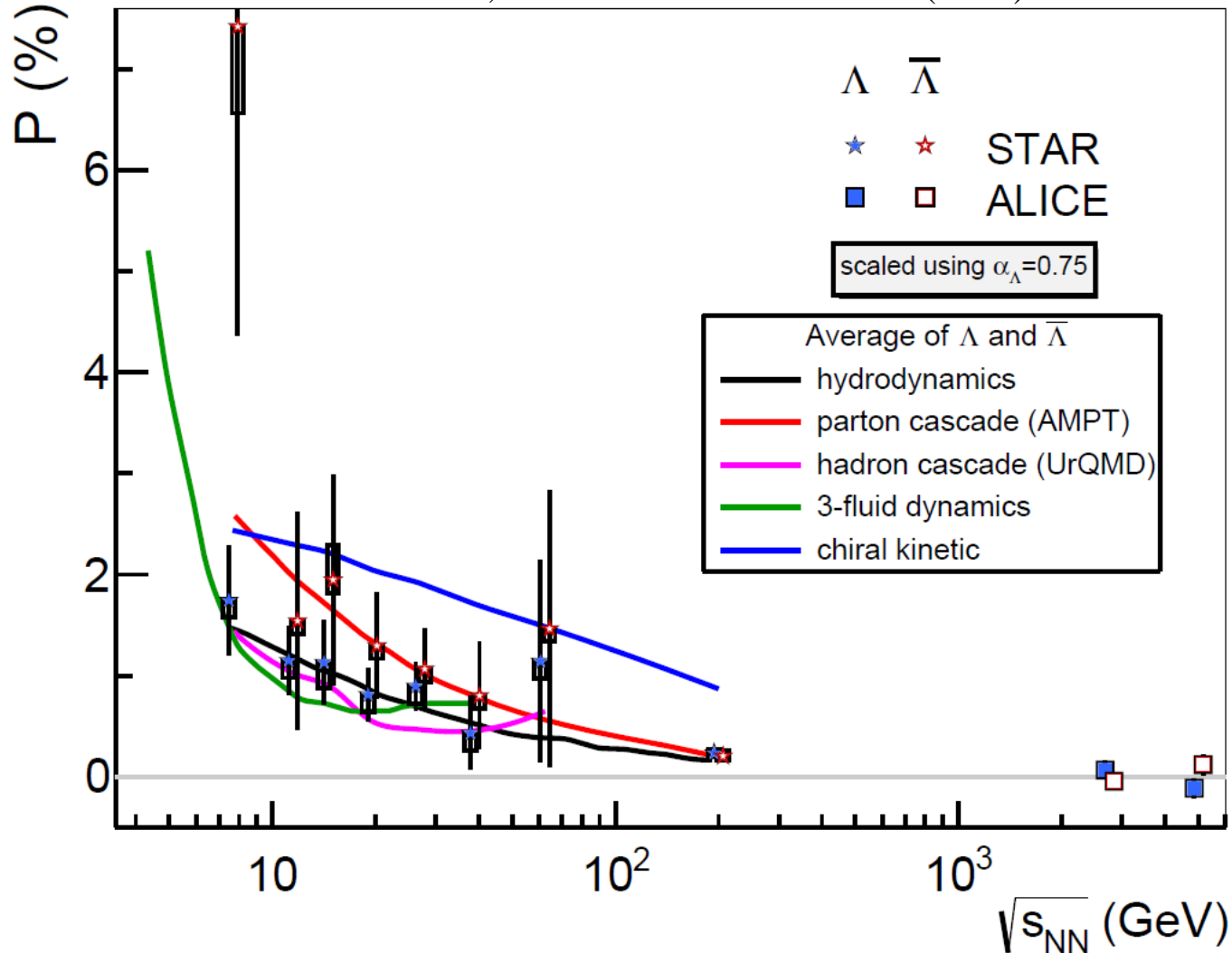
$$P^\mu = \langle P^\mu(p) \rangle = \frac{\int \frac{d^3p}{E} \int d\Sigma_\nu p^\nu f(x, p) P^\mu(x, p)}{\int \frac{d^3p}{E} \int d\Sigma_\nu p^\nu f(x, p)}$$

- Decrease with the collision energy
- $\Lambda - \bar{\Lambda}$ difference negligible



Global polarization

F. Becattini and M. Lisa, Ann.Rev.Nucl.Part.Sci. 70 (2020) 395-423



Viscous hydrodynamics:

Karpenko I, Becattini F. Eur. Phys. J. C77:213 (2017)

Partonic cascade (AMPT):

Li H, Pang L-G, Wang Q, Xia XL. Phys. Rev. C96:054908 (2017)

Hadron cascade (UrQMD):

O. Vitiuk, L. Bravina and E. Zabrodin, Phys.Lett.B 803 (2020) 135298

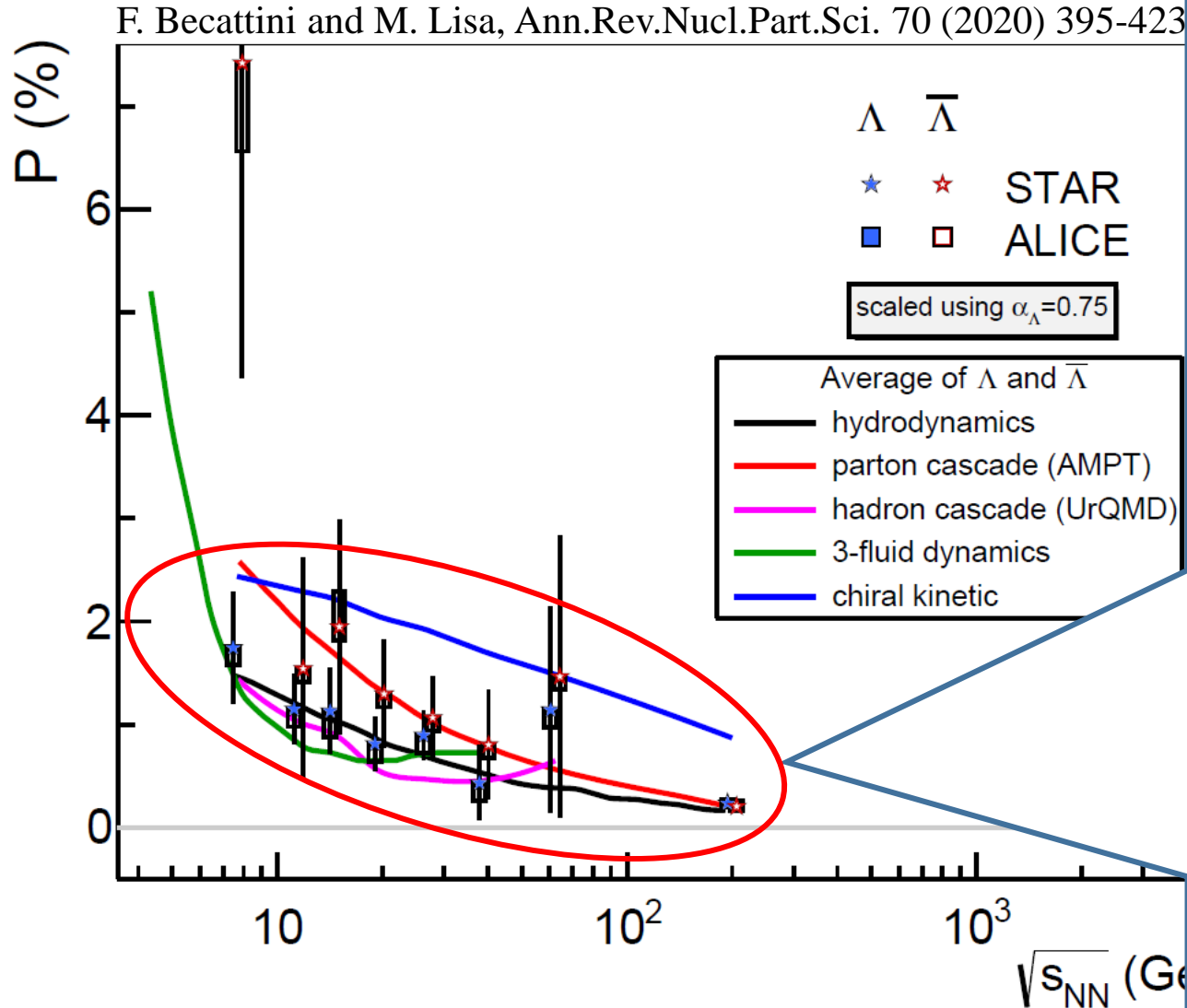
3-fluid dynamics:

Ivanov YB, Toneev VD, Soldatov AA. Phys. Rev. C100:014908 (2019)

Chiral Kinetic Theory:

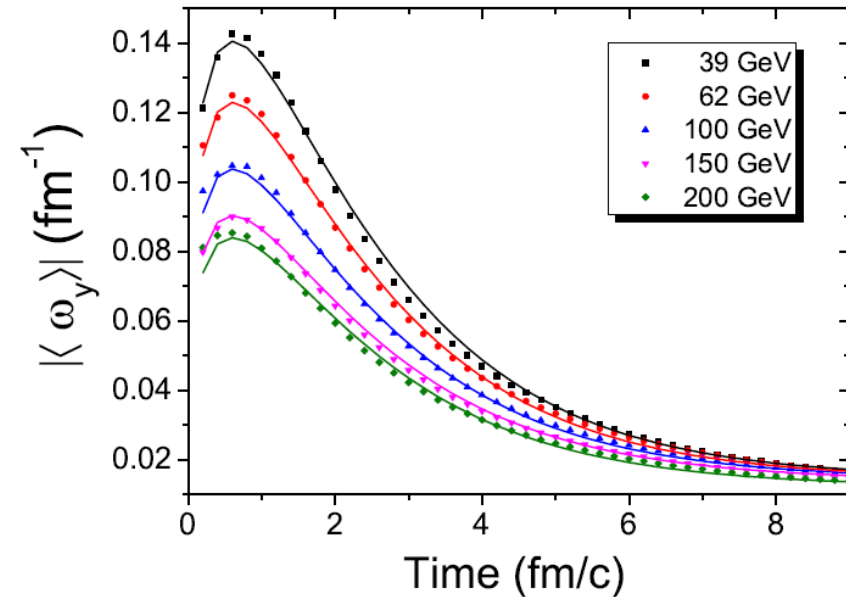
Sun Y, Ko CM. Phys. Rev. C96:024906 (2017)

Global polarization

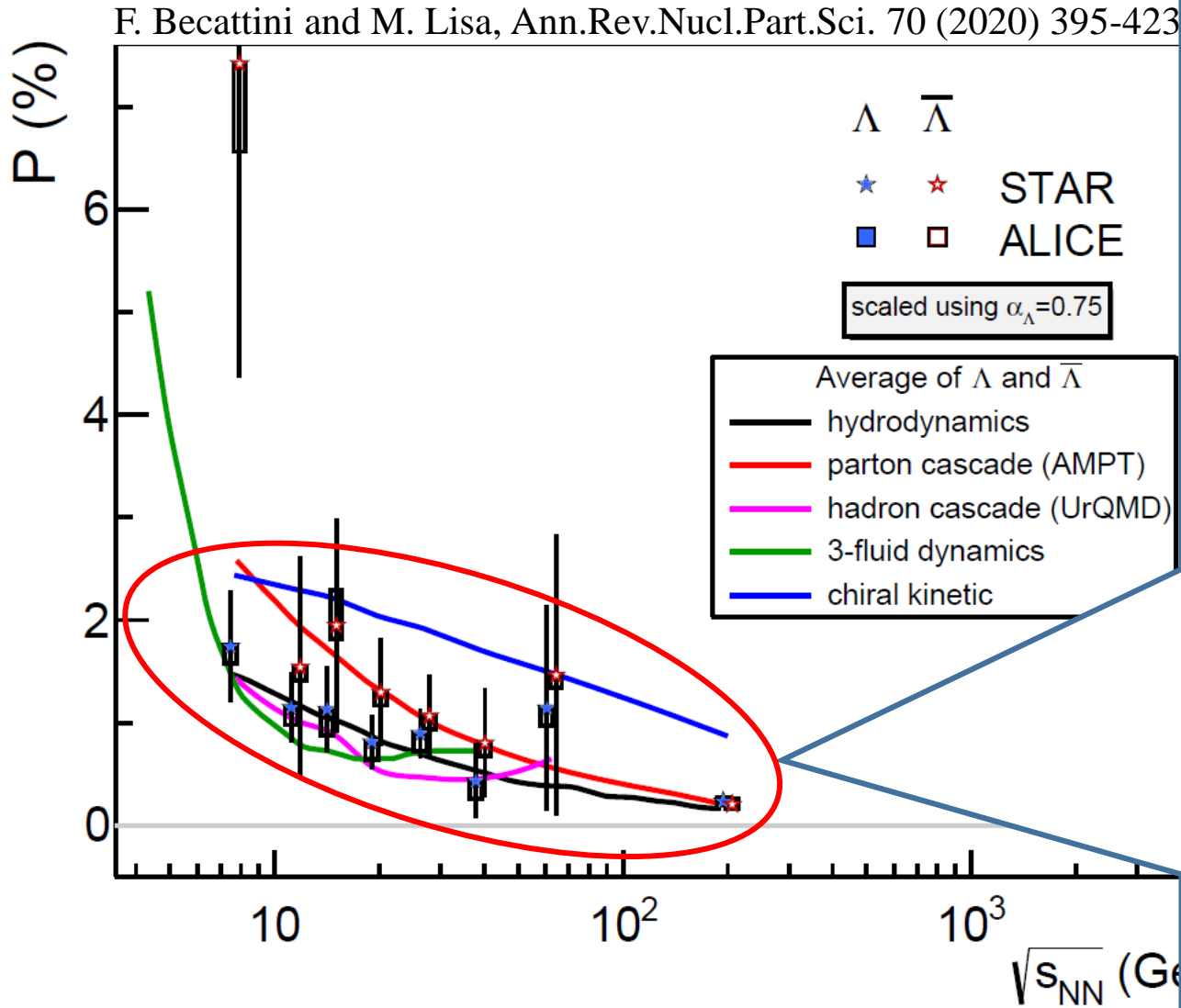


Collision energy dependence

- More transparent and symmetric in the mid-rapidity region in higher energies
[H. Li, et al, PRC 96 \(2017\) 054908](#)
- Longer evolution time will dilute the vorticity effect
[Iu. Karpenko and F. Becattini, EPJC 77 \(2017\) 4, 213](#)
- The inertia moment increase

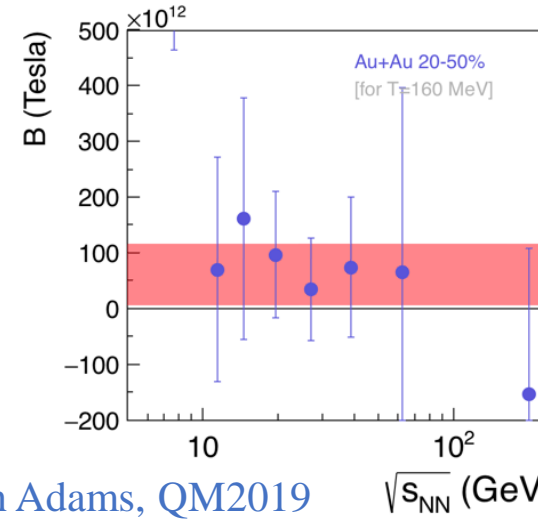


Global polarization



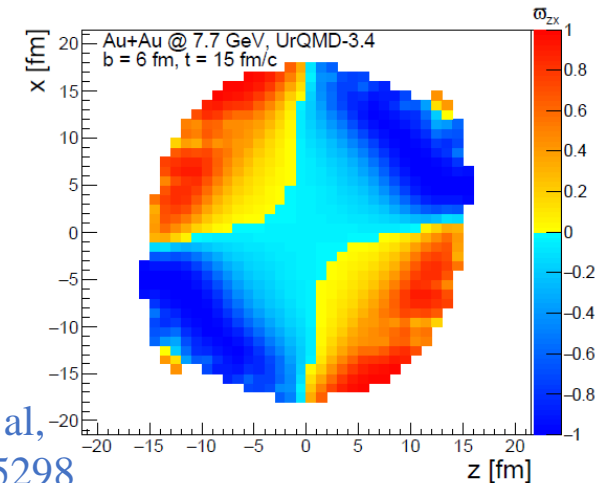
The $\Lambda - \bar{\Lambda}$ splitting

Might from magnetic field, but with large uncertainties



magnetar
 $B \sim 10^{11}$ T

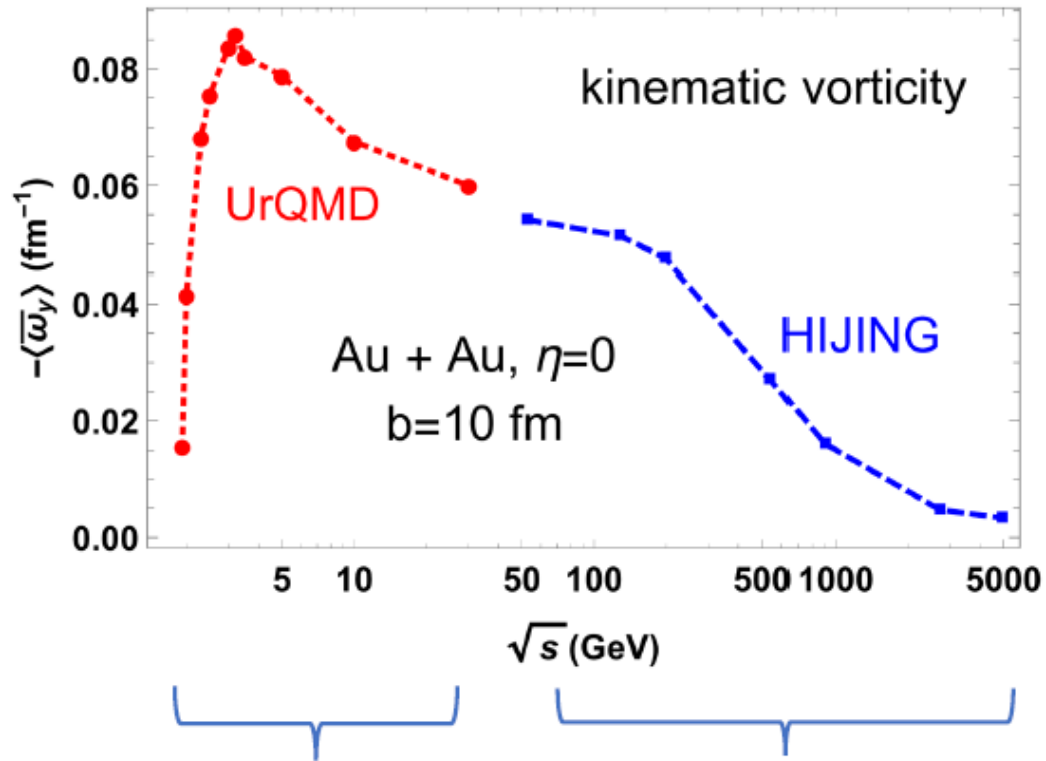
Also might from the different space-time distribution



O. Vitiuk, et al,
 PLB 803,135298

Global polarization at lower energies

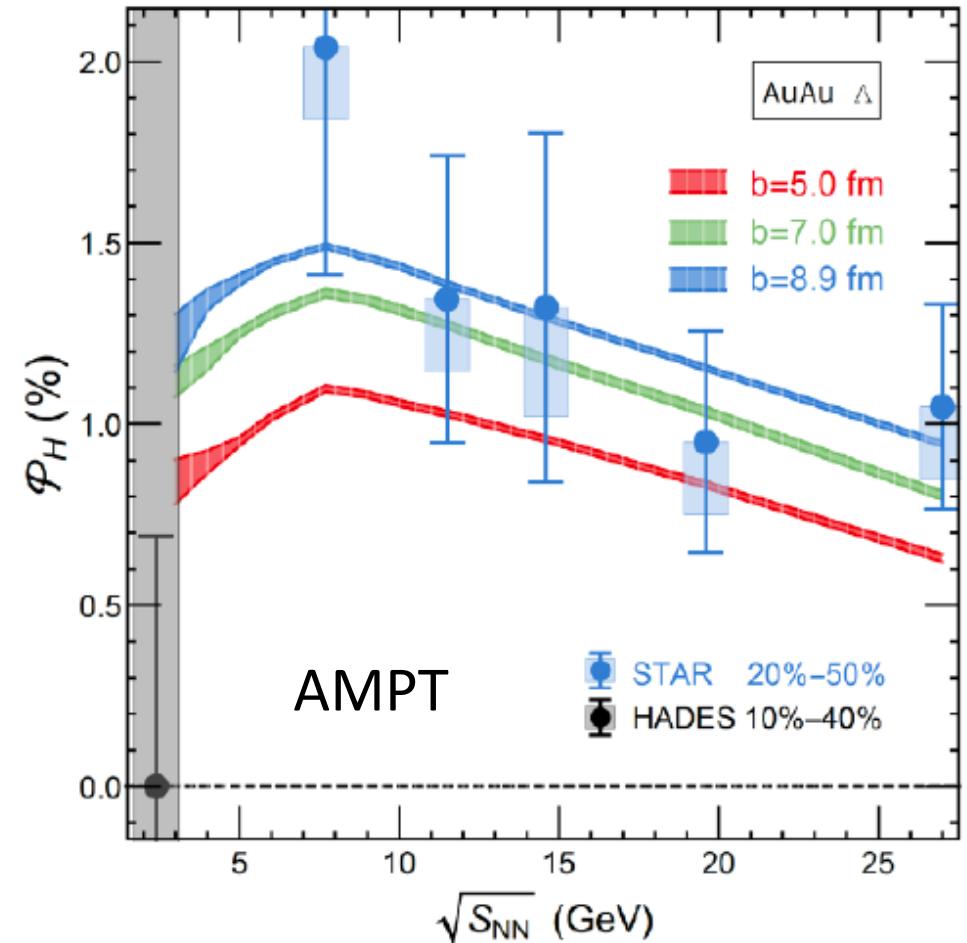
- Transport model predicts a maximum of vorticity around 3-7 GeV
- Need an out of equilibrium theory to calculate



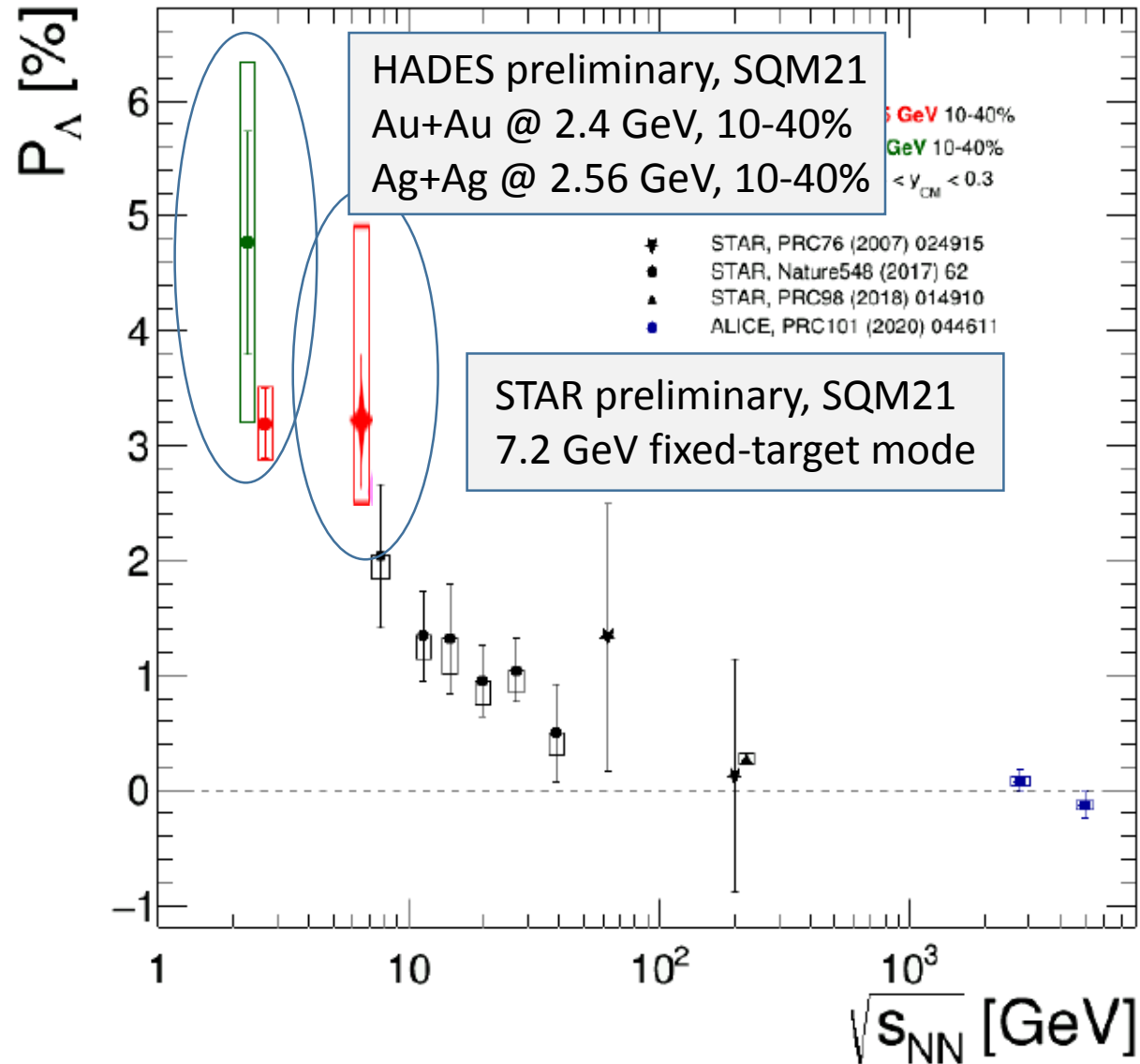
Deng, Huang, Ma and Zhang,
Phys.Rev.C 101 (2020) 6, 064908

W. Deng and X-G. Huang,
Phys.Rev.C 93 (2016) 6, 064907

Y. Guo, et al., arXiv: 2105.13481



Global polarization at lower energies



- P_H still shows increasing trend down to 2.4 GeV
- Will it 'turns-off' at lower energies?

HADES

(1) Au+Au 2012:

➤ $\sqrt{s_{NN}} = 2.4 \text{ GeV}$

➤ $7 \cdot 10^9$ events

(2) Ag+Ag 2019:

➤ $\sqrt{s_{NN}} = 2.55 \text{ GeV}$

➤ $14 \cdot 10^9$ events

STAR

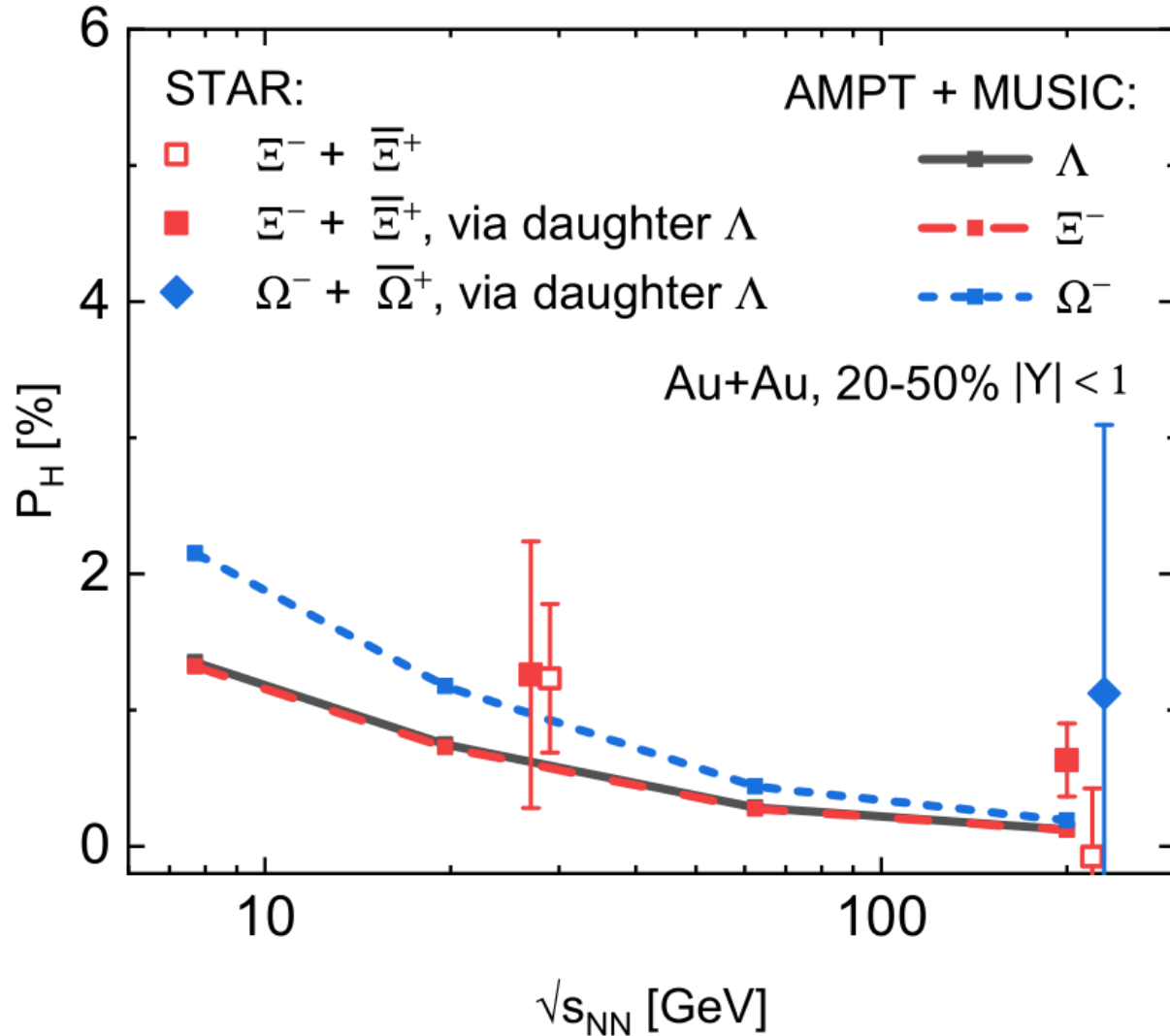
More data will come from BES-II+FXT

FXT (GeV): 3.0, 3.2, 3.5, 3.9, 4.5, 5.2, 5.2, 6.2, 7.7

Collider (GeV): 7.7, 9.1, 11.5, 14.5, 17.3, 19.6

Global Ξ^- and Ω^- polarization

BF, K. Xu, X-G, Huang, H. Song, Phys.Rev.C 103 (2021) 2, 024903



$$S^\mu(x, p) = -\frac{1}{2m} \frac{S(S+1)}{3} [1 - f(x, p)] \epsilon^{\mu\nu\rho\sigma} p_\sigma \bar{\omega}_{\nu\rho}$$

Spin ratio:

$$S_{\Omega^-} : S_{\Xi^-} : S_{\Lambda} = 3 : 1 : 1$$

Mass ratio:

$$m_{\Omega^-} : m_{\Xi^-} : m_{\Lambda} = 1.5 : 1.2 : 1$$

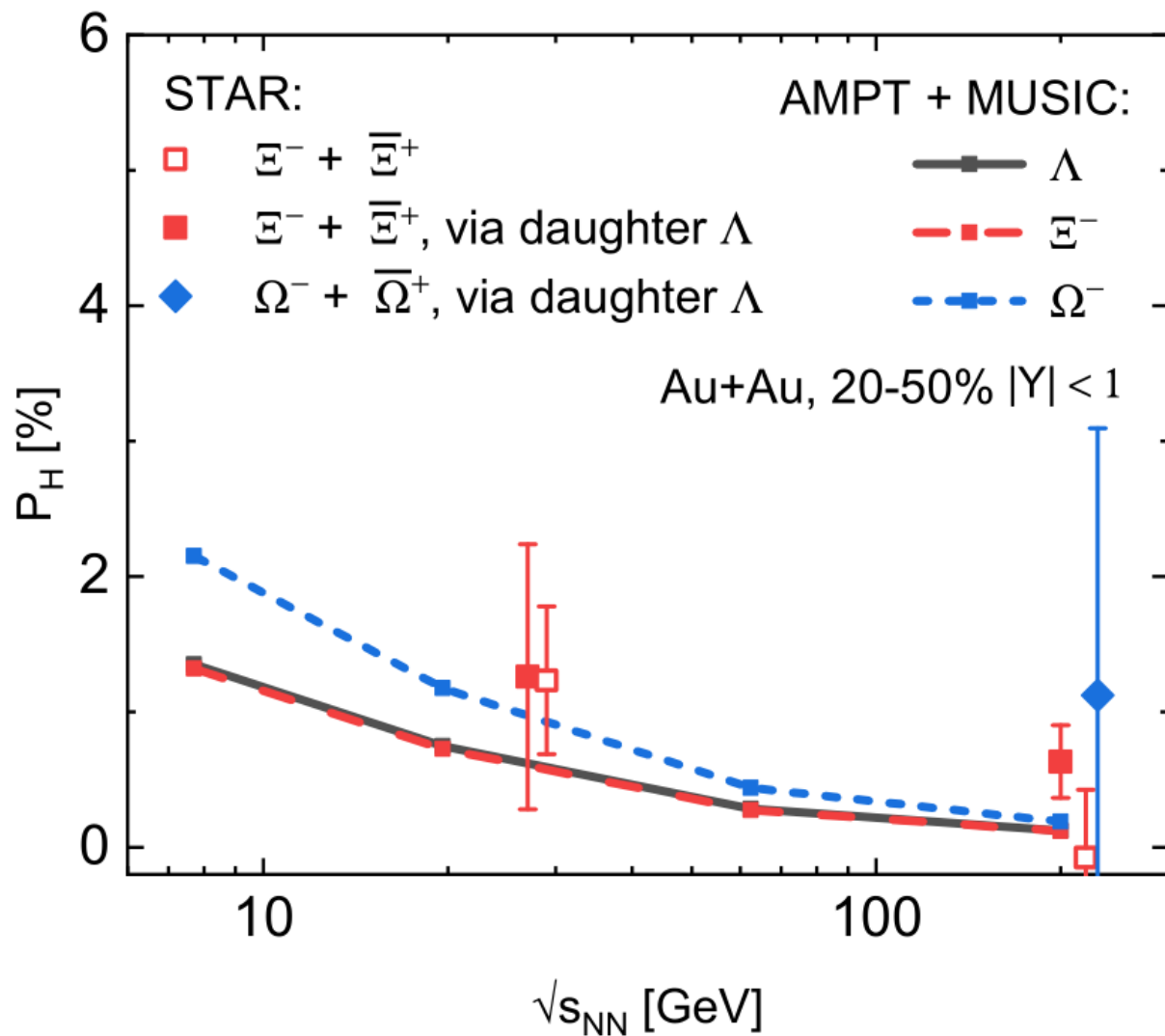
Magnetic moments ratio:

$$|M_{\Omega^-}| : |M_{\Xi^-}| : |M_{\Lambda}| \approx 3 : 1 : 1$$

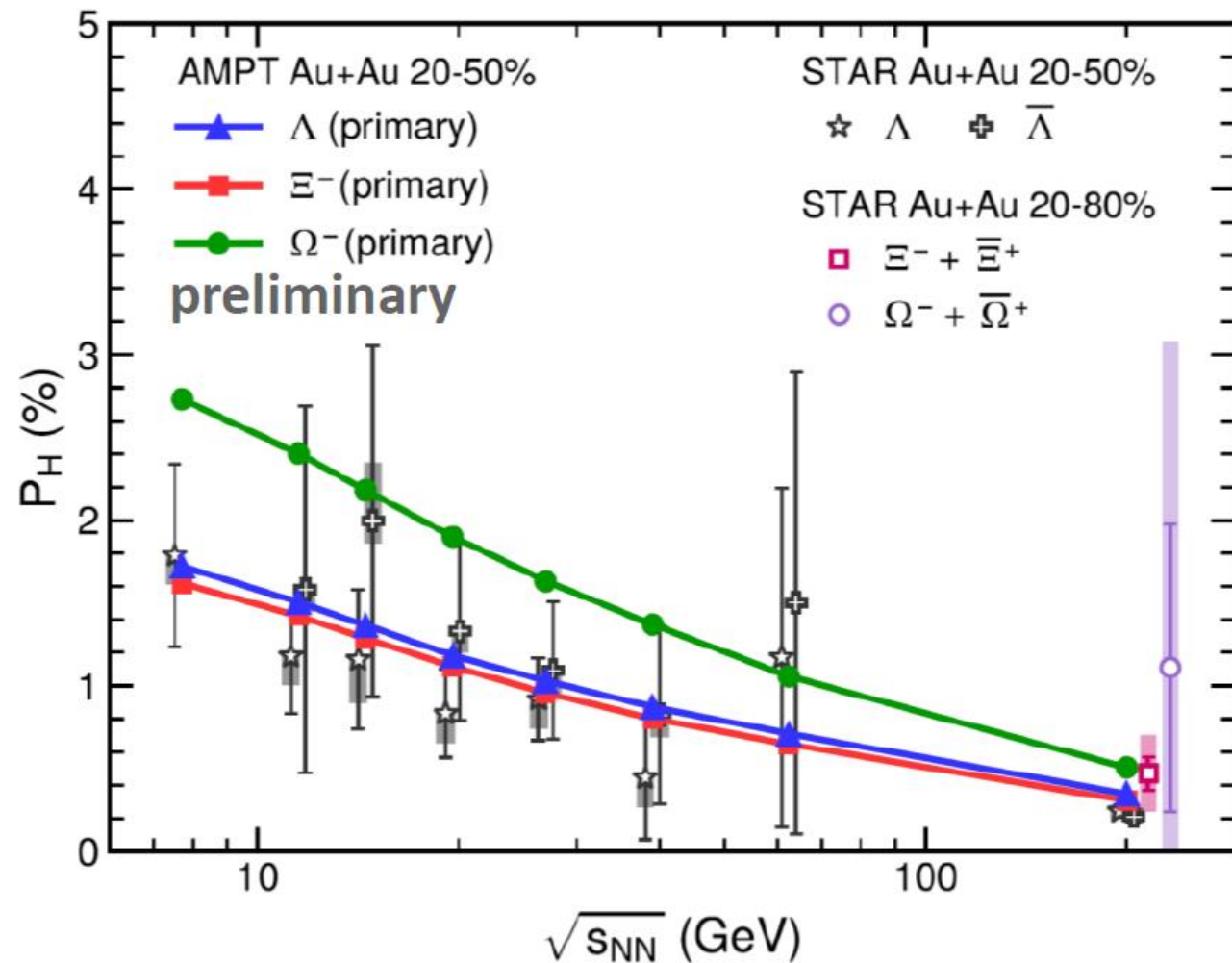
- Baseline for future feed-down and magnetic field study

Global Ξ^- and Ω^- polarization

BF, K. Xu, X-G, Huang, H. Song, Phys.Rev.C 103 (2021) 2, 024903

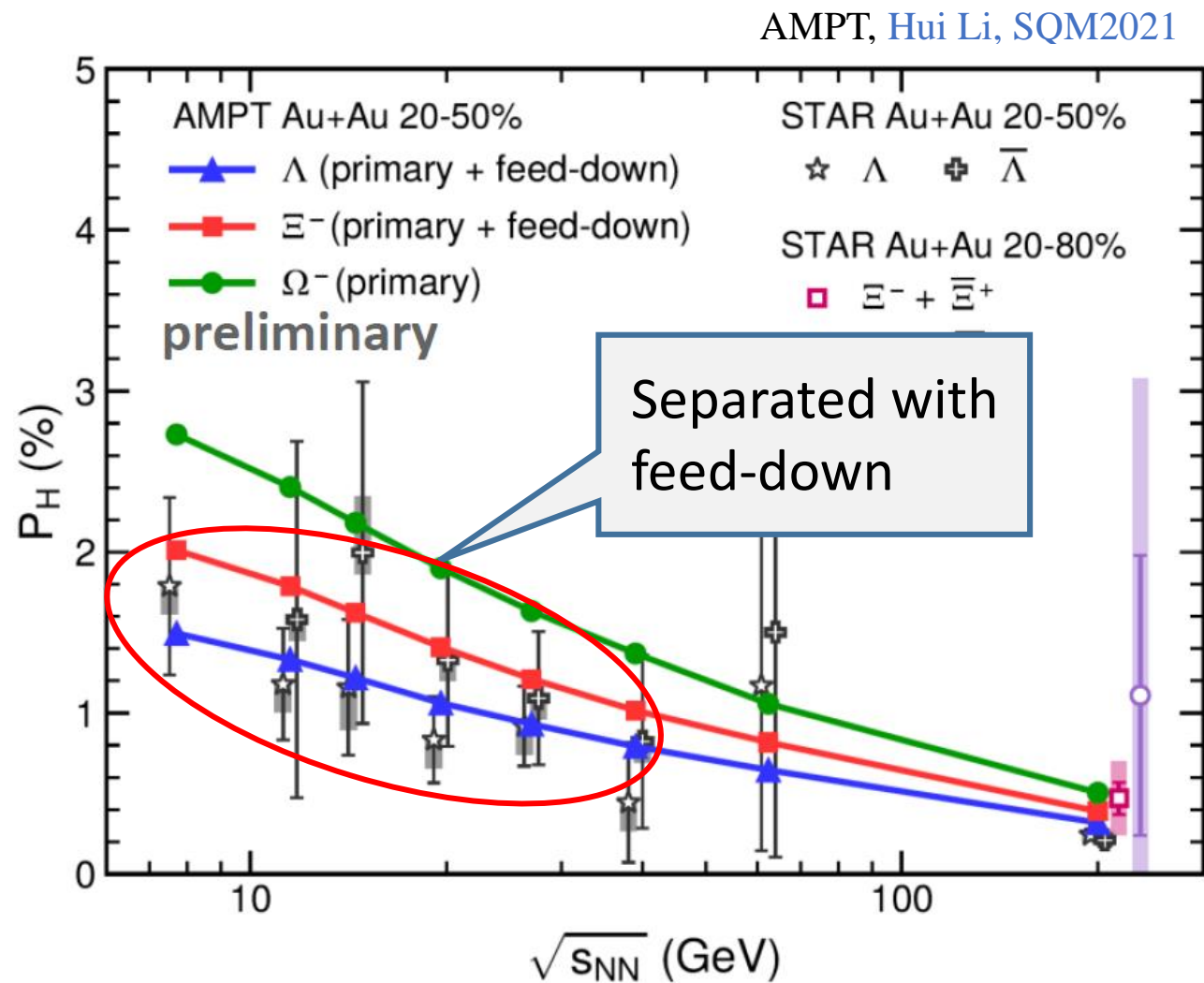
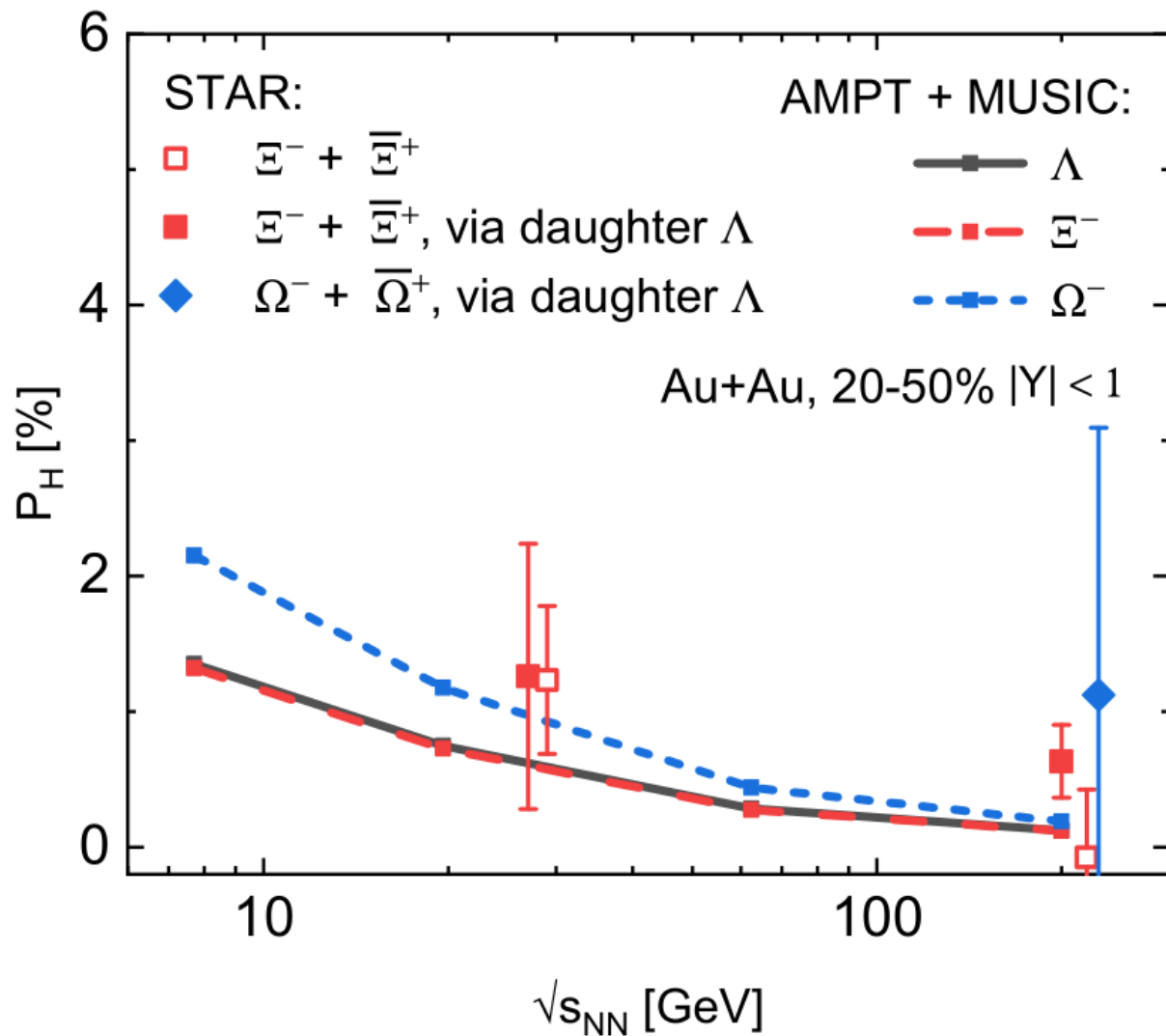


AMPT, Hui Li, SQM2021



Global Ξ^- and Ω^- polarization

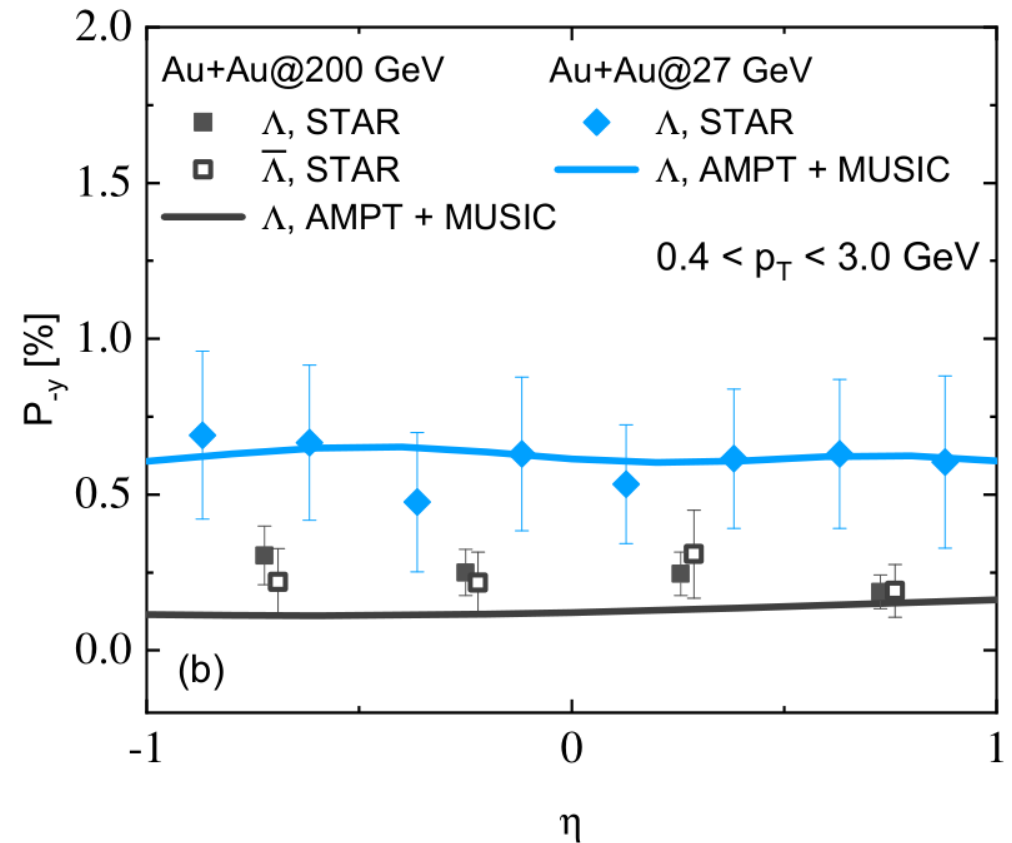
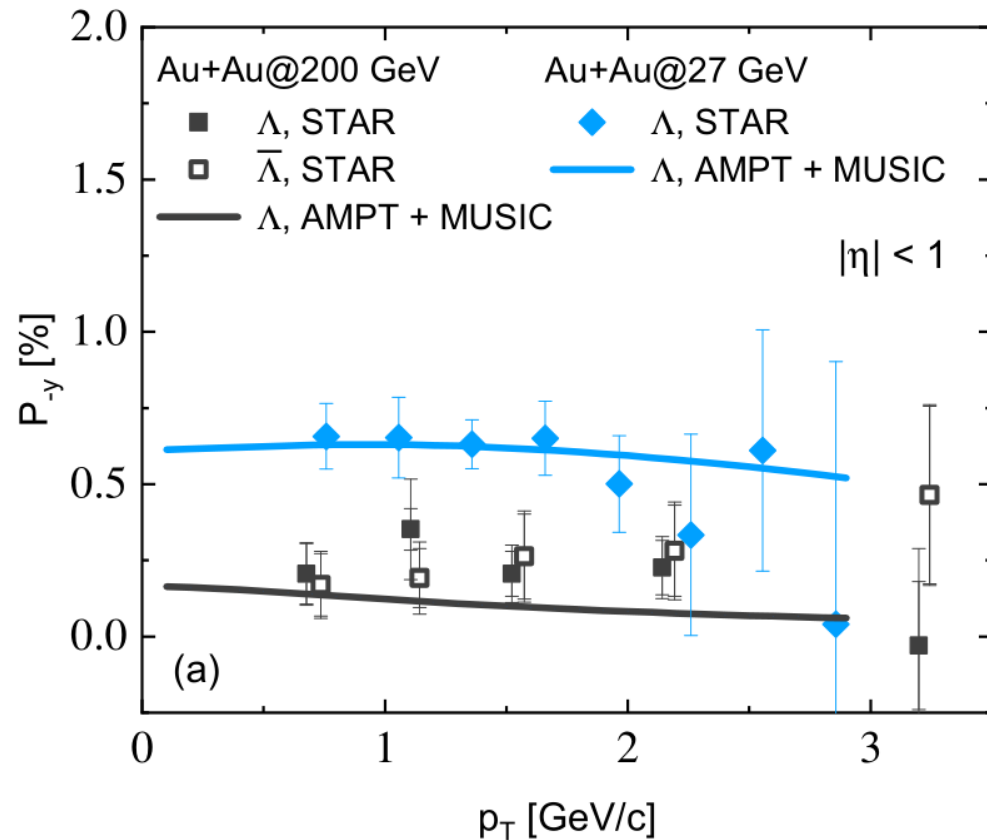
BF, K. Xu, X-G, Huang, H. Song, Phys.Rev.C 103 (2021) 2, 024903



Local polarization puzzle

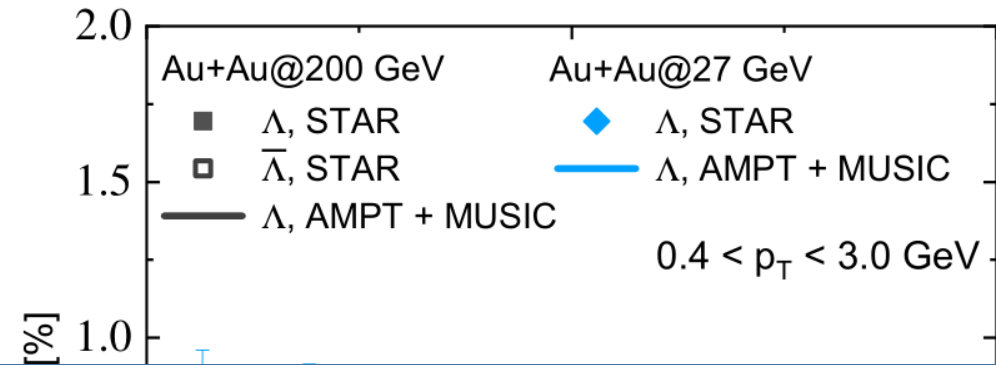
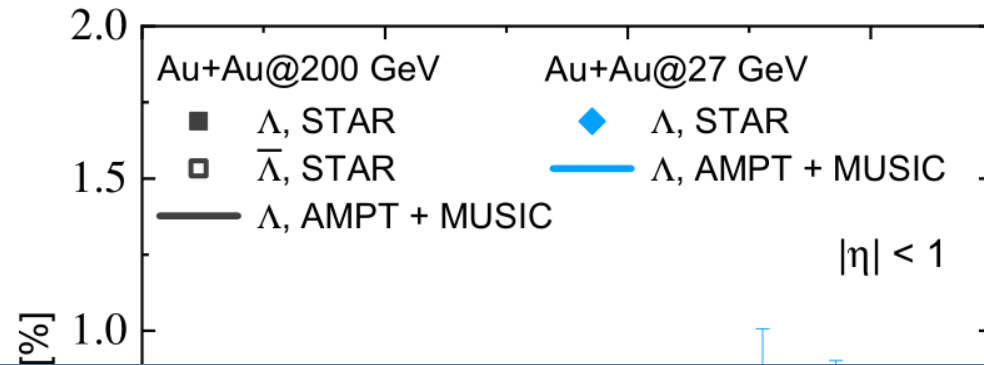
local polarization: p_T and η dependence

- $P_y(p_T)$ and $P_y(\eta)$ Describes data within error bars

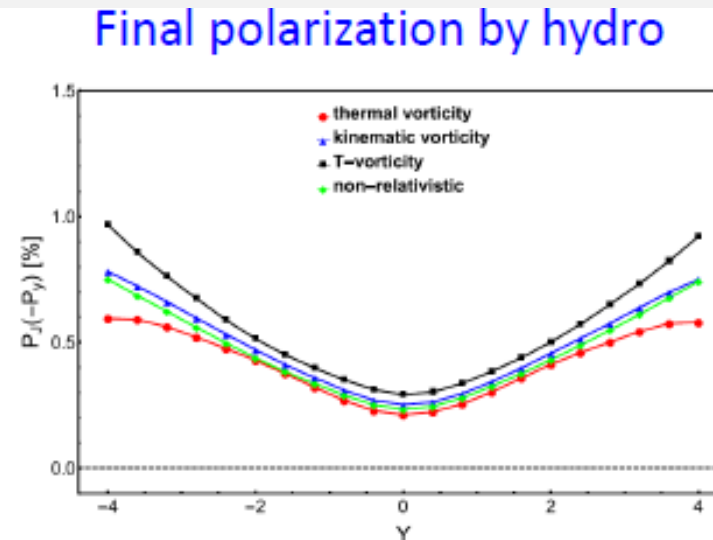
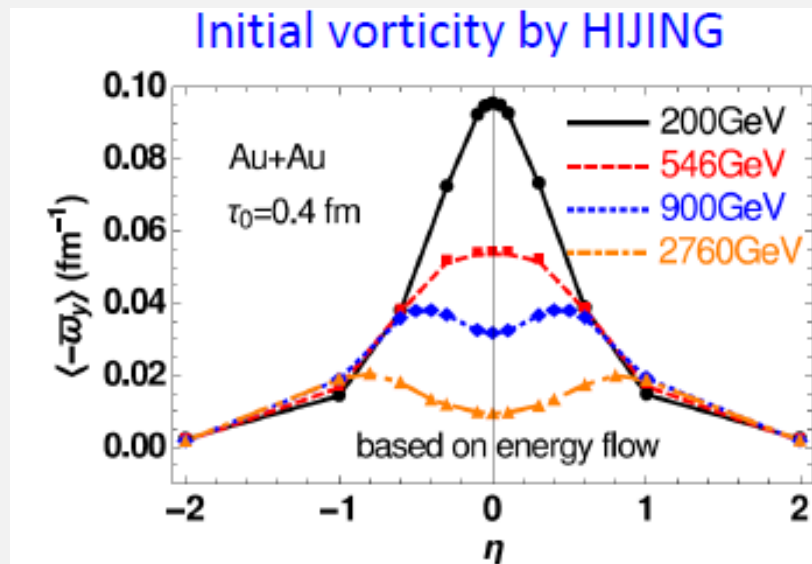


local polarization: p_T and η dependence

- $P_y(p_T)$ and $P_y(\eta)$ Describes data within error bars



- how about large rapidity?



HIJING:

W-T. Deng and X-G. Huang
 PRC 93 (2016) 6, 064907

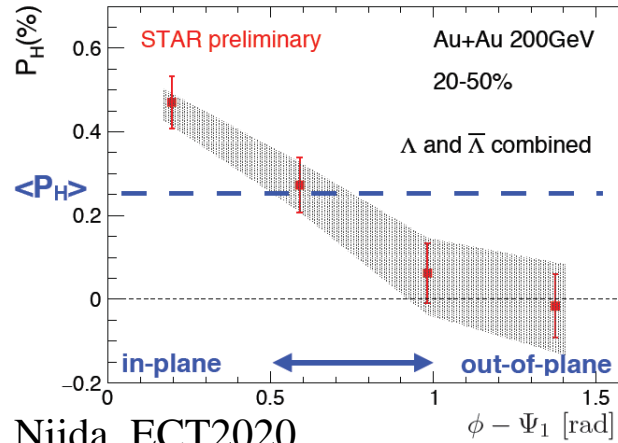
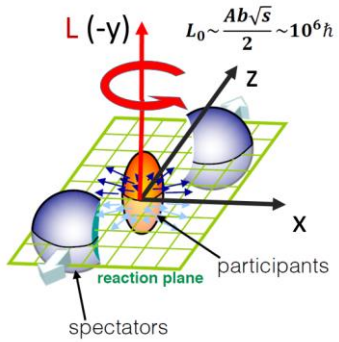
Hydro:

H-Z. Wu, L-G. Pang, X-G.
 Huang and Q. Wang
 PRR 1 (2019) 033058

local polarization: ϕ dependence

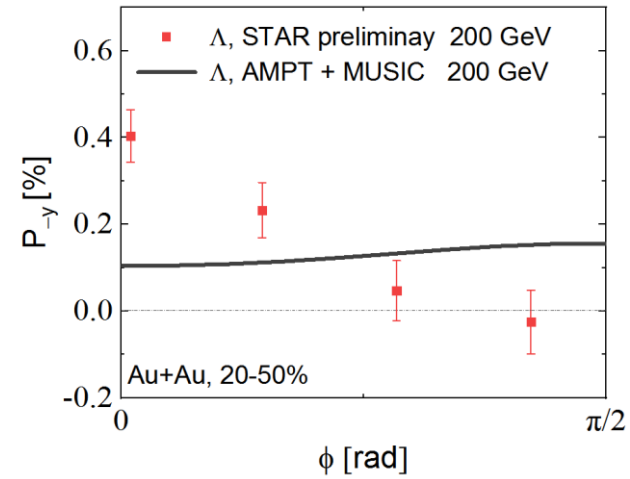
Experiment data

$$P^y(\phi)$$



T. Niida, ECT2020

Hydrodynamics



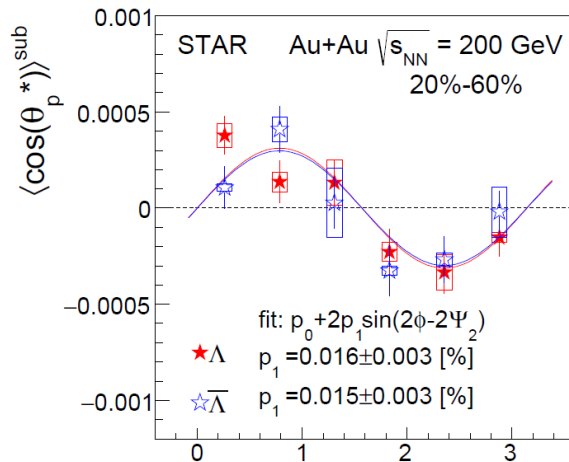
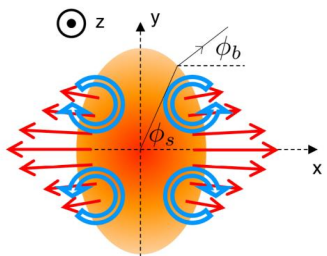
BF, Xu, Huang, Song,
PRC103 (2021) 2, 024903

See also:

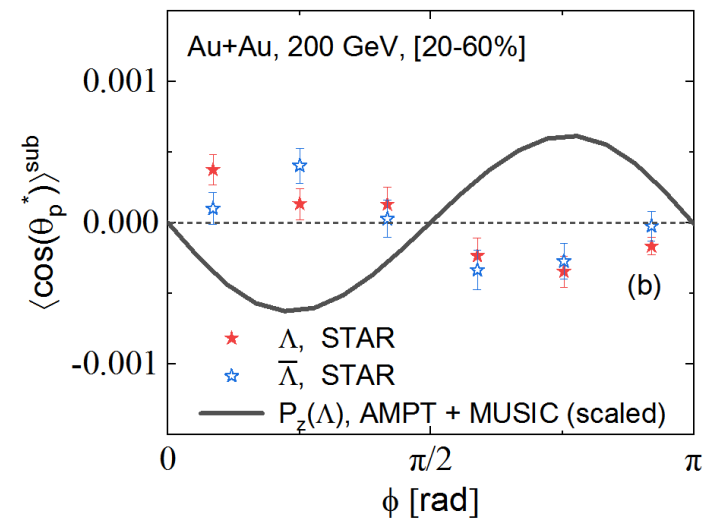
Karpenko, Becattini,
EPJC 77 (2017) 4, 213

D. Wei, et al.,
PRC 99 (2019) 014905

$$P^z(\phi)$$



PRL 123 (2019) 132301 $\phi - \Psi_2$ [rad]



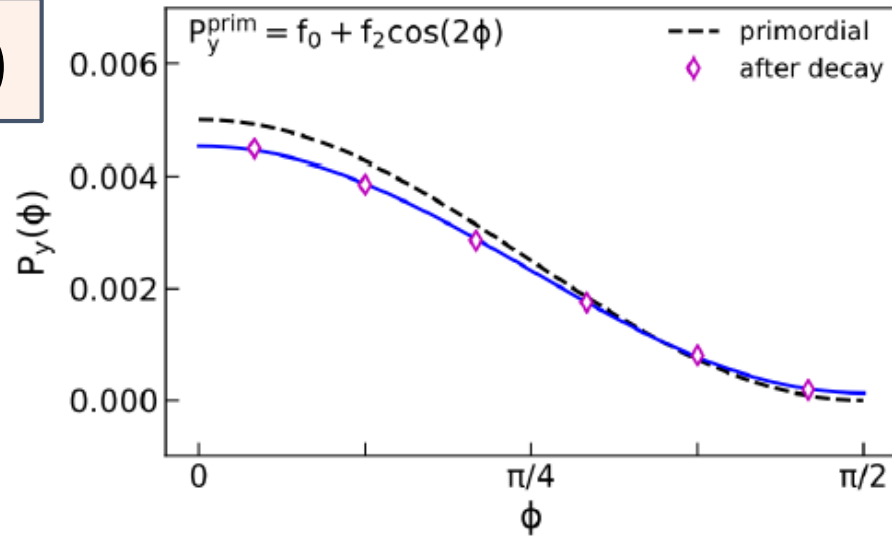
X. Xia, et al.,
PRC 98 (2018) 024905

Becattini, Karpenko,
PRL 120 (2018) 012302

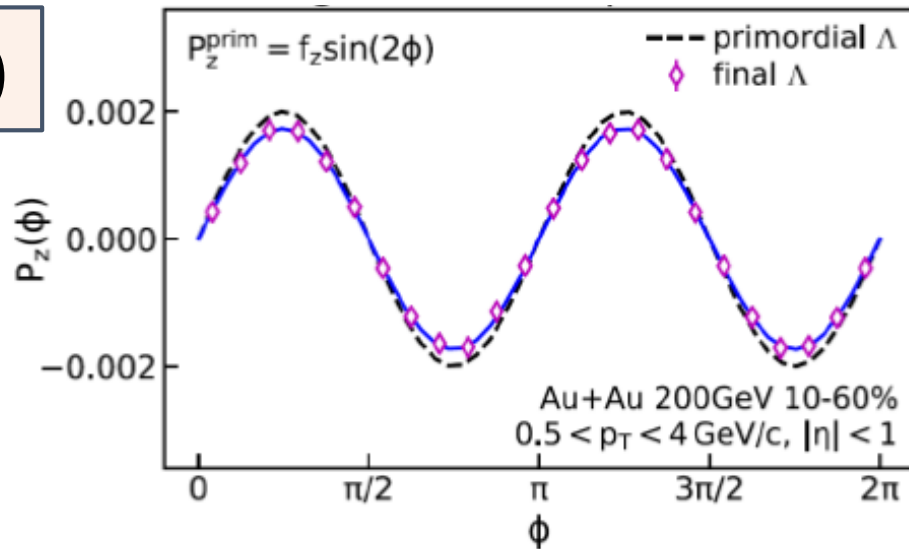
Efforts to resolve the 'sign puzzle'

- Feed-down effects (Xia, Li, Huang, Huang, PRC 2019, Becattini, Cao, Speranza, EPJC 2019)

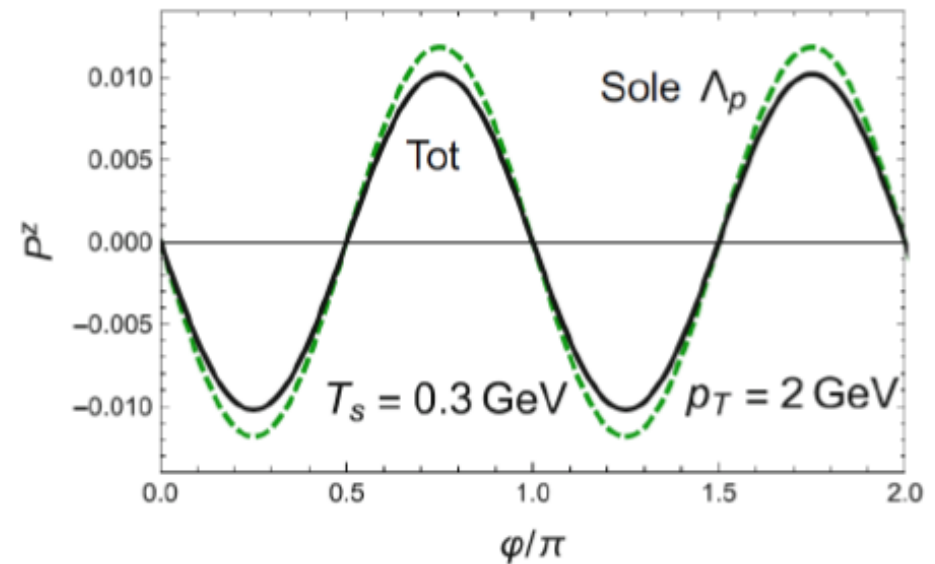
$$P^y(\phi)$$



$$P^z(\phi)$$



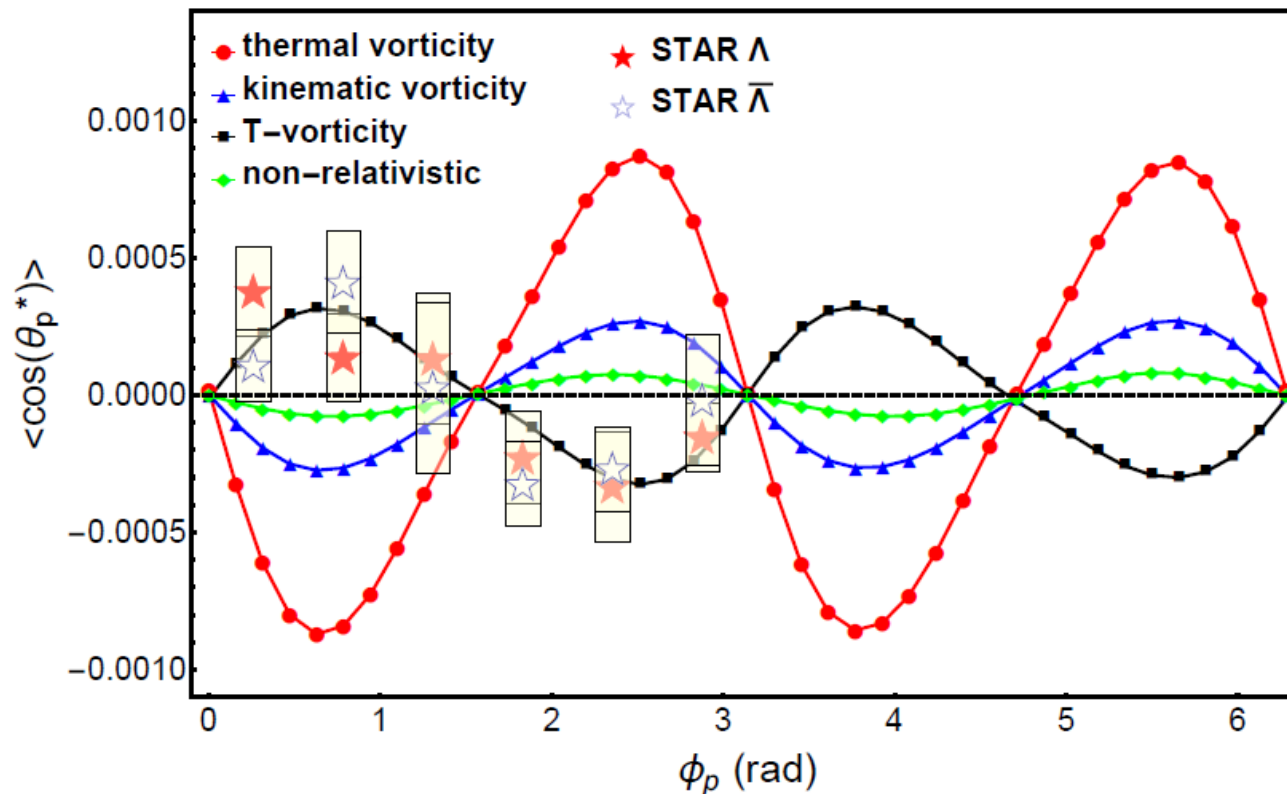
- About 80% of final Λ from decays
- Feed-down effect suppress $\sim 10 - 20\%$ primordial spin polarization



Efforts to resolve the 'sign puzzle'

- Feed-down effects (Xia, Li, Huang, Huang, PRC 2019, Becattini, Cao, Speranza, EPJC 2019)
- Other spin chemical potential (Wu, Pang, Huang, Wang, PRR 2019)

AMPT IS (includes angular momentum) + 3D viscous hydro (CLVisc



Red Line: thermal vorticity

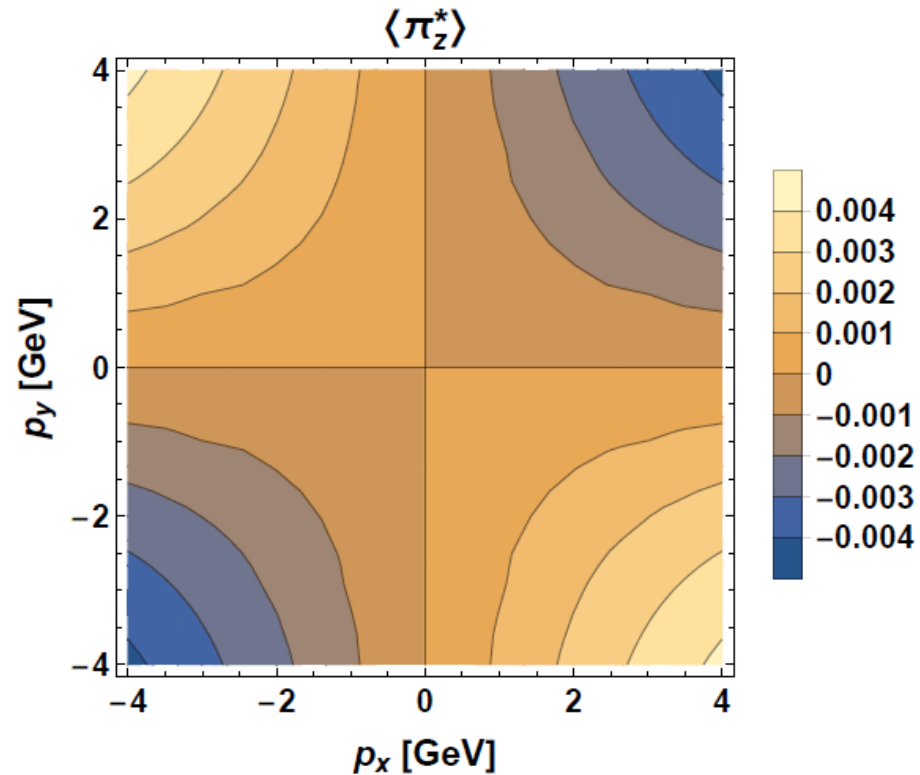
$$\omega_{\mu\nu}^{(th)} = -\frac{1}{2} (\partial_\mu(u_\nu/T) - \partial_\nu(u_\mu/T))$$

Black Line: T-vorticity

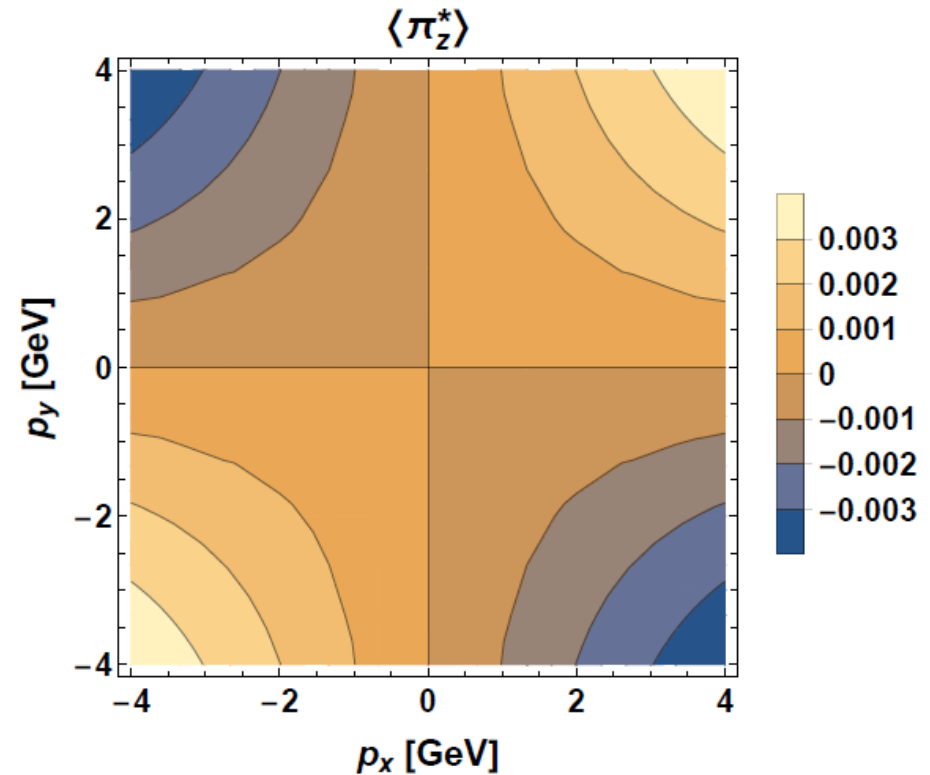
$$\omega_{\mu\nu}^{(T)} = -\frac{1}{2} (\partial_\mu(u_\nu T) - \partial_\nu(u_\mu T))$$

Efforts to resolve the 'sign puzzle'

- Feed-down effects (Xia, Li, Huang, Huang, PRC 2019, Becattini, Cao, Speranza, EPJC 2019)
- Other spin chemical potential (Wu, Pang, Huang, Wang, PRR 2019)
- Polarization from projected thermal vorticity (Florkowski, Kumar, Ryblewski, Mazeliauskas, PRC 2019)



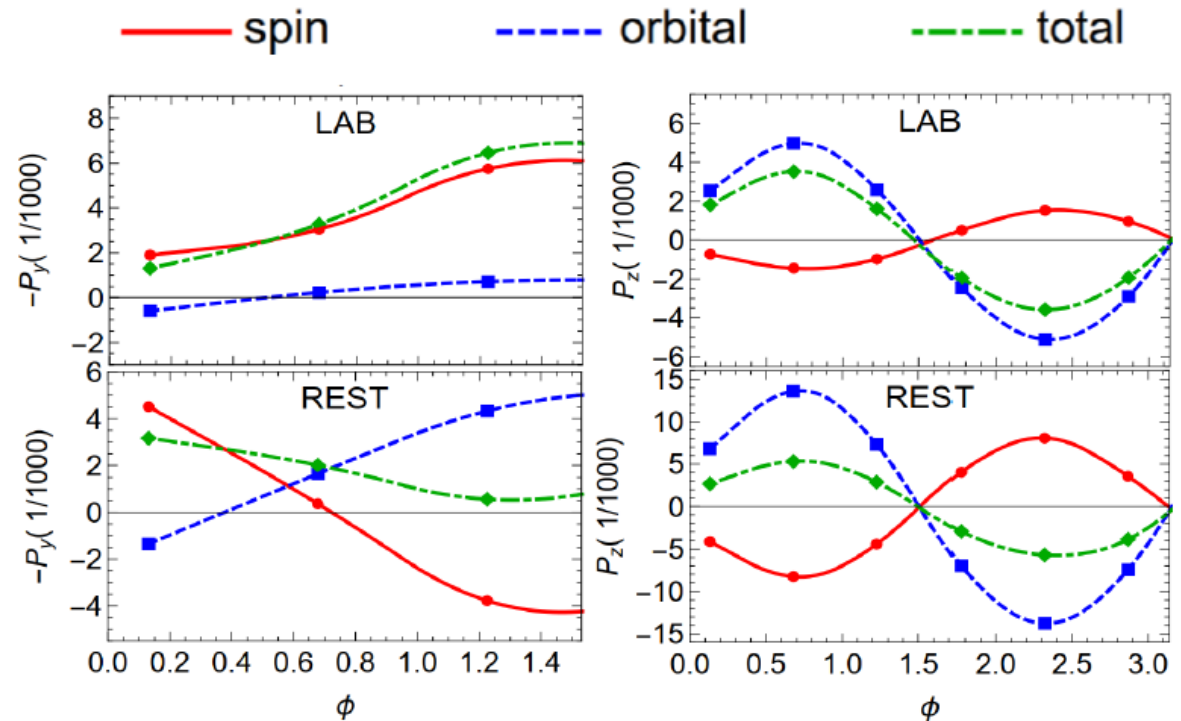
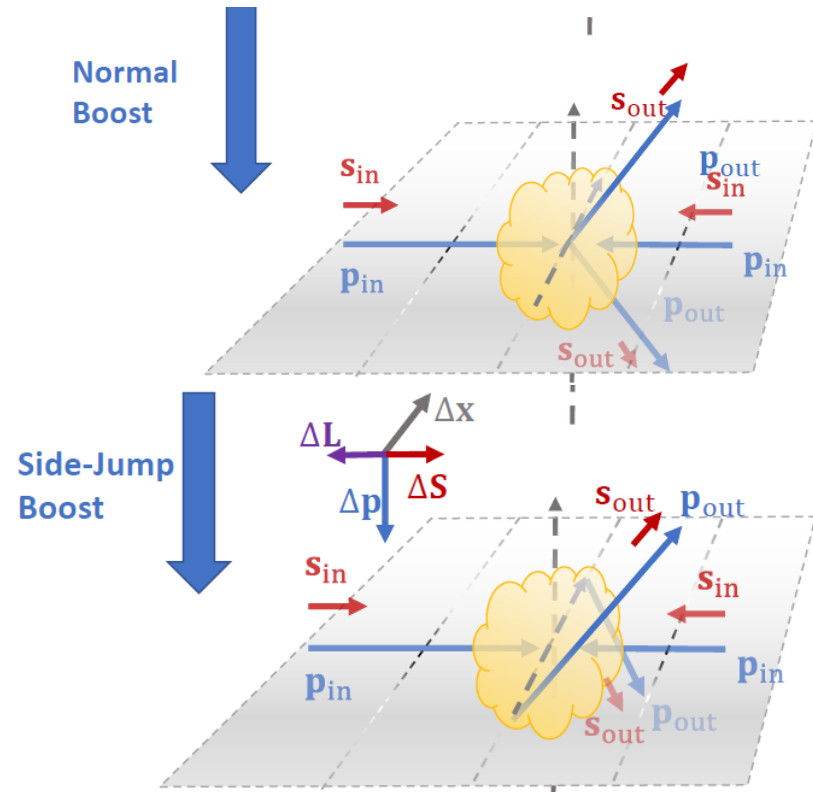
Standard thermal vorticity:
$$\overline{\omega}^{\mu\nu} = -\frac{1}{2} (\partial^\mu \beta^\nu - \partial^\nu \beta^\mu)$$



Projected thermal vorticity:
$$\overline{\omega}_{\text{proj}}^{\mu\nu} = \overline{\omega}_{\alpha\beta} \Delta_\alpha^\mu \Delta_\beta^\nu$$

Efforts to resolve the 'sign puzzle'

- Feed-down effects (Xia, Li, Huang, Huang, PRC 2019, Becattini, Cao, Speranza, EPJC 2019)
- Other spin chemical potential (Wu, Pang, Huang, Wang, PRR 2019)
- Polarization from projected thermal vorticity (Florkowski, Kumar, Ryblewski, Mazeliauskas, PRC 2019)
- Side-jump in CKT (Liu, Ko, Sun, PRL 2019)



Efforts to resolve the 'sign puzzle'

- Feed-down effects (Xia, Li, Huang, Huang, PRC 2019, Becattini, Cao, Speranza, EPJC 2019)
- Other spin chemical potential (Wu, Pang, Huang, Wang, PRR 2019)
- Polarization from projected thermal vorticity (Florkowski, Kumar, Ryblewski, Mazeliauskas, PRC 2019)
- Side-jump in CKT (Liu, Ko, Sun, PRL 2019)
- Spin as a dynamical d.o.f:
 - spin hydrodynamics (Florkowski, et al., PRC2017, Hattori, et al., PLB 2019, Shi, et al, PRC 2021, ...)
 - spin kinetic theory (Gao and Liang, PRD 2019, Weickgenannt ,et al PRD 2019, Hattori, et al PRD 2019, Wang, et al, PRD 2019, Liu, et al, CPC 2020, Hattori, et al, PRD 2019, ...)
- Final hadronic interactions (Xie and Csernai, ECT talk 2020, Csernai, Kapusta, Welle, PRC 2019)
- ...

**Still open questions and more precise understanding needed
about spin and its dynamics**

Shear Induced Polarization (SIP)

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin, arXiv: 2103.10403

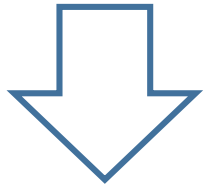
Hydrodynamic gradients

Derivatives of the velocity field:

$$\partial_\mu u_\nu(x)$$

Anti-symmetric: vorticity

$$\omega^\mu = \frac{1}{2} \epsilon^{\mu\nu\alpha\beta} u_\nu \partial_\alpha^\perp u_\beta$$



(Thermal) vorticity induced polarization

In condensed matter physics:

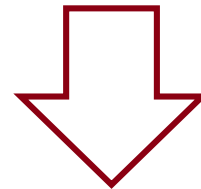
R. Takahashi, et al., Nature Physics (2016) 12, 52-56

In heavy ion collision:

F. Becattini (2013) and later works

Symmetric: shear stress

$$\sigma^{\mu\nu} = \frac{1}{2} (\partial_\perp^\mu u^\nu + \partial_\perp^\nu u^\mu) - \frac{1}{3} \Delta^{\mu\nu} \partial_\perp \cdot u$$



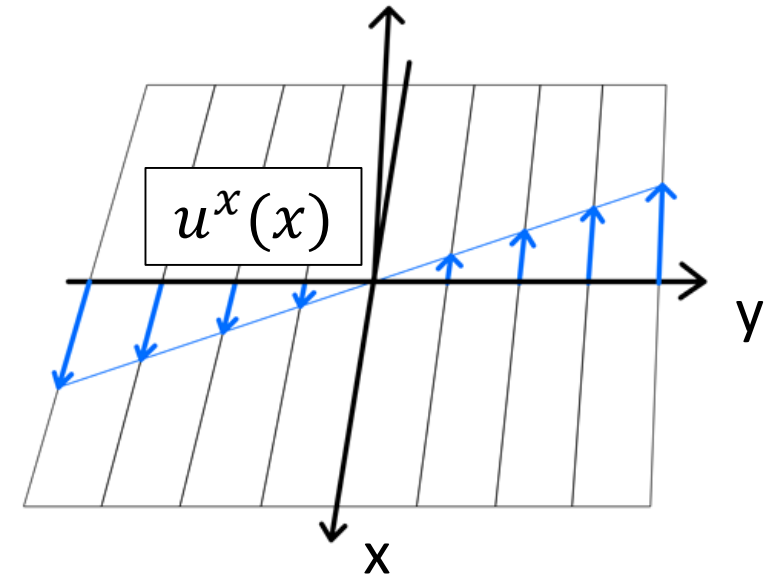
Shear Induced polarization: ?

[Strain induced polarization]

In crystal physics:

S. Crooker and D. Smith, PRL (2005) 94, 236601

T. Kissikov, et al., Nature Comm. (2018) 9, 1058



Shear effects in heavy ion collisions will be discussed in this talk

Shear Induced Polarization (SIP)

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

Axial Wigner function from CKT ([Chen, Son, Stephanov, PRL 115 \(2015\) 2, 021601](#))

$$\mathcal{A}^\mu = \sum_\lambda \left(\lambda p^\mu f_\lambda + \frac{1}{2} \frac{\epsilon^{\mu\nu\alpha\rho} p_\nu u_\alpha \partial_\rho f_\lambda}{p \cdot u} \right)$$

Expand \mathcal{A}^μ to 1st order gradient of the fields:

$$\mathcal{A}^\mu = \frac{1}{2} \beta n_0 (1 - n_0) \left\{ \underbrace{\epsilon^{\mu\nu\alpha\lambda} p_\nu \partial_\alpha^\perp u_\lambda}_{\text{Vorticity}} + \underbrace{2\epsilon^{\mu\nu\alpha\lambda} u_\nu p_\alpha [\beta^{-1} (\partial_\lambda \beta)]}_{\text{T gradient (spin Nernst effect)}} - \underbrace{2 \frac{p_\perp^2}{\epsilon_0} \epsilon^{\mu\nu\alpha\rho} u_\nu Q_\alpha^\lambda \sigma_{\rho\lambda}}_{\text{Shear strength}} \right\}$$

- Identical form by linear response theory with **arbitrary mass** ([S. Liu and Y. Yin, arXiv: 2103.09200](#))
- No free parameter
- Different mass sensitivity of each term

$$Q^{\mu\nu} = -p_\perp^\mu p_\perp^\nu / p_\perp^2 + \Delta^{\mu\nu} / 3$$

$$\sigma^{\mu\nu} = \frac{1}{2} (\partial_\perp^\mu u^\nu + \partial_\perp^\nu u^\mu) - \frac{1}{3} \Delta^{\mu\nu} \partial_\perp \cdot u$$

Shear Induced Polarization (SIP)

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

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$$\text{Total } P^\mu = [\text{Vorticity}] + [\text{T gradient}] + [\text{Shear}]$$

Shear Induced Polarization (SIP)

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

Axial Wigner fu

To one-loop order (in charge neutral fluid)

Expand \mathcal{A}^μ to

$$\epsilon^{\mu\nu\alpha\lambda} p_\nu \partial_\alpha (\beta u)_\lambda$$

Thermal vorticity

$$\varpi_{\mu\nu} = \frac{1}{2} (\partial_\nu (\beta u_\mu) - \partial_\mu (\beta u_\nu))$$

$$\mathcal{A}^\mu = \frac{1}{2} \beta n_0 (1 - n_0) \left\{ \epsilon^{\mu\nu\alpha\lambda} p_\nu \partial_\alpha^\perp u_\lambda + 2 \epsilon^{\mu\nu\alpha\lambda} u_\nu p_\alpha [\beta^{-1} (\partial_\lambda \beta)] - 2 \frac{p_\perp^2}{\epsilon_0} \epsilon^{\mu\nu\alpha\rho} u_\nu Q_\alpha^\lambda \sigma_{\rho\lambda} \right\}$$

Vorticity

T gradient
(spin Nernst effect)

Shear strength

$$\text{Total } P^\mu = [\text{Vorticity}] + [\text{T gradient}] + [\text{Shear}]$$

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Expand \mathcal{A}^μ to

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Thermal vorticity

$$\varpi_{\mu\nu} = \frac{1}{2} (\partial_\nu (\beta u_\mu) - \partial_\mu (\beta u_\nu))$$

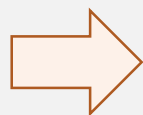
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Vorticity

T gradient
(spin Nernst effect)

Shear strength

$$\text{Total } P^\mu = [\text{Vorticity}] + [\text{T gradient}] + [\text{Shear}]$$



$$\text{Total } P^\mu = [\text{Thermal vorticity}] + [\text{Shear}]$$

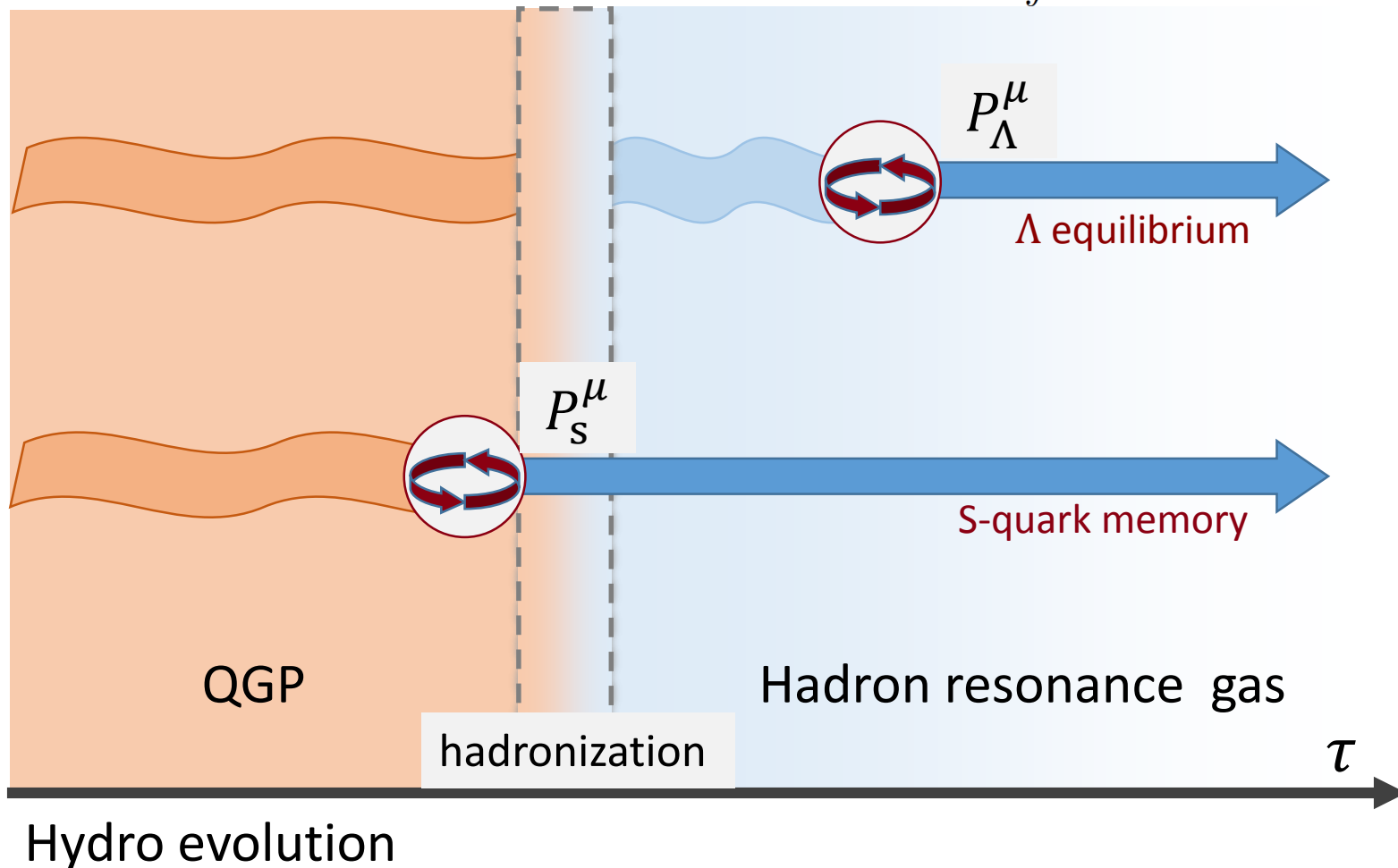
The only new effect

Similar result obtained independently by
Becattini, Buzzegoli, Palermo, arXiv: 2103.10917

' Λ equilibrium' vs. 'S-quark memory'

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

Spin Cooper-Frye:
$$P^\mu(\mathbf{p}) = \frac{\int d\Sigma^\alpha p_\alpha \mathcal{A}^\mu(x, \mathbf{p}; m)}{2m \int d\Sigma^\alpha p_\alpha n(\beta\varepsilon_0)}$$



' Λ equilibrium'

$$\tau_{\text{spin}, \Lambda} \rightarrow 0$$

Polarization of Λ -hyperon

$$P_\Lambda^\mu(p)$$

F. Becattini (2013)

and later hydrodynamic(transport) calculations

'S-quark memory'

$$\tau_{\text{spin}, \Lambda} \rightarrow \infty$$

Polarization of S-quark

$$P_S^\mu(p)$$

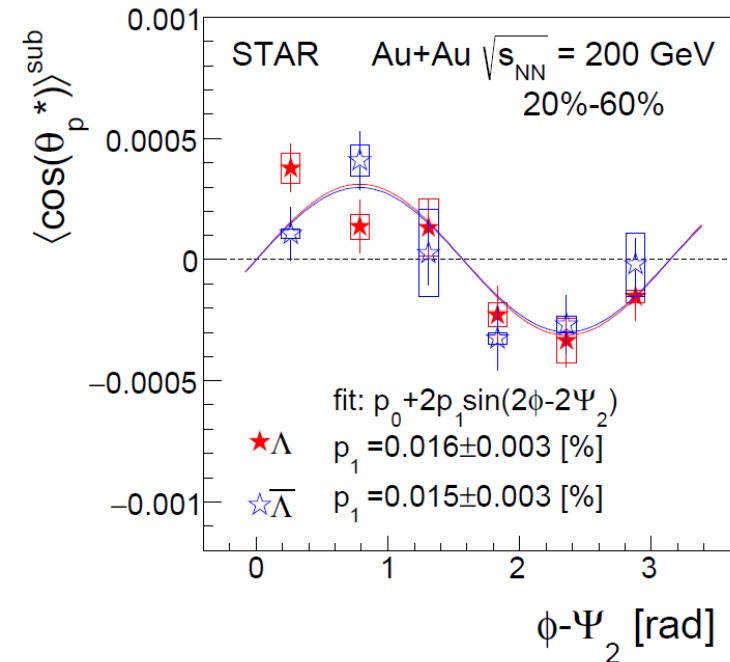
Z.-T. Liang, X.-N. Wang, PRL 94 (2005) 102301

Quark model: $P_\Lambda \sim P_S$

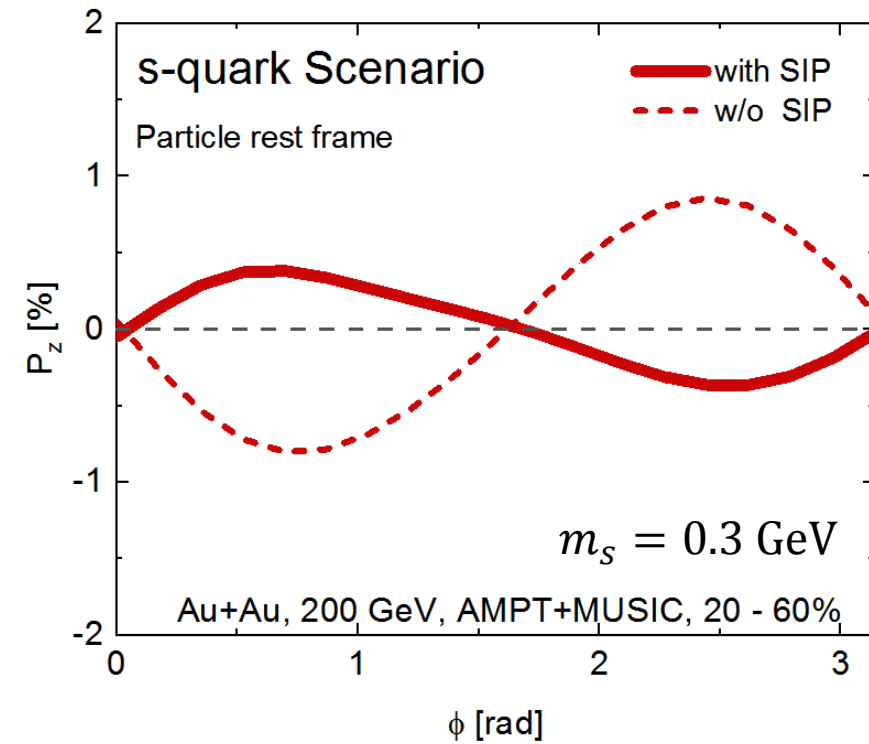
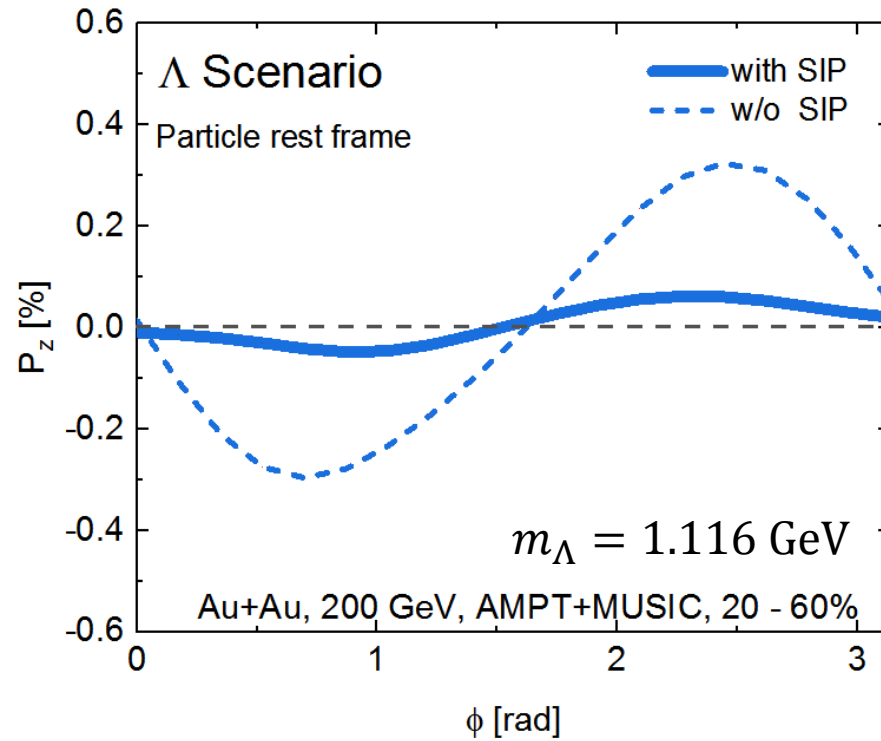
$P_z(\phi)$ with SIP

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

$$\text{Total } P^\mu = [\text{thermal vorticity}] + [\text{Shear}]$$



STAR, Phys.Rev.Lett. 123 (2019) 132301

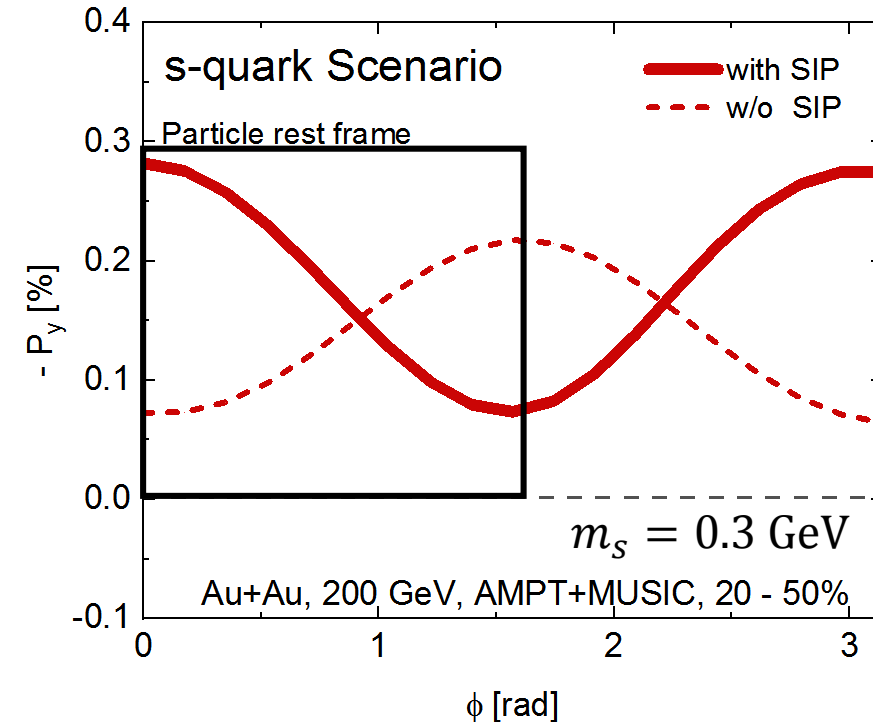
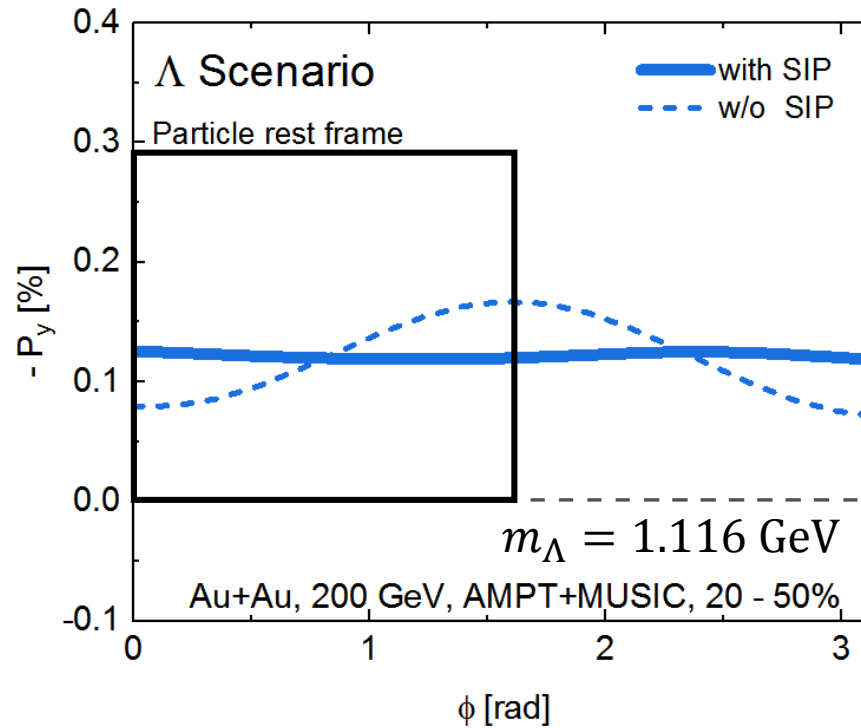
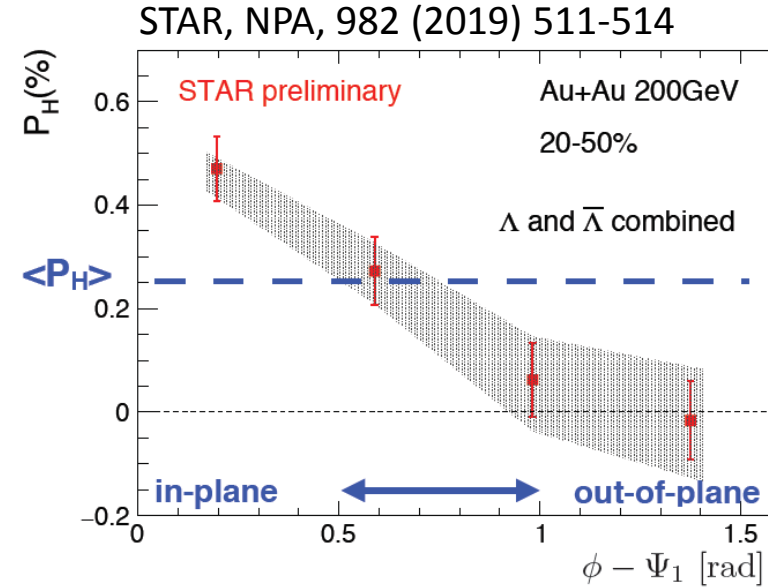


- In the scenario of 'S-quark memory', the total P^μ with SIP qualitatively agrees with data

$P_y(\phi)$ with SIP

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

$$\text{Total } P^\mu = [\text{thermal vorticity}] + [\text{shear}]$$

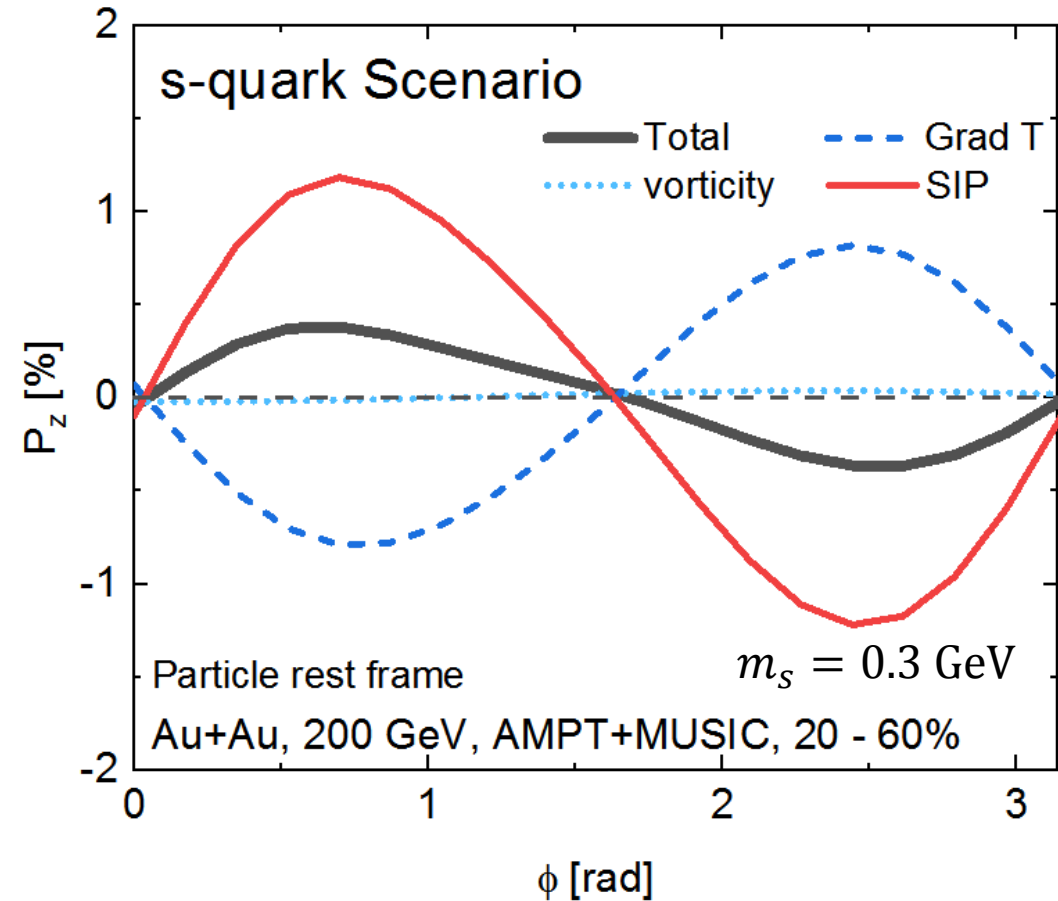
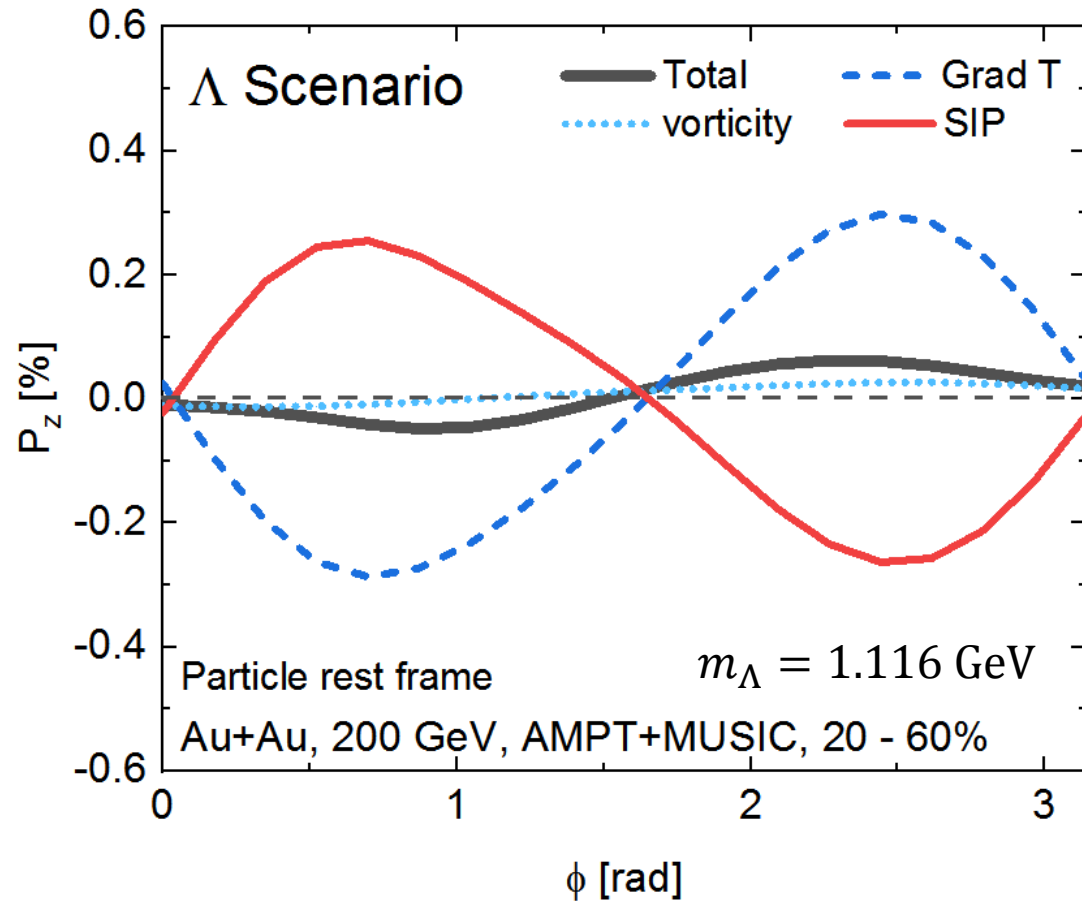


- In the scenario of ‘S-quark memory’, the total P^μ with SIP qualitatively agrees with data

Competition of P_z : Grad T vs. SIP

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

$$\text{Total } P^\mu = [\text{thermal vorticity}] + [\text{shear}] = [\text{vorticity}] + [\text{Grad T}] + [\text{shear}]$$

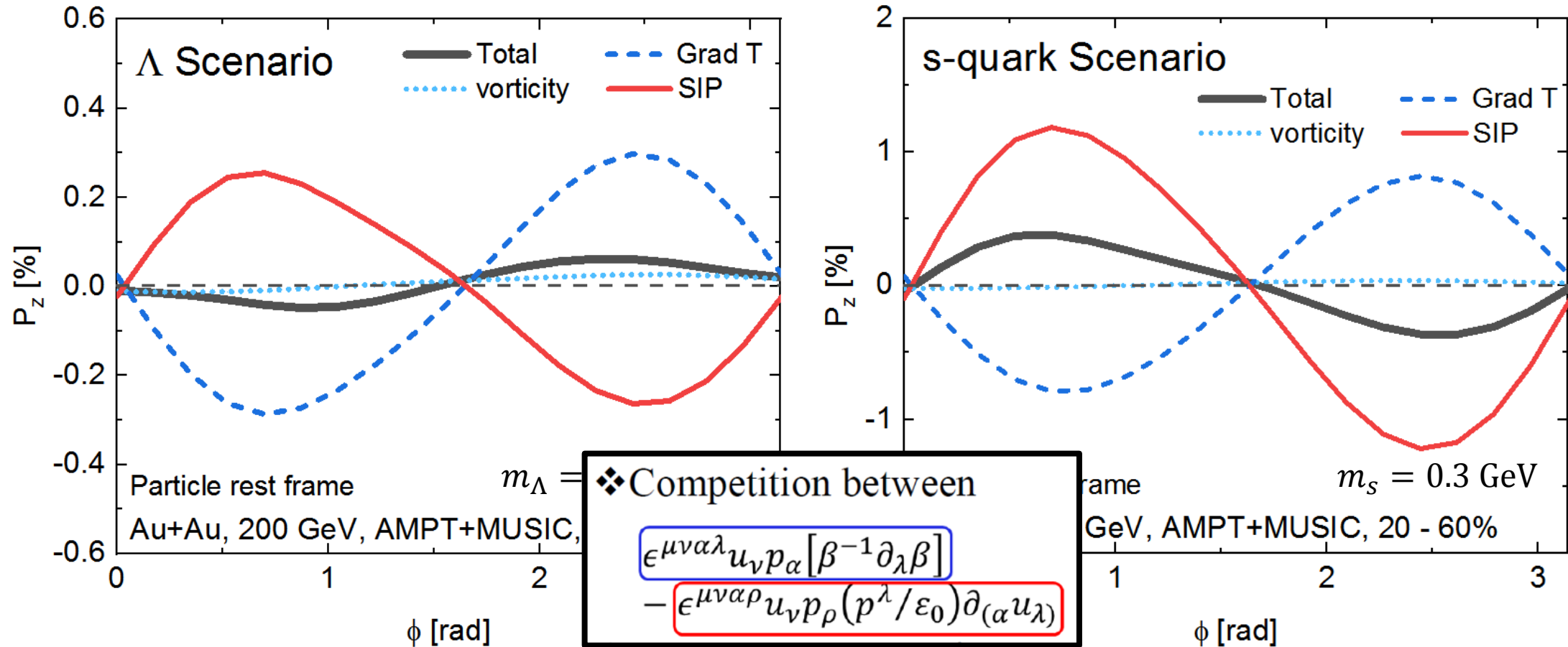


- [vorticity] ~ 0
- [SIP] and [Grad T] show similar magnitude but opposite sign

Competition of P_z : Grad T vs. SIP

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

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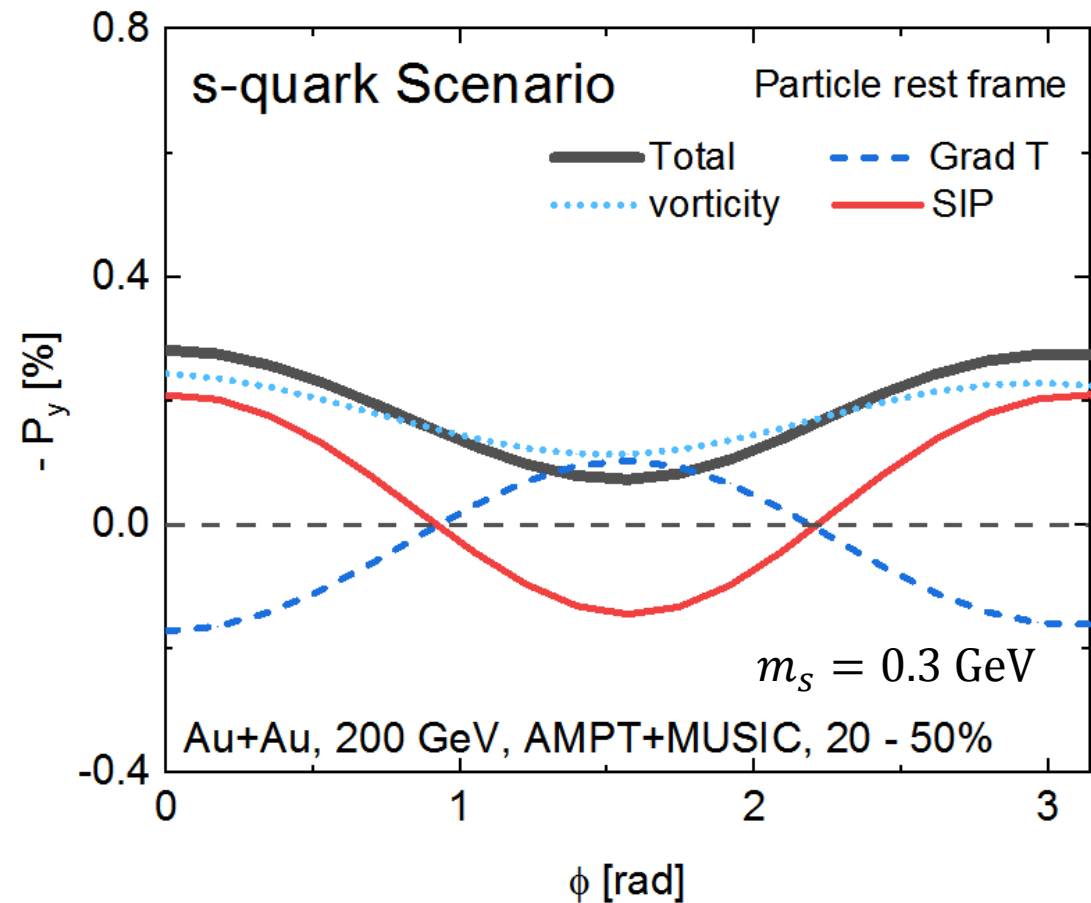
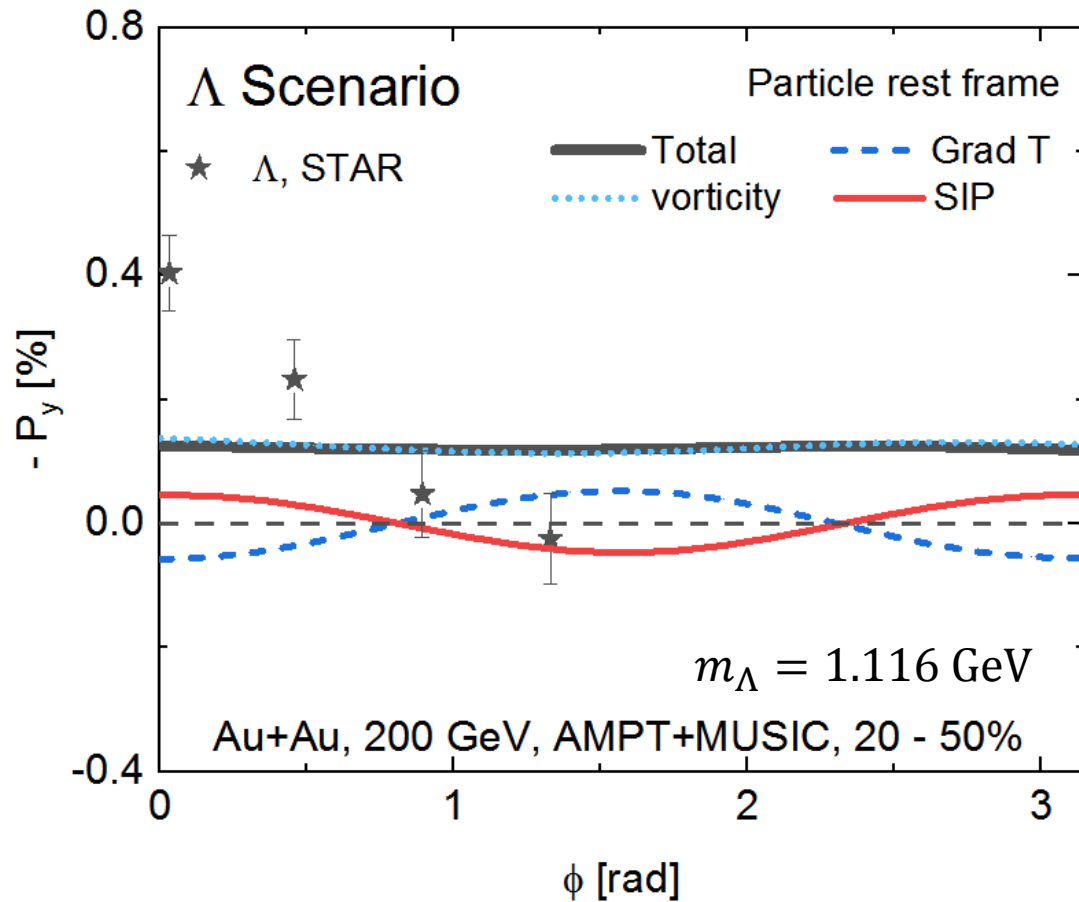


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Competition of P_y : Grad T vs. SIP

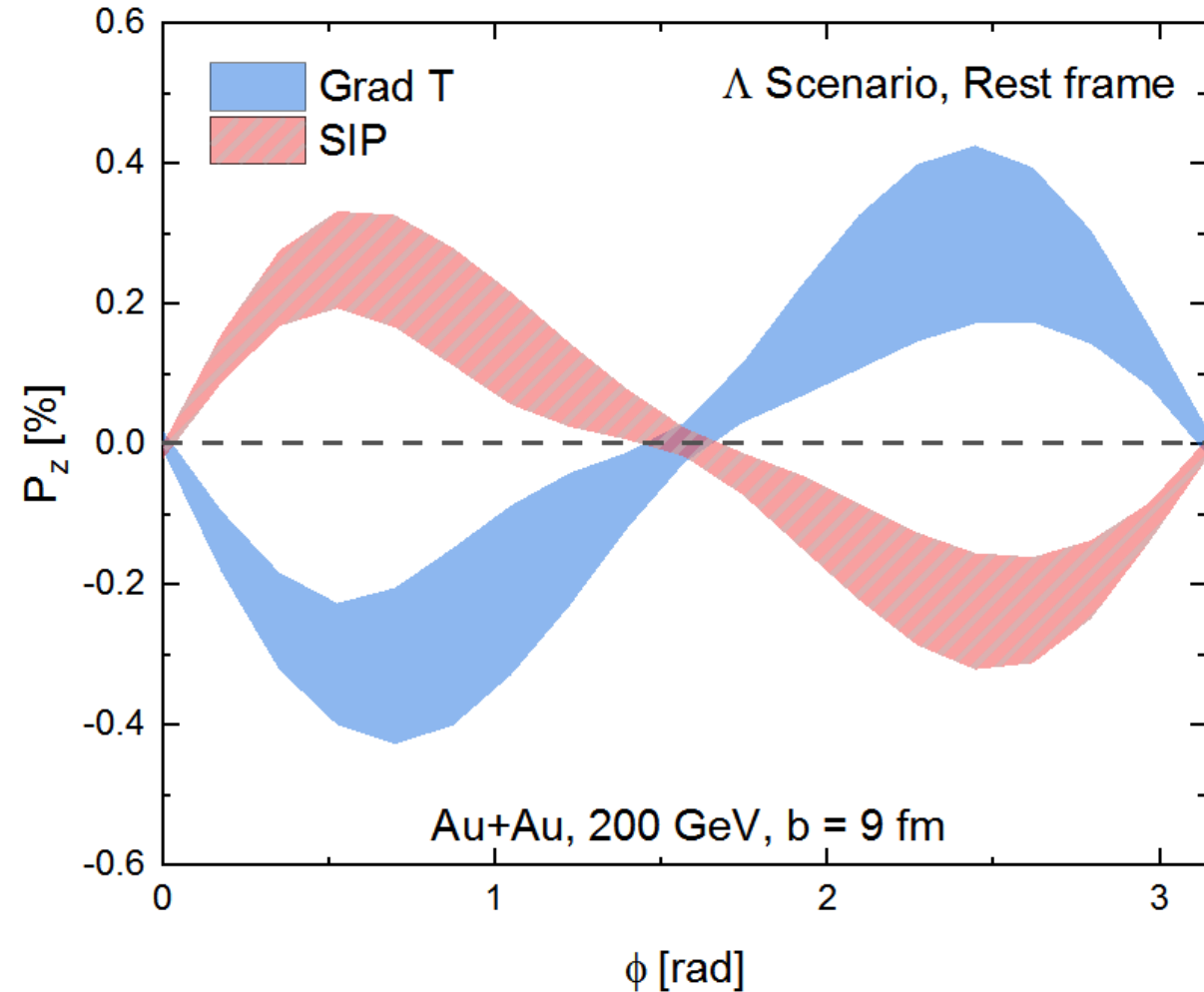
BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

$$\text{Total } P^\mu = [\text{thermal vorticity}] + [\text{shear}] = [\text{vorticity}] + [\text{Grad T}] + [\text{shear}]$$



- [vorticity] dominates the global polarization
- [SIP] and [Grad T] show similar magnitude but opposite sign

Robustness of the competition

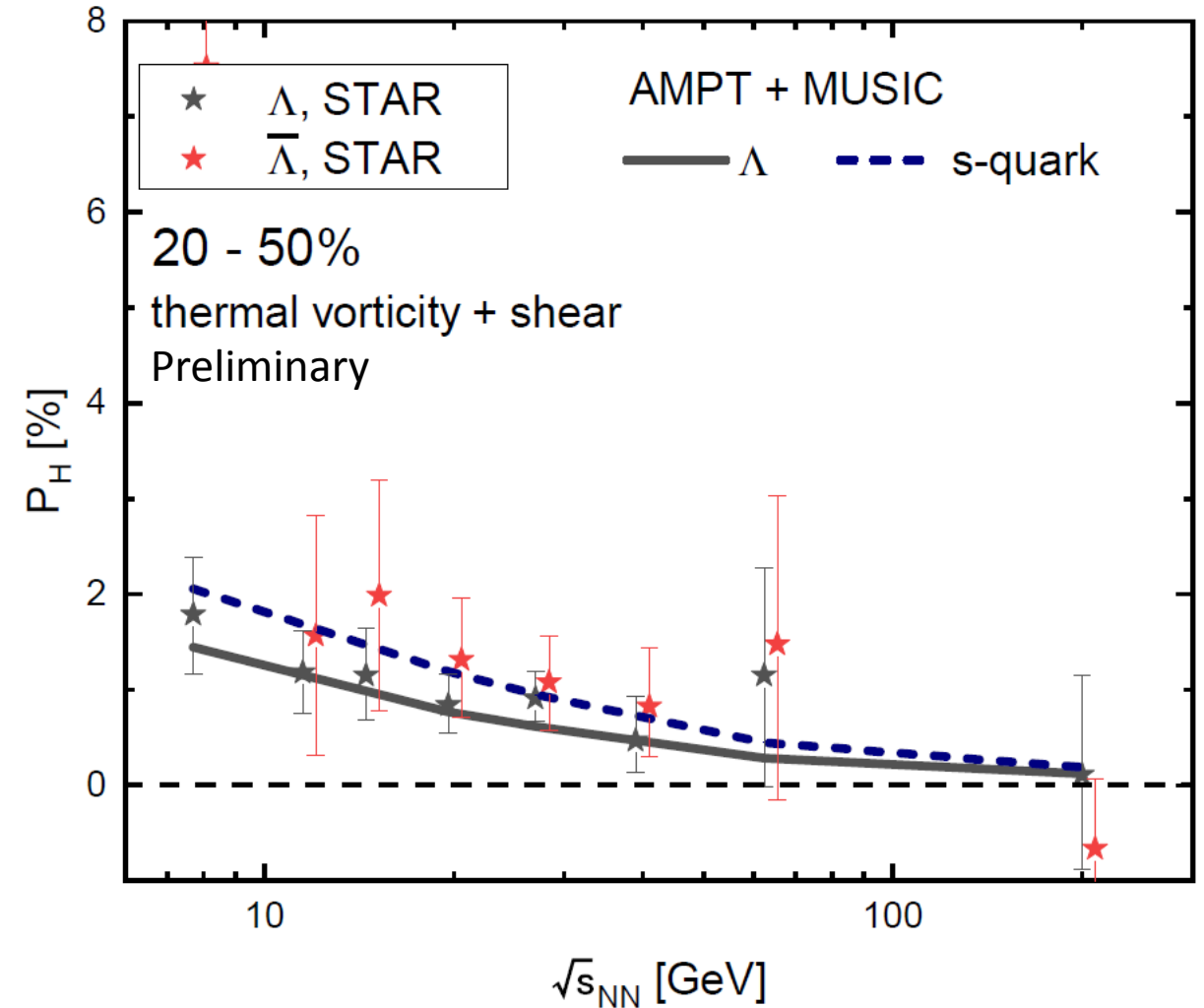
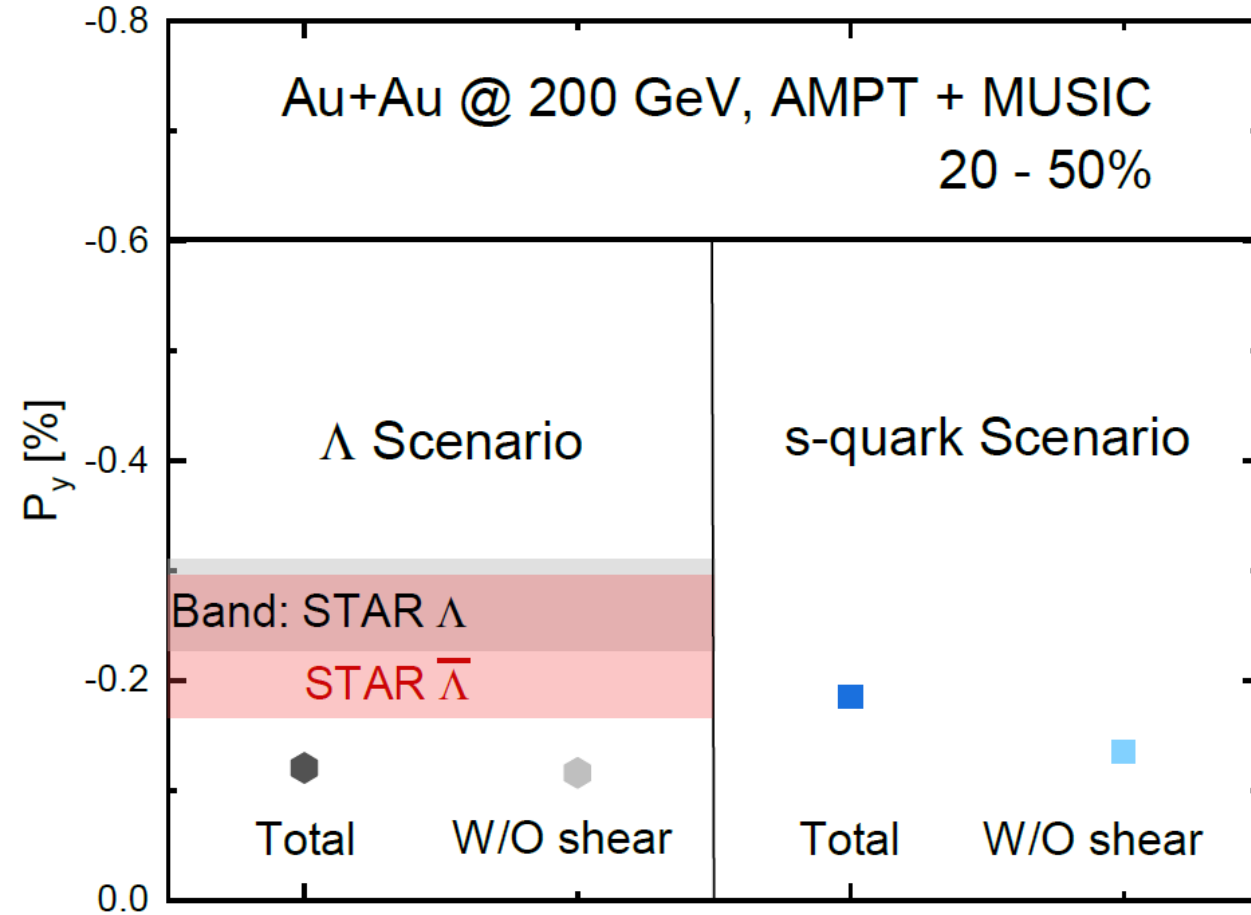


Band: possible flexibility of [Grad T] and [SIP]

- Initial flow: on \rightarrow off
- Initial condition: AMPT \rightarrow Glauber
- Shear viscosity: 0.08 \rightarrow off
- Bulk viscosity: $\zeta/s(T)$ \rightarrow off
- Freeze-out temperature:
167 MeV \rightarrow 157 MeV

Global polarization with shear effect

$$\text{Total } P^\mu = [\text{thermal vorticity}] + [\text{Shear}]$$



Sensitivity to frame

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

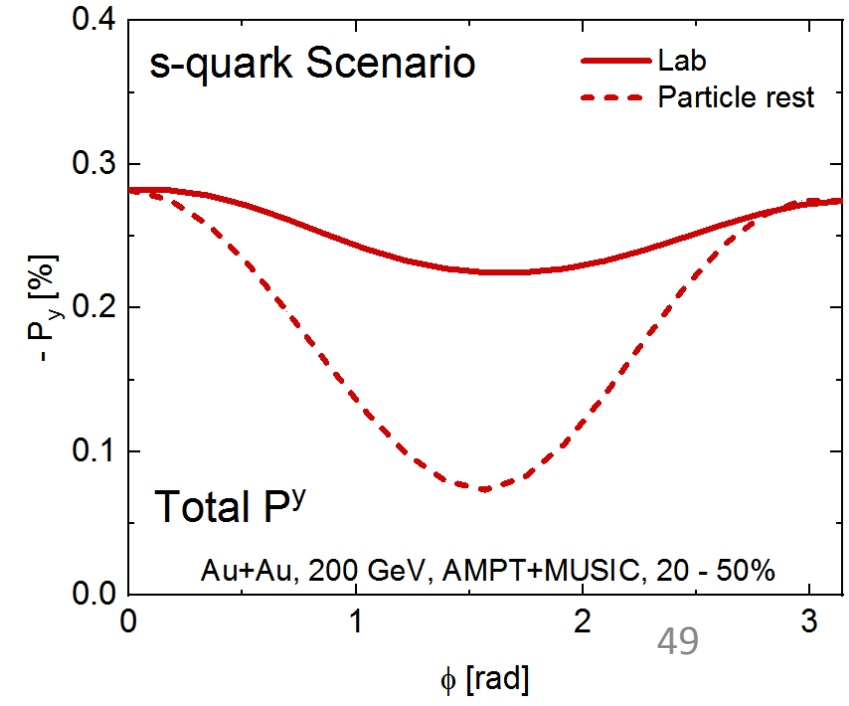
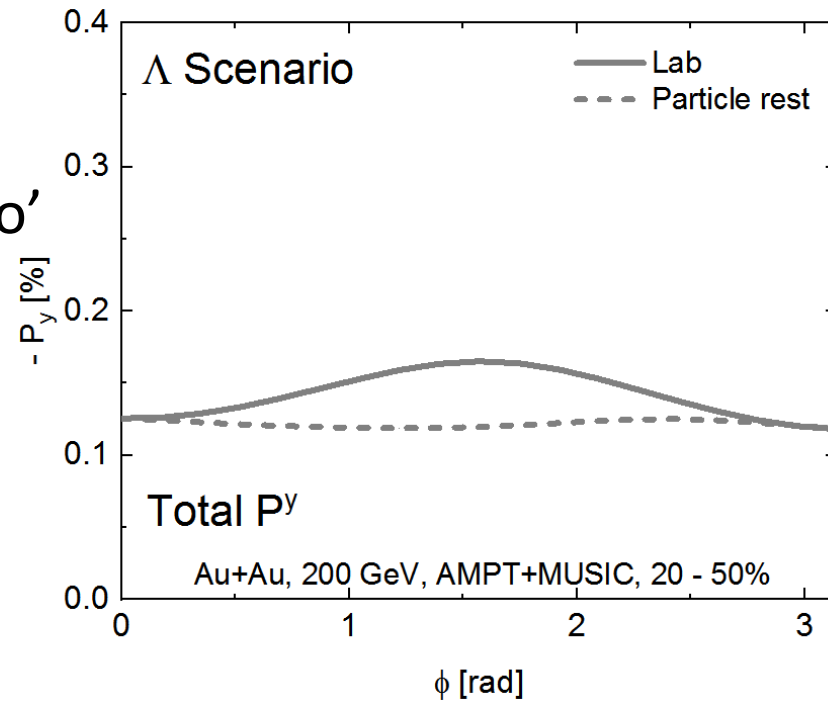
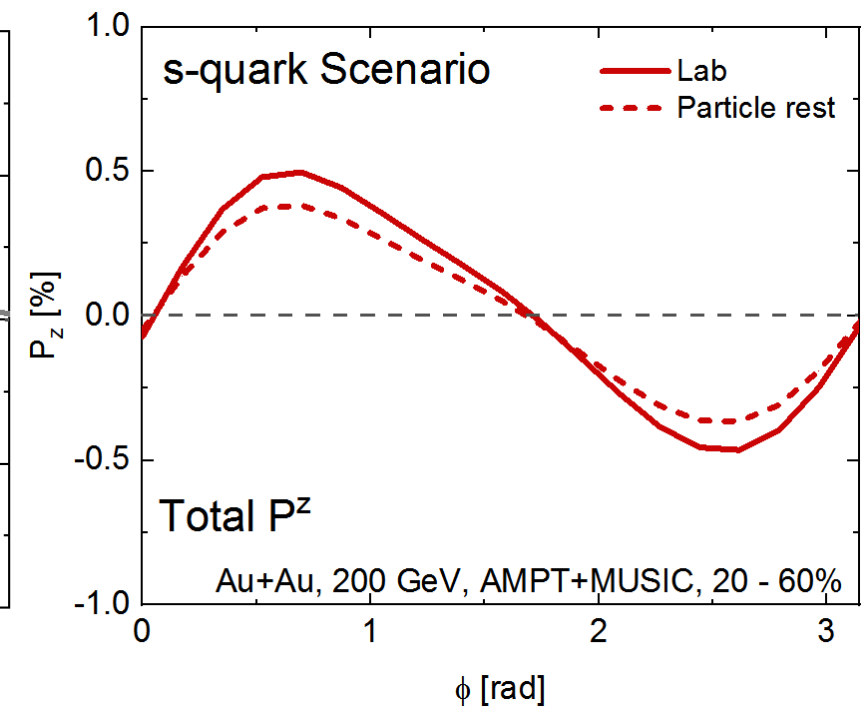
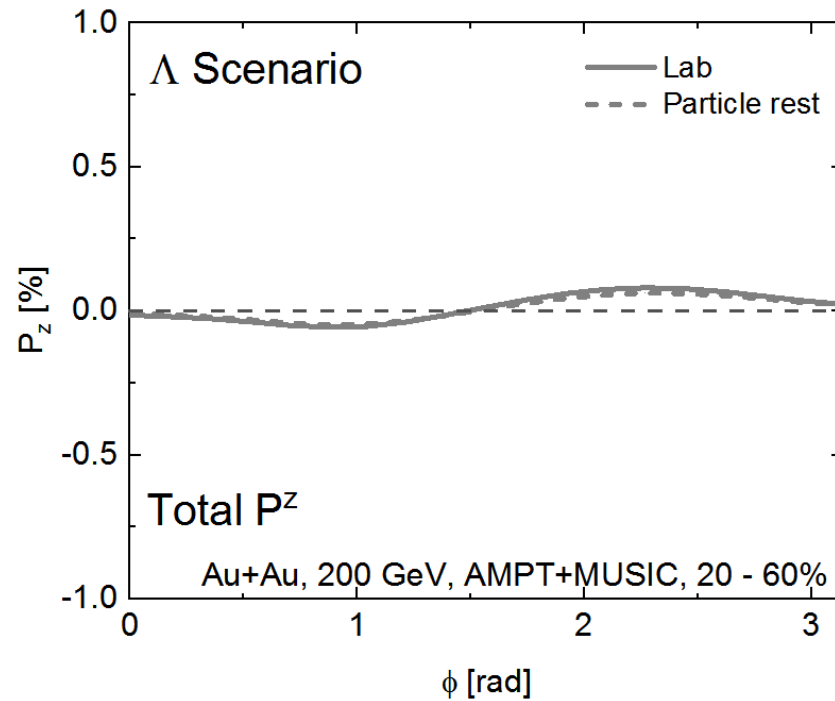
- $P^z(\phi)$

not sensitive to frame

- $P^y(\phi)$

sensitive to frame,

especially in 'S-quark scenario'



A brief comparison with F. Becattini's work

F. Becattini, et al. [arXiv: 2103.10917](#), [arXiv: 2103.14621](#)

- 1) The definition of (thermal) shear formula
- 2) T-gradient effect on freeze-out surface

Comparison with the results from F. Becattini

Spin polarization F. Becattini, et al. arXiv: 2103.10917, arXiv: 2103.14621

$$S^\mu = S_{\varpi}^\mu + S_{\xi}^\mu$$

Thermal vorticity effect:

$$S^\mu(p) = -\frac{1}{8m} \epsilon^{\mu\rho\sigma\tau} p_\tau \frac{\int_{\Sigma} d\Sigma \cdot p n_F (1 - n_F) \varpi_{\rho\sigma}}{\int_{\Sigma} d\Sigma \cdot p n_F}$$

$$\varpi_{\mu\nu} = -\frac{1}{2} (\partial_\mu \beta_\nu - \partial_\nu \beta_\mu)$$

Thermal shear effect:

$$S_{\xi}^\mu(p) = -\frac{1}{4m} \epsilon^{\mu\nu\sigma\tau} \frac{p_\tau p^\rho}{\epsilon} \frac{\int_{\Sigma} d\Sigma \cdot p n_F (1 - n_F) \hat{t}_\nu \xi_{\sigma\rho}}{\int_{\Sigma} d\Sigma \cdot p n_F}$$

$$\xi_{\mu\nu} = \frac{1}{2} (\partial_\mu \beta_\nu + \partial_\nu \beta_\mu)$$

Polarization formula used in our work:

$$A^\mu = \frac{1}{2} \beta n_0 (1 - n_0) \left\{ \underbrace{\epsilon^{\mu\nu\alpha\lambda} p_\nu \partial_\alpha^\perp u_\lambda + 2\epsilon^{\mu\nu\alpha\lambda} u_\nu p_\alpha [\beta^{-1} (\partial_\lambda \beta)]}_{\text{[Thermal vorticity]}} - \beta n_0 (1 - n_0) \frac{1}{\epsilon_0} \epsilon^{\mu\nu\alpha\rho} u_\nu p_\rho p^\lambda \partial_{(\alpha}^\perp u_{\lambda)} \right\}$$

[Thermal vorticity]

[Shear effect]

Comparison with the results from F. Becattini

Spin polarization F. Becattini, et al. arXiv: 2103.10917, arXiv: 2103.14621

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1) Different choice of \hat{t}_ν or u_ν

Comparison with the results from F. Becattini

Spin polarization F. Becattini, et al. arXiv: 2103.10917, arXiv: 2103.14621

$$S^\mu = S_\omega^\mu + S_\xi^\mu$$

Thermal vorticity effect:

$$S^\mu(p) = -\frac{1}{8m} \epsilon^{\mu\rho\sigma\tau} p_\tau \frac{\int_\Sigma d\Sigma \cdot p n_F (1 - n_F) \varpi_{\rho\sigma}}{\int_\Sigma d\Sigma \cdot p n_F}$$

Thermal shear effect:

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Polarization formula used in our work:

$$A^\mu = \frac{1}{2} \beta n_0 (1 - n_0) \left\{ \underbrace{\epsilon^{\mu\nu\alpha\lambda} p_\nu \partial_\alpha^\perp u_\lambda}_{\text{[Thermal vorticity]}} + 2 \epsilon^{\mu\nu\alpha\lambda} u_\nu p_\alpha \underbrace{[\beta^{-1} (\partial_\lambda^\perp \epsilon_0)]}_{\text{[Shear effect]}} \right\}$$

1) Different choice of \hat{t}_ν or u_ν

If we change $\hat{t}_\nu \rightarrow u_\nu$ in Becattini's definition:

- **Identical** definition of total polarization

$$P^\mu = \text{[thermal vorticity]} + \text{[shear]}$$

- Using the equation of motion:

$$(u \cdot \partial) u_\mu = -\beta^{-1} \partial_\mu^\perp \beta$$

the [thermal vorticity] and [shear]

definition are identical individually

Same (not precisely the same) formula

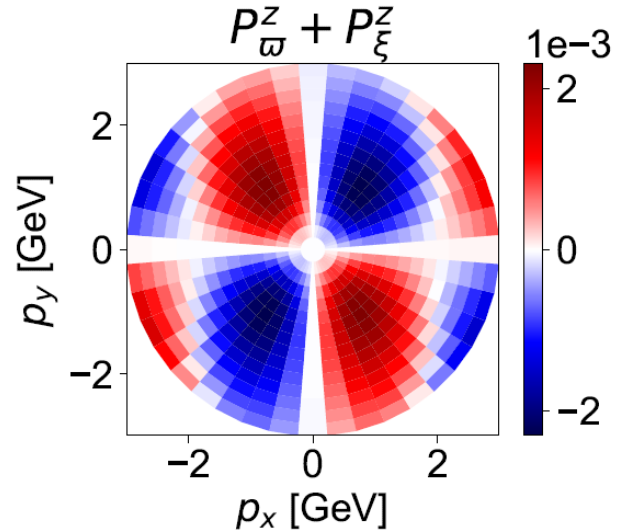
* From F. Becattini's HENPIC talk

Comparison with the results from F. Becattini

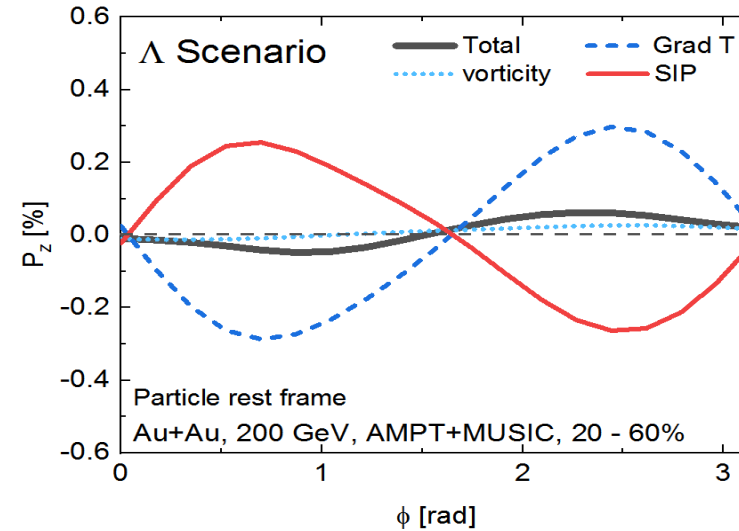
2) T-gradient effect

- Simply use $P^\mu = [\text{thermal vorticity}] + [\text{shear}]$ for Λ hyperon can't reproduce the sign

F. Becattini, et al. arXiv: 2103.14621



BF, S. Liu, L. -G. Pang, H. Song, Y. Yin, arXiv: 2103.10403

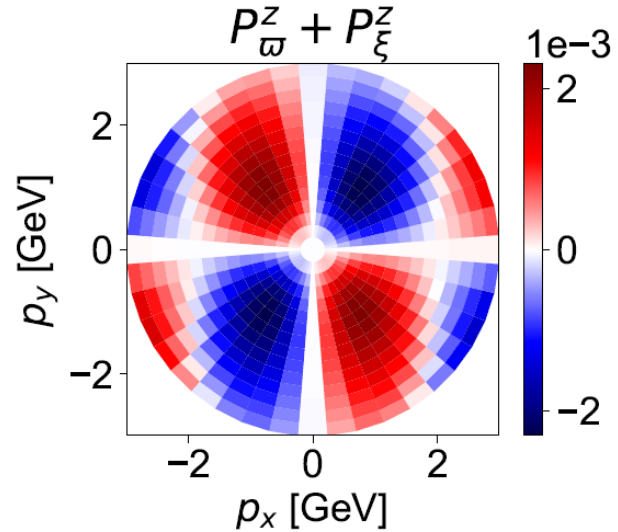


Comparison with the results from F. Becattini

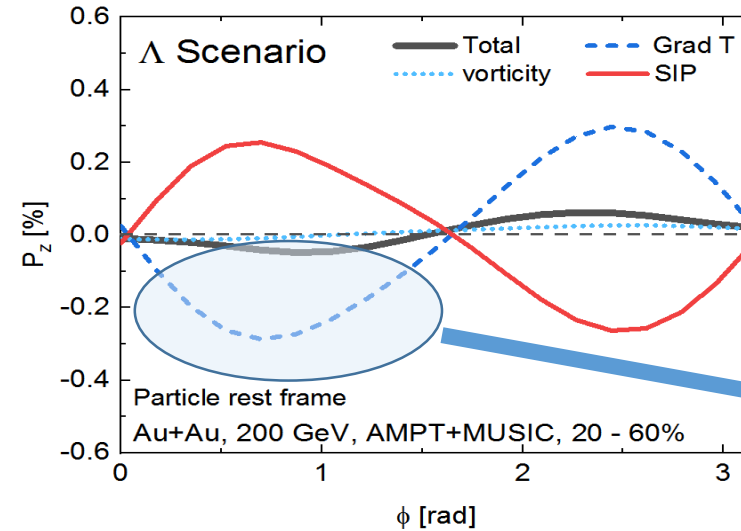
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BF, S. Liu, L. -G. Pang, H. Song, Y. Yin, arXiv: 2103.10403



T-gradient

- They assume the T-gradient is negligible (isothermal freeze-out)

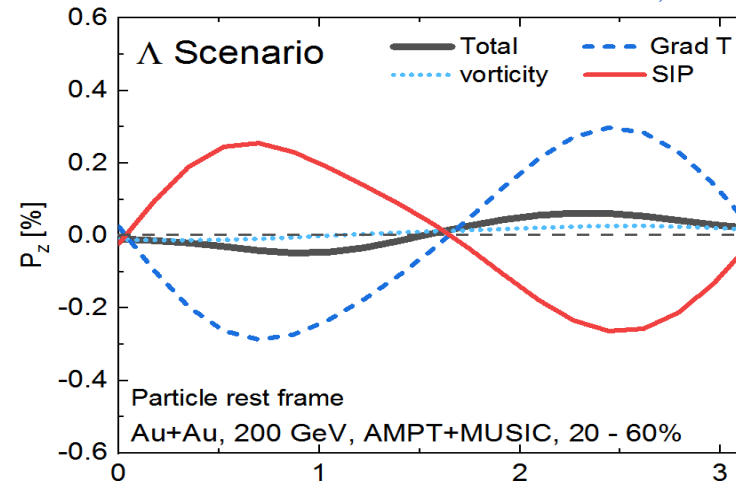
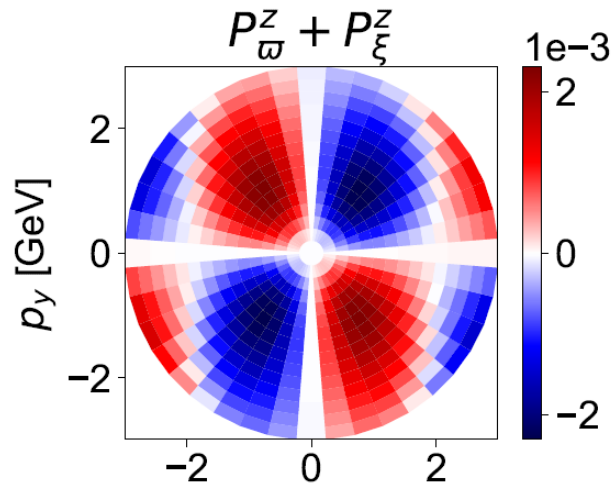
[thermal vorticity]	$\varpi_{\mu\nu} = -\frac{1}{2} (\partial_\mu \beta_\nu - \partial_\nu \beta_\mu)$	\Rightarrow	$\omega_{\rho\sigma} = \frac{1}{2} (\partial_\sigma u_\rho - \partial_\rho u_\sigma)$	[kinetic vorticity]
[thermal shear]	$\xi_{\mu\nu} = \frac{1}{2} (\partial_\mu \beta_\nu + \partial_\nu \beta_\mu)$	\Rightarrow	$\Xi_{\rho\sigma} = \frac{1}{2} (\partial_\sigma u_\rho + \partial_\rho u_\sigma)$	[kinetic shear]

Comparison with the results from F. Becattini

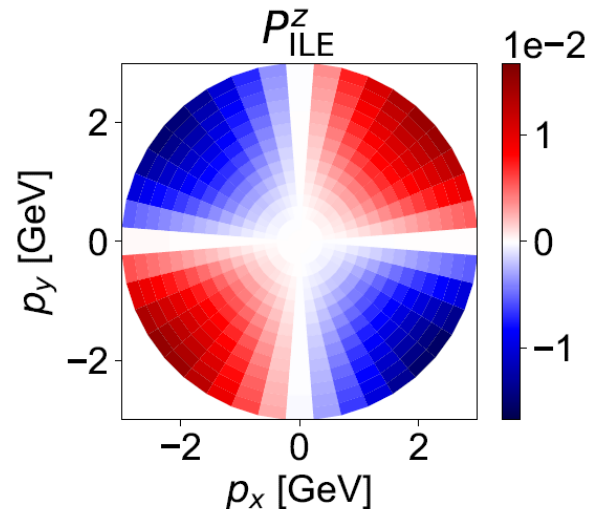
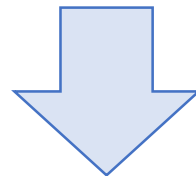
2) T-gradient effect

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

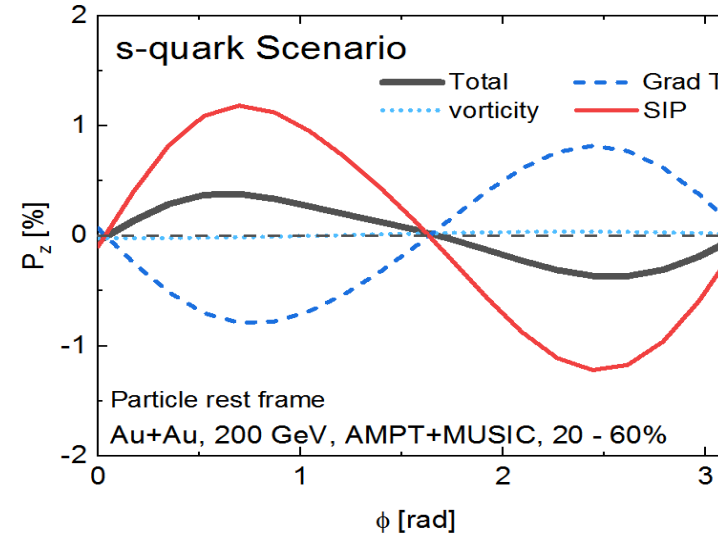
F. Becattini, et al.
arXiv: 2103.14621



T-gradient excluded



T-gradient included
Using s-quark scenario



Comparison with the results from F. Becattini

2) T-gradient effect

BF, S. Liu, L. -G. Pang, H. Song, Y. Yin,
arXiv: 2103.10403

F. Becattini, et al.
arXiv: 2103.14621

- 1) Different choice of \hat{t}_ν or u_ν (almost same)
- 2) T-gradient effect is included in our work (conventional pic.)

[thermal vorticity] + [shear]

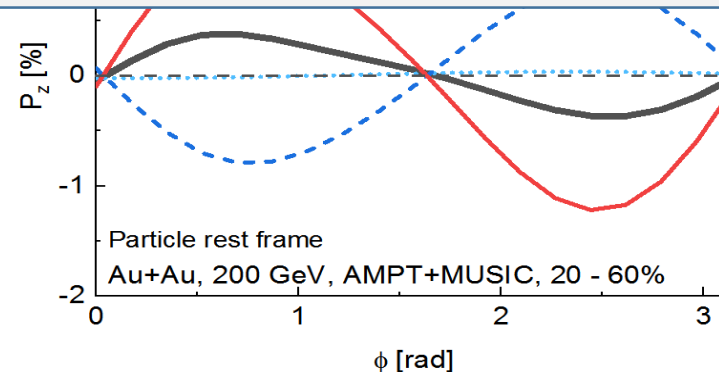
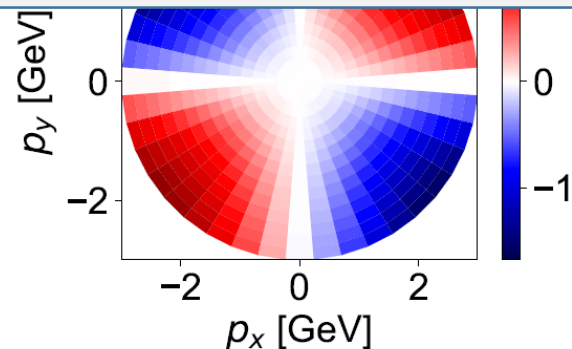
and excluded in the result of arXiv: 2103.14621

[kinematic vorticity] + [kinematic shear]

Shear is important and contribute a 'right' sign in both cases!

T-gradient ex

ent included
-quark scenario



Summary & Outlook

- Spin polarization opens a new door to study the properties of QCD matter
- Conventional thermal vorticity describes the global polarization but fails at local polarization
- New discovered shear effect always provides 'same sign' like experimental data
- 'Strange memory' scenario might provide insights on the hadronization mechanism

- To quantitative calculation: spin hadronization / hadronic evolution
- Higher order observables like v_3 in collective flow
- Will it helps to understand the spin alignment puzzle?

Back up

Comparison with the results from F. Becattini

The isothermal freeze-out picture (F. Becattini, et al. arXiv: 2103.10917, arXiv: 2103.14621)

- Taylor expansion of the density operator (take T outside in isothermal assumption)

$$\hat{\rho}_{\text{LE}} \simeq \frac{1}{Z_{\text{LE}}} \exp \left[-\beta_\nu(x) \hat{P}^\nu - \partial_\lambda \beta_\nu(x) \int_\Sigma d\Sigma_\mu(y) (y-x)^\lambda \hat{T}^{\mu\nu}(y) \right] \quad \Rightarrow \quad \hat{\rho}_{\text{LE}} \simeq \frac{1}{Z_{\text{LE}}} \exp \left[-\beta_\nu(x) \hat{P}^\nu + \right. \\ \left. - \frac{1}{T} \partial_\lambda u_\nu(x) \int_\Sigma d\Sigma_\mu(y) (y-x)^\lambda \hat{T}^{\mu\nu}(y) \right]$$

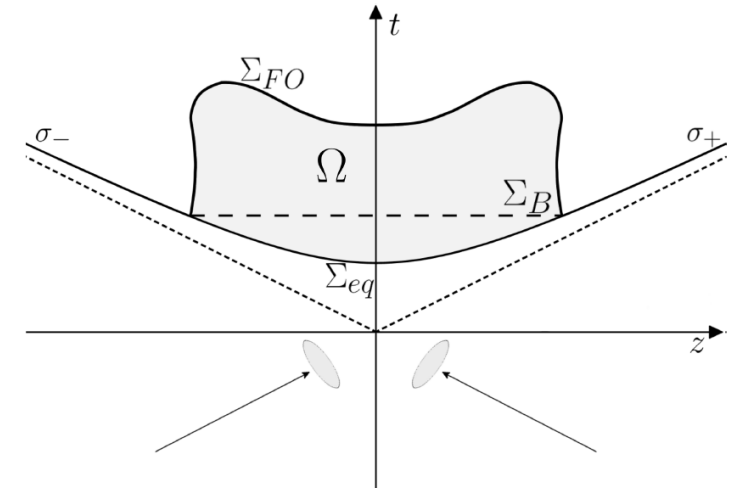
$$\beta_\nu(y) \simeq \beta_\nu(x) + \partial_\lambda \beta_\nu(x) (y-x)^\lambda$$

- Is it self-consistent with the definition of equal-time surface?

$$\widehat{W}_{ab}^+(x, k) = \theta(k^0) \theta(k^2) \frac{1}{(2\pi)^4} \int d^4s e^{-ik \cdot s} : \bar{\Psi}_b(x + s/2) \Psi_a(x - s/2) :$$

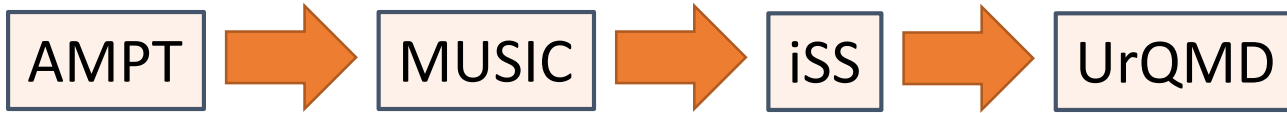
$$\langle \widehat{W}_{ab}^+(x, k) \rangle_{\text{LE}} \simeq \langle \widehat{W}_{ab}^+(x, k) \rangle_{\beta(x)} + \Delta W_{ab}^+(x, k),$$

$$\Delta W_{ab}^+(x, k) = - \int_0^1 dz \int_\Sigma d\Sigma_\lambda(y) \Delta \beta_\rho(x, y) \langle \widehat{W}_{ab}^+(x, k) \hat{T}^{\lambda\rho}(y + iz\beta(x)) \rangle_{c, \beta(x)}$$



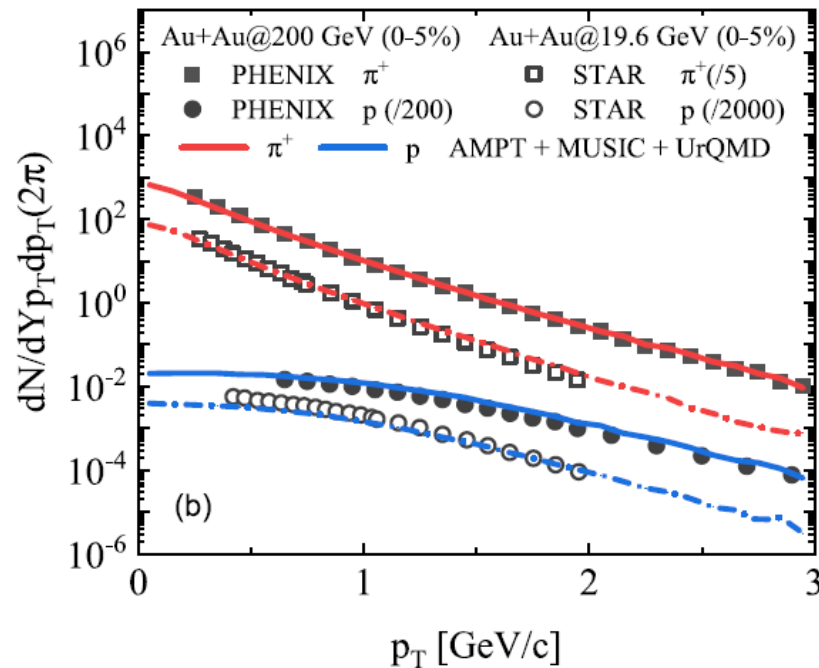
Well calibrated hydrodynamic model

BF, K. Xu, X-G, Huang, H. Song,
Phys.Rev.C 103 (2021) 2, 024903

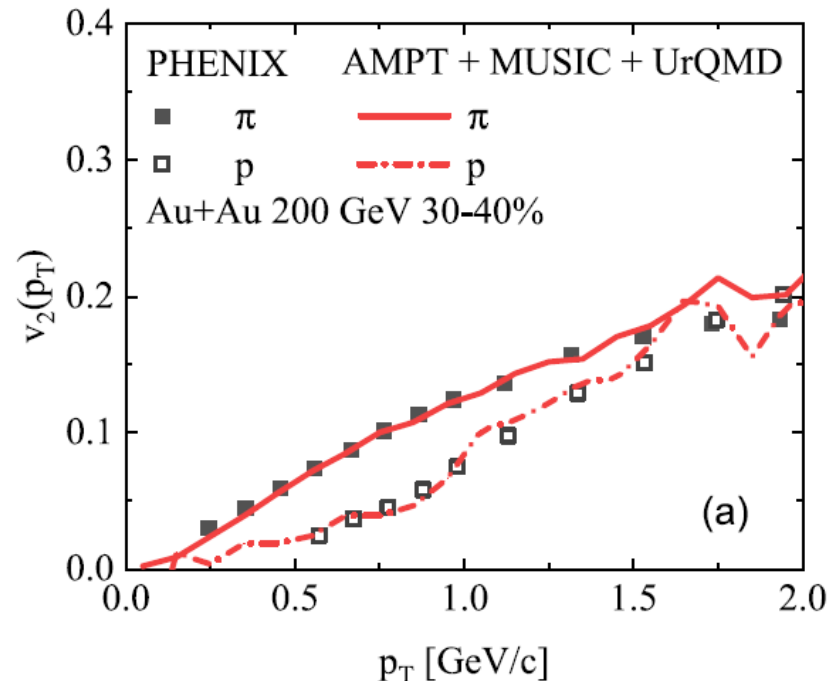


Parameters are tuned to reproduce the soft hadron observables

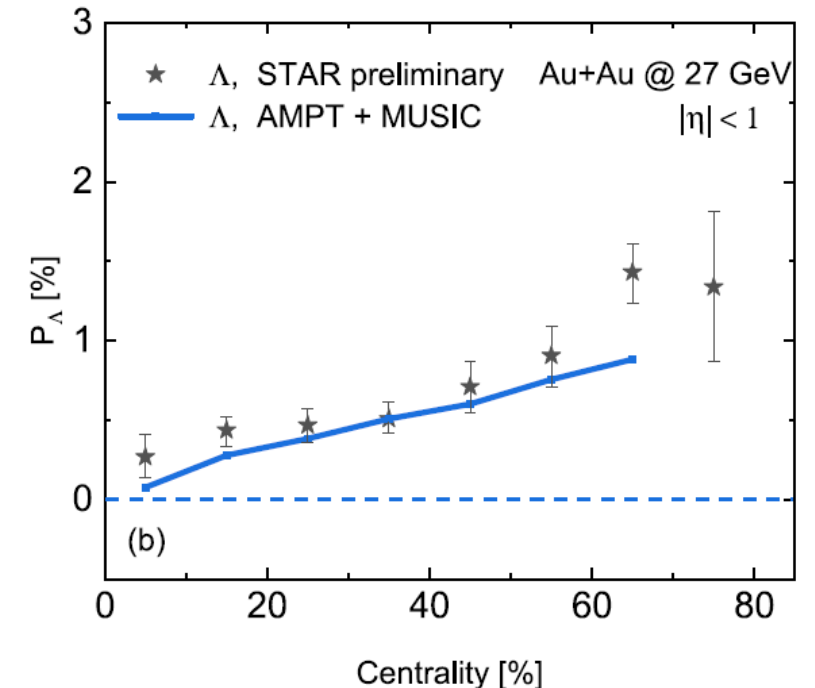
Transverse momentum spectra



$v_2(p_T)$



Global Polarization from thermal vorticity



Shear Induce Polarization (SIP)

The formula can be rewritten in a more friendly way:

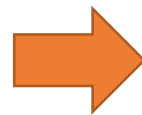
$$S^\mu(x, p) = \mathcal{A}^\mu / 4m = \beta n_{\text{FD}}(1 - n_{\text{FD}}) \left[\underbrace{-(p \cdot \omega^\mu) u^\mu}_{\text{[vorticity]}} + \underbrace{\varepsilon_u \omega^\mu + \varepsilon^{\mu\nu\alpha\lambda} u_\nu p_\alpha (\partial_{\perp, \lambda} \log \beta)}_{\text{[Grad T]}} - \underbrace{\varepsilon^{\mu\nu\alpha\lambda} \frac{u_\nu}{\varepsilon_u} Q_\alpha^\rho Q_{\lambda\rho}}_{\text{[SIP]}} \right]$$

The standard formula from thermal vorticity:

$$S^\mu(x, p) = -\frac{1}{8m} (1 - f) \left\{ \underbrace{\frac{1}{T} (2(p \cdot u) \omega^\mu - 2(p \cdot \omega) u^\mu)}_{\text{[vorticity]}} + \underbrace{\varepsilon^{\mu\nu\rho\sigma} p_\nu \partial_\rho (1/T) u_\sigma}_{\text{[Grad T / 2]}} + \underbrace{\frac{1}{T} \varepsilon^{\mu\nu\rho\sigma} p_\nu u_\rho D u_\sigma}_{\text{[Acceleration / 2]}} \right\}$$

If the fluid is ideal and uncharged:

$$\text{[Acceleration]} = \text{[Grad T]}$$



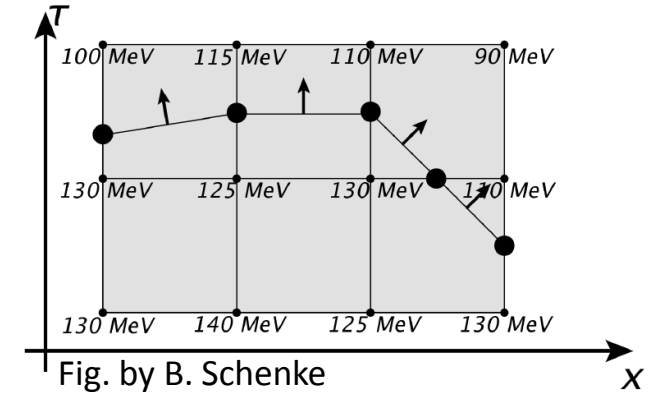
$$\begin{aligned} \text{Total } P^\mu &= \text{[vorticity]} + \text{[Grad T]} + \text{[SIP]} \\ &= \text{[thermal vorticity]} + \text{[SIP]} \end{aligned}$$

Comparison with the results from F. Becattini

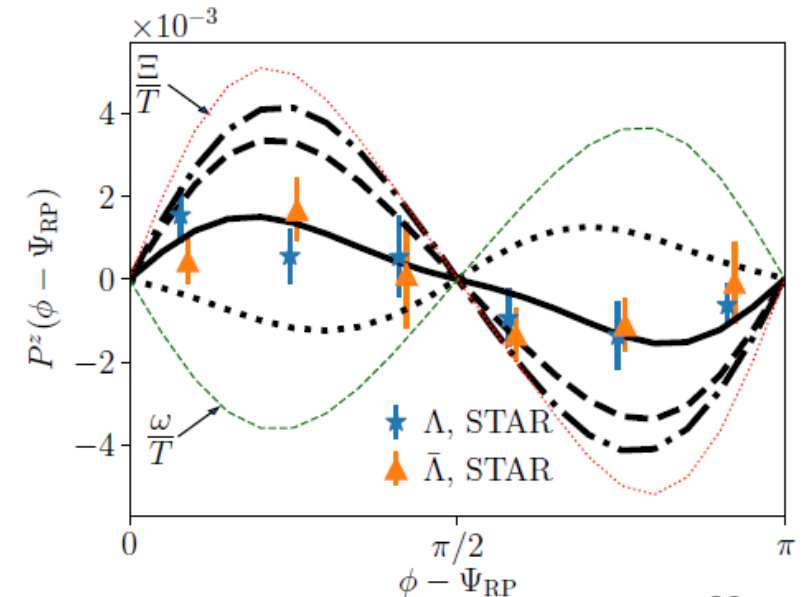
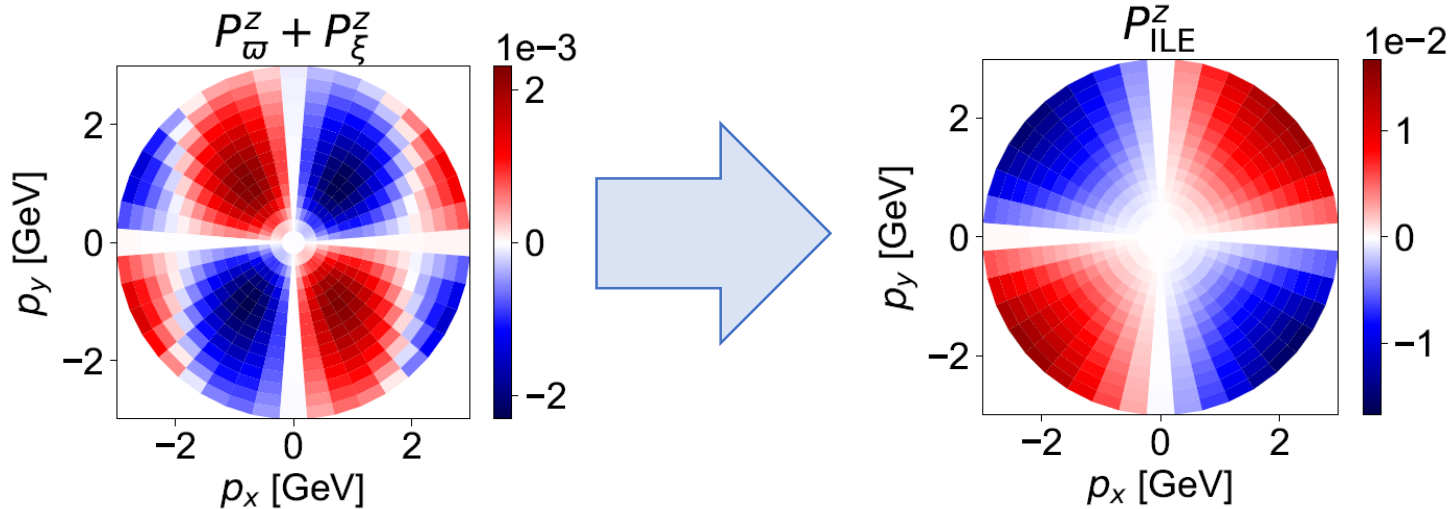
The isothermal freeze-out picture (F. Becattini, et al. arXiv: 2103.14621)

$$S_{\text{ILE}}^\mu(p) = -\epsilon^{\mu\rho\sigma\tau} p_\tau \frac{\int_\Sigma d\Sigma \cdot p n_F (1 - n_F) \left[\omega_{\rho\sigma} + 2 \hat{t}_\rho \frac{p^\lambda}{\epsilon} \Xi_{\lambda\sigma} \right]}{8mT_{\text{dec}} \int_\Sigma d\Sigma \cdot p n_F}$$

$$\omega_{\rho\sigma} = \frac{1}{2} (\partial_\sigma u_\rho - \partial_\rho u_\sigma) \quad \Xi_{\rho\sigma} = \frac{1}{2} (\partial_\sigma u_\rho + \partial_\rho u_\sigma)$$



- With the T-gradient removed, the thermal vorticity (shear) is replaced by kinematic vorticity (shear)



1) T-gradient on the freeze-out surface