

Equation of state of dense matter from multi-messenger observations of neutron stars

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Contents

- Introduction on dense matter;
- Symmetry energy, maximum mass, typical radius, strange phase transition;
- Take-home message

Neutron stars as dense matter probes

- QCD: The theory which describes the interaction of nucleons and quarks;
- Heavy-ion collisions (HICs) and lattice QCD (LQCD) sensitive primarily to high T , low μ regions;
- Electromagnetic (EM) and gravitational wave (GW) observations of neutron stars are ideal probe of cold, dense QCD.

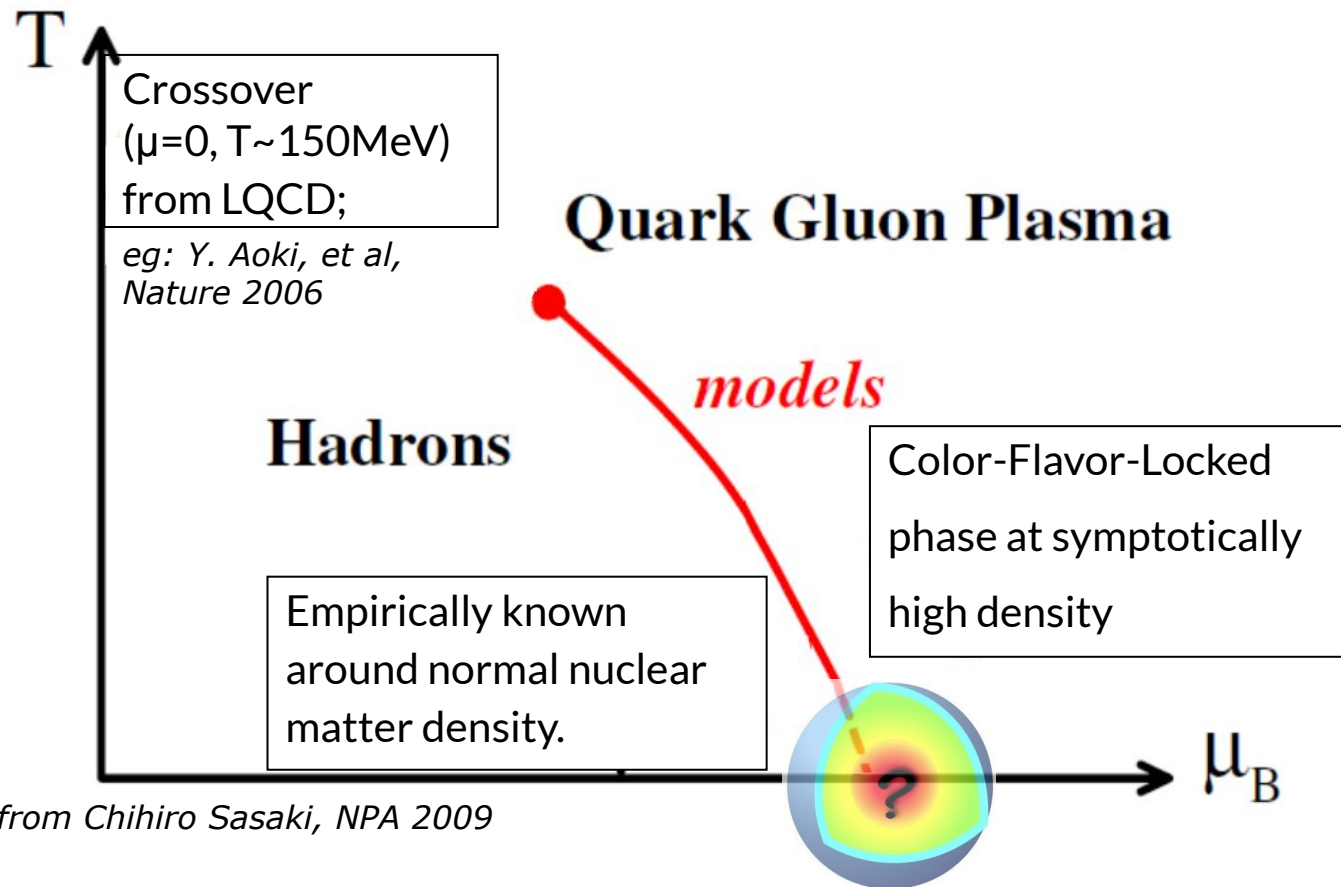


Fig. from Chihiro Sasaki, NPA 2009

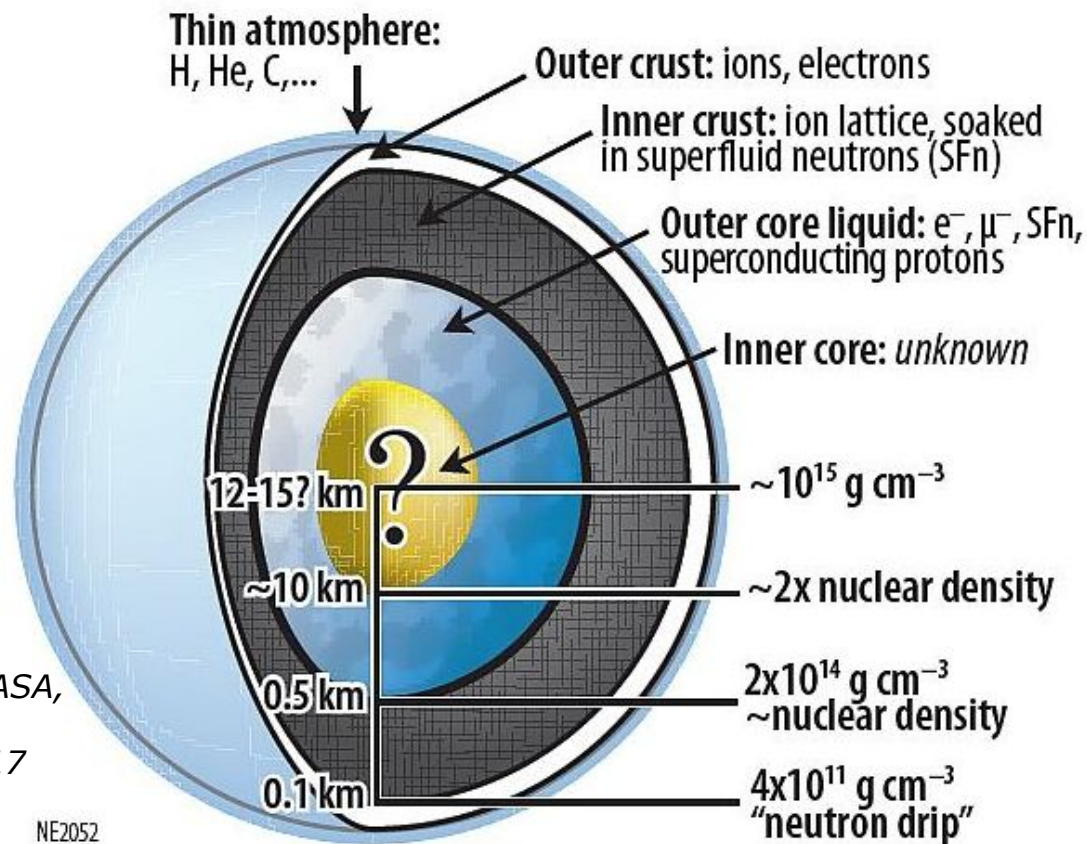
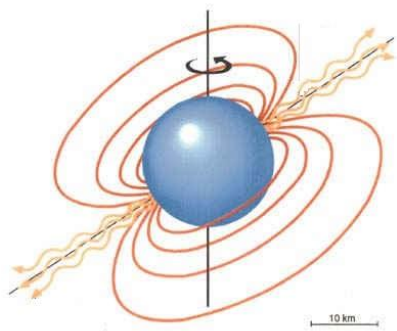
Neutron star structure and size

- Radius: $R \sim 10 - 13.6 \text{ km}$; Mass $M \sim 1.2 - 3 M_{\odot}$;
- For $R = 10 \text{ km}$, $M = 1.4 M_{\odot}$, average number density $\sim 0.4 \text{ fm}^{-3}$; average (energy) density: $\sim 6.9 \times 10^{14} \text{ g/cm}^3 \sim (2-3)\rho_0$;
- Spin frequency $\sim 714 \text{ Hz}$ (fastest known); Magnetic fields: $\sim 10^8 - 10^{14} \text{ G}$.



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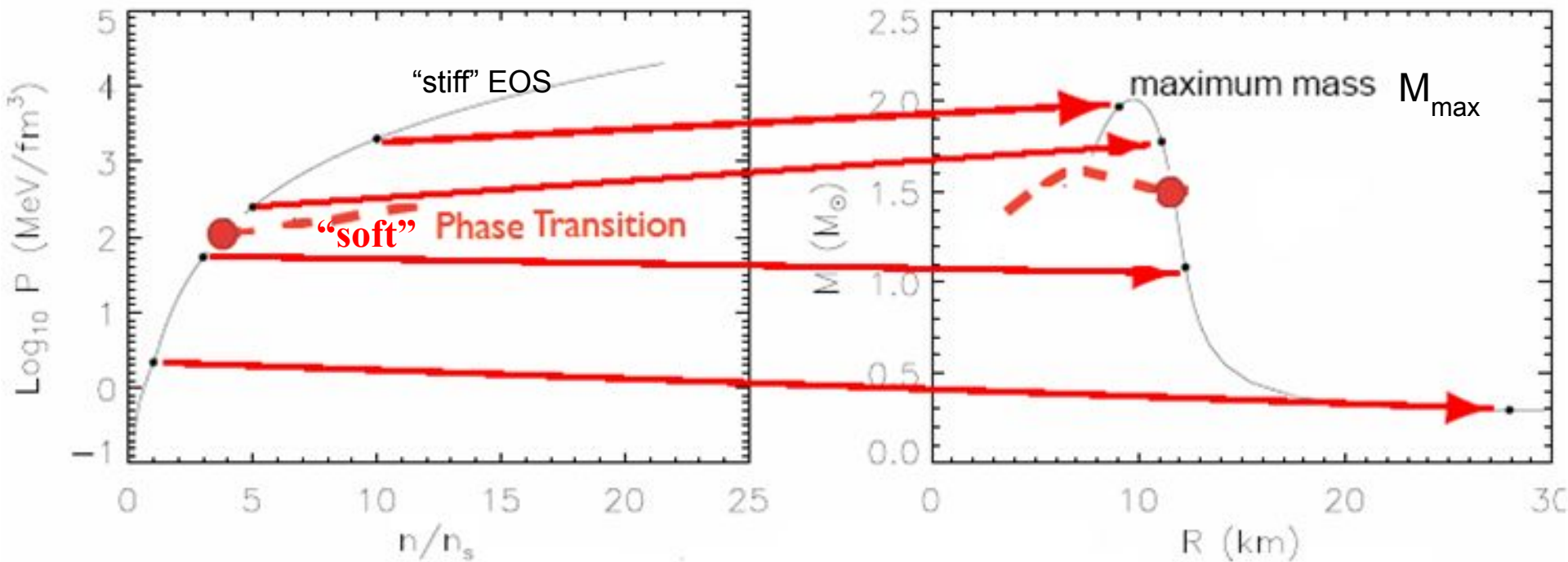


(image credit: NASA,
NICER Team)
Launch: Feb. 2017

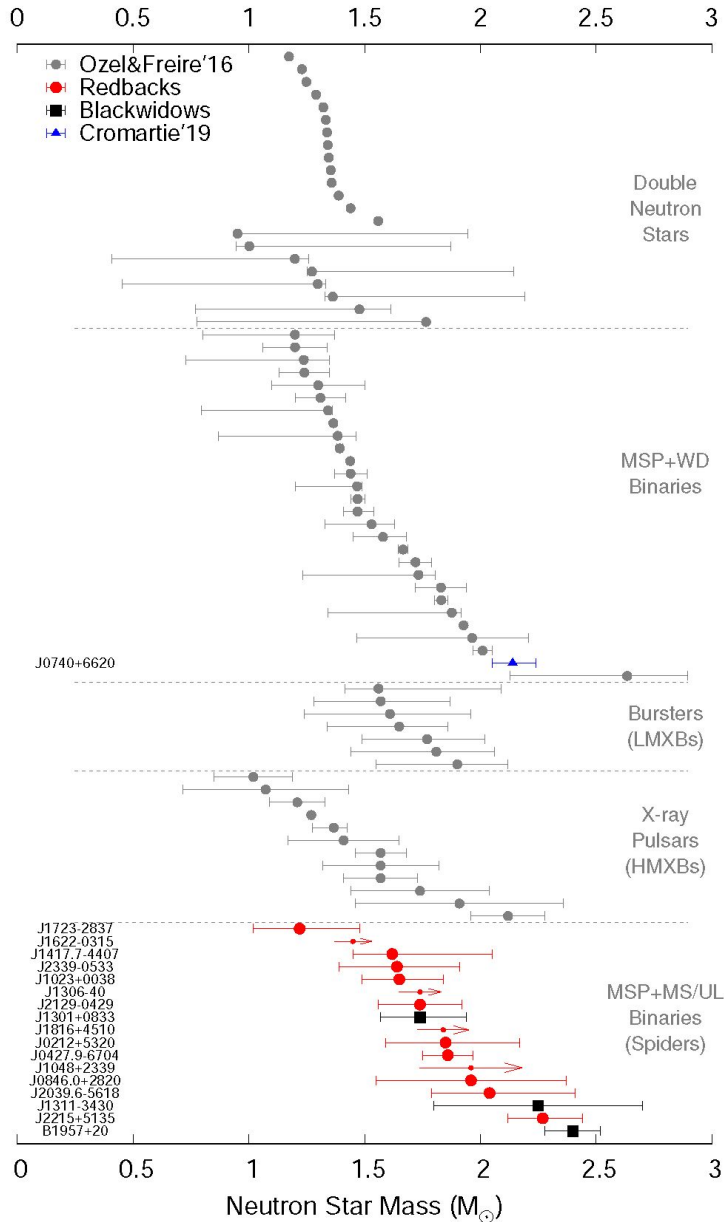
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Neutron star M-R relation and the equation of state

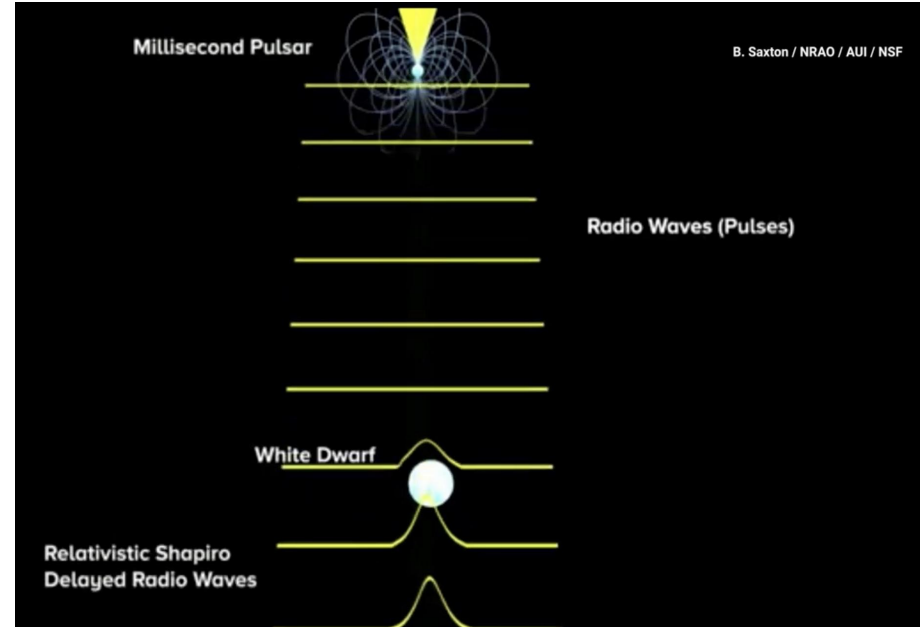
- M-R relation is unique to the underlying equation of state (EOS):
- $M_{\text{max}}(\text{EOS}) \geq \text{all measured neutron star masses};$
- $M_{\text{max}} \geq 2.14^{+0.20}_{-0.18} M_{\odot}$: **Very stringent constraint on the EOS!**



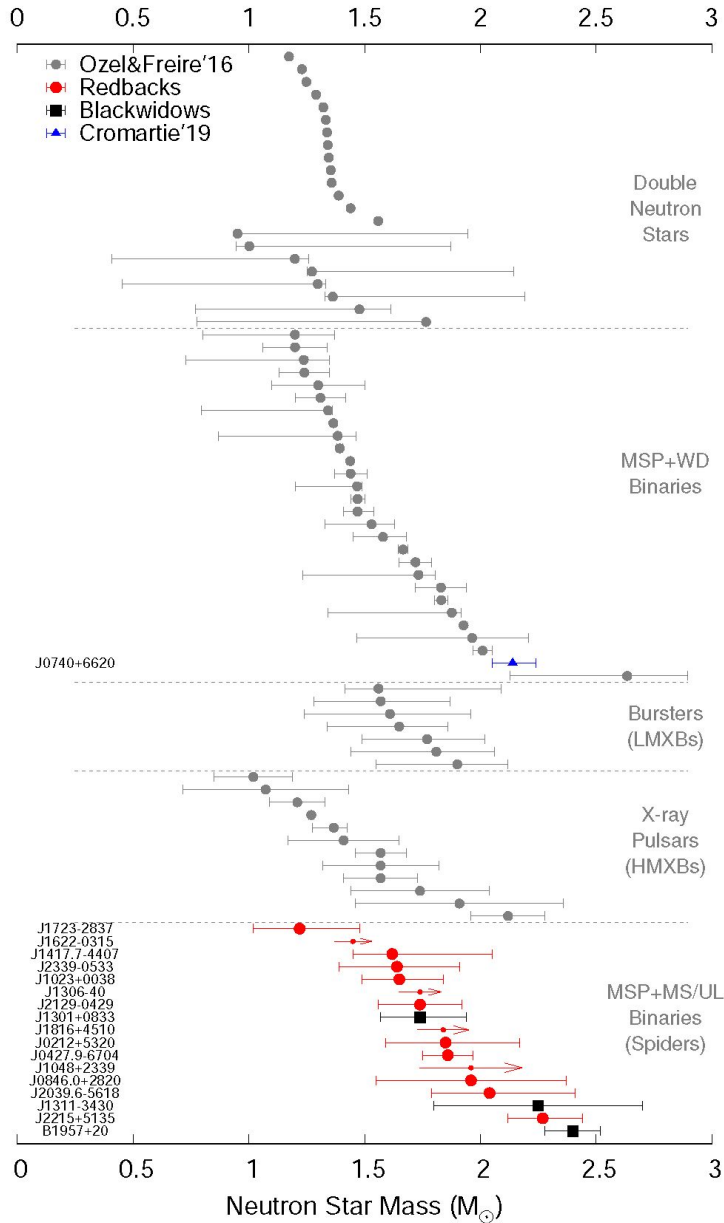
Neutron star maximum mass: Observational



- $M_{\max}(\text{EOS}) \geq \text{all measured neutron star masses};$
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Neutron star maximum mass: Observational

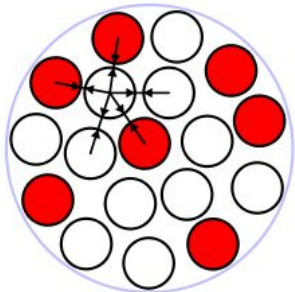


- $M_{\max}(\text{EOS}) \geq \text{all measured neutron star masses};$
- $M_{\max} \geq 2.14^{+0.20}_{-0.18} M_{\odot}$: **Very stringent constraint on the EOS!**

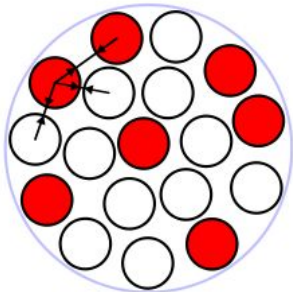


Basic things about EOS

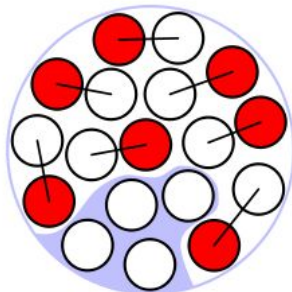
Nuclear binding



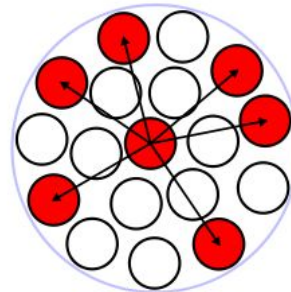
Volume



Surface



Asymmetry



Coulomb

$$B(A, Z) = a_V A + a_S A^{\frac{2}{3}} + S_N \frac{(N - Z)^2}{A} + a_C \frac{Z^2}{A^{\frac{1}{3}}}$$

$$4\pi R^2$$

$$R = R_0 A^{1/3}$$

$$R^2 \propto A^{2/3}$$

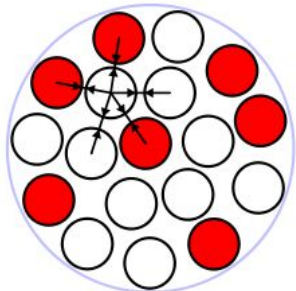
$$\frac{Q_1 Q_2}{4\pi\epsilon_0 R}$$

$$\propto \frac{1}{R}$$

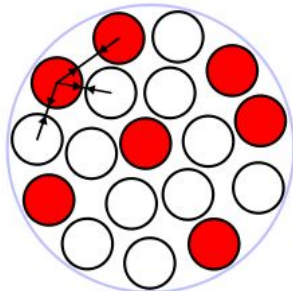
$$\propto \frac{1}{A^{1/3}}$$

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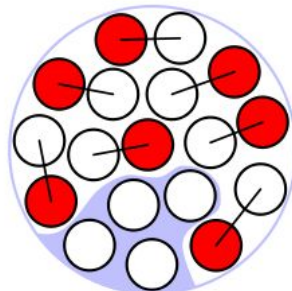
Nuclear matter = infinite uniform system of nucleons interacting through the strong interaction



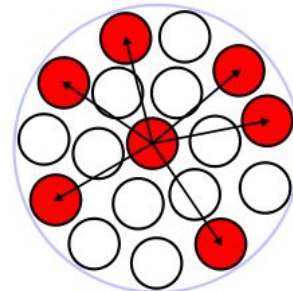
Volume



Surface



Asymmetry



Coulomb

$$V \rightarrow \infty$$

$$A \rightarrow \infty$$

$$Z \rightarrow \infty$$

$$A/V = \rho \neq \infty$$

$$B(A, Z) = a_V A + a_S A^{2/3} + S_N \frac{(N - Z)^2}{A} + a_C \frac{Z^2}{A^{1/3}}$$

$$4\pi R^2$$

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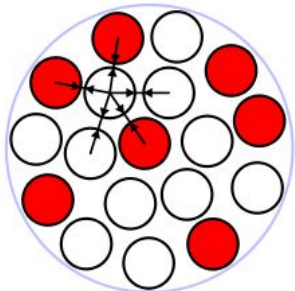
$$R^2 \propto A^{2/3}$$

$$\frac{Q_1 Q_2}{4\pi\epsilon_0 R}$$

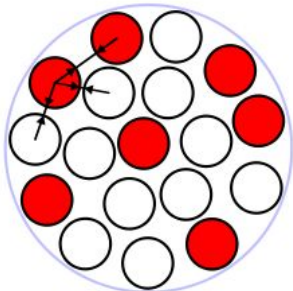
$$\propto \frac{1}{R}$$

$$\propto \frac{1}{A^{1/3}}$$

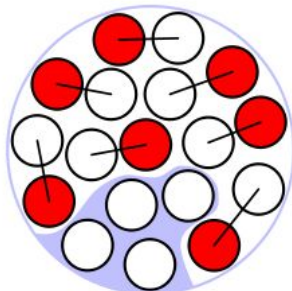
Nuclear matter equation of state, mainly $P(\rho)$



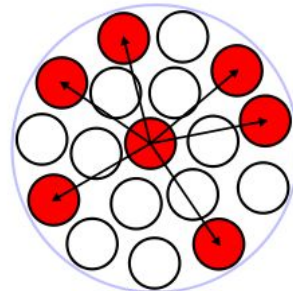
Volume



Surface



Asymmetry



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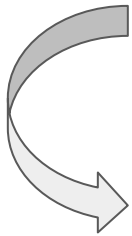
$$V \rightarrow \infty$$

$$A \rightarrow \infty$$

$$Z \rightarrow \infty$$

$$A/V = \rho \neq \infty$$

$$B(A, Z) = a_V A + a_S A^{\frac{2}{3}} + S_N \frac{(N - Z)^2}{A} + a_C \frac{Z^2}{A^{\frac{1}{3}}}$$



$$E(\rho, \delta) \approx E_0(\rho) + E_{\text{sym}}(\rho) \delta^2$$

$$(N-Z)/A \rightarrow$$

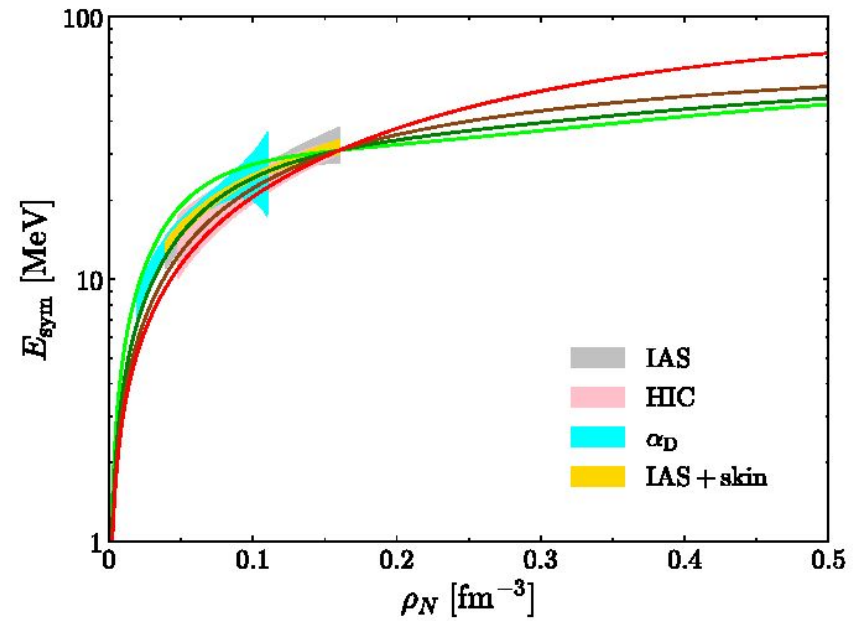
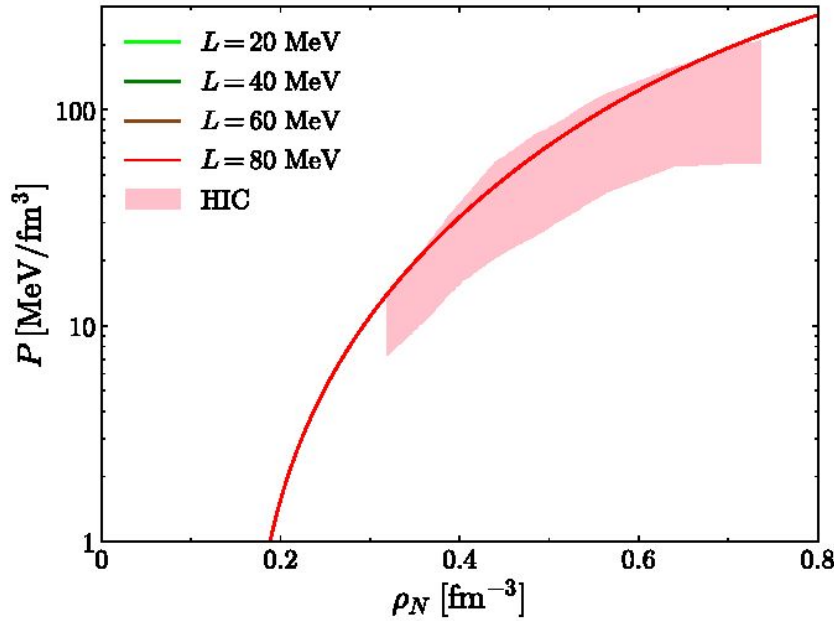
$$\delta = (\rho_n - \rho_p)/\rho$$

$$P(\rho) = \rho^2 (\partial^2 E / \partial^2 \rho) \quad \text{symmetry energy}$$

$$L(\rho) = dE_{\text{sym}}(\rho)/d\rho$$

Nuclear matter equation of state, mainly $P(\rho)$

- $L \sim 30-60$ MeV, if following ab-initio calculations and other constraints.



$$E(\rho, \delta) \approx E_0(\rho) + E_{\text{sym}}(\rho)\delta^2$$

$$P(\rho) = \rho^2 (\partial^2 E / \partial^2 \rho) \quad \text{symmetry energy}$$

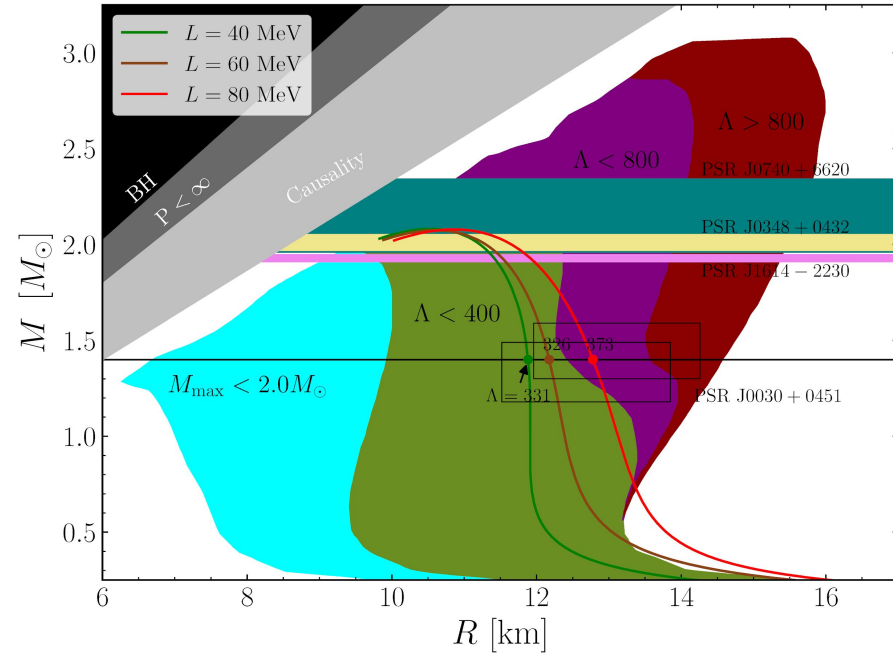
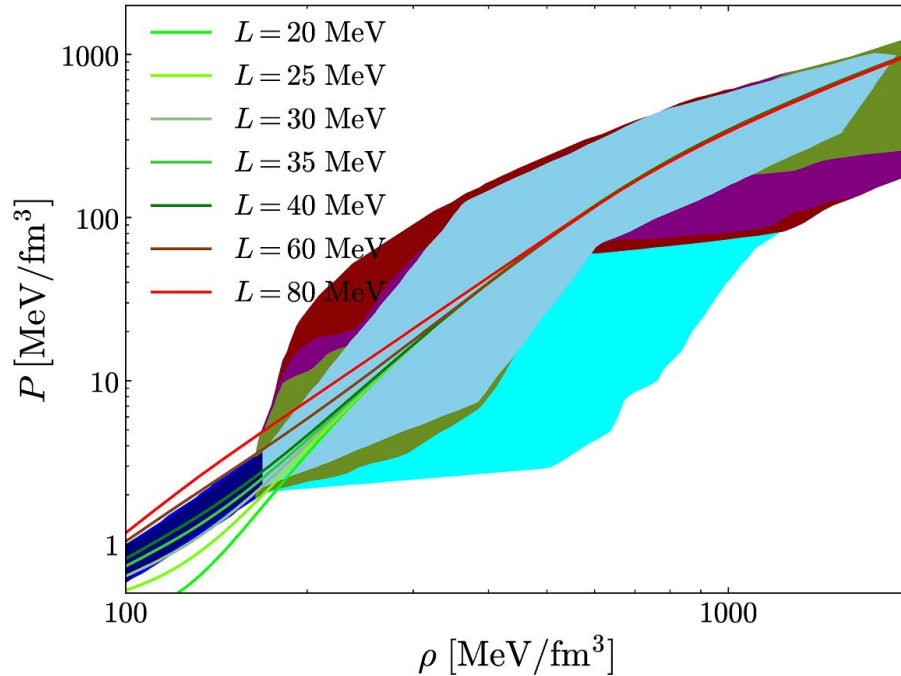


Zhu, Zhou & AL*,
1802.05510, ApJ

$$L(\rho) = dE_{\text{sym}}(\rho)/d\rho$$

Neutron star M-R relation and the equation of state

- EOS confronting with multi-messenger neutron star observations on $M_{\text{Max}}, R_{1.4}, \Lambda$.



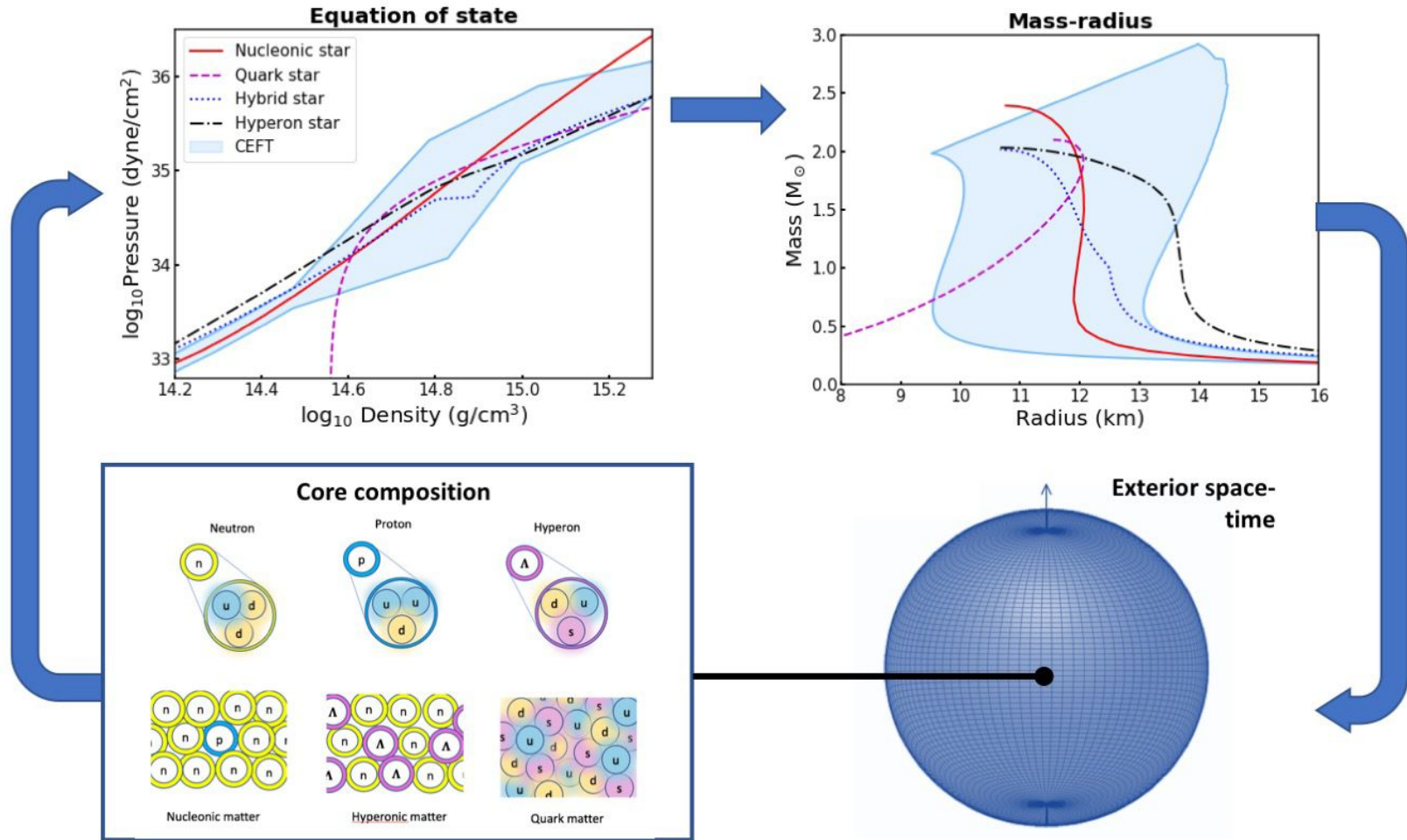
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Radius measurements

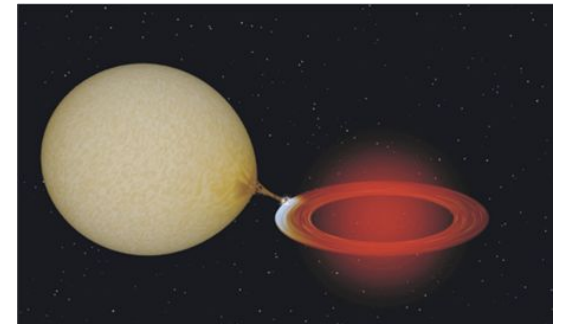
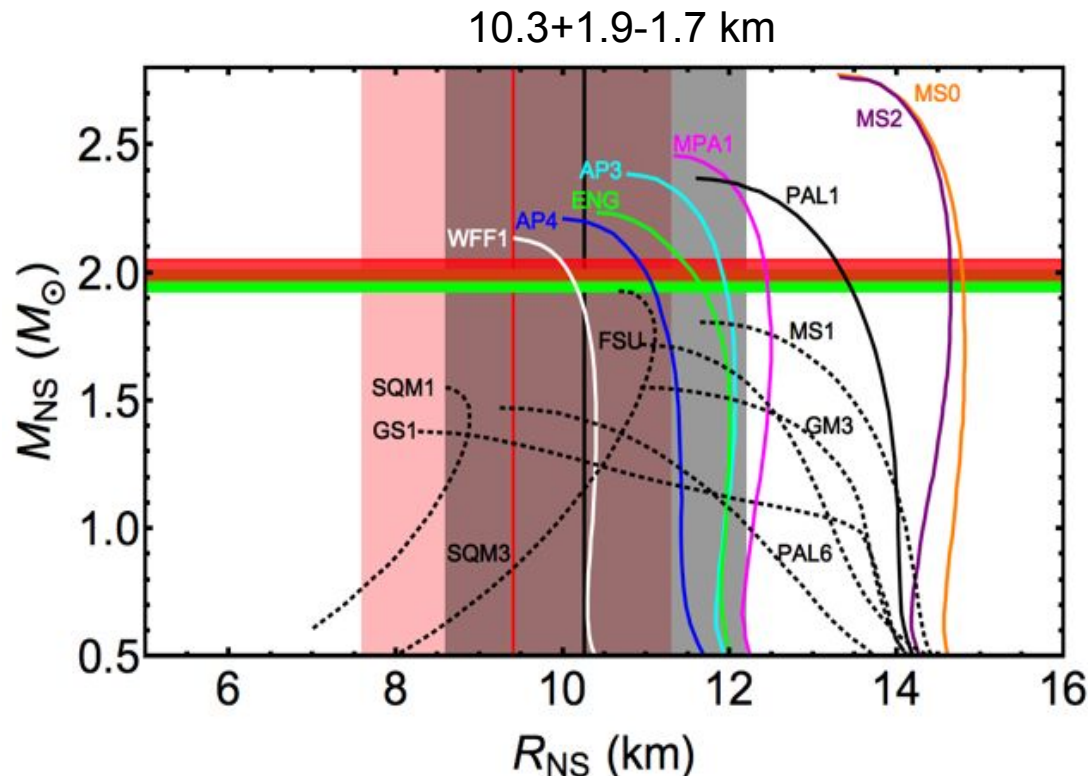
X-ray observations of the neutron star surface permit radius measurements



STROBE-X White paper

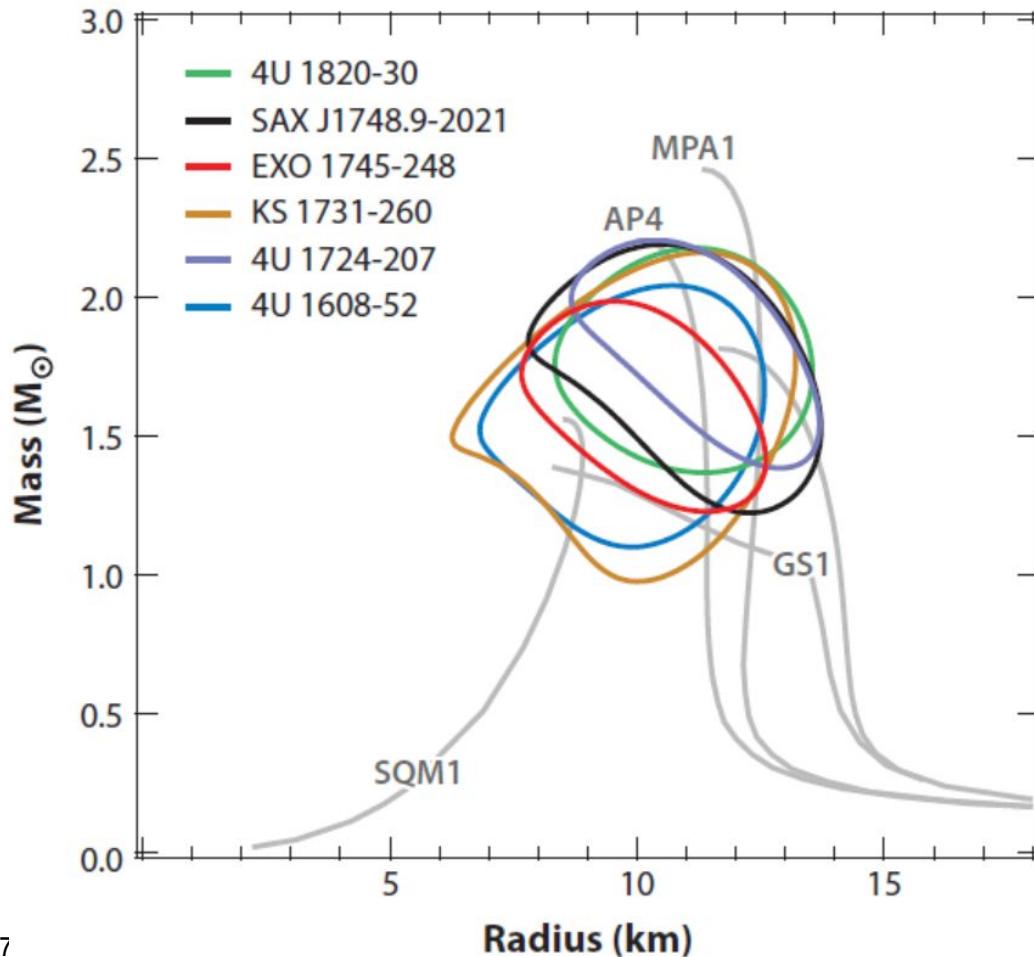
X-ray observations of the neutron star surface permit radius measurements 1/3

- Quiescent low-mass X-ray binaries;
- Many analysis assumptions on e.g., atmosphere, negligible surface magnetic field, isotropic emission, slowly rotating;
- Routinely used but only place weak constraints on EOS;



X-ray observations of the neutron star surface permit radius measurements 2/3

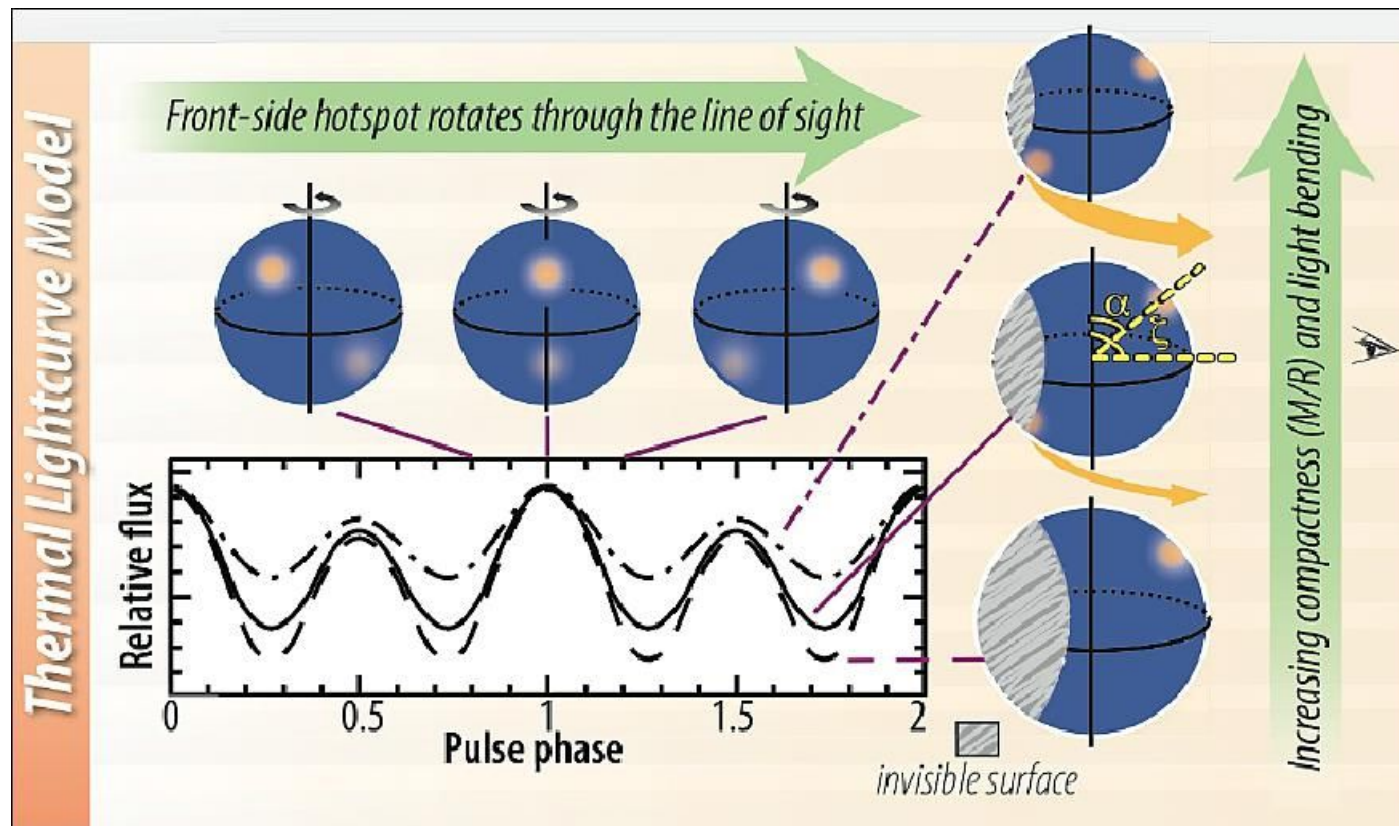
- Type I X-ray bursts;
- Many difficulties (e.g., burst selecting; distance; atmosphere).



Özel & Freire 2016

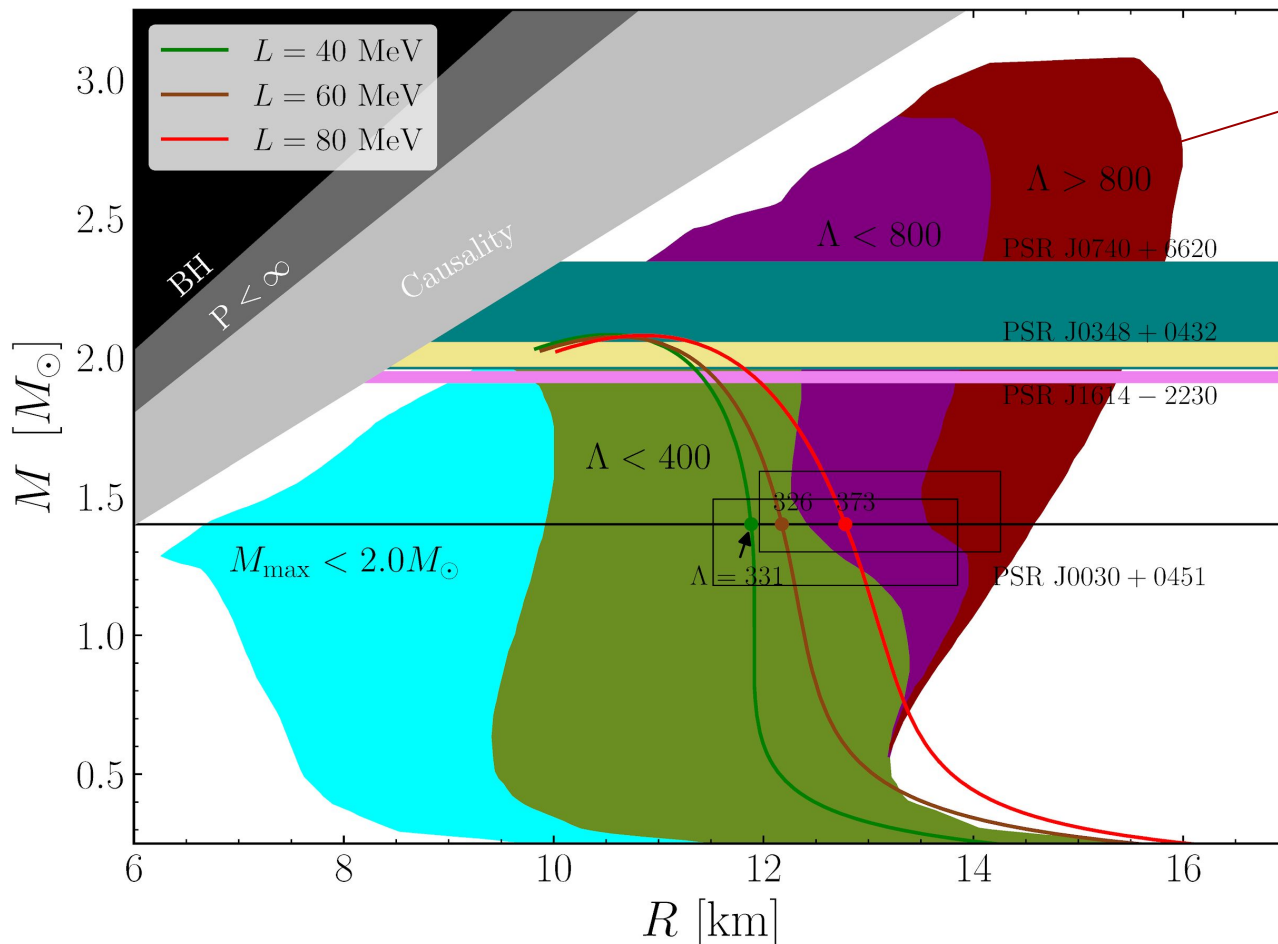
X-ray observations of the neutron star surface permit radius measurements 3/3

- Pulsed emission caused by hot spots on a rotating neutron star can help measure the compactness M/R ;
- NICER, eXTP(~ 2025), ATHENA(~ 2030), STROBE-X(~ 2030);



Joint estimation of the mass and radius of neutron stars by NICER

- For PSR J0030+0451: $M = 1.44^{+0.15}_{-0.14} M_{\odot}$, $R = 13.02^{+1.24}_{-1.06}$ km (Miller et al. 2019)
(68% CFL)
 $M = 1.34^{+0.15}_{-0.16} M_{\odot}$, $R = 12.71^{+1.14}_{-1.19}$ km (Riley et al. 2019)



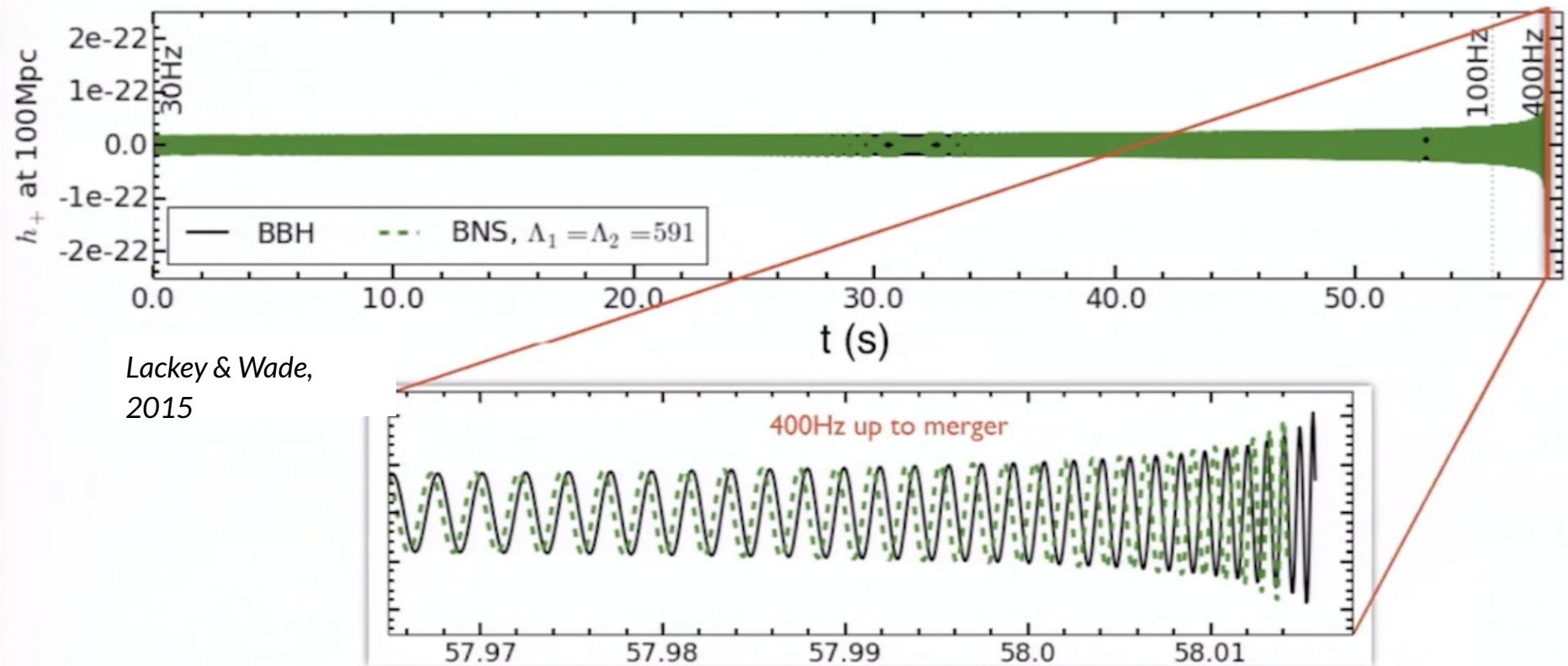
excluded by $\Lambda(1.4) \lesssim 800$ of GW170817

$$\Lambda = \frac{2}{3} k_2 \left(\frac{R}{M} \right)^5$$

Neutron stars
(especially the radii)
strongly constrain L .

Tidal deformability from binary neutron star mergers

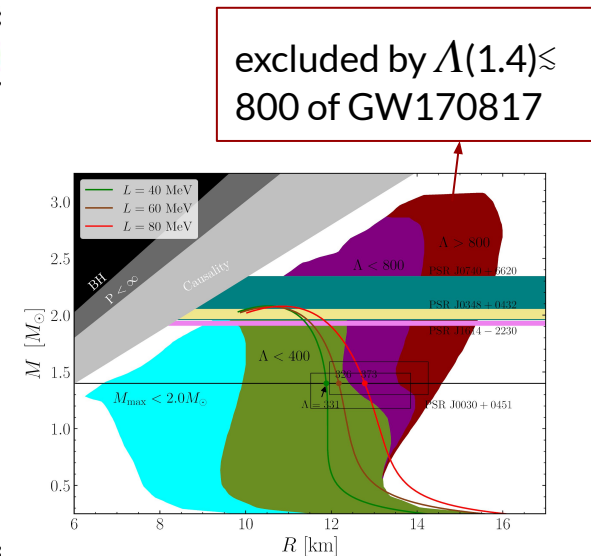
- Finite size effects of the merging star will alter the late inspiral GW signal
- Dimensionless tidal deformability of each star: $\Lambda = \frac{2}{3}k_2\left(\frac{R}{M}\right)^5$



Tidal deformability from GW170817

- Λ_1, Λ_2 depends on M/R and the EOS: $\Lambda = \frac{2}{3}k_2\left(\frac{R}{M}\right)^5$
- Assume that GW170817 is a binary neutron star;
- Both neutron stars obey the same EOS;

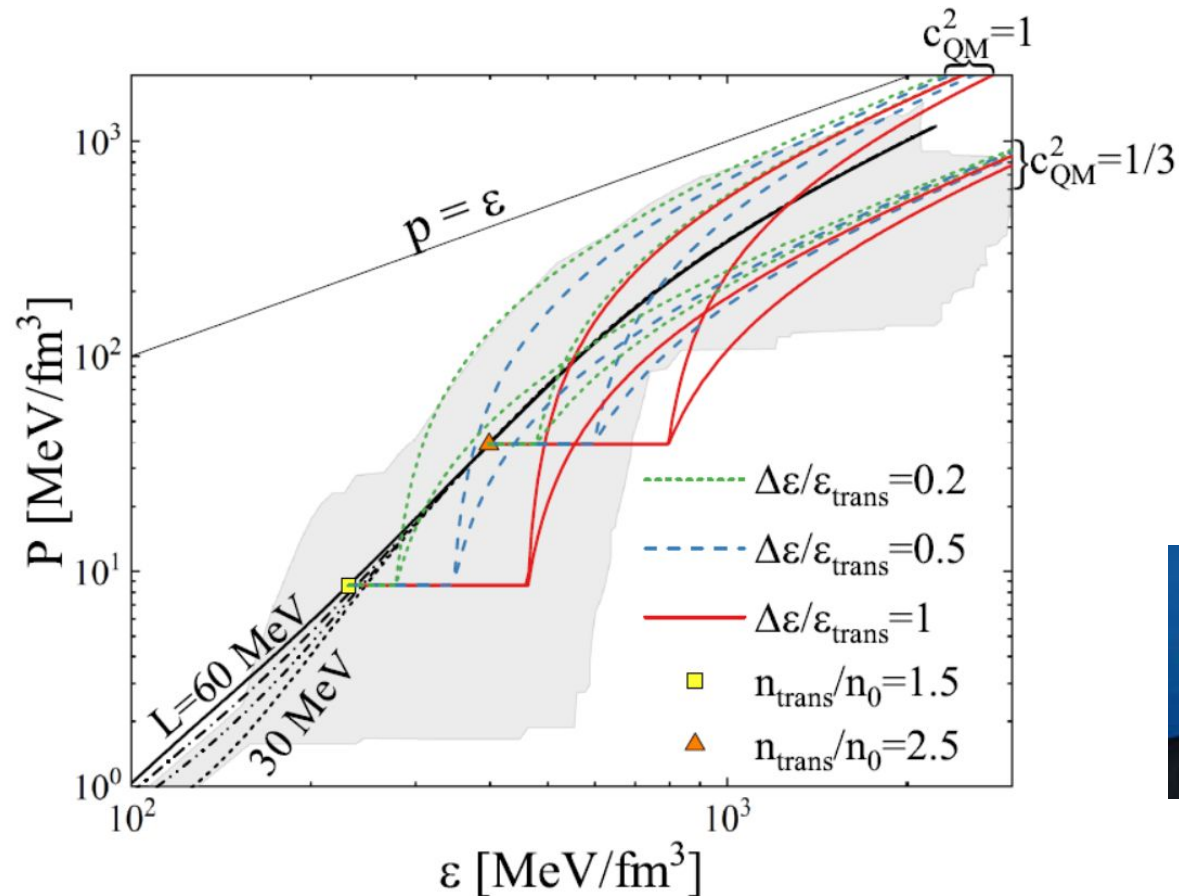
	Low-spin priors ($ \chi \leq 0.05$)
Primary mass m_1	$1.36\text{--}1.60 M_\odot$
Secondary mass m_2	$1.17\text{--}1.36 M_\odot$
Chirp mass $\mathcal{M}$	$1.188^{+0.004}_{-0.002} M_\odot$
Mass ratio m_2/m_1	$0.7\text{--}1.0$
Total mass m_{tot}	$2.74^{+0.04}_{-0.01} M_\odot$
Radiated energy E_{rad}	$> 0.025 M_\odot c^2$
Luminosity distance D_L	$40^{+8}_{-14} \text{ Mpc}$
Viewing angle Θ	$\leq 55^\circ$
Using NGC 4993 location	$\leq 28^\circ$
Combined dimensionless tidal deformability $\tilde{\Lambda}$	≤ 800
Dimensionless tidal deformability $\Lambda(1.4M_\odot)$	≤ 800



More physics necessary at the EOS modelling stage:
With prior considering phase transition!

Including strangeness phase transition

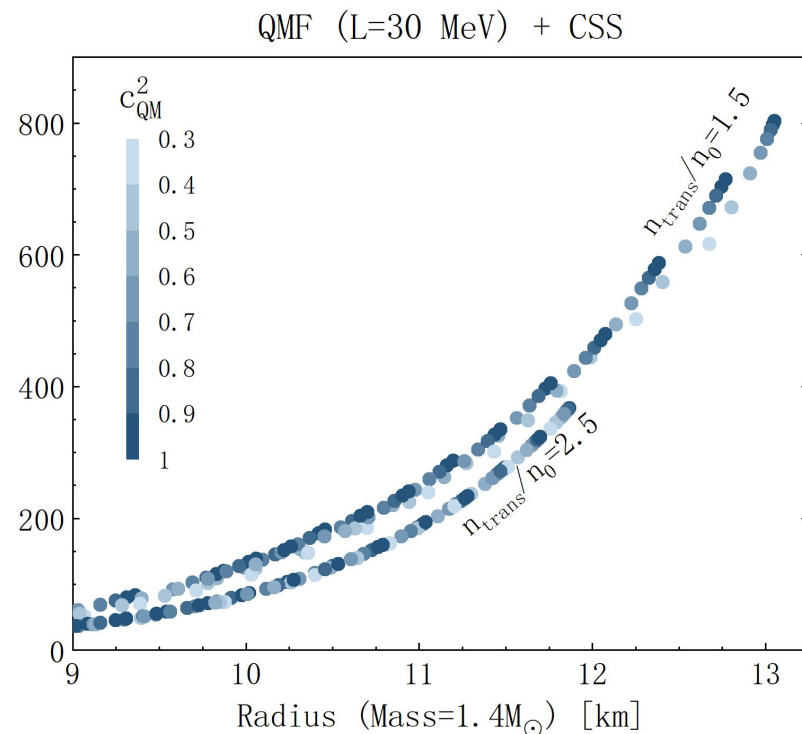
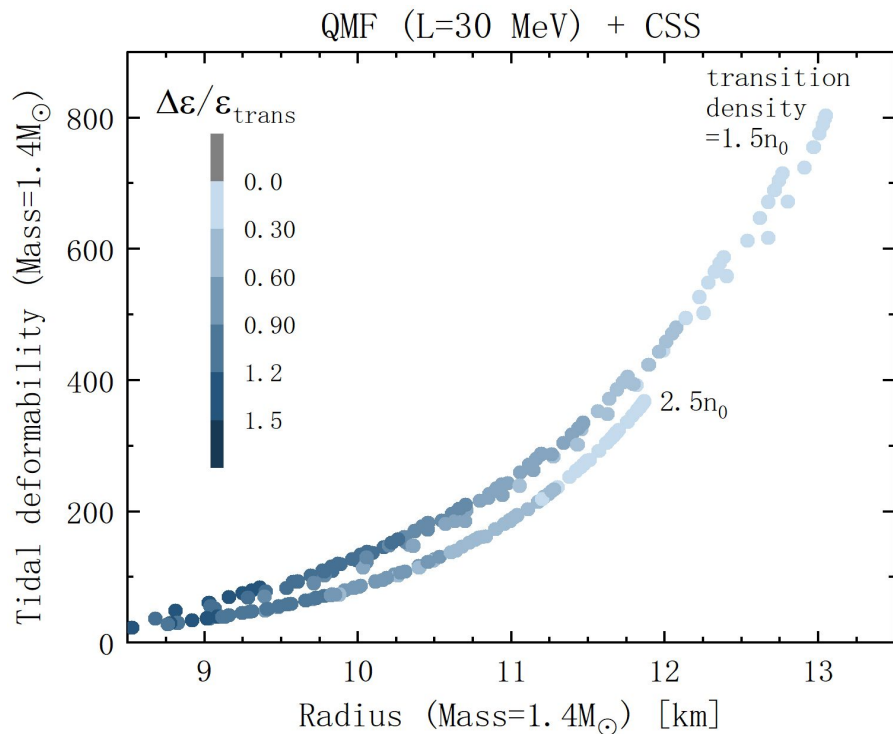
- QMF (quark mean-field) nuclear matter EOS + constant-speed-of-sound (CSS) parametrization for high-density (quark matter) EOS;
- Assuming strong first-order phase transition, most promising scenario to be tested or distinguished from pure hadronic matter by future observations.



*Miao et al. (2020)
to be submitted*

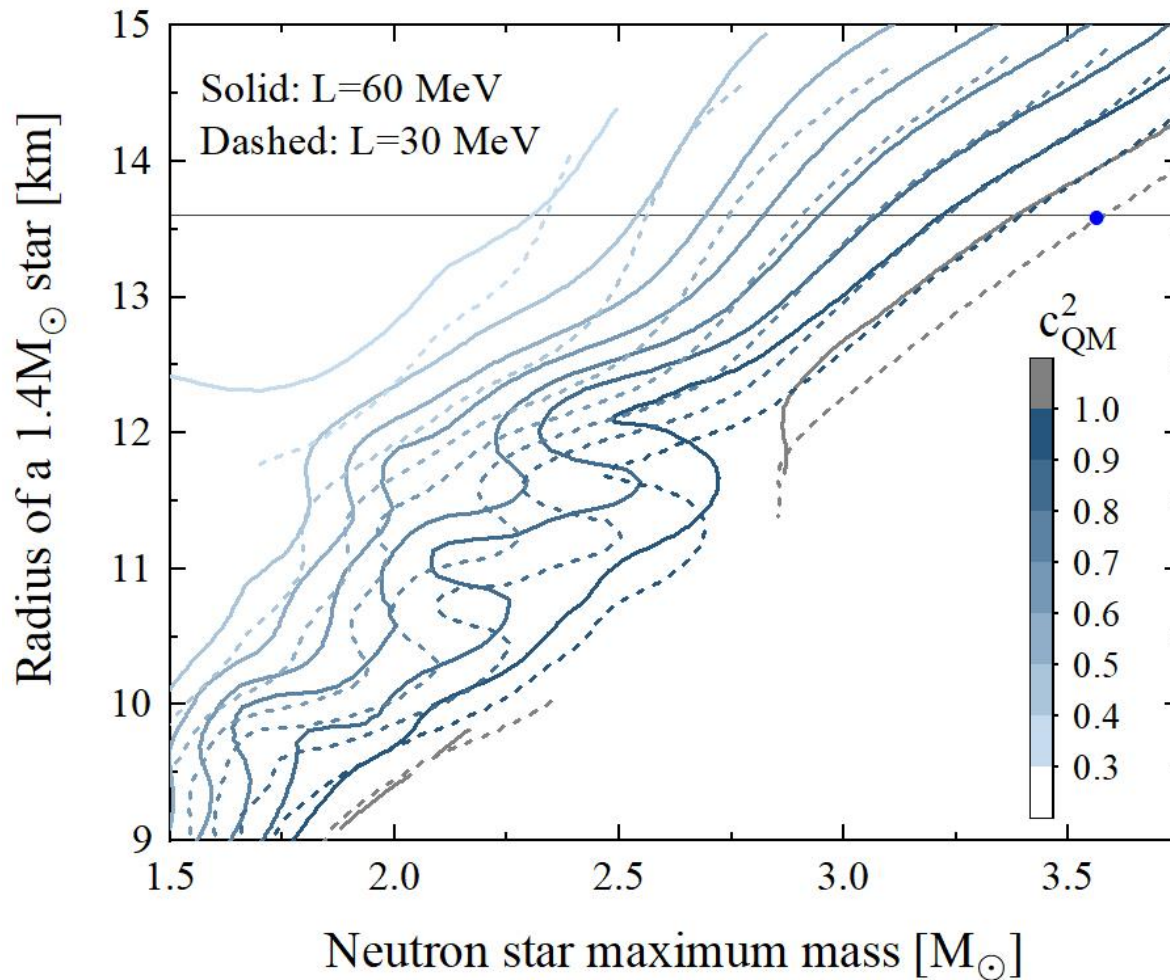
Tidal deformability of hybrid stars

- Unknown threshold density has a non-trivial effect on empirical Λ -R relations for a given nuclear matter model.

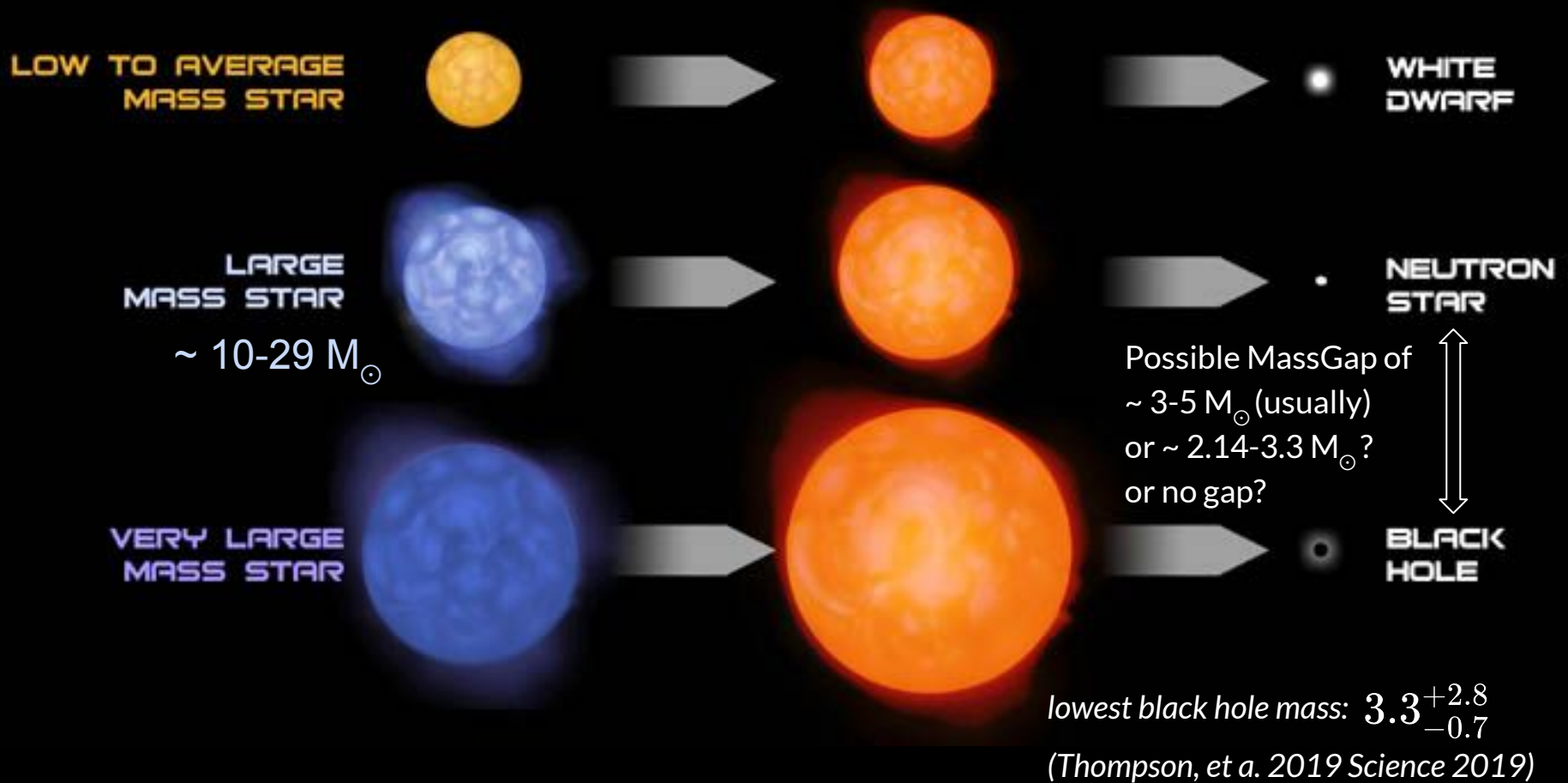


Neutron star maximum mass: Theoretical

- Robust upper limit on the maximum mass $\sim 3.6 M_{\odot}$ based on the causality condition.

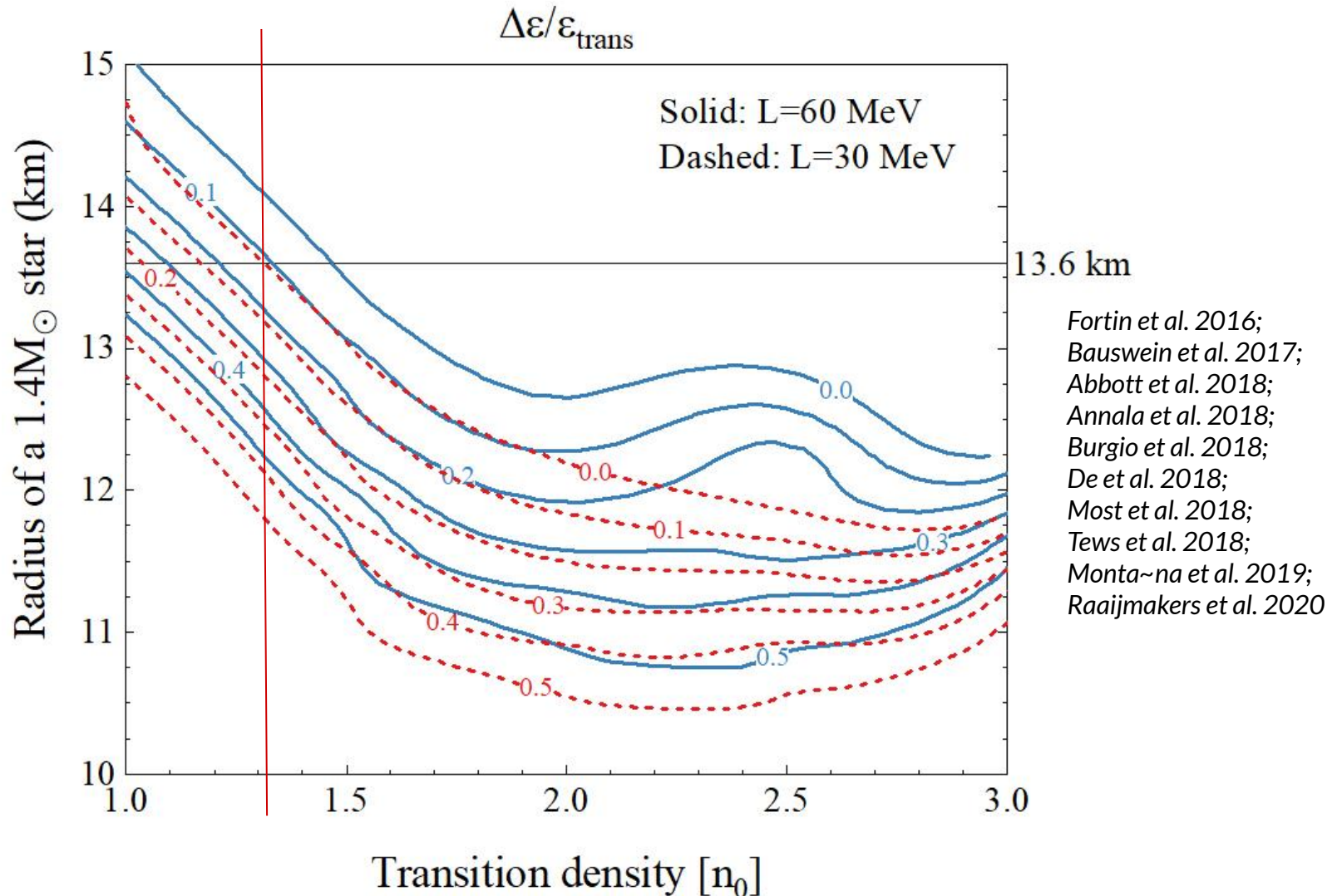


Neutron star maximum mass



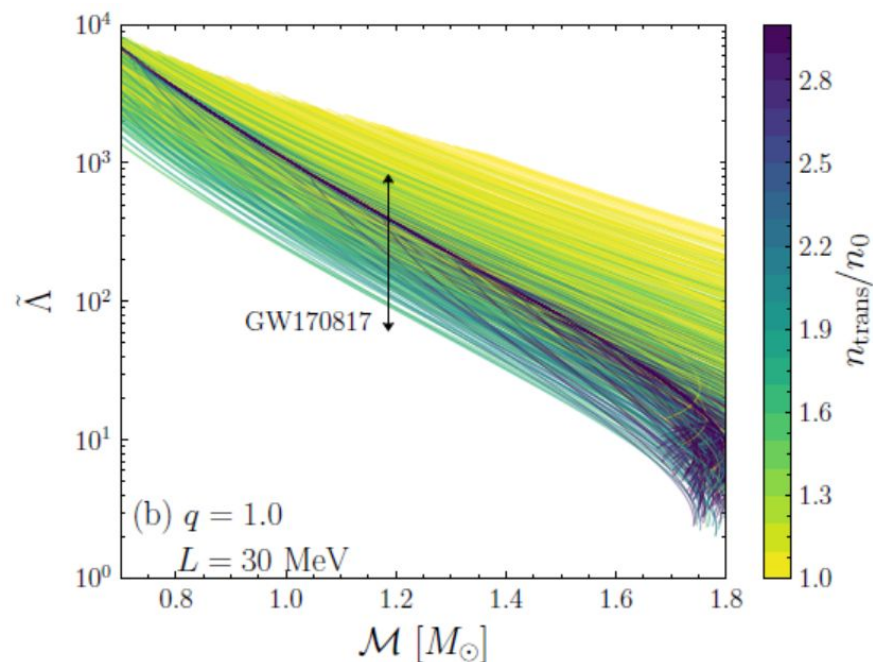
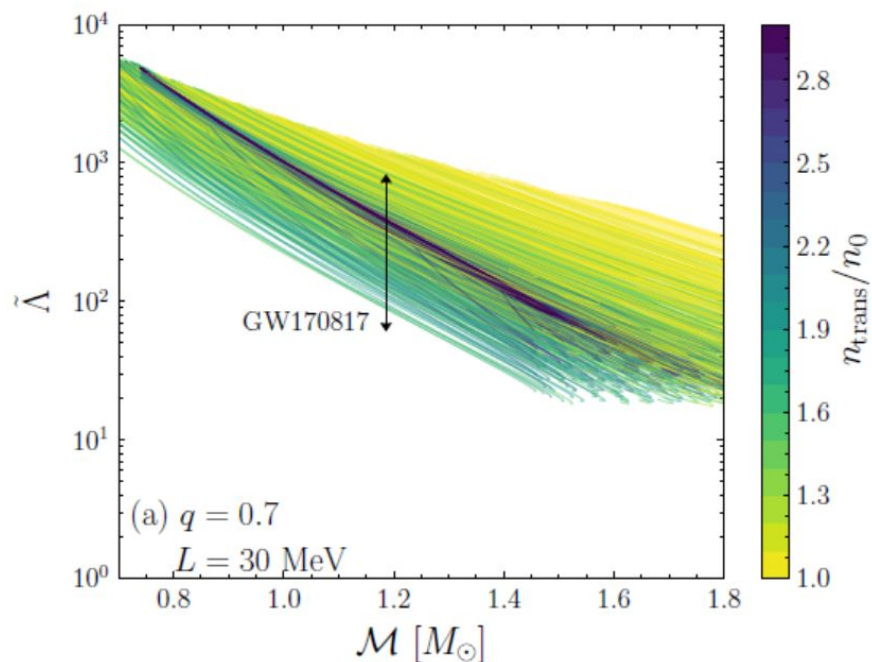
New limits on phase transition onset density

- Onset density $> \sim 1.3n_0$ from a conservative radius limit $R_{1.4} < 13.6$ km.



Current Λ uncertainties for hybrid stars within QMF+CSS

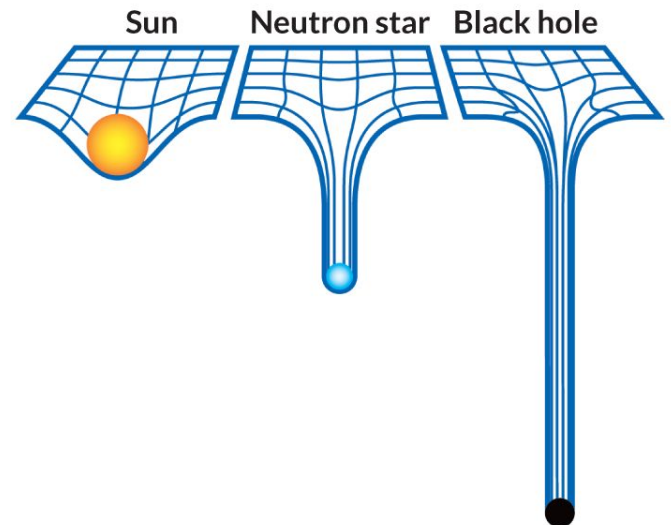
- Very low onset density $< \sim 1.3n_0$ also strongly disfavored by GW170817;
- More neutron star mergers with different chirp masses and mass ratios measured hold promise of reducing the uncertainties significantly.



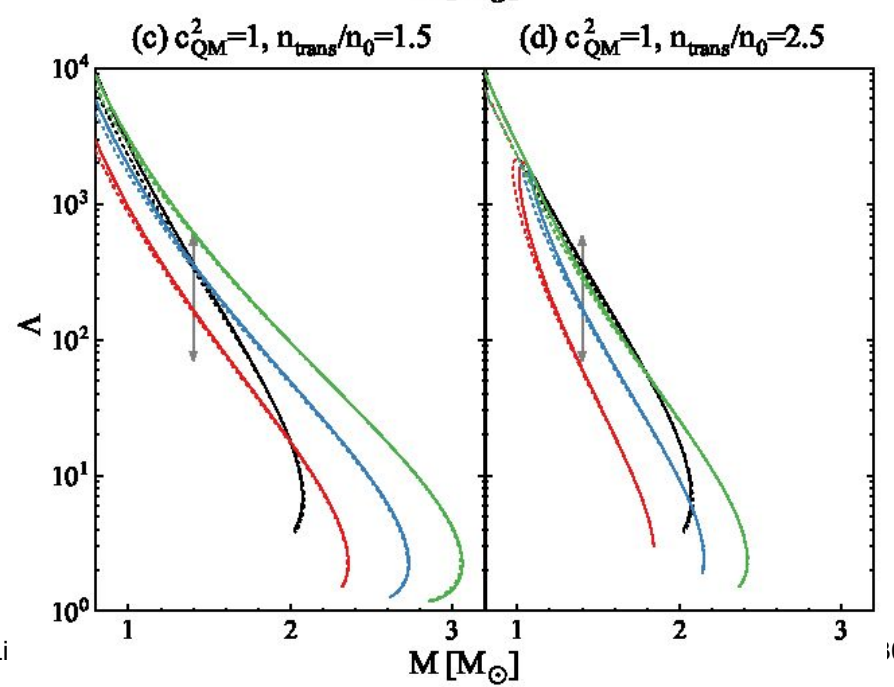
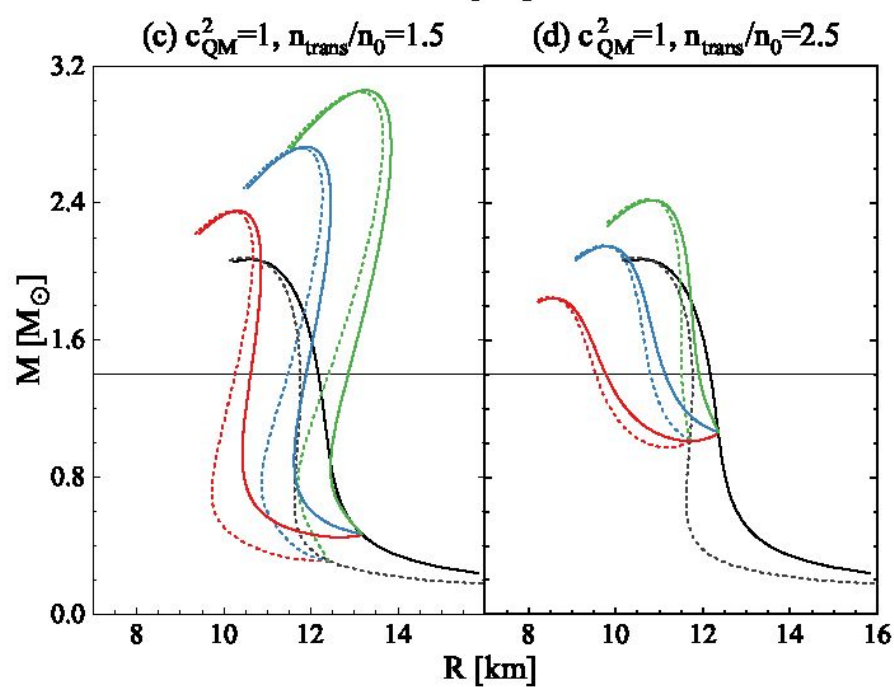
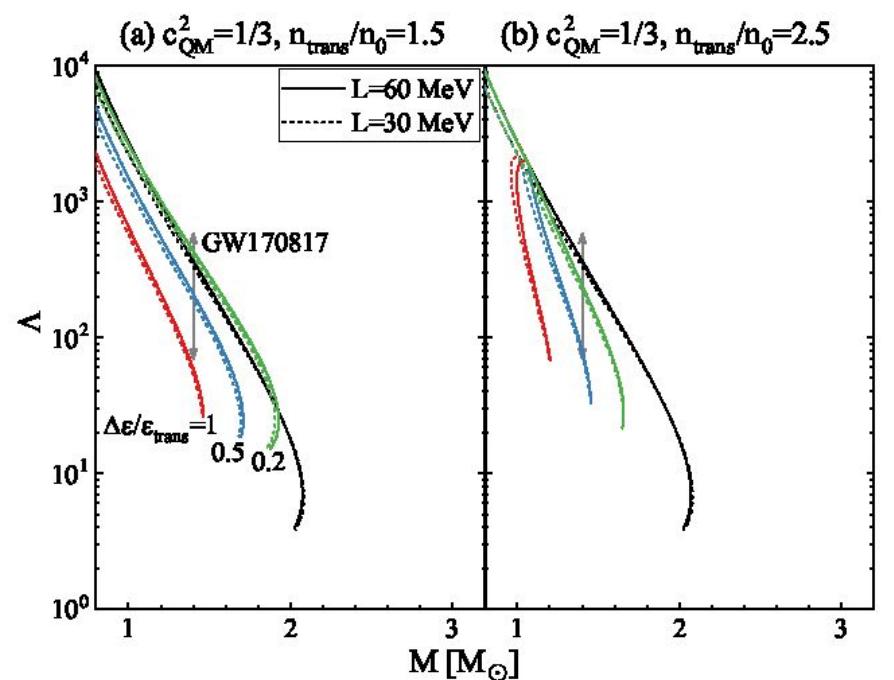
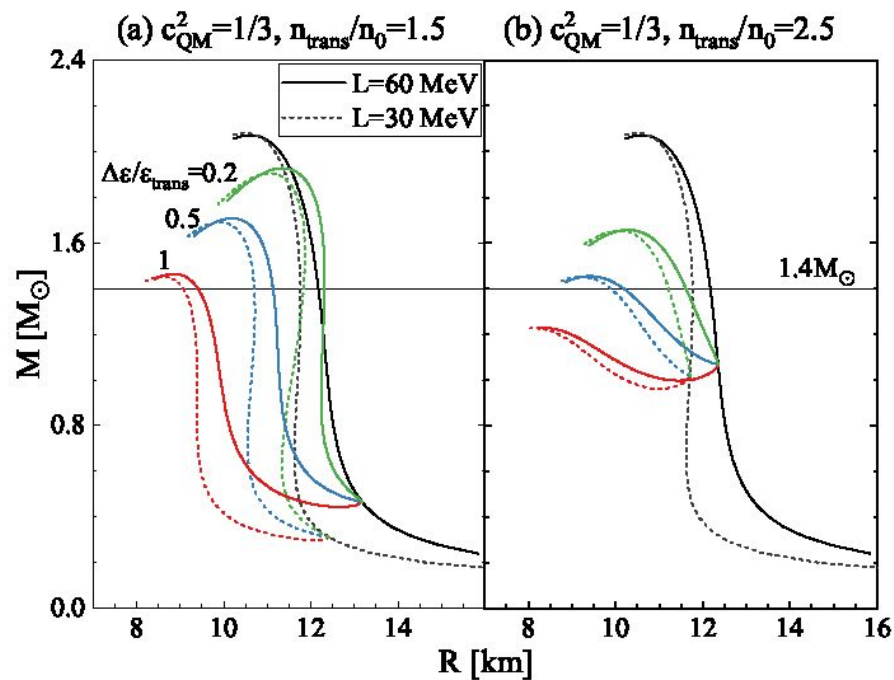
$$\tilde{\Lambda} = \frac{16}{13} \frac{(m_1 + 12m_2)m_1^4}{(m_1 + m_2)^5} \Lambda_1 + (1 \leftrightarrow 2)$$

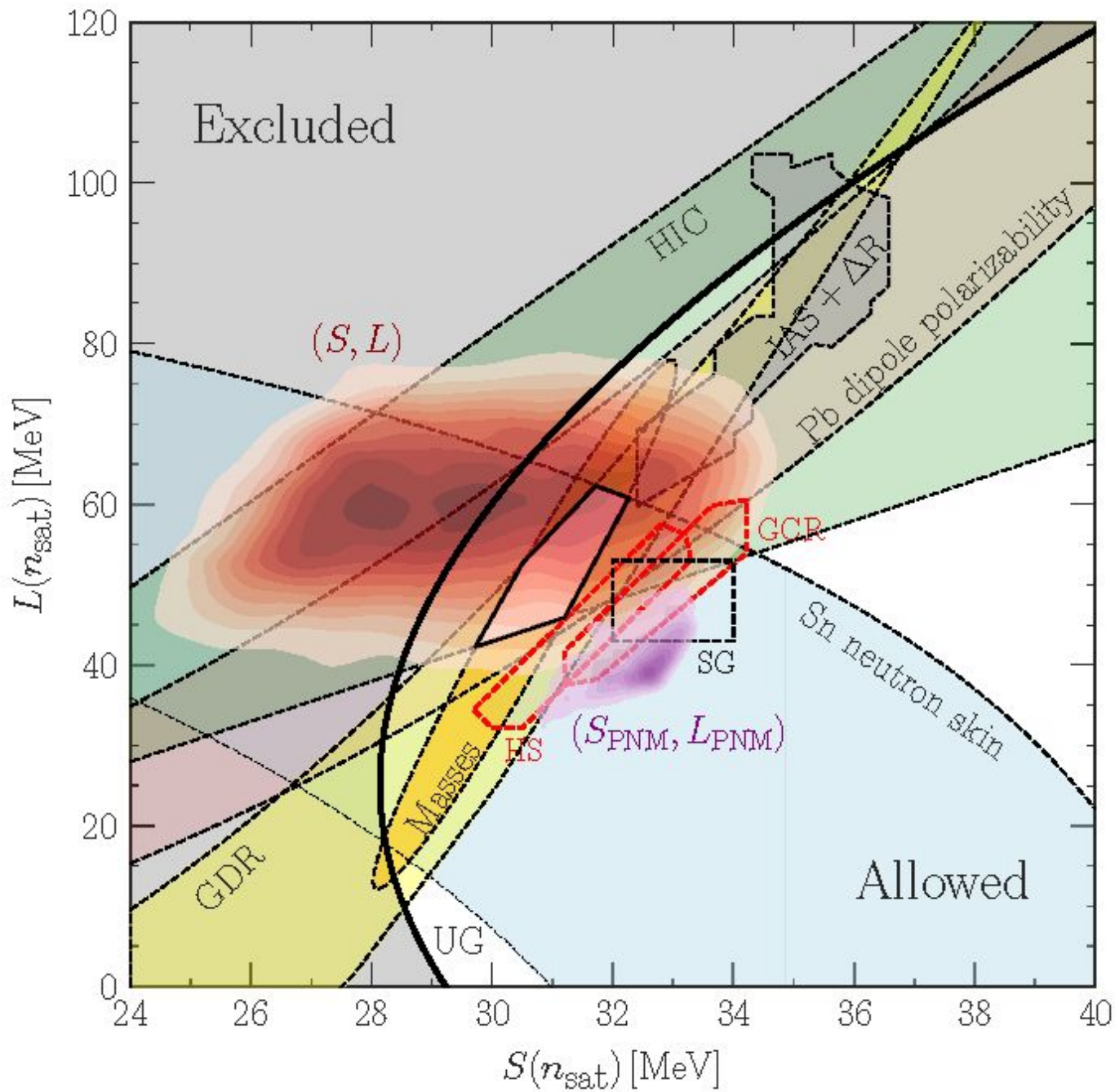
Take-home message

- The “golden” event of GW170817 brings the best time of multi-messenger era;
- The golden age of neutron-star physics has arrived!
(*Nature*|doi:10.1038/d41586-020-00590-8)
- Limits on symmetry energy: $L \sim 30\text{-}60$ MeV;
- New limits on maximum mass: $\sim 2.3\text{-}3.3$ (observational) $\sim 2.4\text{-}3.6$ (theoretical);
- New limits on radii: $\sim 10\text{-}13.6$ km;
- EOS: Not too stiff/soft; stiff-low soft-high?
- The composition: Strangeness present lower than ~ 1.3 times nuclear density.



Backup slides

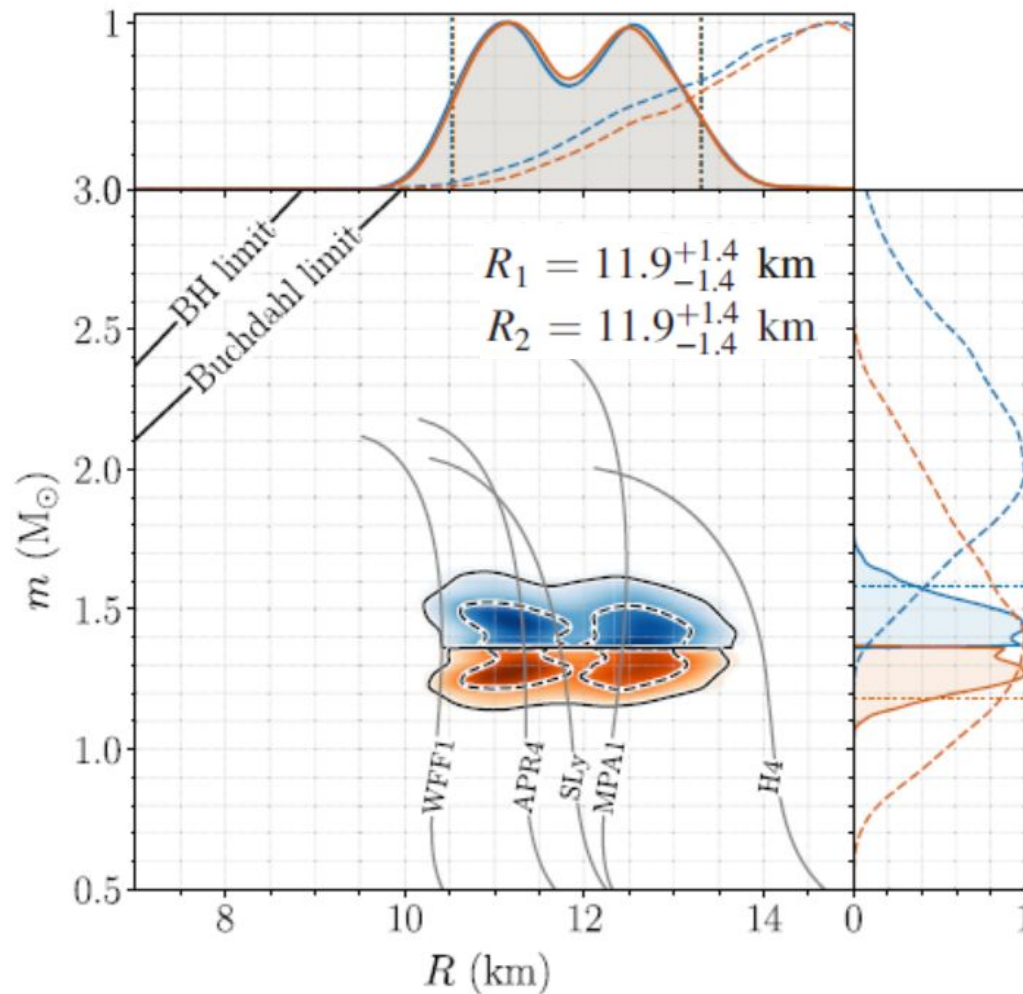




Lonardoni et al.
2020

GW 170817: GW signal

$$\Gamma = (\rho + P)(dP/d\rho)/P$$

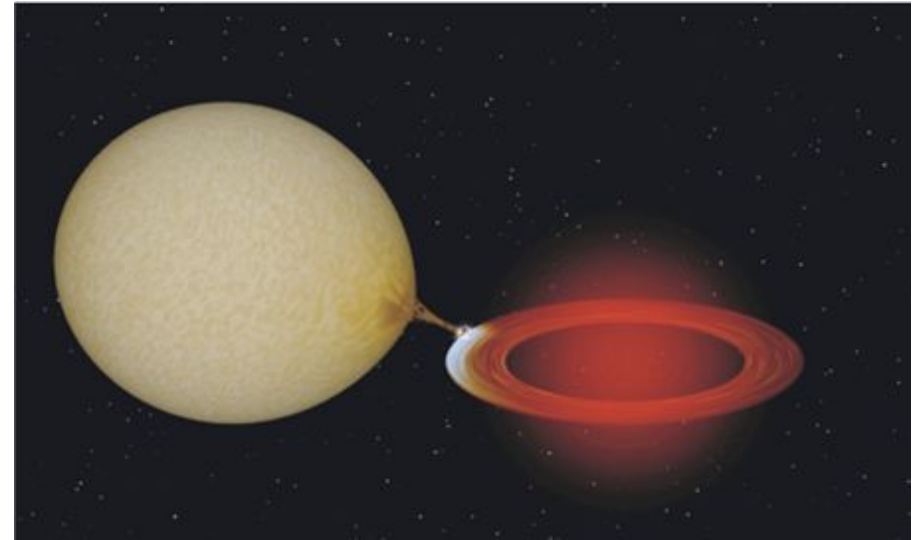
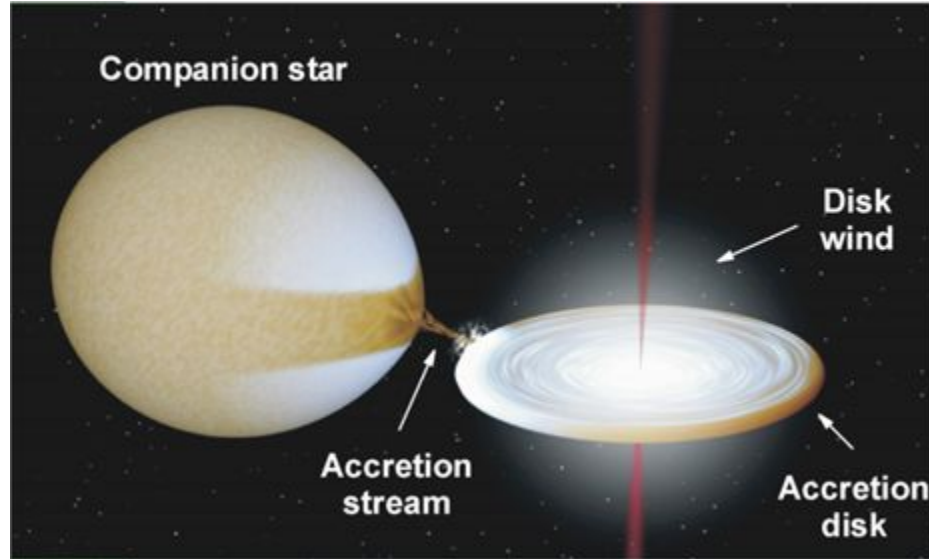


- Piecewise polytrope EOS: Logarithm of the adiabatic index (Γ) of the EOSs are treated as polynomial: **Little to no microphysics;**
- More physics necessary at the EOS modelling stage: With prior considering phase transition, **results less constrained;**
- Tidal deformability with strangeness phase transitions (Zhu, Zhou & **AL***, 1802.05510, ApJ)

LVC group, 2018 PRL

X-ray observations of the neutron star surface permit radius measurements

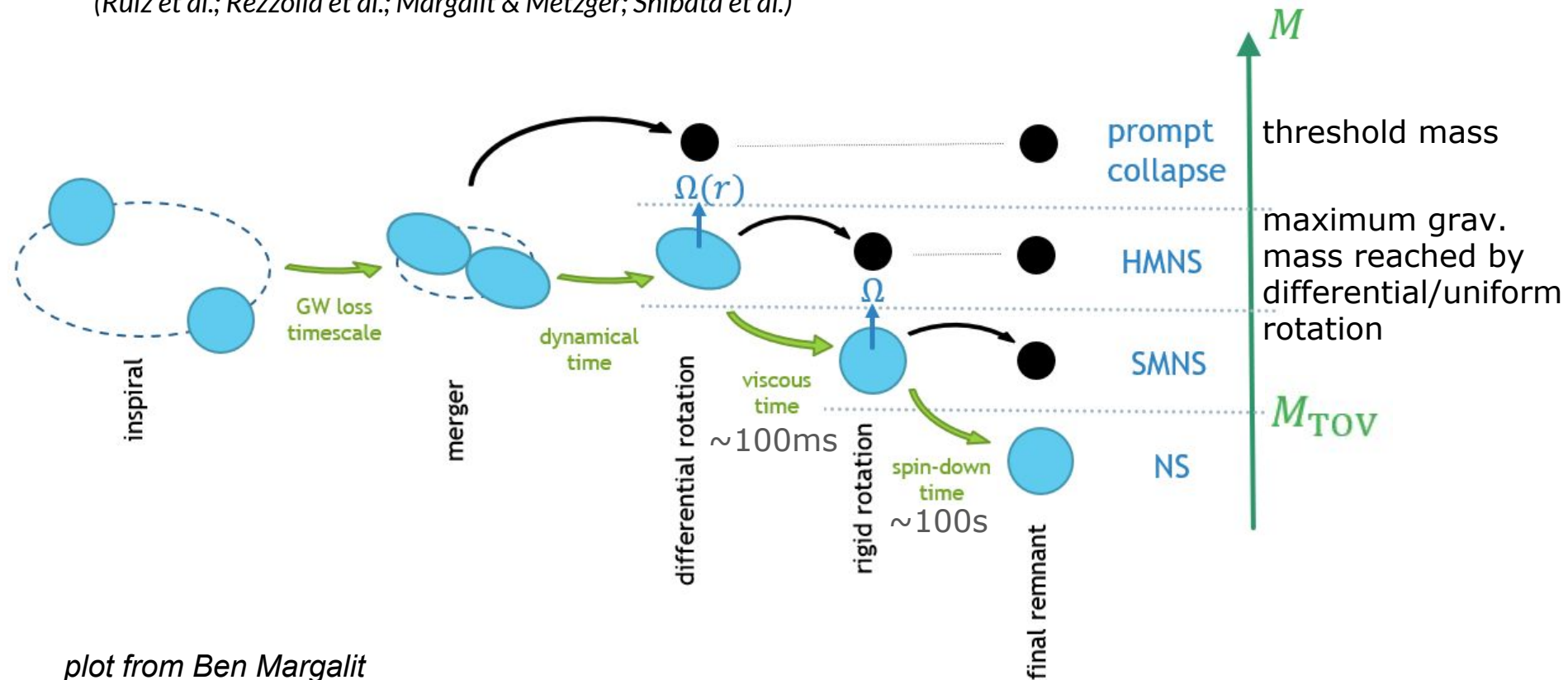
- Quiescent low-mass X-ray binaries;
- Also many analysis assumptions on e.g., atmosphere, negligible surface magnetic field, isotropic emission, slowly rotating;
- Routinely used but only place weak constraints on EOS;



Merger remnants from binary neutron star mergers

- GW & SGRB & kilonova: EOS sensitive: Confronting with numerical simulations;
- A neutron star maximum mass $< \sim 2.3M_{\odot}$ may be indicated from EM observations.

(Ruiz et al.; Rezzolla et al.; Margalit & Metzger; Shibata et al.)



plot from Ben Margalit

Merger remnants from binary neutron star mergers

- Sensitive to the maximum mass (Li et al. 2017);
- Further information coming from kilonova events.

