



# Transverse polarization of $\Lambda$ hyperons in single-inclusive leptonic annihilations

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# The first TH prediction on transverse $\Lambda$ polarization

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## Transverse Quark Polarization in Large- $p_T$ Reactions, $e^+e^-$ Jets, and Leptoproduction: A Test of Quantum Chromodynamics

G. L. Kane

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and

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(Received 5 July 1978)

It is interesting to calculate the deviation from zero for  $m_q \neq 0$ , to order  $\alpha_s$ . The explicit result for  $e^+e^- \rightarrow q\bar{q}$  is, for arbitrary  $m_q$  and large  $Q^2$ ,

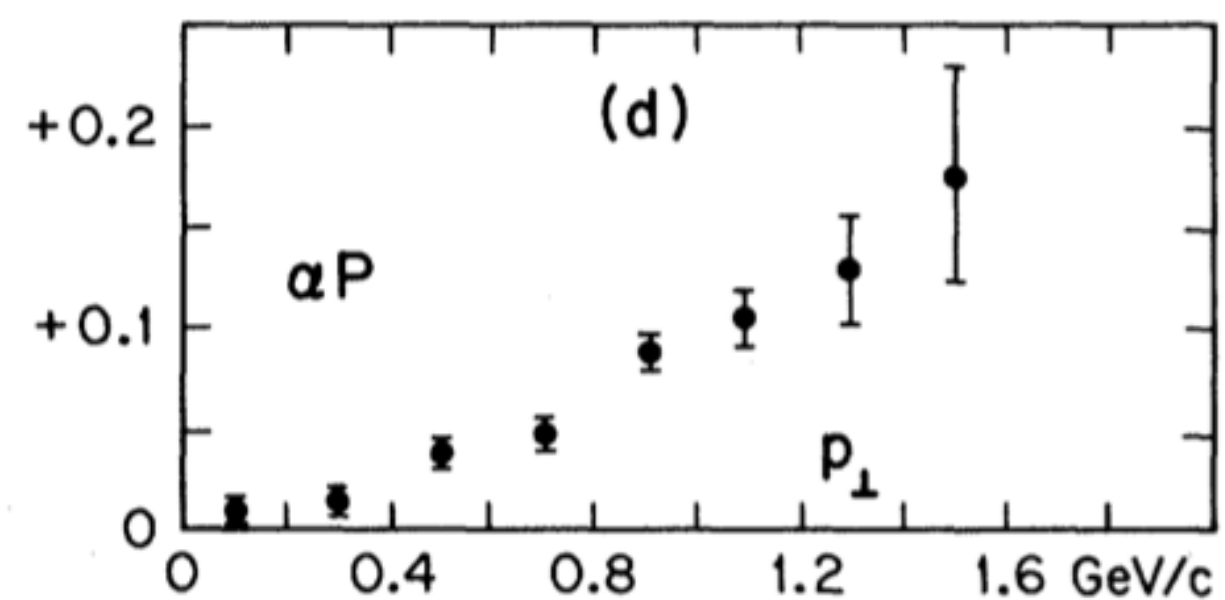
$$P = \left( \frac{4\alpha_s}{3} \right) \frac{m_q}{Q^2} \frac{\sin\theta \cos\theta}{1 + \cos^2\theta}.$$

Whatever observable is used, the variation with  $Q^2$  and the c.m. scattering angle  $\theta$  can be tested.  $P$  is the polarization transverse to the scattering plane, calculated through order  $\alpha_s$  in QCD.

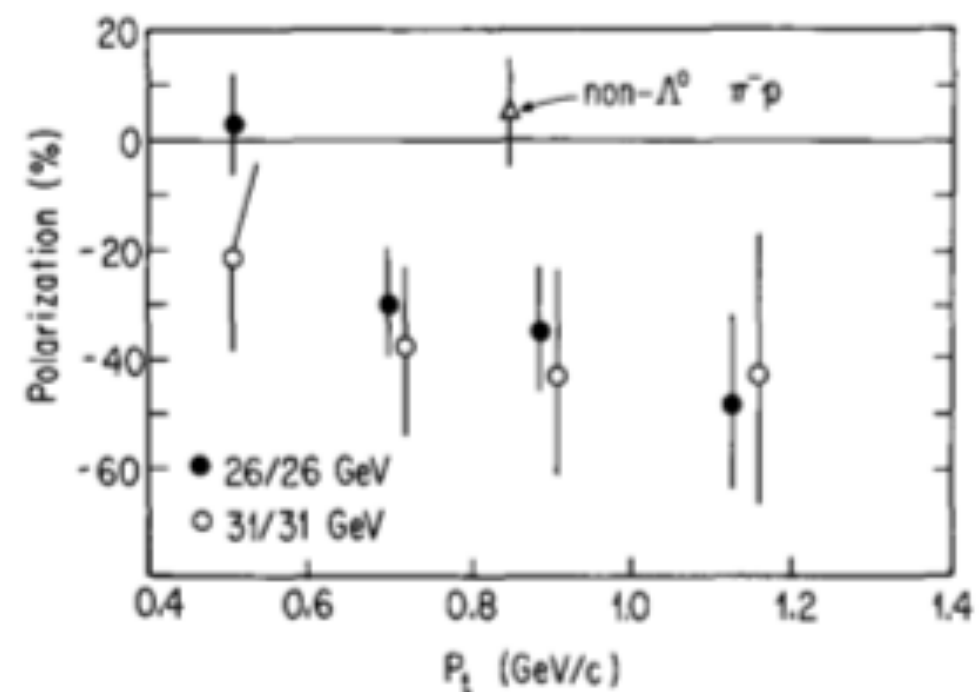
In this note we have pointed out that the asymmetry off a polarized target, and the transverse polarization of a produced quark in  $e^+e^- \rightarrow q\bar{q}$ , or in  $qq \rightarrow qq$  at large  $p_T$ , or in leptoproduction, should all be calculable perturbatively in QCD. The result is zero for  $m_q = 0$  and is numerically small if we calculate  $m_q/\sqrt{s}$  corrections for light quarks. We discuss how to test the predictions. At least for the cases when  $P$  is small, tests should be available soon in large- $p_T$  production [where currently  $P(\Lambda) = 25\%$  for  $p_T \gtrsim 2 \text{ GeV}/c$ ], and  $e^+e^-$  reactions. While fragmentation effects could dilute polarizations, they cannot (by parity considerations) induce polarization. Consequently, observation of significant polarizations in the above reactions would contradict either QCD or its applicability.

# EXP on transverse $\Lambda$ polarization

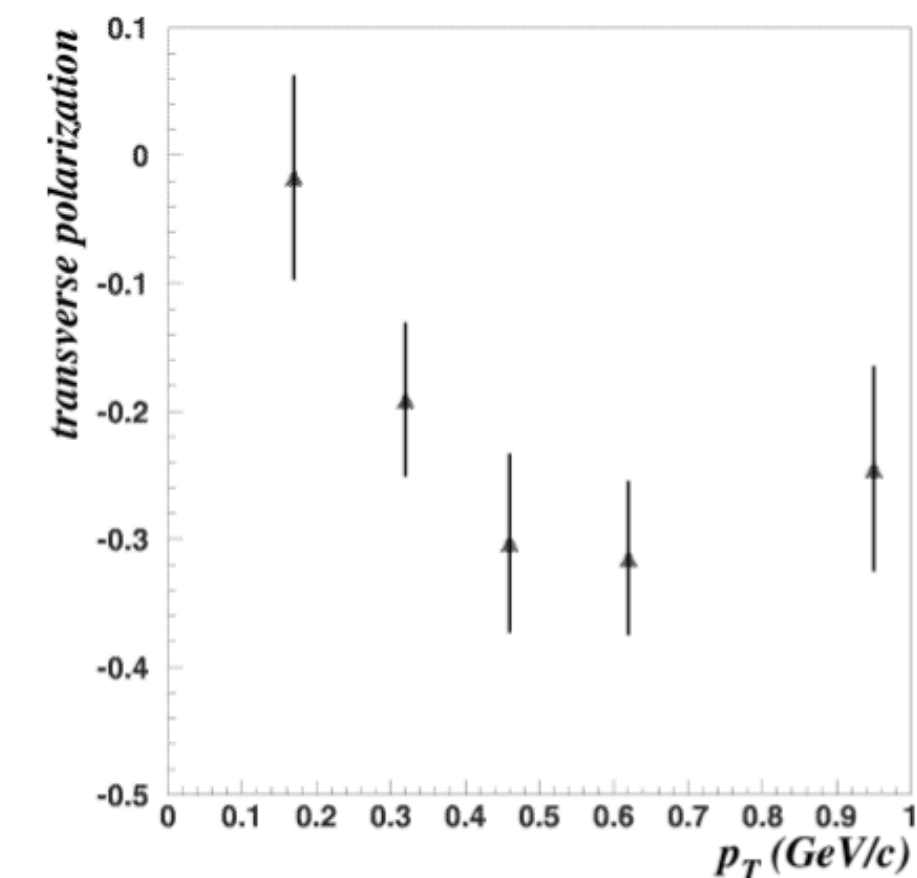
**Bunce et.al. '76**  $p + Be \rightarrow \Lambda^\uparrow + X$



**Erhan et.al. '79**  $pp \rightarrow \Lambda^\uparrow X$

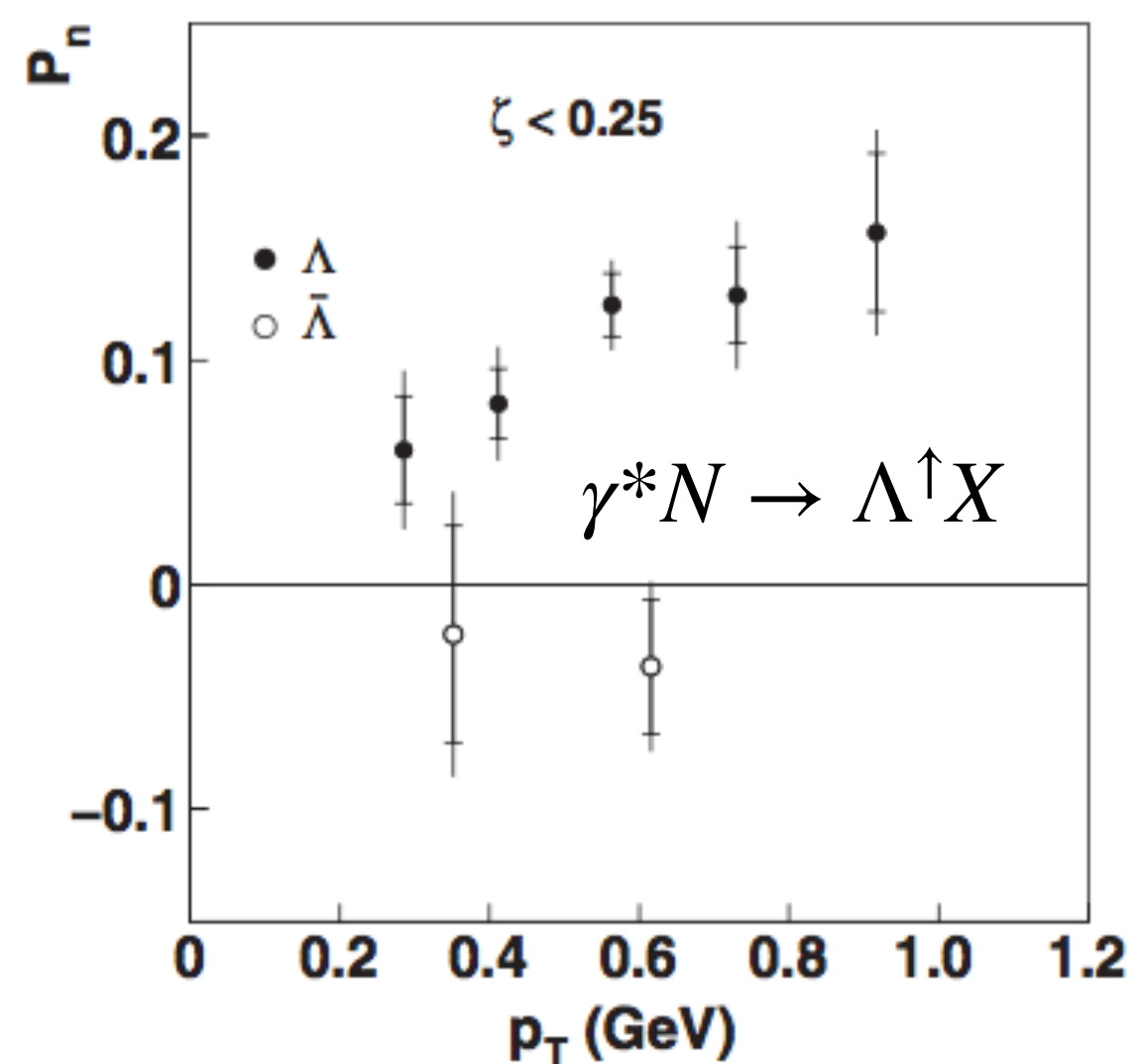


**NOMAD '20**  $\nu N \rightarrow \Lambda^\uparrow X$

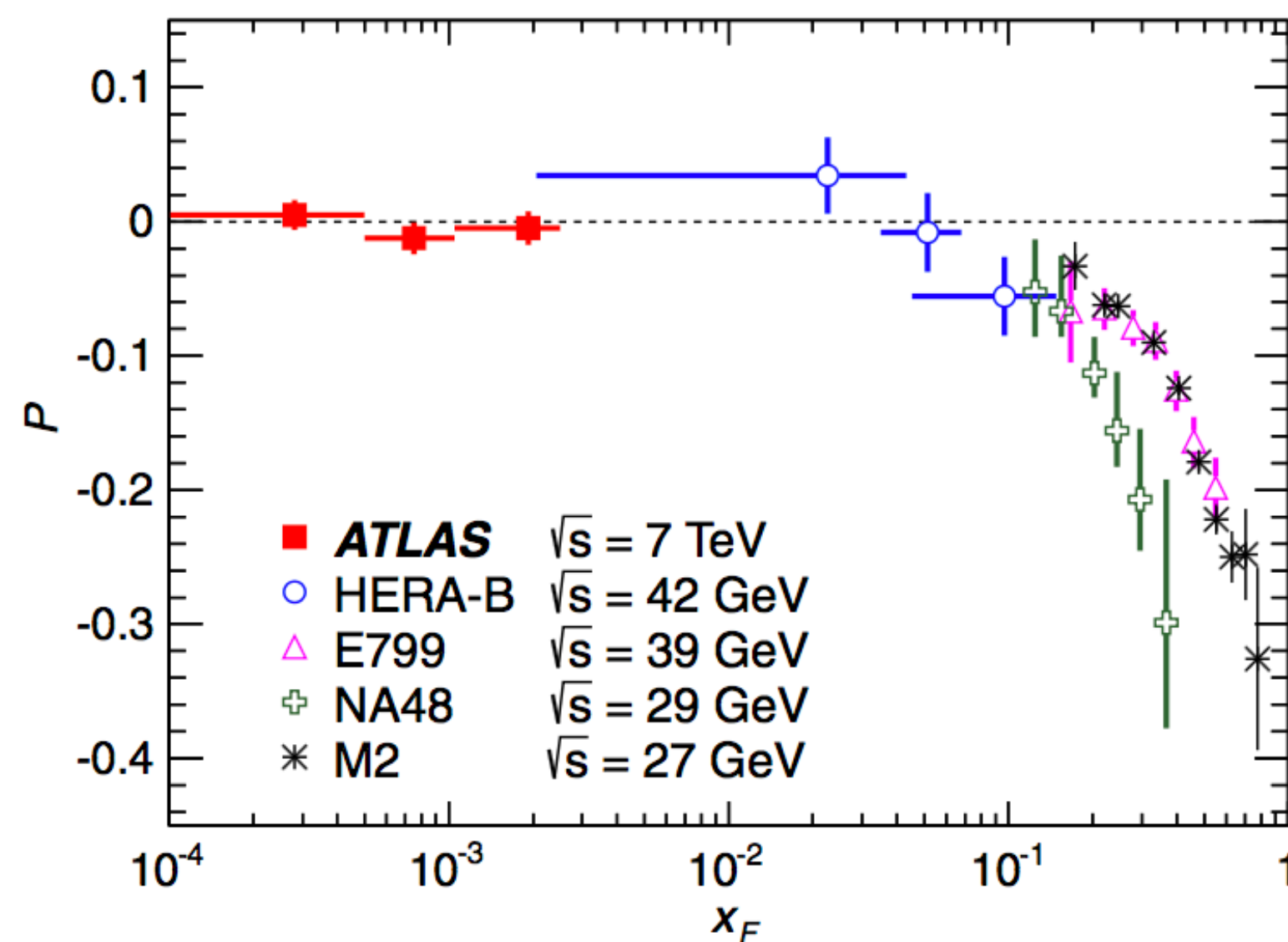


**HERMES '76**

A. AIRAPETIAN *et al.*



**Atlas '15**

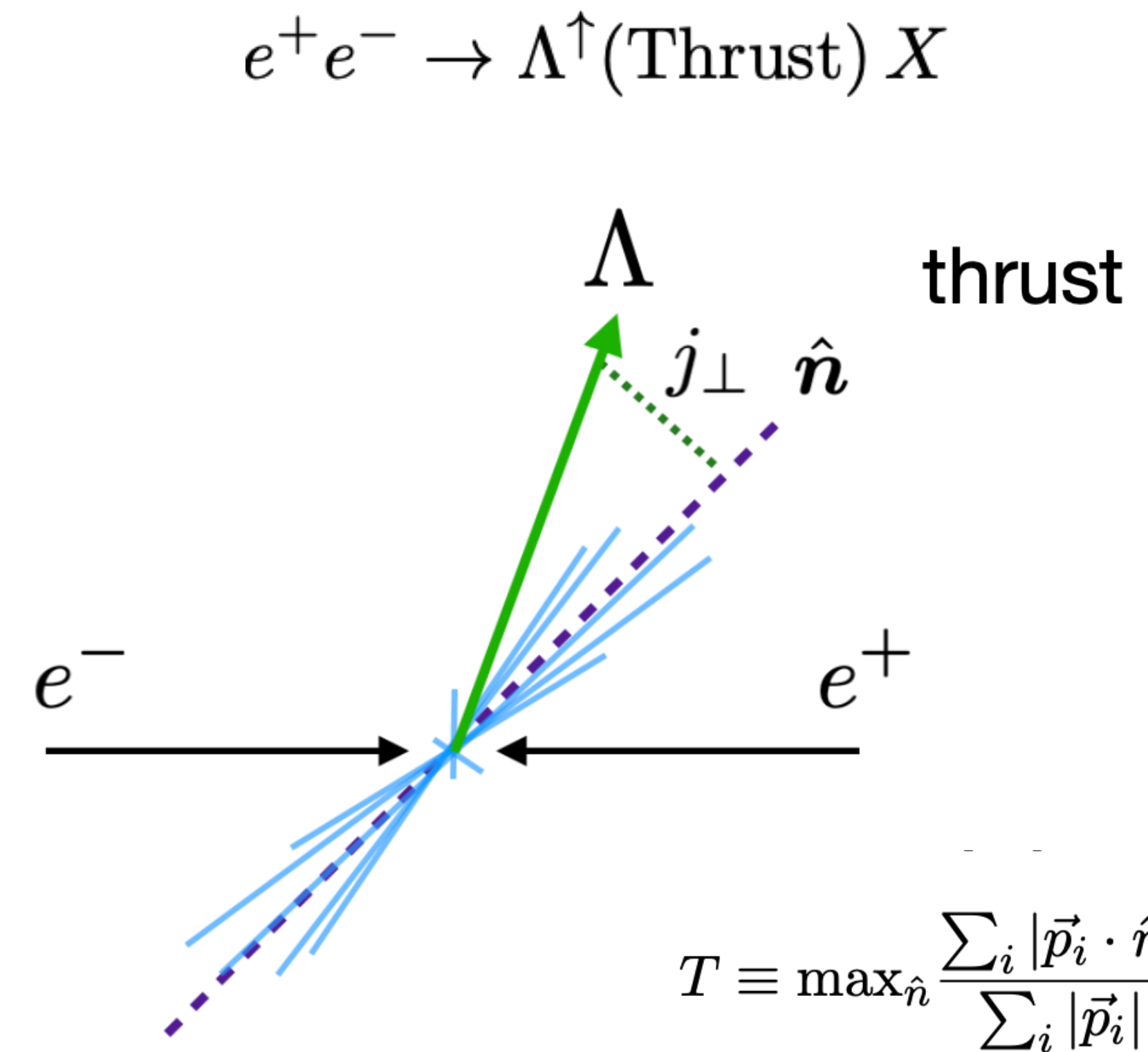
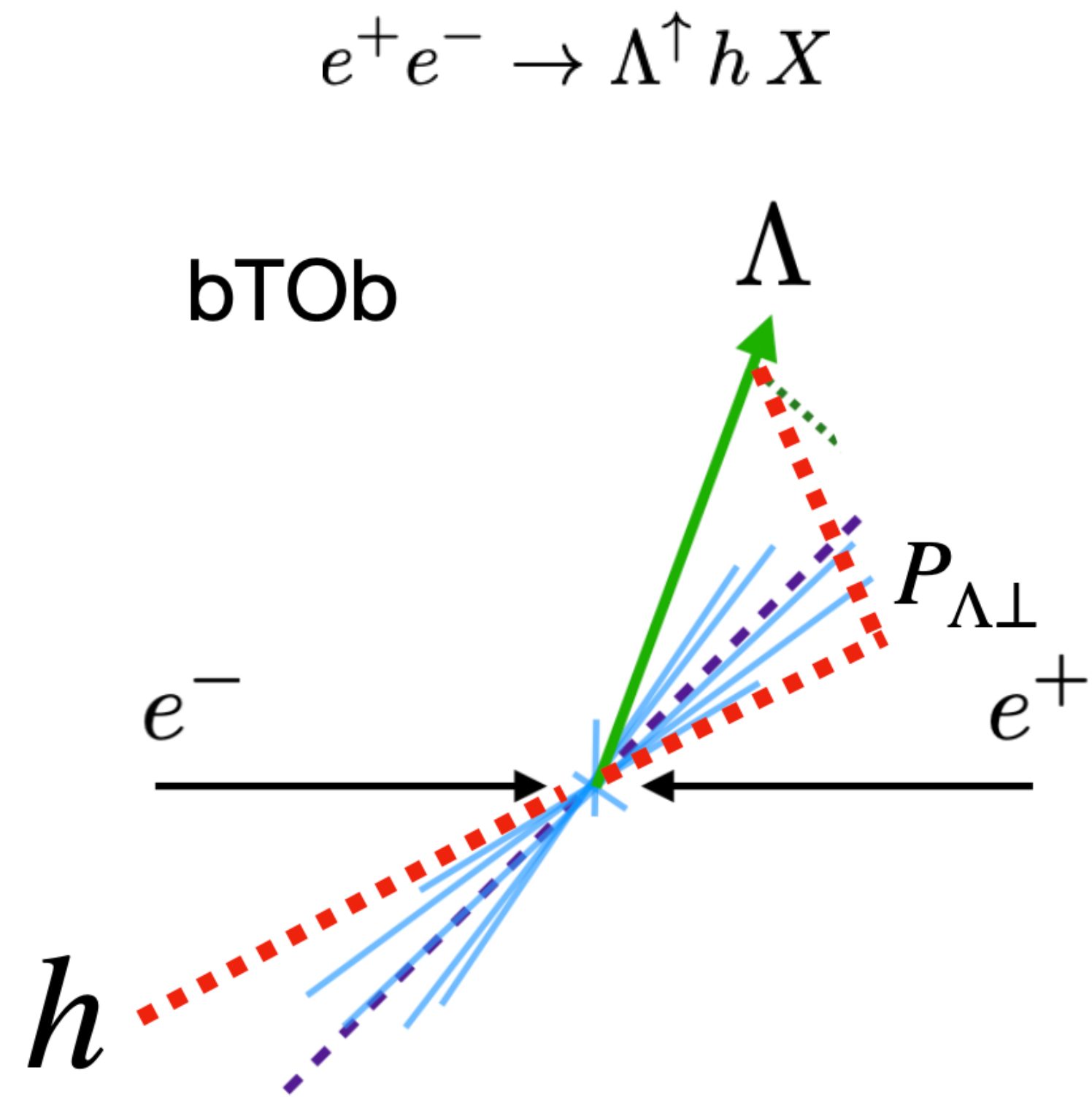


Ma, Schmidt, Soffer, Yang '01  
Liang, Wang '06

...

# Transverse $\Lambda$ polarization in electron positron collisions

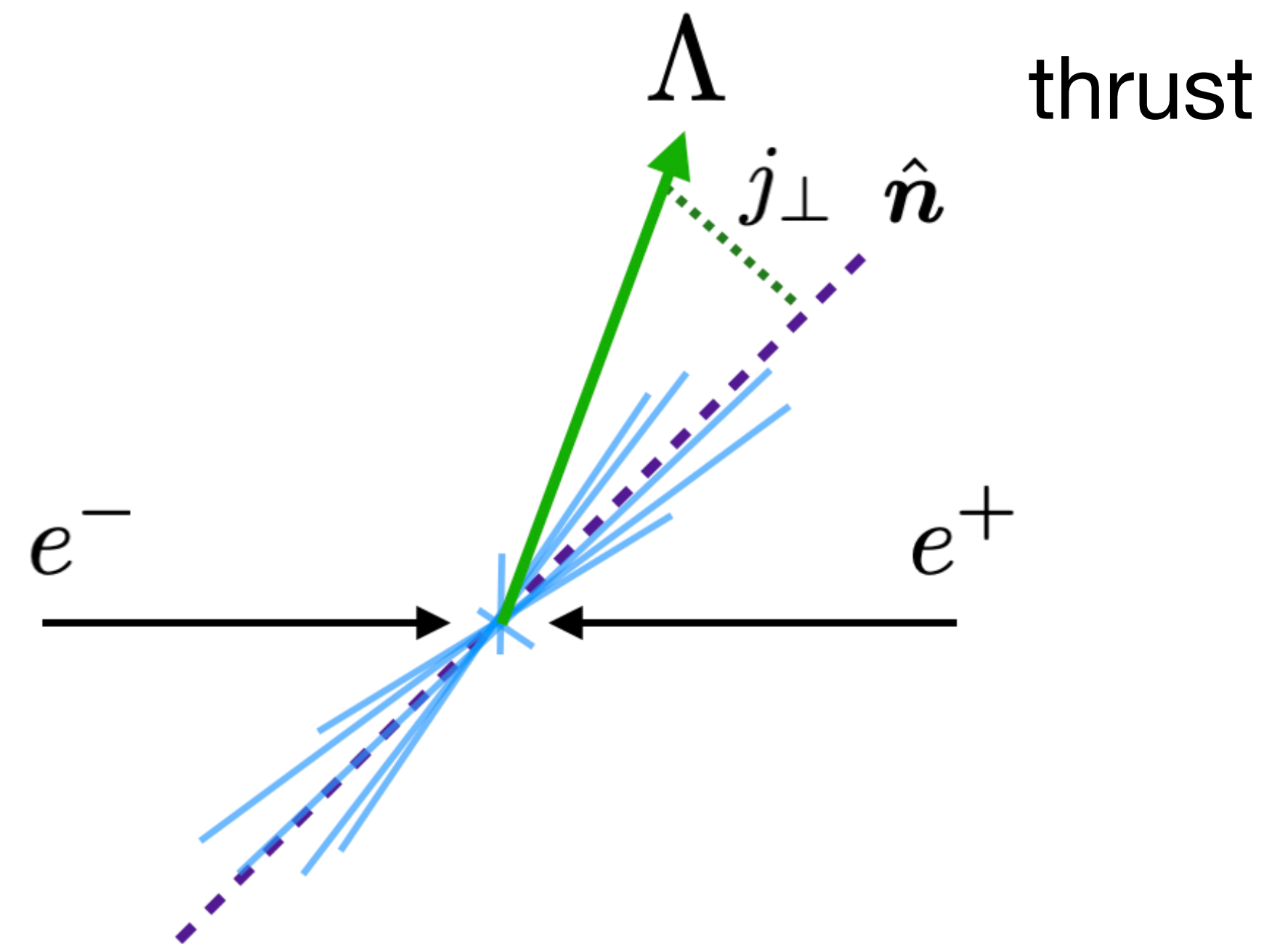
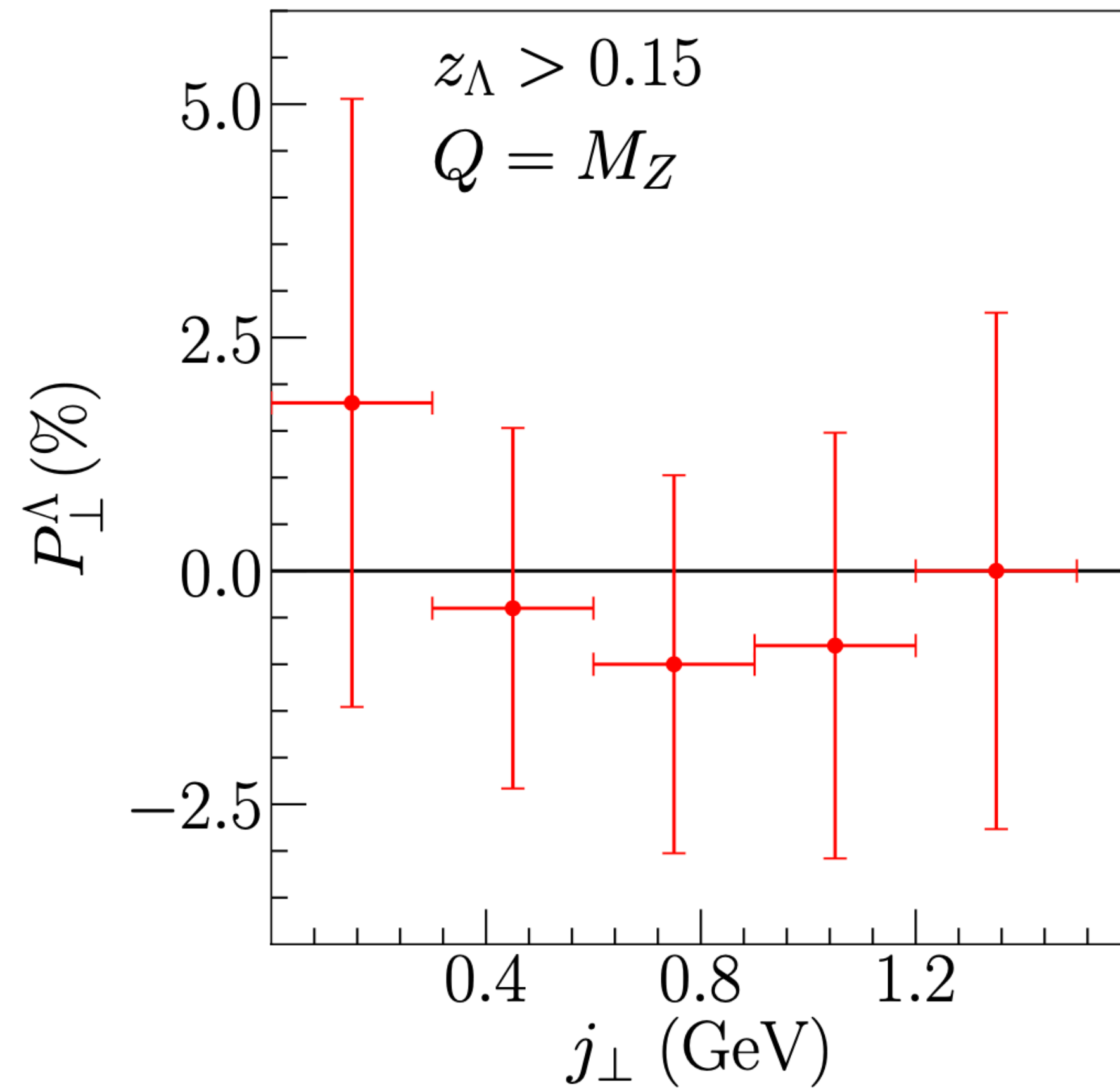
In N+N or l+N collisions, it is not possible to disentangle initial-state effects, related to dynamics inside the colliding hadrons, and final-state effects, related to the fragmentation of the partons.



**$e^+e^-$  cleanest way to access fragmentation functions**

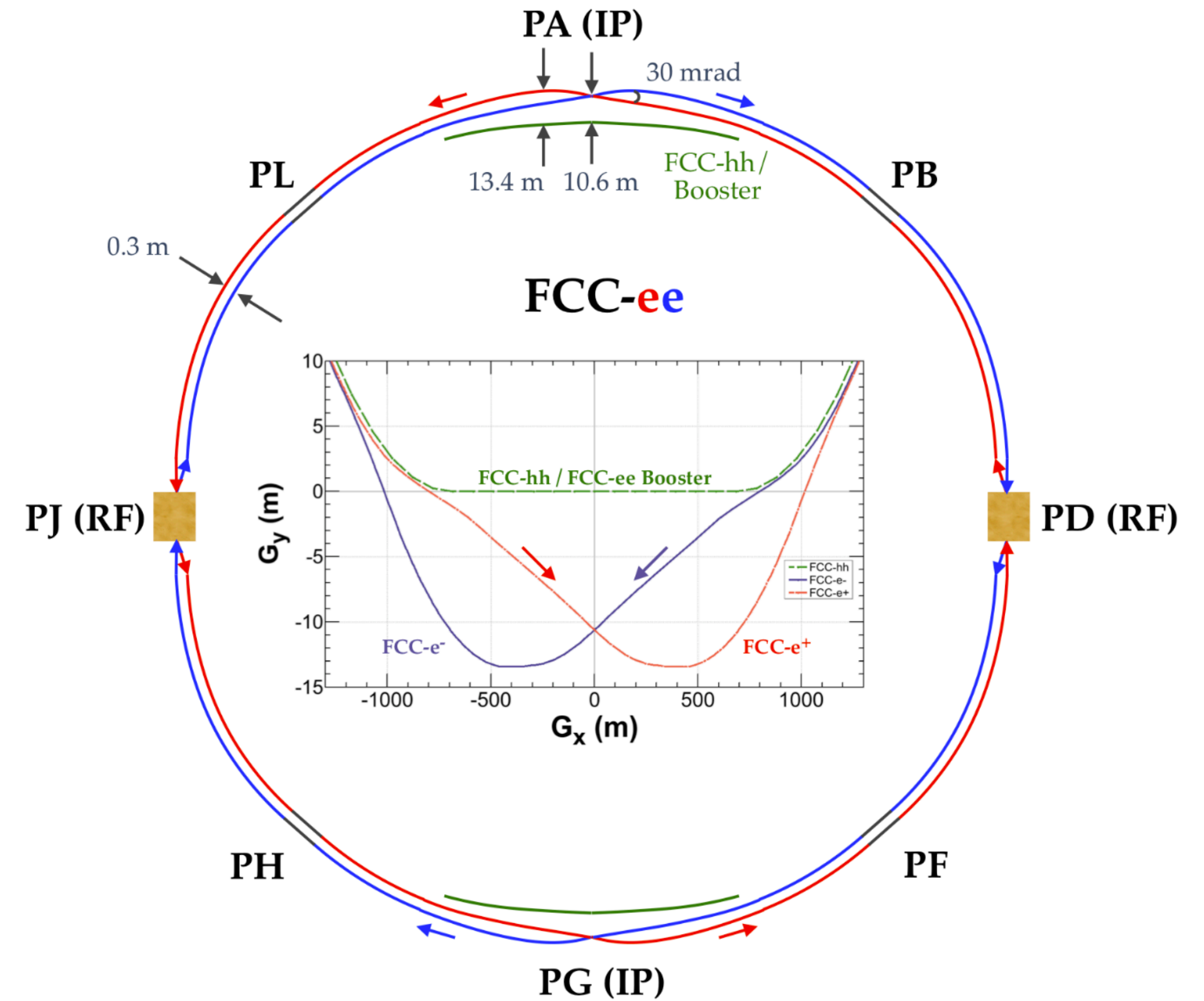
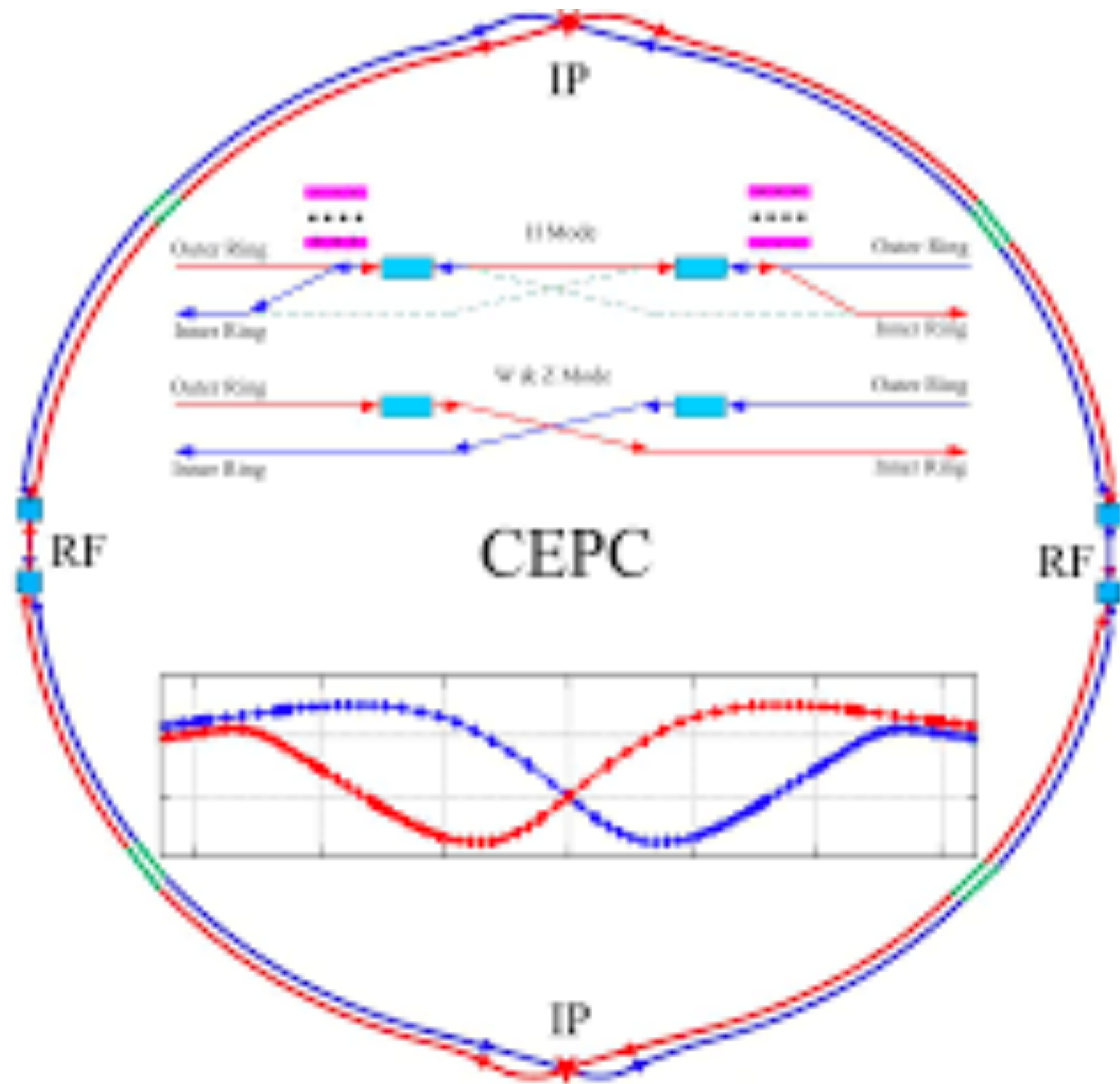
# Transverse $\Lambda$ polarization at the LEP

OPAL '97

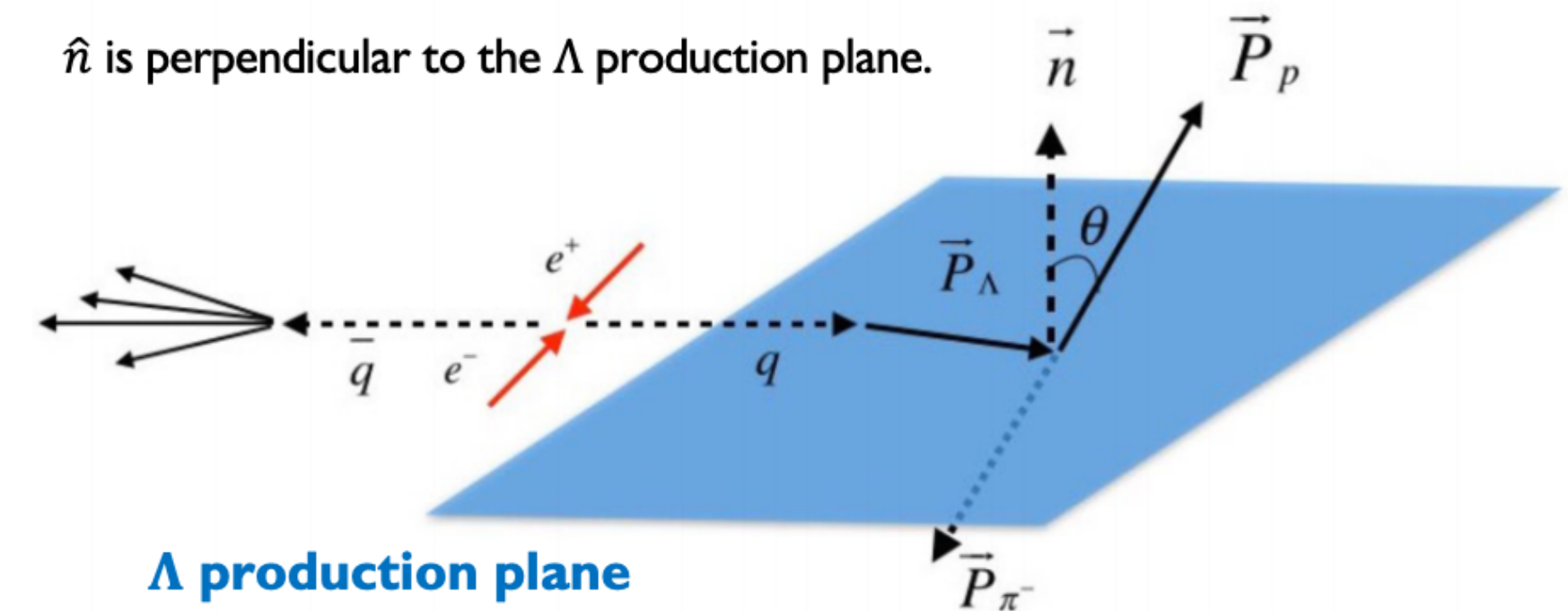
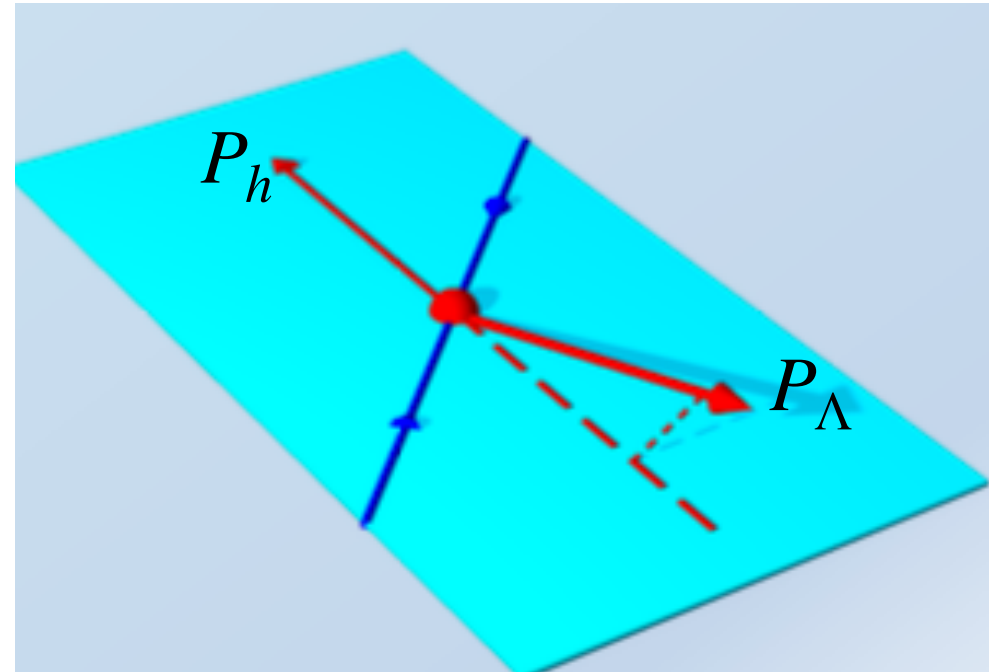


**No significant transverse polarization is observed at the LEP**

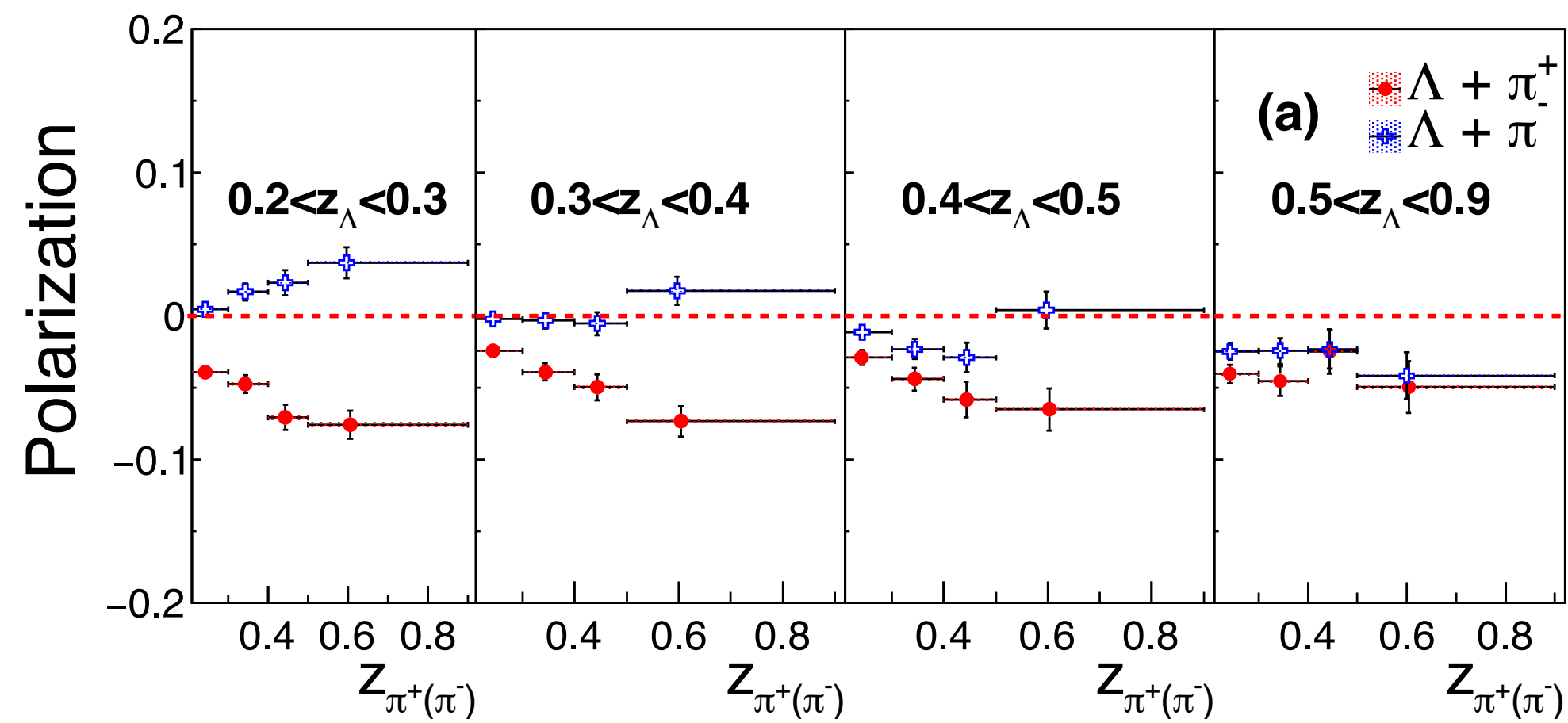
# Transverse $\Lambda$ polarization at the future $e^+e^-$ collider ??



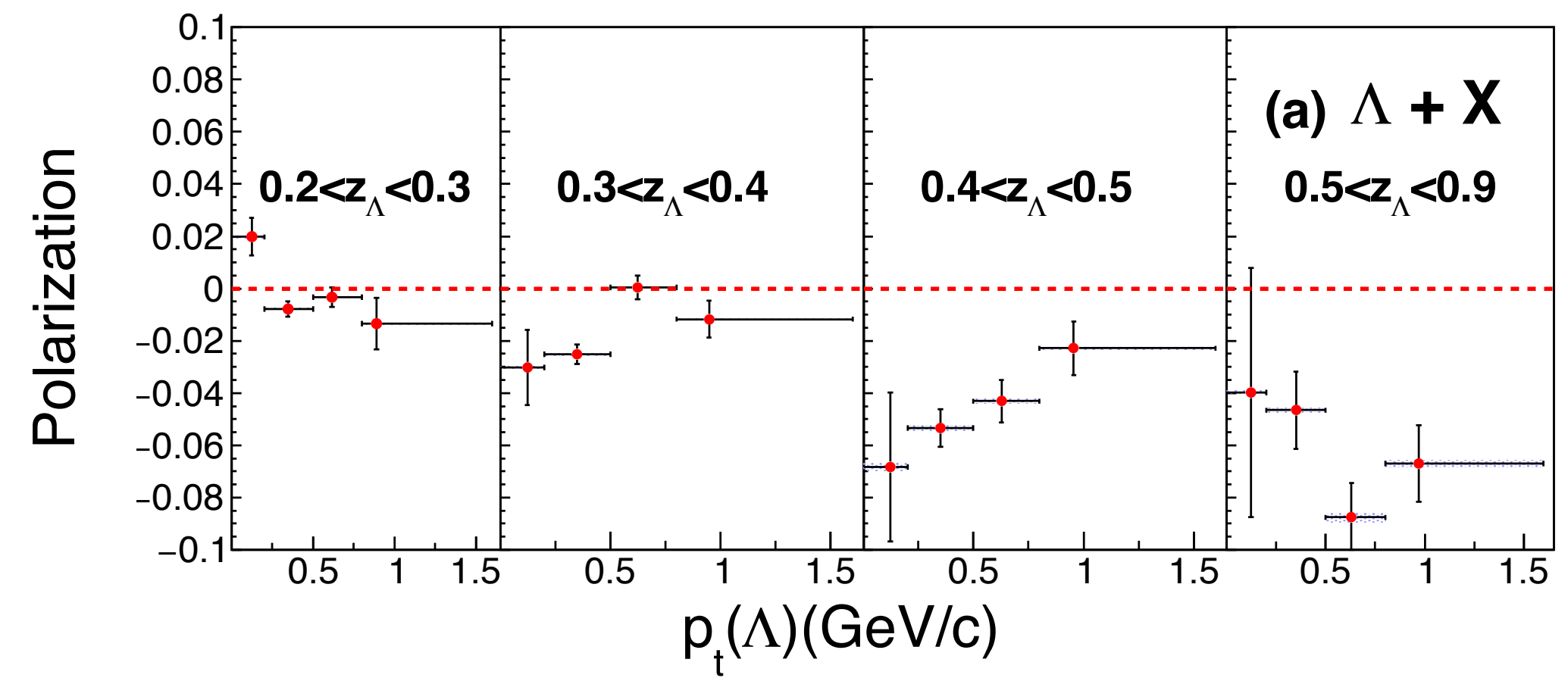
# Transverse $\Lambda$ polarization at the Belle



Belle '18 PRL



$$e^+e^- \rightarrow \Lambda^\uparrow h X$$



$$e^+e^- \rightarrow \Lambda^\uparrow(\text{Thrust}) X$$

# Theory framework on transverse $\Lambda$ polarization

$$e^+e^- \rightarrow \Lambda^\uparrow h X$$

$$e^+e^- \rightarrow \Lambda^\uparrow(\text{Thrust}) X$$

Collins-Soper-Sterman, Ji-Ma-Yuan, Soft-Collinear Effective Theory... ..

???

## TMD factorization two scale problem

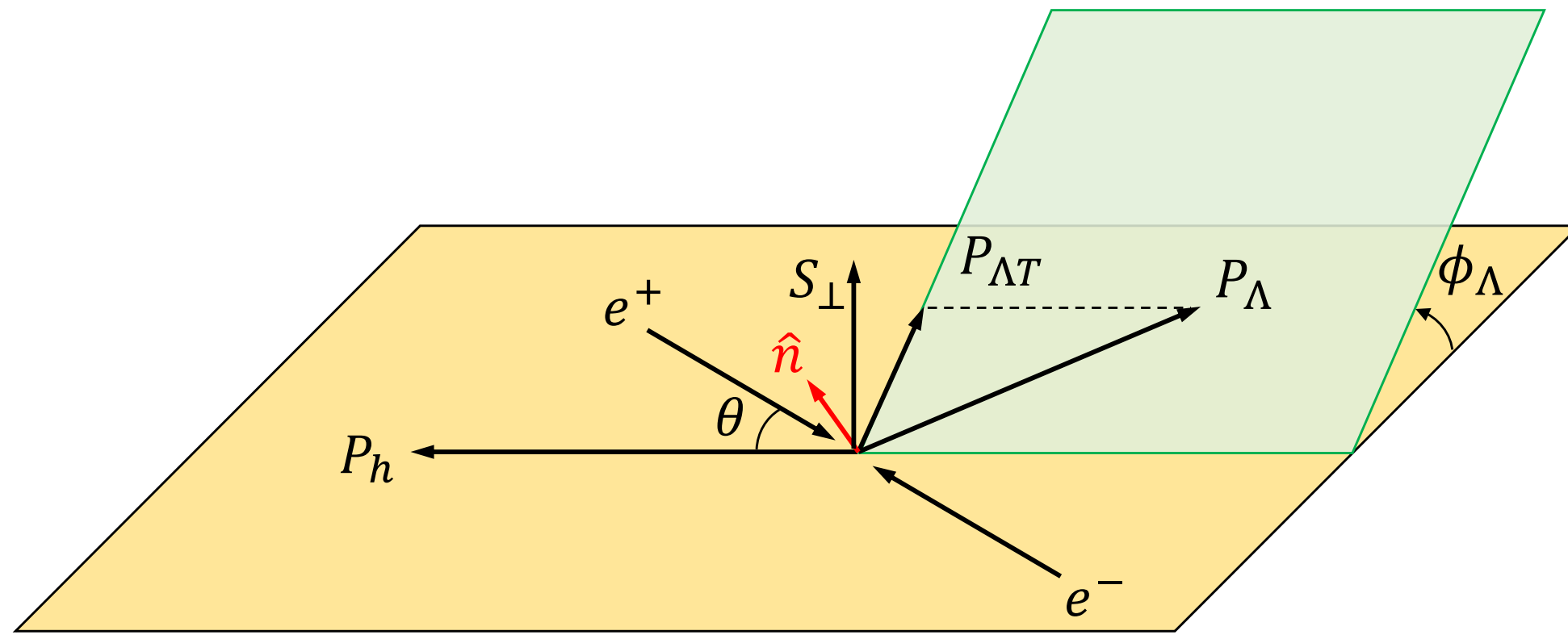
$$\Lambda_{QCD} \lesssim j_\perp \ll Q$$

**Is it the same (polarizing) fragmentation function in these two measurements ???**

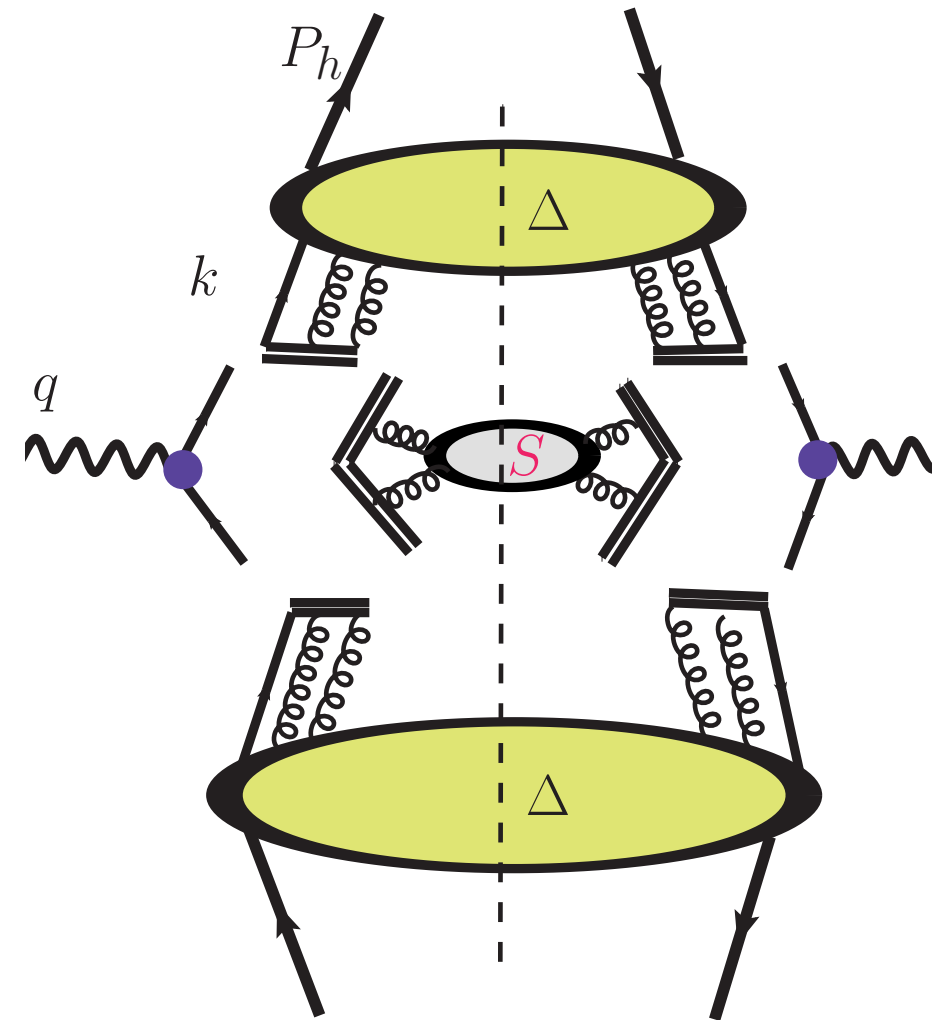
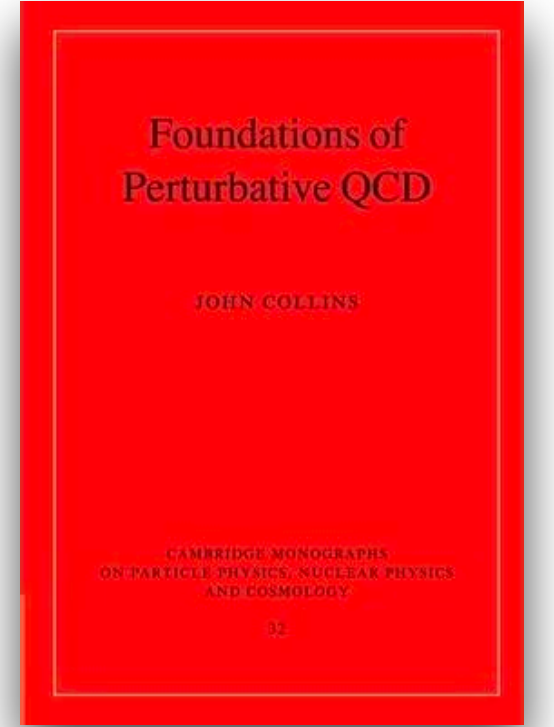


# Back-to-back $\Lambda+h$

$$e^-(\ell) + e^+(\ell') \rightarrow \gamma^*(q) \rightarrow h(P_h) + \Lambda(P_\Lambda, \mathbf{S}_\perp) + X$$



TMD factorization theorems have been established for back-to-back  $\Lambda+h$



$$W^{\mu\nu} \stackrel{\text{prelim}}{=} \frac{8\pi^3 z_A z_B}{Q^2} \sum_f \text{Tr} k_{A,\gamma}^+ \gamma^- H_f^\nu(Q) k_{B,\gamma}^- \gamma^+ \bar{H}_f^\mu(Q) \\ \times \int \frac{d^{2-2\epsilon} \mathbf{b}_T}{(2\pi)^{2-2\epsilon}} e^{-i\mathbf{q}_{hT} \cdot \mathbf{b}_T} \tilde{S}(\mathbf{b}_T) \tilde{D}_{1, H_A/f}(z_A, \mathbf{b}_T) \tilde{D}_{1, H_B/\bar{f}}(z_B, \mathbf{b}_T) \\ + \text{polarized terms.}$$

also see Hui Li's talk

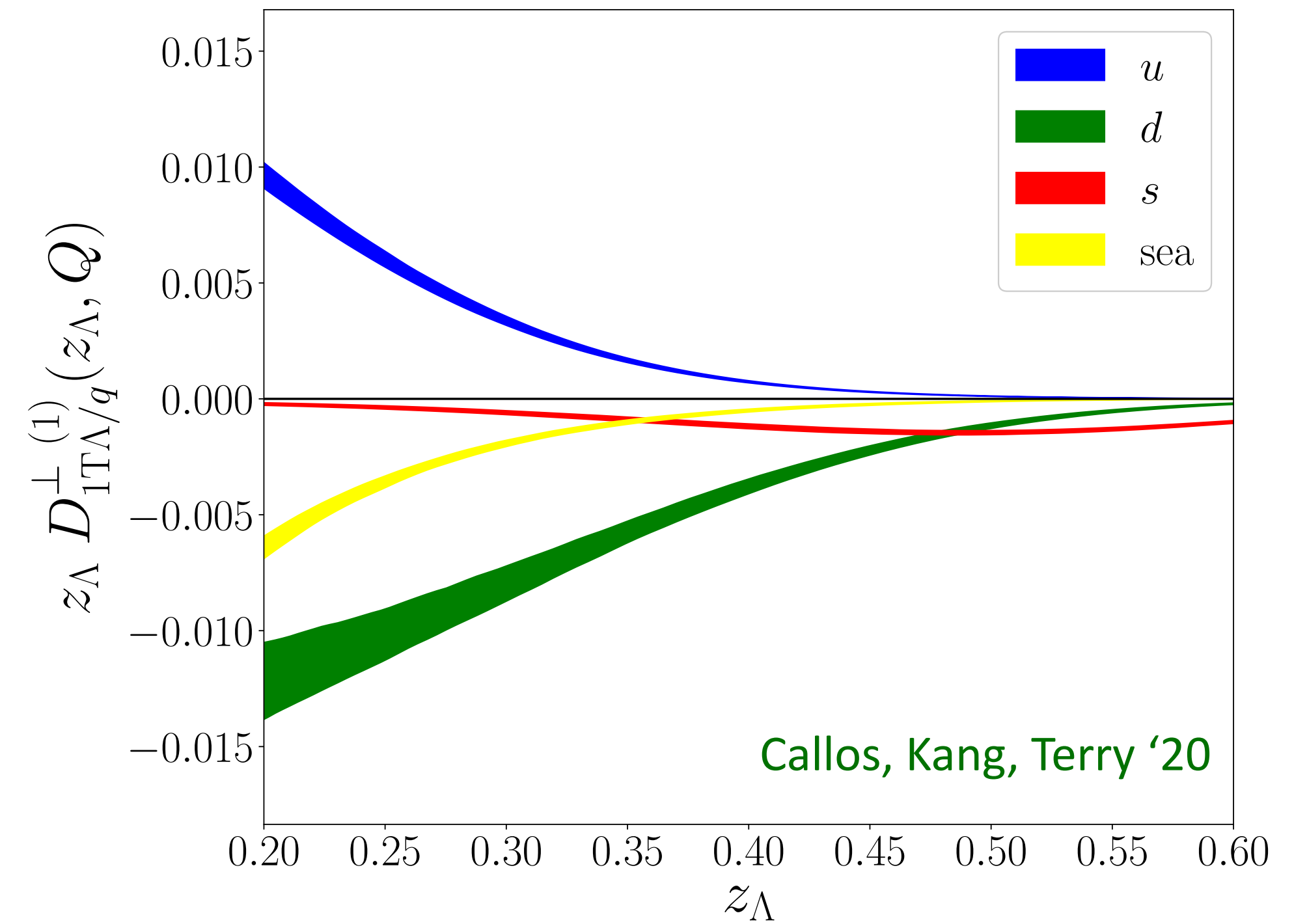
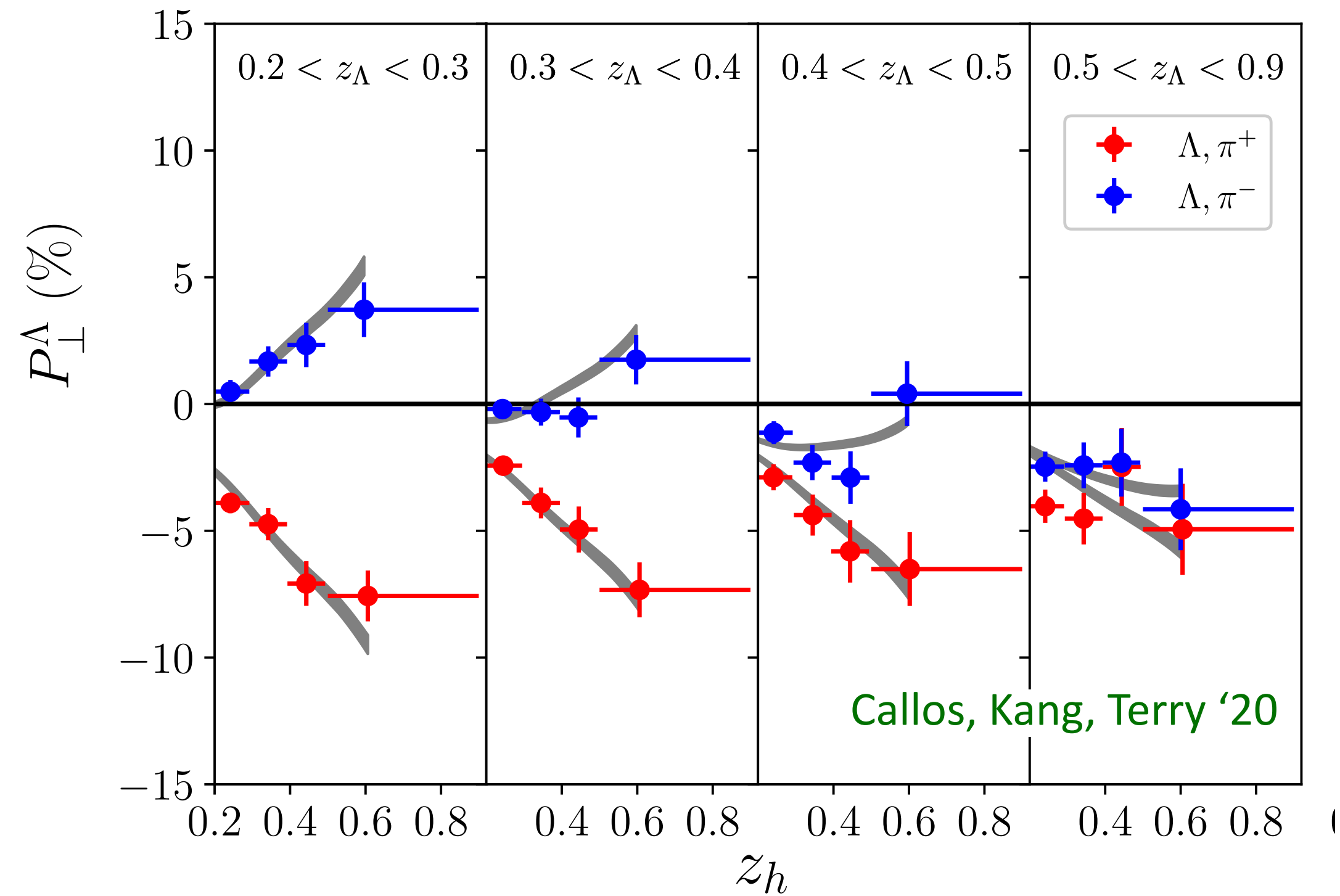
Spin-dependent cross section is factorized as:

$$\frac{d\sigma(\mathbf{S}_\perp)}{d\mathcal{P} \mathcal{S} d^2 \mathbf{q}_\perp} = \sigma_0 \left\{ \mathcal{F} [D_{\Lambda/q} D_{h/\bar{q}}] + |\mathbf{S}_\perp| \sin(\phi_S - \phi_\Lambda) \frac{1}{z_\Lambda M_\Lambda} \mathcal{F} \left[ \hat{\mathbf{P}}_{\Lambda T} \cdot \mathbf{p}_{\Lambda\perp} D_{1T,\Lambda/q}^\perp D_{h/\bar{q}} \right] + \dots \right\}$$

**Polarizing fragmentation function**

see Xue's talk on Collins functions

# Fitting of PFFs from $\Lambda+h$ data



Yang, Lu, Schmidt '17

D'Alesio, Murgia, Zaccheddu '20

Callos, Kang, Terry '20

Li, Wang, Yang, Lu '20

... ..

Spectator model: see Mao's talk

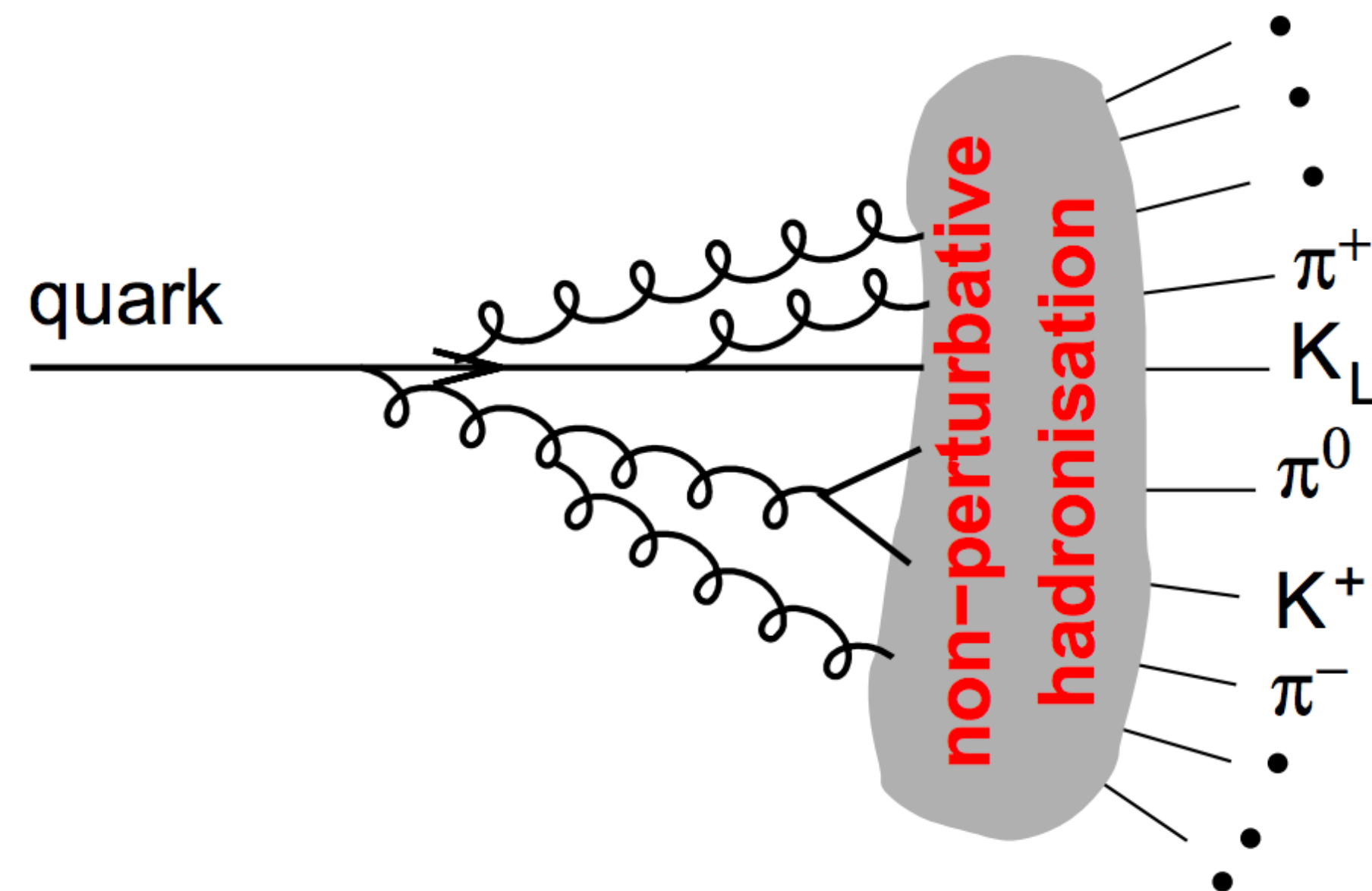
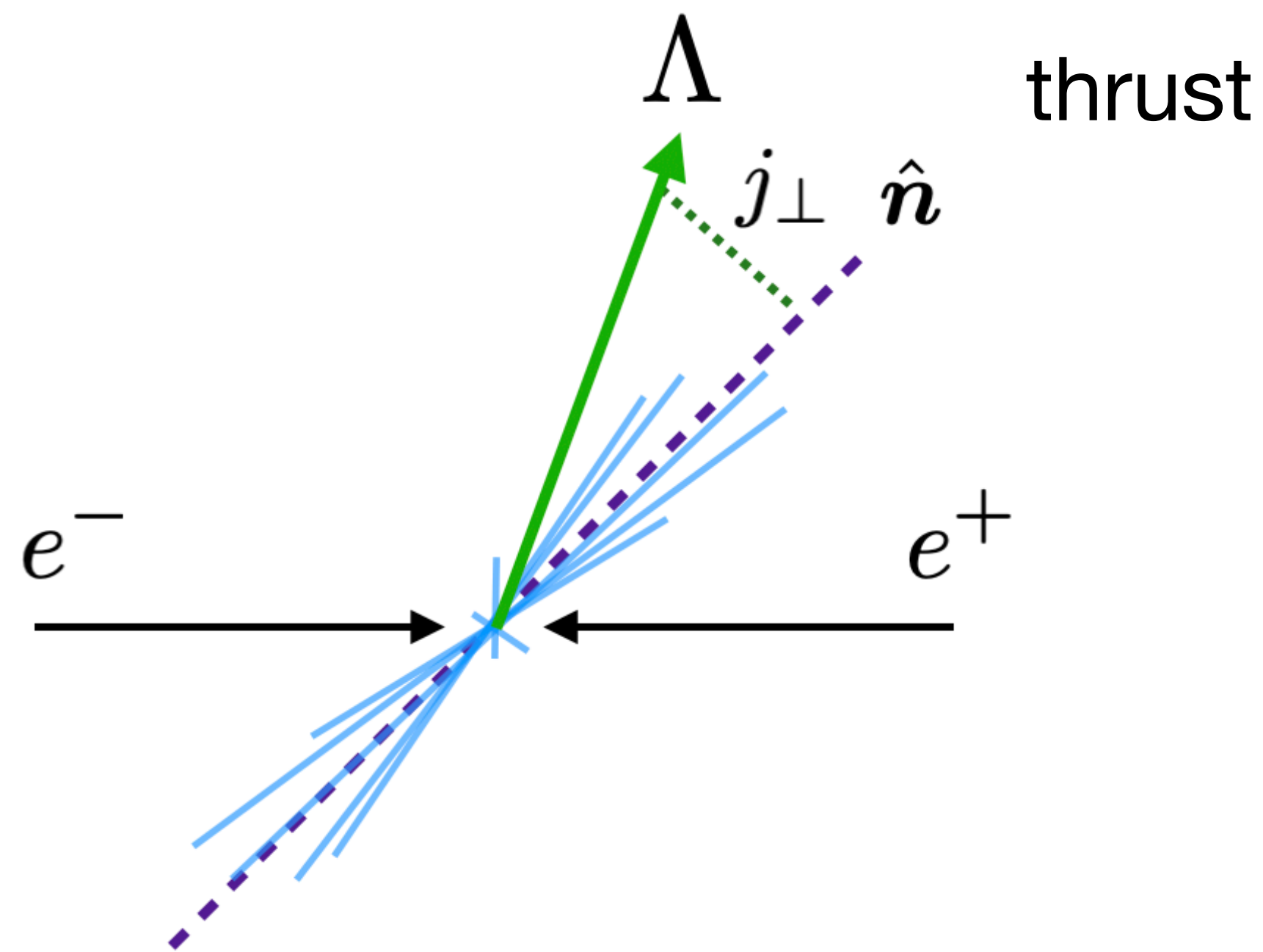
Light-front quantization: See Chandan, Lan, Xu, Zhao's talk

.....

# TMD factorization for $\Lambda(\text{thrust})$

Parton (quark or gluon) fragmentation and hadronization

High-energy partons lead to collimated bunches of hadrons



Wei, Chen, Song, Liang '14; Yang, Chen, Liang '17,.....(Twist-4 FF, Parton model on the jet)

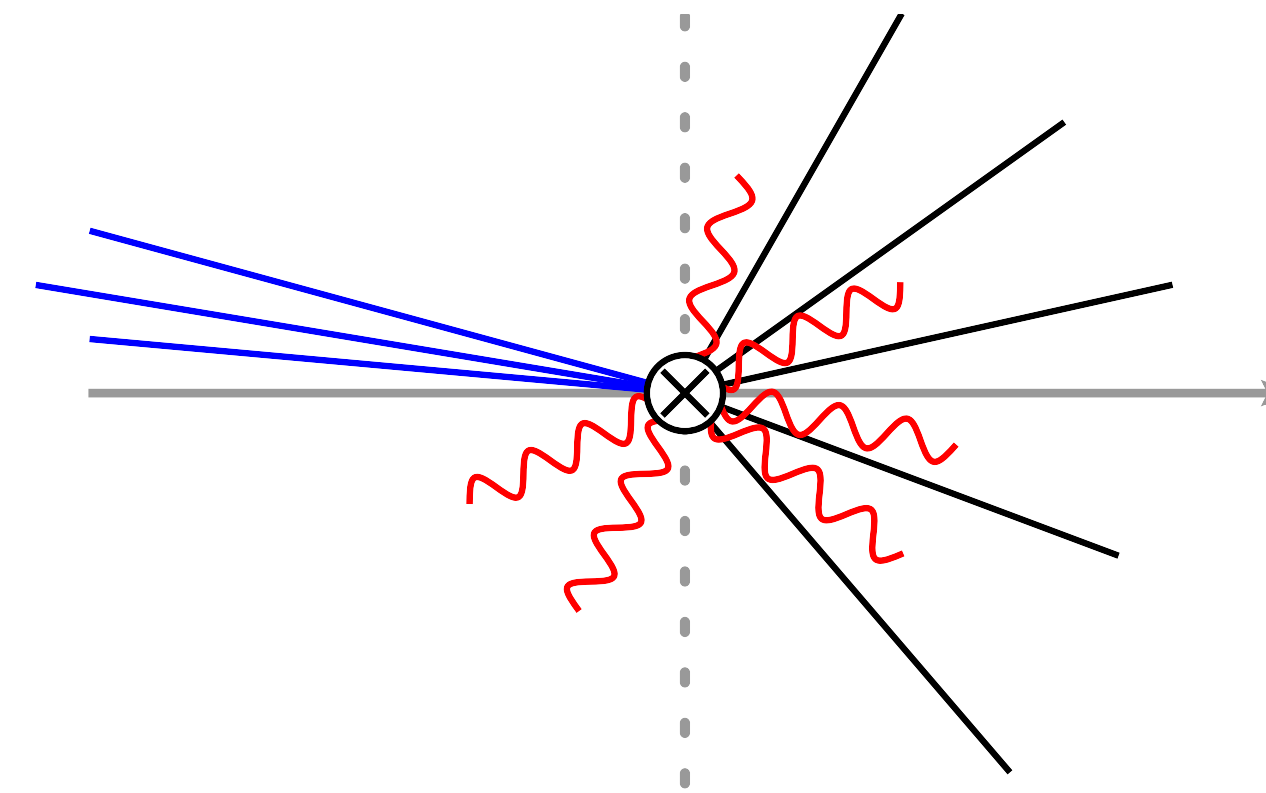
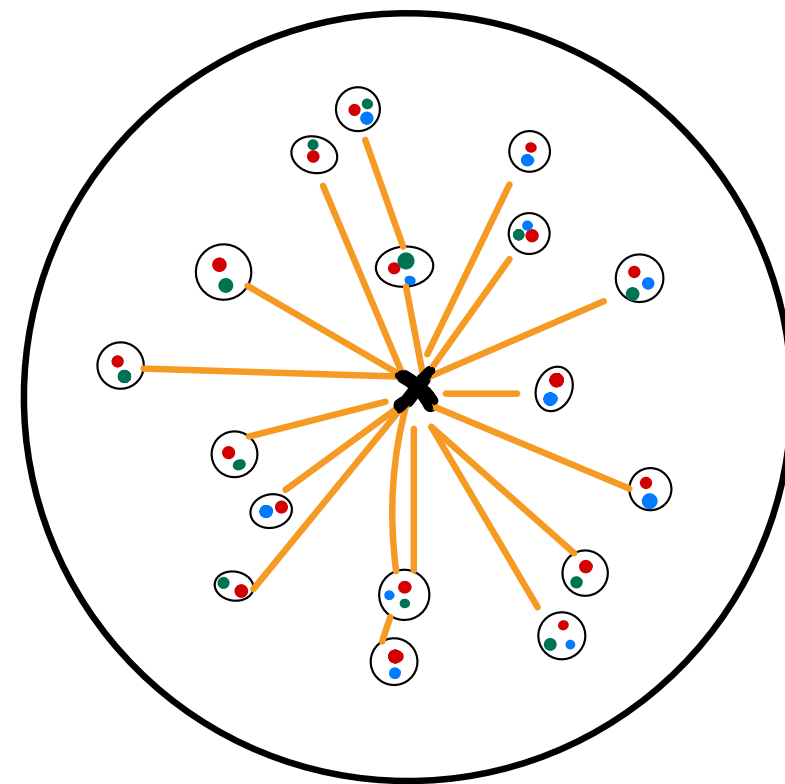
**Jets are not the same as partons**  
**Jets inherit quantum property of partons**

# TMD factorization formula on the jet broadening

(Becher, Rahn, DYS '17 JHEP)

Definition of the broadening:

$$b_N = \sum_{i \in \text{jets}} |\vec{p}_i^\perp|$$



Construction of the theory formalism  $b_N \ll Q$

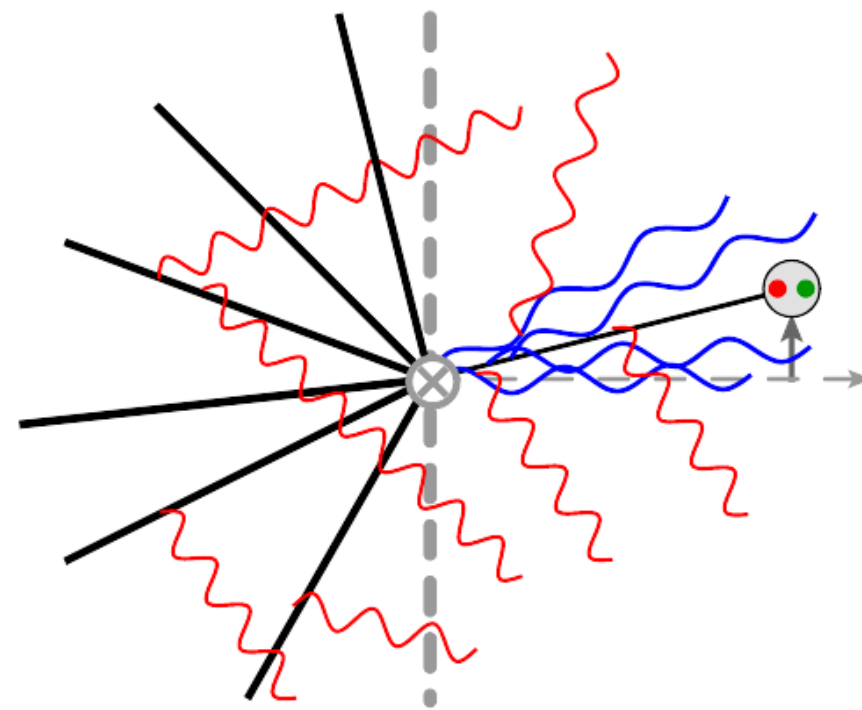
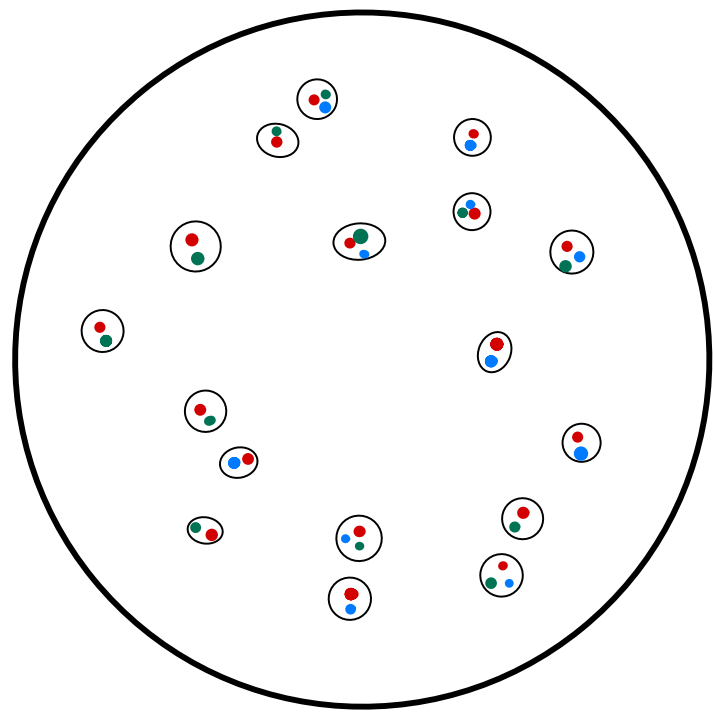
- Two scales in the problem
- Rely on effective field theory: SCET + Jet Effective Theory (Becher, Neubert, Rothen, DYS '16 PRL)

$$\frac{d\sigma}{db_N} = \sum_{f=q,\bar{q},g} \int db_N^s \int d^{d-2} p_N^\perp \mathcal{J}_f(b_N - b_N^s, p_N^\perp) \sum_{m=1}^{\infty} \langle \mathcal{H}_m^f(\{\underline{n}\}, Q) \otimes \mathcal{S}_m(\{\underline{n}\}, b_N^s, -p_N^\perp) \rangle$$

**Rapidity divergence cancellation is verified at two-loop order !!!**

# Factorization on single hadron unpolarized TMDs

(Kang, DYS, Zhao '20 JHEP)



**hard:**  $p_h \sim Q(1, 1, 1)$

**collinear:**  $p_c \sim Q(\lambda^2, 1, \lambda)$

**soft:**  $p_s \sim Q(\lambda, \lambda, \lambda)$

$$\lambda = j_T/Q \ll 1$$

**TMD factorization formula:**

TMDFFs

$$\frac{d\sigma}{dz_h d^2\vec{j}_T} = \sum_{i=q,\bar{q},g} \int \frac{d^2\vec{b}}{(2\pi)^2} e^{i\vec{b}\cdot\vec{j}_T/z_h} \sum_{m=2}^{\infty} \frac{1}{N_c} \text{Tr}_c \left[ \mathcal{H}_m^i(\{\underline{n}\}, Q, \mu) \otimes \mathcal{S}_m(\{\underline{n}\}, b, \mu, \nu) \right] D_{h/i}(z_h, b, \mu, \zeta/\nu^2)$$

“Multi-Wilson-line structure” Becher, Neubert, Rothen, DYS '16 PRL,...

A similar structure is also mentioned in Boglione & Simonelli '20 within the CSS framework

## All-order resummation formula:

$$\frac{d\sigma}{dz_h d^2\vec{j}_T} = \sigma_0 \sum_{i=q,\bar{q}} e_i^2 \int_0^\infty \frac{b db}{2\pi} J_0(bj_T/z_h) e^{-S_{\text{pert}}(\mu_{b^*}, \mu_h) - S_{\text{NP}}(b, Q_0, Q)} \frac{1}{z_h^2} D_{h/i}(z_h, \mu_{b^*}) U_{\text{NG}}(\mu_{b^*}, \mu_h)$$

**QCD evolution between  $Q$  and  $j_T$**

**Linear part:**  $S_{\text{pert}}(\mu_b, \mu_h) = \int_{\mu_b}^{\mu_h} \frac{d\mu}{\mu} \left[ \Gamma_{\text{cusp}}(\alpha_s) \ln\left(\frac{Q^2}{\mu^2}\right) - 2\gamma^{D_q}(\alpha_s) - \gamma^S(\alpha_s) \right]$

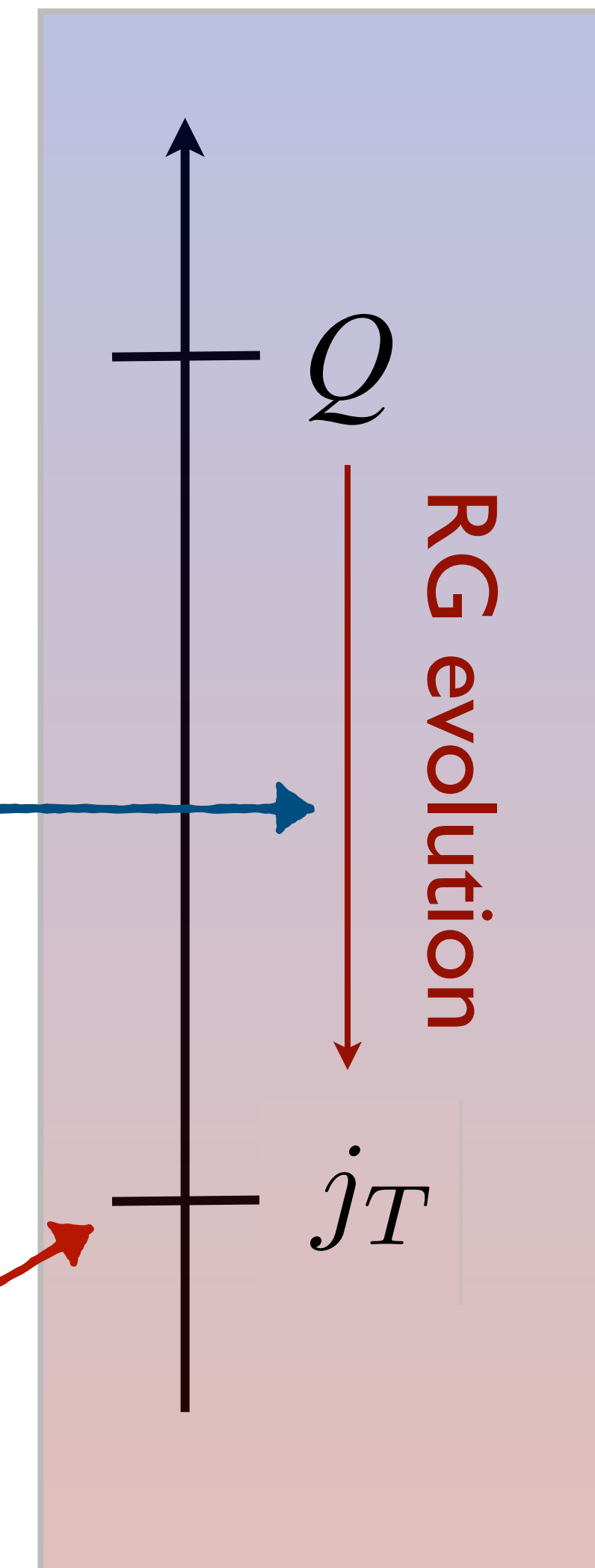
**Non-linear part:**  $U_{\text{NG}}(\mu_{b^*}, \mu_h) = \exp\left[-C_A C_F \frac{\pi^2}{3} u^2 \frac{1+(au)^2}{1+(bu)^c}\right]$   
 Dasgupta, Salam '01

**Non-perturbative corrections:**  $j_T \sim \Lambda_{\text{QCD}}$

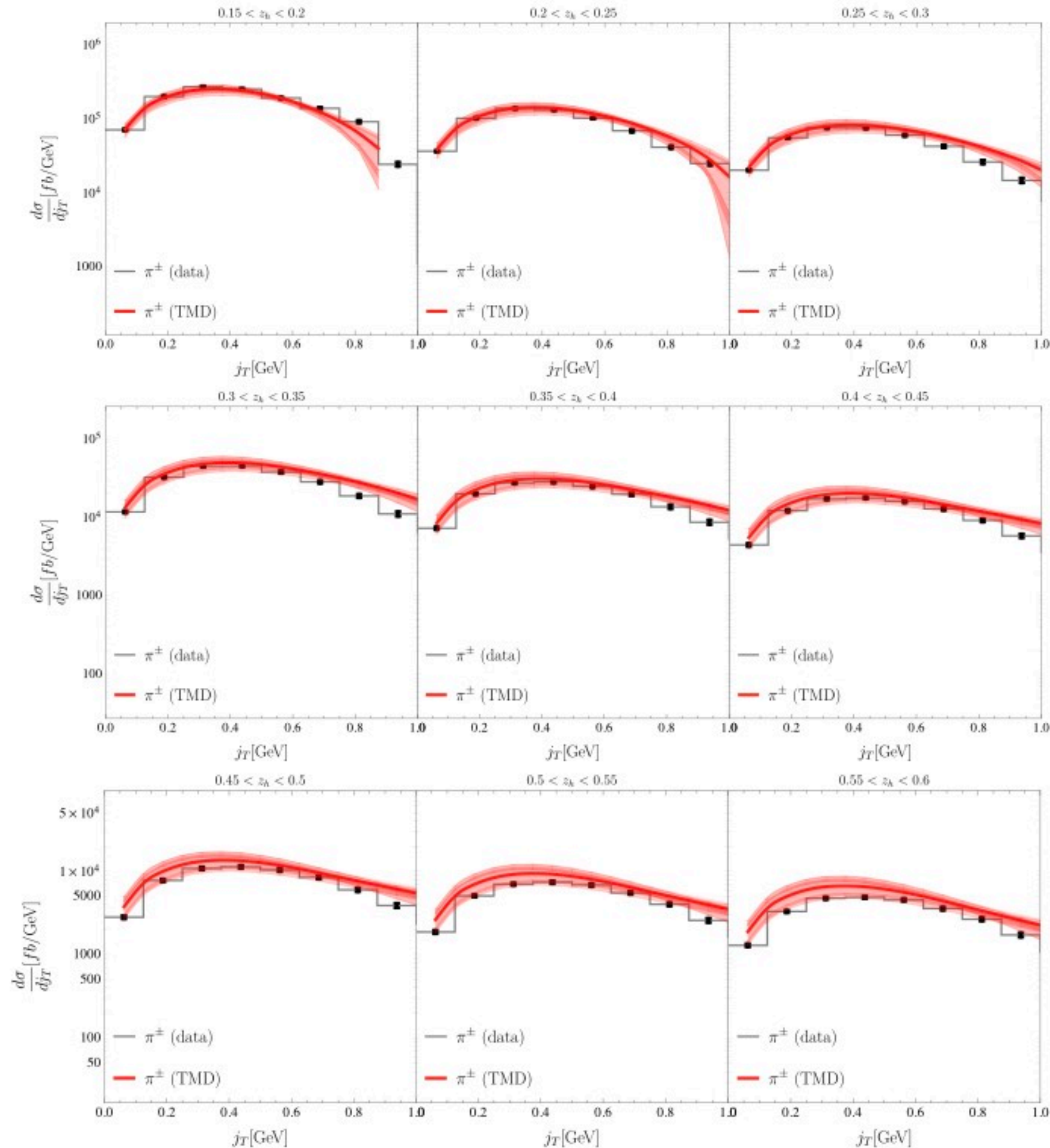
$S_{\text{NP}}(b, Q_0, Q) = \frac{g_2}{2} \ln\left(\frac{b}{b_*}\right) \ln\left(\frac{Q}{Q_0}\right) + \frac{g_h}{z_h^2} b^2$  **fitted in standard TMD processes**  
 Sun, Isaacson, Yuan, Yuan '14  
 also see Yibo Yang's talk on LQCD predictions

**Non-perturbative collinear FFs**  $D_{h/i}(z_h, \mu_{b^*})$  **(DSS2014)**

de Florian, *et.al.* '15

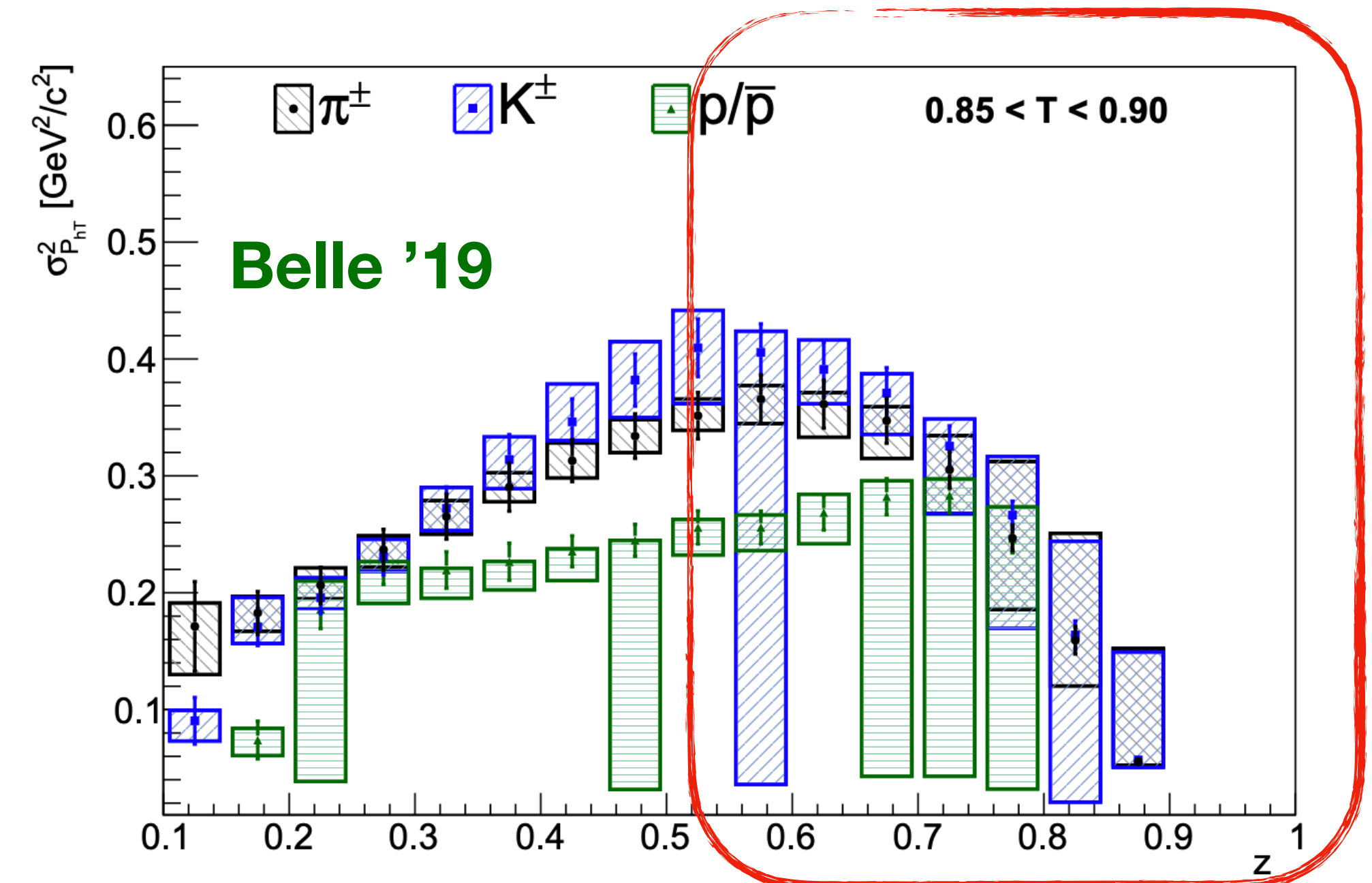


# Numerical results



- Our TMD resummation formula gives a good description of the shape of  $j_T$  distribution as  $z_h < 0.65$
- As  $z_h > 0.65$ , one needs to also include threshold resummation effects

$$\frac{d\sigma}{dz_h d^2\vec{j}_T} \propto \frac{1}{\pi\sigma_{j_T}^2} \exp\left(-j_T^2/\sigma_{j_T}^2\right)$$

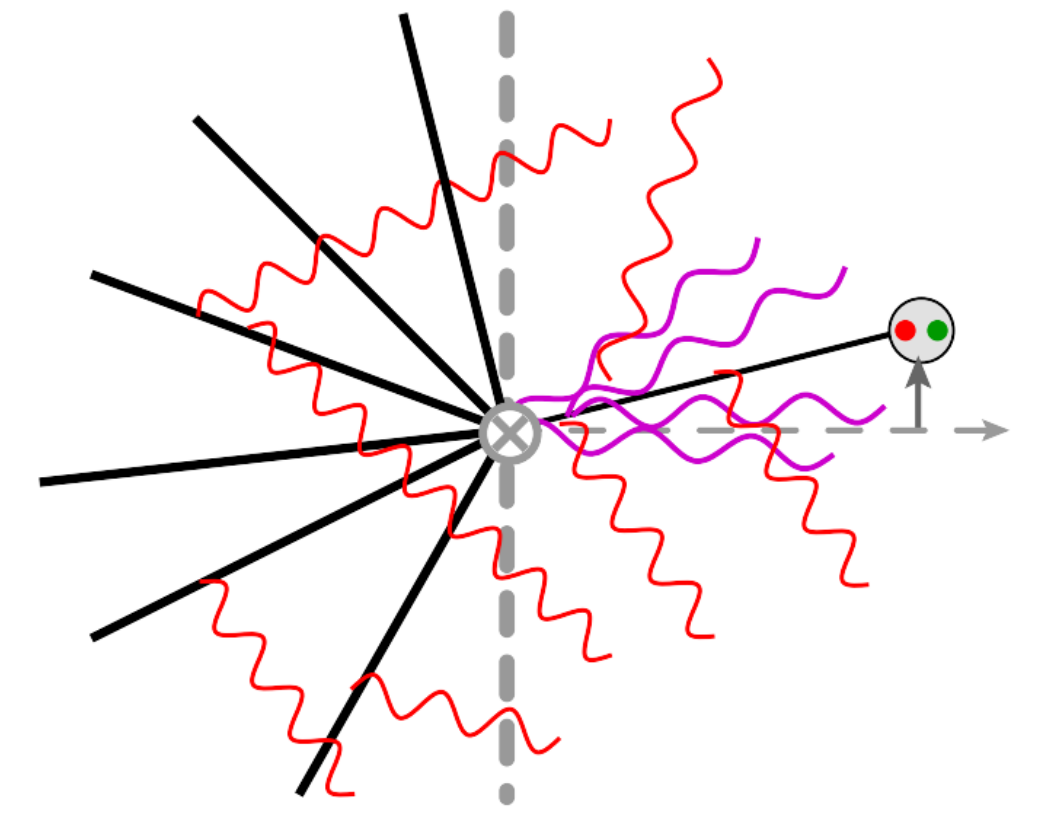


# Joint threshold and TMD factorization

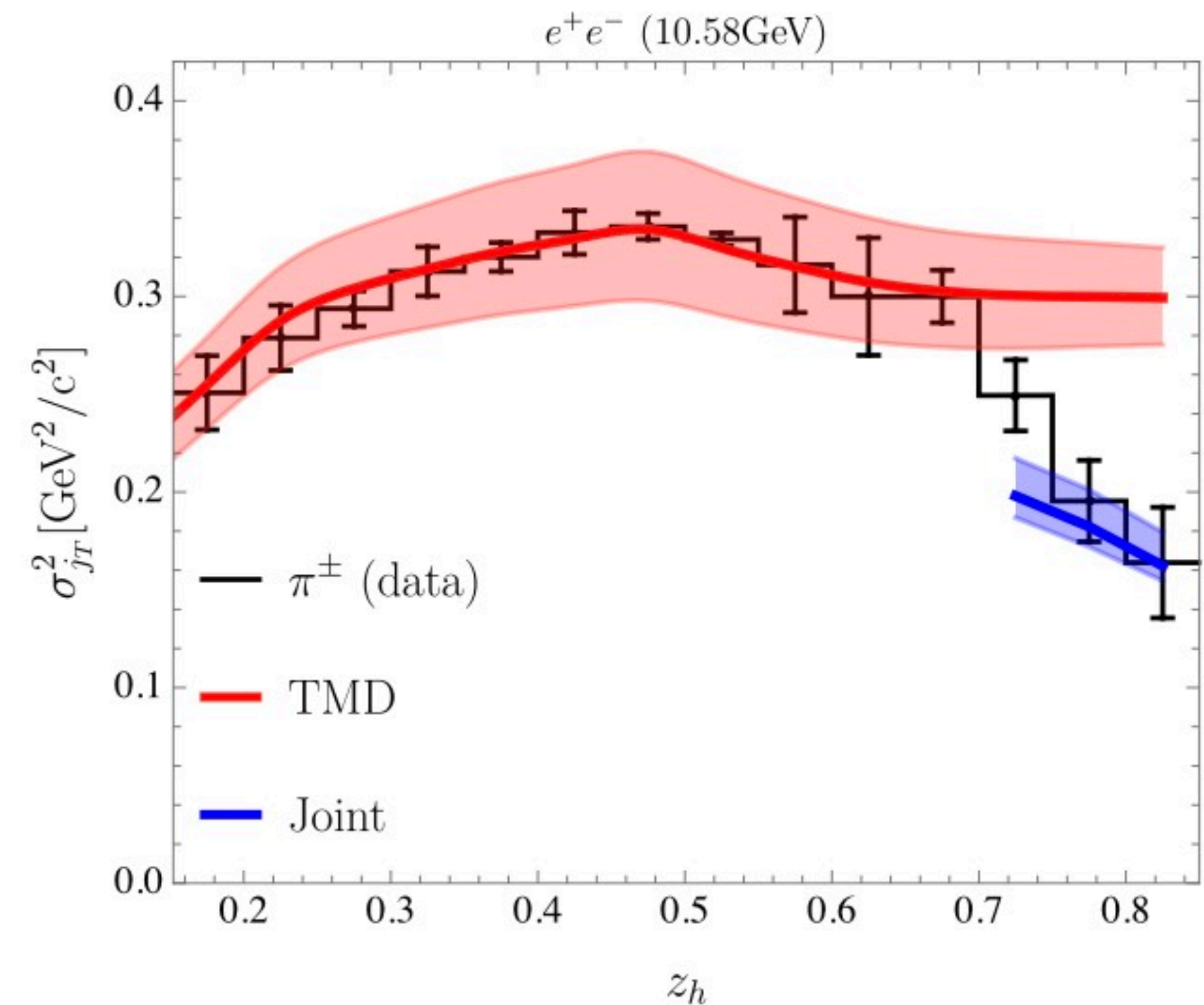
**Joint factorization:**  $z_h \rightarrow 1$  &  $j_T \ll Q$

**Resummation formula:**

$$\frac{d\sigma}{dz_h d^2\vec{j}_T} = \sigma_0 \sum_{i=q,\bar{q}} \int_0^\infty \frac{b db}{2\pi} J_0(bj_T/z_h) \frac{1}{z_h^2} \int_{z_h}^1 \frac{dz}{z} e^{-\hat{S}_{\text{pert}}(\mu_{b^*}, \mu_h) - \hat{S}_{\text{NP}}(b, Q_0, Q)} \frac{e^{-2\gamma_E \eta}}{\Gamma(2\eta)} \frac{1}{1-z} D_{h/i}(z_h/z, \mu_h) U_{\text{NG}}(\mu_{b^*}, \mu_h)$$



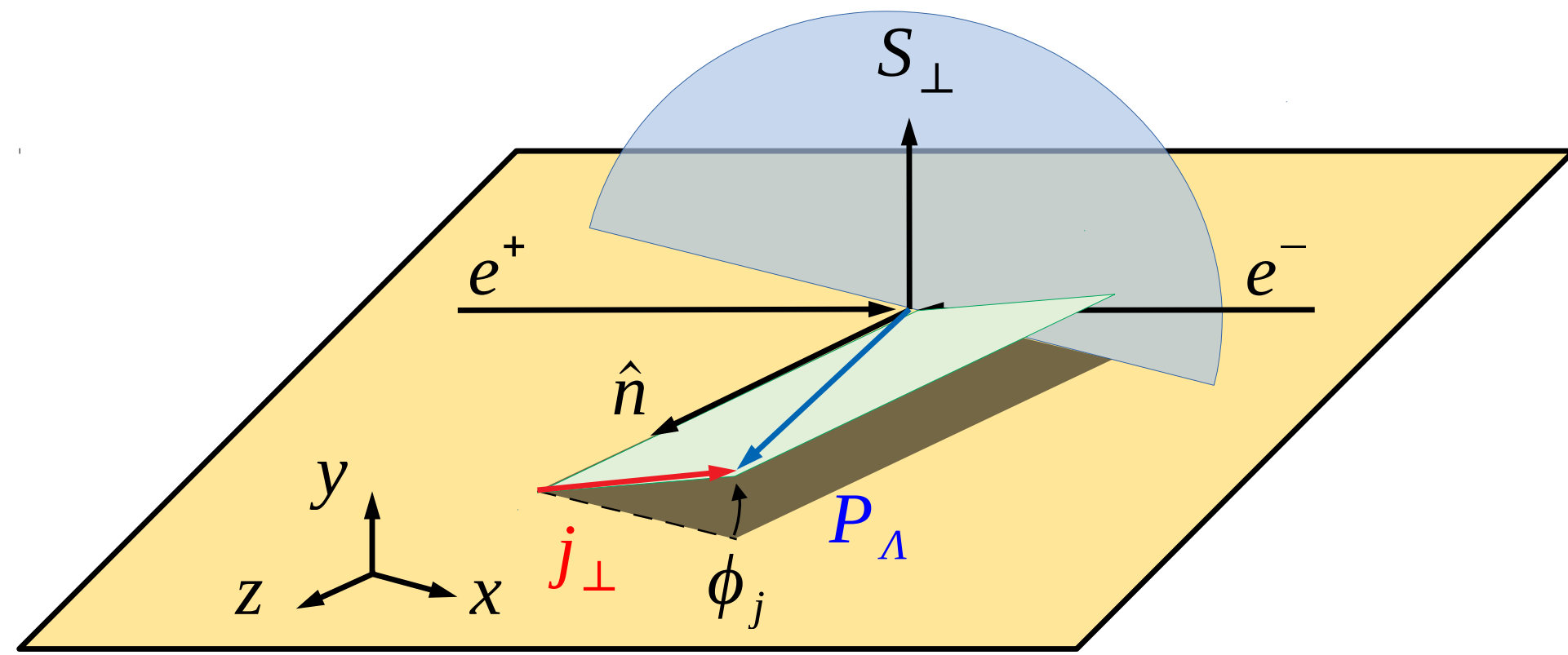
- The Gaussian width of the  $j_T$  distribution given by the TMD formalism freeze to a certain value.
- After including joint threshold and TMD resummation effects, the theoretical predictions are consistent with the data





# Factorization on transverse polarized $\Lambda$ hyperon production with the thrust axis

Gamberg, Kang, DYS, Terry, Zhao 2101.XXXXX

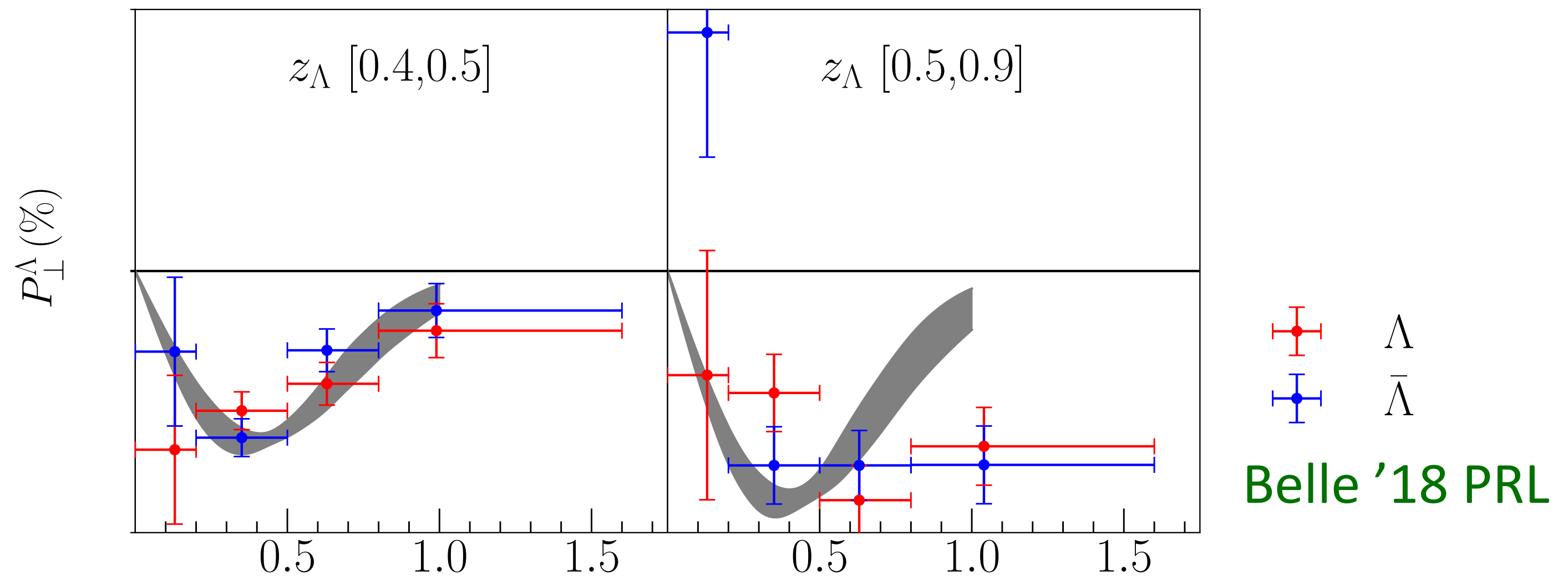


$$P_{\perp}^{\Lambda}(z_{\Lambda}, j_{\perp}) = \frac{d\Delta\sigma}{dz_{\Lambda}d^2j_{\perp}} \bigg/ \frac{d\sigma}{dz_{\Lambda}d^2j_{\perp}}$$

Theory predictions are consistent with Belle data

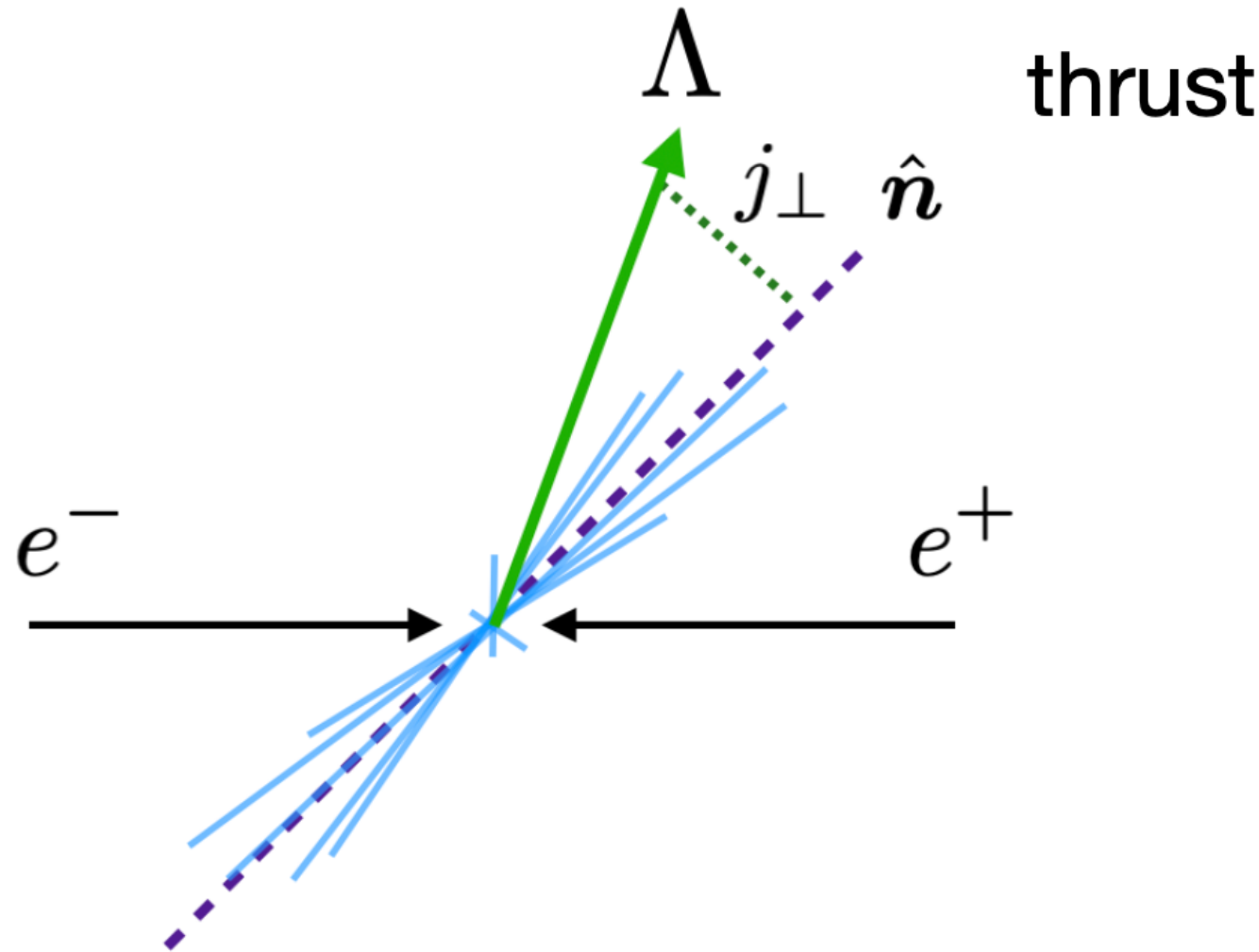
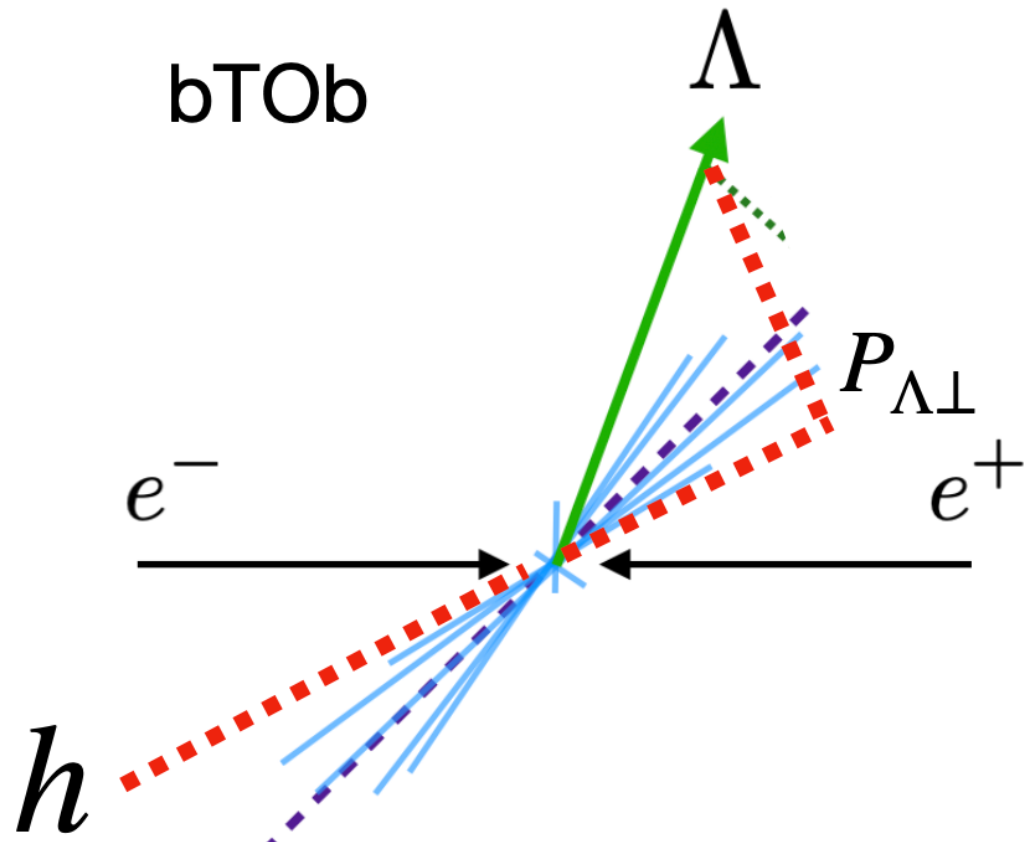
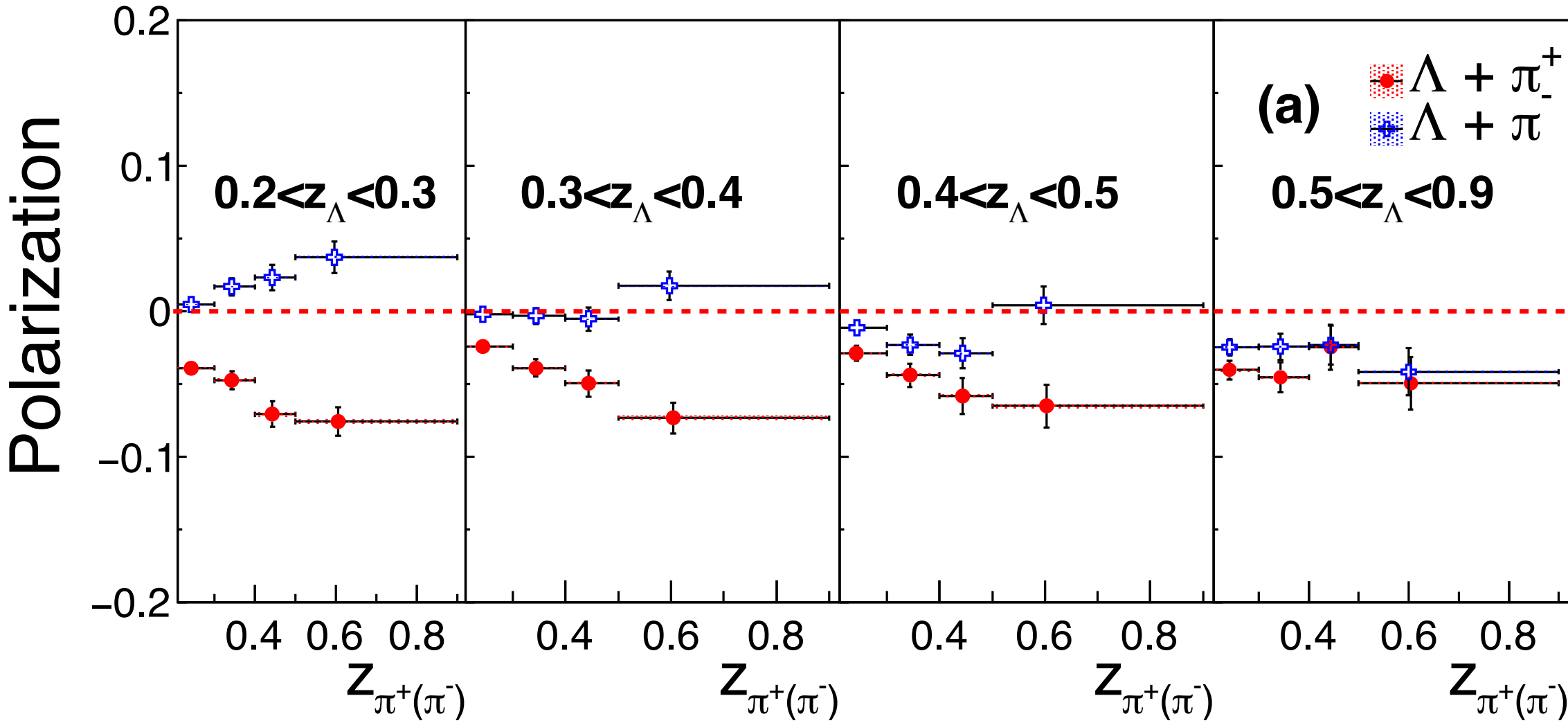
## Theory formula including QCD evolution

$$\begin{aligned} \frac{d\Delta\sigma}{dz_{\Lambda}d^2j_{\perp}} &= \frac{d\sigma(\mathbf{S}_{\perp})}{dz_{\Lambda}d^2j_{\perp}} - \frac{d\sigma(-\mathbf{S}_{\perp})}{dz_{\Lambda}d^2j_{\perp}} \\ &= \sigma_0 \sin(\phi_s - \phi_j) \sum_q e_q^2 \int_0^{\infty} \frac{b^2 db}{2\pi} J_1\left(\frac{bj_{\perp}}{z_{\Lambda}}\right) \\ &\times \frac{M_{\Lambda}}{z_{\Lambda}^2} D_{1T, \Lambda/q}^{\perp(1)}(z_{\Lambda}, \mu_{b_*}) e^{-S_{\text{NP}}^{\perp}(b, z_{\Lambda}, Q'_0, Q) - S_{\text{pert}}(\mu_{b_*}, Q)} \\ &\times U_{\text{NG}}(\mu_{b_*}, Q) \end{aligned}$$



# Flavor separation of PFFs

Belle '18 PRL



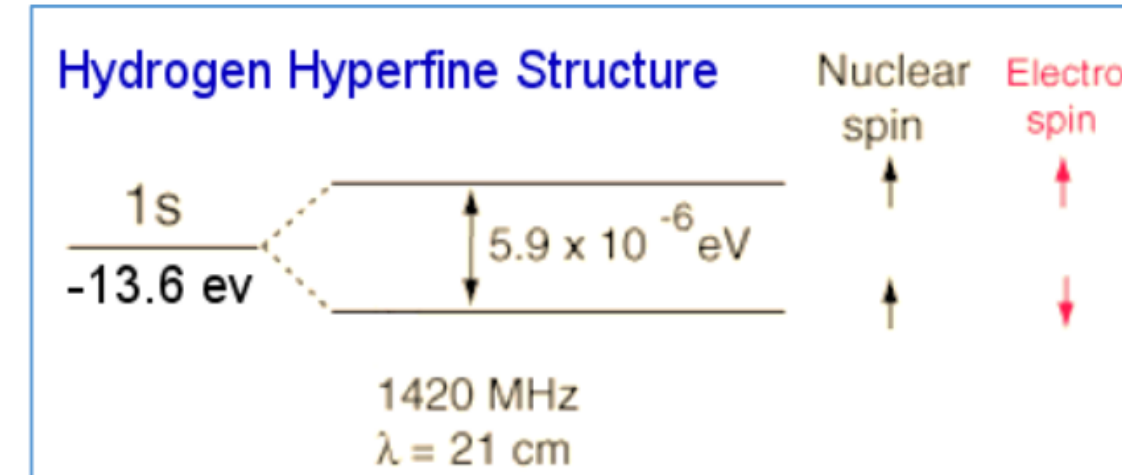
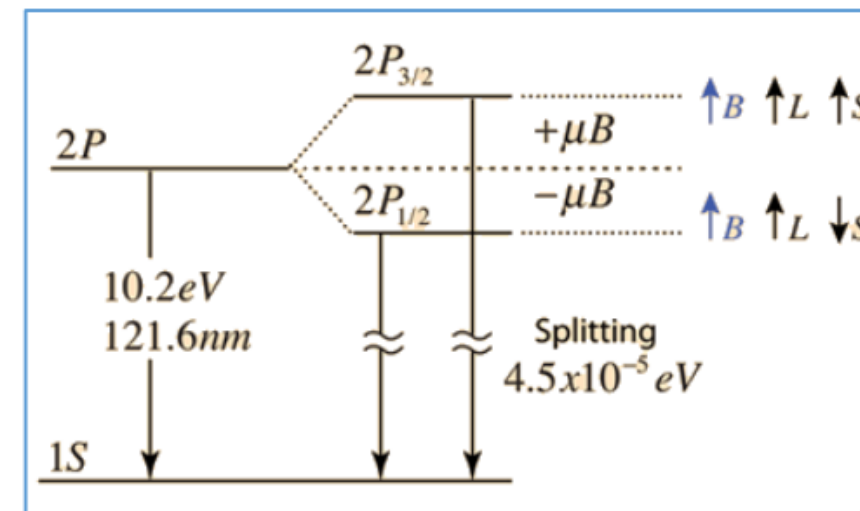
**Jets inherit quantum property of partons !!!**



**Jet substructure**

# Why spectroscopy—Atomic

We need high precision



$$\frac{1}{\lambda_{\text{vac}}} = R \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$



Johannes Rydberg



Niels Henrik David Bohr



Edward W. Morley



Arnold Sommerfeld



Albert Abraham Michelson



Wolfgang Pauli

Fine structure

Hyperfine structure

Lisheng Geng's talk

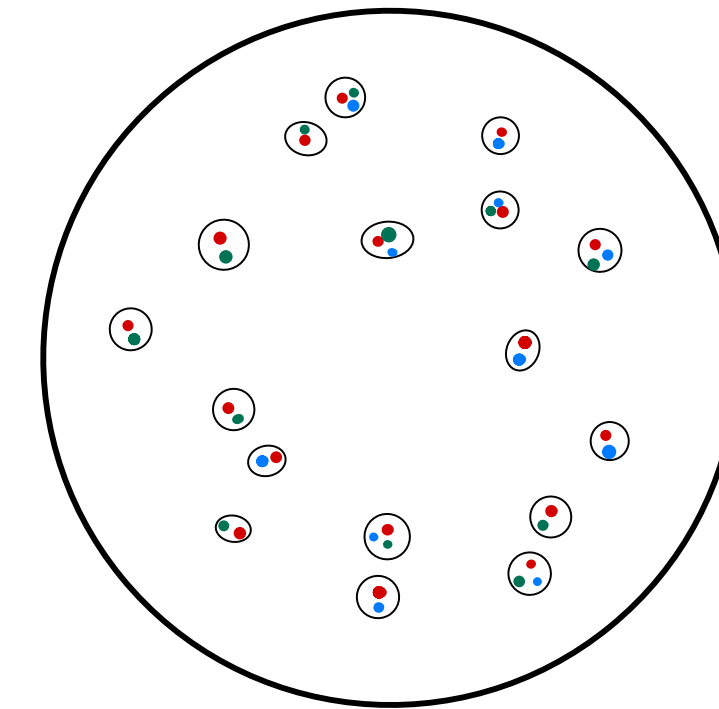
# Flavor separation and the jet electric charge

## A PARAMETRIZATION OF THE PROPERTIES OF QUARK JETS \*

R.D. FIELD and R.P. FEYNMAN

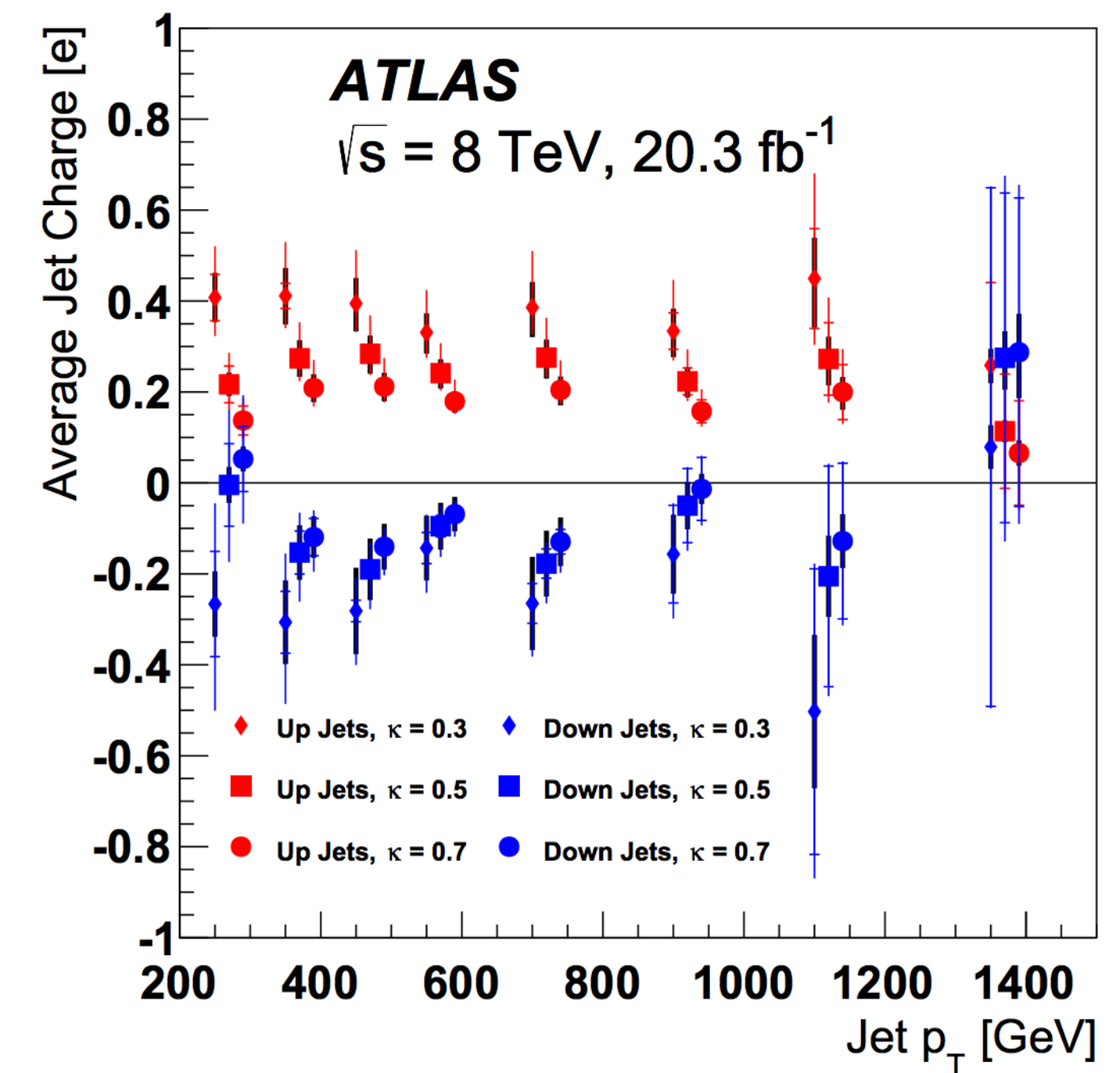
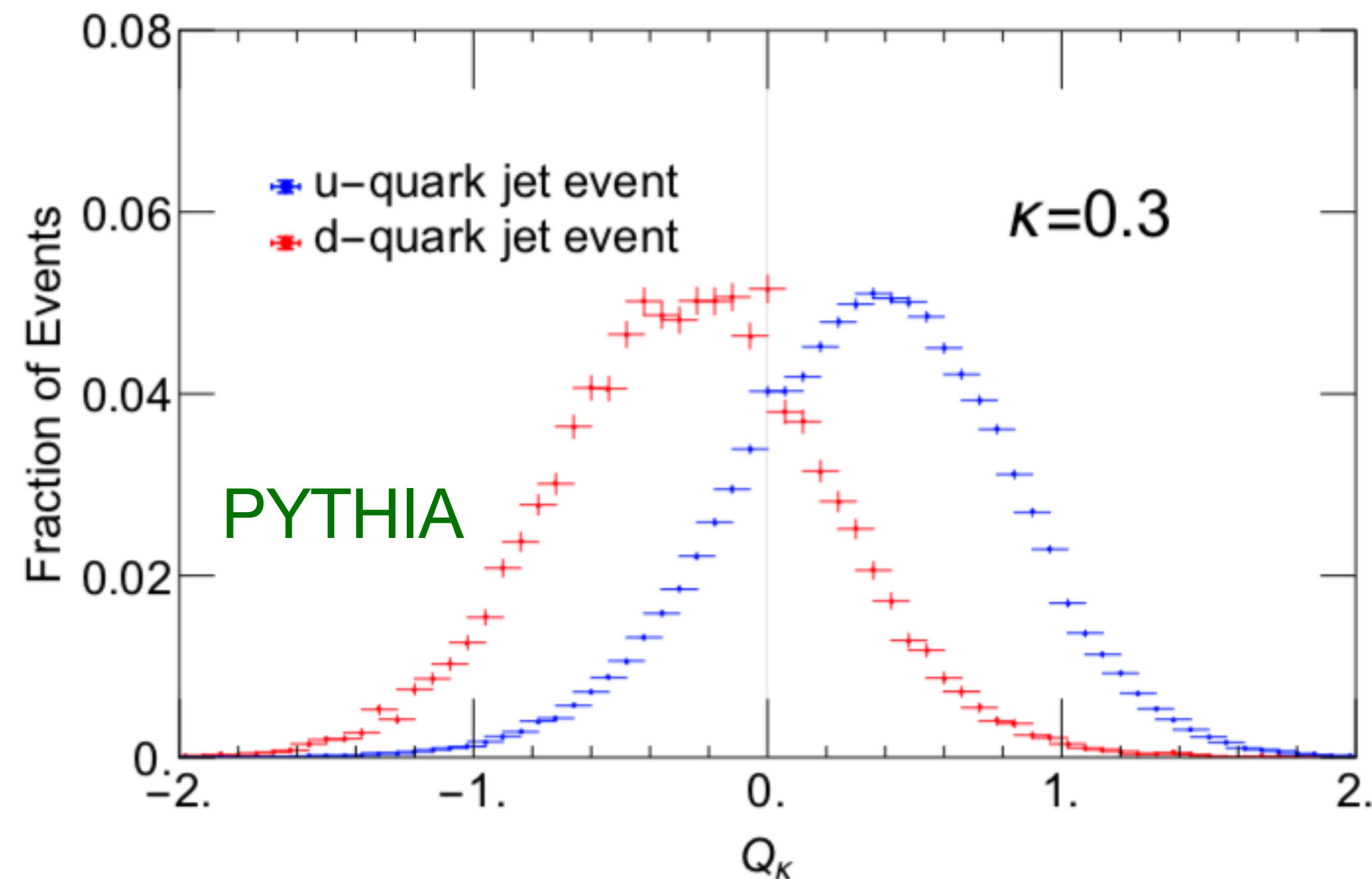
California Institute of Technology, Pasadena, California 91125, USA

Received 11 October 1977



Definition:

$$Q_\kappa = \sum_i \left( \frac{p_{i,T}}{p_J} \right)^\kappa Q_i$$



## Jet Charge: A Flavor Prism for Spin Asymmetries at the Electron-Ion Collider

Zhong-Bo Kang<sup>1,2,3,\*</sup>, Xiaohui Liu<sup>4,5,†</sup>, Sonny Mantry<sup>6,‡</sup> and Ding Yu Shao<sup>1,2,3,§</sup>

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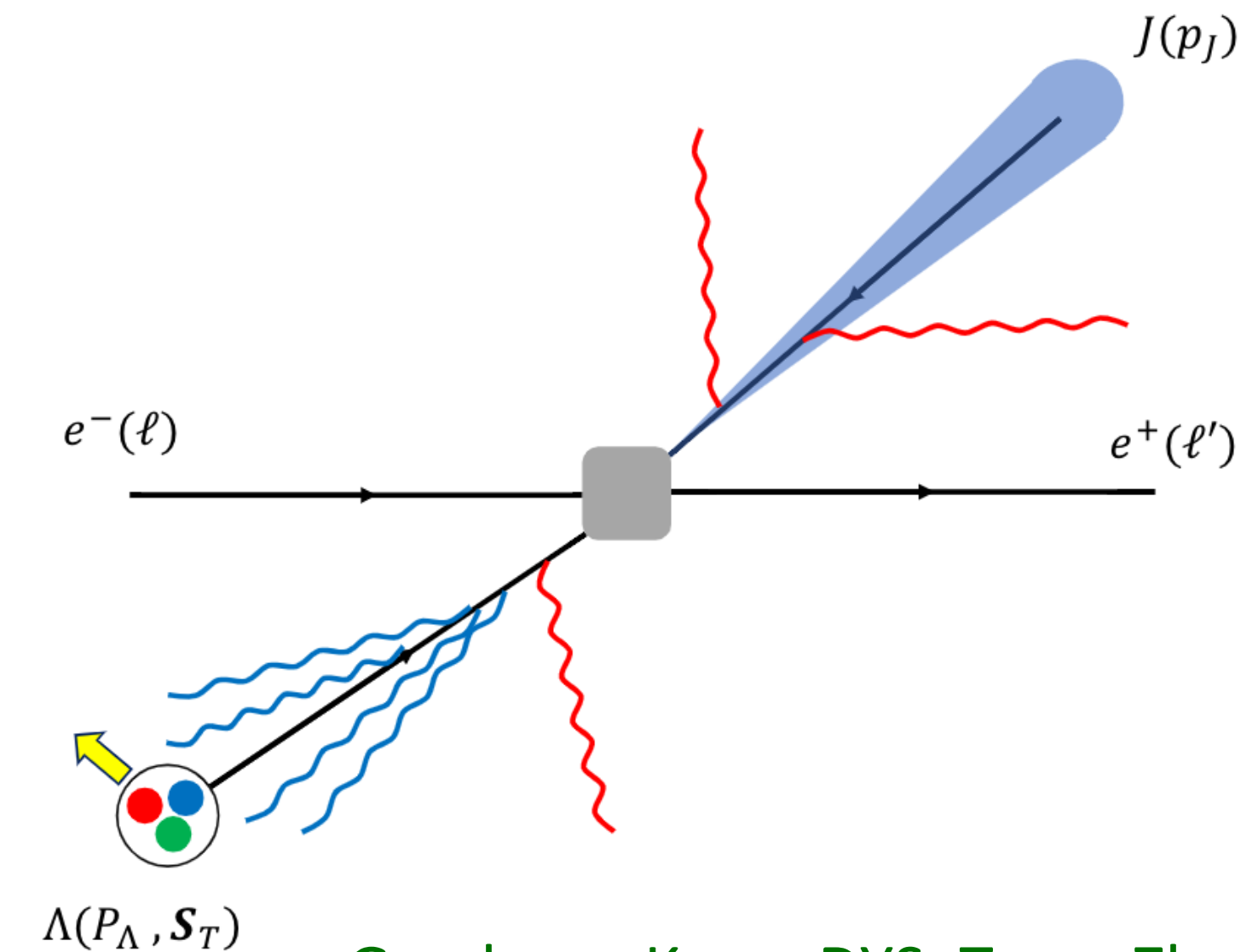
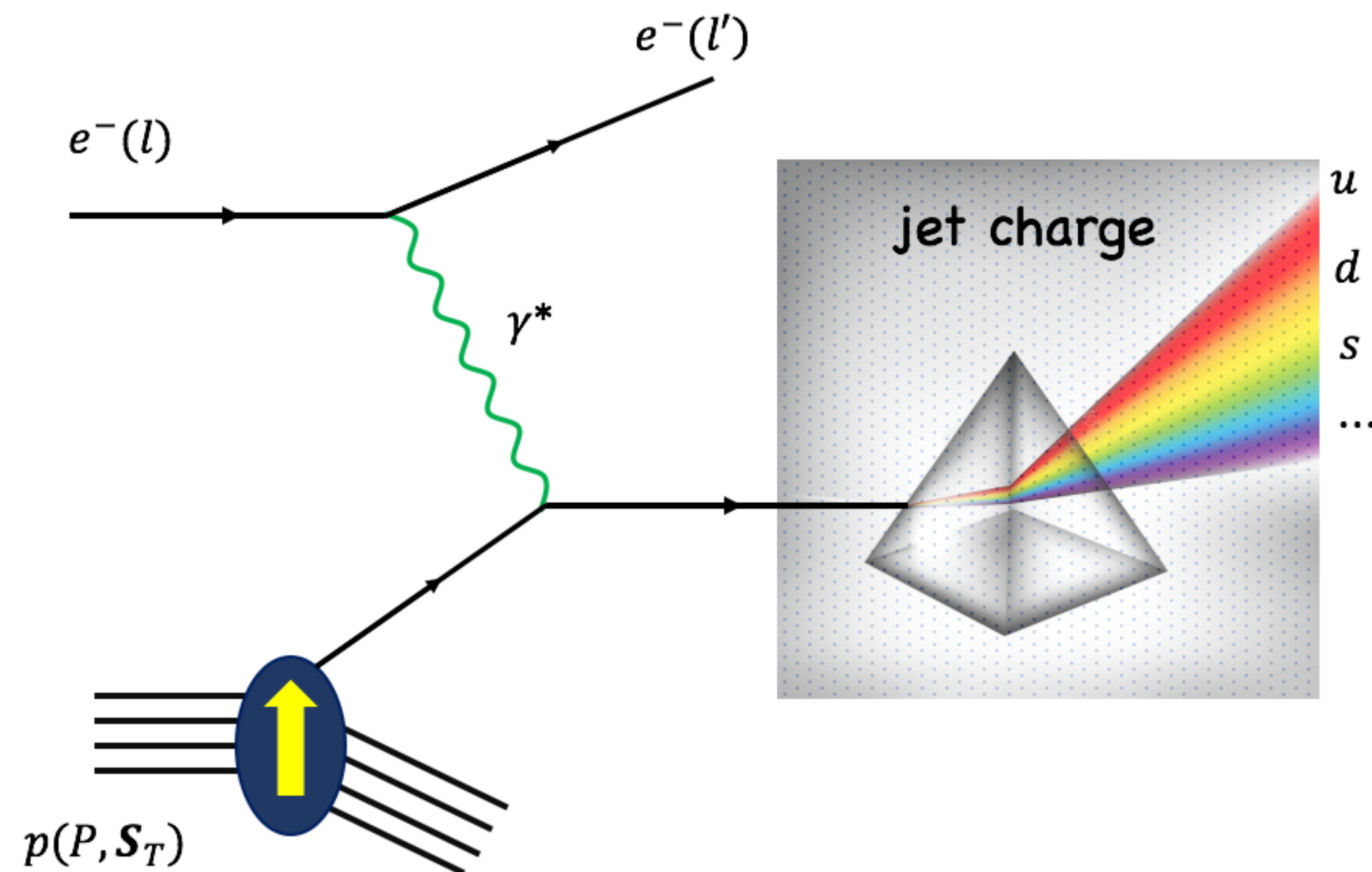
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 (Received 13 August 2020; revised 29 September 2020; accepted 5 November 2020; published 8 December 2020)



Gamberg, Kang, DYS, Terry, Zhao in progress

# Summary and Outlook

- We develop the theory framework to study transverse polarization effects for  $\Lambda(\text{thrust})$  production in  $e^+e^-$  collisions
  - EFT approach, model independent
  - TMD factorization formula, rapidity divergence is cancelled at two loop
  - Include QCD evolution (both linear and non-linear) from  $Q$  to  $j_T \gtrsim \Lambda_{\text{QCD}}$
  - Our predictions are consistent with Belle data
  - Verify the universality of polarizing fragmentation function
  - We propose to use jet charge to separate different flavors of PFFs at the Belle
- Jets and jet substructures can be calculated in pQCD, which offer new opportunity to understand hadron structures

**Thank you**

# Welcome to Fudan!!!

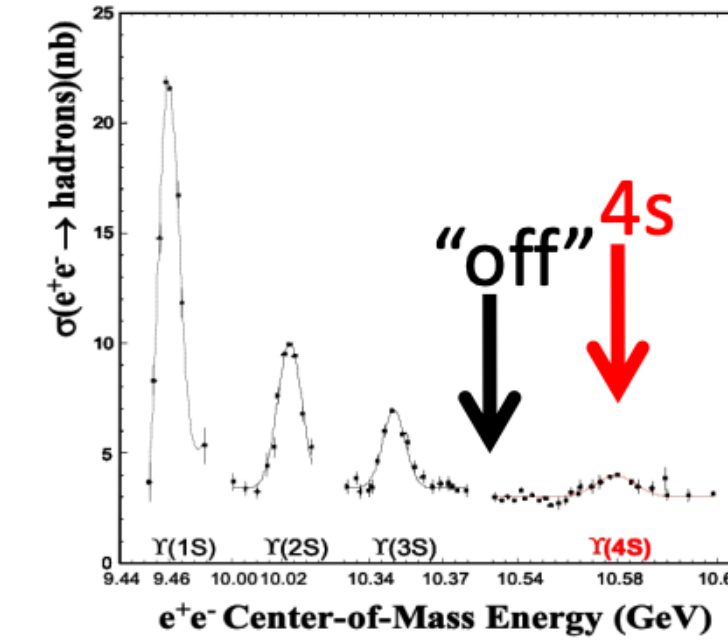
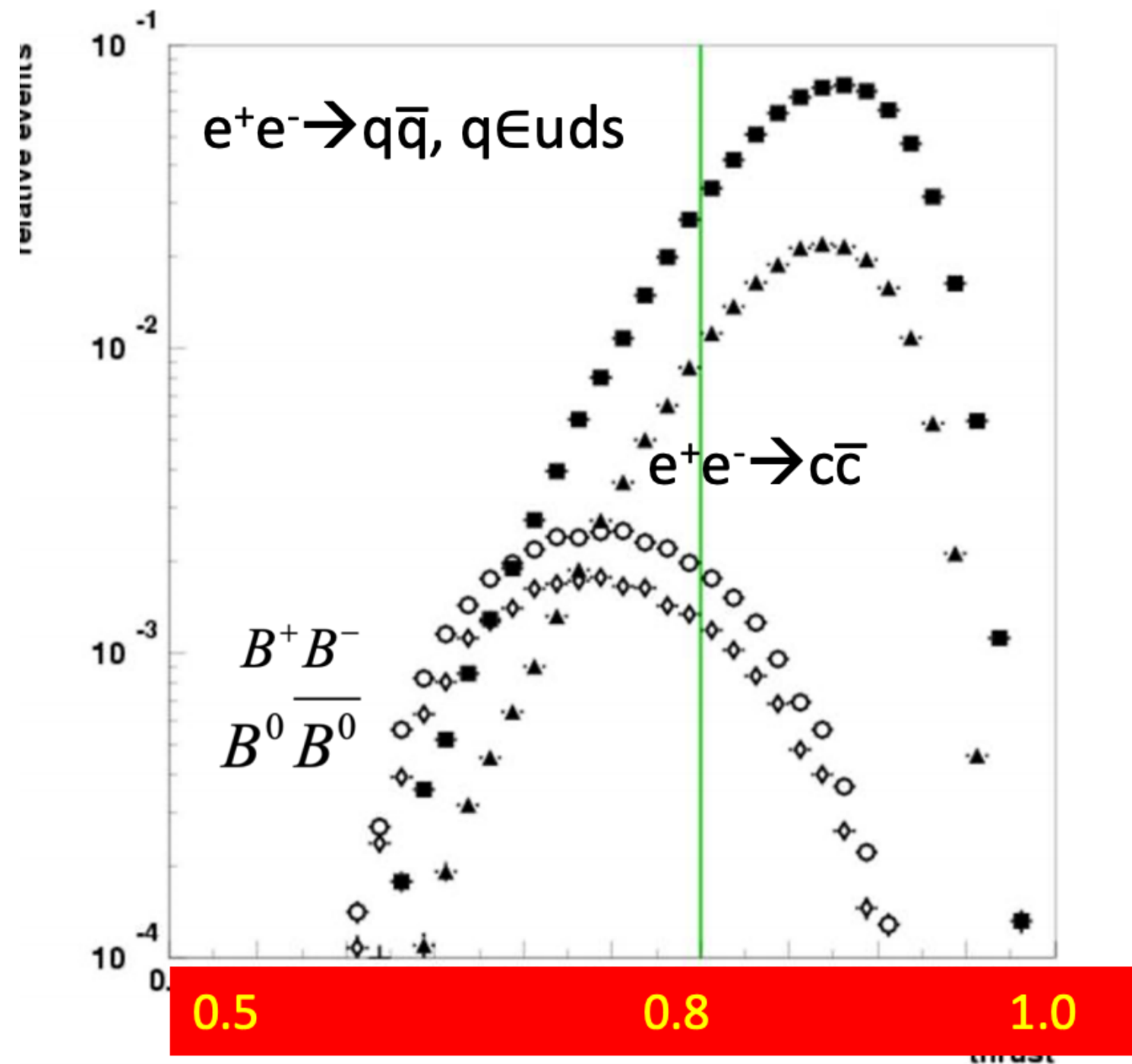


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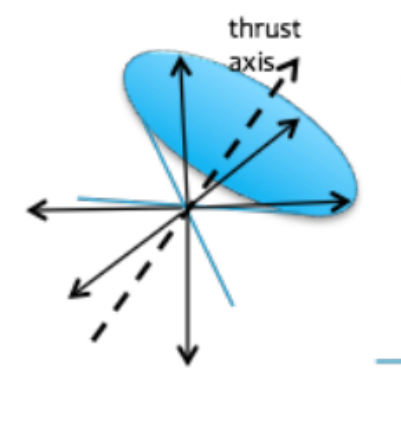
# Backup

# Lots of data off resonance, easy to remove resonance background

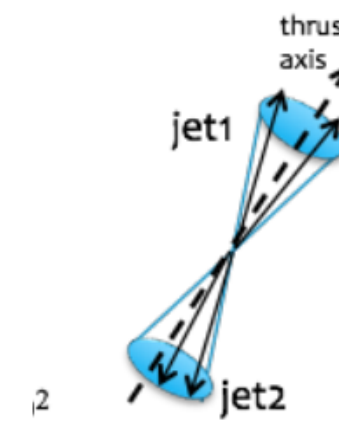


- small B contribution (<1%) in high thrust sample
- >75% of X-section continuum under  $\Upsilon$  (4S) resonance
- $\sim 100 \text{ fb}^{-1} \rightarrow \sim 1000 \text{ fb}^{-1}$

$$\text{Thrust: } T = \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$$



$T \sim 0.5$



$T \sim 1$

