



# Hidden-charm molecule with strangeness

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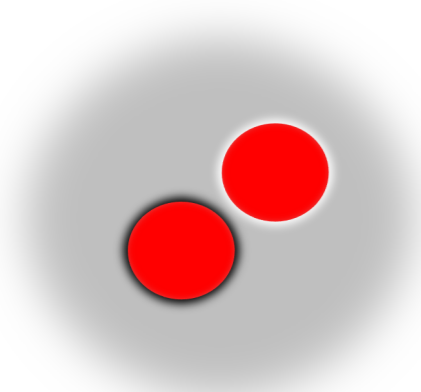
Based on arXiv: 2011.08725

In collaboration with Xu Cao, Feng-Kun Guo, Juan Nieves, Manuel Pavon Valderrama

第五届“强子谱和强子结构研讨会”，2021/1/24

- Hadron structure
- $Z_c$  family
- Molecular interpretation of  $Z_c(3900)$
- Line shape and pole position of  $Z_{cs}(3985)$
- Summary

## □ Conventional hadrons

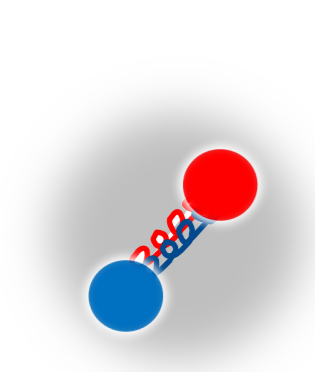


meson

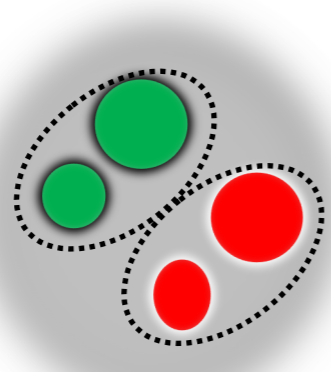


baryon

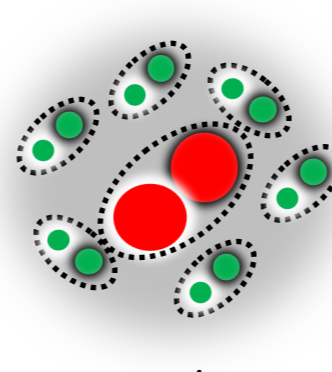
## □ Proposals for the heavy exotic hadrons



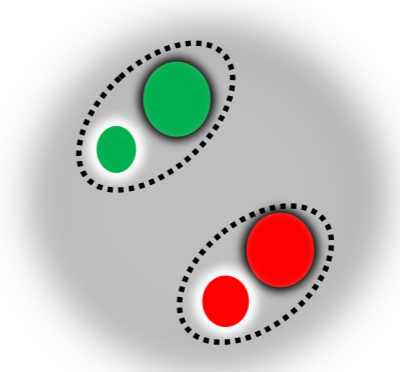
hybrid



Compact  
multiquark



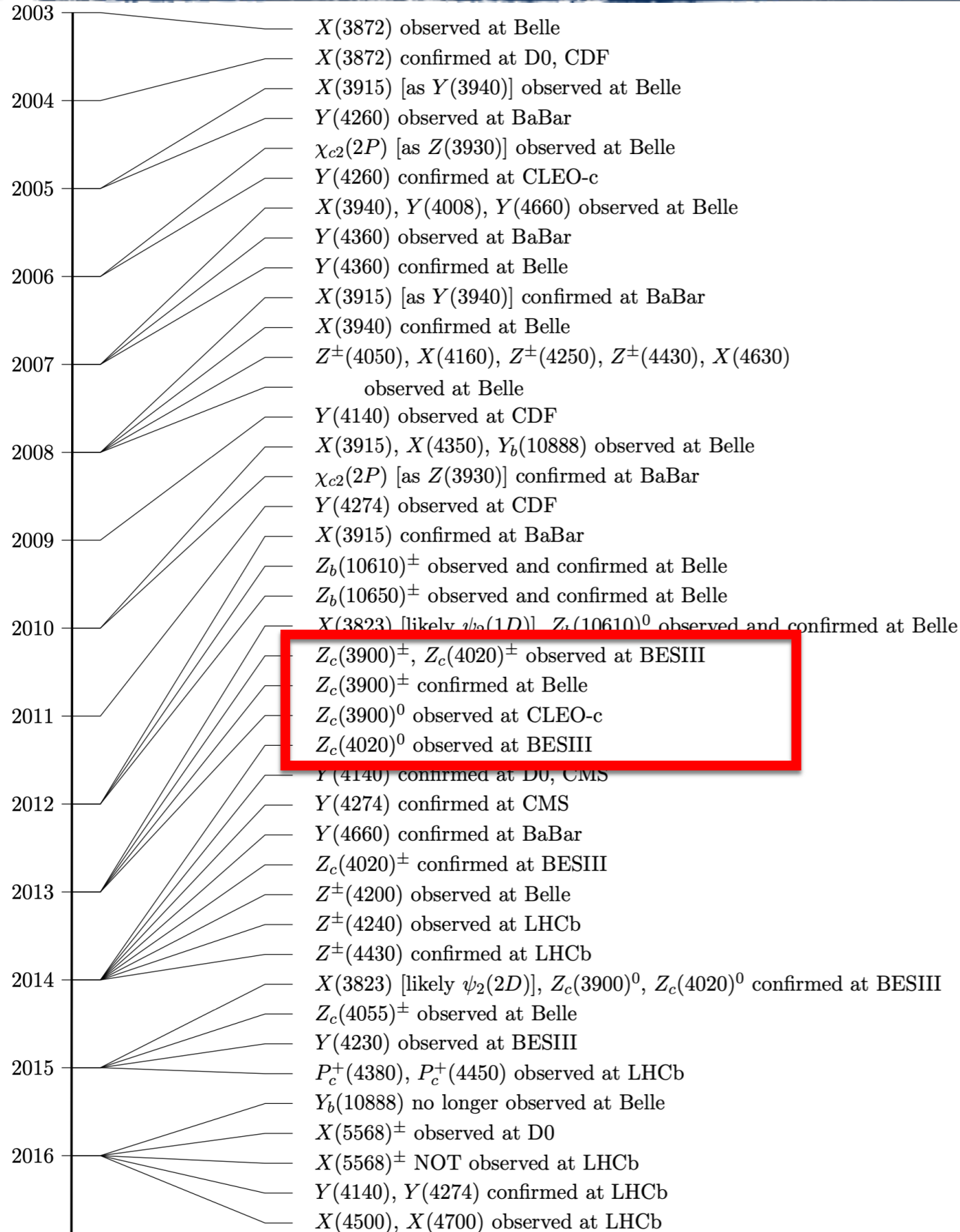
Hadro-  
Quarkonium



Hadronic  
molecule

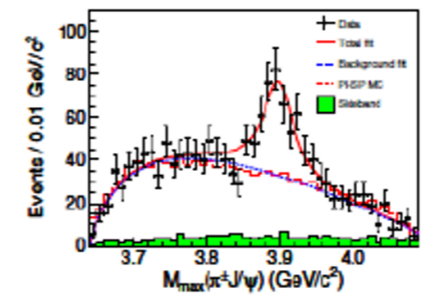
- Hadron structure is a platform to study the QCD in low energy region.
- Quark model classified the hadrons very well.
- However, many new hadrons can not fit into the conventional hadrons (mass and properties).

# Exotic hadrons in Zc family



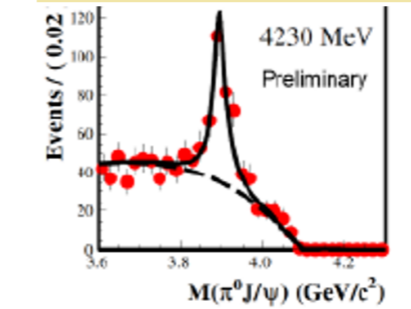
Lebed, Mitchell, Swanson, PPNP93(2017)143

$Z_c(3900)^+$   
PRL 110, 252001 (2013)



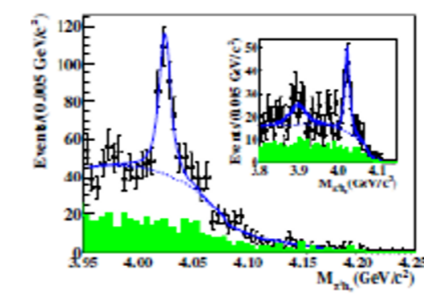
$$e^+e^- \rightarrow \pi^- \pi^+ J/\psi$$

$Z_c(3900)^0$   
PRL 115, 112003 (2015)



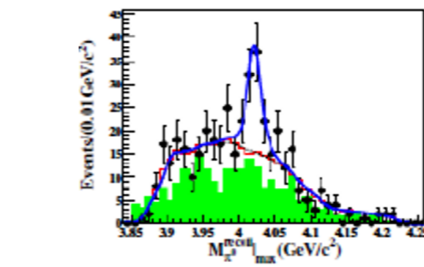
$$e^+e^- \rightarrow \pi^0 \pi^0 J/\psi$$

$Z_c(4020)^+$   
PRL 111, 242001(2013)



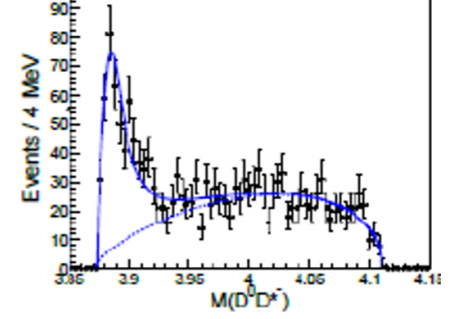
$$e^+e^- \rightarrow \pi^- \pi^+ h_c$$

$Z_c(4020)^0$   
PRL113,212002 (2014)



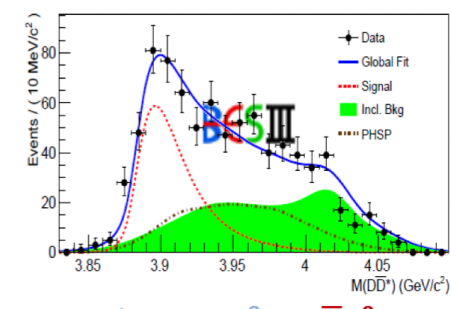
$$e^+e^- \rightarrow \pi^0 \pi^0 h_c$$

$Z_c(3885)^+$   
PRL 112, 022001(2014)



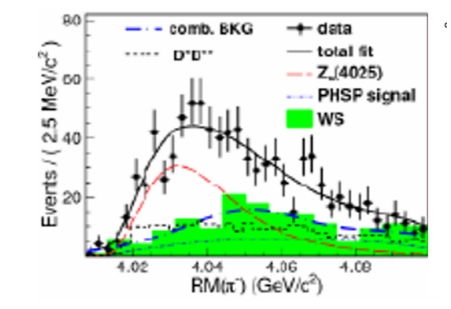
$$e^+e^- \rightarrow \pi^- (D\bar{D}^*)^+$$

$Z_c(3885)^0$   
PRL115, 222002 (2015)



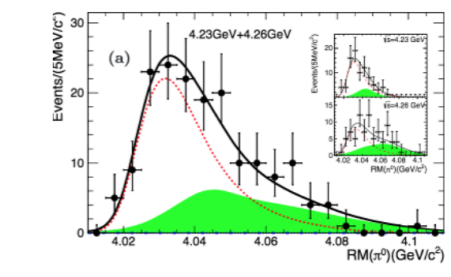
$$e^+e^- \rightarrow \pi^0 (D^* \bar{D})^0$$

$Z_c(4025)^+$   
PRL 112, 132001 (2014)



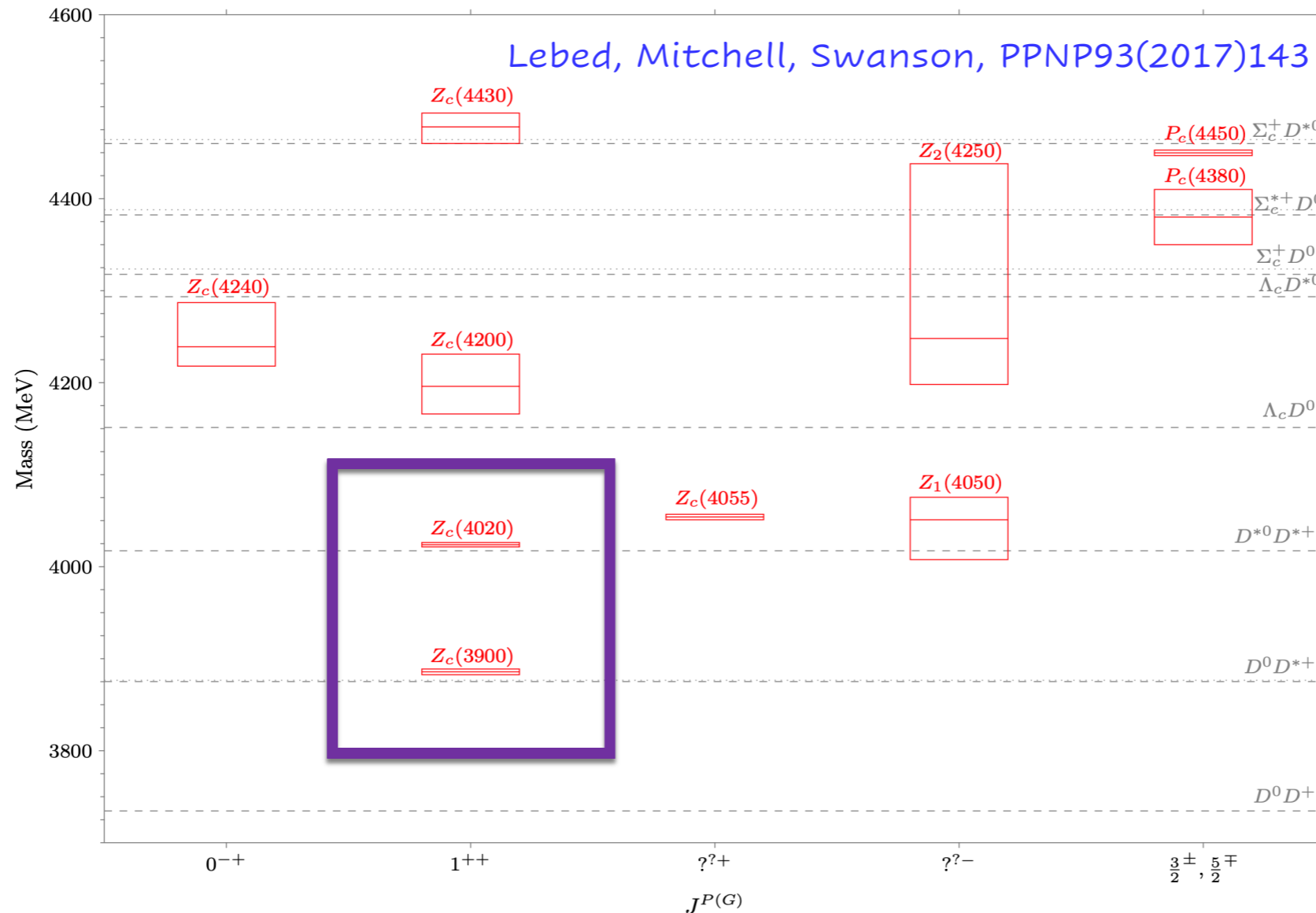
$$e^+e^- \rightarrow \pi^- (D^* \bar{D}^*)^+$$

$Z_c(4025)^0$   
PRL115, 182002 (2015)



$$e^+e^- \rightarrow \pi^0 (D^* \bar{D}^*)^0$$

# Exotic hadrons in $Z_c$ family



- $Z_c$  states were observed in the hidden- and open-charm channel;
- Unsuccessful searches for  $Z_c$ s by Belle and BES3 in the hidden channel.

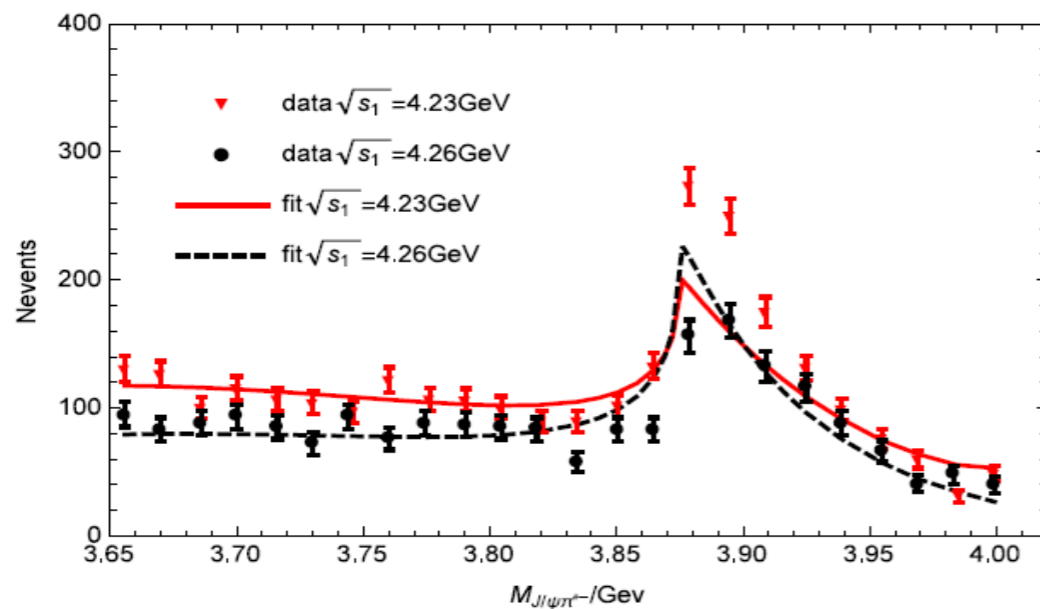
PRD77, 011105(2008); PRD89,072015(2014); PRD97, 071101(2018)

# Zc(3900): kinematical effect or molecular?

- The charged one was observed in  $J/\psi\pi^\pm$  mass distribution by BESIII and Belle.

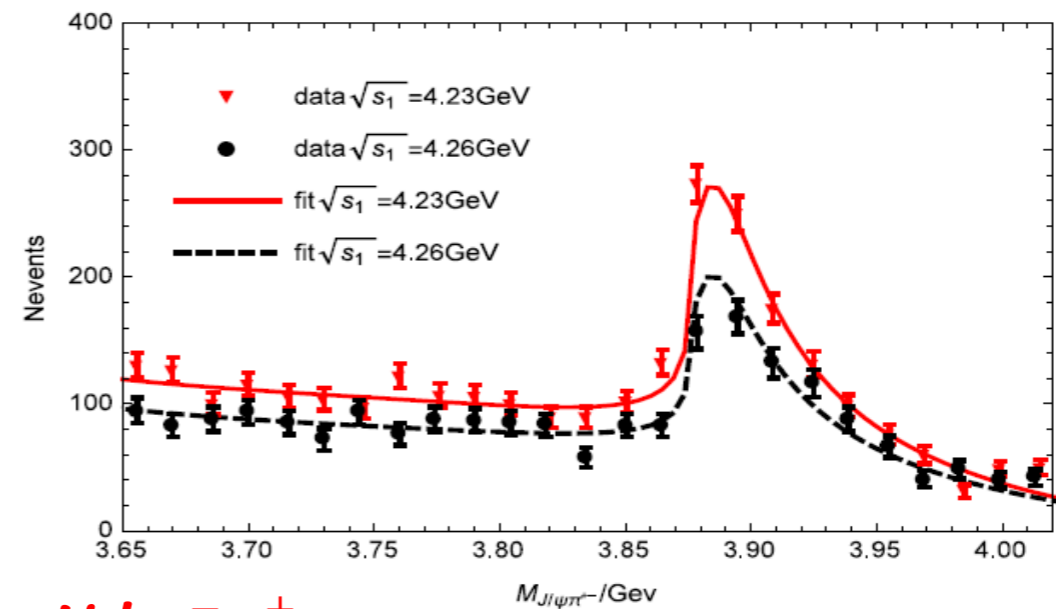
BESIII, PRL110(2013)252001; Belle, PRL110(2013)252002

- Must contain at least 4 quarks,  $c\bar{c}u\bar{d}$ , slightly above the  $D^*\bar{D}$  threshold, mainly  $D^*\bar{D}$  molecular? Or tetraquark, hybrid...?
- Kinematical cusp effect? In this scenario, it is not self consistent.  
Guo, Hanhart, Wang and Zhao, PRD91(2015)051504
- Hadronic molecule, not triangle singularity  
Gong, Pang, Wang and Zheng, EPJC78 (2018)276



(a)

Triangle singularity



(b)

Hadronic molecule

# Z<sub>c</sub>(3900): absence in B decay

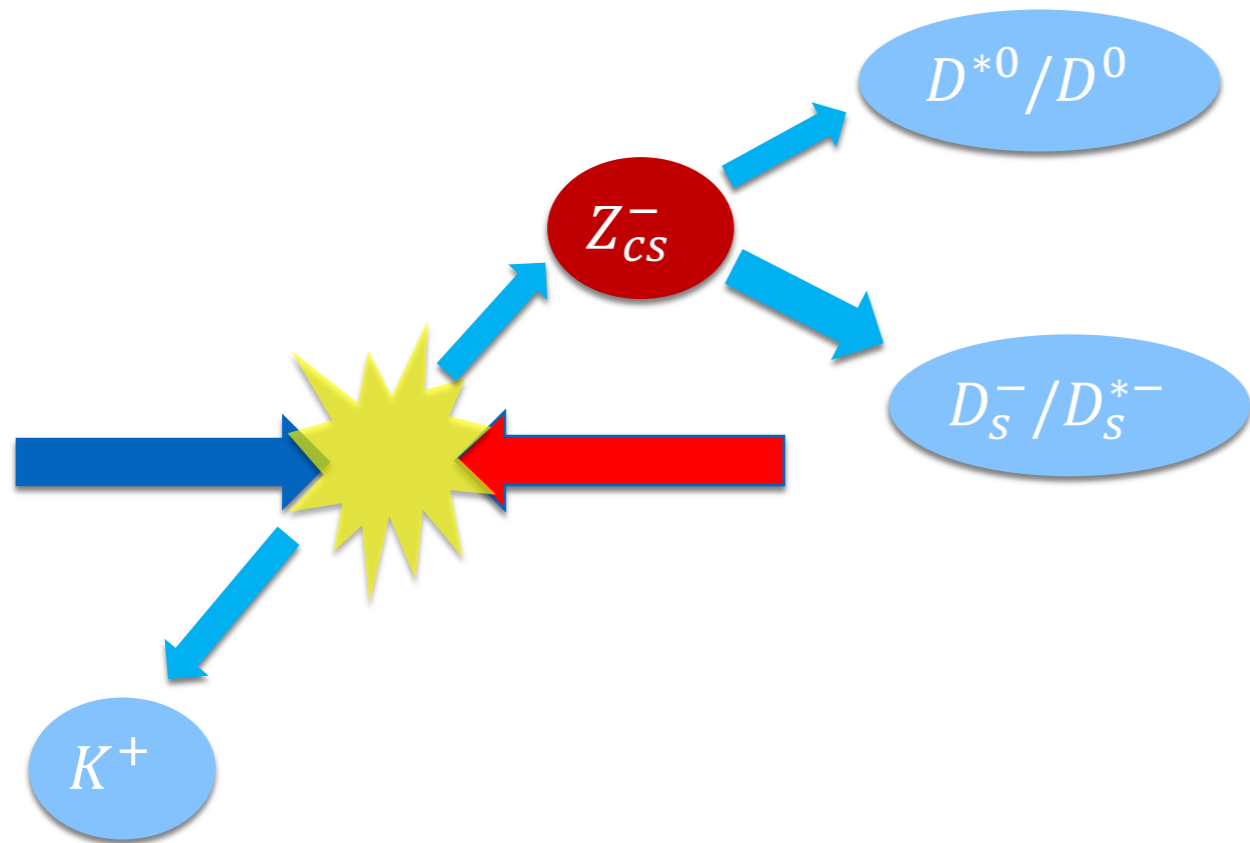
- The Z<sub>c</sub>(3900) was found through  $e^+e^- \rightarrow J/\psi\pi\pi$  and  $D^*\bar{D}\pi$ .
- However, it was not found in the  $B \rightarrow KZ_c(Z_c \rightarrow J/\psi\pi)$  decay. Instead, the Z<sub>c</sub>(4200) and Z<sub>c</sub>(4430) were found.

Belle, PRD90(2014)112009

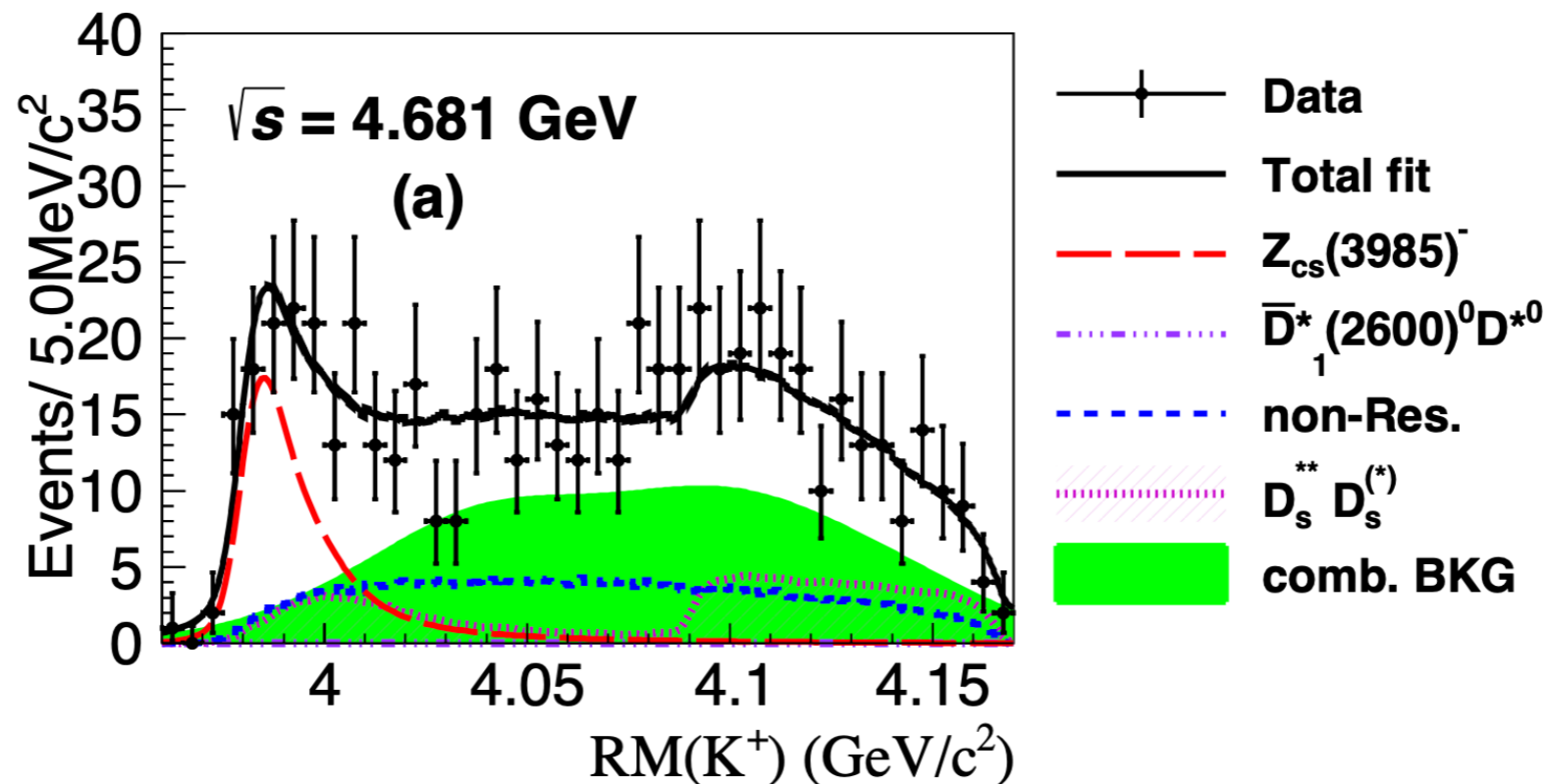
- The absence may have something to do with its internal structure.
- Under the hadronic molecular picture, both X(3872) and Z<sub>c</sub>(3900) have  $D^*\bar{D}$  constituent. The isospin of the Z<sub>c</sub>(3900) is 1, while for the X(3872) is 0.
- The production of the  $D^*\bar{D}$  pair with isospin 1 is highly suppressed in B decays.
  - The Z<sub>c</sub>(3900) being a  $D^*\bar{D}$  hadronic molecule naturally explains its absence in the B decays.

Yang, Wang and Meissner, PLB775(2017)50

# Zcs signal in $e^+e^- \rightarrow K^+(D_s^-D^{*0} + D_s^{*-}D^0)$



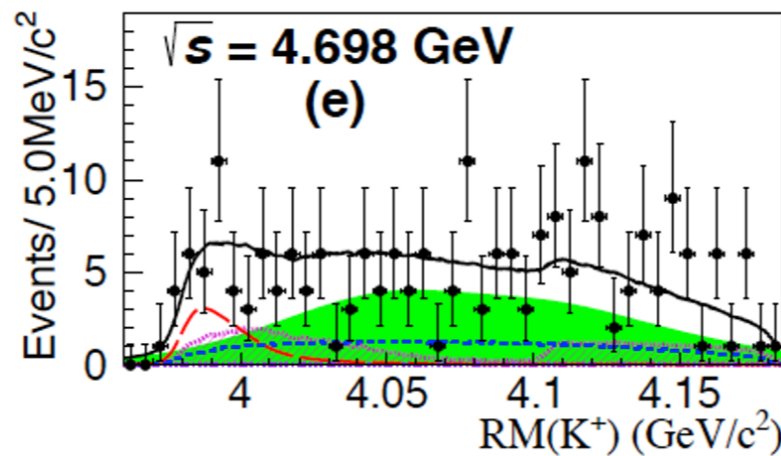
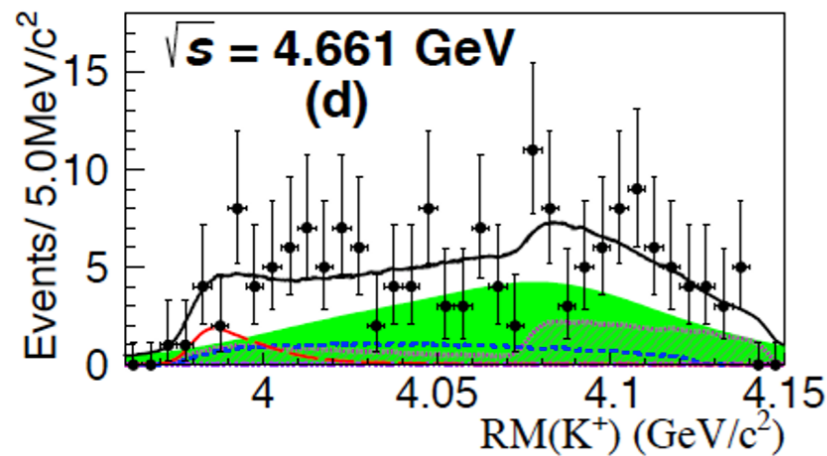
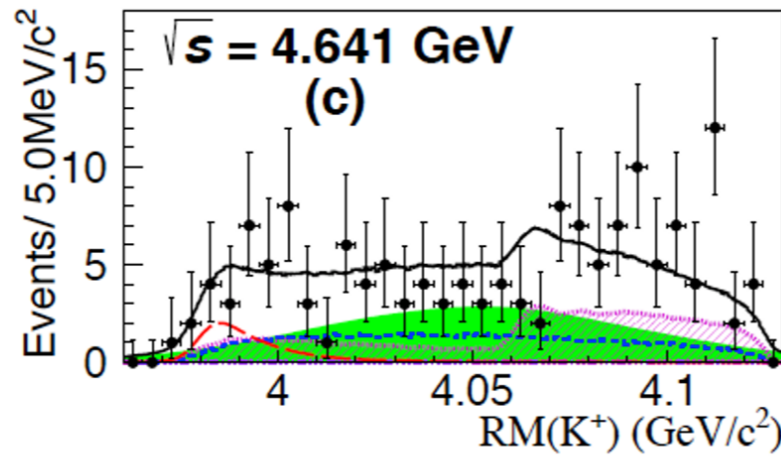
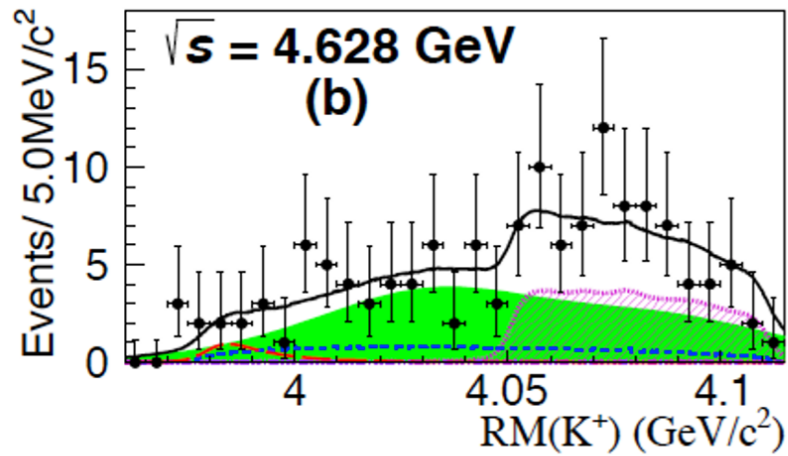
- The recoil mass distribution was studied by BES3;
- A clear peak was found at energy point 4.681GeV;
- Search at other 4 energies was also performed.





# Zcs signal in $e^+e^- \rightarrow K^+(D_s^-D^{*0} + D_s^{*-}D^0)$

➤ The Zcs structure was also observed in other four energy points.



$\sqrt{s}$ (GeV)	$\mathcal{L}_{\text{int}}$ ( $\text{pb}^{-1}$ )
4.628	511.1
4.641	541.4
4.661	523.6
4.681	1643.4
4.698	526.2

arXiv: 2011.07855

➤ There exists one particle in the energy range:

$$\psi(4660) \quad I^G(J^{PC}) = 0^-(1^{--})$$

$\psi(4660)$  MASS

$4633 \pm 7 \text{ MeV} (S = 1.4)$

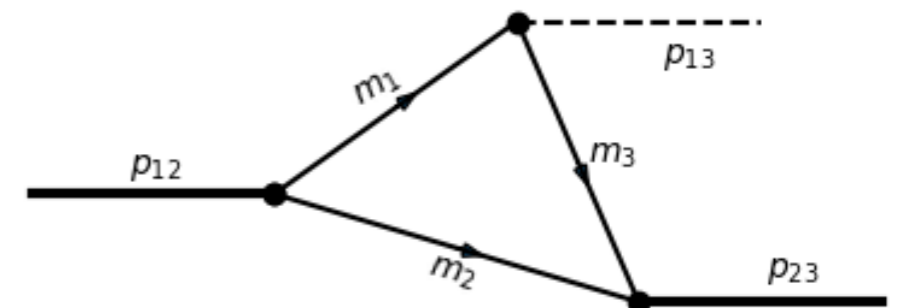
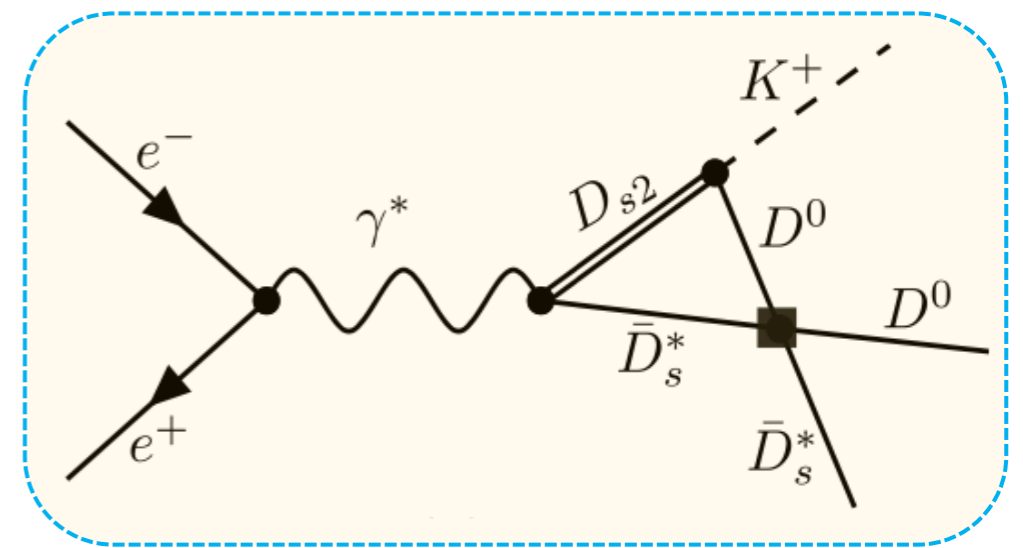
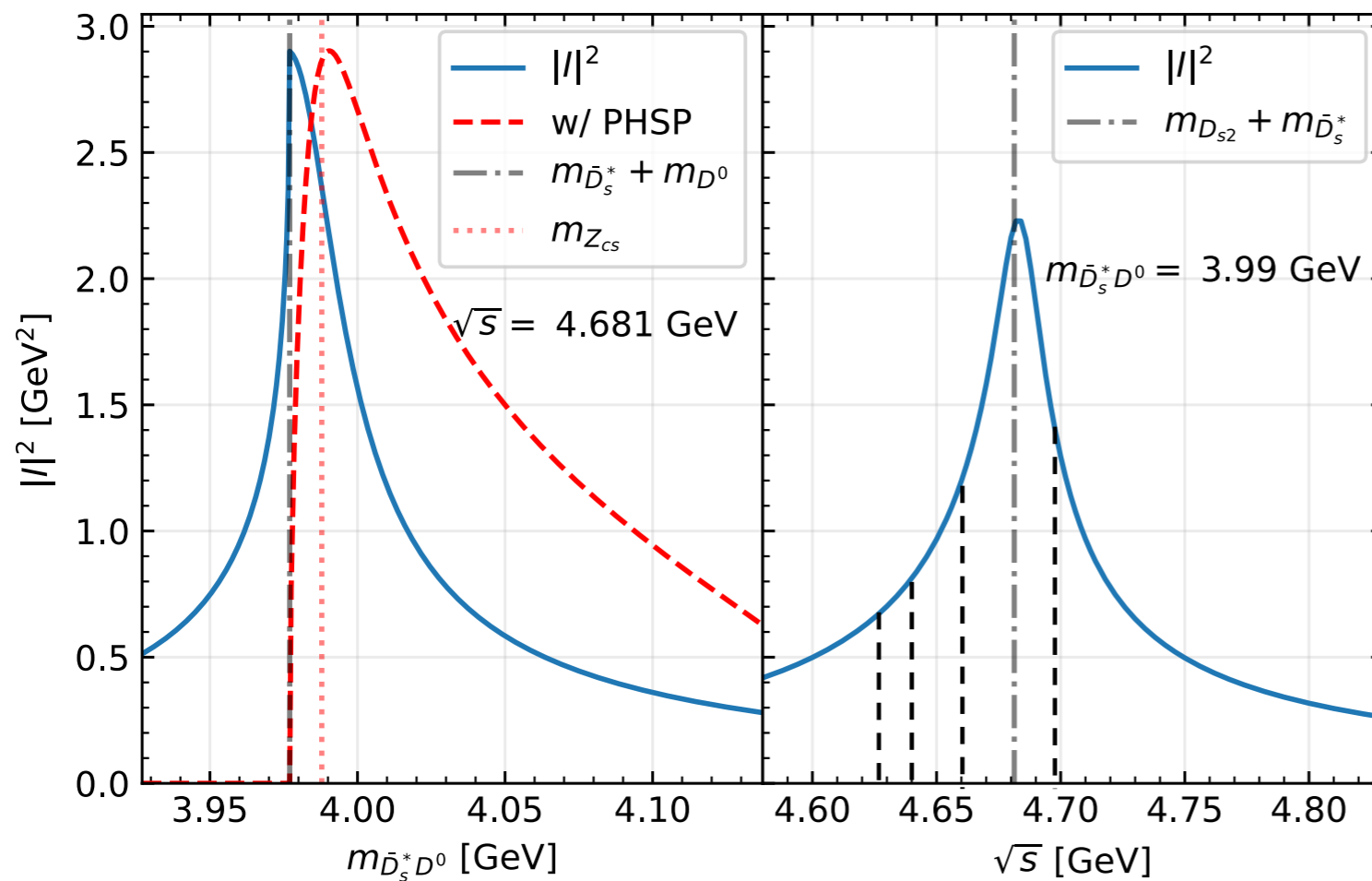
$\psi(4660)$  WIDTH

$64 \pm 9 \text{ MeV}$

# Triangle singularity in $Z_{cs}$ production

- There is such triangle diagram which appears as peak around threshold at c.m. energy 4.681 GeV;
- It can enhance the production of near-threshold hadronic molecules.

Guo, Liu and Sakai, PPNP112,103757; Guo, Hanhart, Meissner, Wang, Zhao and Zou, RMP90,015004



$$= I(m_1, m_2, m_3, p_{13}, p_{12}, p_{23})$$

Energy points: [4.628, 4.641, 4.661, 4.681, 4.698] GeV

# Zcs in $e^+e^- \rightarrow K^+(D_s^- D^{*0} + D_s^{*-} D^0)$

- Constant-contant EFT:  
(for virtual/bound state)

$$V_{\text{virtual}}^{(O)} = C^{(O)}$$

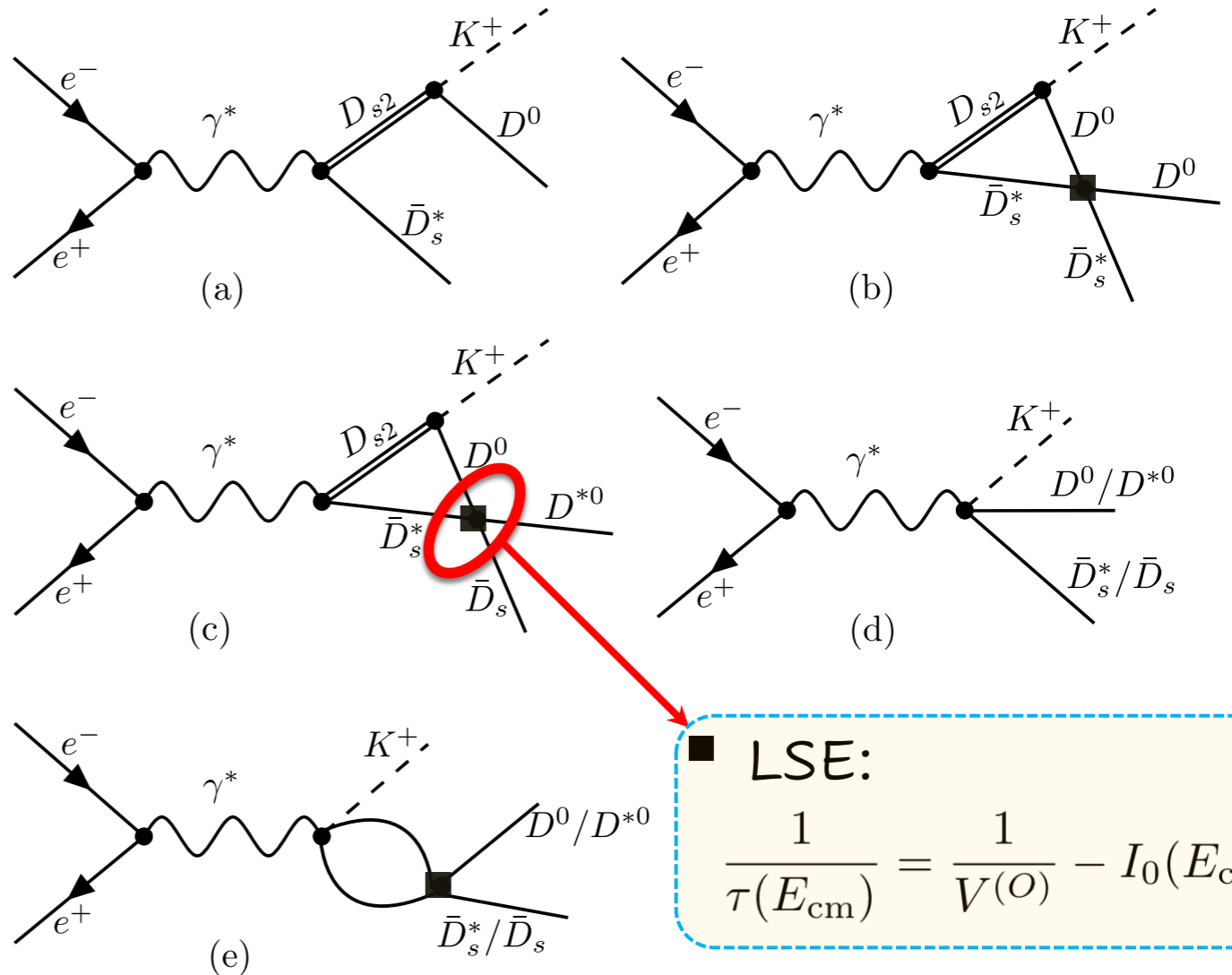
- Resonance EFT:

$$V_{\text{res}}^{(O)} = C^{(O)} + 2D^{(O)} k^2$$

Other fit parameters:

- N: overall constant (e+e- vertex);
- r: relative weight between diagrams (d,e) and diagrams (a,b,c);

$$\frac{dN}{dm_{23}} = \frac{d\sigma}{dm_{23}} \mathcal{L}_{\text{int}} \bar{\epsilon} f_{\text{corr}}$$



■ LSE:

$$\frac{1}{\tau(E_{\text{cm}})} = \frac{1}{V^{(O)}} - I_0(E_{\text{cm}}; \Lambda)$$

$\sqrt{s}$ (GeV)	$\mathcal{L}_{\text{int}}$ (pb <sup>-1</sup> )	$n_{\text{sig}}$	$f_{\text{corr}} \bar{\epsilon}$ (%)	$\sigma^B \cdot \mathcal{B}$ (pb)
4.628	511.1	$4.2^{+6.1}_{-4.2}$	1.03	$0.8^{+1.2}_{-0.8} \pm 0.6 (< 3.0)$
4.641	541.4	$9.3^{+7.3}_{-6.2}$	1.09	$1.6^{+1.2}_{-1.1} \pm 1.3 (< 4.4)$
4.661	523.6	$10.6^{+8.9}_{-7.4}$	1.28	$1.6^{+1.3}_{-1.1} \pm 0.8 (< 4.0)$
4.681	1643.4	$85.2^{+17.6}_{-15.6}$	1.18	$4.4^{+0.9}_{-0.8} \pm 1.4$
4.698	526.2	$17.8^{+8.1}_{-7.2}$	1.42	$2.4^{+1.1}_{-1.0} \pm 1.2 (< 4.7)$

# Fits of Zcs line shapes

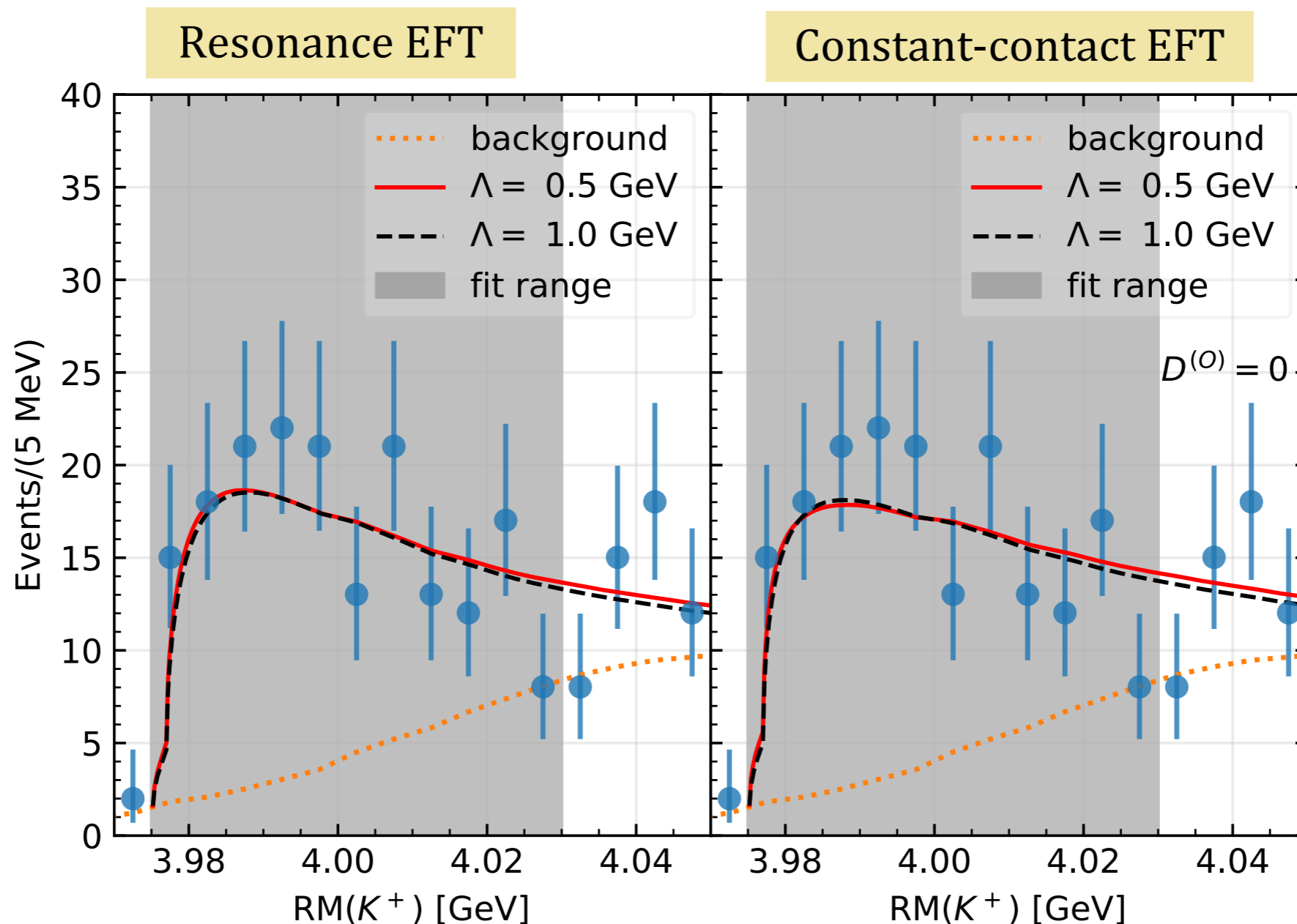
- Constant-contact EFT:  
(for virtual/bound state)

$$V_{\text{virtual}}^{(0)} = C^{(0)}$$

- Resonance EFT:

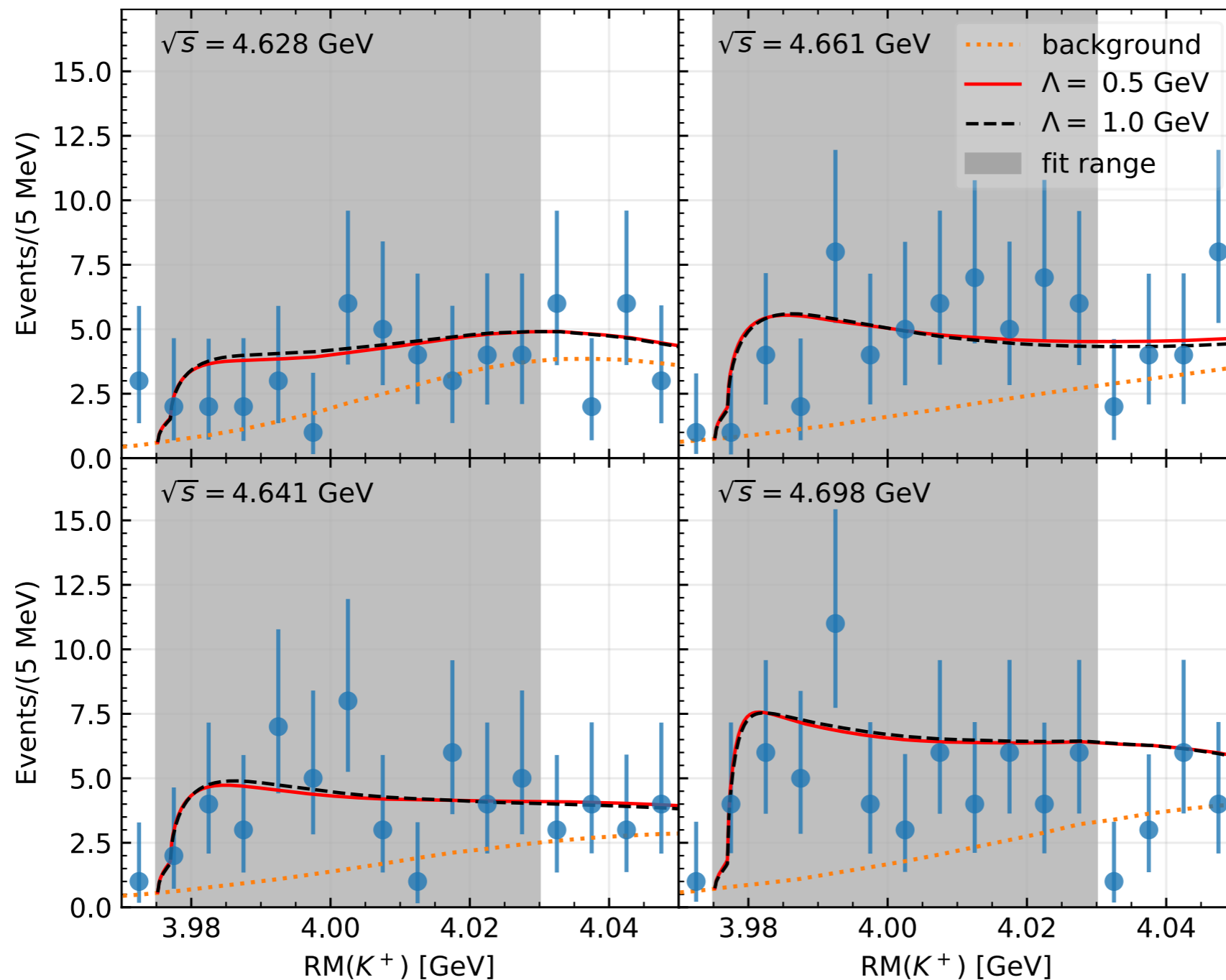
$$V_{\text{res}}^{(0)} = C^{(0)} + 2D^{(0)} k^2$$

Energy points: 4.681 GeV



# Fits of Zcs line shapes

- The fits are quite well,  $\chi^2/dof \approx 0.6$  for both cases.



Resonance EFT

Energy points: [4.628, 4.641, 4.661, 4.698] GeV

- The LECs in fitting Zcs line shapes:  
for constant-contact EFT:

$$C^{(O)}(\Lambda) = -0.77_{-0.10}^{+0.12} \left( -0.45_{-0.04}^{+0.05} \right) \text{ fm}^2,$$

for resonant EFT:

$$C^{(O)}(\Lambda) = -0.72_{-0.13}^{+0.18} \left( -0.44_{-0.05}^{+0.06} \right) \text{ fm}^2,$$

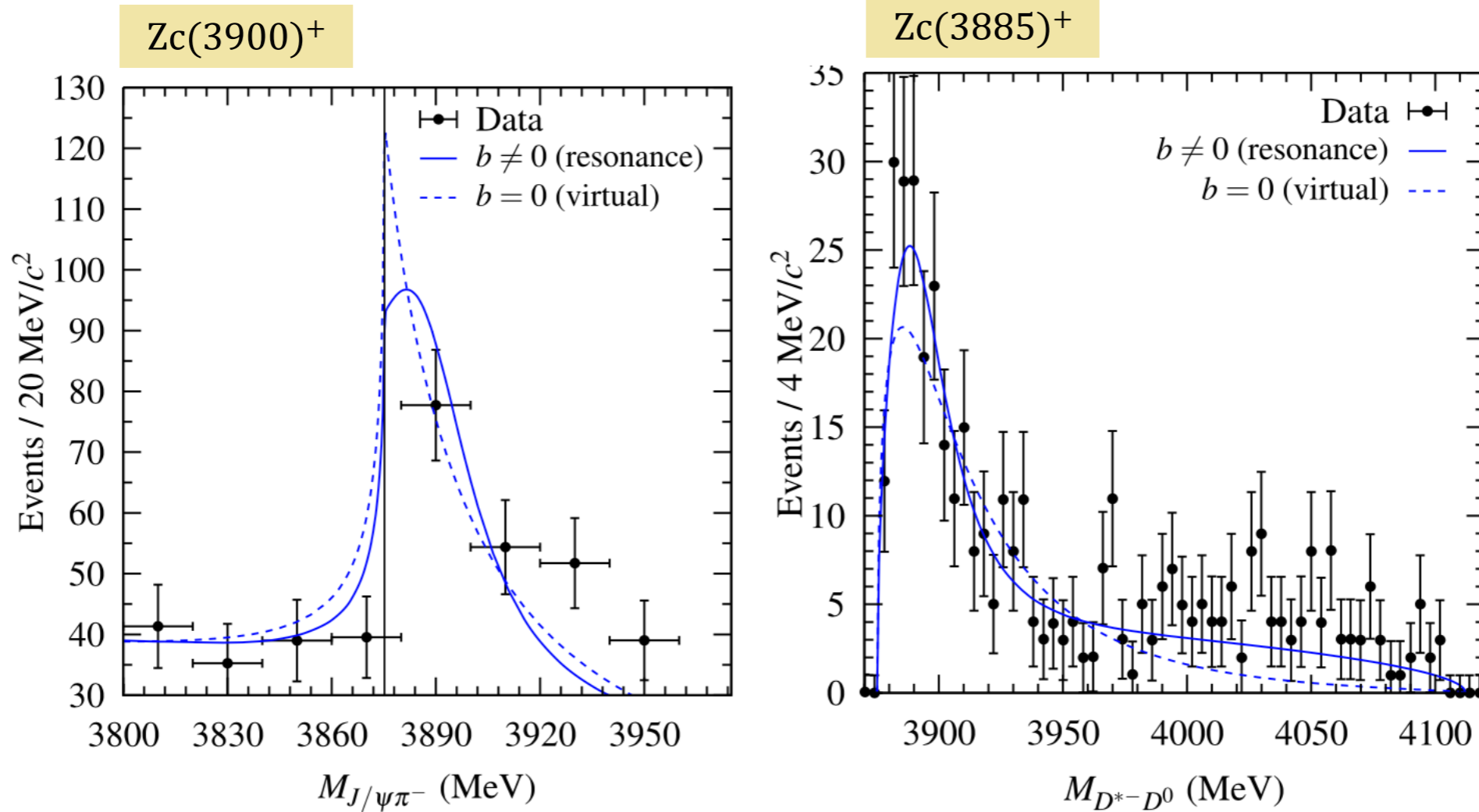
$$D^{(O)}(\Lambda) = -0.17_{-0.21}^{+0.21} \left( -0.025_{-0.049}^{+0.066} \right) \text{ fm}^4,$$

Potential	States	Thresholds	Masses ( $\Lambda = 0.5$ GeV)	Masses ( $\Lambda = 1$ GeV)	Experiment
$V_{\text{virtual}}^{(O)}$	$\frac{1}{\sqrt{2}}(D\bar{D}^* - D^*\bar{D})$	3875.8	$3871_{-3}^{+2}$	$3867_{-7}^{+4}$	$3884.4 \pm 2.5$ [11]
	$D^*\bar{D}^*$	4017.2	$4014_{-3}^{+2}$	$4012_{-6}^{+3}$	$4024.1 \pm 1.9$ [11]
	$D\bar{D}_s^* - D^*\bar{D}_s$	3979.4, 3976.9	$3974_{-3}^{+2}$	$3971_{-6}^{+3}$	
	$D^*\bar{D}_s^*$	4120.8	$4117_{-5}^{+3}$	$4115_{-6}^{+3}$	
Potential	States	Thresholds	Masses ( $\Lambda = 0.5$ GeV)	Masses ( $\Lambda = 1$ GeV)	Experiment
$V_{\text{res}}^{(O)}$	$\frac{1}{\sqrt{2}}(D\bar{D}^* - D^*\bar{D})$	3875.8	$3861_{-0}^{+20} - i6_{-6}^{+14}$ (R/V)	$3861_{-35}^{+16} - i0_{-0}^{+29}$ (R/V)	$3884.4 \pm 2.5$ [11]
	$D^*\bar{D}^*$	4017.2	$4004_{-0}^{+18} - i0_{-0}^{+20}$ (R/V)	$4006_{-37}^{+10} - i0_{-0}^{+28}$ (R/V)	$4024.1 \pm 1.9$ [11]
	$D\bar{D}_s^* - D^*\bar{D}_s$	3979.4, 3976.9	$3963_{-0}^{+20} - i3_{-3}^{+16}$ (R/V)	$3966_{-36}^{+12} - i0_{-0}^{+20}$ (R/V)	$3982.5_{-3.3}^{+2.8} - i25.6_{-10.6}^{+12.1}$ [4]
	$D^*\bar{D}_s^*$	4120.8	$4110_{-0}^{+14} - i0_{-0}^{+19}$ (R/V)	$4111_{-25}^{+9} - i0_{-0}^{+15}$ (R/V)	

# Zc(3900): line shape in $J/\psi\pi$ and $D^{*-}D^0$ channels



Albaladejo, Guo, Hidalgo and Nieves, PLB755,337(2016)



$M_{Z_c}$ (MeV)	$\Gamma_{Z_c}/2$ (MeV)	Ref.	Final state
$3894 \pm 6 \pm 1$	$30 \pm 12 \pm 6$	$\Lambda_2 = 1.0$ GeV	$J/\psi \pi, \bar{D}^* D$
$3886 \pm 4 \pm 1$	$22 \pm 6 \pm 4$	$\Lambda_2 = 0.5$ GeV	$J/\psi \pi, \bar{D}^* D$
$3831 \pm 26^{+7}_{-28}$	virtual state	$\Lambda_2 = 1.0$ GeV	$J/\psi \pi, \bar{D}^* D$
$3844 \pm 19^{+12}_{-21}$	virtual state	$\Lambda_2 = 0.5$ GeV	$J/\psi \pi, \bar{D}^* D$

# LECs and Poles from Zc(3900) case



- The LECs in reproducing the pole position of Zc(3900):  
for constant-contact EFT:

$$C^{(O)}(\Lambda) = -0.29_{-0.32}^{+0.15} \left( -0.28_{-0.39}^{+0.08} \right) \text{ fm}^2 ,$$

for resonant EFT:

$$C^{(O)}(\Lambda) = -0.06_{-0.16}^{+0.24} \left( -0.22_{-0.06}^{+0.10} \right) \text{ fm}^2 ,$$

$$D^{(O)}(\Lambda) = -0.31_{-0.17}^{+0.10} \left( -0.09_{-0.07}^{+0.03} \right) \text{ fm}^4 .$$

Potential	States	Thresholds	Masses ( $\Lambda = 0.5$ GeV)	Masses ( $\Lambda = 1$ GeV)	Experiment
$V_{\text{virtual}}^{(O)}$	$\frac{1}{\sqrt{2}}(D\bar{D}^* - D^*\bar{D})$	3875.8	Input [19]	Input [19]	$3888.4 \pm 2.5$ [11]
	$D^*\bar{D}^*$	4017.2	$3988_{-27}^{+21}$	$3978_{-36}^{+25}$	$4024.1 \pm 1.9$ [11]
	$D\bar{D}_s^*/D^*\bar{D}_s$	3979.4/3976.9	$3948_{-27}^{+22}$	$3937_{-36}^{+25}$	
	$D^*\bar{D}_s^*$	4120.8	$4092_{-26}^{+21}$	$4083_{-35}^{+24}$	
Potential	States	Thresholds	Masses ( $\Lambda = 0.5$ GeV)	Masses ( $\Lambda = 1$ GeV)	Experiment
$V_{\text{res}}^{(O)}$	$\frac{1}{\sqrt{2}}(D\bar{D}^* - D^*\bar{D})$	3875.8	Input [19]	Input [19]	$3888.4 \pm 2.5$ [11]
	$D^*\bar{D}^*$	4017.2	$4025 \pm 4 - i(21 \pm 7)$	$4035 \pm 6 - i(29 \pm 13)$	$4024.1 \pm 1.9$ [11]
	$D\bar{D}_s^*/D^*\bar{D}_s$	3979.4/3976.9	$3986 \pm 4 - i(22 \pm 7)$	$3996 \pm 6 - i(30 \pm 13)$	$3982.5_{-3.3}^{+2.8} - i25.6_{-10.6}^{+12.1}$ [4]
	$D^*\bar{D}_s^*$	4120.8	$4129 \pm 4 - i(21 \pm 7)$	$4138 \pm 6 - i(28 \pm 12)$	



- Two EFTs correspond to two origins: virtual/bound and resonance states. Both can fit the line shapes very well.
- Triangle singularity plays an important role.
- $Z_c$  and  $Z_{cs}$  are partners in  $SU(3)$ -flavor symmetry with molecular configurations.
- High statistic measurements from different channels or energies are needed to:
  - classify the origin of  $Z_{cs}$ ;
  - reduce the error of pole position.

**Thank you!**