

# Introduction to $e^+e^-$ Physics & Simulation

	$T_0$		+5		+10		+15		+20		...	+26
ILC	0.5/ab 250 GeV			1.5/ab 250 GeV			1.0/ab 500 GeV	0.2/ab $2m_{top}$	3/ab 500 GeV			
CEPC	5.6/ab 240 GeV			16/ab $M_Z$	2.6 /ab $2M_W$					SppC =>		
CLIC	1.0/ab 380 GeV					2.5/ab 1.5 TeV			5.0/ab => until +28 3.0 TeV			
FCC	150/ab <u>ee</u> , $M_Z$	10/ab <u>ee</u> , $2M_W$	5/ab <u>ee</u> , 240 GeV			1.7/ab <u>ee</u> , $2m_{top}$						hh.eh =>
LHeC	0.06/ab			0.2/ab			0.72/ab					
HE-LHC	10/ab per experiment in 20y											
FCC eh/hh	20/ab per experiment in 25y											

Junping Tian (U. Tokyo)

MCnet Beijing School for Event Generators, June 28-July 2, 2021

# plan

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(i) Mini-intro to future e+e- experiments

Lecture 1

(ii) Higgs Property Measurements

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(iii) New Particle Searches

(iv) Top-quark & EW Measurements

Lecture 2

(v) Global Interpretation in SM EFT

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focus will be on experimental concepts “why / what / how”  
please learn theoretical concepts “why” from other lectures



# (i) future e+e- collider proposals

	$\sqrt{s}$	beam polarisation	$\int L dt$ (baseline)	R&D phase
<b>ILC</b>	0.1 - 1 TeV	e-: 80% e+: 30% (20%)	2 ab <sup>-1</sup> @ 250 GeV 0.2 ab <sup>-1</sup> @ 350 GeV 4 ab <sup>-1</sup> @ 500 GeV 8 ab <sup>-1</sup> @ 1 TeV	TDR 2013
<b>CLIC</b>	0.35 - 3 TeV	e-: (80%) e+: 0%	1 ab <sup>-1</sup> @ 380 GeV 2.5 ab <sup>-1</sup> @ 1.5 TeV 5 ab <sup>-1</sup> @ 3 TeV	CDR 2012
<b>CEPC</b>	90 - 240 GeV	e-: 0% e+: 0%	5.6 ab <sup>-1</sup> @ 250 GeV 16 ab <sup>-1</sup> @ M <sub>Z</sub> 2.6 ab <sup>-1</sup> @ 2M <sub>w</sub>	CDR 2018
<b>FCC-ee</b>	90 - 350 GeV	e-: 0% e+: 0%	150 ab <sup>-1</sup> @ M <sub>Z</sub> 10 ab <sup>-1</sup> @ 2M <sub>w</sub> 5 ab <sup>-1</sup> @ 250 GeV 1.7 ab <sup>-1</sup> @ 365 GeV	CDR 2018

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- ▶ O(10<sup>6</sup>) Higgs; O(10<sup>9</sup>-10<sup>12</sup>) Z; O(10<sup>8</sup>) W; O(10<sup>6</sup>) t-quark; ? #BSM; etc
- ▶ What physics can be advanced? Roles played by  $\sqrt{s}$ ,  $\int L$ , Polarisation?

## (i-1) basic concepts on accelerators

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know better our tools which often constrain physics exploration

what behind  $\sqrt{s}$   $L$  ( $\int L dt$ )  $P$  ?

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### ► **Radio-Frequency acceleration**



Electromagnetic fields oscillate at a perfect timing  $l_i = \beta_i \frac{\lambda_{\text{RF}}}{2}$

Gradient: ILC 31.5 MV/m; CLIC 100 MV/m

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## ► Magnetic field (transverse acceleration)

$$R = \frac{E}{ecB}$$

SPPC / FCC-hh:  $E = 100\text{TeV}$ ,  $R = 100\text{km}$ ;  $B \sim 16\text{T}$

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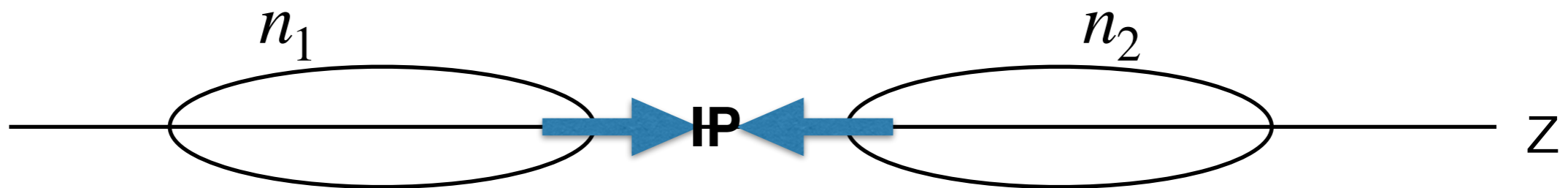
## ▶ **Plasma Wakefield acceleration (~10 GV/m)**

long way to go

# (i-1) basic concepts on accelerators

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## ► Luminosity (beam dynamics)



$$L = f_{coll} \frac{n_1 n_2}{4\pi\sigma_x^* \sigma_y^*} F$$

$f_{coll}$  average collision frequency (large in storage ring)

$\sigma_x^*, \sigma_y^*$  bunch size in transverse direction (“Nano Beam”)

$n_1, n_2$  # of particles in a beam bunch

► **Synchrotron Radiation**

$$P = \frac{e^2 c}{6\pi\epsilon_0} \frac{1}{(m_0 c^2)^4} \frac{E^4}{R^2}$$

radiation power  
(—> muon collider)

$$\Delta E[\text{keV}] = 88.5 \frac{E^4[\text{GeV}]^4}{R[\text{m}]}$$

E loss per turn for electron  
(~3GeV! for R=100km E=240GeV)

► **Beam Polarisation**

$$P = \frac{N_R - N_L}{N_R + N_L}$$

spinning particles precess around B-field direction

hard to preserve longitudinal polarisation in a ring; transverse possible



## (i-2) basic concepts on detectors

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what behind

Vertex / timing resolution

Momentum / Jet Energy Resolution

Flavor-tagging Efficiency

Particle Identification Efficiency

?

## (i-2) basic concepts on detectors

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what behind

- Vertex / timing resolution
- Momentum / Jet Energy Resolution
- Flavor-tagging Efficiency
- Particle Identification Efficiency

?

▶ **passage of particles through matter**

- ionization / atom excitation
- multiple scattering
- bremsstrahlung / pair production
- nuclear interaction
- Cherenkov radiation

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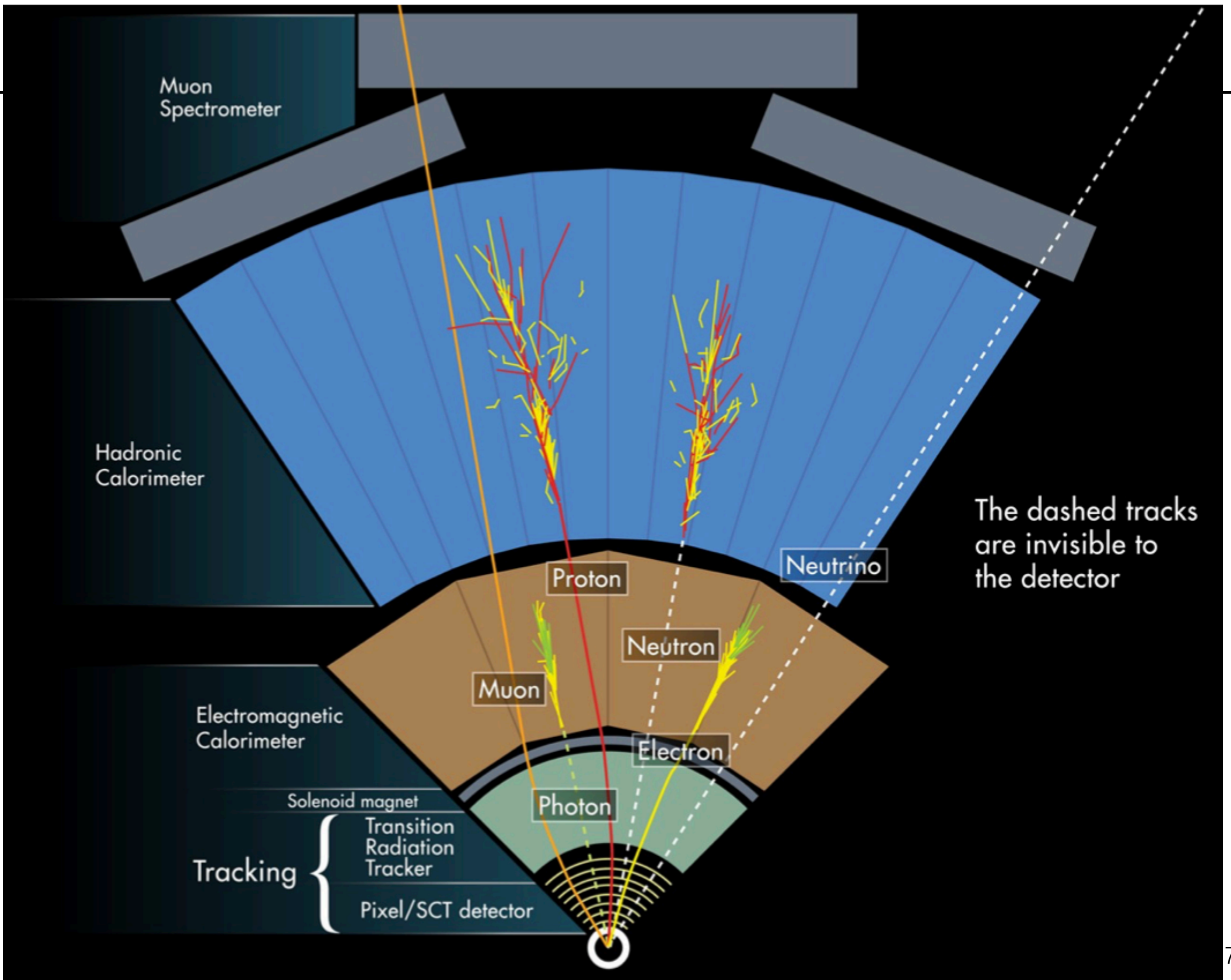
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### ▶ **type of detectors**

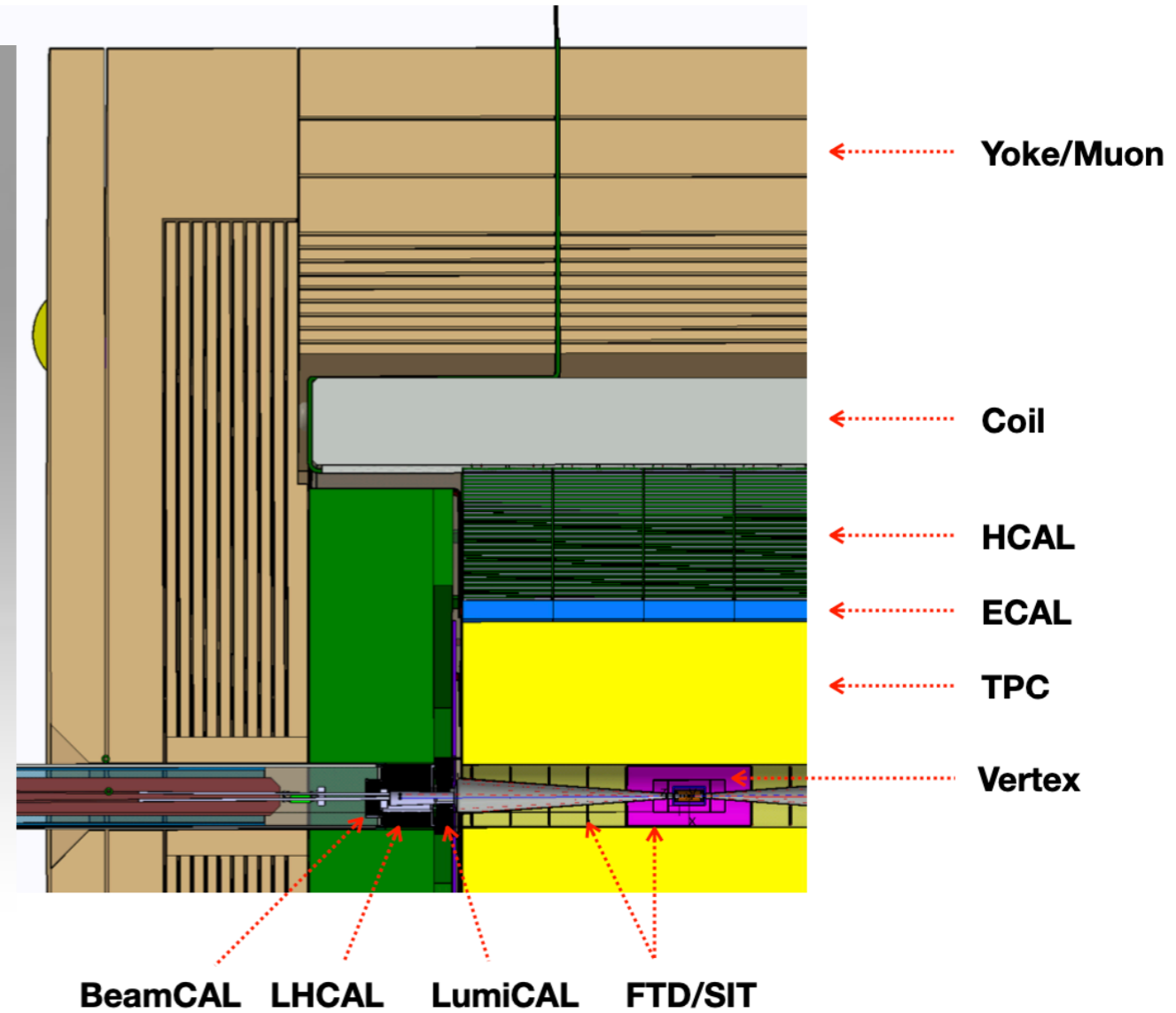
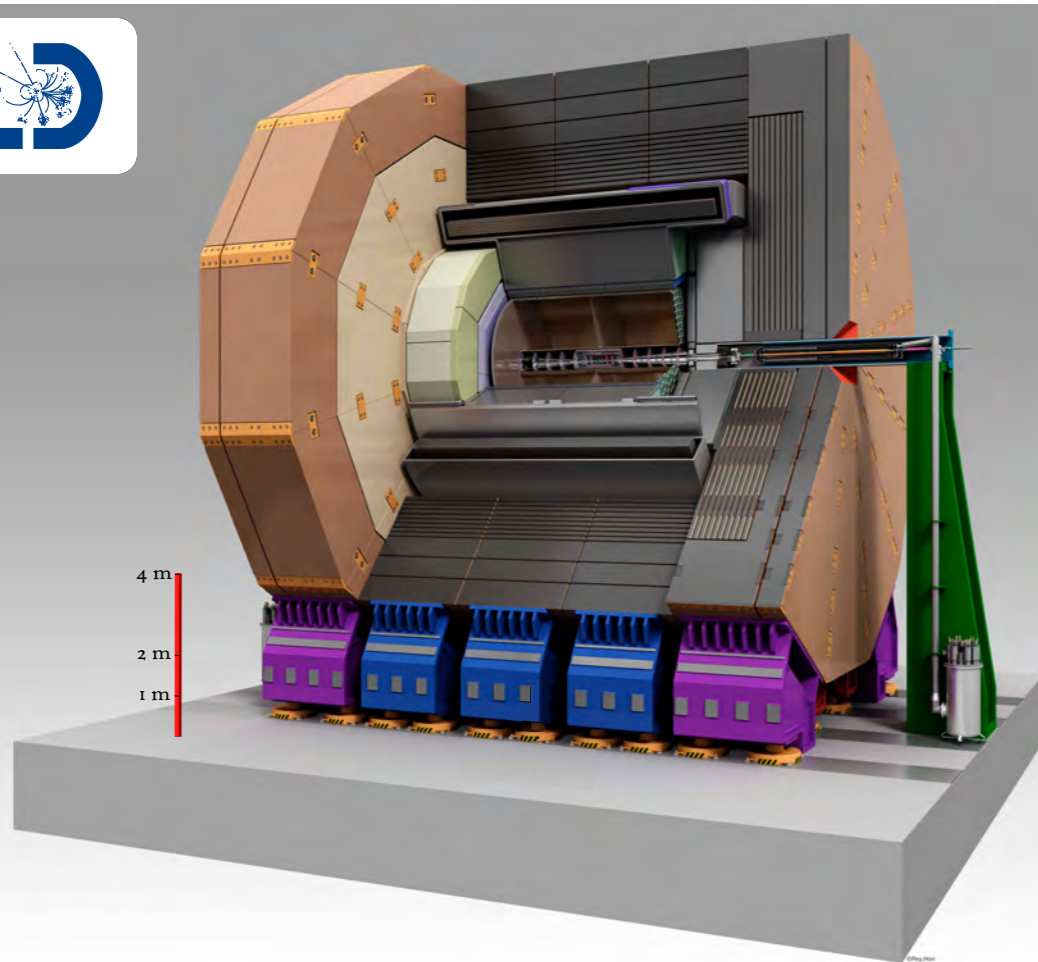
- vertex / tracking
- sampling calorimeters
- homogeneous calorimeters
- timing detectors
- ...

{ gaseous  
silicon  
scintillator  
... }

{ digital  
analog  
semi-digi  
... }



# (i-2) basic concepts on detectors

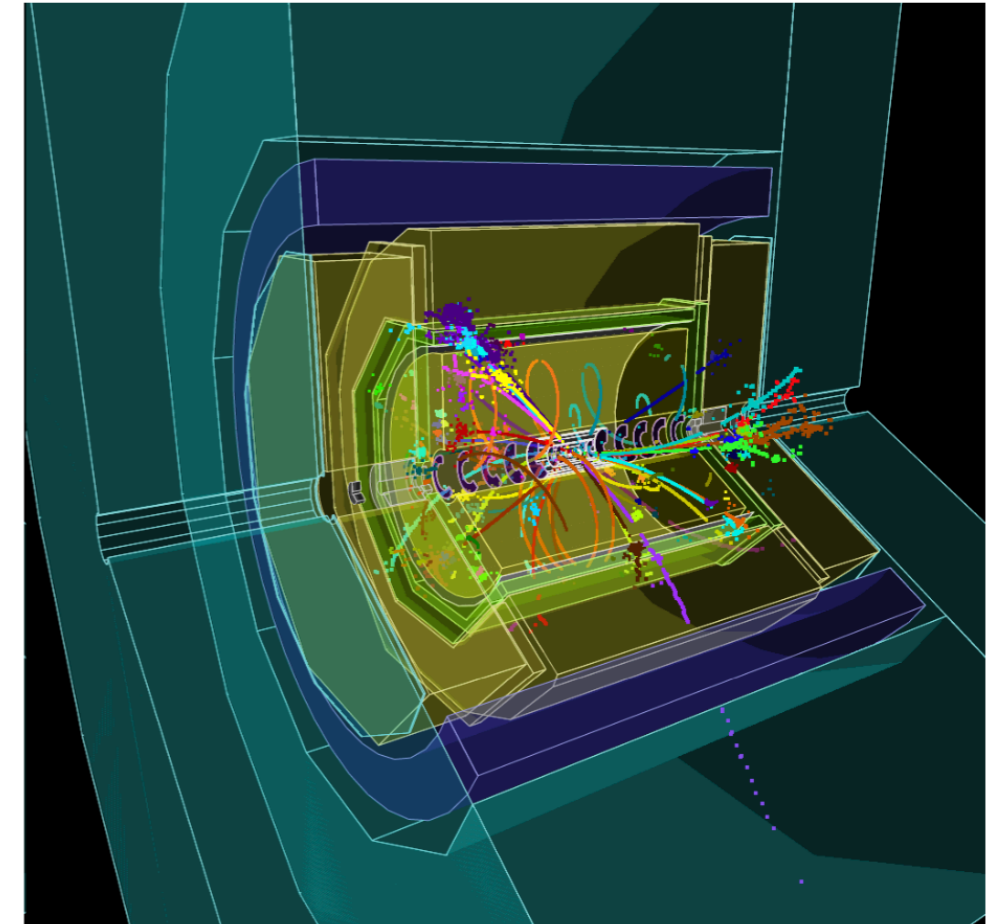


► **Particle Flow Detector**

particle flow approach tries to reconstruct every individual particle produced in an event

key challenge is to separate the showers produced by particles from a same jet

—> highly granular calorimeters



Component	Detector	Energy Fract.	Energy Res.	Jet Energy Res.
Charged Particles ( $X^\pm$ )	Tracker	$\sim 0.6 E_j$	$10^{-4} E_{X^\pm}^2$	$< 3.6 \times 10^{-5} E_j^2$
Photons ( $\gamma$ )	ECAL	$\sim 0.3 E_j$	$0.15 \sqrt{E_\gamma}$	$0.08 \sqrt{E_j}$
Neutral Hadrons ( $h^0$ )	HCAL	$\sim 0.1 E_j$	$0.55 \sqrt{E_{h^0}}$	$0.17 \sqrt{E_j}$

► **typical tracking performance**

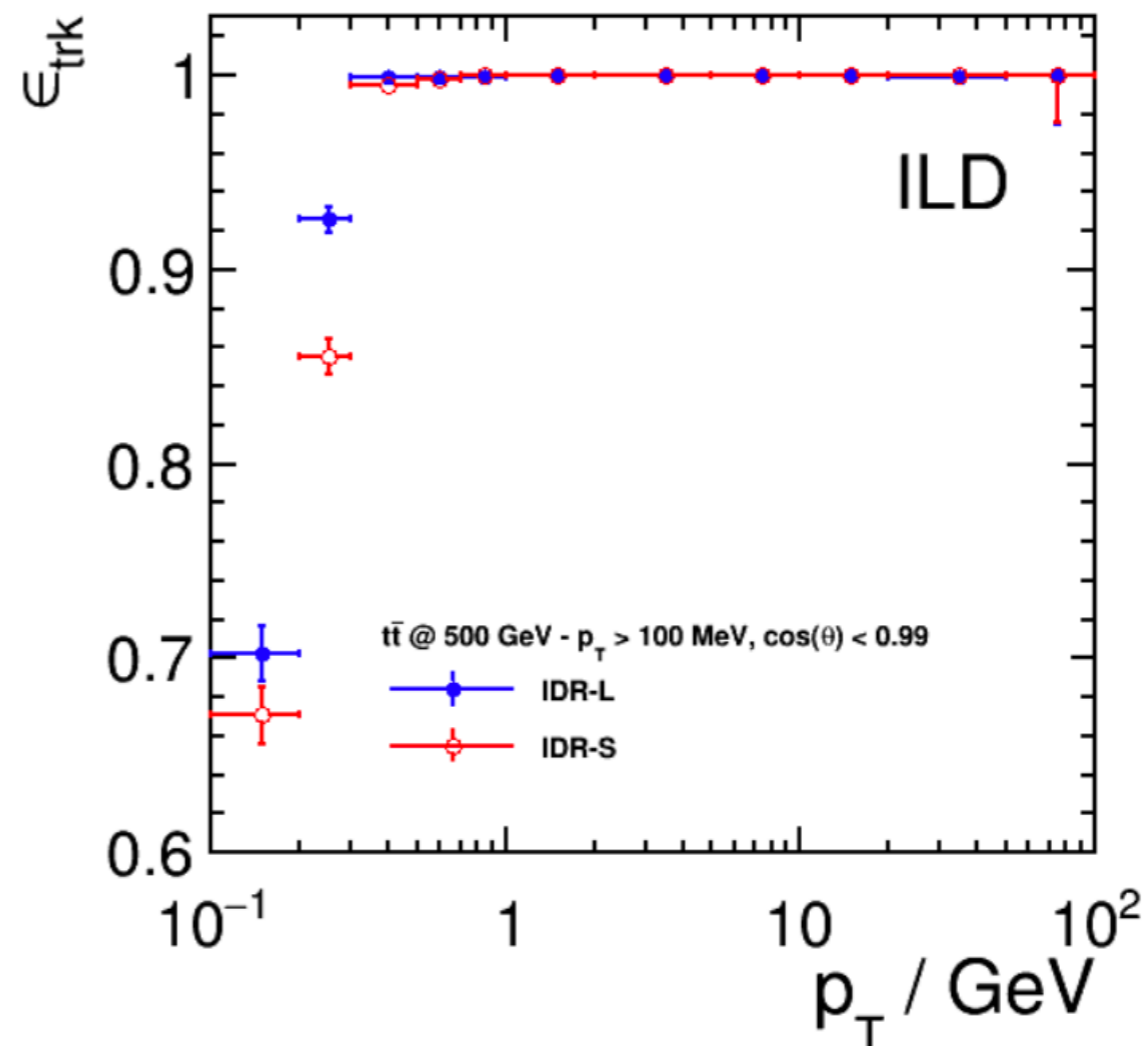
momentum resolution

$$\Delta_{1/P_t} = \frac{\Delta P_t}{P_t^2} \sim 2 \times 10^{-5} [\text{GeV}^{-1}]$$

~0.2% for  $P_t \sim 100 \text{ GeV}$

tracking efficiency

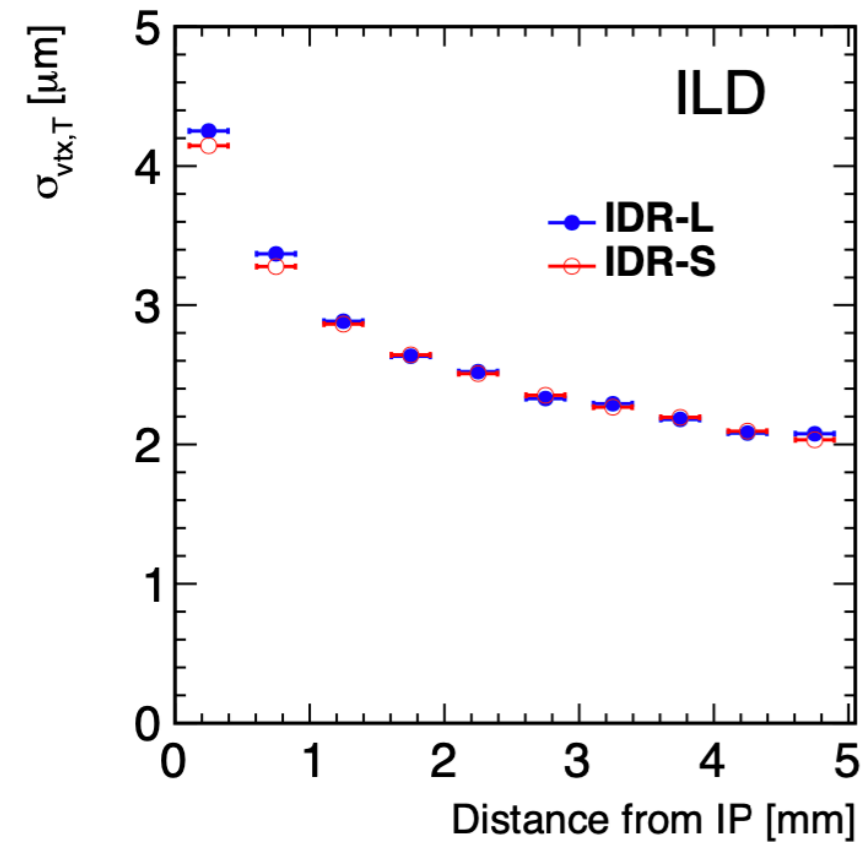
~100% for  $P_T > 300 \text{ MeV}$





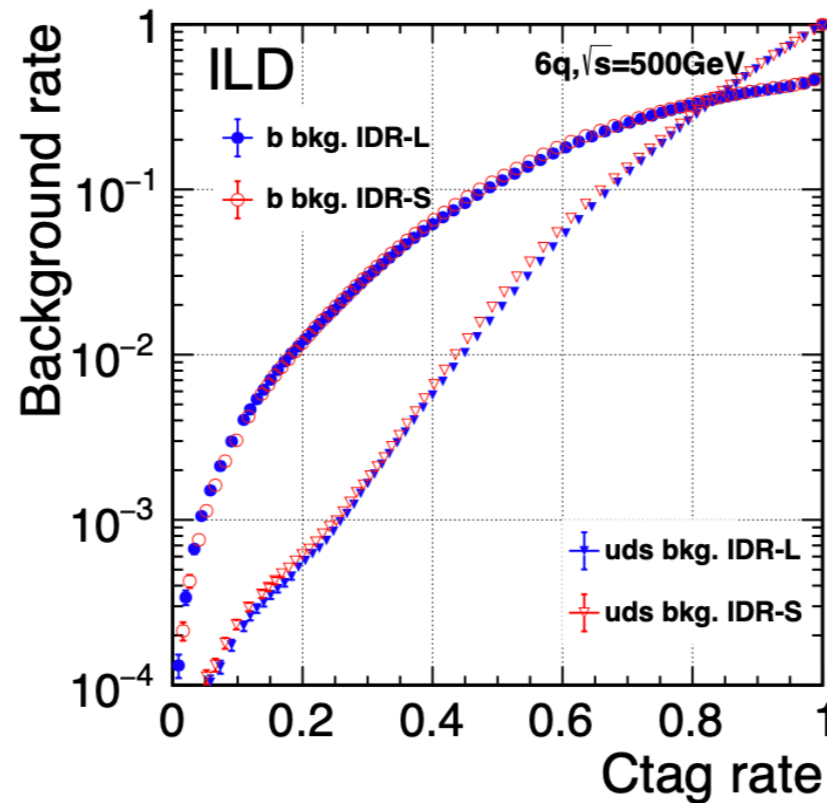
(i-2) basic concepts on detectors

► **vertex / flavor-tagging performance**



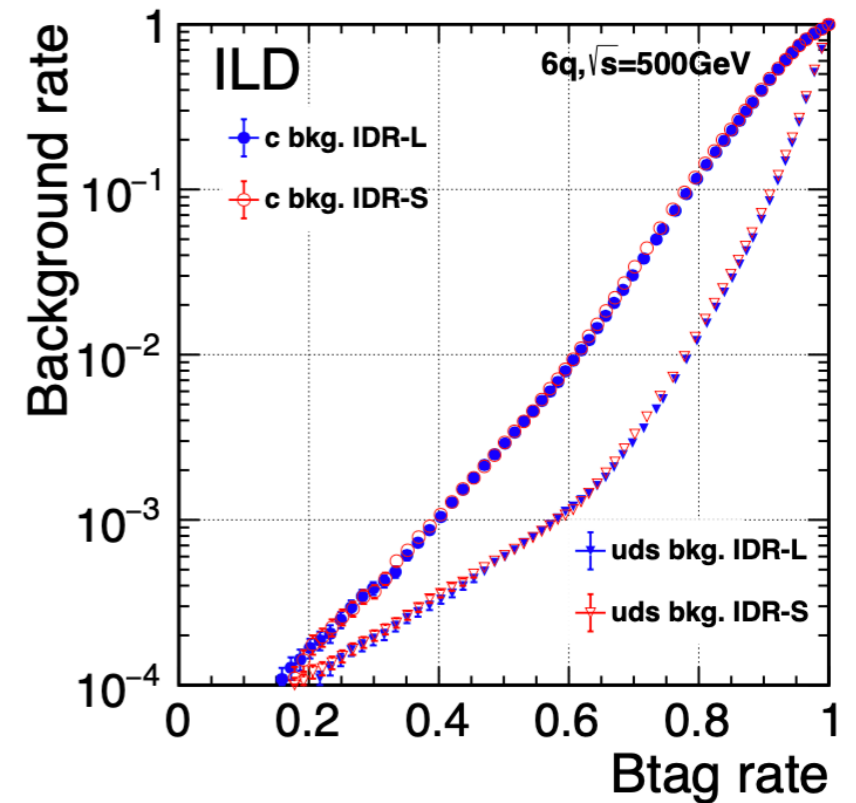
secondary vertex  
position from c-jets

$$\Delta r \sim 2\mu\text{m}$$



flavor-tagging  
c-jet

$$\varepsilon \sim 50\% \text{ (10\% b)}$$



flavor-tagging  
b-jet

$$\varepsilon \sim 80\% \text{ (10\% c)}$$

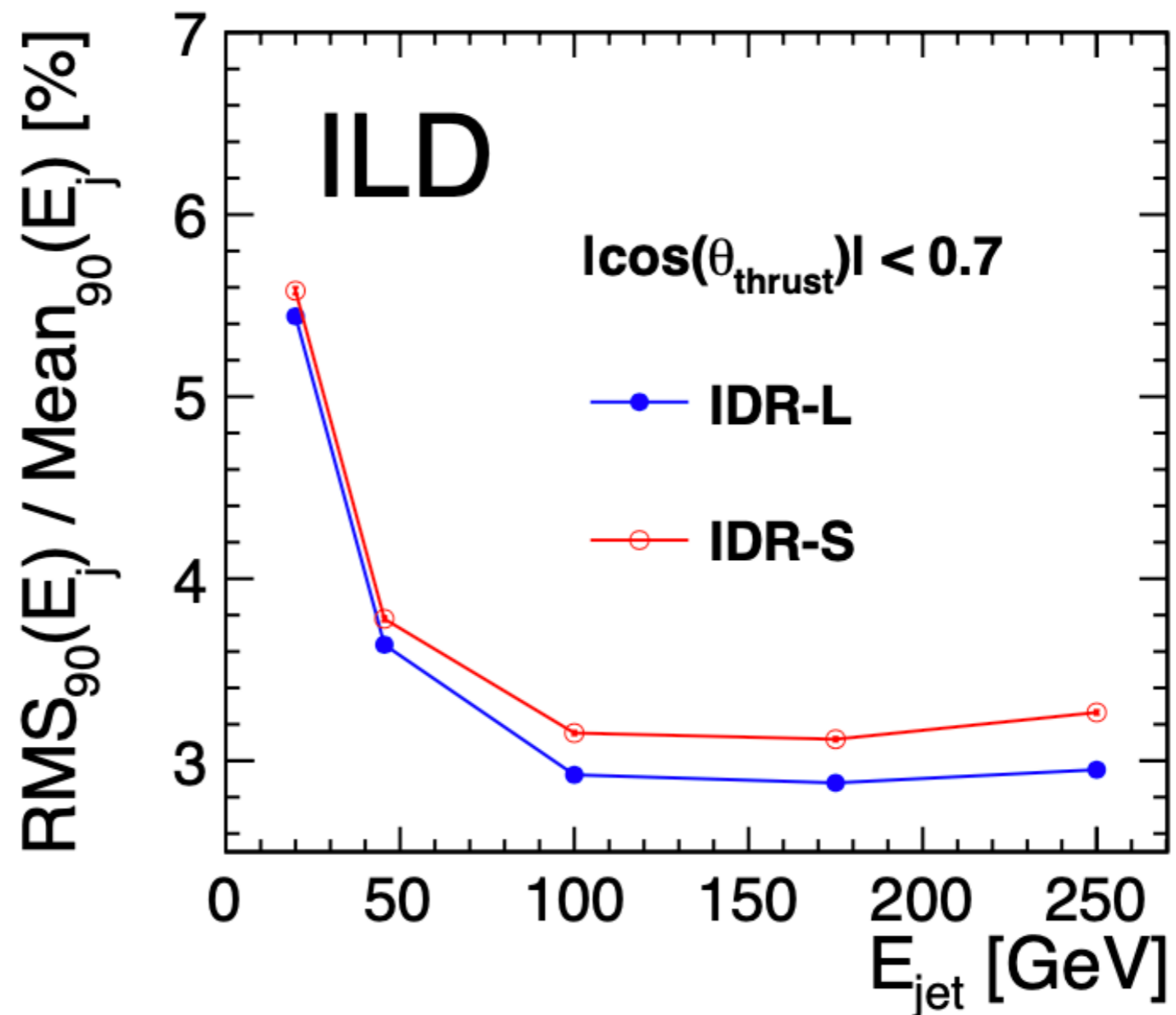


► performance on jet energy resolution

$$\frac{\Delta E}{E} = \frac{30\%}{\sqrt{E}} + c$$

(E in GeV)

$$\Delta E / E \sim 3-4\%$$



(i) from event generators to real life

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► **event generator: WHIZARD / MadGraph / Sherpa / Pythia...**

hard interaction; ISR; beamstrahlung

parton showering; hadronization; decay

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▶ **detector simulation**

full detector simulation; pile-up; (GEANT4)

fast simulation; simple smearing; (DELPHES / SGV)

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▶ **event reconstruction**

digitization; tracking; particle flow analysis (PandoraPFA)

vertex reconstruction; jet clustering; flavor tagging (LCFIPlus)

(i) from event generators to real life

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- ▶ **event generator: WHIZARD / MadGraph / Sherpa / Pythia...**
  - hard interaction; ISR; beamstrahlung
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  - digitization; tracking; particle flow analysis (PandoraPFA)
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- ▶ **physics analysis**

## (ii) $e^+e^-$ physics: big questions

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- data say there are **at least five missing pieces in the SM**

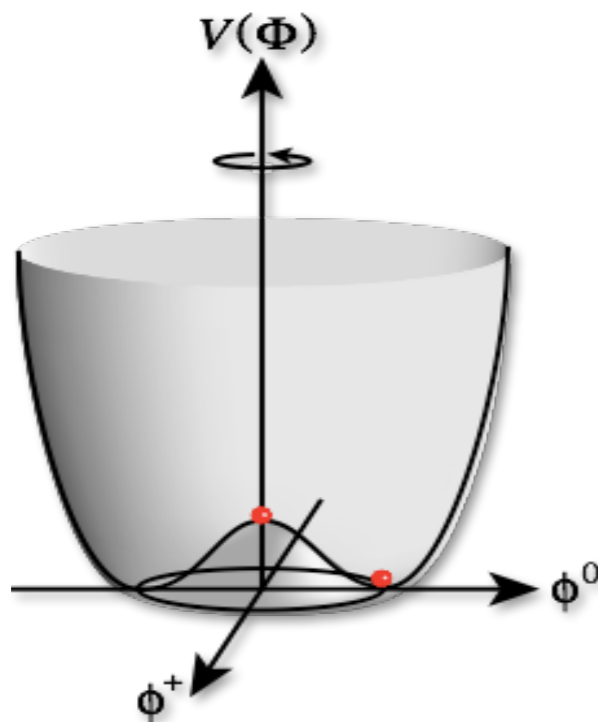
[H. Murayama]

- **dark matter (2003)**
- **neutrino mass (1998)**
- **dark energy (1998)**
- **inflation (2003)**
- **matter anti-matter asymmetry (2003)**

how can future e+e- colliders help?

## (ii) Higgs physics: mystery in Electroweak Symmetry Breaking

$$V(|\Phi|) = \mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$

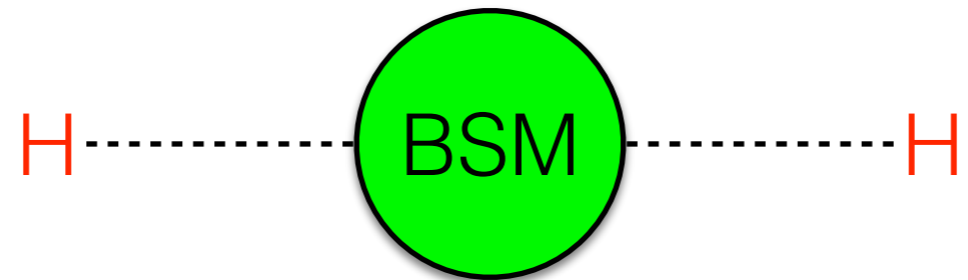


- H(125) discovery
  - elementary or composite? any siblings?
- What is the origin of EWSB?
  - why  $\mu^2 < 0$ ? underlying dynamics?
- What BSM protects  $m_H$ ?
- Connection to big questions?

$$M_H^2 = M_{\text{tree}}^2 + \left( \text{Higgs loop} \right) + \left( \text{top loop} \right) + \left( \text{WZ loop} \right) + \left( \text{BSM} \right)$$



# golden time: BSM hunting



direct searches

future e+e-...

**LHC**

$\tilde{t}, \tilde{g}, \tilde{\chi}, H^\pm, Z', \dots$

indirect searches

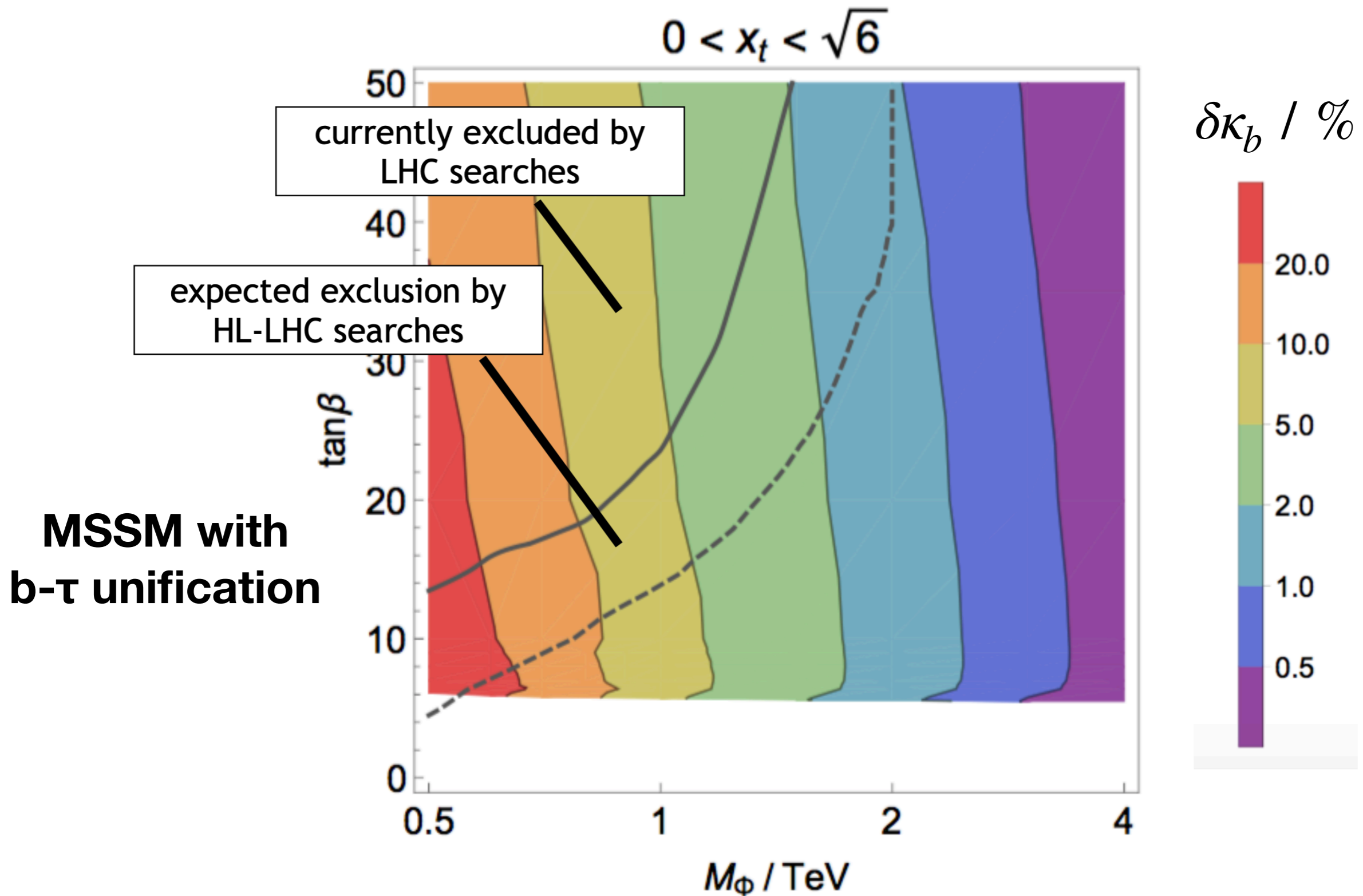
LHC

**future e+e- ...**

precision Higgs & SM couplings

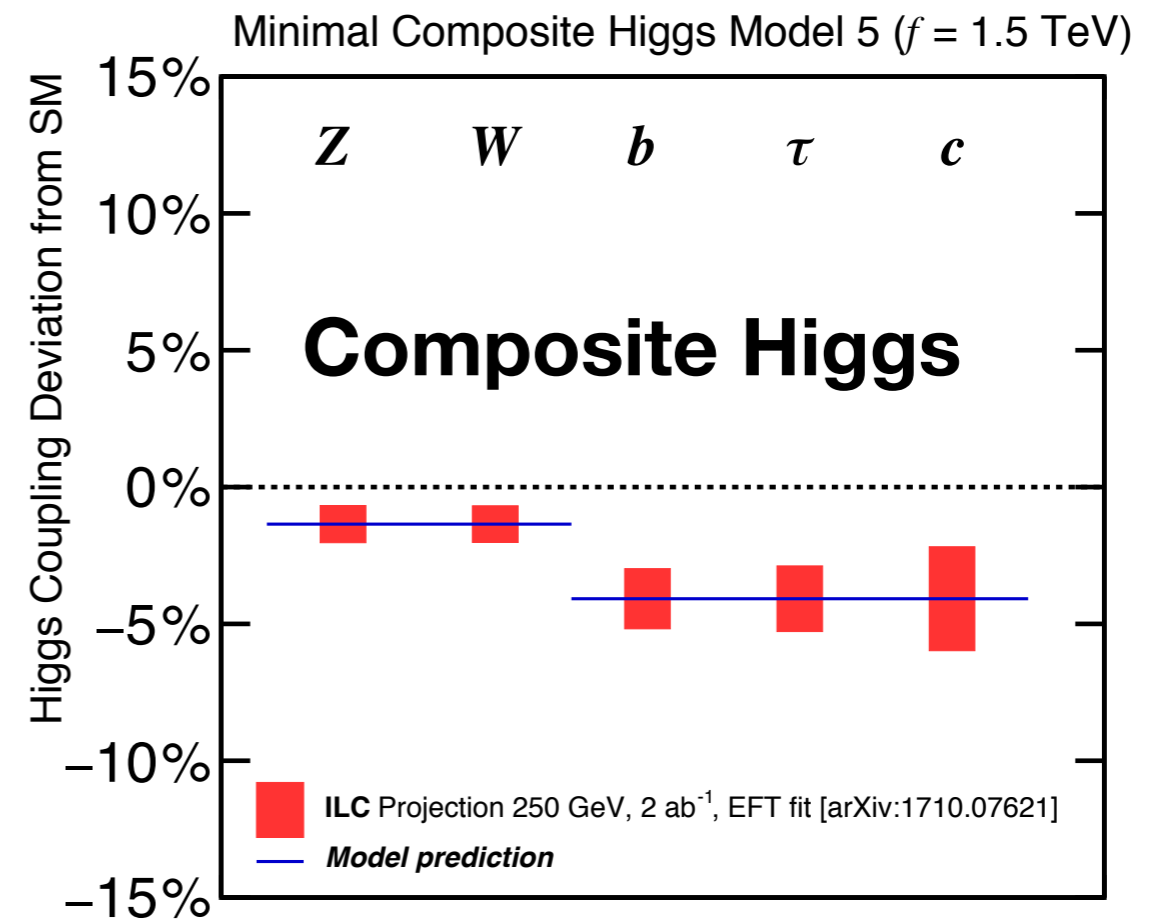
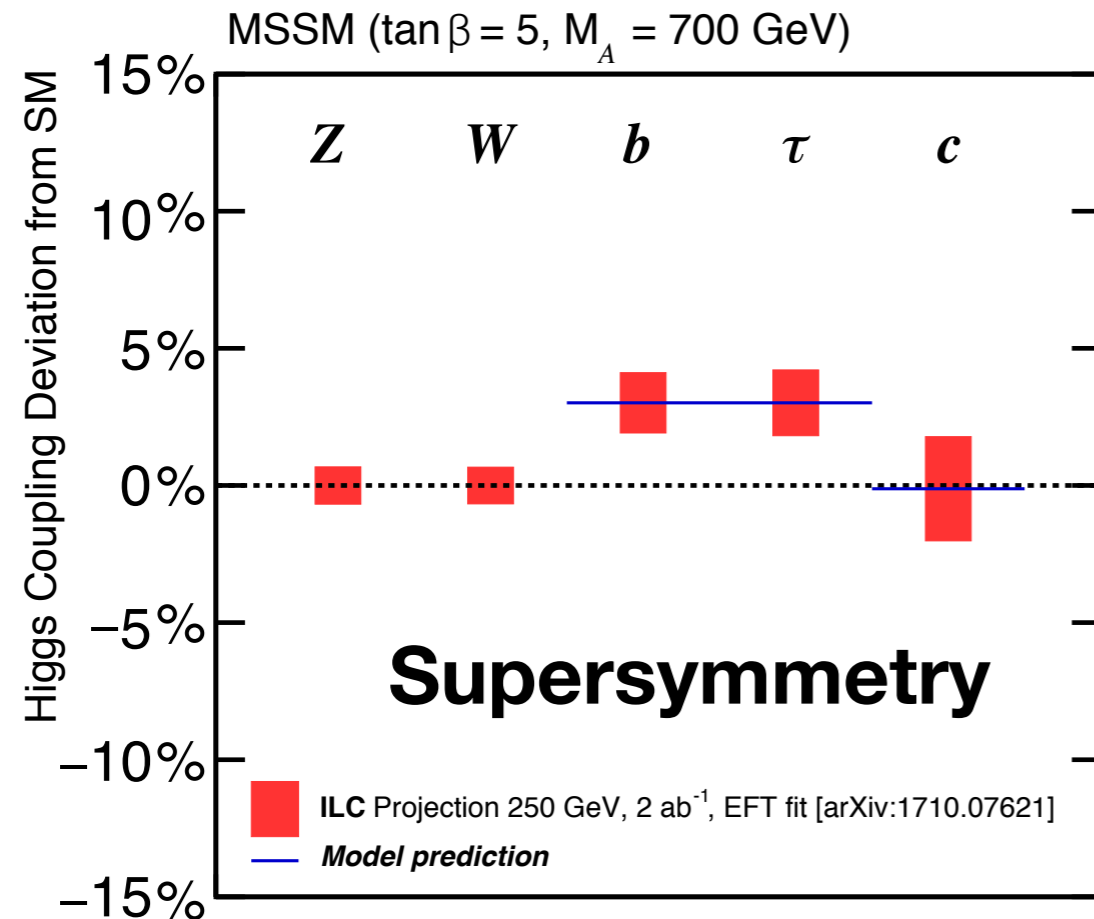
- ▶ there must be BSM around EW scale, we just need to find it out

# direct vs indirect searches: complementarity



[Wells, Zhang, arXiv:1711.04774]

# opportunities from precision Higgs couplings



arXiv: 1306.6352

- ▶ measuring deviation pattern will tell a lot about BSM

general guidelines for Higgs coupling meas. @ future  $e^+e^-$

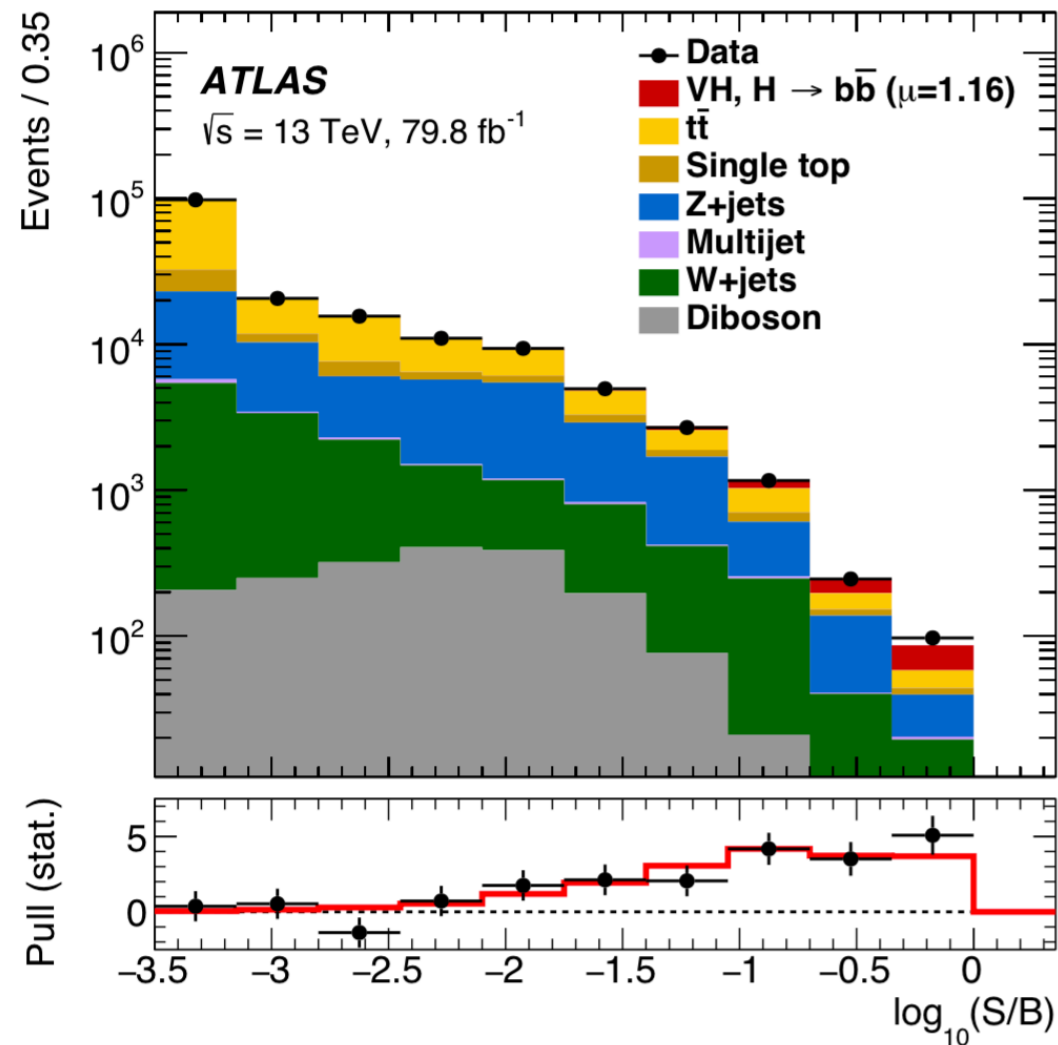
—in light of what have been found at LHC

- new particles are heavy, deviation is small, 1-10% for  $m_{\text{BSM}} \sim 1\text{TeV}$ : need measurement with **1% precision** or below so that deviations with SM can be discovered
- measurement needs to be as **model-independent** as possible: so that the true BSM model can be discriminated from others, future HEP direction hence can be decided

# statistics vs S/B: example on $H \rightarrow bb$ discovery

LHC (super Higgs factory # $10^8$ )

$e^+e^-$  (Higgs factory # $10^6$ )



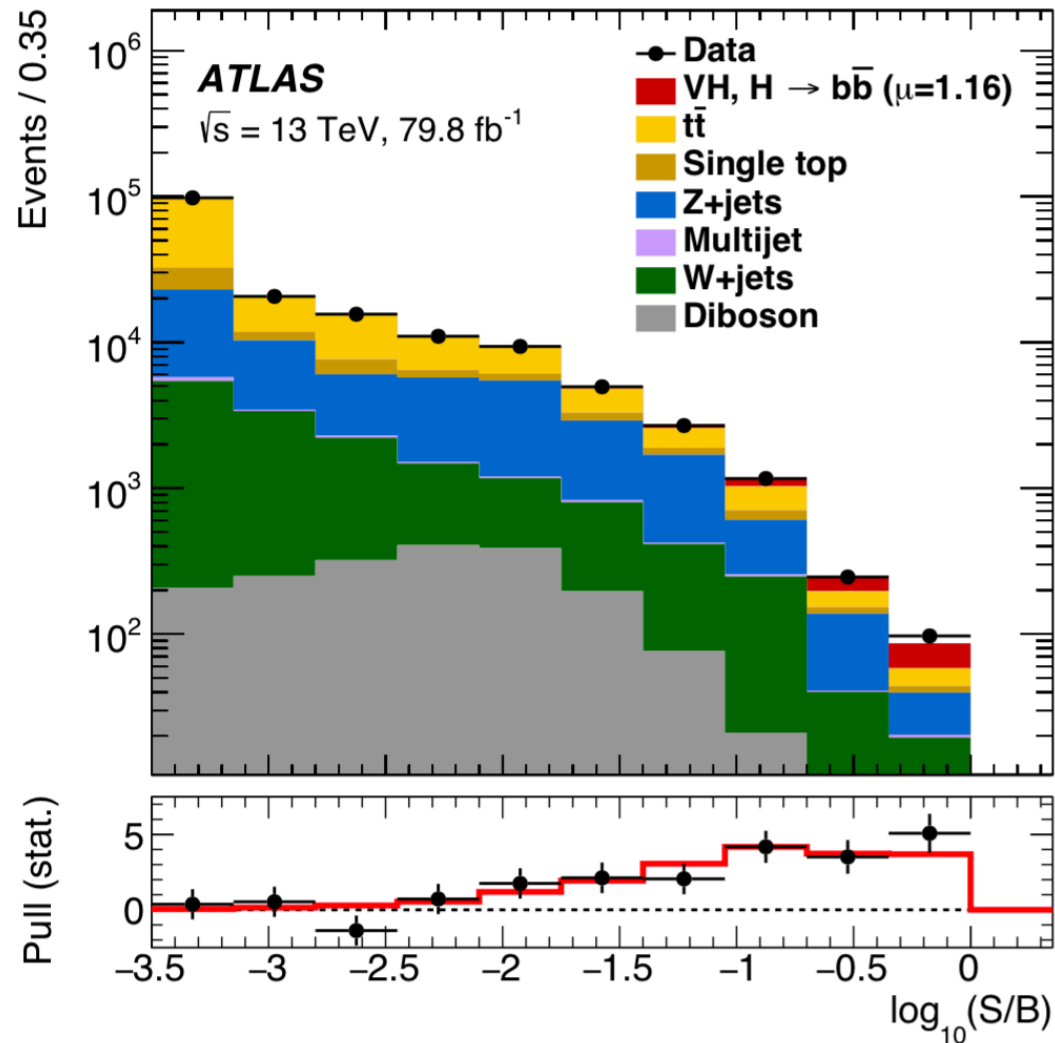
# of Higgs produced:  $\sim 4,000,000$

significance:  $5.4\sigma$

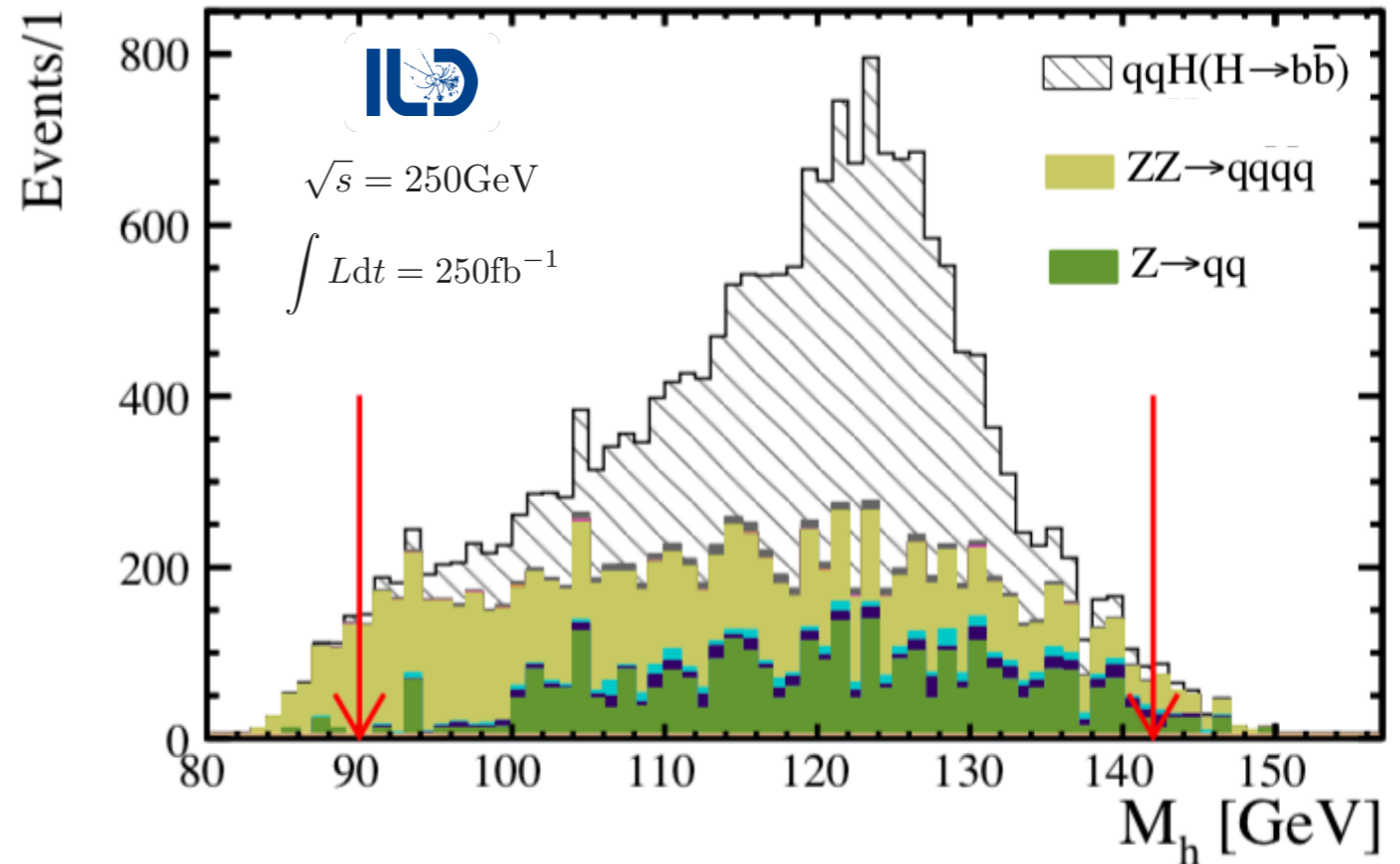
[ATLAS, 1808.08238; CMS, 1808.08242]

# statistics vs S/B: example on $H \rightarrow b\bar{b}$ discovery

LHC (super Higgs factory # $10^8$ )



$e^+e^-$  (Higgs factory # $10^6$ )



**full detector simulation**

# of Higgs produced:  $\sim 4,000,000$

$\sim 400$

significance:  $5.4\sigma$

$5.2\sigma$

[ATLAS, 1808.08238; CMS, 1808.08242]

[Ogawa, PhD Thesis (Sokendai)]

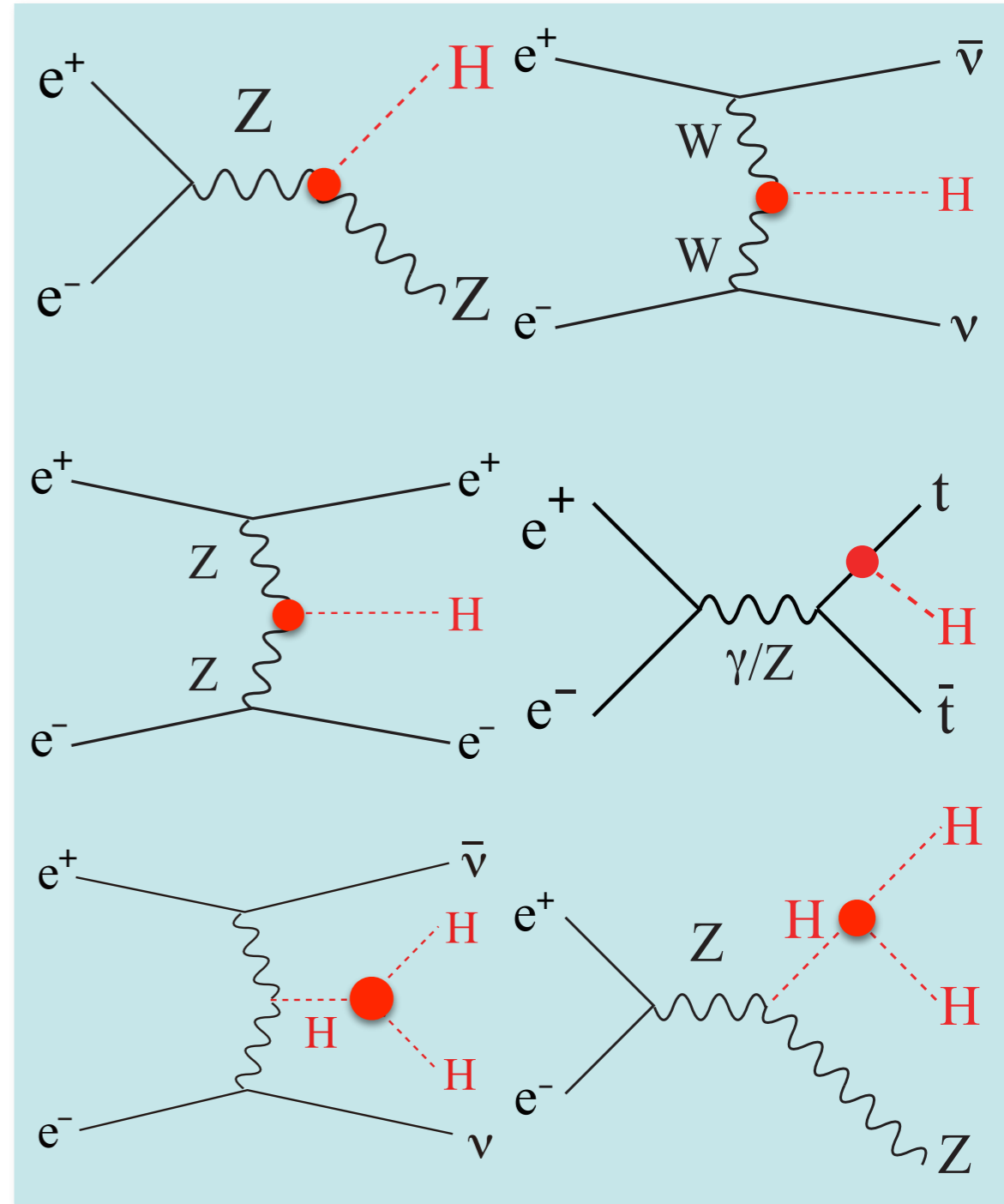
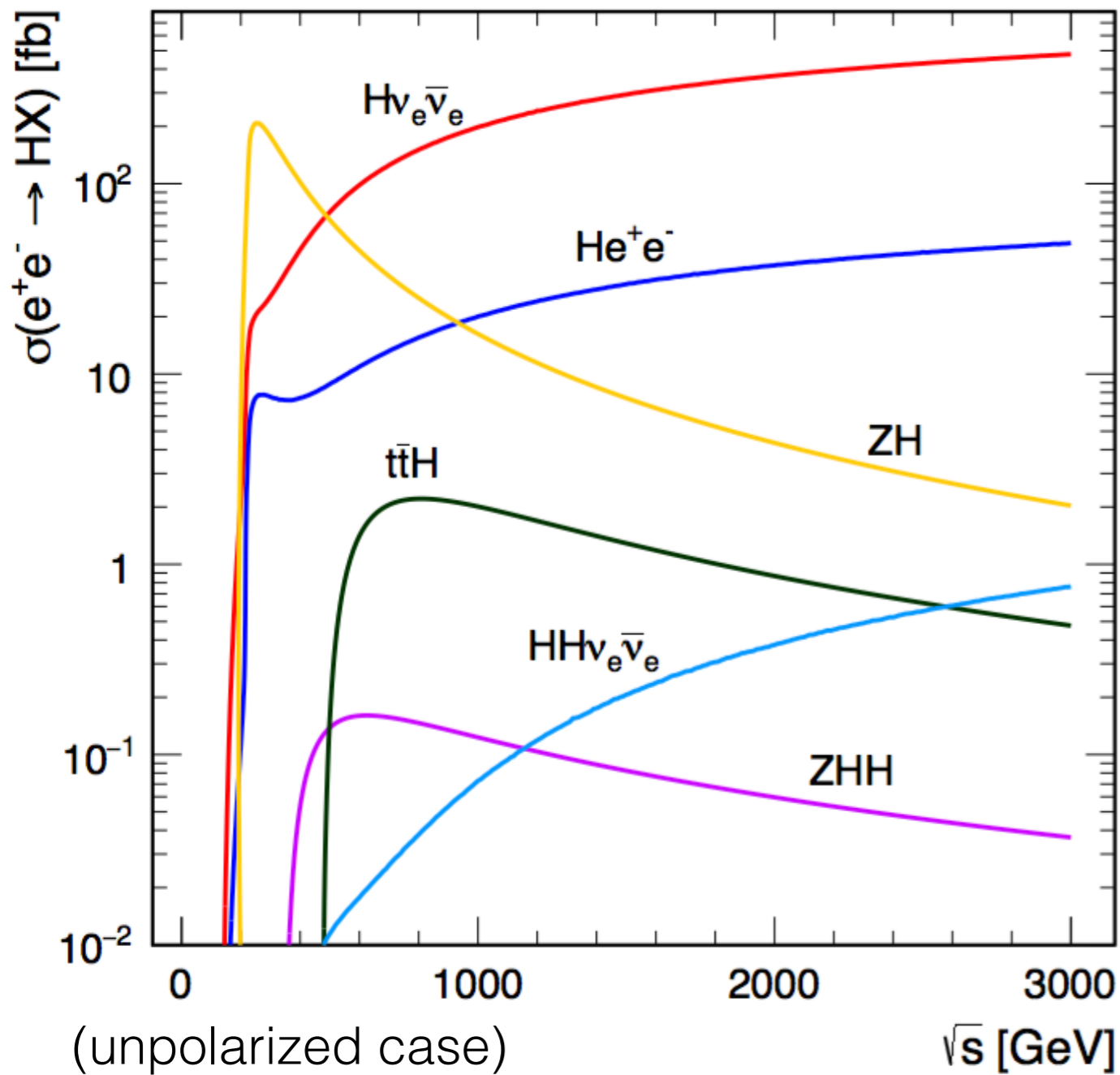
“that is much much easier, infinitely easier,  
on a  $e^+e^-$  machine than on a proton machine”



youtube: Burton Richter #mylinearcollider, 2015



# Higgs productions at $e^+e^-$



- two apparent important thresholds:  $\sqrt{s} \sim \mathbf{250}$  GeV for ZH,  $\sim \mathbf{500}$  GeV for ZHH and ttH
- + another threshold for t t-bar, important for vacuum stability



# Higgs properties: what we would like to measure

reconstruct the Higgs sector in a bottom-up and model independent way

$$\text{Mass \& } J^{\text{CP}} \quad M_h \quad \Gamma_h \quad J^{\text{CP}}$$

new CP violating source?

$$L_{\text{Higgs}} \quad hhh : -6i\lambda v = -3i\frac{m_h^2}{v}, \quad hhhh : -6i\lambda = -3i\frac{m_h^2}{v^2}$$

probe Higgs potential, EWBG?

$$L_{\text{Gauge}} \quad W_\mu^+ W_\nu^- h : i\frac{g^2 v}{2} g_{\mu\nu} = 2i\frac{M_W^2}{v} g_{\mu\nu}, \quad W_\mu^+ W_\nu^- hh : i\frac{g^2}{2} g_{\mu\nu} = 2i\frac{M_W^2}{v^2} g_{\mu\nu},$$

$$Z_\mu Z_\nu h : i\frac{g^2 + g'^2 v}{2} g_{\mu\nu} = 2i\frac{M_Z^2}{v} g_{\mu\nu}, \quad Z_\mu Z_\nu hh : i\frac{g^2 + g'^2}{2} g_{\mu\nu} = 2i\frac{M_Z^2}{v^2} g_{\mu\nu}$$

SU(2) nature?  
m<sub>v</sub> from SSB?

$$L_{\text{Yukawa}} \quad h\bar{f}f : -i\frac{y^f}{\sqrt{2}} = -i\frac{m_f}{v}$$

m<sub>f</sub> from Yukawa coupling?  
2HDM?

$$L_{\text{Loop}} \quad h\gamma\gamma \quad hgg \quad h\gamma Z$$

new particles in the loop?

**+ possible exotic/anomalous interactions of Higgs**

# what are the direct experimental observables

- ☑  $\sigma_{ZH}$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow bb), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow bb)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow cc), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow cc)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow gg), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow gg)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow WW^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow WW^*)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow ZZ^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow ZZ^*)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow \tau\tau), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \tau\tau)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow \gamma\gamma / \gamma Z), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \gamma\gamma / \gamma Z)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow \mu\mu), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \mu\mu)$
- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow \text{inv.} / \text{exotic})$
- ☑  $\sigma_{ttH} \times \text{Br}(H \rightarrow bb)$
- ☑  $\sigma_{ZH\bar{H}} \times \text{Br}^2(H \rightarrow bb), \sigma_{\nu\nu H\bar{H}} \times \text{Br}^2(H \rightarrow bb)$

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- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow WW^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow WW^*)$
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- ☑  $\sigma_{ZH} \times \text{Br}(H \rightarrow \gamma\gamma / \gamma Z), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \gamma\gamma / \gamma Z)$
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- ☑  $\sigma_{ttH} \times \text{Br}(H \rightarrow bb)$
- ☑  $\sigma_{ZH\bar{H}} \times \text{Br}^2(H \rightarrow bb), \sigma_{\nu\nu H\bar{H}} \times \text{Br}^2(H \rightarrow bb)$

► note the important complementarity with LHC

## (ii) Higgs property measurements at $e^+e^-$

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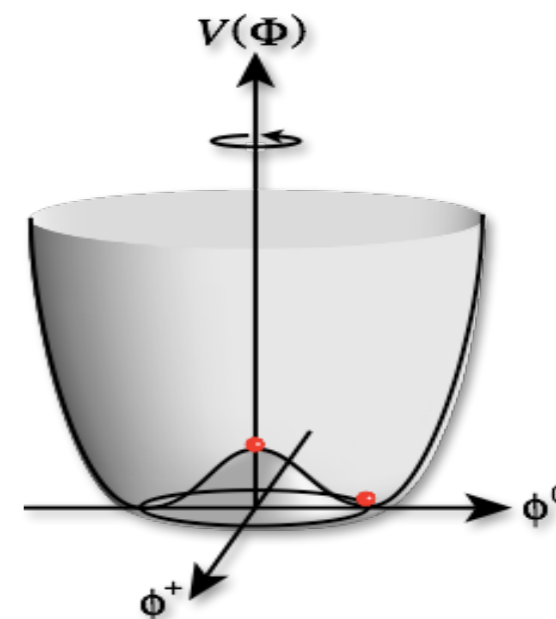
I will explain in fare details for 1-2 analyses, talk very briefly in other ones; mainly focus on physics issues instead of analysis techniques, which are important as well and can be learned from the references.

- (1) Higgs self-coupling analysis
- (2) recoil mass analysis
- (3) Higgs CP
- (4)  $H \rightarrow bb/cc/gg$
- (5) Higgs total width
- (6) top-Yukawa coupling
- (7) ...

as usual, selection is always biased

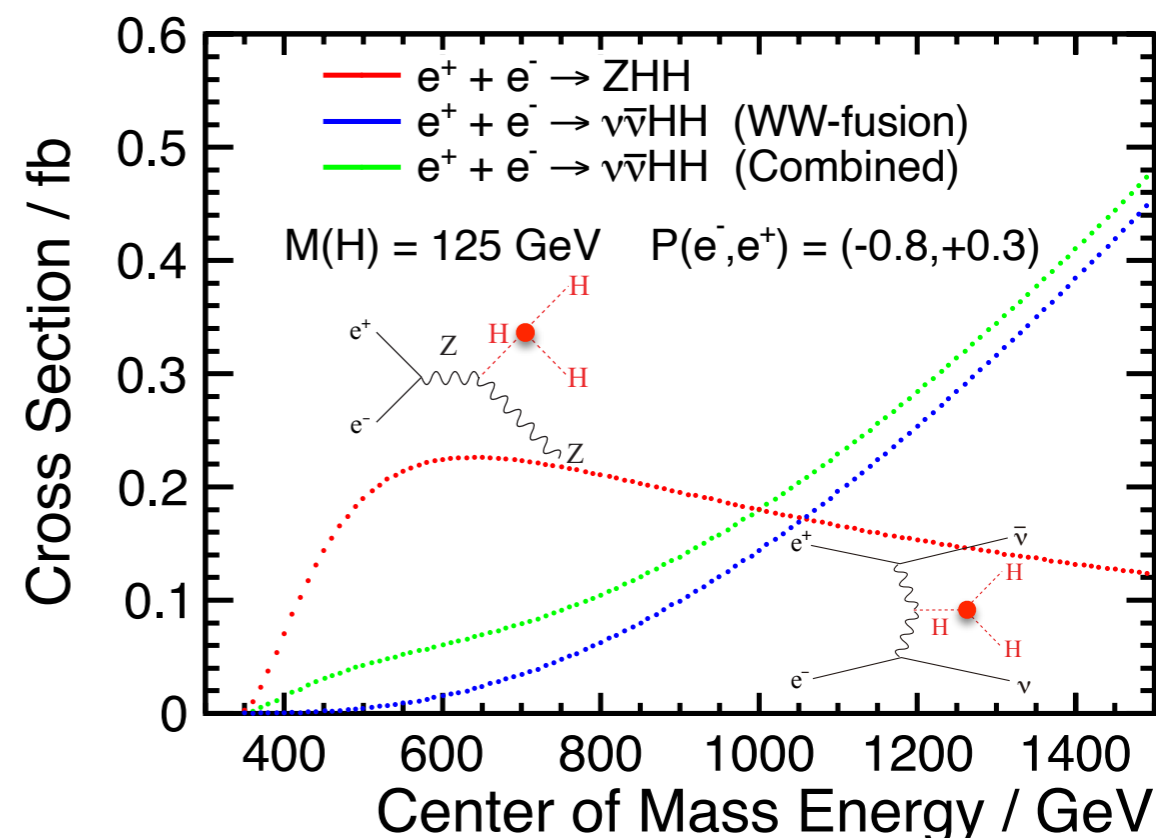
## (ii-1) Higgs self-coupling

- ▶ direct probe of the Higgs potential
- ▶ large deviation ( $> 20\%$ ) motivated by electroweak baryogenesis, could be  $\sim 100\%$
- ▶  $\sqrt{s} \geq 500$  GeV,  $e^+e^- \rightarrow ZHH$
- ▶  $\sqrt{s} \geq 1$  TeV,  $e^+e^- \rightarrow \nu\bar{\nu}HH$  (WW-fusion)

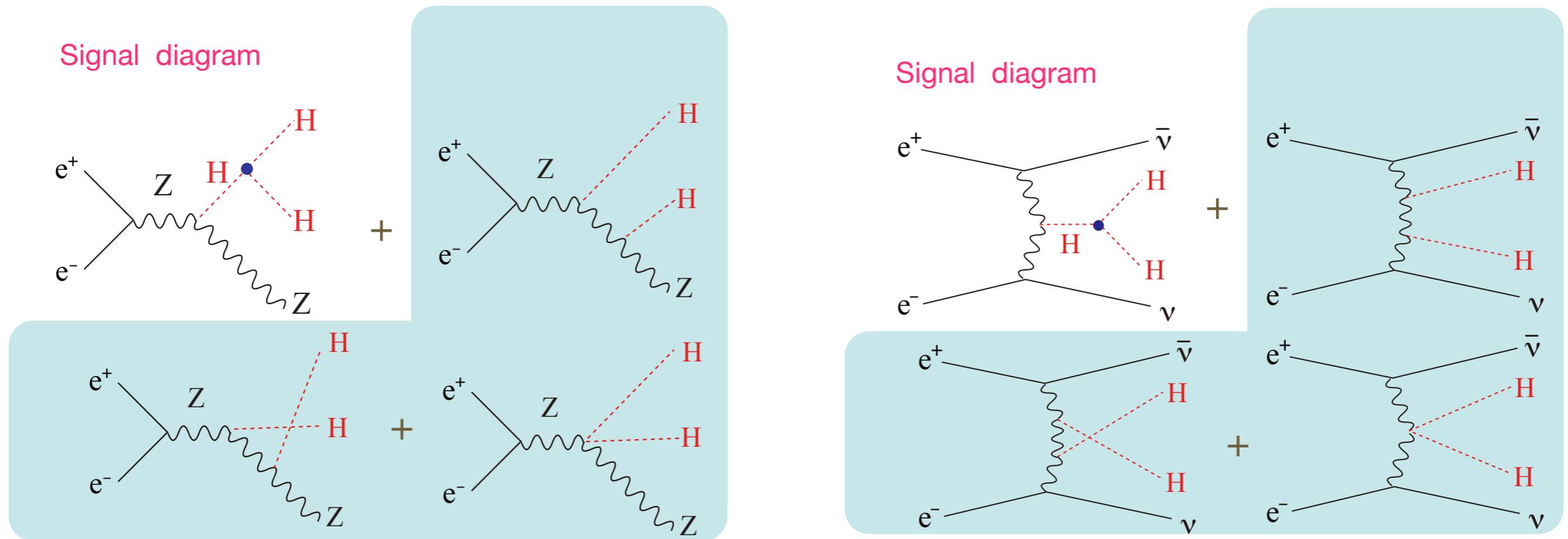


ILC	$\Delta\lambda_{HHH}/\lambda_{HHH}$	500 GeV	+ 1 TeV
	H20	27%	10%

CLIC	1.4 TeV	+3 TeV
	24%	11%



# physics issues: diagrams for double Higgs production



$$\sigma = S\lambda^2 + I\lambda + B$$

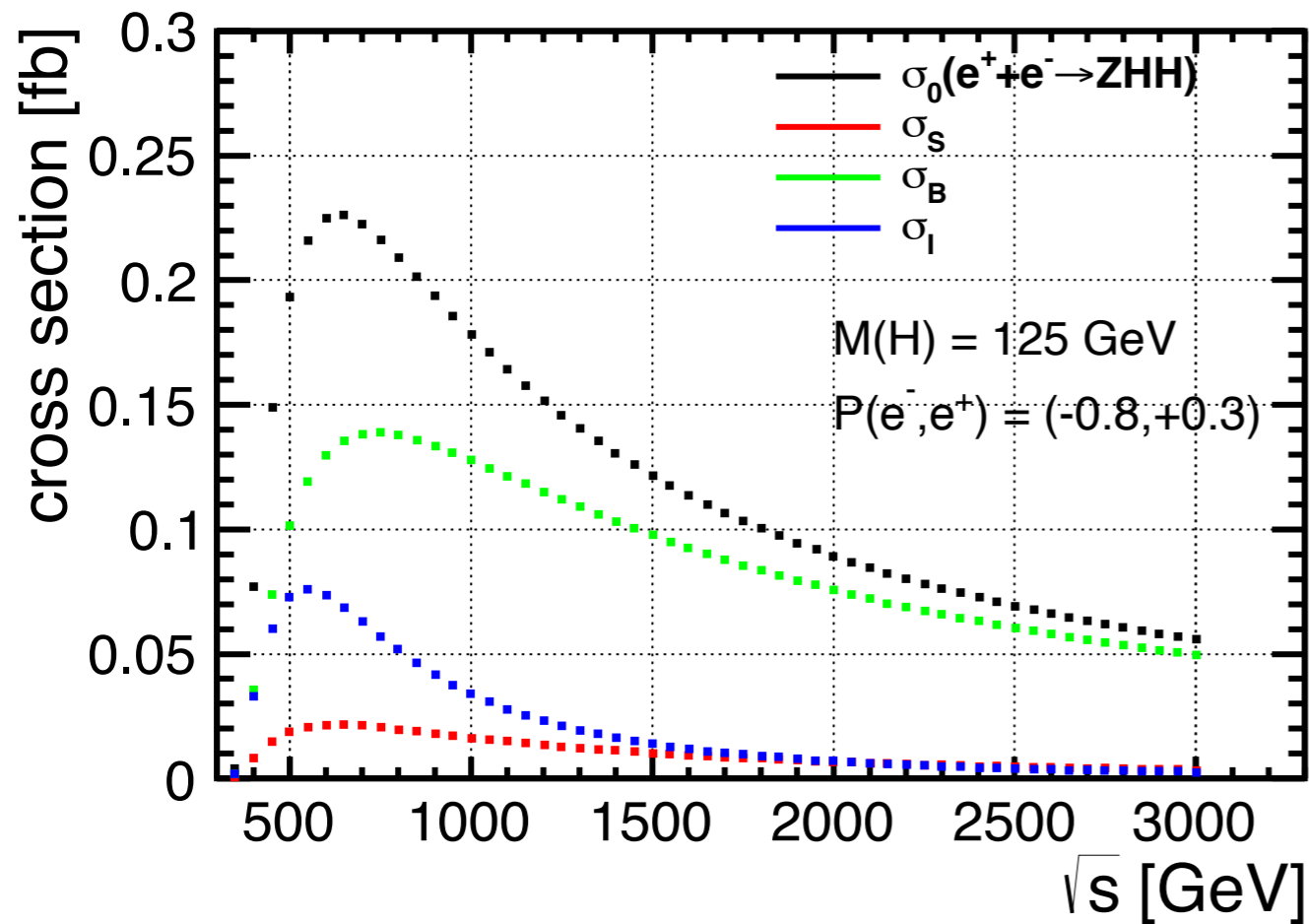
(signal diagram) (interference) (background diagram)

- ▶ the sensitivity of  $\lambda$  is determined not just by the apparent total cross section, in fact is determined by S and I term;
- ▶ if B term dominates, measurement would be very difficult

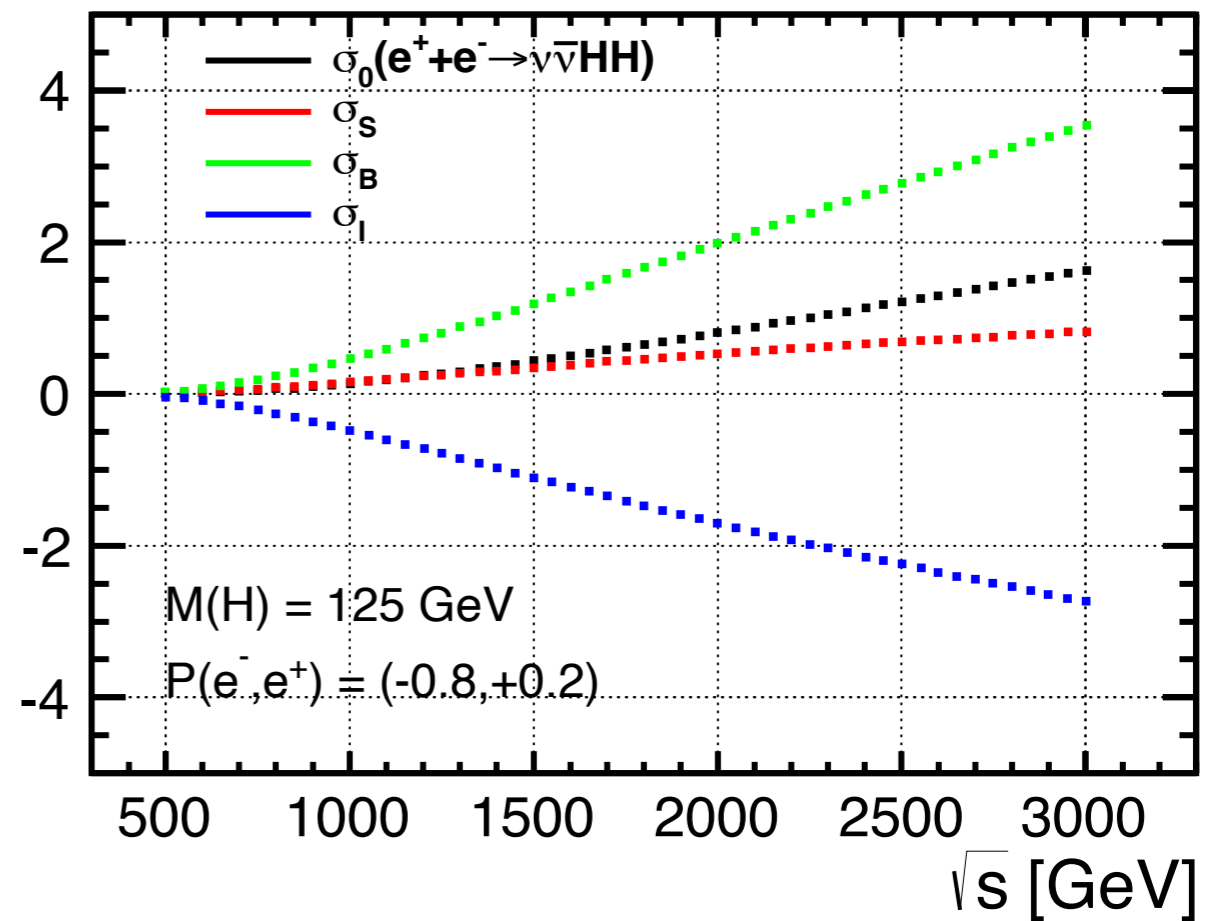
# double Higgs x-section: breakdown for each diagram

$$\sigma = S\lambda^2 + I\lambda + B$$

ZHH



$\nu\nu HH$

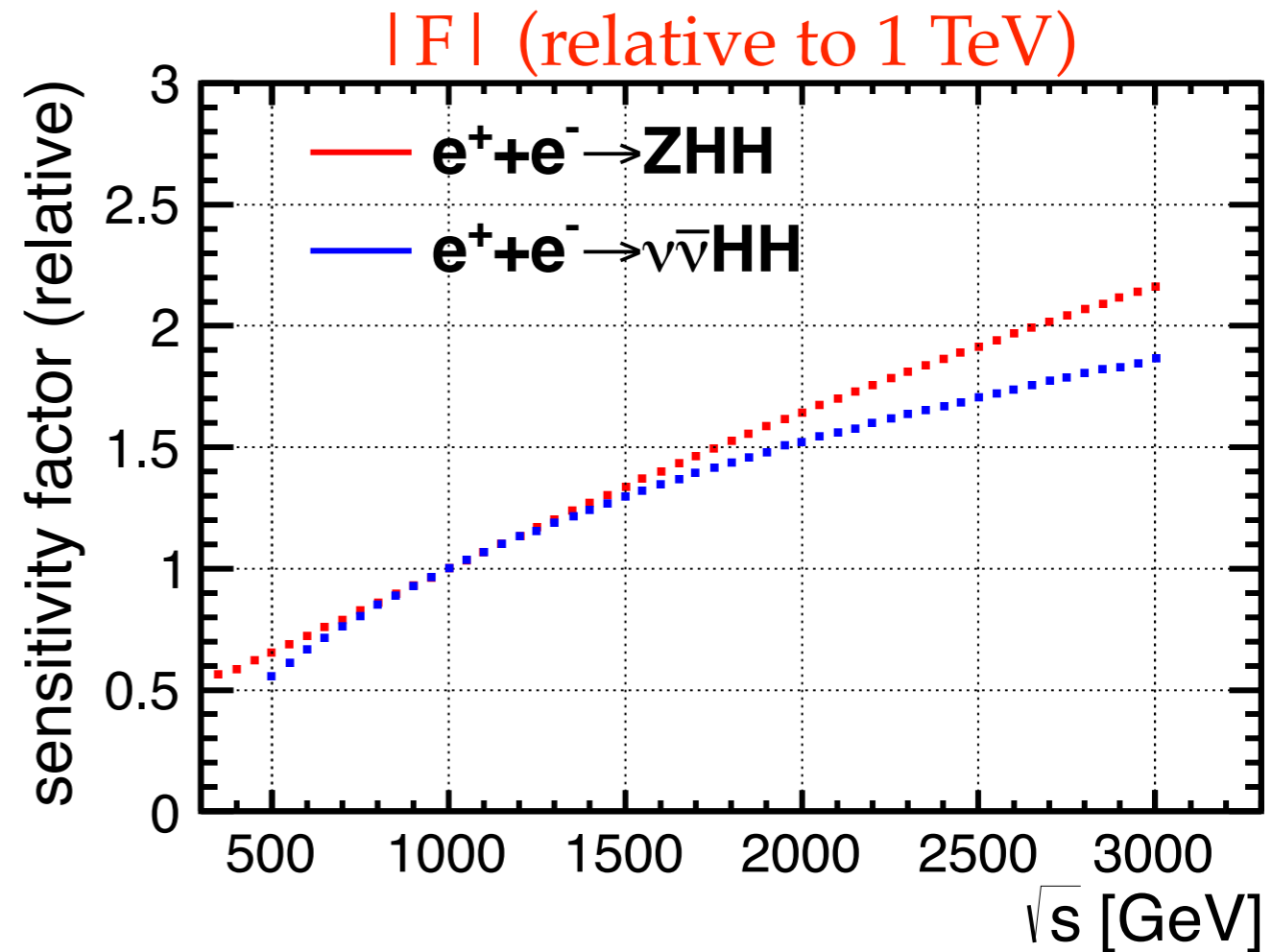
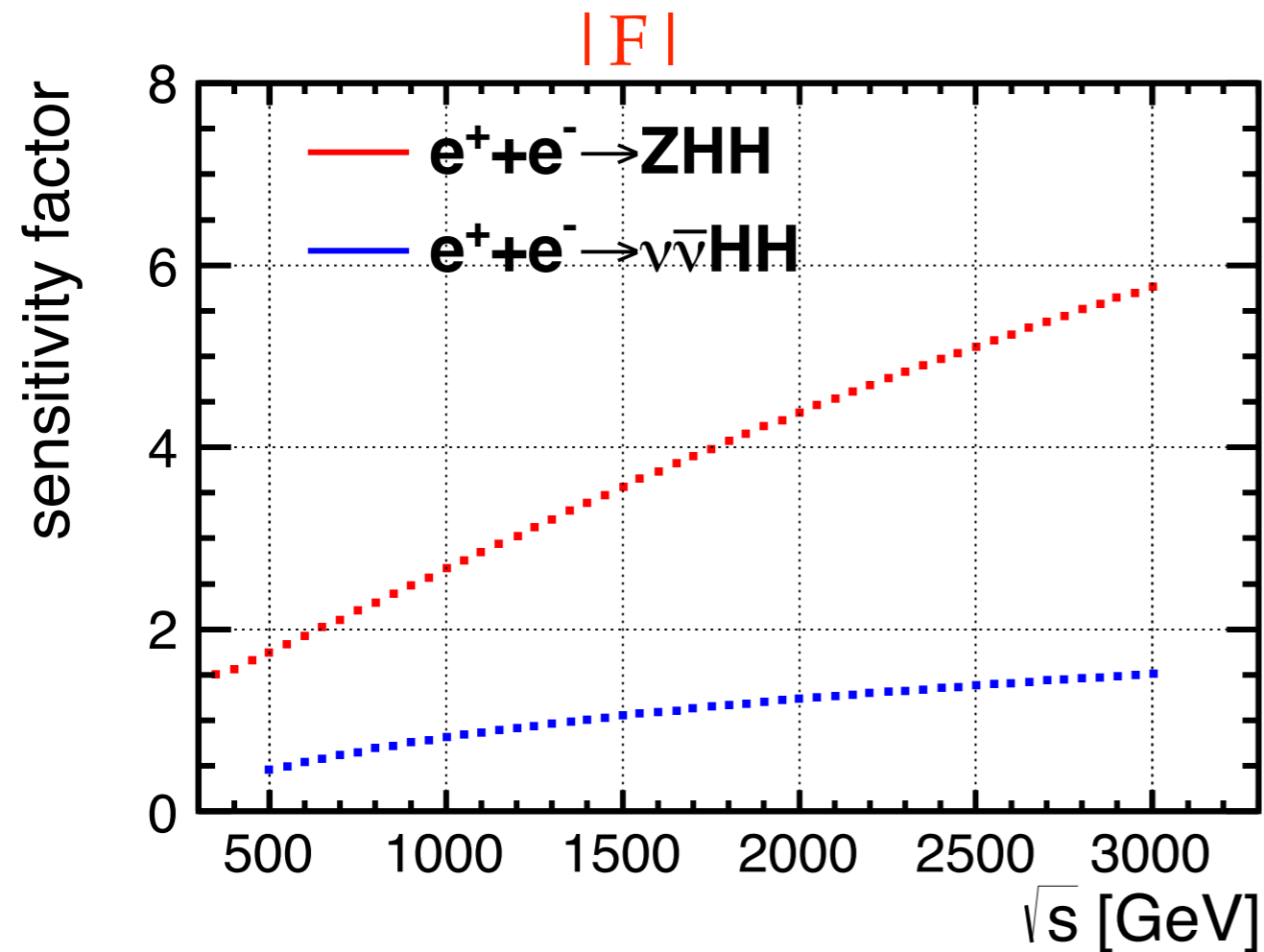


# Higgs self-coupling: from $\sigma$ to $\lambda$

$$\frac{\delta\lambda}{\lambda} = F \cdot \frac{\delta\sigma}{\sigma}$$

$$F = \frac{\sigma}{2S\lambda^2 + I\lambda}$$

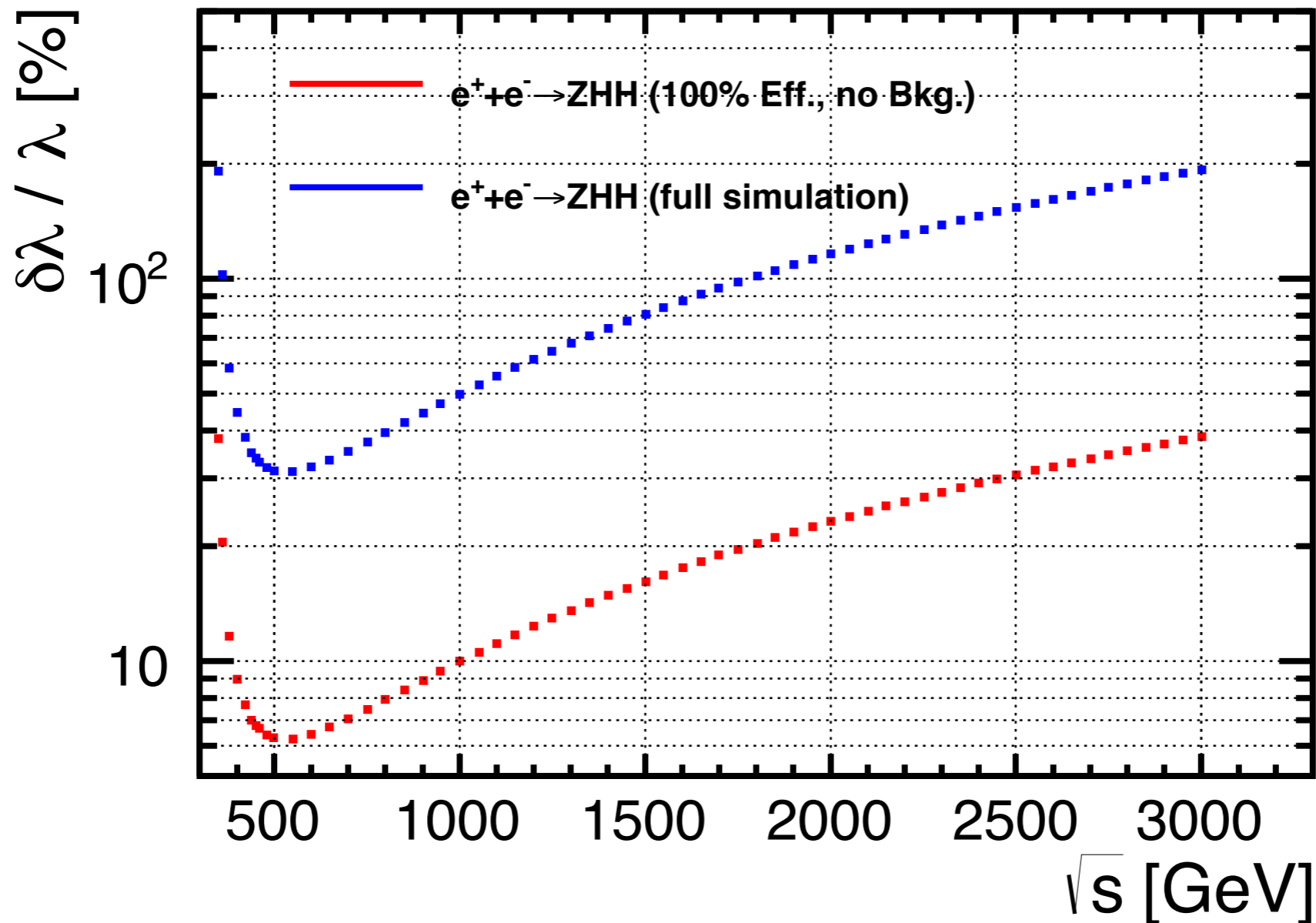
sensitivity factor





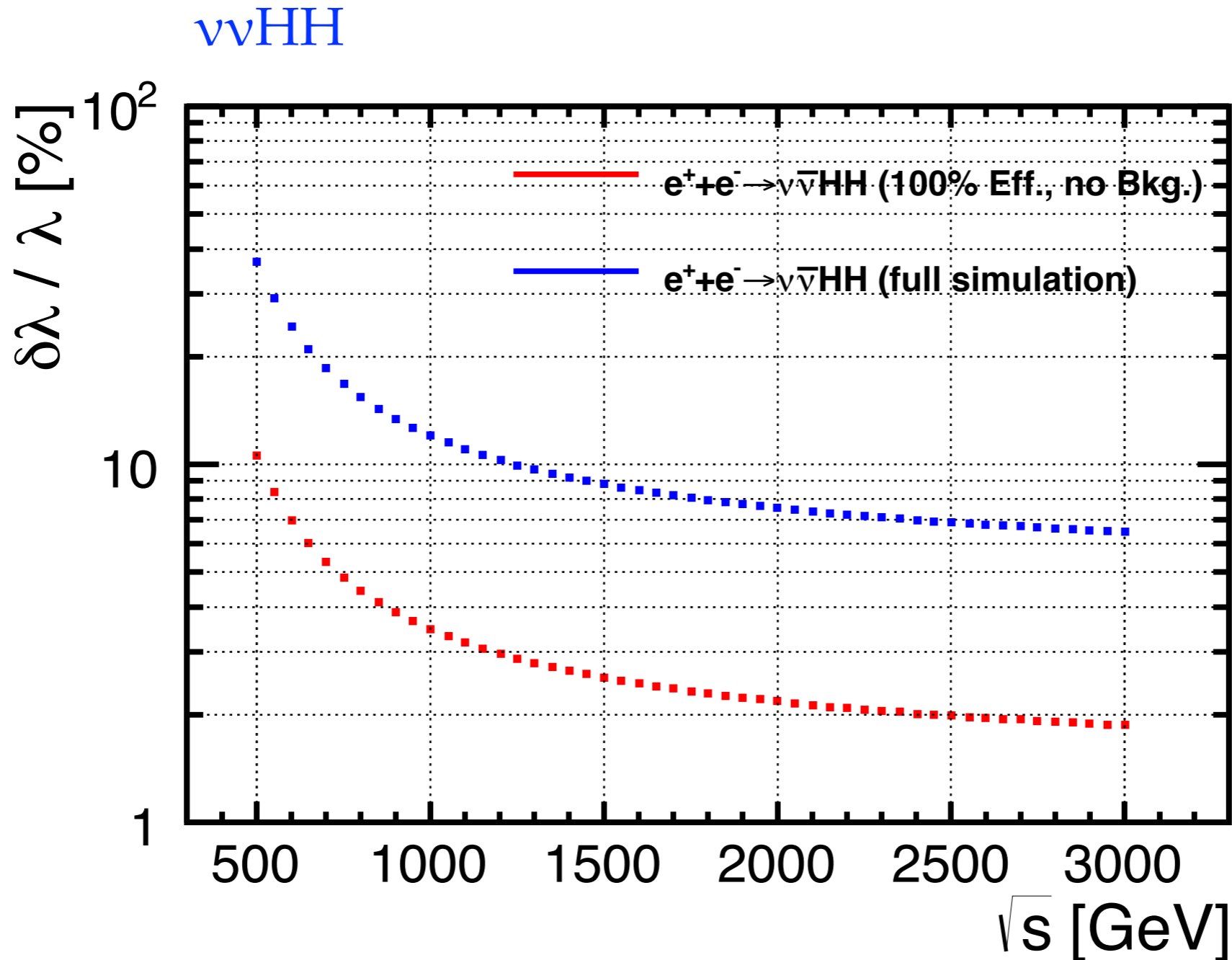
# expected precision of $\lambda$ : impact from analysis & $\sqrt{s}$

ZHH



- ▶ **for ZHH: 500 GeV** is optimal,  $\delta\lambda/\lambda \sim 6\% : 30\%$ , mild dependence between around **500-600 GeV**, significantly worse at much lower or higher  $\sqrt{s}$
- ▶ **huge room for improvement** (waiting for you to narrow down the gap)

# expected precision of $\lambda$ : impact from analysis & $\sqrt{s}$

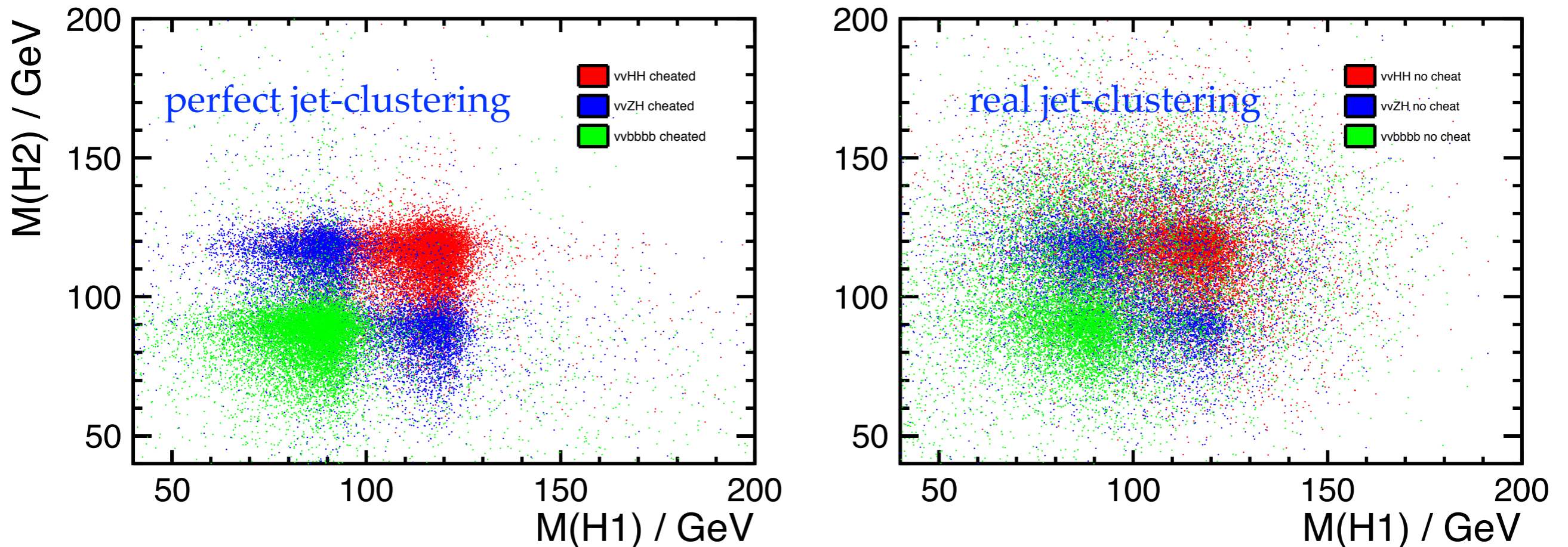


- ▶ **for  $\nu\nu HH$** : significantly better going from 500 GeV to **1 TeV**,  $\delta\lambda/\lambda \sim 10\%$  achievable when  $\sqrt{s} \geq 1\text{TeV}$ ;
- ▶ better at higher  $\sqrt{s}$ , not drastically, from 1 TeV to 3 TeV, improved by 50%

# one limiting factor: jet-clustering algorithm

ZHH->vvbbbb (BG: ZZH and ZZZ)

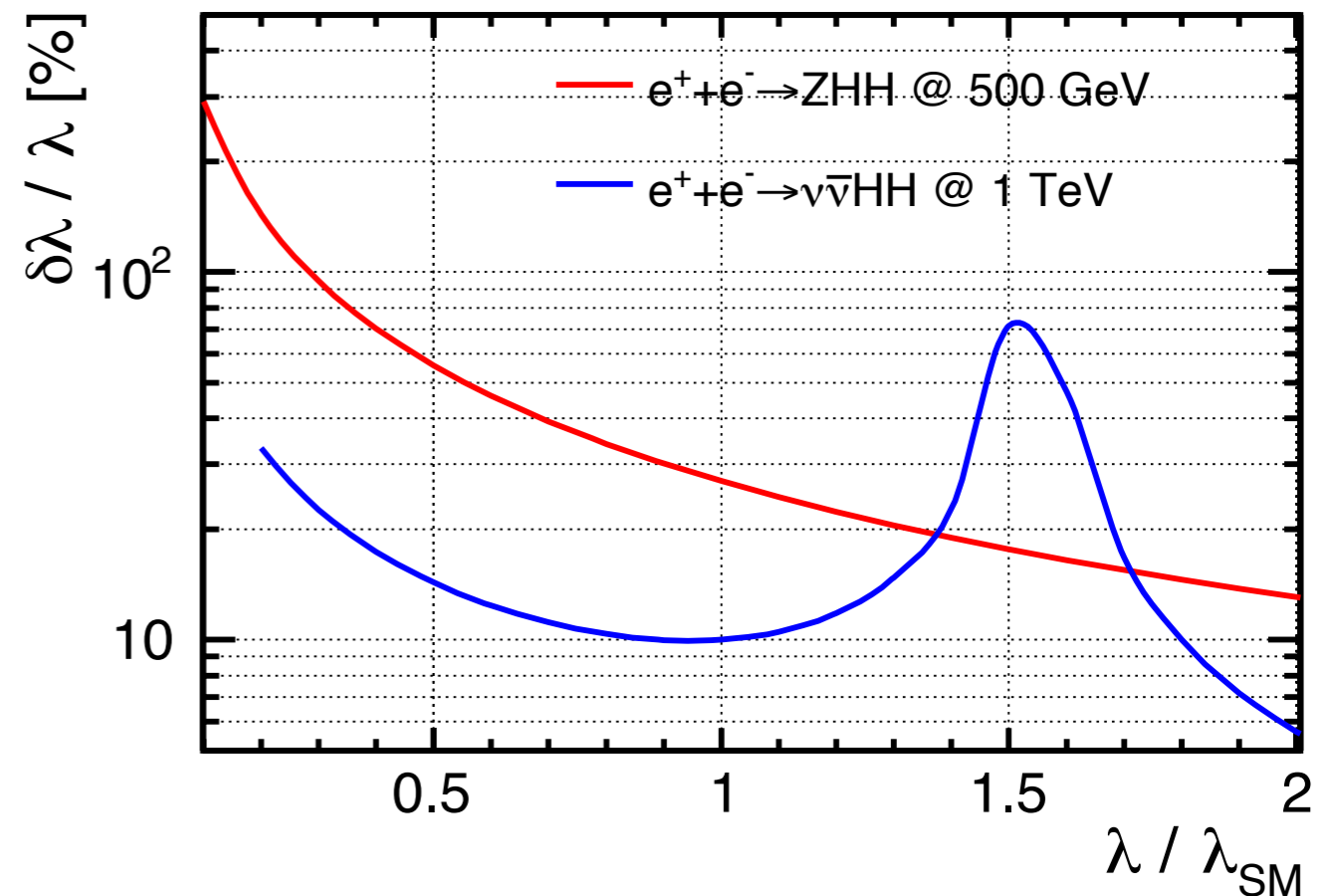
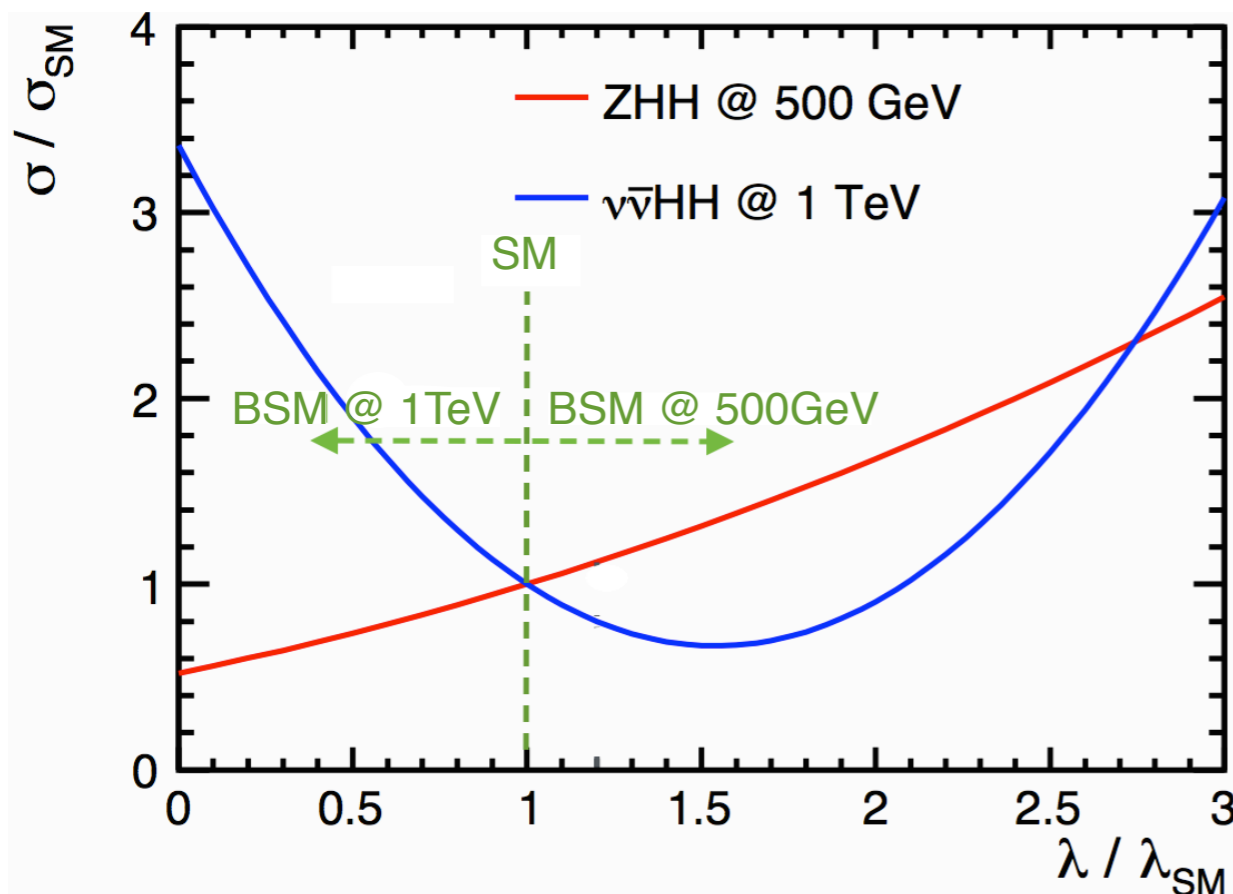
scatter plot of two Higgs masses



- ▶ the **mis-clustering** of particles degrades significantly the separation between signal and BG.
- ▶ it is studied that using perfect **color-singlet jet-clustering** can improve  $\delta\lambda/\lambda$  by **40%**!

# Higgs self-coupling: when $\lambda_{HHH} \neq \lambda_{SM}$ ?

- ▶ **constructive** interference in **ZHH**, while **destructive** in  **$\nu\bar{\nu}HH$**  (& LHC): **complementarity** between ILC & LHC, between  $\sqrt{s} \sim 500$  GeV and  $>1$ TeV
- ▶ if  $\lambda_{HHH} / \lambda_{SM} = 2$ , Higgs self-coupling can be measured to  **$\sim 15\%$**  using ZHH at 500 GeV  $e^+e^-$

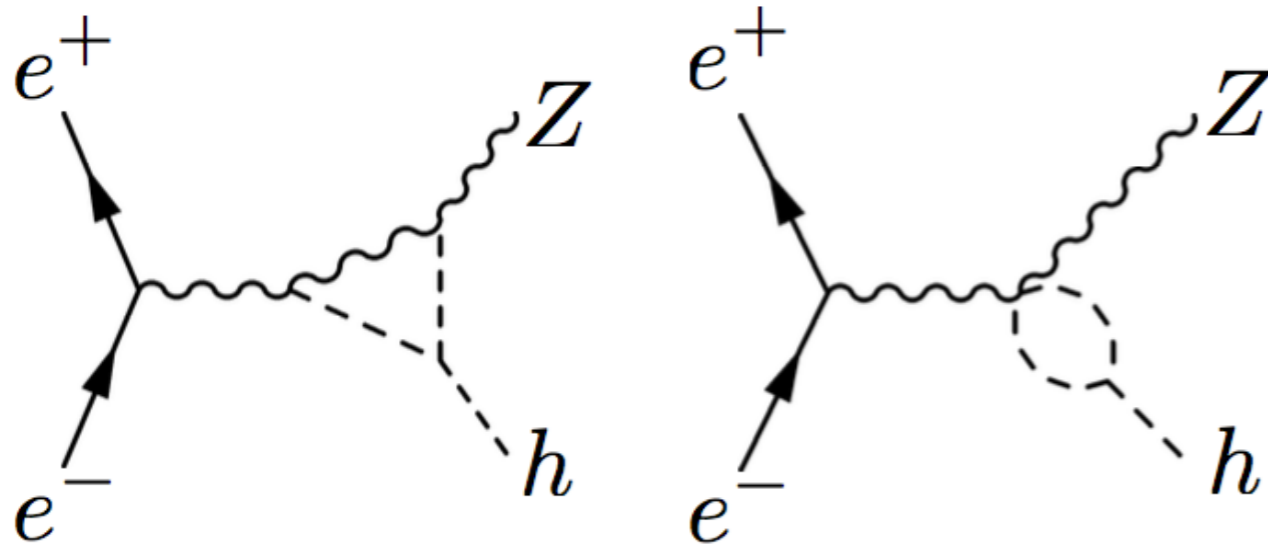


references for  
large deviations

e.g.

Grojean, et al., PRD71, 036001; Kanemura, et al., 1508.03245; Kaori, Senaha, PHLTA,B747,152; Perelstein, et al., JHEP 1407, 108

# Higgs self-coupling: indirect determination

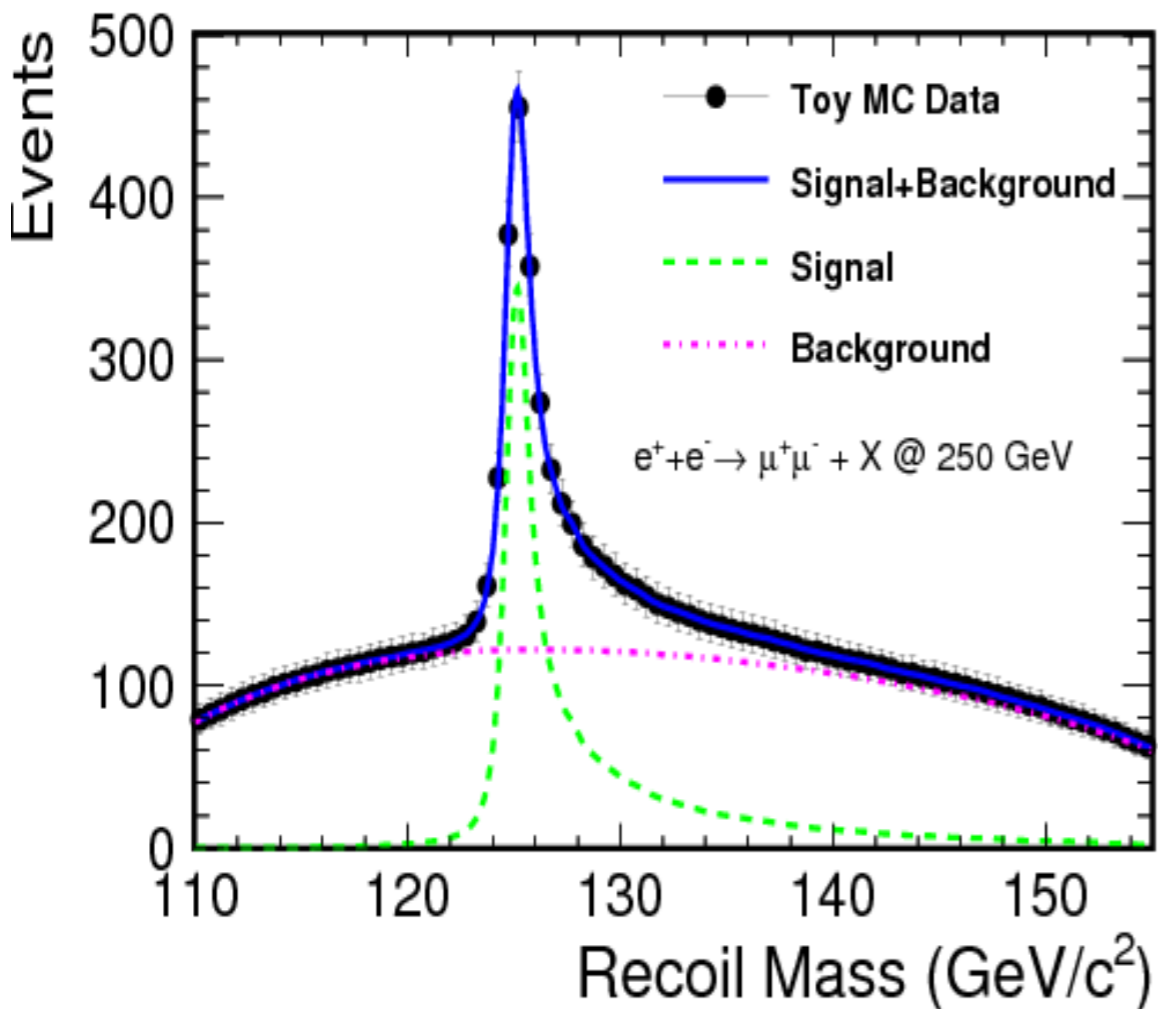


McCullough, arXiv:1312.3322

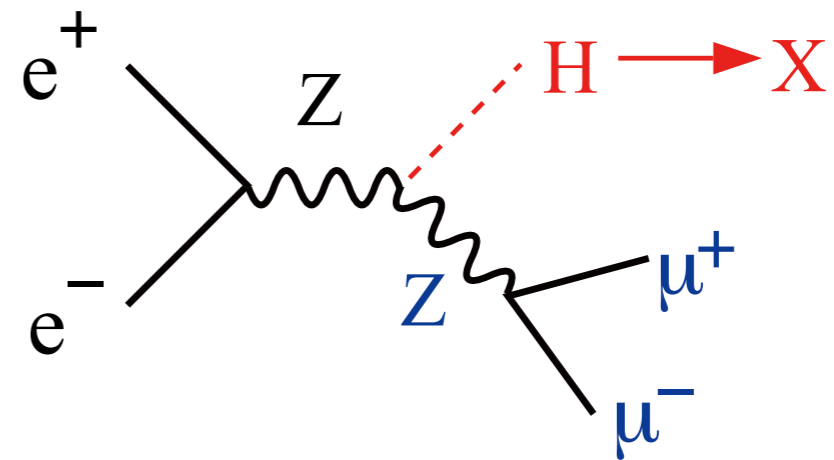
$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

- ▶ if only  $\delta h$  is deviated  $\rightarrow \delta h \sim 28\%$
- ▶ if both  $\delta z$  and  $\delta h$  deviated  $\rightarrow \delta h \sim 90\%$
- ▶  $\delta\sigma$  could receive contributions from many other sources
- ▶ open question: what happens after taking into account all possible modifications? (Lecture 2)
  - can we measure quartic Higgs self-coupling?

## (ii-2) inclusive $\sigma_{ZH}$ : unique key @ $e^+e^-$



$$\Delta m_H = 14 \text{ MeV}$$

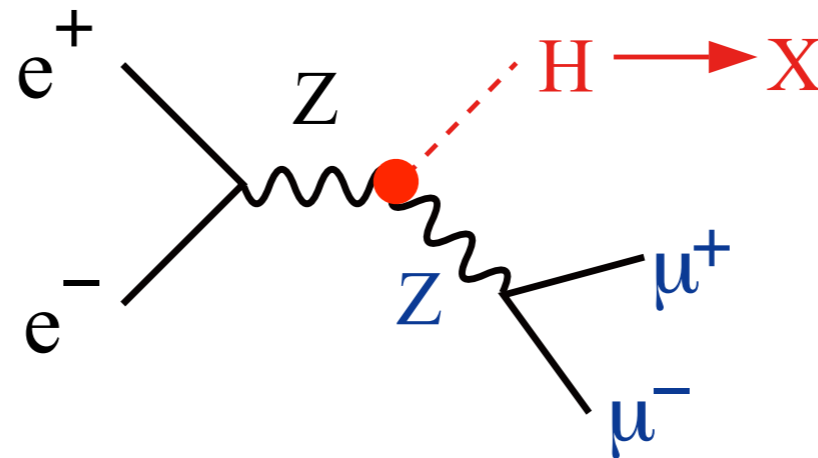


$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

- ▶ well defined initial states at  $e^+e^-$
- ▶ recoil mass technique  $\rightarrow$  tag Z only
- ▶ Higgs is tagged without looking into H decay
- ▶ **absolute cross section** of  $e^+e^- \rightarrow ZH$

for  $Z \rightarrow ll$  (leptonic recoil), Yan et al, arXiv:1604.07524;  
for  $Z \rightarrow qq$  (hadronic recoil), Thomson, arXiv:1509.02853

what does model independence mean?



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

- ▶ meas. of  $\sigma_{ZH}$  doesn't depend on how Higgs decays
- ▶ meas. of  $\sigma_{ZH}$  doesn't depend on underlying  $HZZ$  vertex

is it really possible?

## independent of H decay modes?

$$e^+ + e^- \rightarrow ZH \rightarrow l^+ l^- / q\bar{q} + X$$

- ▶ this question is almost equivalent to whether we can tag the Z decay products unambiguously
- ▶ might be easy in Z->ll, certainly not trivial in Z->qq
- ▶ even in Z->ll mode, we know there can be isolated leptons from Higgs decay, e.g. H->WW\*/τ τ/ZZ, which get mis-identified as leptons from Z decay
- ▶ keep in mind we are targeting 0.1-1% precision measurement



## efficiencies breakdown (leptonic recoil)

H $\rightarrow$ XX	bb	cc	gg	$\tau\tau$	WW*	ZZ*	$\gamma\gamma$	$\gamma Z$
BR (SM)	57.8%	2.7%	8.6%	6.4%	21.6%	2.7%	0.23%	0.16%
Lepton Finder	93.70%	93.69%	93.40%	94.02%	94.04%	94.36%	93.75%	94.08%
Lepton ID+Precut	93.68%	93.66%	93.37%	93.93%	93.94%	93.71%	93.63%	93.22%
$M_{l+l-} \in [73, 120]$ GeV	89.94%	91.74%	91.40%	91.90%	91.82%	91.81%	91.73%	91.47%
$p_T^{l+l-} \in [10, 70]$ GeV	89.94%	90.08%	89.68%	90.18%	90.04%	90.16%	89.99%	89.71%
$ \cos \theta_{\text{miss}}  < 0.98$	89.94%	90.08%	89.68%	90.16%	90.04%	90.16%	89.91%	89.41%
BDT $> -0.25$	88.90%	89.04%	88.63%	89.12%	88.96%	89.11%	88.91%	88.28%
$M_{\text{rec}} \in [110, 155]$ GeV	88.25%	88.35%	87.98%	88.43%	88.33%	88.52%	88.21%	87.64%

- ▶ every cut is applied very carefully to avoid large bias, still  $\sim 1\%$
- ▶ nevertheless, it becomes almost a paradox:
  - ☑ no cut, no bias; looser cuts, less bias
  - ☑ extremely tighter cuts, less bias;
  - ☑ too loose or too tight cuts  $\rightarrow$  remain too much background or too little signal  $\rightarrow$  bad precision measurement

# efficiencies breakdown (hadronic recoil)

Decay mode	$\epsilon_{\mathcal{L}>0.65}^{\text{vis.}}$	$\epsilon_{\mathcal{L}>0.60}^{\text{invis.}}$	$\epsilon^{\text{vis.}} + \epsilon^{\text{invis.}}$
H $\rightarrow$ invis.	<0.1 %	23.5 %	23.5 %
H $\rightarrow$ q $\bar{q}$ /gg	22.6 %	<0.1 %	22.6 %
H $\rightarrow$ WW*	22.1 %	0.1 %	22.2 %
H $\rightarrow$ ZZ*	20.6 %	1.1 %	21.7 %
H $\rightarrow$ $\tau^+\tau^-$	25.3 %	0.2 %	25.5 %
H $\rightarrow$ $\gamma\gamma$	25.7 %	<0.1 %	25.7 %
H $\rightarrow$ Z $\gamma$	18.6 %	0.3 %	18.9 %
H $\rightarrow$ WW* $\rightarrow$ q $\bar{q}$ q $\bar{q}$	20.8 %	<0.1 %	20.8 %
H $\rightarrow$ WW* $\rightarrow$ q $\bar{q}$ l $\nu$	23.3 %	<0.1 %	23.3 %
H $\rightarrow$ WW* $\rightarrow$ q $\bar{q}$ $\tau\nu$	23.1 %	<0.1 %	23.1 %
H $\rightarrow$ WW* $\rightarrow$ l $\nu$ l $\nu$	26.5 %	0.1 %	26.5 %
H $\rightarrow$ WW* $\rightarrow$ l $\nu$ $\tau\nu$	21.1 %	0.5 %	21.6 %
H $\rightarrow$ WW* $\rightarrow$ $\tau\nu$ $\tau\nu$	16.3 %	2.3 %	18.7 %

► relative bias can be as large as **~15%**

## a nice trick: categorization

$$\sigma_{ZH} = \sigma^{cat1} + \sigma^{cat2} + \sigma^{cat3} + \sigma^{cat4} + \dots$$

- ▶ if we have a complete list of categories
- ▶ then we only need to keep all selection cuts independent of decay mode in each category;
- ▶ selections cuts among categories can be very different

for example

$$\sigma_{ZH} = \sigma^{H \rightarrow \text{invisible}} + \sigma^{H \rightarrow \text{visible}}$$

## a realistic solution: make use of individual BR measurement

$$\sigma_{ZH} = \frac{N_S}{R_f L \bar{\epsilon}} \quad \bar{\epsilon} \equiv \sum_i B_i \epsilon_i$$

$N_S$ : # of signal

$R_f$ : BR of  $Z \rightarrow ff$

$L$ : int. luminosity

$B_i$ : BR of H decay mode  $i$

$\epsilon_i$ : efficiency of mode  $i$

- ▶ if every  $\epsilon_i$  is same  $\rightarrow \sum B_i = 1$ ; no need for any knowledge about  $B_i$
- ▶ nevertheless, we can measure many of the  $\sigma \times B_i$ ; assume  $i=1..n$  is known with  $\Delta B_i$ ;  $i=n+1, \dots$  is unknown, sum up to  $B_x$ ;

known modes

systematic error to  $\sigma_{ZH}$

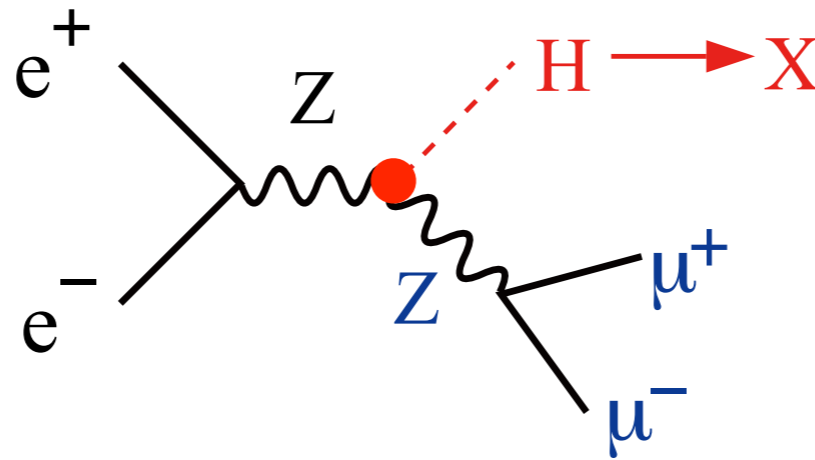
unknown modes

$$\frac{\Delta \sigma_{ZH}}{\sigma_{ZH}} = \frac{\Delta \bar{\epsilon}}{\bar{\epsilon}} = \sqrt{\sum_{i=1}^n \Delta B_i^2 \left( \frac{\epsilon_i}{\epsilon_0} - 1 \right)^2}$$

$$\frac{\Delta \sigma_{ZH}}{\sigma_{ZH}} = \frac{\Delta \bar{\epsilon}}{\bar{\epsilon}} < \sum_{i=n+1} B_i \frac{\delta \epsilon_{\max}}{\epsilon_0} = B_x \frac{\delta \epsilon_{\max}}{\epsilon_0}$$

- ▶ leptonic recoil, demonstrated possible  $\delta \sigma_{ZH} \sim 0.1\%$  for  $B_x < 10\%$
- ▶ hadronic recoil, still need more work for  $\delta \sigma_{ZH} < 1\%$  for  $B_x < 10\%$

## independent of HZZ vertex?

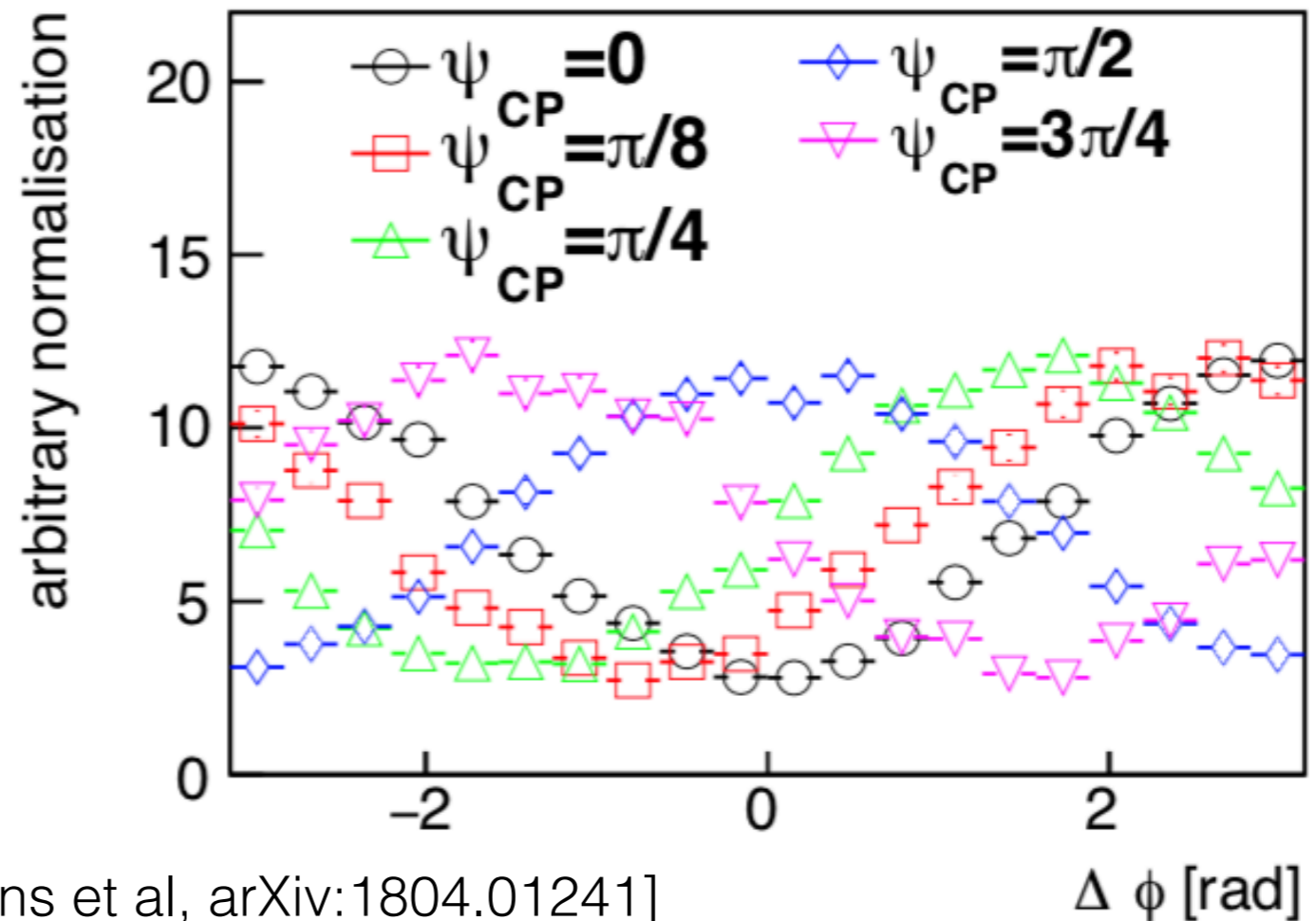
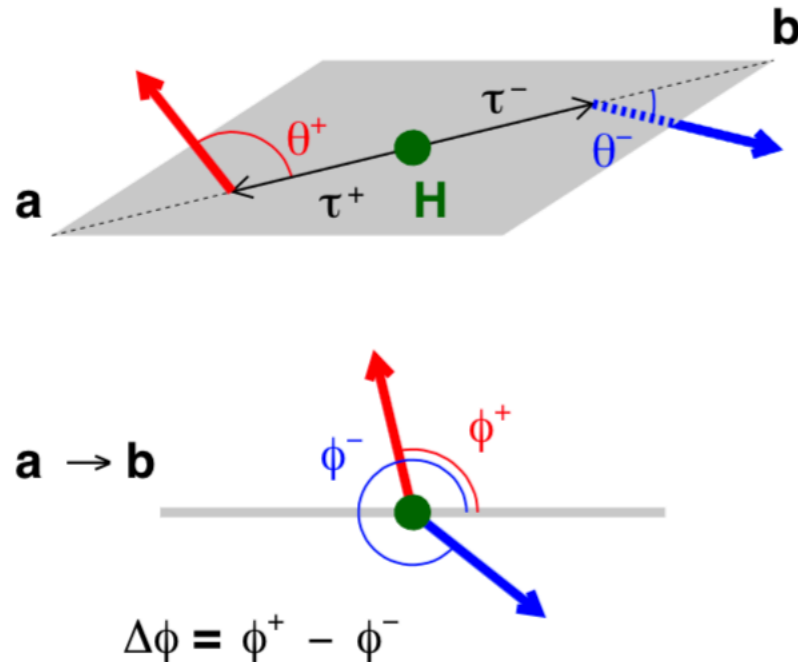


- ▶ different HZZ vertex might change angular distributions of Z
  - ▶ hence, this question is equivalent to whether the selection cuts are democratic for all production angles of Z
- open question, this is not sufficiently studied yet**

## (ii-3) Higgs CP in $H \rightarrow \tau^+ \tau^-$

► CP is essential to understand structures of all Higgs couplings

$$L_{Hff} = -\frac{m_f}{v} H \bar{f} (\cos \Phi_{CP} + i \gamma^5 \sin \Phi_{CP}) f$$



$$\Delta\Phi_{CP} \sim 4.3^\circ$$

[Jeans et al, arXiv:1804.01241]

$\Delta\phi$  [rad]

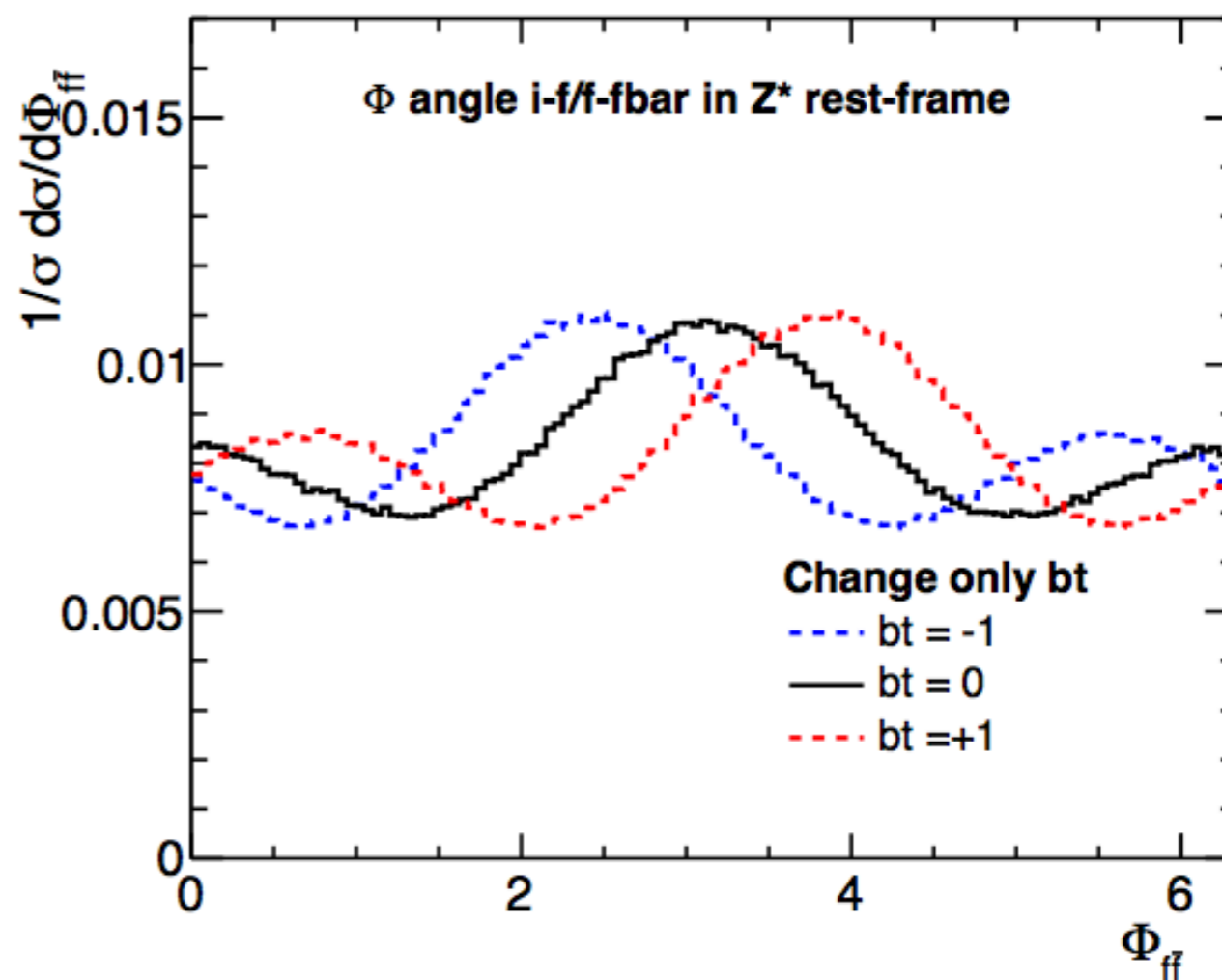
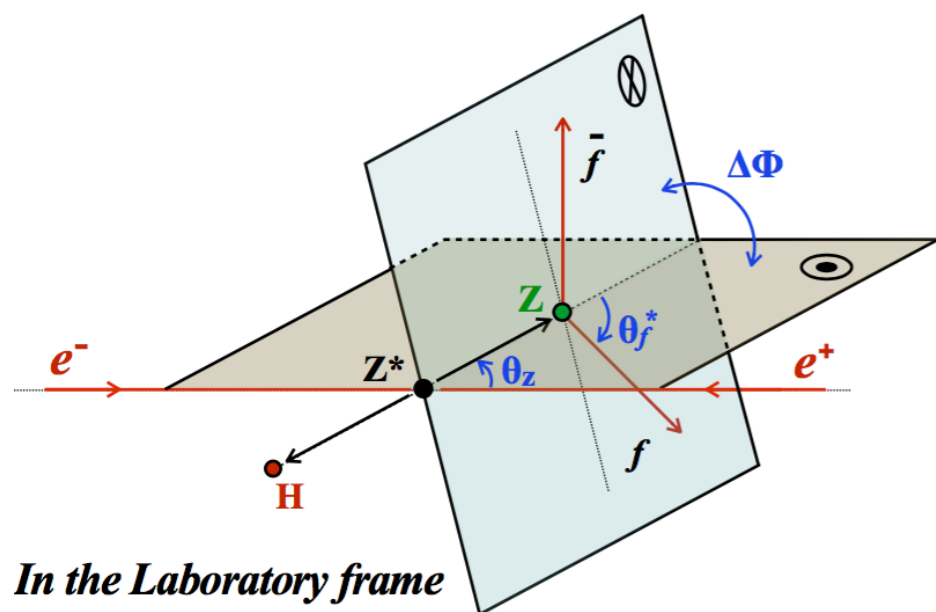
- ❑ is it good enough for discovering EW Baryogenesis?
- ❑ large room to improve in experiment

### (ii-3) Higgs CP in HZZ coupling

$$L_{hZZ} = M_Z^2 \left( \frac{1}{v} + \frac{a}{\Lambda} \right) h Z_\mu Z^\mu + \frac{b}{2\Lambda} h Z_{\mu\nu} Z^{\mu\nu} + \frac{\tilde{b}}{2\Lambda} h Z_{\mu\nu} \tilde{Z}_{\mu\nu}$$

(CP-odd)

$$e^+ + e^- \rightarrow Zh \rightarrow f \bar{f} h$$



@  $\sqrt{s} = 250\text{GeV}$

$$\Delta \tilde{b} \sim 0.016 \quad (\text{for } \Lambda = 1\text{TeV})$$

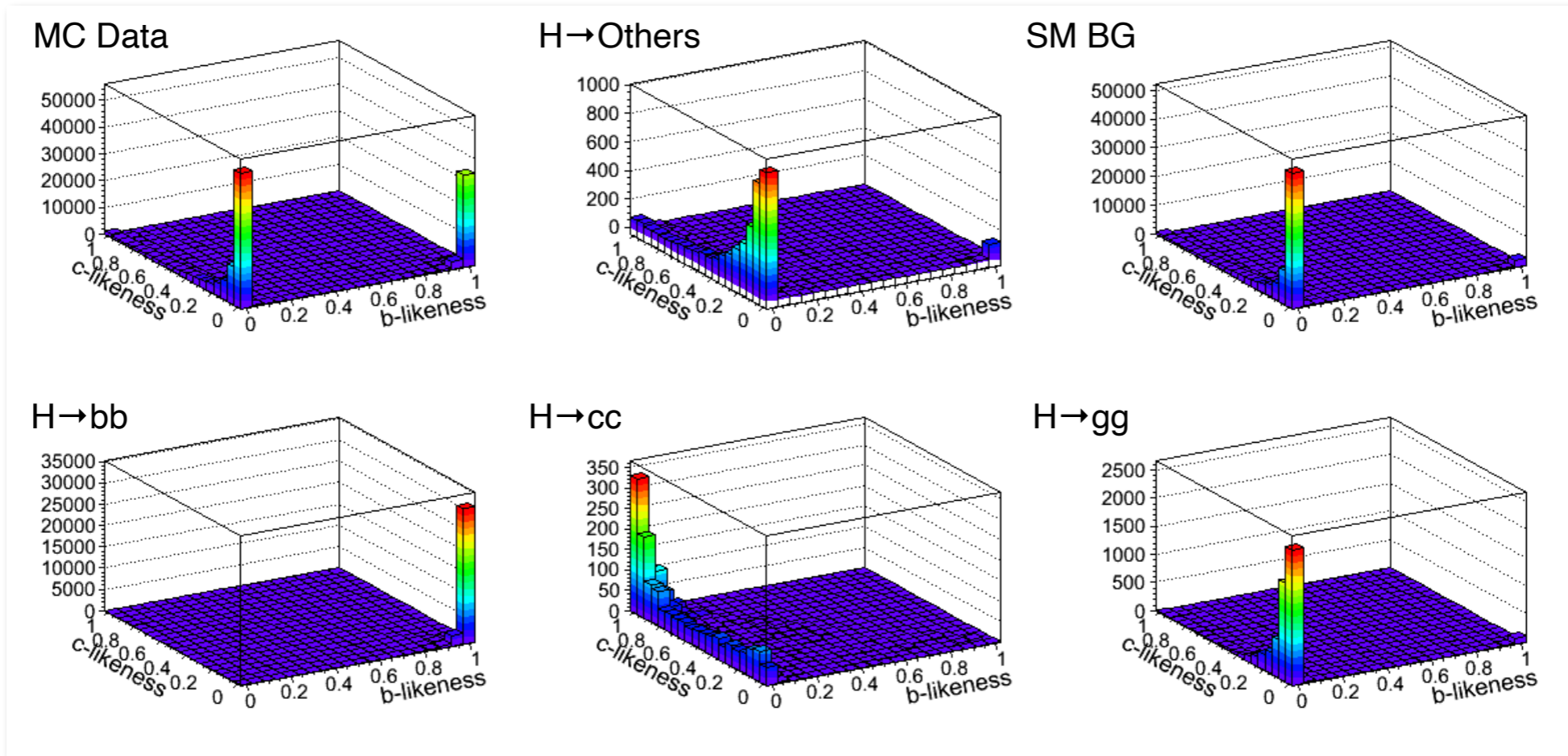
[Ogawa et al, arXiv:1712.09772]



## (ii-4) Higgs direct couplings to bb, cc and gg

- ▶ clean environment at e+e-; excellent b- and c-tagging performance
- ▶ bb/cc/gg modes can be separated simultaneously by template fitting

**e+e- → ZH → ff(jj): b-likeness .vs. c-likeness**



**directly  
measured**



$$\begin{aligned} \sigma_{ZH} \cdot \text{Br}(H \rightarrow b\bar{b}) &\propto g_{HZZ}^2 g_{Hbb}^2 / \Gamma_H \\ \sigma_{ZH} \cdot \text{Br}(H \rightarrow c\bar{c}) &\propto g_{HZZ}^2 g_{Hcc}^2 / \Gamma_H \\ \sigma_{ZH} \cdot \text{Br}(H \rightarrow gg) &\propto g_{HZZ}^2 g_{Hgg}^2 / \Gamma_H \end{aligned}$$

**with  $\Gamma_H$**



**$\delta g_{Hbb}$**

**$\delta g_{Hcc}$**

**$\delta g_{Hgg}$**



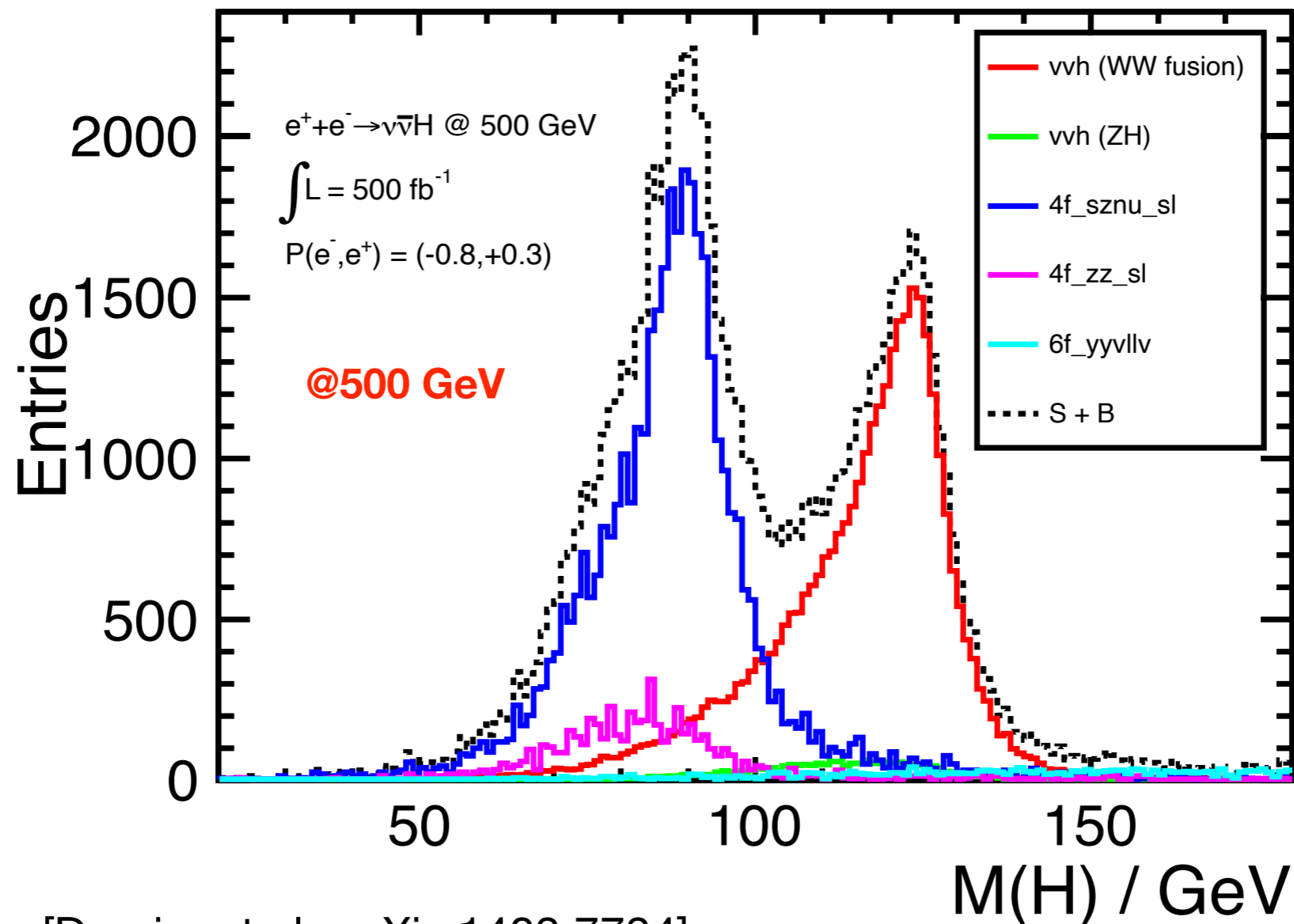
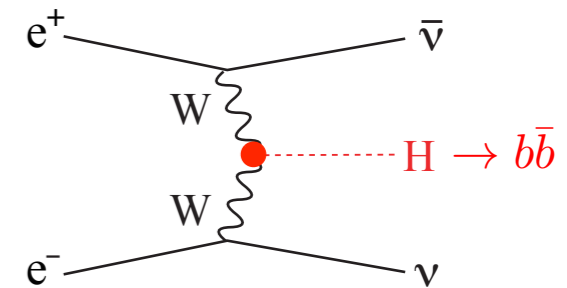
## (ii-5) WW-fusion channel & Higgs total width $\Gamma_H$

$$\Gamma_H = \frac{\Gamma_{HZZ}}{\text{Br}(H \rightarrow ZZ^*)} \propto \frac{g_{HZZ}^2}{\text{Br}(H \rightarrow ZZ^*)}$$

—> Br(H->ZZ\*) very small

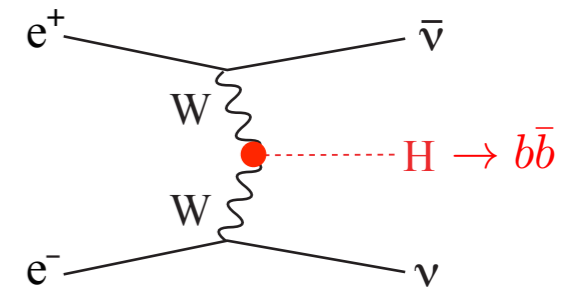
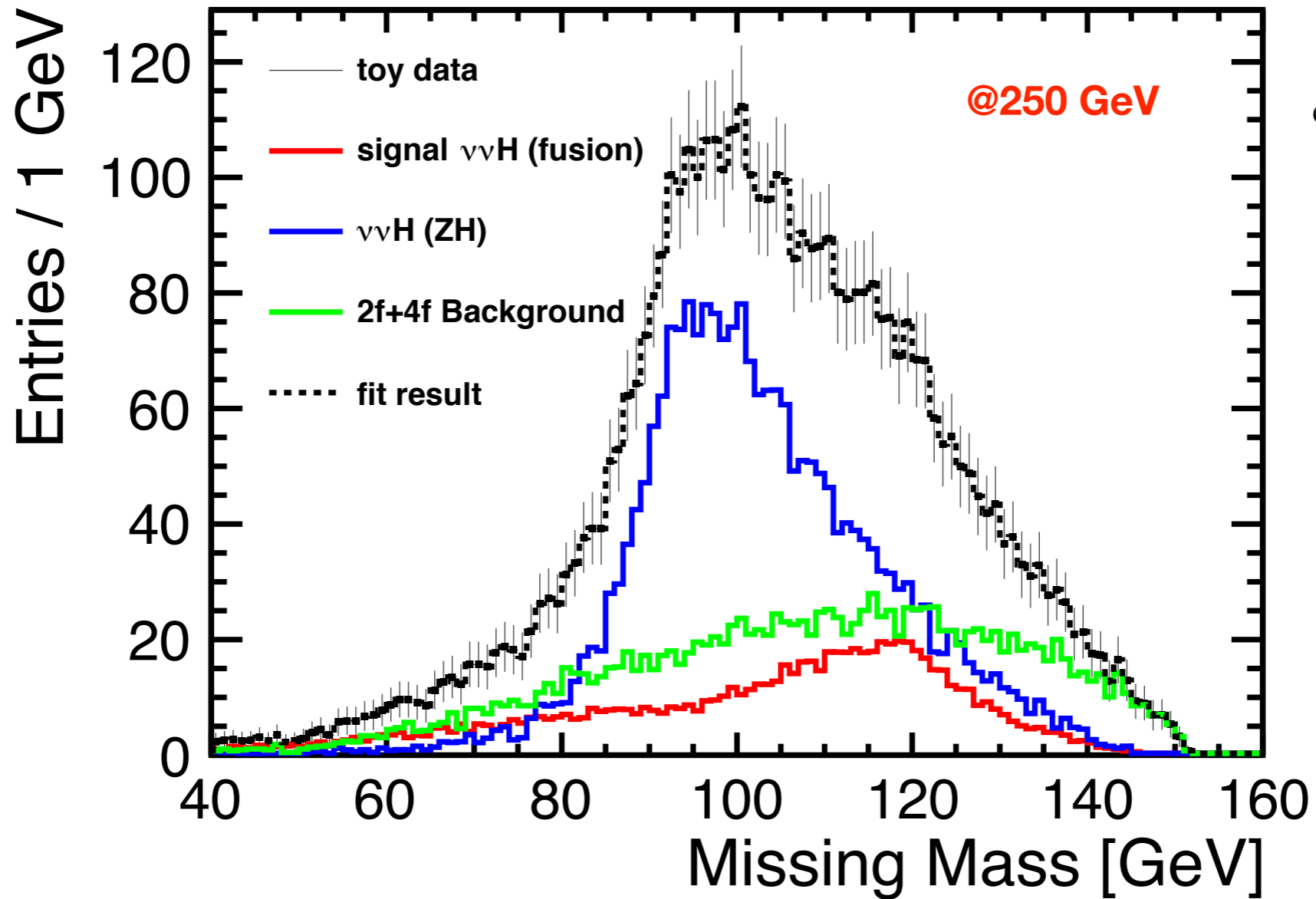
★ 
$$\Gamma_H = \frac{\Gamma_{HWW}}{\text{Br}(H \rightarrow WW^*)} \propto \frac{g_{HWW}^2}{\text{Br}(H \rightarrow WW^*)}$$

—> better option!



[Duerig, et al., arXiv:1403.7734]

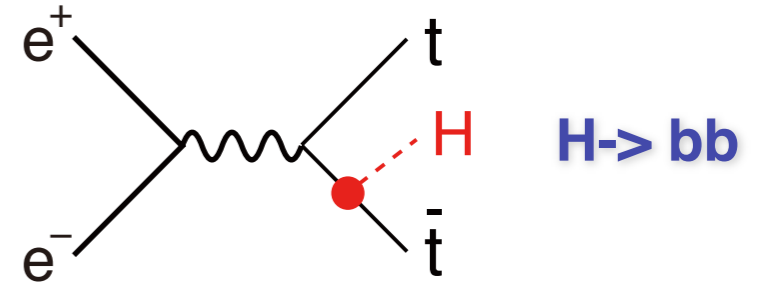
very different at  $\sqrt{s}=250$  GeV



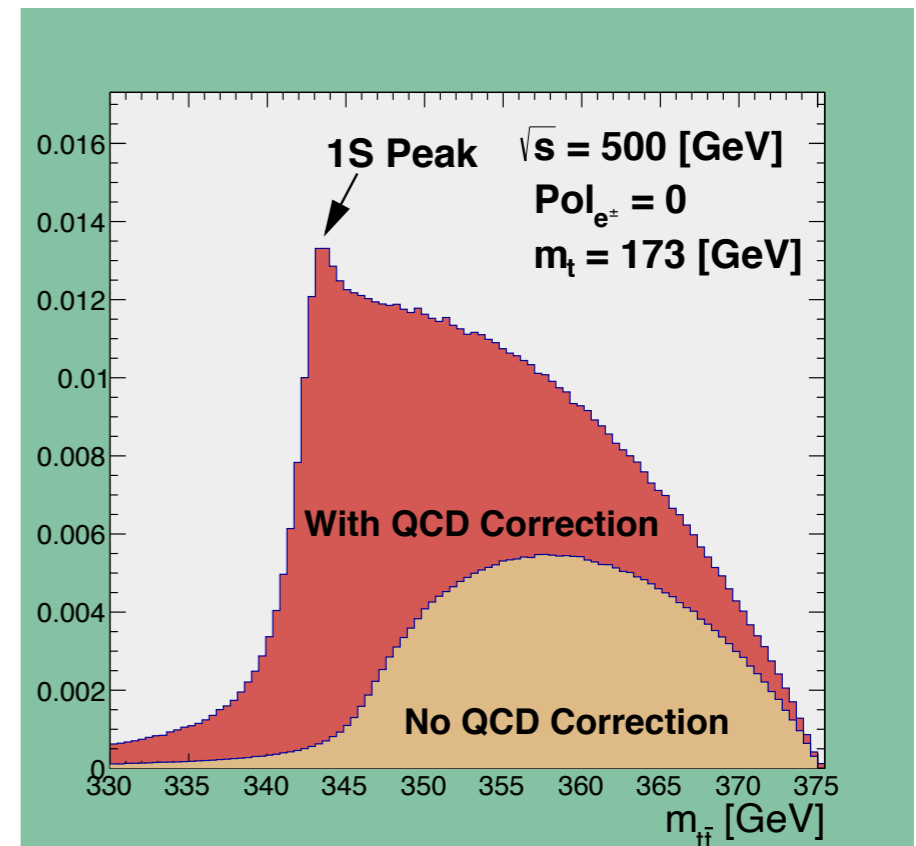
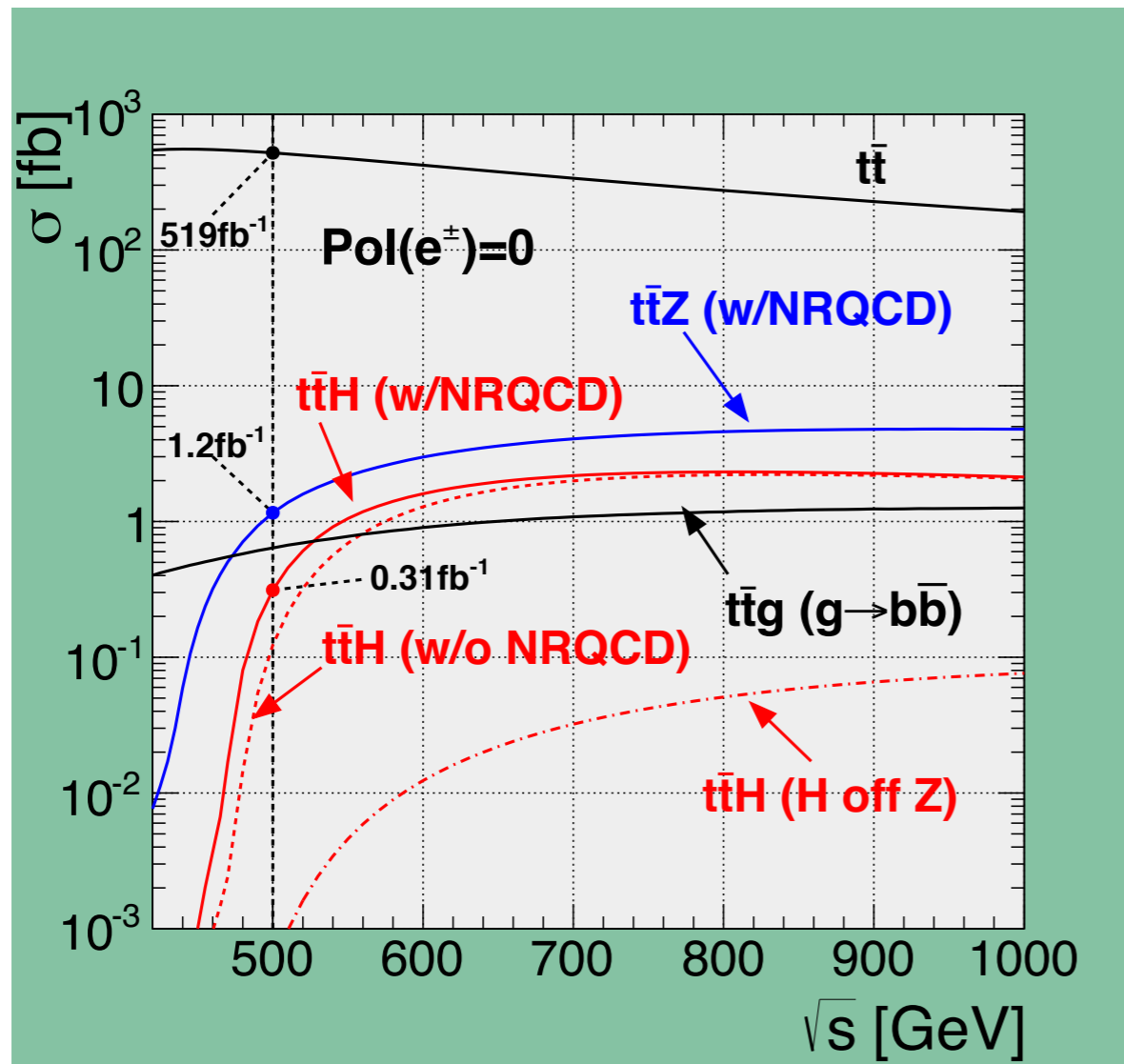
$\rho = -34\%$  correlation between  
 $\sigma_{\nu\nu H} \times BR(H \rightarrow b\bar{b})$  and  $\sigma_{ZH} \times BR(H \rightarrow b\bar{b})$

## (ii-6) Top-Yukawa coupling

- ▶ largest Yukawa coupling; crucial role
- ▶ non-relativistic  $t\bar{t}$  bound state correction: enhancement by  $\sim 2$  at 500 GeV
- ▶ Higgs CP measurement

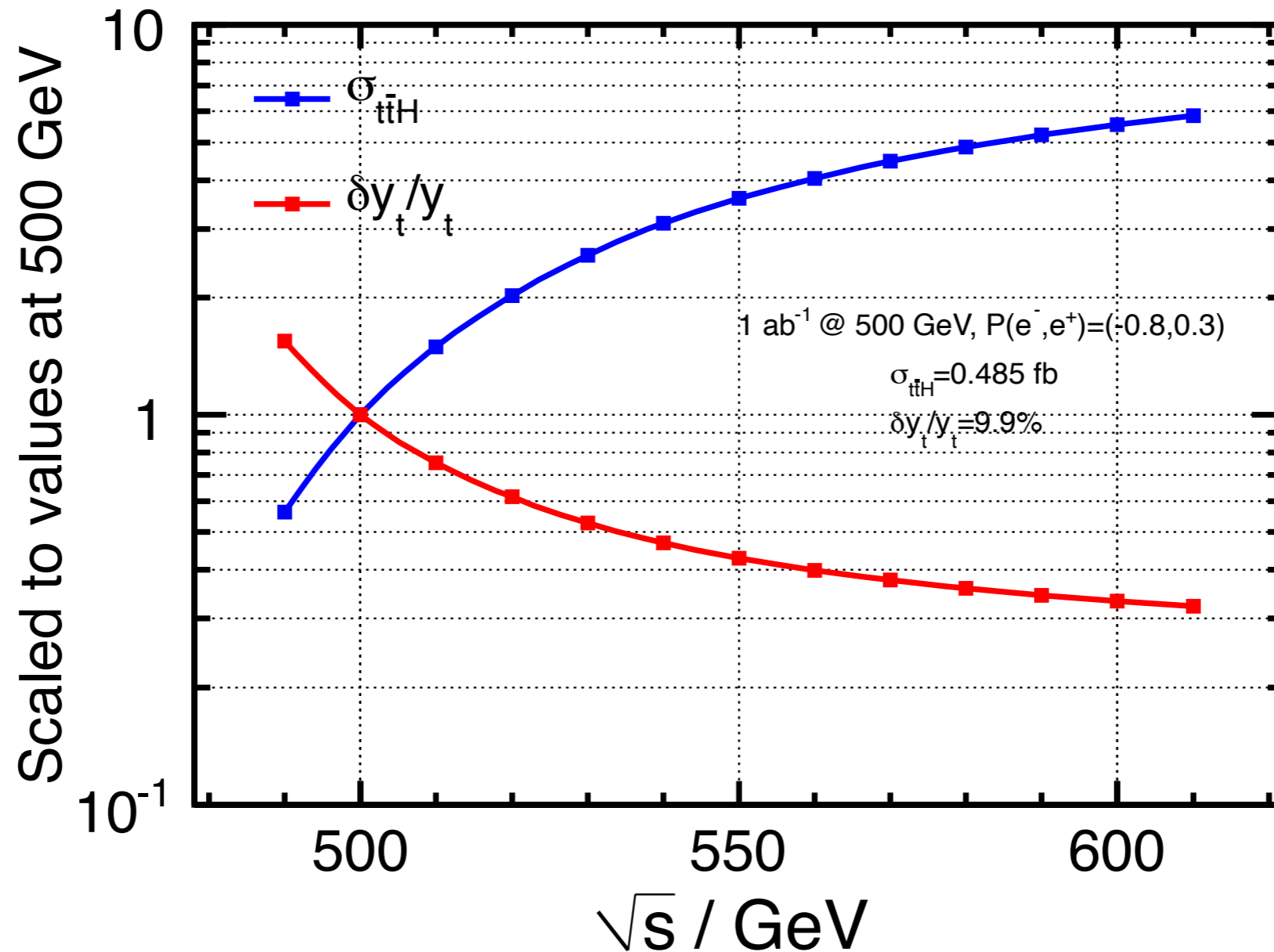


$\Delta g_{ttH} / g_{ttH}$	500 GeV	+ 1 TeV
ILC	6.3%	1.5%



Yonamine, et al., PRD84, 014033;  
Price, et al., Eur. Phys. J. C75 (2015) 309

# Top-Yukawa coupling: impact of $\sqrt{s}$



[Y. Sudo]

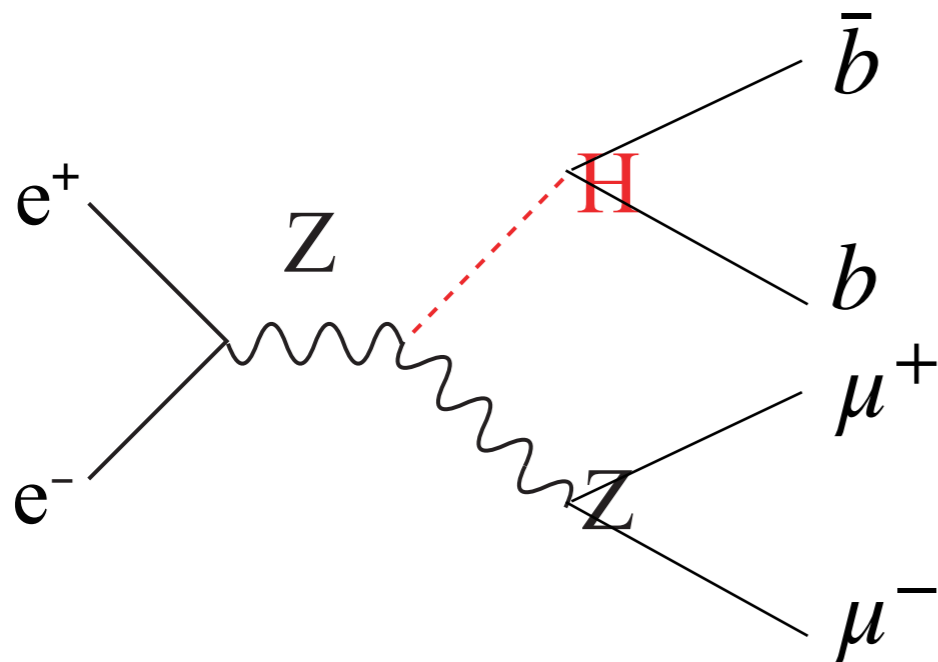
► increase  $\sqrt{s}$  slightly by 50 GeV can improve  $\delta y_t$  by a factor of 2

(ii-7) how do we actually determine Higgs couplings?

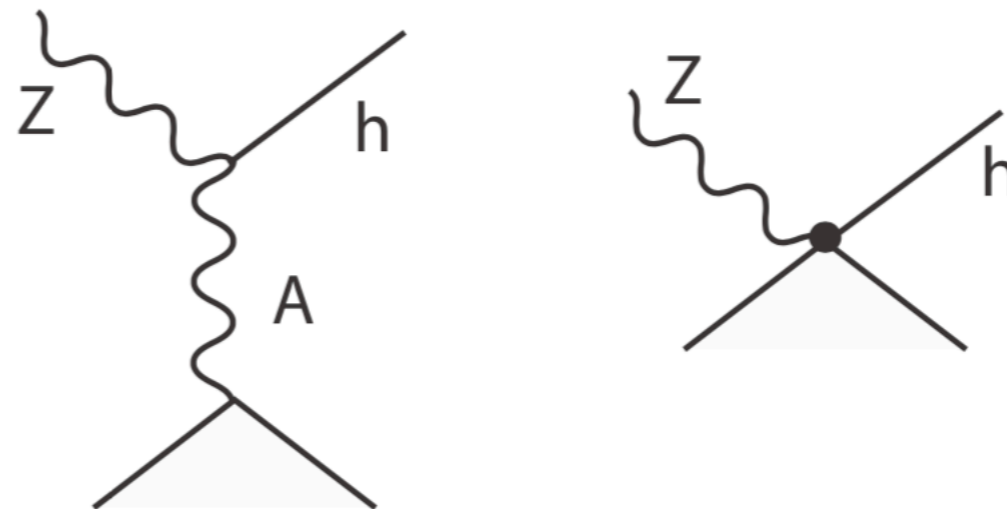
suppose we discover a deviation in, e.g. cross section of

$$e^+e^- \rightarrow ZH \rightarrow (\mu\mu)(bb)$$

then we would like to know which coupling is deviated:



- $hbb$  coupling?
- $hZZ$  coupling?
- $Z\mu\mu$  coupling?
- $Zee$  coupling?
- new diagrams?



# From observables to couplings — Global Fit

$$\chi^2 = \sum_{i=1}^n \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2$$

$Y_i$ : measured values by experiments

$Y'_i$ : predicted values by underlying theory

$\Delta Y_i$ : measurement uncertainty

$n$ : number of independent observables

## ► kappa formalism

$$Y'_i = F_i \cdot \frac{g_{HA_i A_i}^2 \cdot g_{HB_i B_i}^2}{\Gamma_0} \quad \begin{array}{l} (A_i = Z, W, t) \\ (B_i = b, c, \tau, \mu, g, \gamma, Z, W : \text{decay}) \end{array}$$

$$g_{HXX} = \kappa_X \cdot g_{HXX}^{SM}$$

## ► effective field theory formalism (Lecture 2)

# From observables to couplings — Global Fit

in case there are correlated observables

$$\chi^2 = \sum_{i=1}^n \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2 + (Y_j - Y'_j)^T C_j^{-1} (Y_j - Y'_j)$$

$Y_j$ : column vector of correlated observables

$C_j$ : covariance matrix for those observables

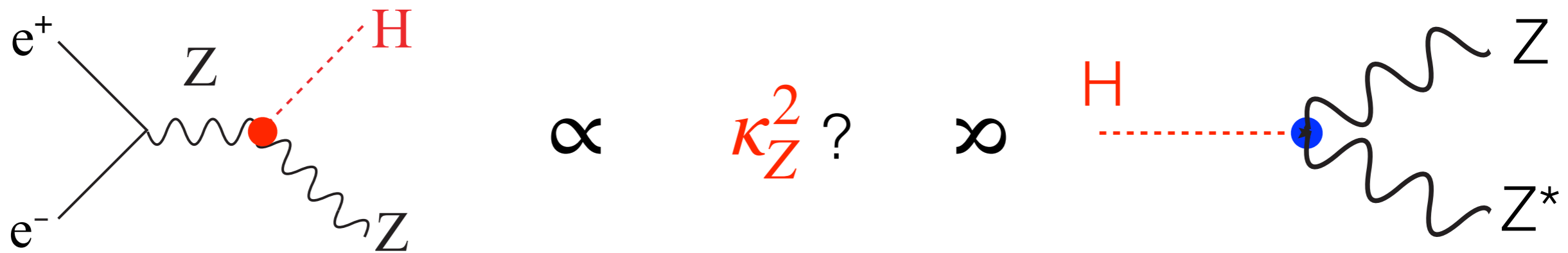
# Higgs coupling determination — kappa formalism

- 1) recoil mass technique  $\longrightarrow$  inclusive  $\sigma_{Zh}$
- 2)  $\sigma_{Zh} \longrightarrow \mathbf{K}_Z \longrightarrow \Gamma(h \rightarrow ZZ^*)$
- 3)  $W$ -fusion  $\nu_e \nu_e h \longrightarrow \mathbf{K}_W \longrightarrow \Gamma(h \rightarrow WW^*)$
- 4) total width  $\mathbf{\Gamma}_h = \Gamma(h \rightarrow ZZ^*) / \text{BR}(h \rightarrow ZZ^*)$
- 5) or  $\mathbf{\Gamma}_h = \Gamma(h \rightarrow WW^*) / \text{BR}(h \rightarrow WW^*)$
- 6) then all other couplings  $\text{BR}(h \rightarrow XX) * \mathbf{\Gamma}_h \rightarrow \mathbf{K}_X$



question in kappa formalism:

$$\frac{\sigma(e^+e^- \rightarrow Zh)}{SM} = \frac{\Gamma(h \rightarrow ZZ^*)}{SM} = \kappa_Z^2 \quad ?$$



- ▶ BSM territory: can deviations be represented by single  $\kappa_Z$ ?
- ▶ How to include radiative corrections in kappa formalism?

# plan

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(i) Mini-intro to future e+e- experiments

Lecture 1

(ii) Higgs Property Measurements

---

(iii) New Particle Searches

(iv) Top-quark & EW Measurements

**Lecture 2**

(v) Global Interpretation in SM EFT

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focus will be on experimental concepts “why / what / how”  
please learn theoretical concepts “why” from other lectures

**supplementary reading for  
accelerator & detector concepts**

(i)

## introduction to accelerators

what behind

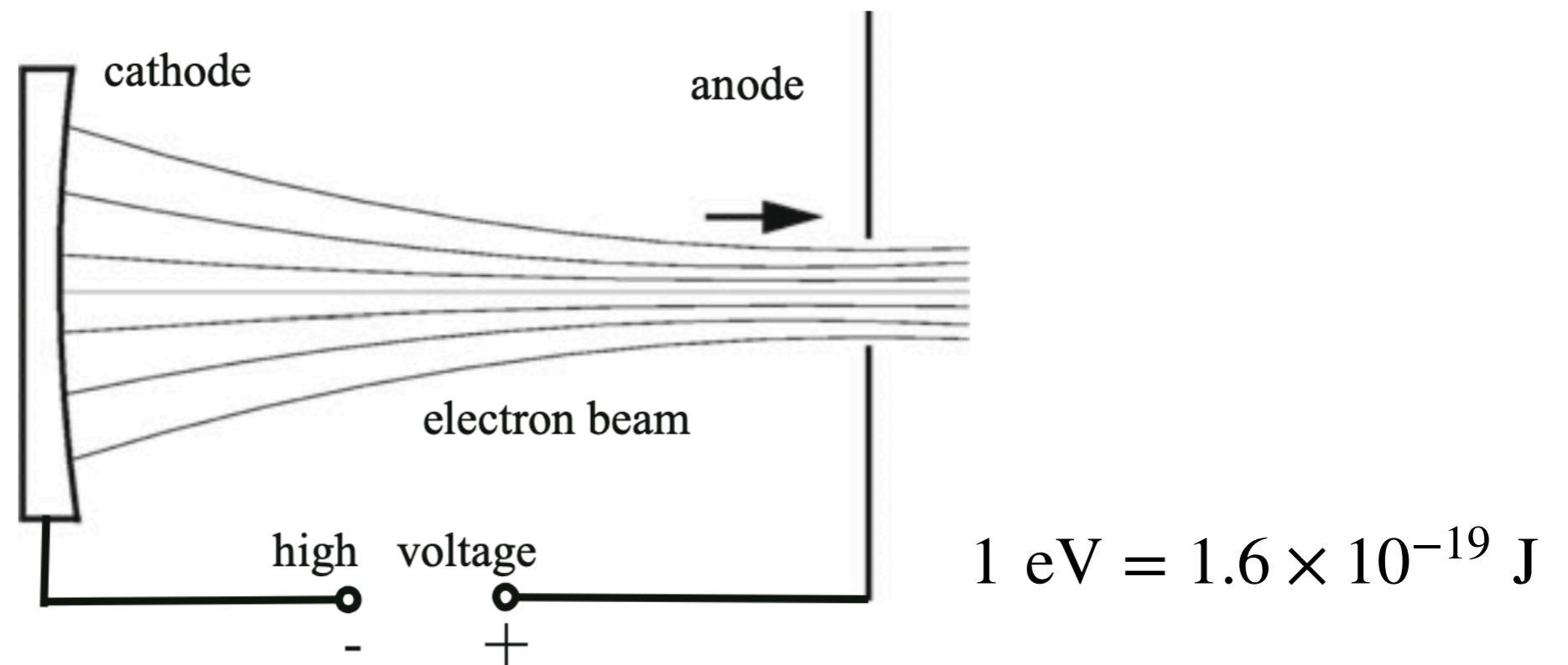
$$\sqrt{s} \quad L \left( \int L dt \right) \quad P$$

- (i.1) basic principles for acceleration
- (i.2) luminosity & a little beam dynamics
- (i.3) beam polarizations
- (i.4) ILC & its specifications

(i.1) basic principles of acceleration

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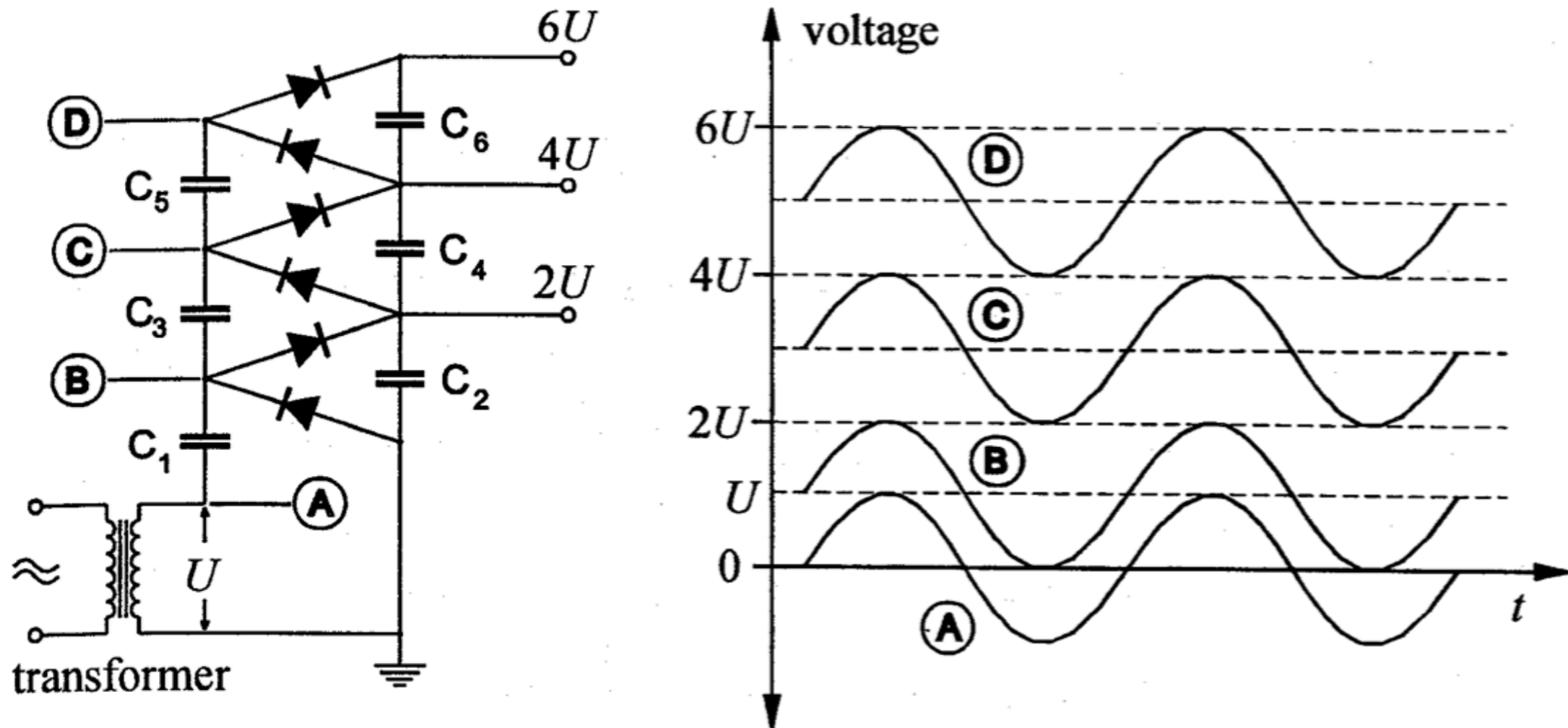
◉ **electrostatic accelerator**



early development: mainly about generating high voltage

(i.1) basic principles of acceleration

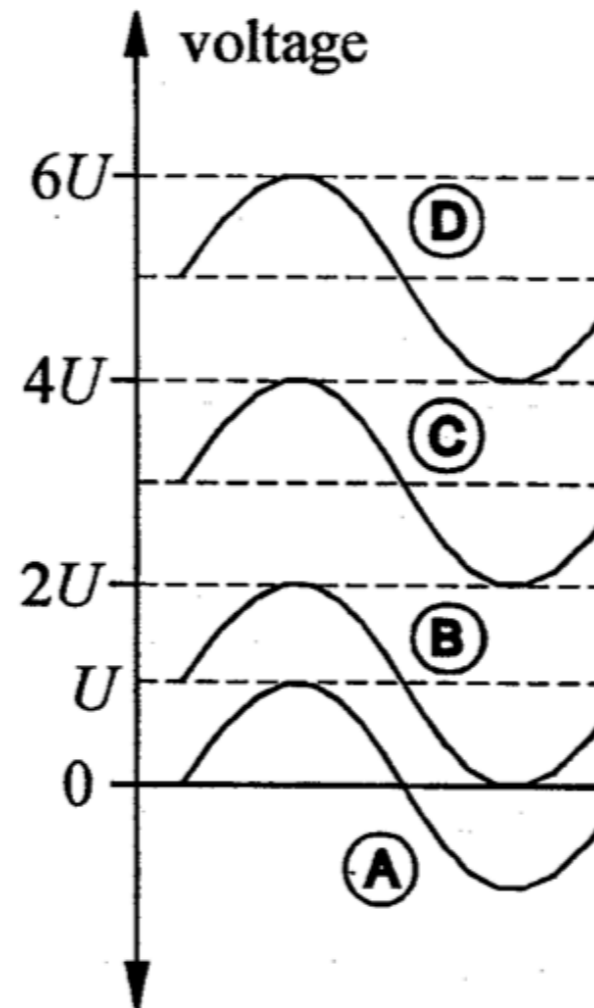
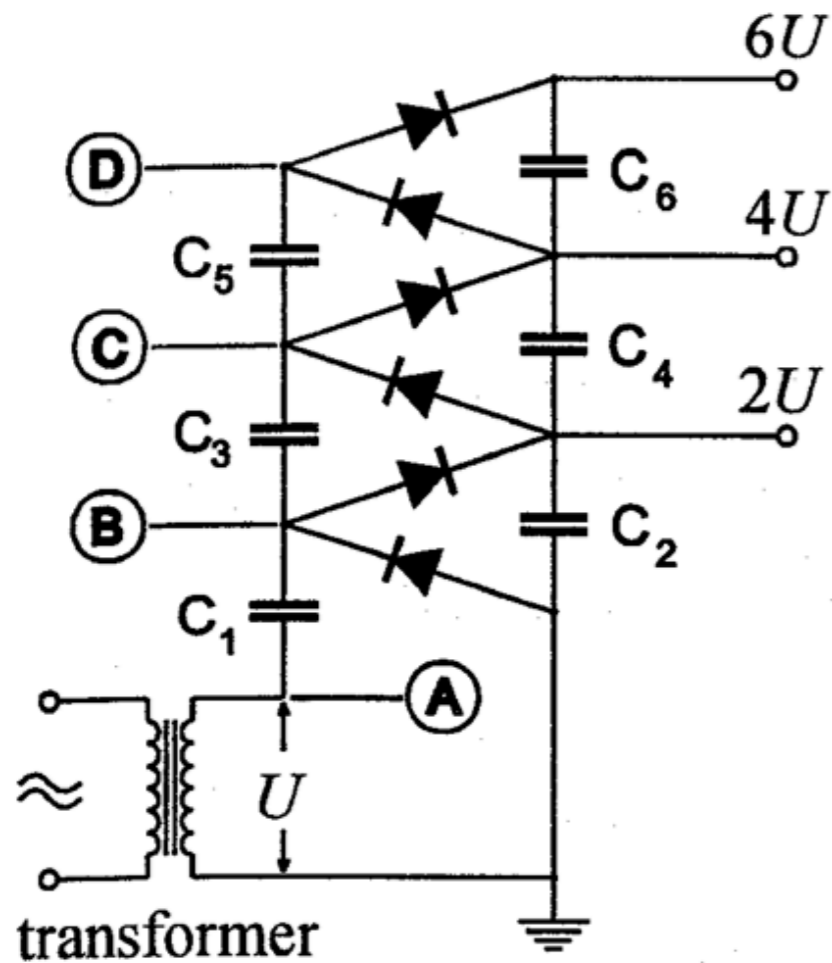
- Cockcroft-Walton cascade generator



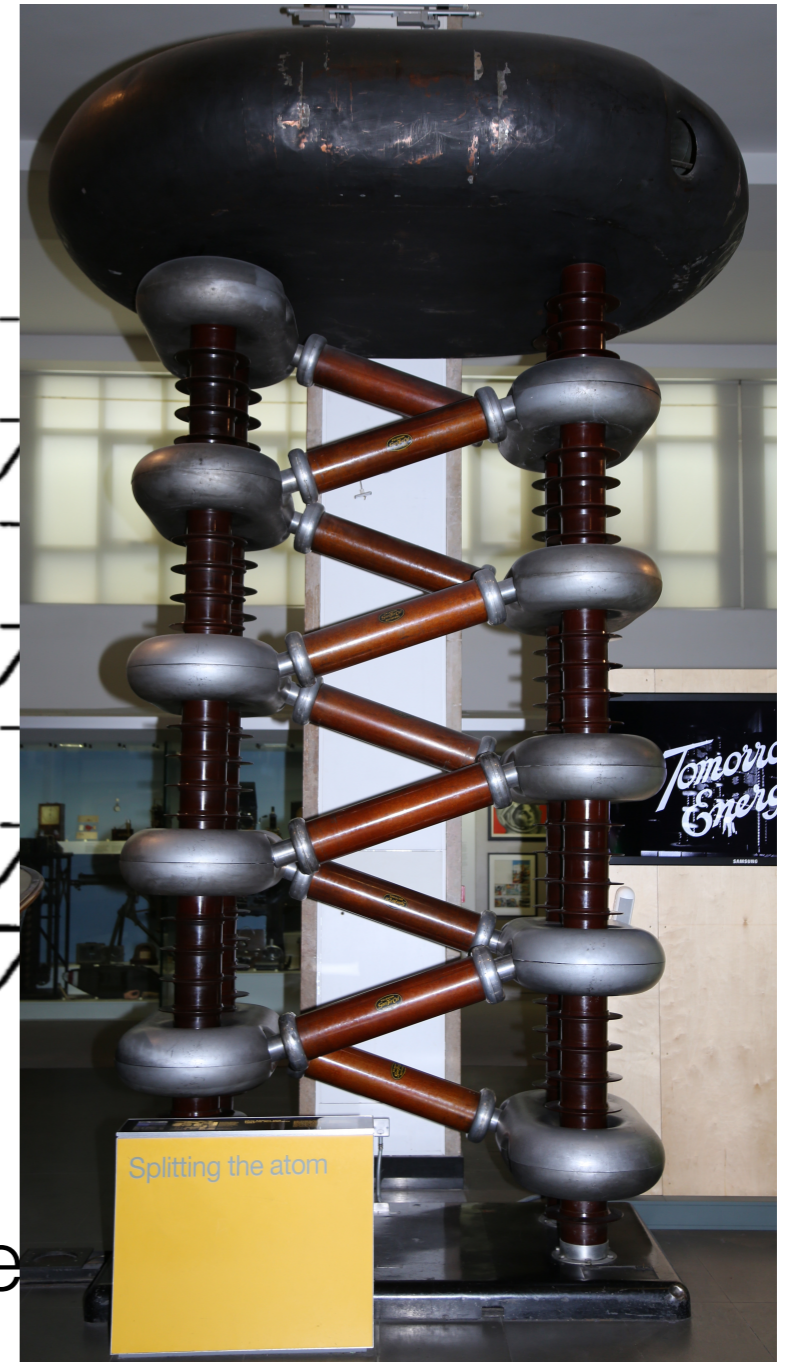
based on a system with multiple rectifiers  
reached  $\sim 0(1)$  MV

(i.1) basic principles of acceleration

- Cockcroft-Walton cascade generator



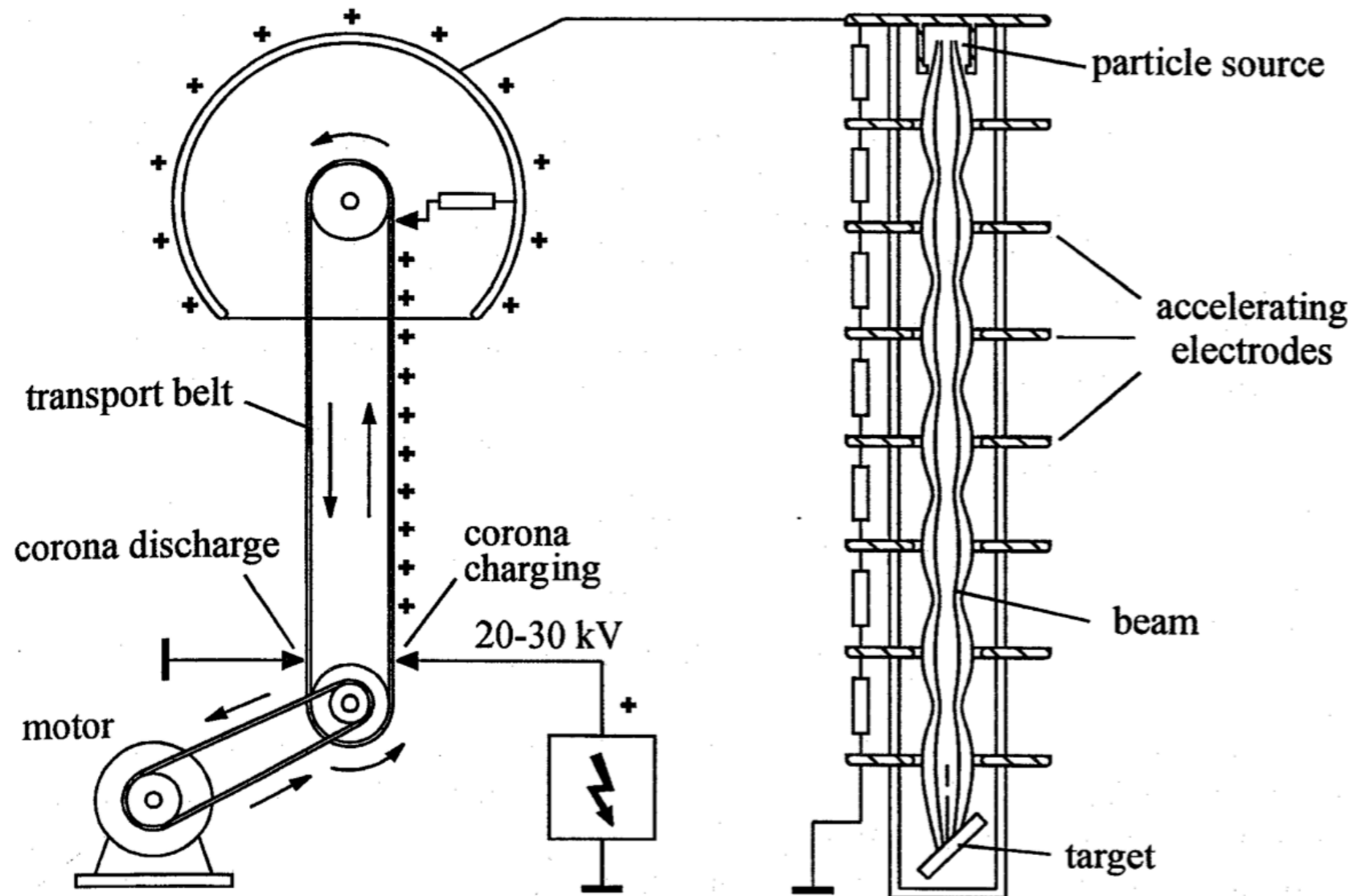
based on a system with multiple re  
reached  $\sim O(1)$  MV



Nat'l Science Museum, London

## (i.1) basic principles of acceleration

- Van de Graaff generator



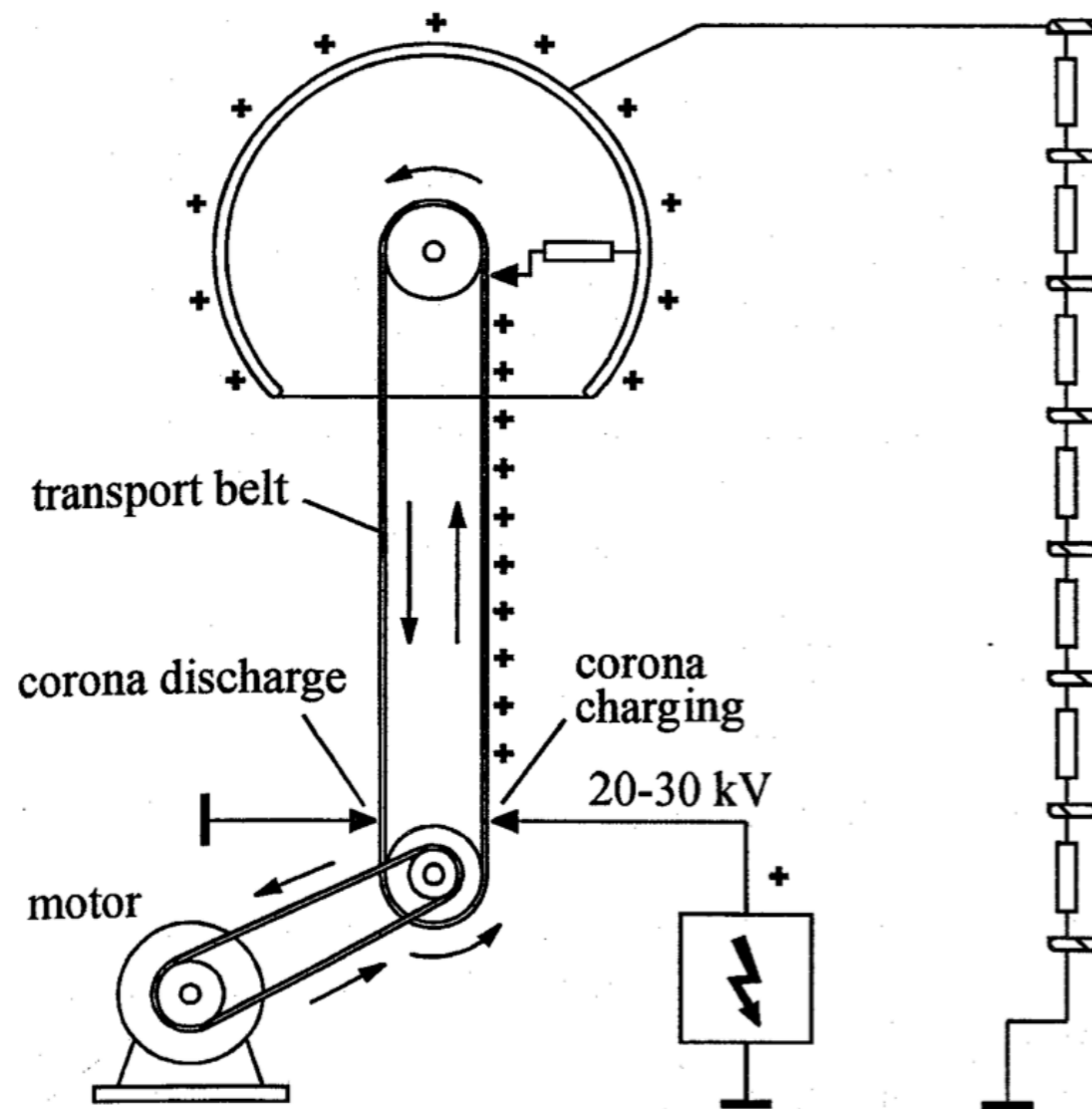
an isolating belt continuously transports charge to a conducting dome:  $O(1-1000)$  MeV



## (i.1) basic principles of acceleration

- Van de Graaff generator

Westinghouse Atom Smasher (1937) 5MV

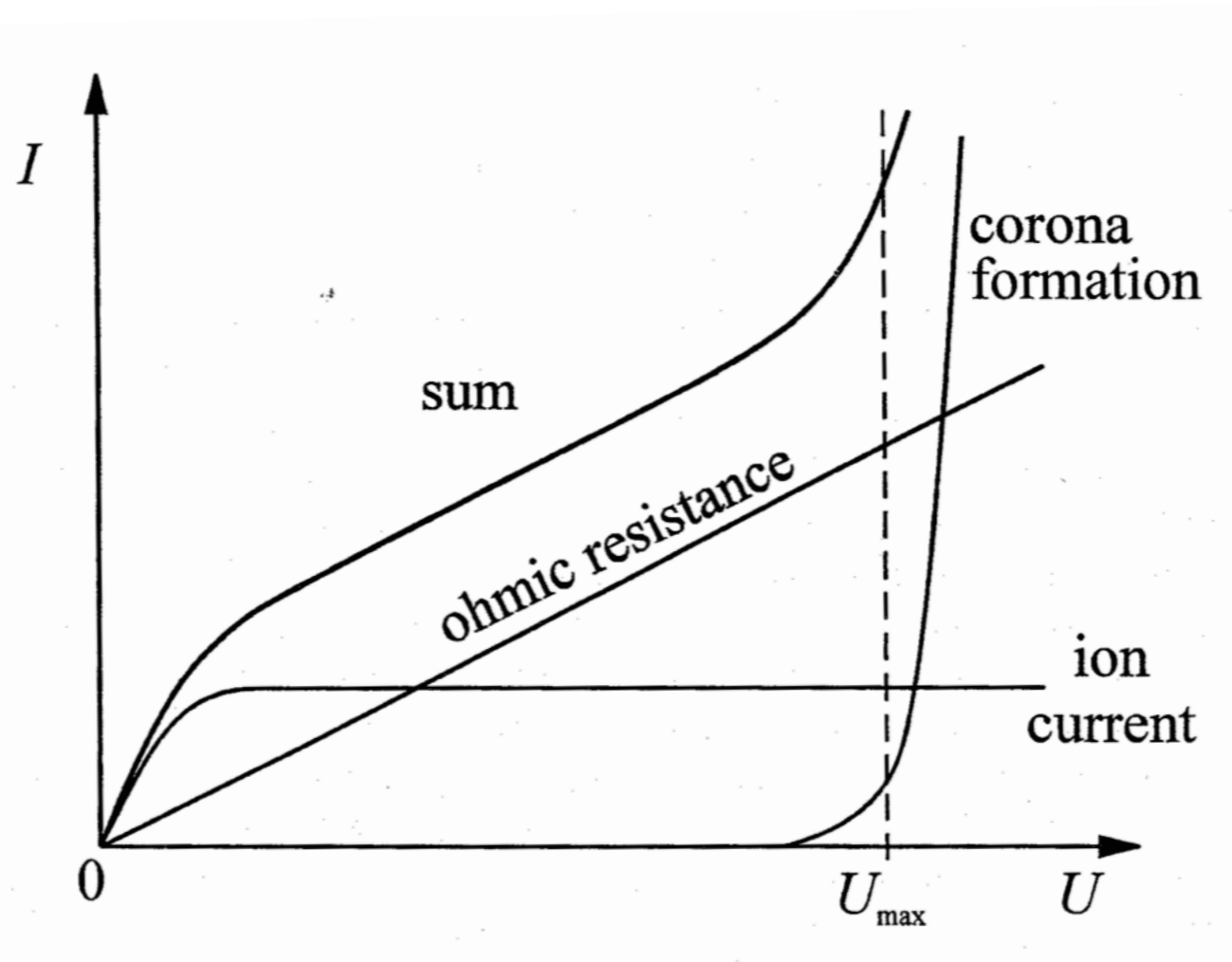


an isolating belt continuously to  
to a conducting dome: O(



## (i.1) basic principles of acceleration

- high-voltage limitation



corona discharge: ionization avalanche near electrode

## (i.1) basic principles of acceleration

---

- high-voltage limitation

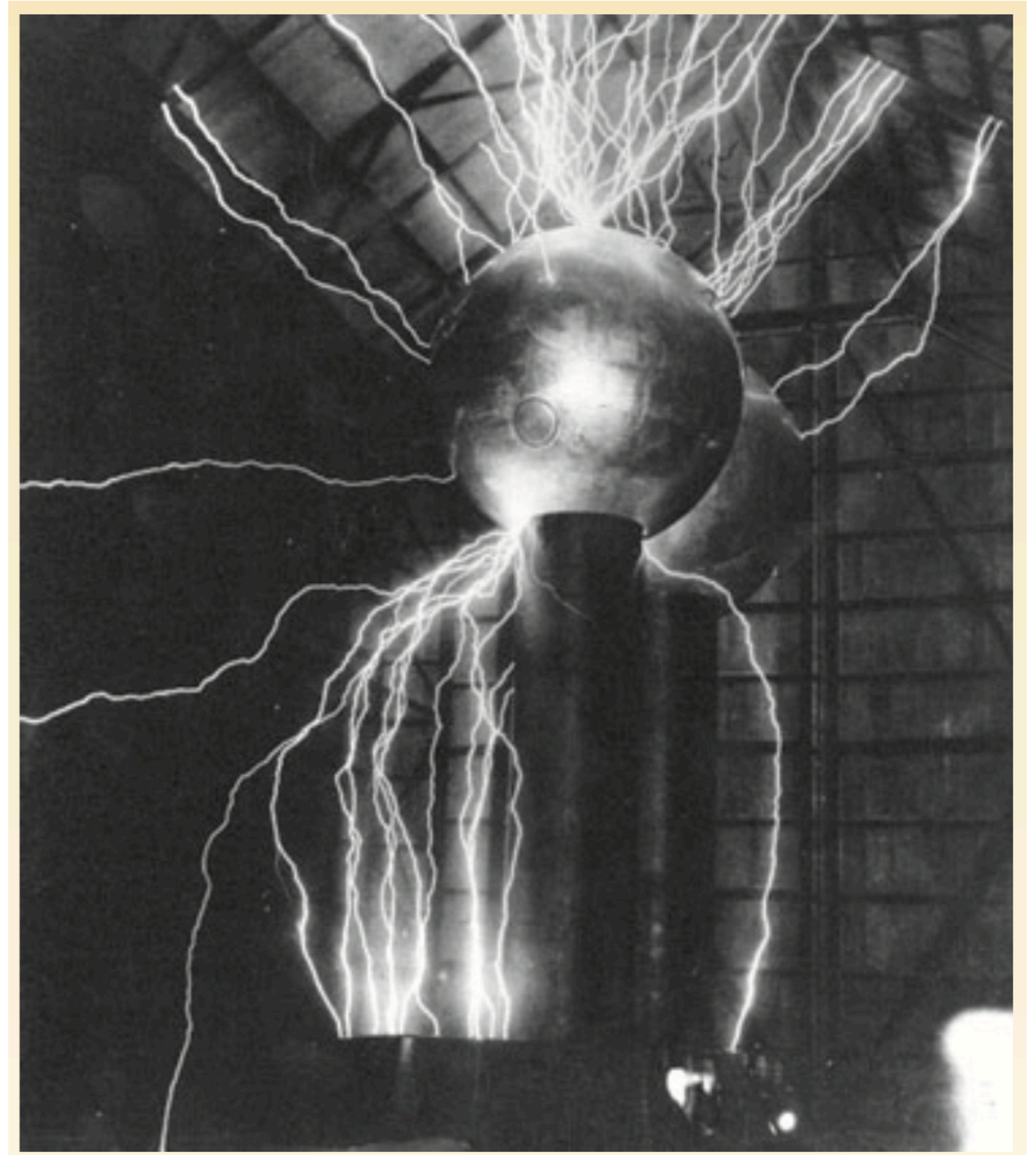




## (i.1) basic principles of acceleration

---

- high-voltage limitation





## (i.1) basic principles of acceleration

---

### ◉ **electrostatic accelerator**

played crucial role for  
the nuclear physics

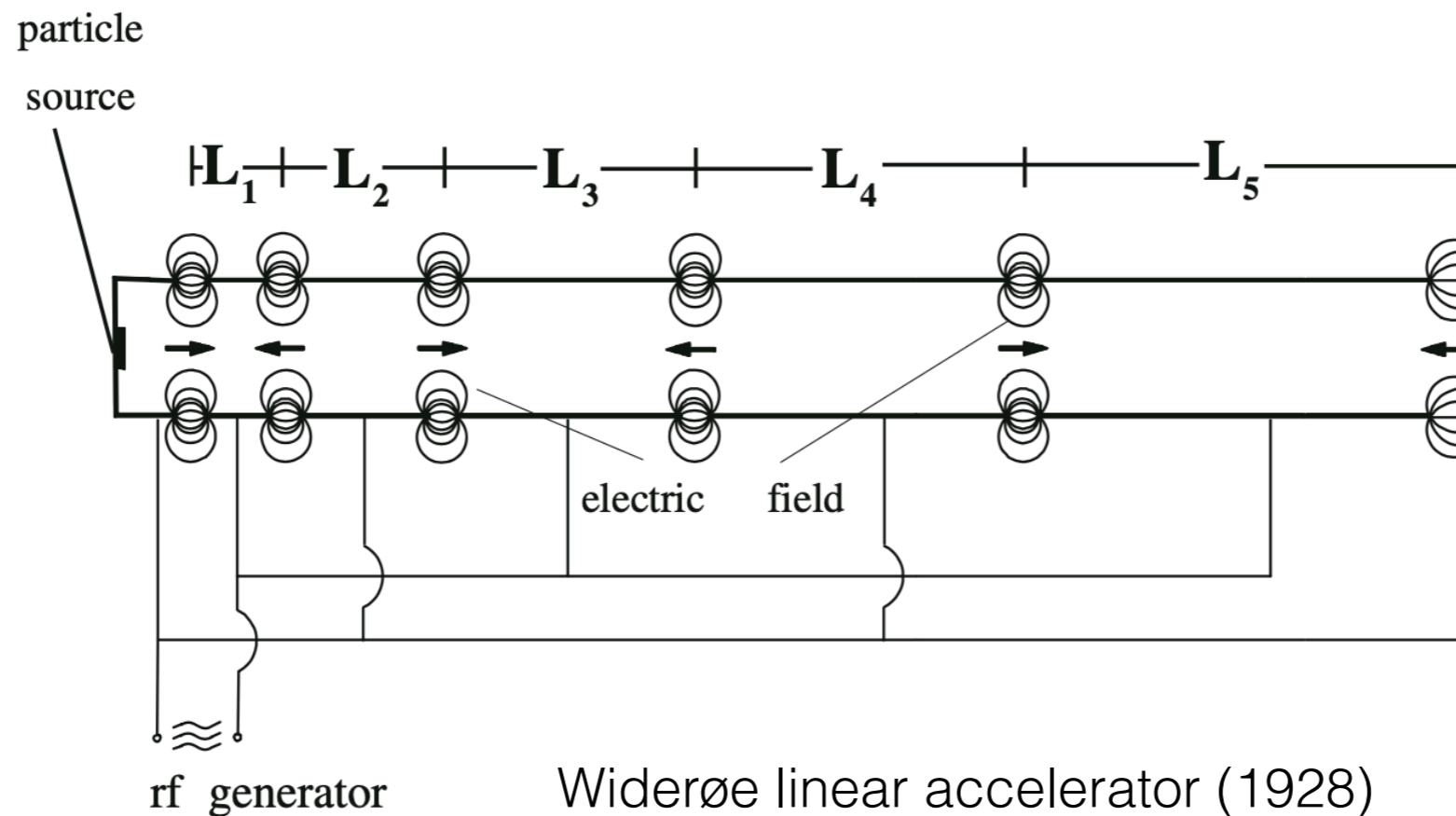
still used nowadays as  
pre-injector



@ CERN Exhibition

(i.1) basic principles of acceleration

◉ **Radio-Frequency (RF) accelerator**



crucial: synchronization of particle motion & RF field

$$L_i = v_i \frac{\tau_{\text{RF}}}{2} = \frac{v_i}{c} \frac{\lambda_{\text{RF}}}{2} = \beta_i \frac{\lambda_{\text{RF}}}{2}$$

for 10 MHz  
 $\lambda_{\text{RF}} = 30\text{m}$

## (i.1) basic principles of acceleration

---

- RF cavity

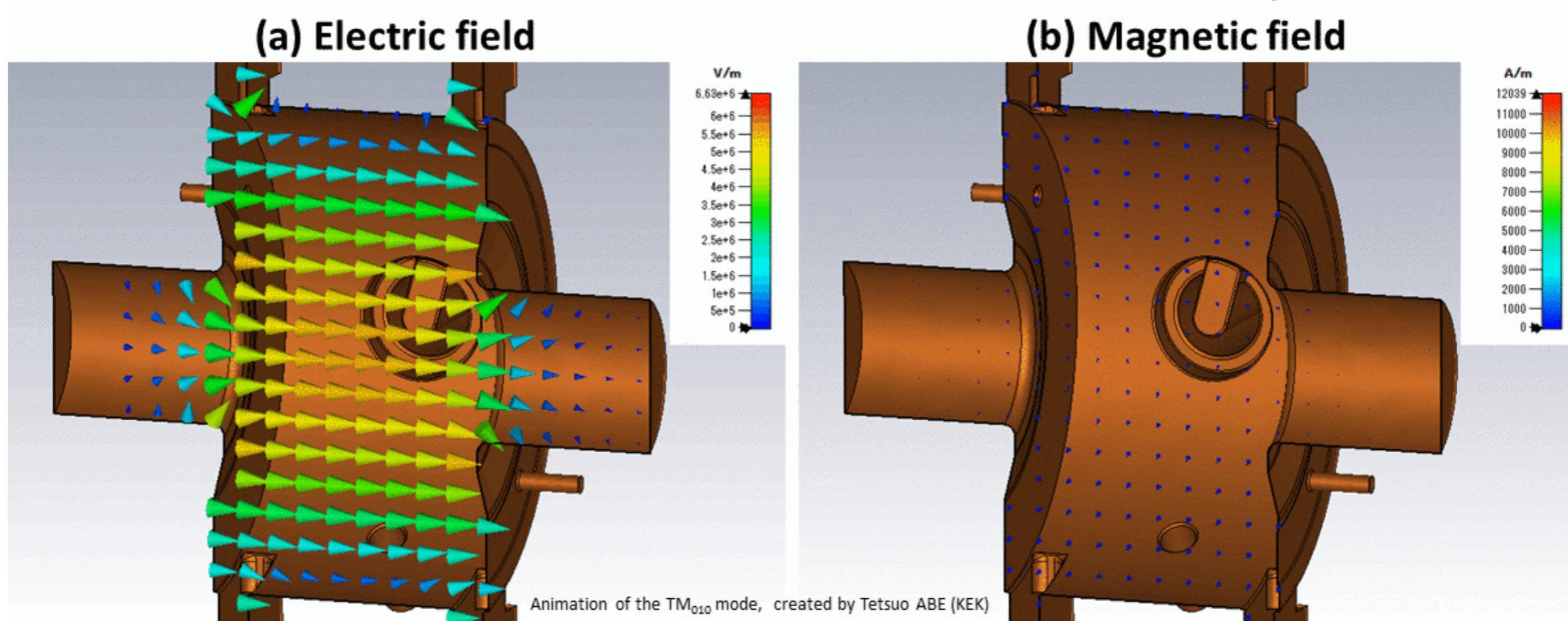
a metal resonator that can store electromagnetic fields



## (i.1) basic principles of acceleration

- RF cavity

a metal resonator that can store electromagnetic fields

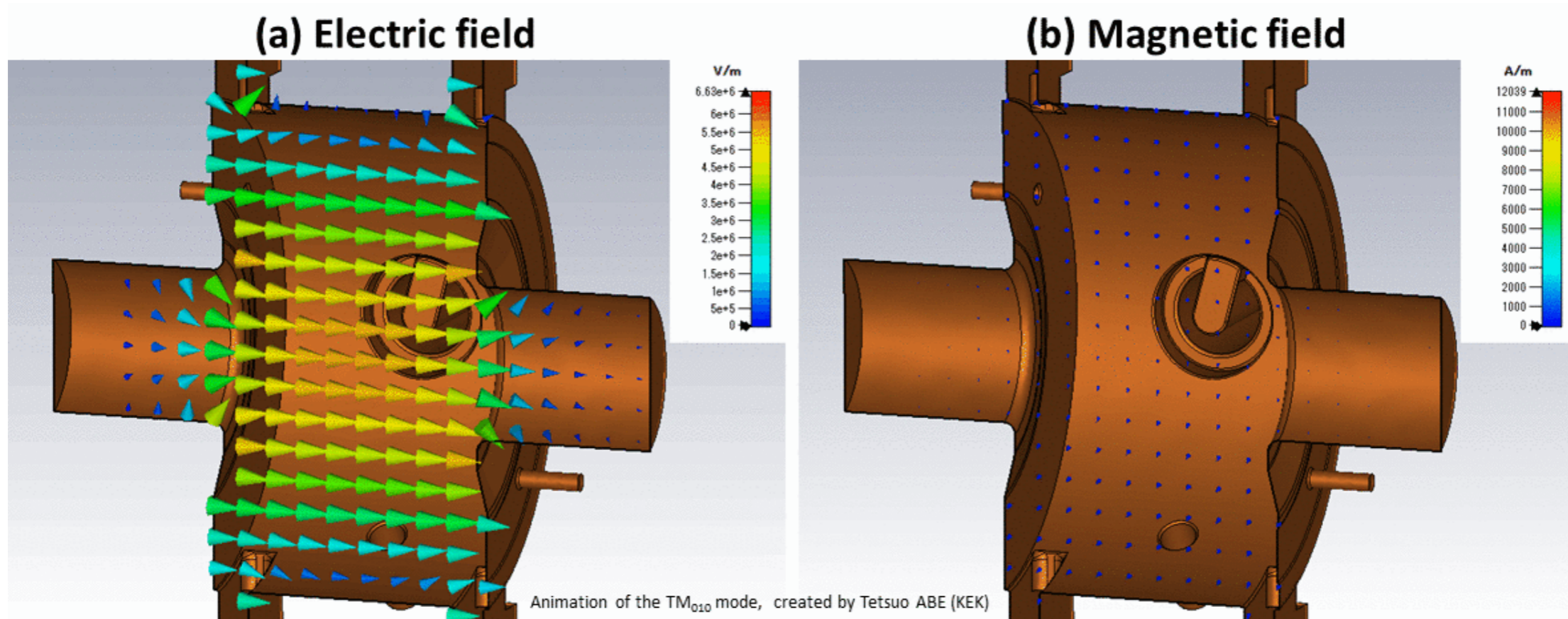




## (i.1) basic principles of acceleration

- RF cavity

a metal resonator that can store electromagnetic fields



most important performance:

Acceleration Gradient [MeV/m]

$Q_0$  (quality factor)  $\sim$  Peak Energy / Energy Loss

## (i.1) basic principles of acceleration

---

- Klystron: produce the RF for cavity

$$L_i = v_i \frac{\tau_{\text{RF}}}{2} = \frac{v_i}{c} \frac{\lambda_{\text{RF}}}{2} = \beta_i \frac{\lambda_{\text{RF}}}{2}$$

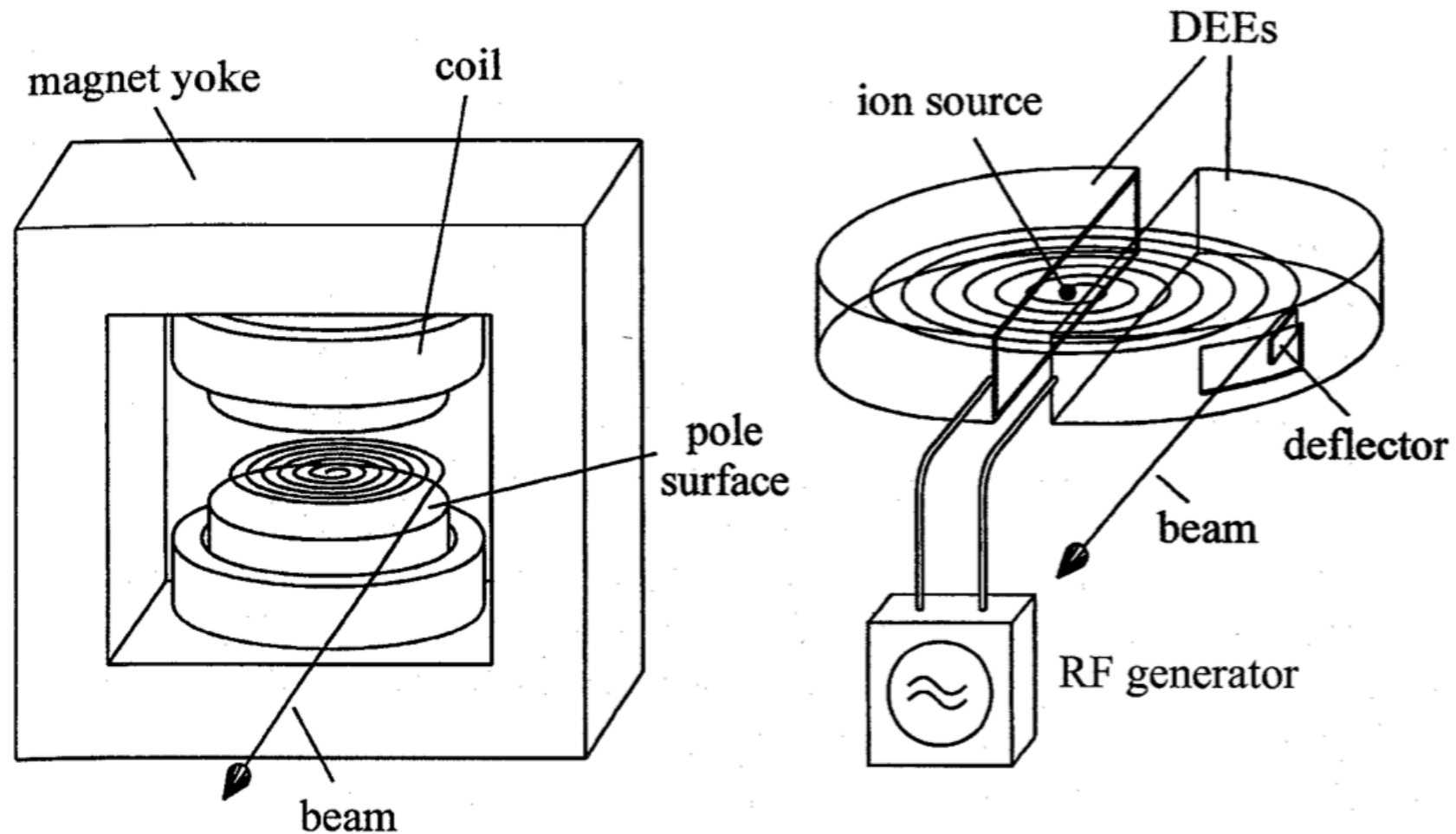
e.g. if for 10 MHz RF,  $\lambda_{\text{RF}} = 30\text{m}$

it is crucial to develop high frequency & high power Klystron

was highly developed during WW II for radar system

## (i.1) basic principles of acceleration

- Cyclotron



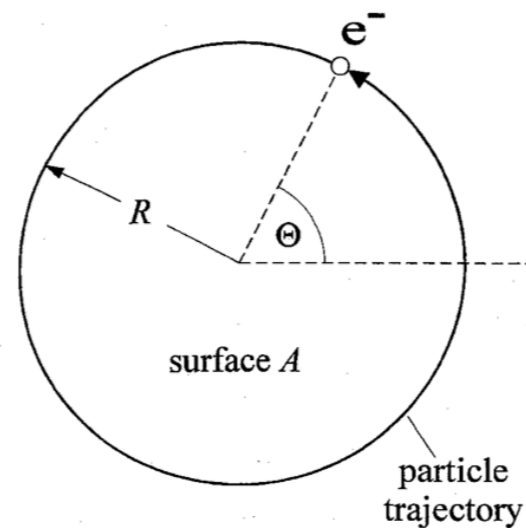
fixed frequency (for non-relativistic particle)

$$\omega = \frac{e}{m} B_z \quad \text{matched exactly by RF}$$

## (i.1) basic principles of acceleration

- Betatron

increasing B-field rapidly, keeping particle orbit fixed



law of induction -> no need any extra acceleration section

$$\oint \vec{E} \cdot d\vec{r} = - \iint \frac{d\vec{B}}{dt} \cdot d\vec{s}$$

Widerøe's betatron condition:  $|B(t)| = 1/2 \langle |B(t)| \rangle + |B_0|$



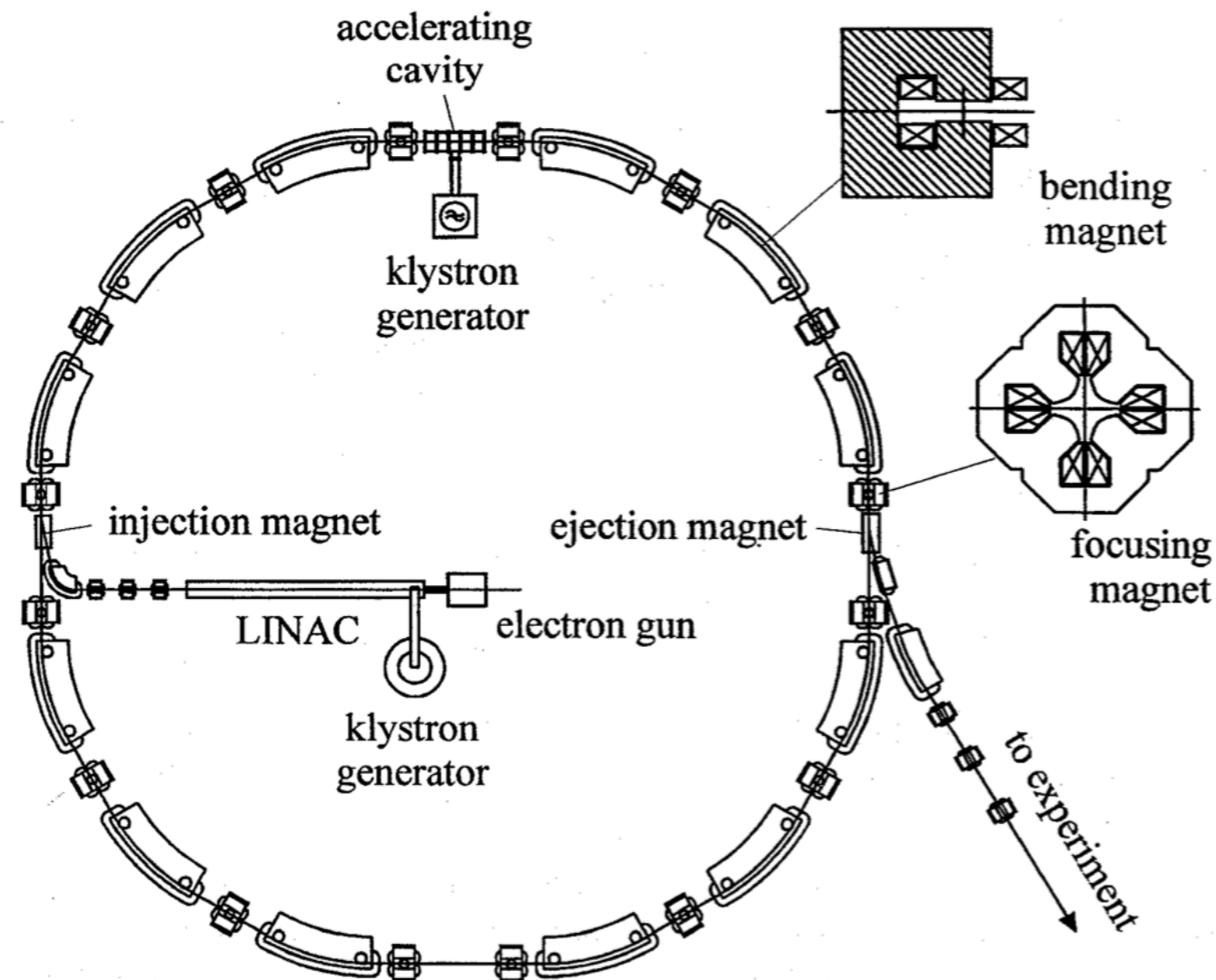


## (i.1) basic principles of acceleration

- synchrotron

fixed orbit; magnet only around orbit; RF acc. section;  
synchronizing magnetic field with energy

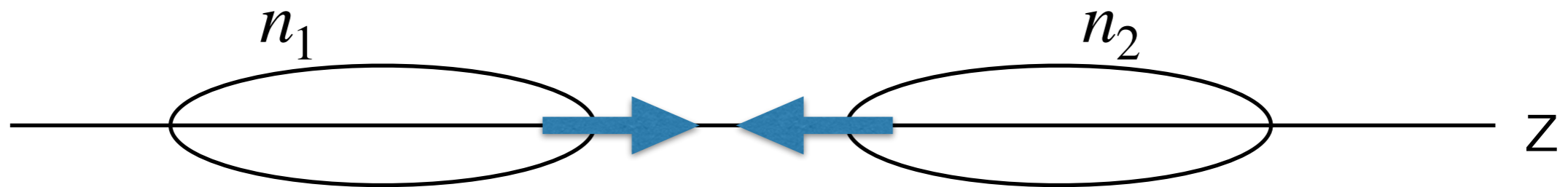
$$R = \frac{E}{ecB}$$



## (i.2) luminosity & beam dynamics

---

- Luminosity



$$L = f_{coll} \frac{n_1 n_2}{4\pi\sigma_x^* \sigma_y^*} F$$

$n_1, n_2$ : # particles in a bunch

$f_{coll}$ : average collision frequency

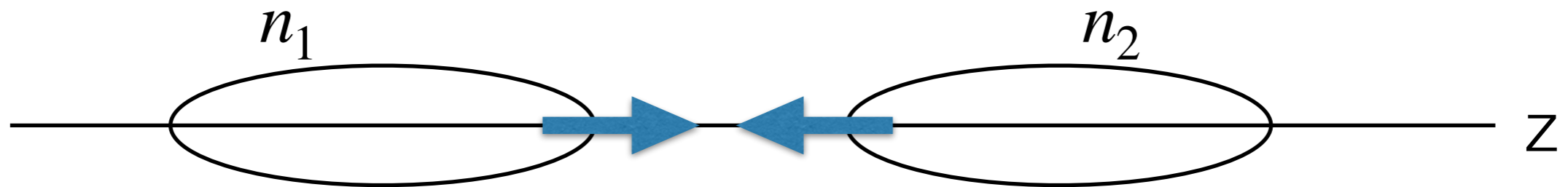
$F$ :  $\sim 1$ , geometric effect (crossing angle, etc)

$\sigma_x, \sigma_y$ : bunch size in the transverse direction  
most non-trivial part

## (i.2) luminosity & beam dynamics

---

- emittance & beta function



$$L = f_{coll} \frac{n_1 n_2}{4\pi\sigma_x^* \sigma_y^*} F$$

$$\sigma_x^2 = \epsilon \cdot \beta$$

↑                      ↙  
emittance            beta function

## (i.2) luminosity & beam dynamics

---

- beam dynamics

in an accelerator, by construction particles follow a nominal trajectory (orbit)

but particles in a beam will always have certain angular divergence, if not steered, after a long travel will hit the accelerator wall

beam steering is necessary

Lorentz force:

$$\mathbf{F} = e(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

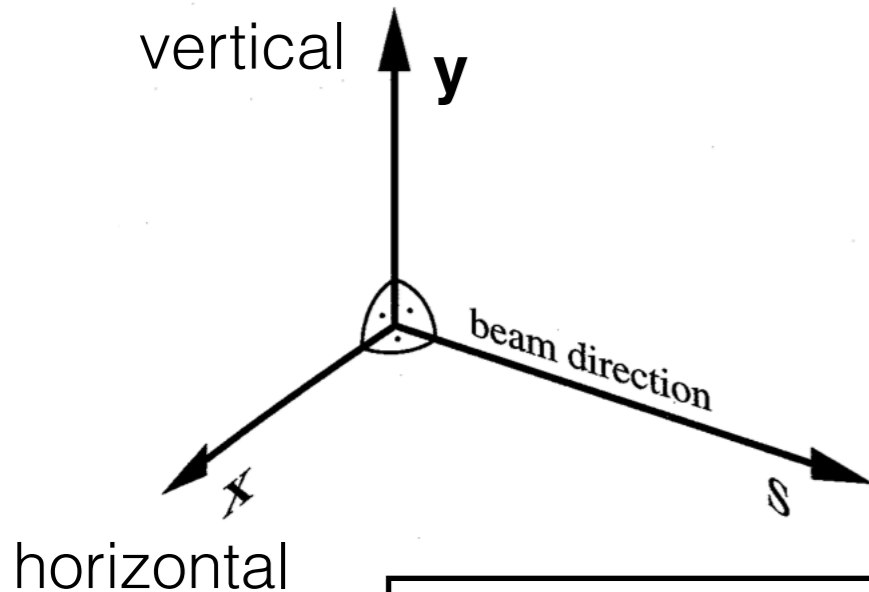
$v=c$ , for  $B=1\text{T}$ ,  $E$  would be  $300\text{ MV/m}$  to compete  
beam steering is almost always done by magnets



## (i.2) luminosity & beam dynamics

- magnets

take as example motion in horizontal plane



$$\frac{1}{R(x)} = \frac{e}{p} B_z(x)$$

$$B_z(x) = B_{z0} + \frac{dB_z}{dx}x + \frac{1}{2!} \frac{d^2 B_z}{dx^2} x^2 + \frac{1}{3!} \frac{d^3 B_z}{dx^3} x^3 + \dots$$

$$\begin{aligned} \frac{e}{p} B_z(x) &= \frac{e}{p} B_{z0} + \frac{e}{p} \frac{dB_z}{dx} x + \frac{1}{2!} \frac{e}{p} \frac{d^2 B_z}{dx^2} x^2 + \frac{1}{3!} \frac{e}{p} \frac{d^3 B_z}{dx^3} x^3 + \dots \\ &= \frac{1}{R} + kx + \frac{1}{2!} mx^2 + \frac{1}{3!} ox^3 + \dots \end{aligned}$$

dipole

quadrupole

sextupole

octupole

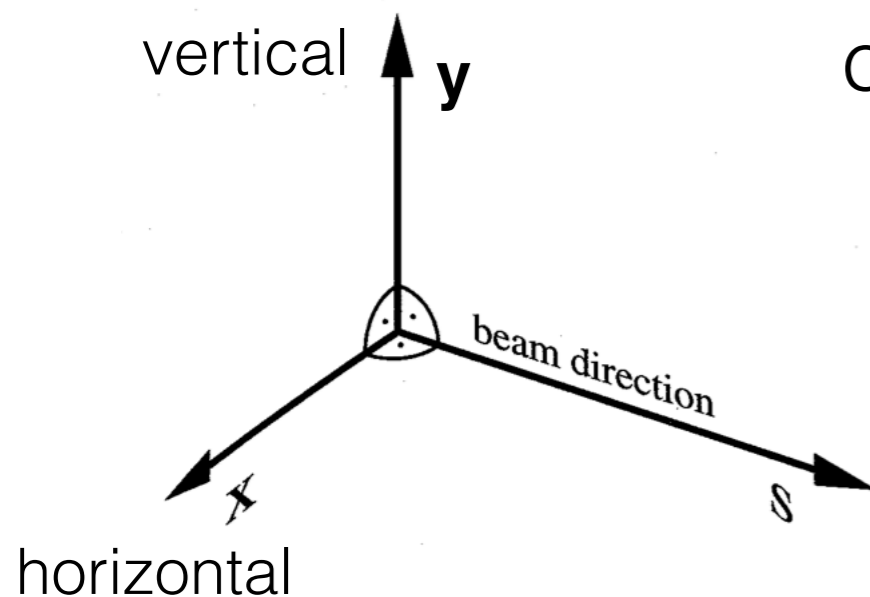
bending

**focusing (k>0)**  
**defocusing (k<0)**

## (i.2) luminosity & beam dynamics

---

- linear beam optics



co-moving coordinate system  $(x, y, s)$

$s$ : along the nominal trajectory

$$x' \equiv \frac{dx}{ds}$$

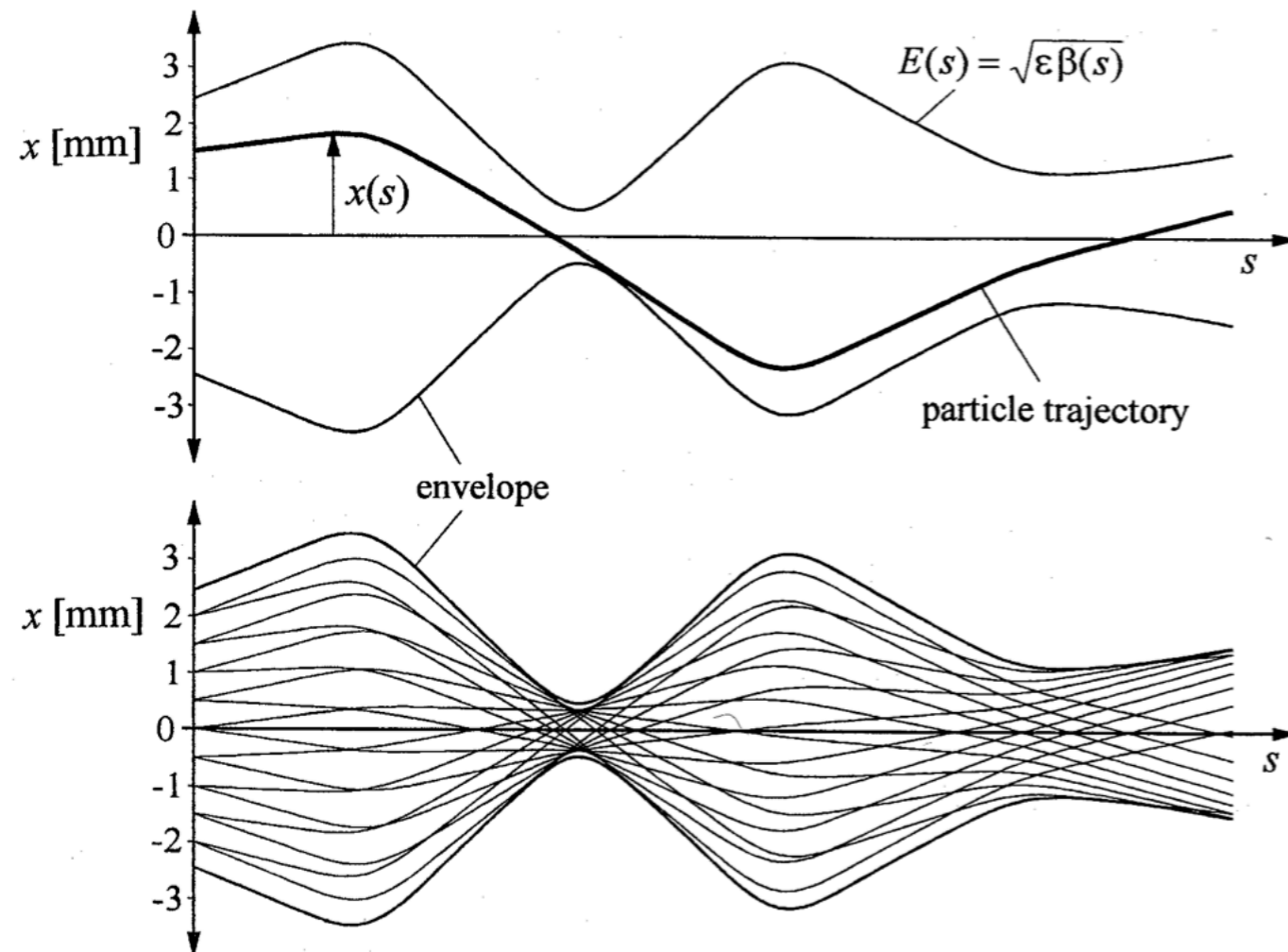
$$x''(s) + \left(\frac{1}{R^2} - k(s)\right)x(s) = 0$$

$$y''(s) + k(s)y(s) = 0$$

(betatron oscillations)

## (i.2) luminosity & beam dynamics

- back to luminosity

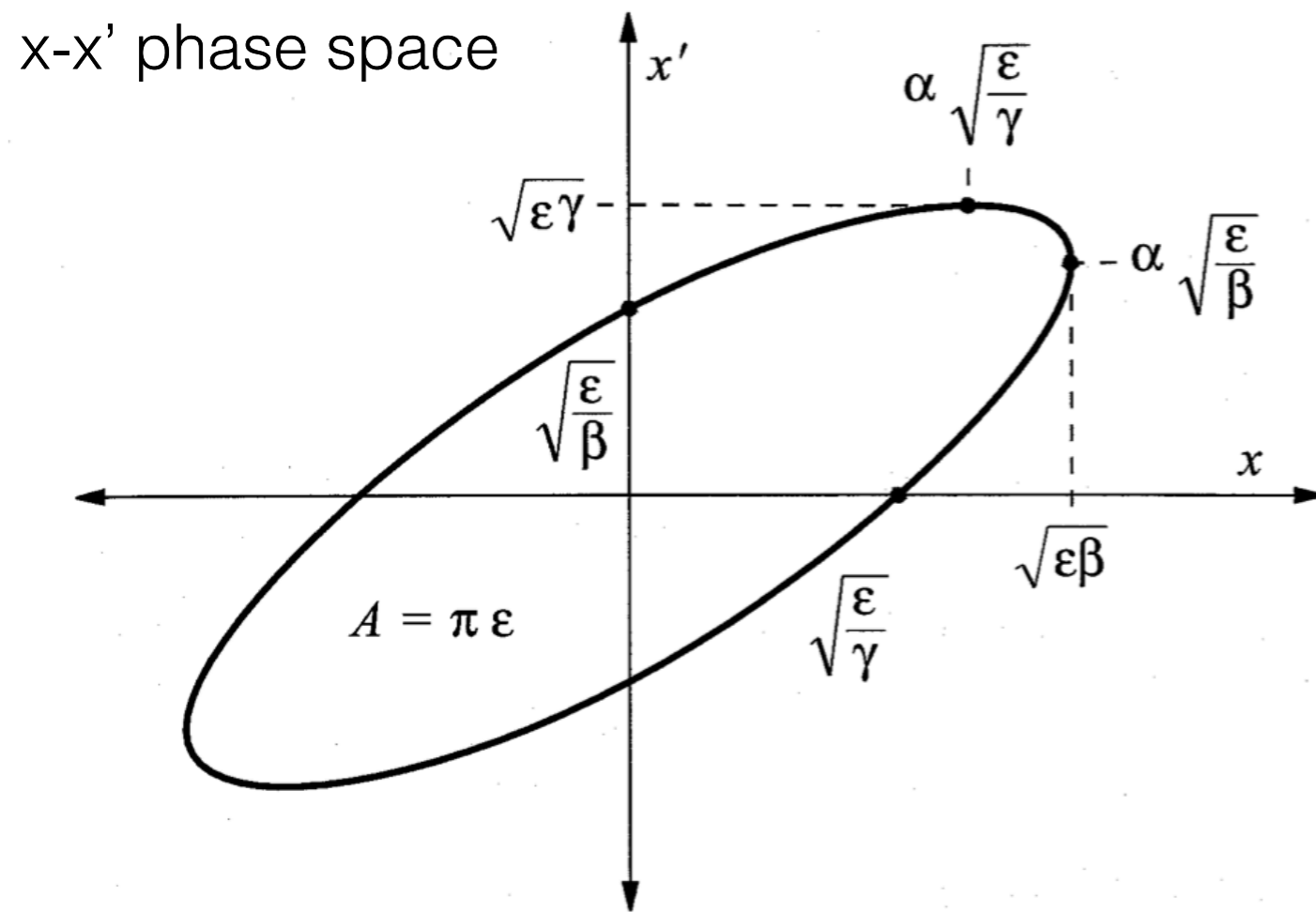


$$L = f_{coll} \frac{n_1 n_2}{4\pi \sigma_x^* \sigma_y^*} F$$

$$\sigma_x^2 = \epsilon \cdot \beta$$

## (i.2) luminosity & beam dynamics

- back to luminosity

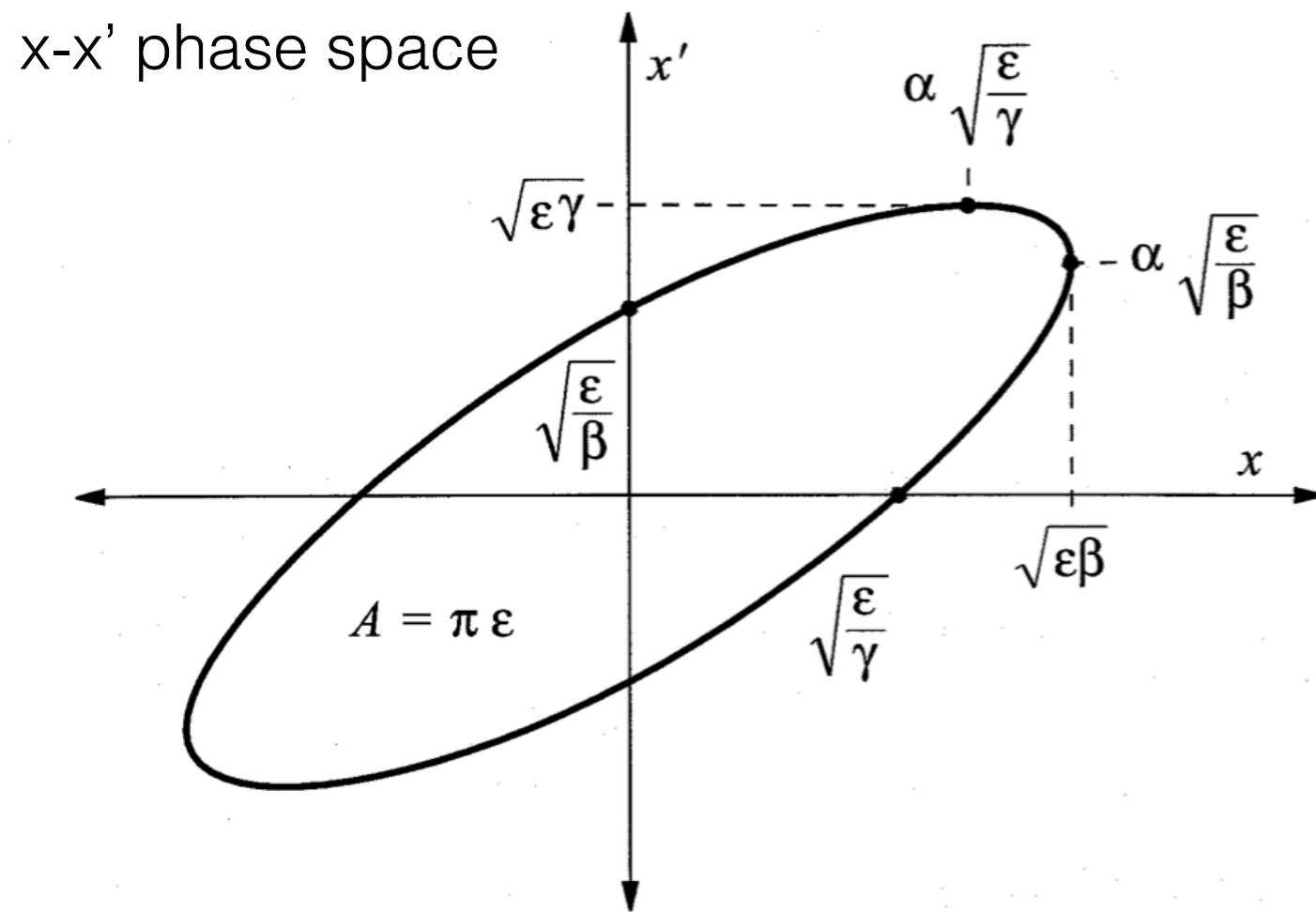


$$L = f_{coll} \frac{n_1 n_2}{4\pi\sigma_x^* \sigma_y^*} F$$

$$\sigma_x^2 = \epsilon \cdot \beta$$

## (i.2) luminosity & beam dynamics

- back to luminosity



$$L = f_{coll} \frac{n_1 n_2}{4\pi\sigma_x^* \sigma_y^*} F$$

$$\sigma_x^2 = \epsilon \cdot \beta$$

**emittance  $\times \pi =$  area of the ellipse**

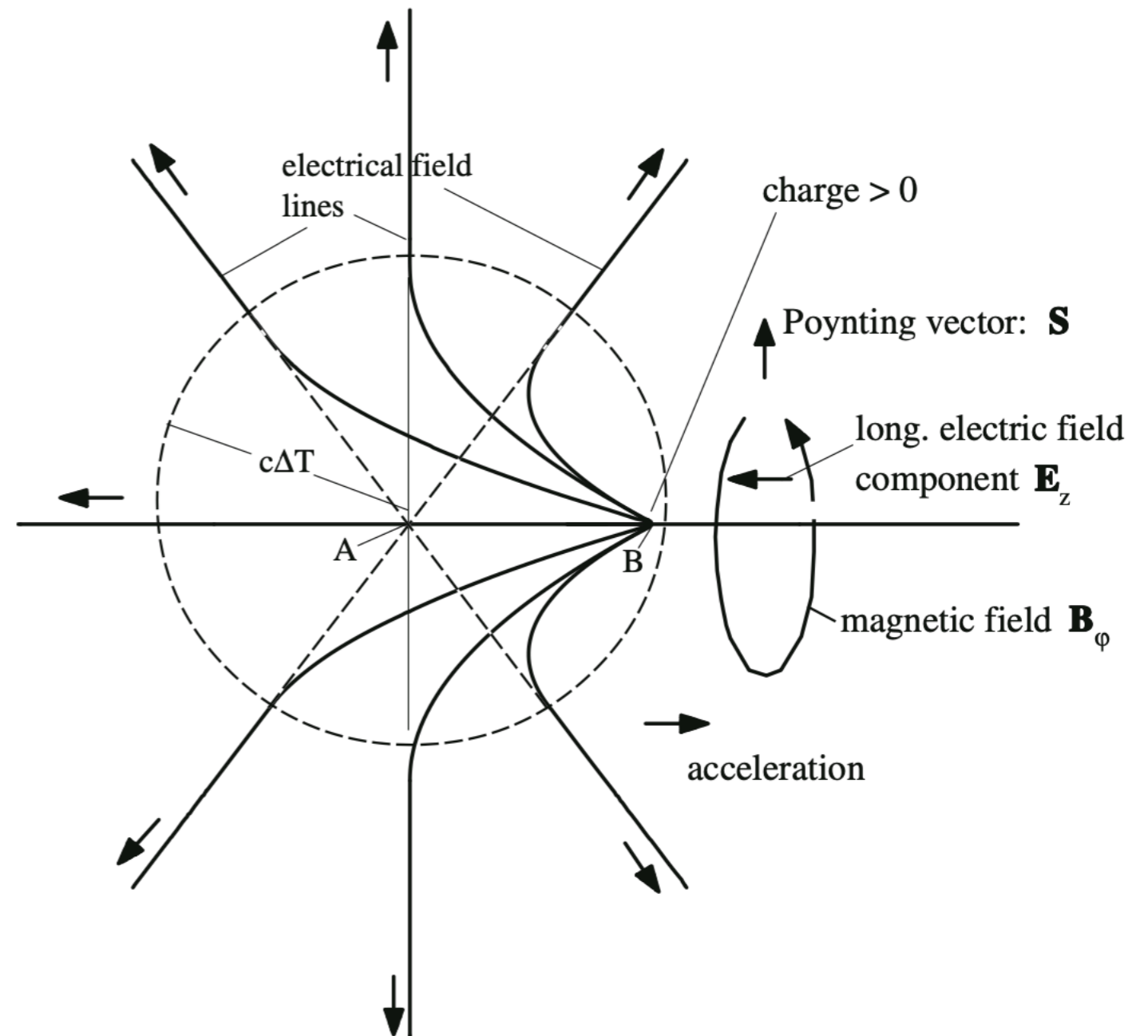
## (i.3) synchrotron radiation

- fundamental process

an accelerating charge

distort electromagnetic field

speed of light  $c$  is finite



propagation of distorted electromagnetic field = synchrotron radiation

(was first seen by eye at a synchrotron)

## (i.3) synchrotron radiation

---

- qualitatively: linear vs circular

synchrotron radiation depends on size of acceleration  $|\mathbf{a}|$

at a linear accelerator

for  $E=100\text{GeV}$ ,  $G=30\text{MeV/m}$ ;  $|\mathbf{a}|=1.4\times 10^3 \text{ m/s}^2$

at a circular accelerator

for  $E=100\text{GeV}$ ,  $R=100\text{km}$ ;  $|\mathbf{a}|=9\times 10^{11} \text{ m/s}^2$

$|\mathbf{a}|$  differ enormously

## (i.3) synchrotron radiation

---

- synchrotron radiation power

at a circular accelerator

$$P = \frac{e^2 c}{6\pi\epsilon_0} \frac{1}{(m_0 c^2)^4} \frac{E^4}{R^2}$$

energy loss per turn (for electron)

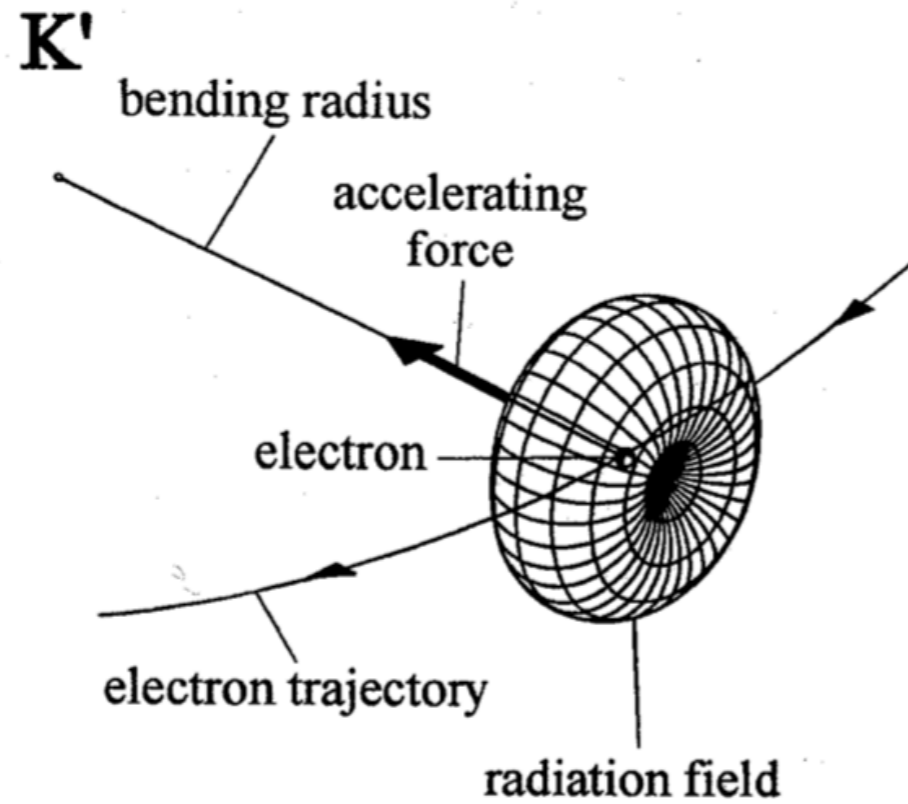
$$\Delta E[\text{keV}] = 88.5 \frac{E^4[\text{GeV}]^4}{R[\text{m}]}$$



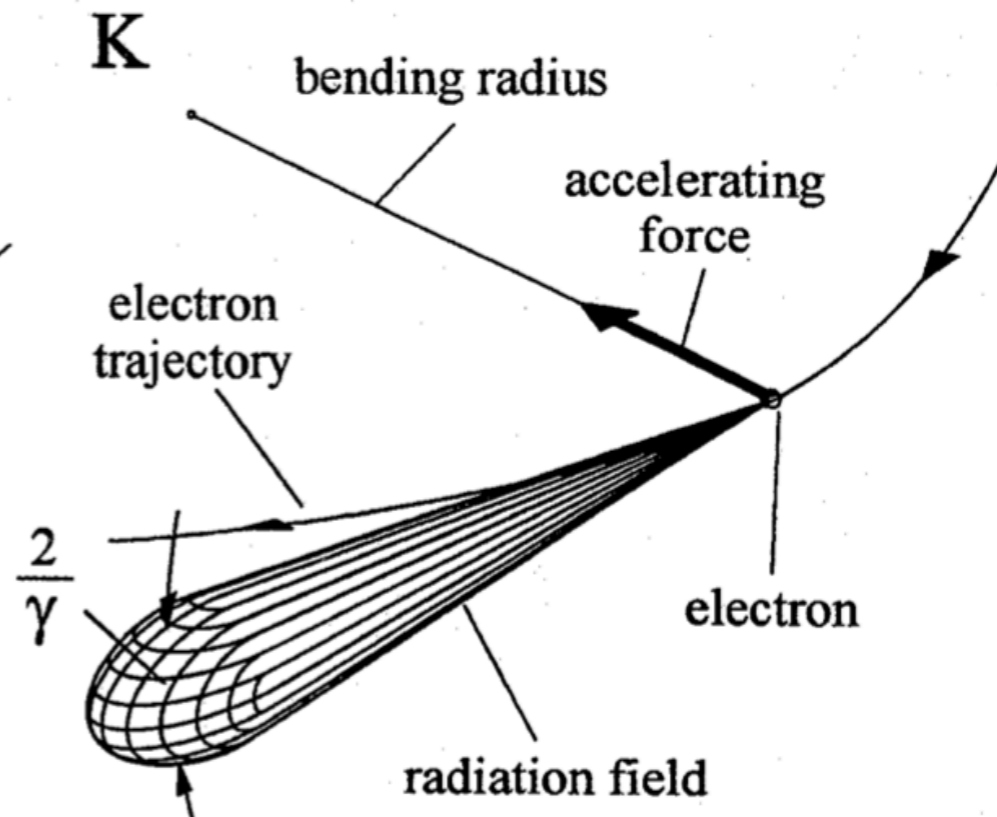
# (i.3) synchrotron radiation

- angular distribution

$$\tan \theta = \frac{1}{\gamma}$$



E.O.M. frame



Lab frame

## (i.3) synchrotron radiation

---

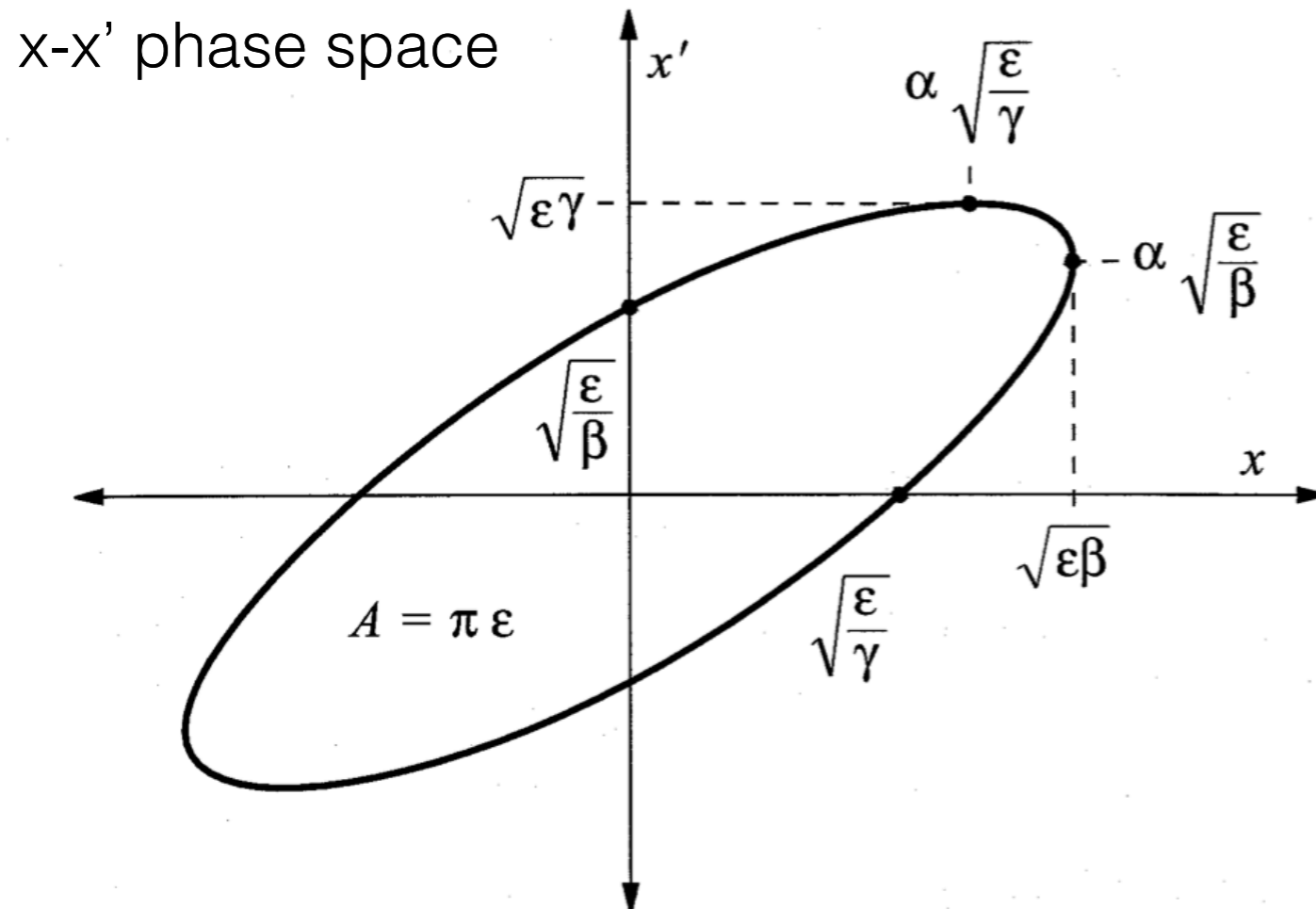
- crucial for linear colliders as well

damping ring: synchrotron radiation can reduce emittance

### (i.3) synchrotron radiation

- crucial for linear colliders as well

damping ring: synchrotron radiation can reduce emittance



## (i.4) beam polarization

---

- definitions

$$P = \frac{N_R - N_L}{N_R + N_L}$$

$N_{R/L}$ : number of R/L-handed e-(e+)

can be longitudinal or transverse

polarized electron source:

a polarized laser to hit a photocathode

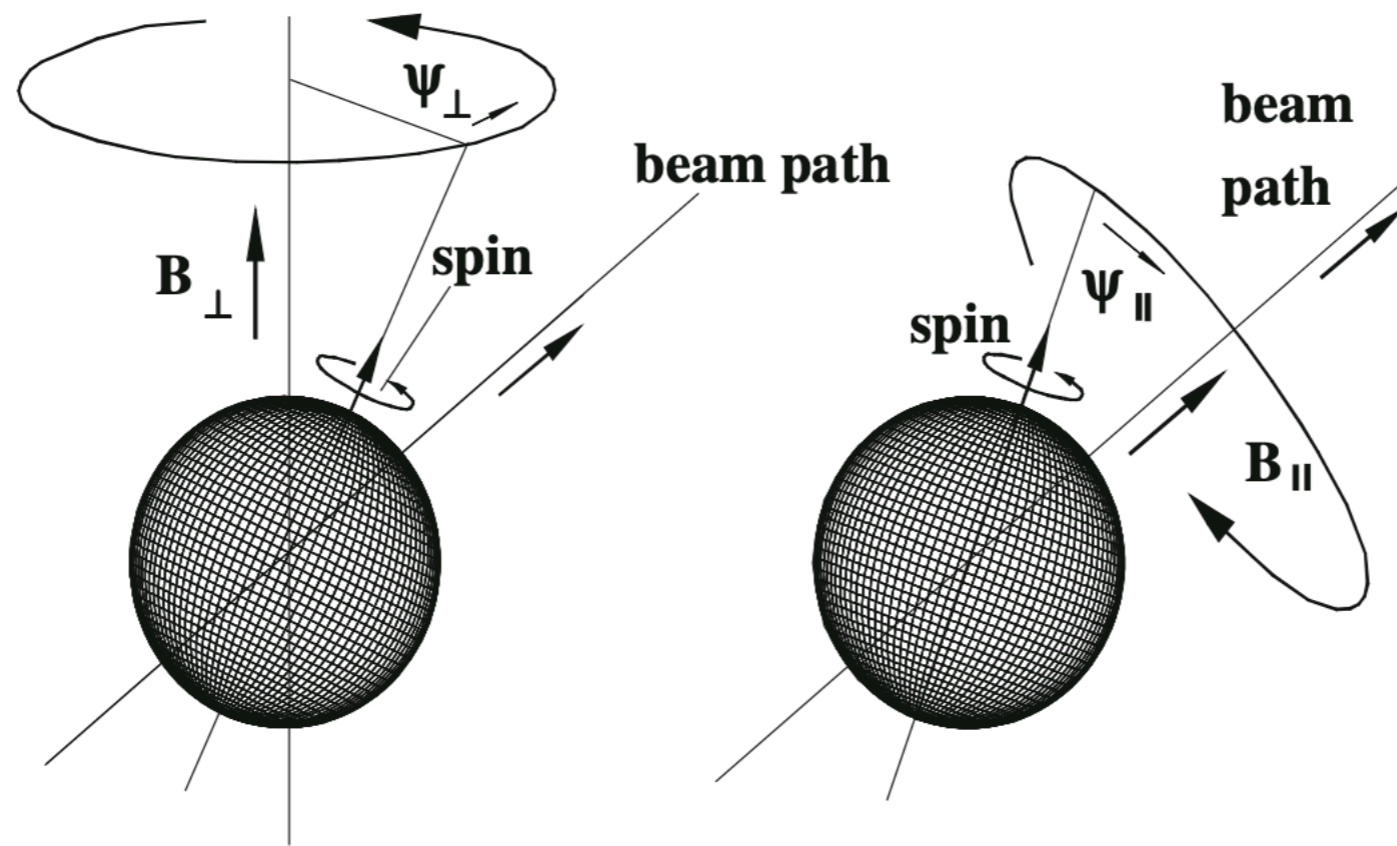
P=80% demonstrated at SLC

polarized positron source:

undulator @ ILC; P=30%

## (i.4) beam polarization

- precession of particle spin under B-field



at a linear collider, to preserve longitudinal beam polarizations,  
spin rotators are needed before & after damping ring  
at a circular collider, transverse beam polarizations are possible

## (i.5) ILC

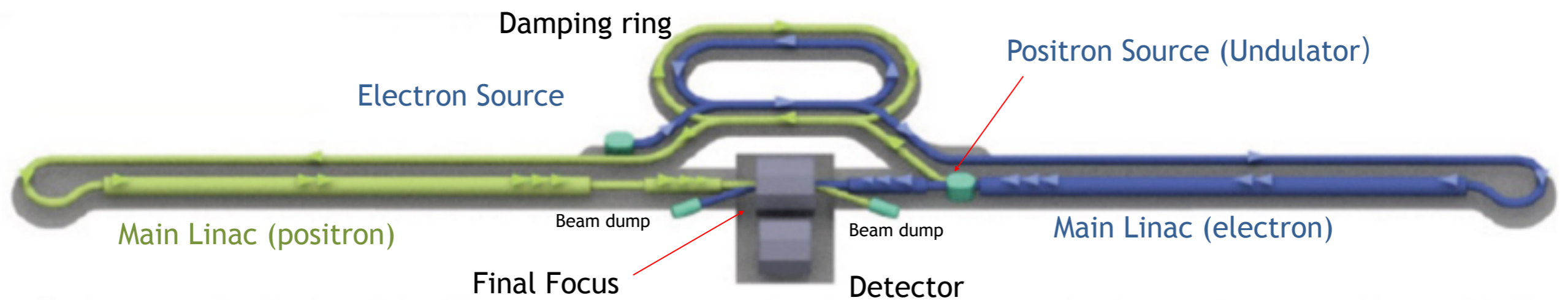
- International Linear Collider (ILC)

key technologies



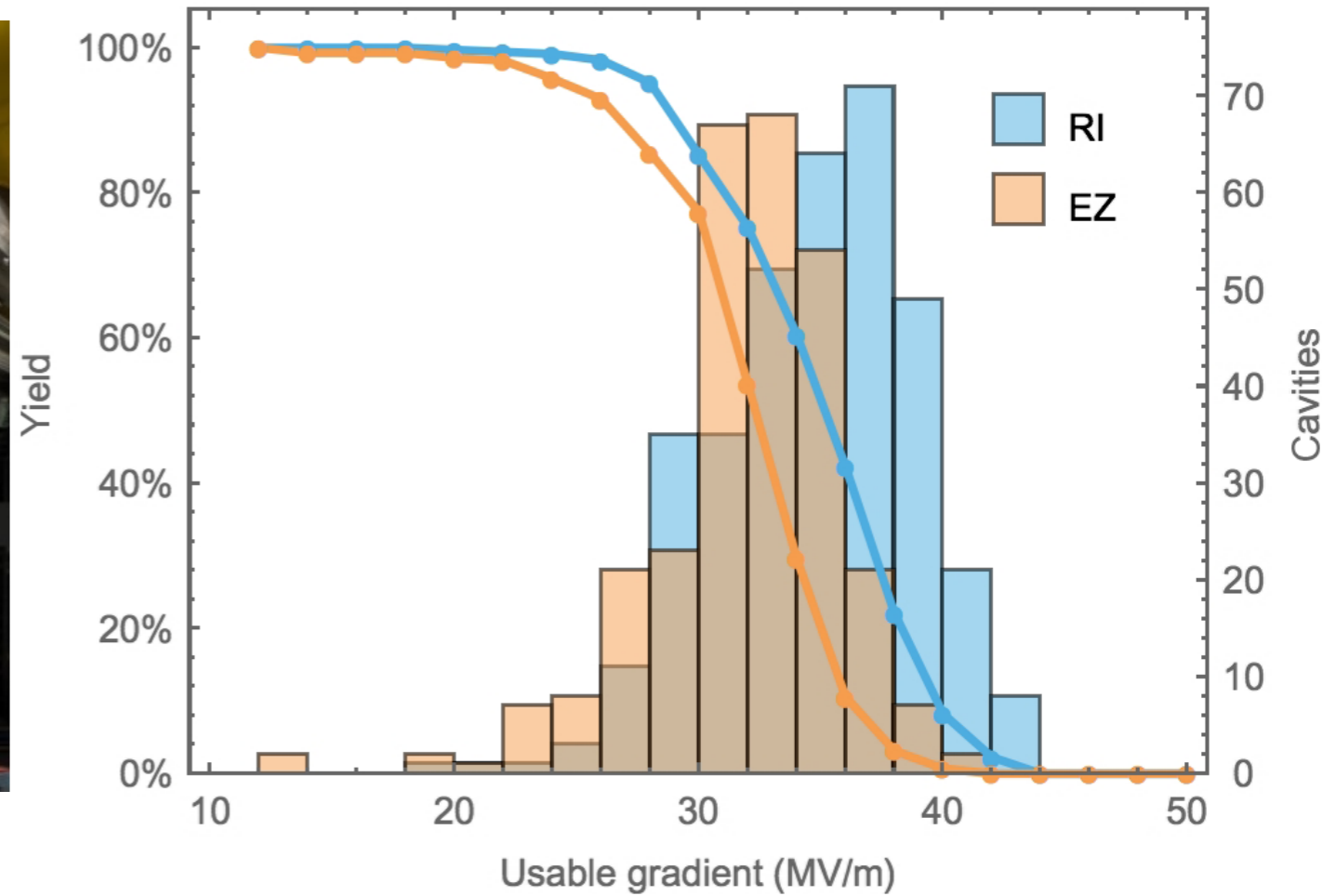
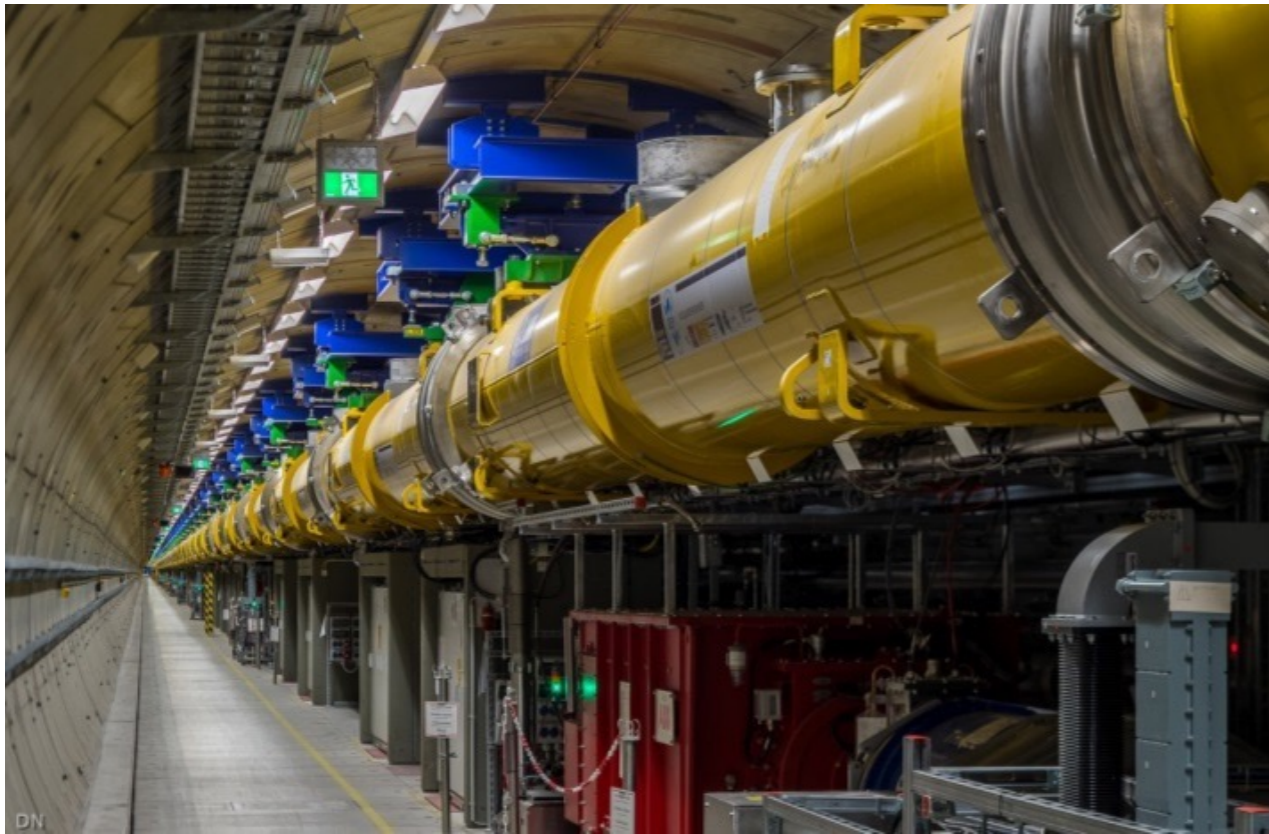
Superconducting RF: 1.3GHz;  $\sim 31.5\text{MeV/m}$

Nano beam:  $\sigma_y \sim 8\text{nm}$ ;  $\sigma_x \sim 500\text{nm}$



## (i.5) ILC

- SRF technology: mature & robust

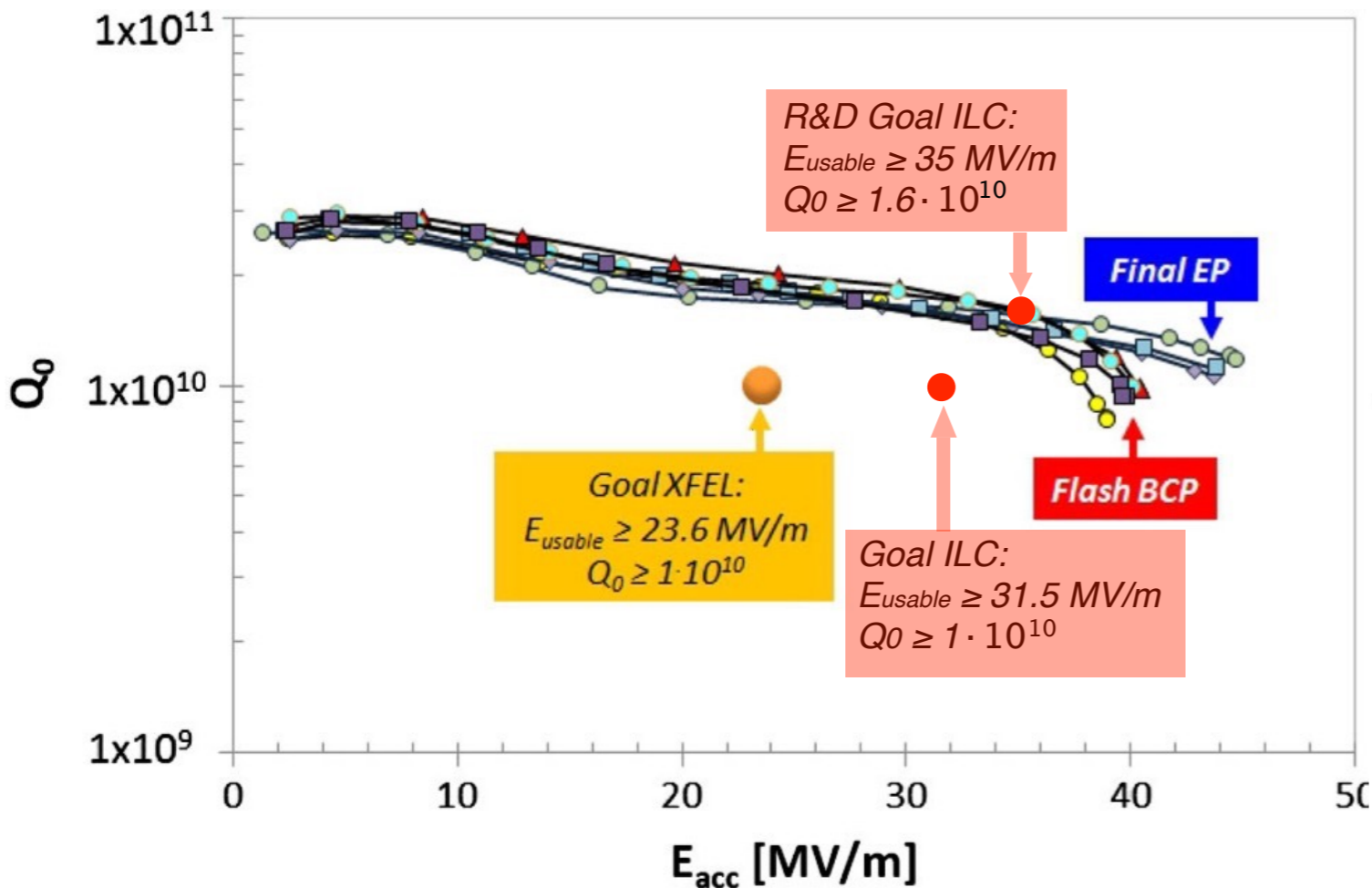


~800 cavities installed & running @ E-XFEL

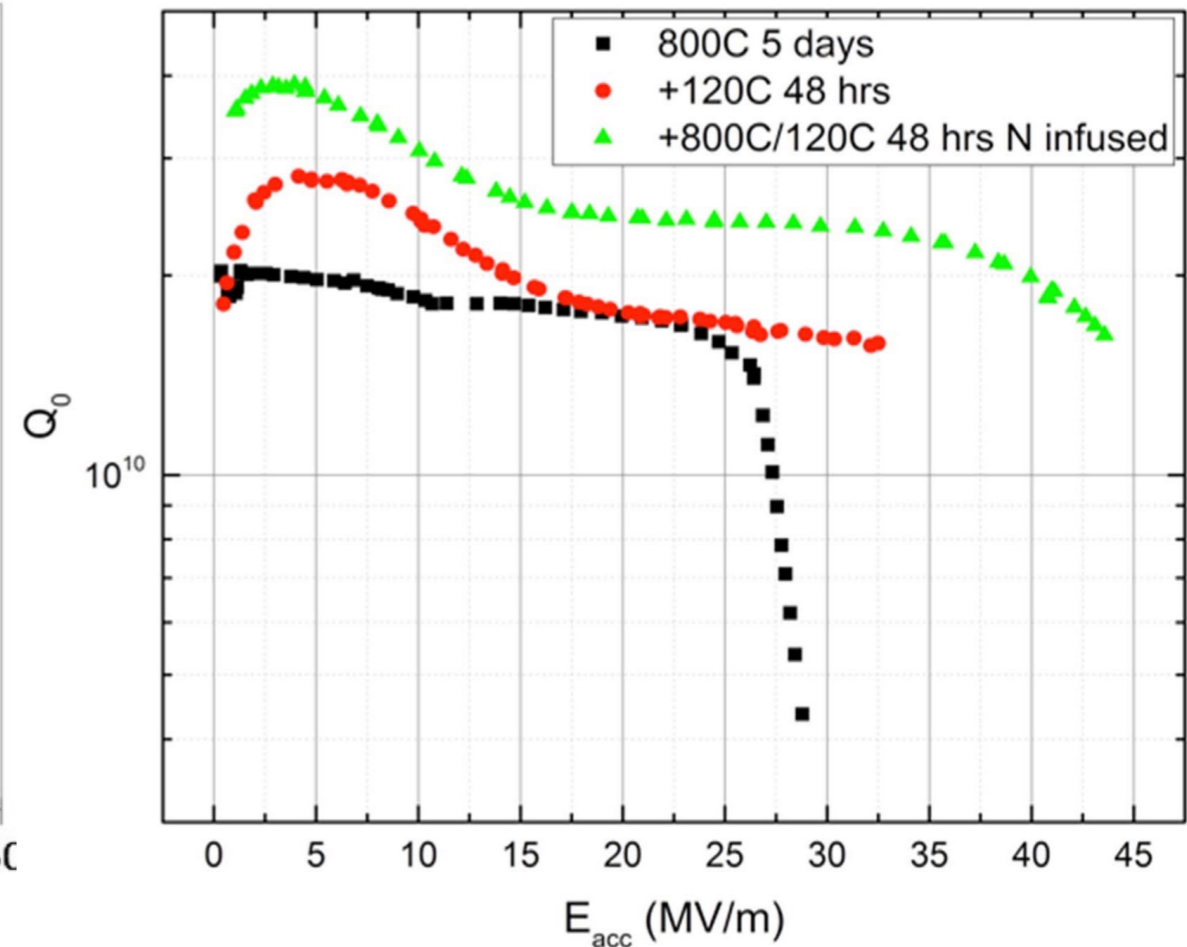


## (i.5) ILC

- SRF technology: potential for further improvement



some of the best cavities  
produced for E-XFEL

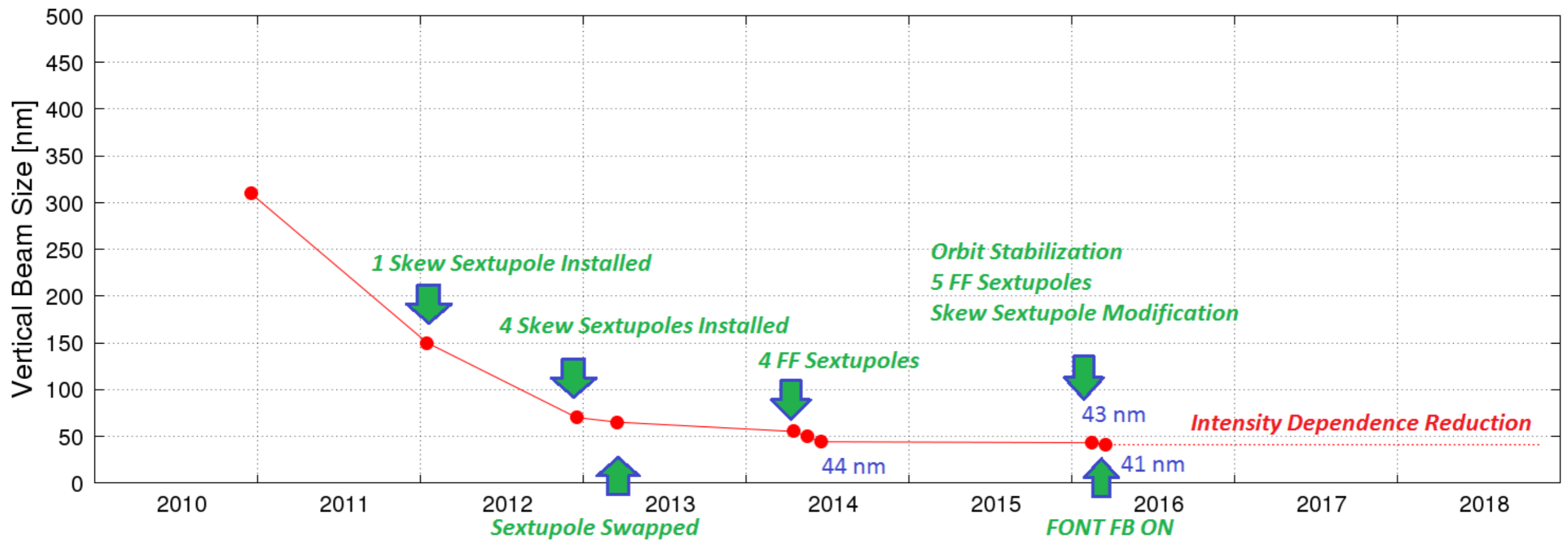


ongoing R&D  
Nitrogen infusion



# (i.5) ILC

- Nano beam: demonstration @ ATF2, KEK



37nm @ 1.3 GeV ~ 5.7nm @ 250 GeV

(ii)

## introduction to detectors

(ii.1) passage of particles through matter

(ii.2) type of detectors

(ii.3) detector concepts @ ILC

(ii.4) detector simulation / reconstruction

## (ii.1) passage of particle through matter

---

- electronic energy loss by charged particles ( $m > m_e$ )

from ionization, atomic excitation

Bethe's equation:

$$\left\langle -\frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 W_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

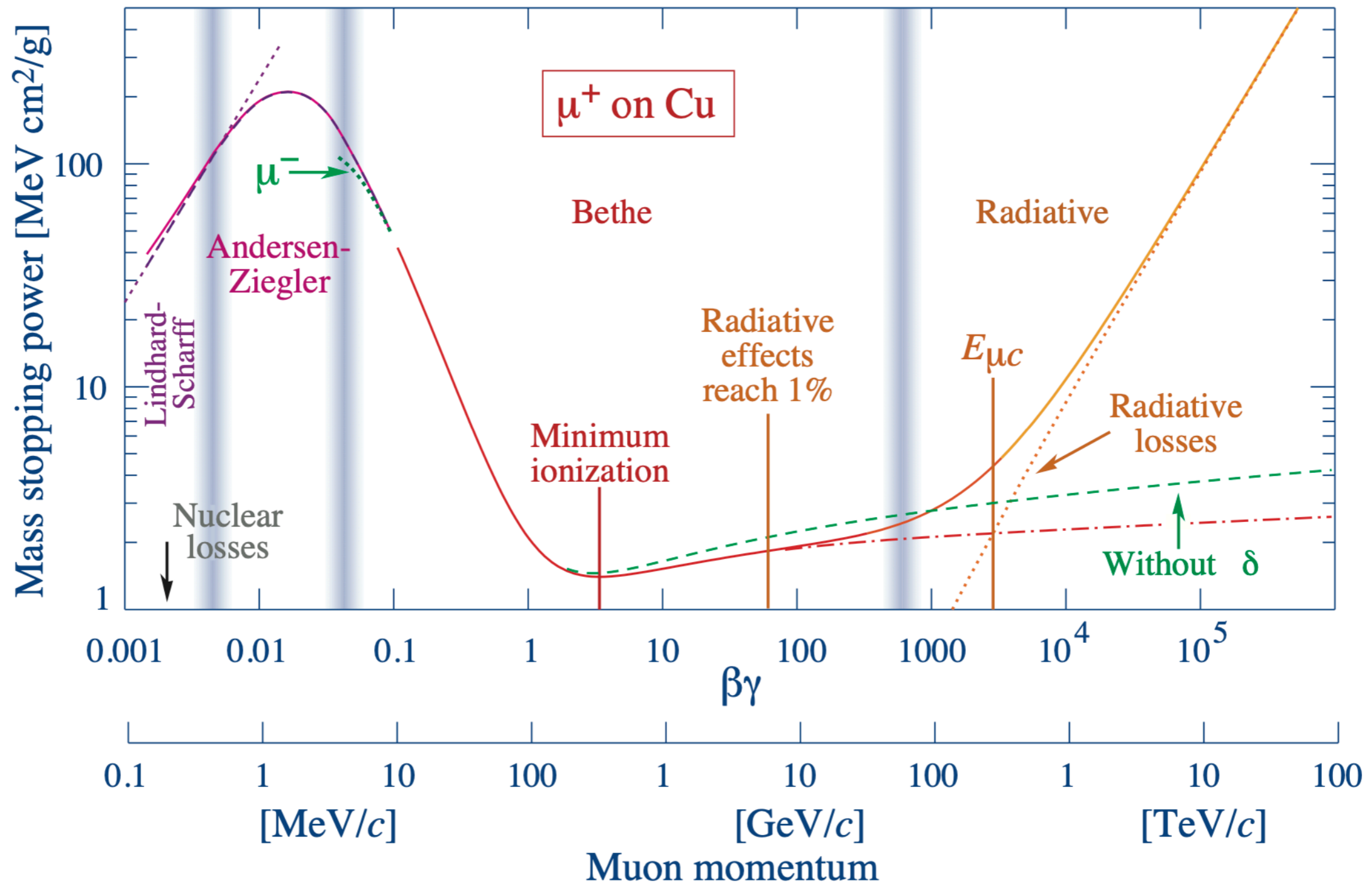
mass stopping power

linear stopping power:  $\times \rho$

logarithmic increase for relativistic particles

(ii.1) passage of particle through matter

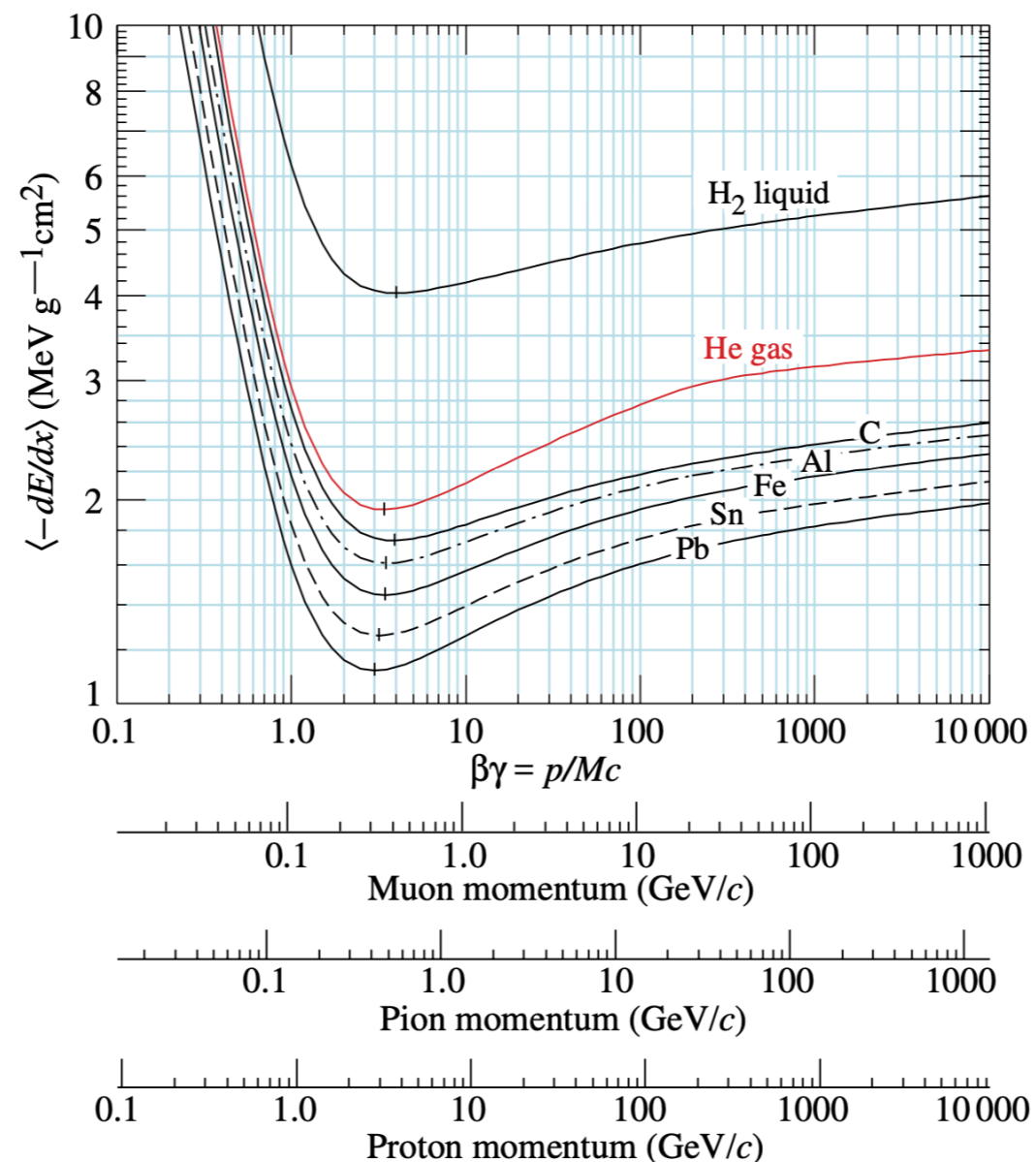
- electronic energy loss by charged particles



## (ii.1) passage of particle through matter

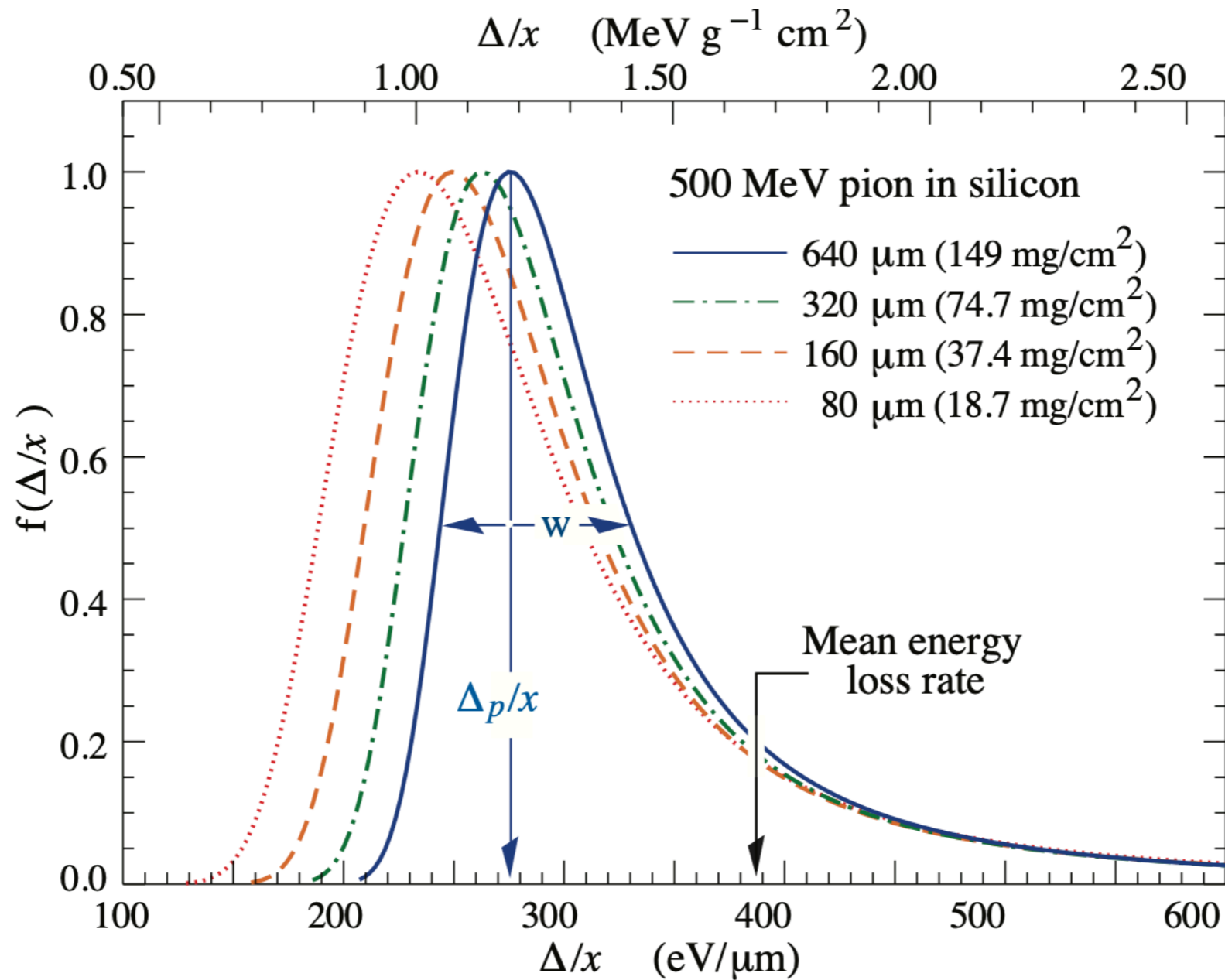
- concept of MIP

1 MIP: an energy deposition of one minimum ionizing particle



## (ii.1) passage of particle through matter

- dE/dx fluctuations: Landau distribution



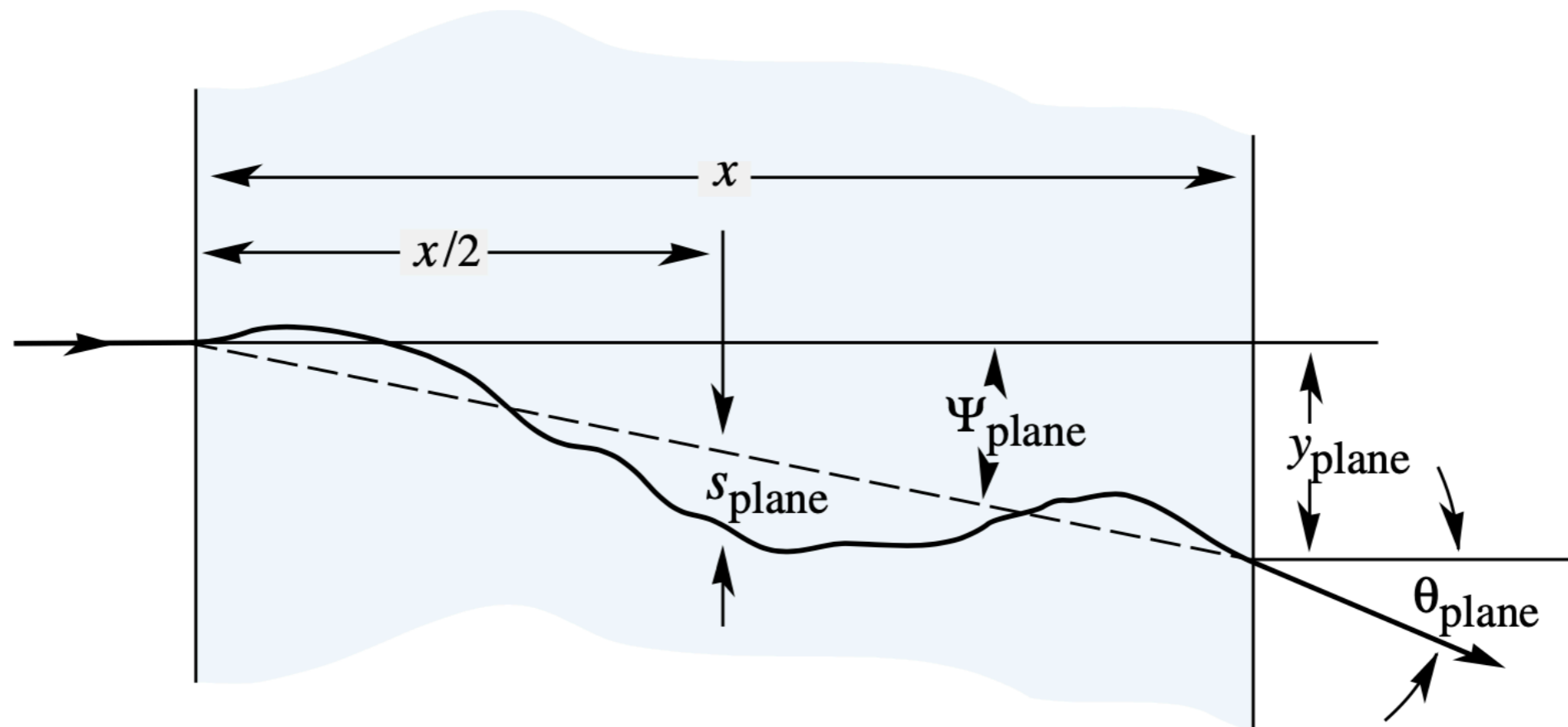
experimentally, the most probable energy loss should be used

## (ii.1) passage of particle through matter

- multiple scattering

a charged particle is deflected by many small scatters

most due to Coulomb scattering from nuclei



important for detector design: material budget

## (ii.1) passage of particle through matter

---

- electromagnetic shower (electron / photon)

electron at rest can't radiate a photon: violate 4-p conservation

$$e^-(P) \rightarrow e^-(p') + \gamma(q)$$

$\begin{array}{c} \sim \\ \otimes \end{array} \frac{m_e^2}{E}$

at relativistic regime, it becomes possible by requiring a small amount of energy transfer from nuclei

for a GeV electron, ~keV transfer

this is Bremsstrahlung

similarly, photon can convert to  $e^+e^-$ : pair production



## (ii.1) passage of particle through matter

---

- radiation length  $X_0$

to characterize energy loss from bremsstrahlung or pair production

use the averaged effects like  $\langle dE/dx \rangle$  is not proper

since they occur infrequently but can lose energy significantly

properer characterization

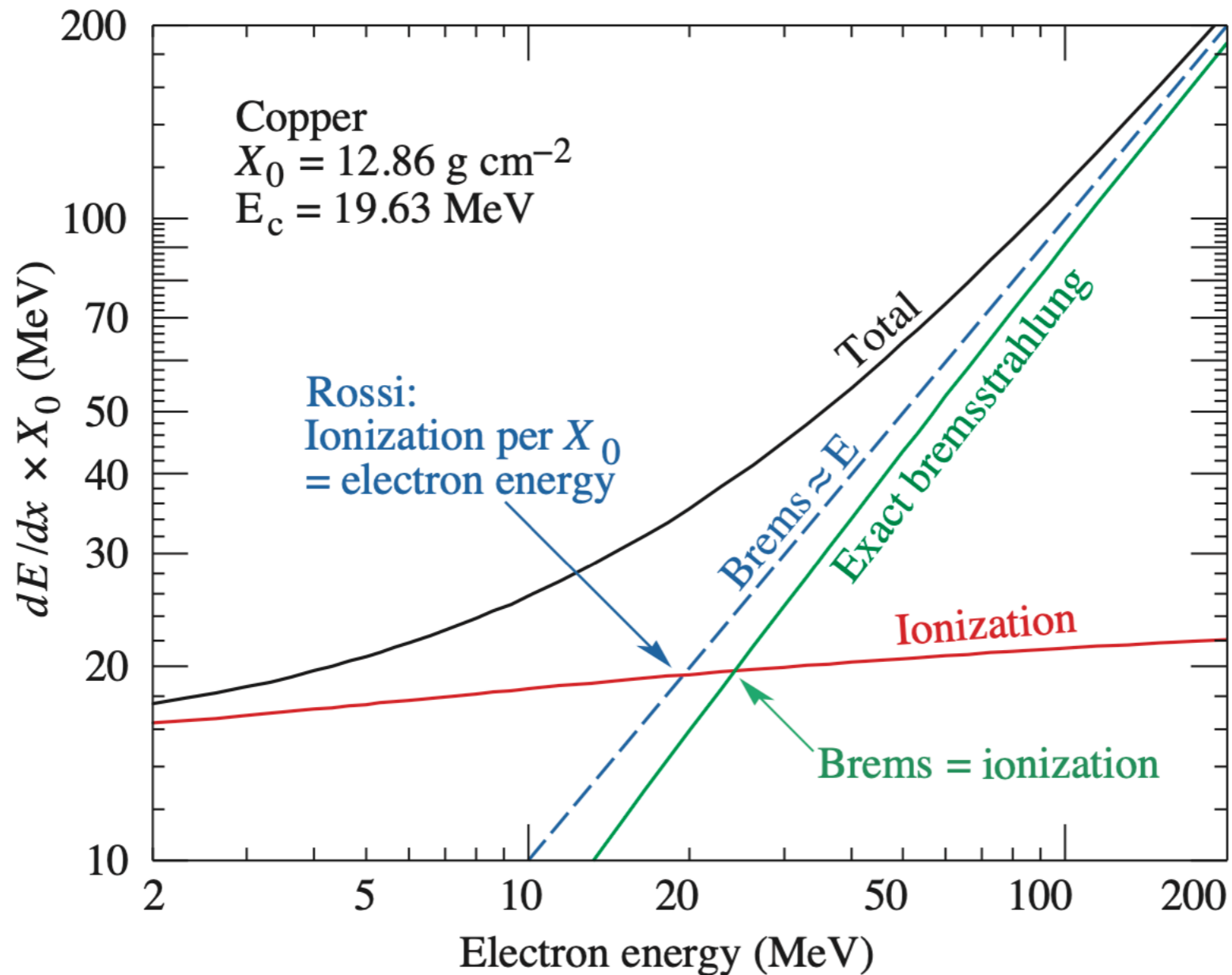
radiation length ( $X_0$ ): the mean distance an electron loses all but 1/e

$$E = E_0 e^{-d/X_0}$$

## (ii.1) passage of particle through matter

- critical energy  $E_c$

bremsstrahlung energy loss  $\sim$  ionization loss



## (ii.1) passage of particle through matter

---

- hadronic shower ( $\pi/K/p/n$ )

strong interaction with nuclei; more complicated shower structure

characterize by interaction length  $\lambda_I$  (in a way similar to  $X_0$ )

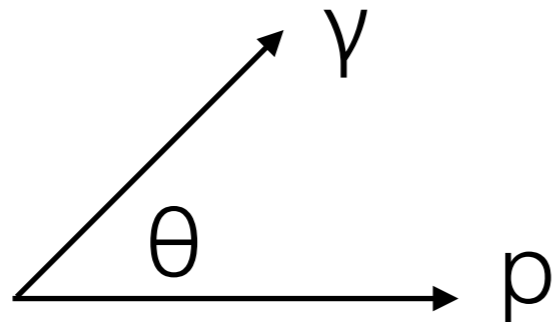
	$X_0$ (cm)	$E_c$ (MeV)	$\lambda_I$ (cm)
Be	35.3	114	59.5
C	18.9	82	38.2
Fe	1.76	22	20.4
W	0.35	8	11.3
Pb	0.56	7	19.9

## (ii.1) passage of particle through matter

---

- Cherenkov radiation

when particles move faster than light in the matter



$$\cos \theta_C = \frac{1}{n\beta}$$

n: index of refraction

similar transition radiation happens when particles move across a border of two different index of refraction

## (ii.2) types of detectors

---

- basic types
  - tracker
  - calorimeter

## (ii.2) types of detectors

- basic types

- tracker

- calorimeter

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PDG

## (ii.2) types of detectors

### • basic types

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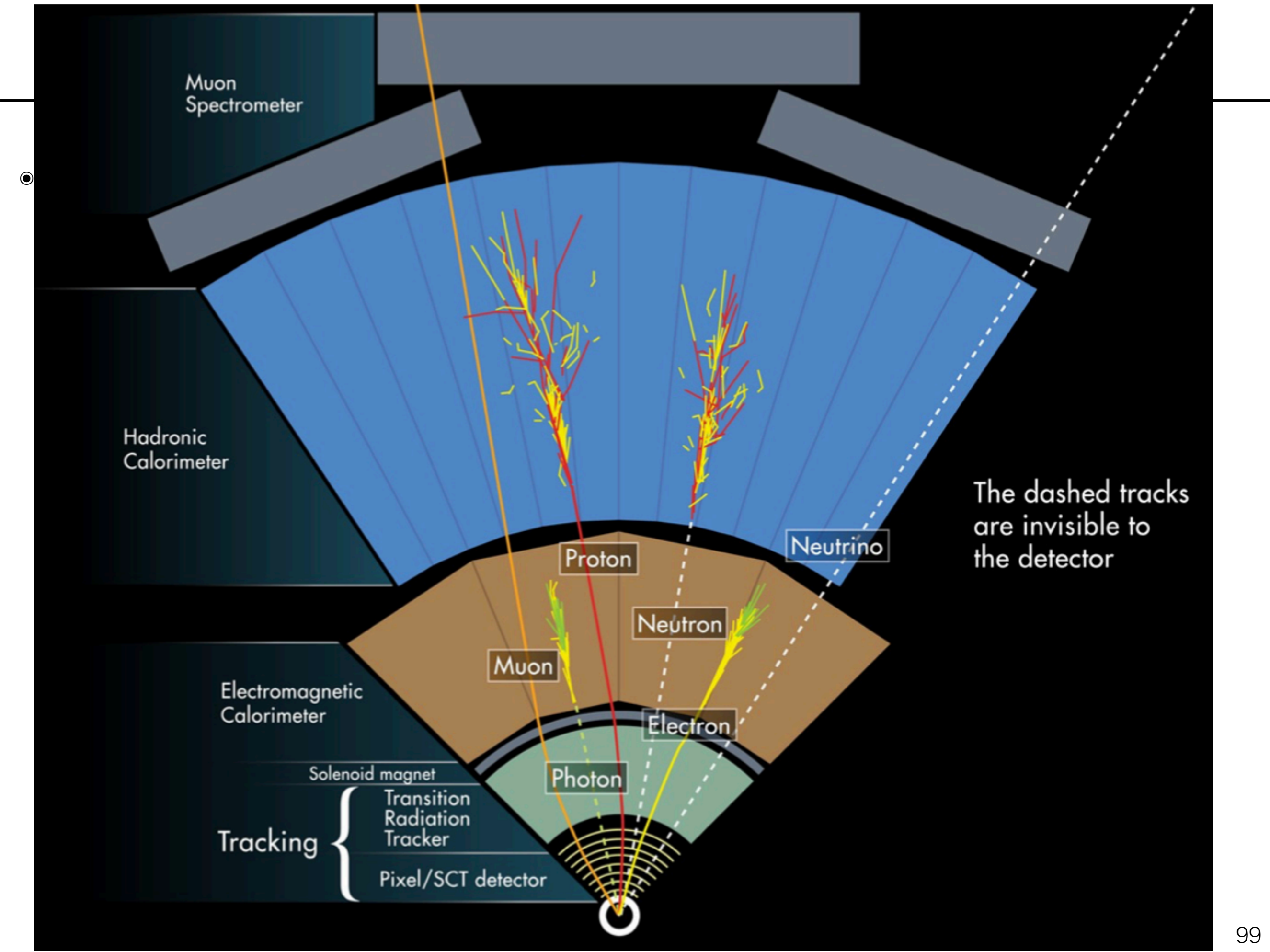
### non-accelerator detectors



## (ii.2) types of detectors

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- an example: various high energy particles in ATLAS



Muon Spectrometer

Hadronic Calorimeter

Electromagnetic Calorimeter

Tracking

Solenoid magnet

Transition Radiation Tracker

Pixel/SCT detector

Proton

Neutron

Muon

Electron

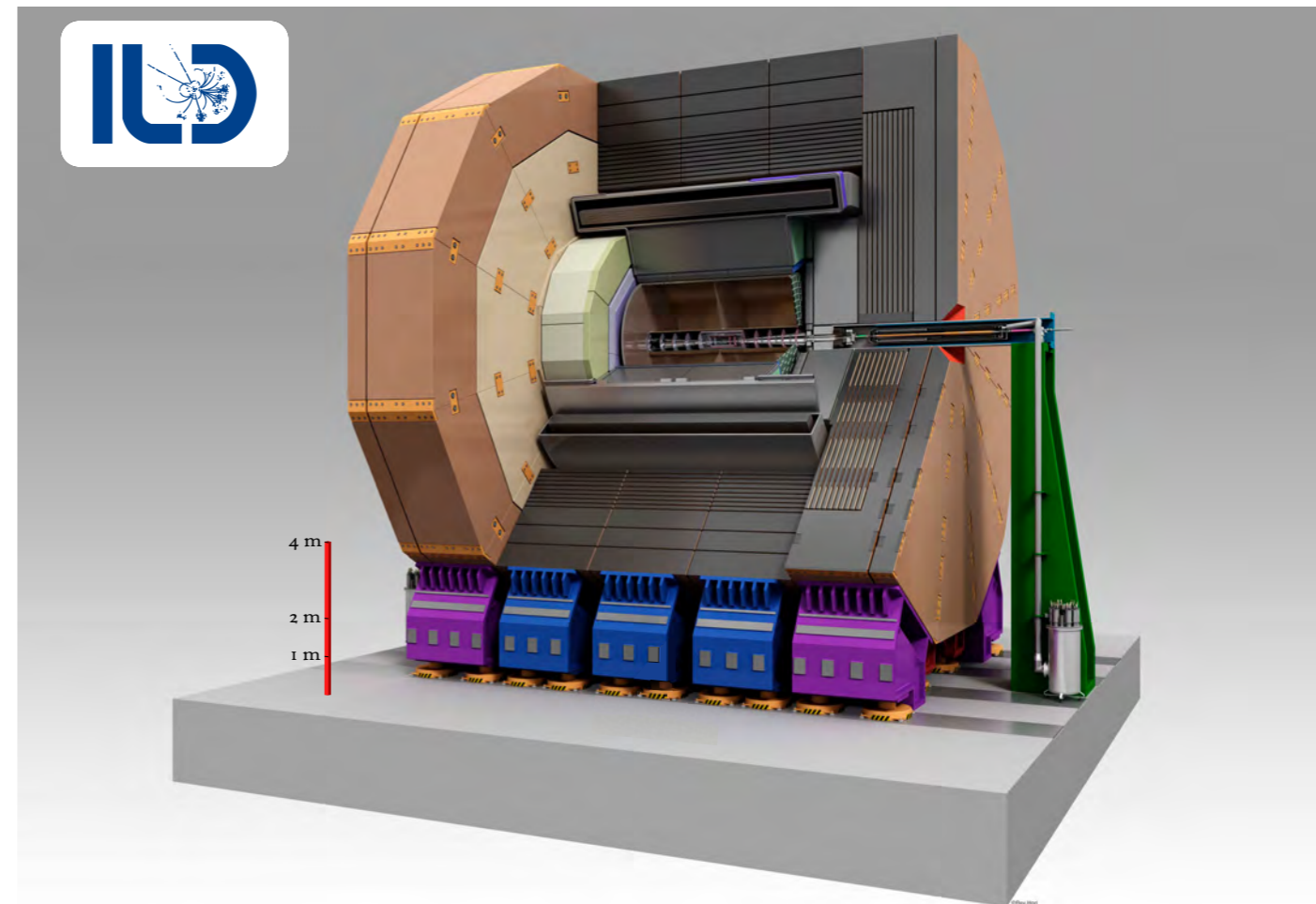
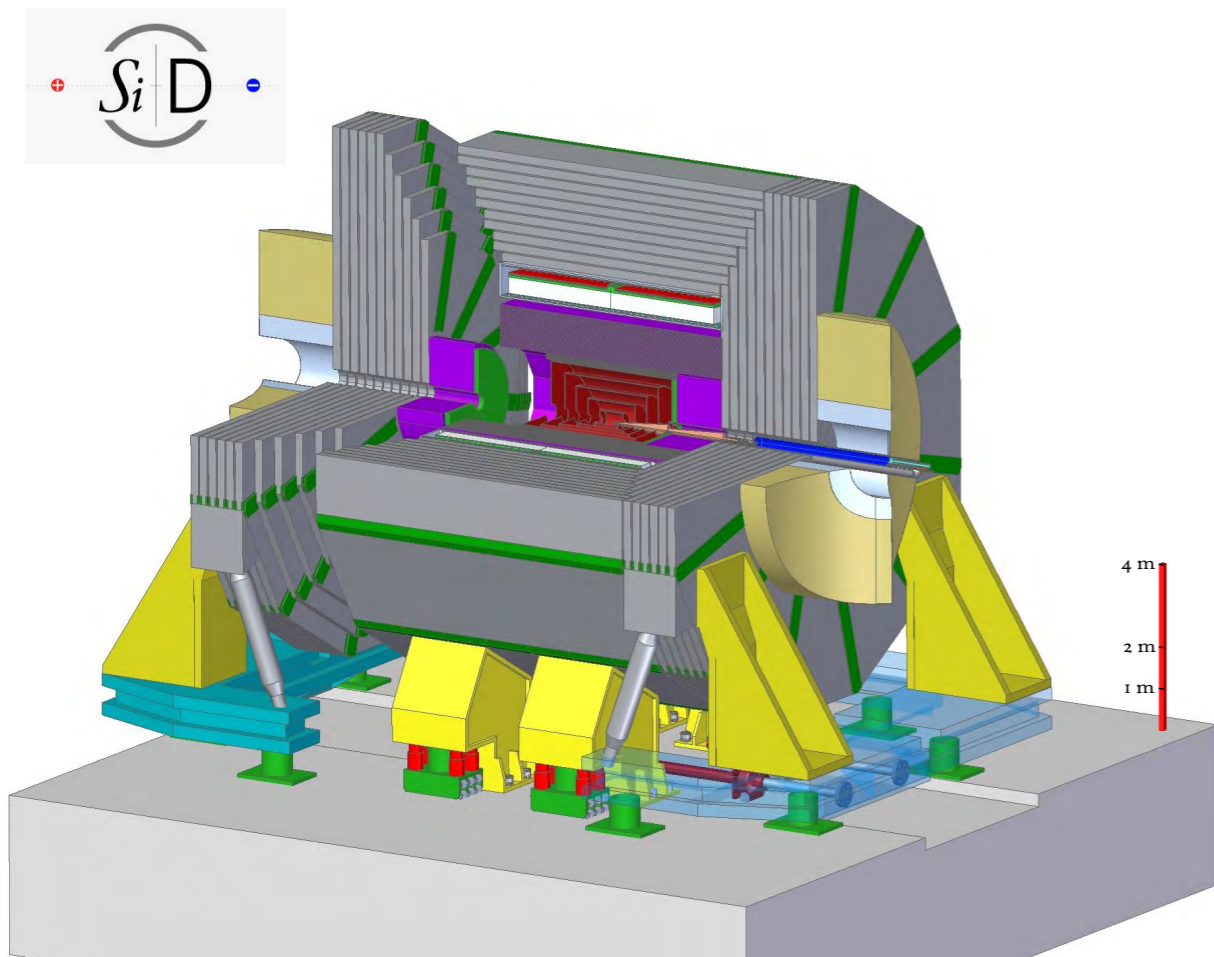
Photon

Neutrino

The dashed tracks are invisible to the detector

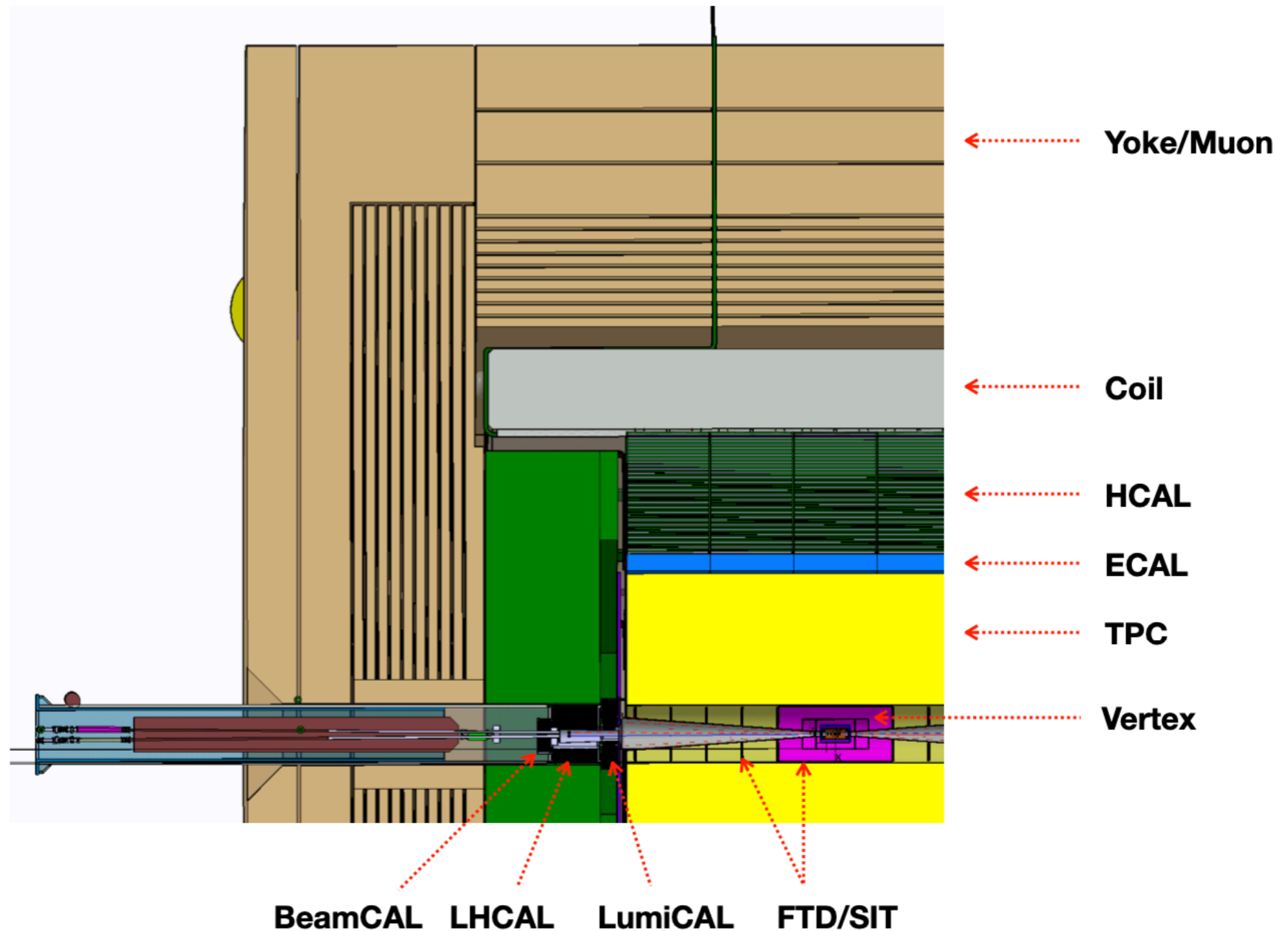
## (ii.3) detectors @ ILC

- two detector concepts; push-pull mechanism in IP



## (ii.3) detectors @ ILC

- ILD: International Large Detector





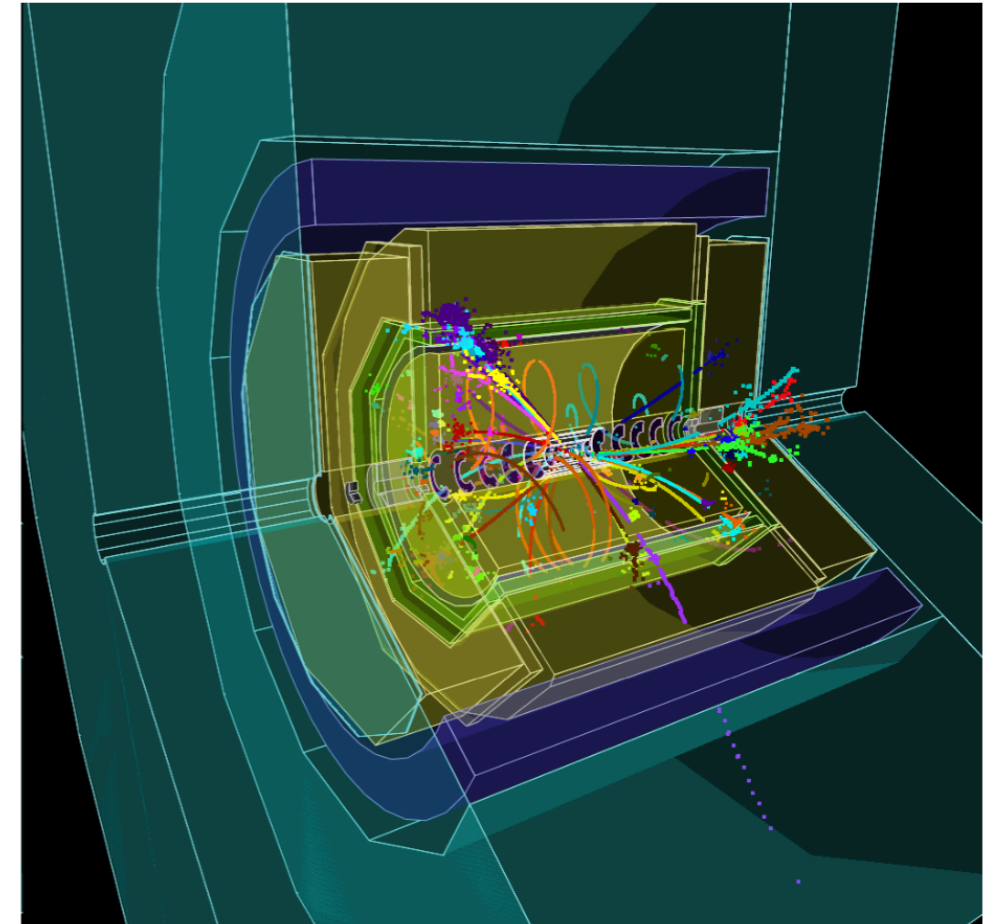
## (ii.3) detectors @ ILC

- concept of Particle Flow

particle flow approach tries to reconstruct every individual particle produced in an event

key challenge is to separate the showers produced by particles from a same jet

-> highly granular calorimeters



Component	Detector	Energy Fract.	Energy Res.	Jet Energy Res.
Charged Particles ( $X^\pm$ )	Tracker	$\sim 0.6 E_j$	$10^{-4} E_{X^\pm}^2$	$< 3.6 \times 10^{-5} E_j^2$
Photons ( $\gamma$ )	ECAL	$\sim 0.3 E_j$	$0.15 \sqrt{E_\gamma}$	$0.08 \sqrt{E_j}$
Neutral Hadrons ( $h^0$ )	HCAL	$\sim 0.1 E_j$	$0.55 \sqrt{E_{h^0}}$	$0.17 \sqrt{E_j}$

## (ii.3) detectors @ ILC

- typical performance

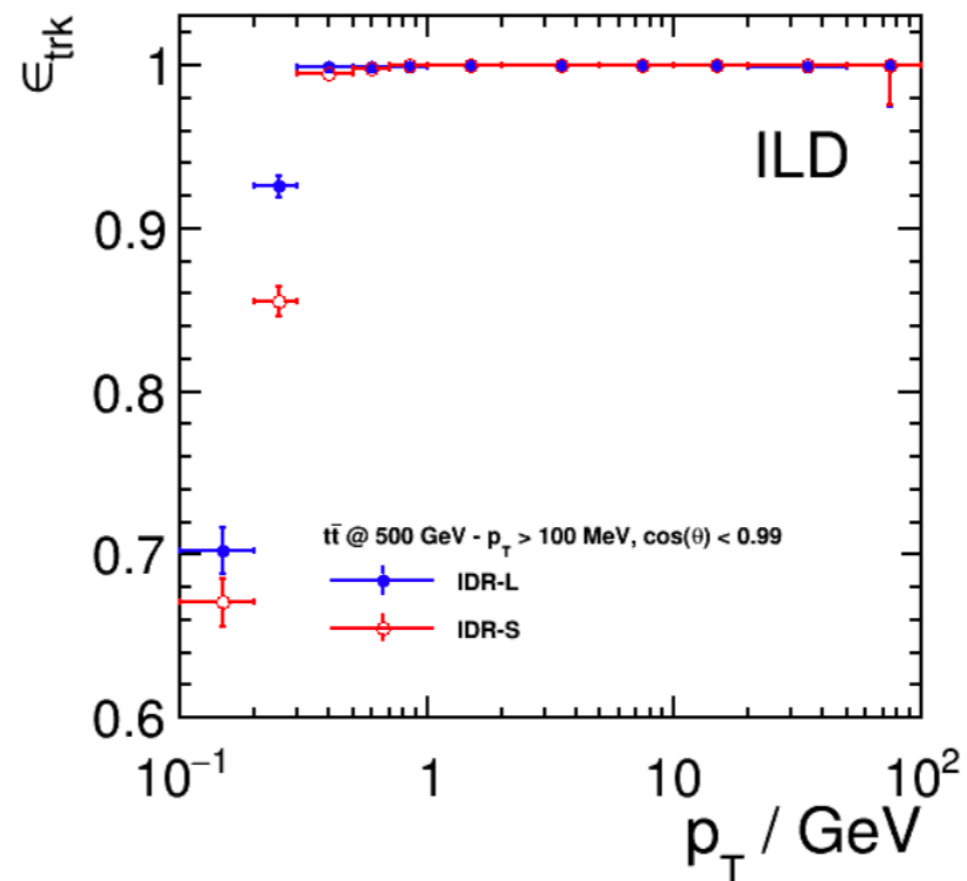
- tracking

momentum resolution

$$\Delta_{1/P_t} = \frac{\Delta P_t}{P_t^2} \sim 2 \times 10^{-5} [\text{GeV}^{-1}]$$

tracking efficiency

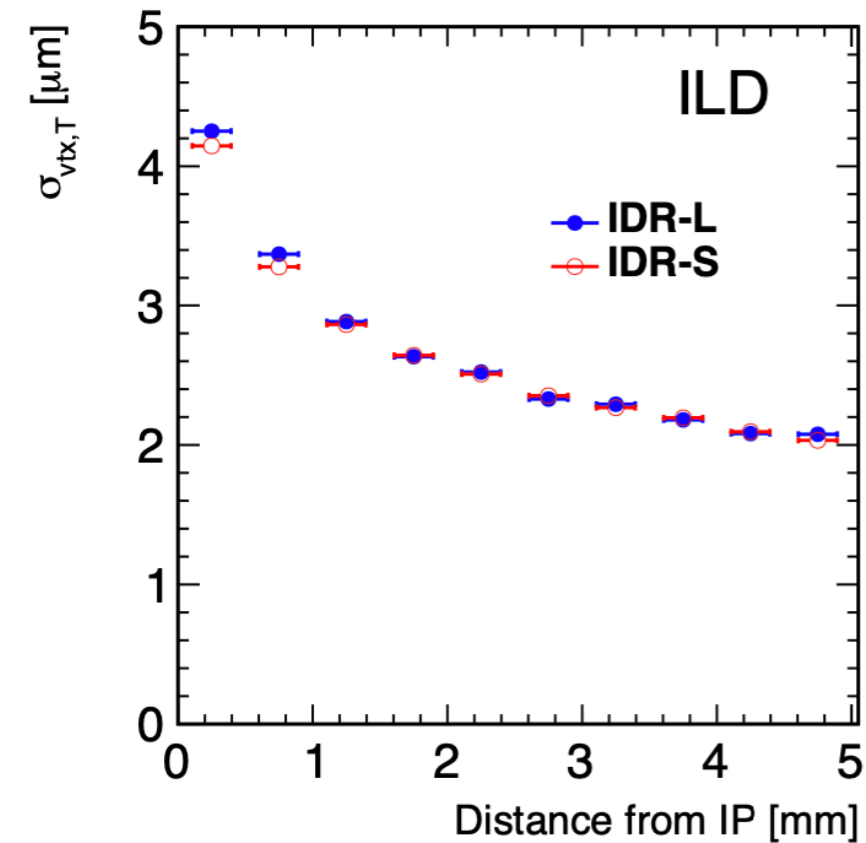
~100% for  $P_T > 300 \text{ MeV}$



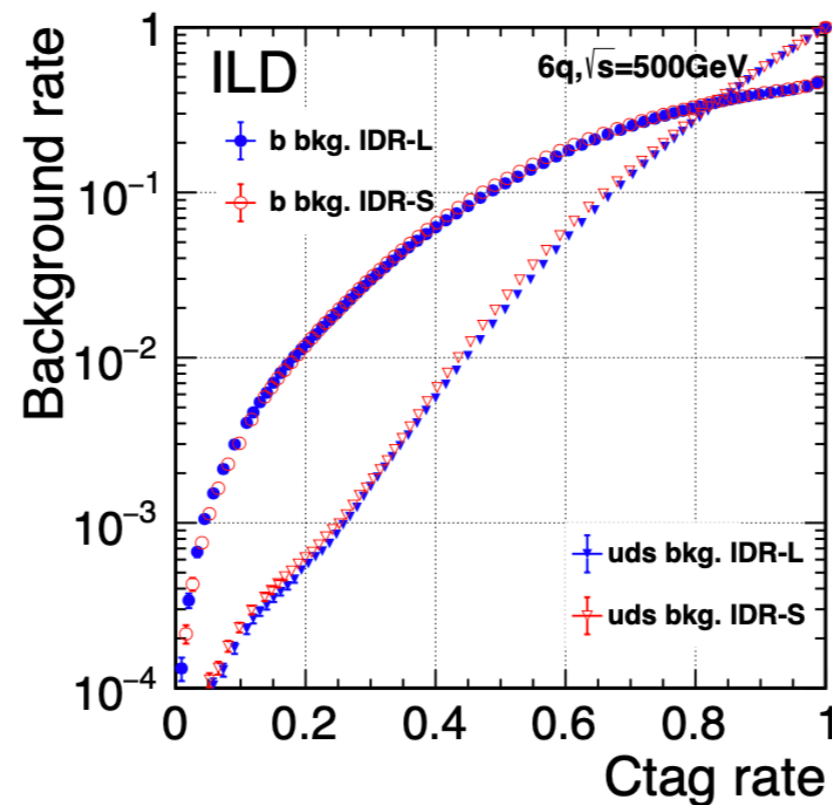
## (ii.3) detectors @ ILC

- typical performance

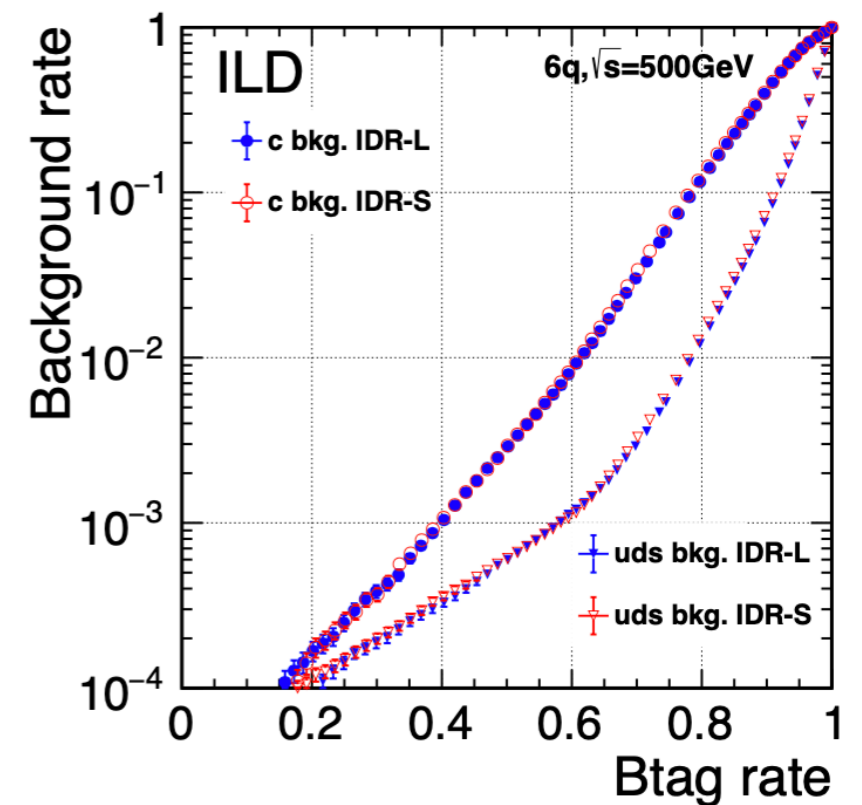
- vertexing



secondary vertex  
position from c-jets



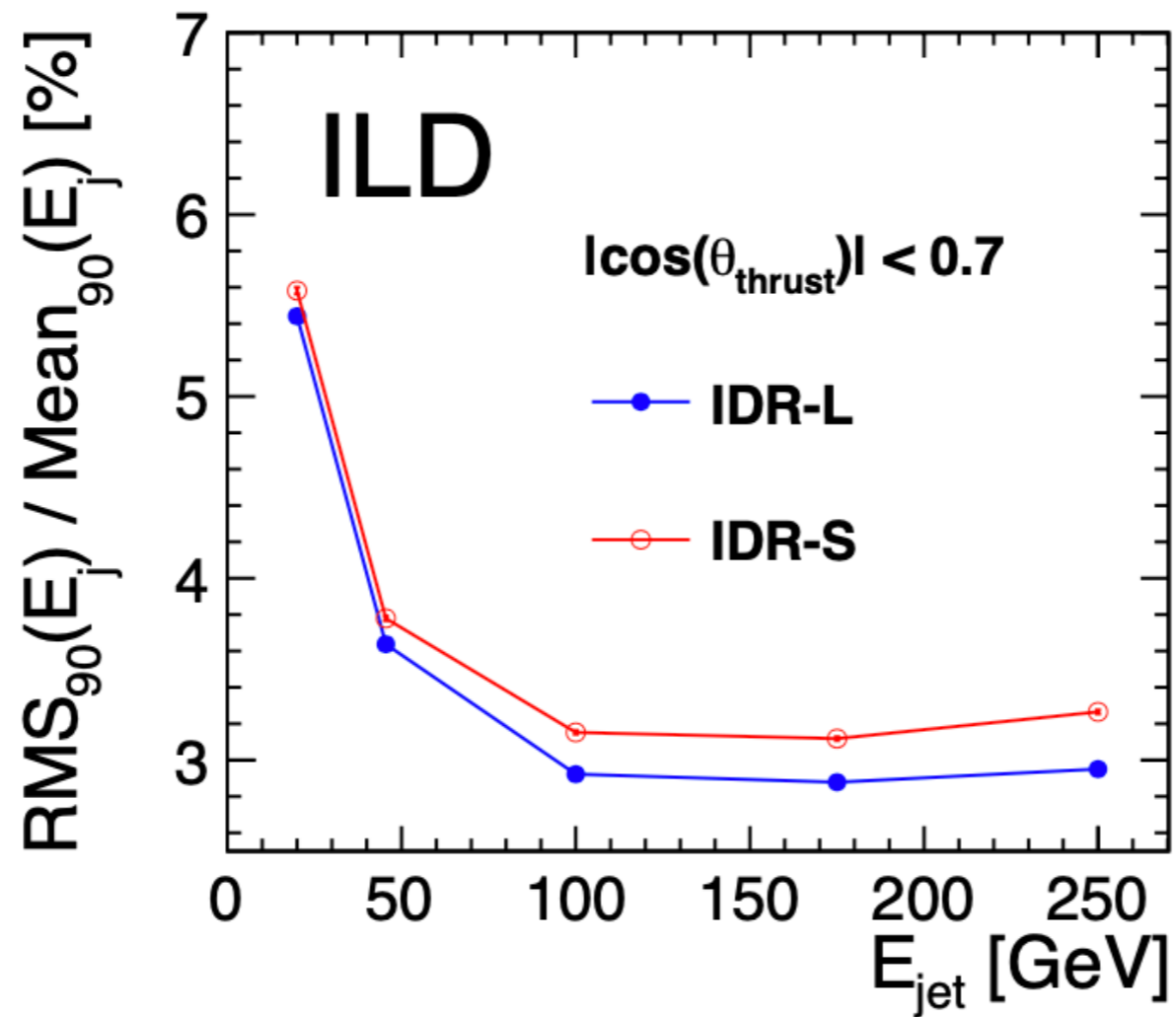
flavor-tagging  
c-jet



flavor-tagging  
b-jet

## (ii.3) detectors @ ILC

- typical performance
  - jet energy resolution





## (ii.4) tools for event simulation & reconstruction

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including effects from ISR & beamstrahlung

parton showering & hadronization by Pythia

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  - full detector simulation; including pile-up events

  - one can also use fast simulation (DELPHES, SGV)

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  - digitization; tracking; particle flow analysis (PandoraPFA)

  - vertex reconstruction; jet clustering; flavor tagging (LCFIPlus)

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- physics analysis

- question: why quadrupole magnets are always placed as a pair?



famous “FODO” structure



- question: why quadrupole magnets are always placed as a pair?



famous “FODO” structure

$$x''(s) + \left(\frac{1}{R^2} - k(s)\right)x(s) = 0$$
$$y''(s) + k(s)y(s) = 0$$

(betatron oscillations)