





# Potential in probes of new physics: rare hyperon decays vs. kaon decays

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#### □ Background & purpose

- $\succ \quad s \to dv \overline{v} \& s \to d\ell^+ \ell^-$
- > Kaons vs. hyperons
- Theoretical framework
- Results and Discussions
- Summary and outlook

# Frontiers in high energy physics



#### **CMS&ATLAS:**

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Higgs Supersymmetric particles New interactions

LCHb&Bellell&BESIII: (Heavy) flavor physics New hadronic states

Indirect detection of NP via rare decays is one of the hottest topics

US Particle Physics Scientific Opportunities: A Strategic Plan for the Next 10 Years

# **Highlights of the year**

the research covered in Physics that **really made waves in and beyond the physics community.** 



#### Four-Quark Matter/BESIII

#### Particle High Five/LHCb



# $s \rightarrow d$ transitions

#### $\Box s \rightarrow d$ transitions are highly suppressed in the SM

the strongest suppression factor



□ As such, they are ideal for tests of the SM and searches for BSM

- G. Buchalla and A. J. Buras, hep-ph/9901288
- V. Cirigliano et al., 1107.6001
- Hai-Bo Li, 1612.01775
- A. A. Alves Junior et al., 1808.03477



#### Latest experimental results



Predictions in SM@1503.02693

NA62@2007.08218(upper limit)



Predictions in SM@1503.02693

- KOTO@1810.09655



□ The K →  $\pi \nu \overline{\nu}$  results imply that there is still room for new physics (NP), but maybe not so much. However, they are only sensitive to the vectorial (parity even) couplings of the s → d currents.

## $K \to \pi \mathcal{V} \overline{\mathcal{V}}$

#### $\Box$ Branching ratio in $K^+ \rightarrow \pi^+ \mathcal{V} \overline{\mathcal{V}}$ further reduced





#### Latest experimental results



□ Although the  $K \rightarrow \pi \pi v \overline{v}$  modes receive contributions from the axial-vectorial type of NP, the current results provide little constraints on them

$$K_L \rightarrow \mu^+ \mu^-$$
 and  $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ 

□ The branching ratio of the  $K_L \rightarrow \mu^+ \mu^-$  decay and the leptonic forward-backward asymmetry (AFB) of the  $K^+ \rightarrow \pi^+ \mu^+ \mu^-$  decay have been measured

BR
$$(K_L \to \mu^+ \mu^-) = (6.84 \pm 0.11) \times 10^{-9}$$
 PTEP 2020, 083C01 (2020)  
 $|A_{FB}| < 2.3 \times 10^{-2}$ , at 90% CL PLB 697, 107 (2011)

They not only are dominated by long-range contributions, but also cannot probe all the interesting axial-vectorial, scalar operators, and their spin flip structures

# Hyperons might be a game changer

- Having spin ½ (instead of spin 0), they lead to different decay modes, observables, as well as sensitivities to the underlying structure of the
  - $s \rightarrow d$  currents



- Experimentally and theoretically more challenging, compared to their kaon siblings
  - > No direct data for  $B_1 \rightarrow B_2 \mathcal{V} \overline{\mathcal{V}}$ ; first theoretical studies only appeared recently
  - > Latest measurement of  $\Sigma^+ \rightarrow p \mu^+ \mu^-$  only with a signal significance of 4.1 sigma

$$\boldsymbol{B}_1 \to \boldsymbol{B}_2 \boldsymbol{\mathcal{V}} \overline{\boldsymbol{\mathcal{V}}}$$

Different from their kaonic counterparts, they are sensitive to both vectorial and axial-vectorial couplings of the  $s \rightarrow d$  currents

#### □ No direct data yet, but promising data from BESIII & LHCb

- BESIII/LHCb experiments in the near future Front. Phys. 12, 121301 (2017) JHEP05(2019)048
- Upper limits derived from Hyperon lifetime PRD 102,015023 (2020)

#### □ On the theory side, the first studies just appeared

Xiao-Hui Hu et al., CPC43(2019)093104; Jusak Tandean, JHEP04(2019)104

#### □ More theoretical studies are needed

- Constraints from/compare with more kaon modes: 2, 3, 4 final states
- The state of the art results from covariant baryon chiral perturbation theory for the relevant form factors

L. S. Geng et al., Phys. Rev. D 79, 094022 (2009) T. Ledwig et al., Phys. Rev. D 90, 054502 (2014)

 $\Sigma^+ \rightarrow p \mu^+ \mu^-$ 

□ Experimental results from HyperCP@PRL 94, 021801 (2004)



 $[8.6^{+6.6}_{-5.4}(\text{stat}) \pm 5.5(\text{syst})] \times 10^{-8}$ 



Di-muon meson 214.3  $\pm$  0.5 MeV

Hype

 $\Sigma^+ \rightarrow p \mu^+ \mu^-$ 



#### **D** Experimental results from LHCb @PRL120, 221803(2018)



# **Our purpose**

Study the hyperon rare decays and compare with their kaon counterparts and investigate their sensitivities to different structures of new physics.

 $\Box s \rightarrow d v \overline{v}$  transitions dominated by short–distance contributions



# **Our purpose**

Study the hyperon rare decays and compare with their kaon counterparts and investigate their sensitivities to different structures of new physics.

 $\Box s \rightarrow d\mu^+\mu^-$  transitions dominated by long-distance contributions



The leptonic forward backward asymmetry can be useful to constrain new physics

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### **The LE effective Hamiltonian** *s* → *d transitions*

**In SM** 
$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \lambda_t \left( \sum_{i=1}^{10} C_i O_i + \sum_{\ell=e,\mu,\tau} C_{\nu_\ell}^L O_{\nu_\ell}^L \right) \quad \lambda_q = V_{qs} V_{qd}^* \text{ Nucl. Phys. B548, 309 (1999)}$$

 $\succ$   $s \rightarrow d \nu \overline{\nu}$  transitions

$$C_{\nu_{\ell}}^{L} = \frac{1}{2\pi \sin^{2} \theta_{W}} \left( \frac{\lambda_{c}}{\lambda_{t}} X_{c}^{\ell} + X_{t} \right) \qquad O_{\nu_{\ell}}^{L} = \alpha \left( \bar{d} \gamma_{\mu} (1 - \gamma_{5}) s \right) \left( \bar{\nu}_{\ell} \gamma^{\mu} (1 - \gamma_{5}) \nu_{\ell} \right)$$

 $\succ$   $s \rightarrow d\ell^+ \ell^-$  transitions

Short-distance 
$$O_7 = \frac{e}{4\pi} m_s \bar{d} \sigma_{\mu\nu} (1+\gamma_5) s F^{\mu\nu}$$
  
 $O_9 = \alpha \left( \bar{d} \gamma_\mu (1-\gamma_5) s \right) \left( \bar{\ell}^- \gamma^\mu \ell^+ \right)$   
 $O_{10} = \alpha \left( \bar{d} \gamma_\mu (1-\gamma_5) s \right) \left( \bar{\ell}^- \gamma^\mu \gamma_5 \ell^+ \right)$   
Long-distance  $\mathcal{M}_{\text{LD}} = -\frac{e^2 G_F}{q^2} \bar{B}_2 \sigma_{\mu\nu} q^\nu (a+b\gamma_5) B_1 \bar{\ell}^- \gamma^\mu \ell^+ - e^2 G_F \bar{B}_2 \gamma_\mu (c+d\gamma_5) B_1 \bar{\ell}^- \gamma^\mu \ell^+$   
 $\Box$  In BSM (NP)  $\Sigma^+ \to p\gamma^*$ 

The NP operators can be obtained by a chiral flip in the quark current, and one also has scalar, pseudoscalar and their primed operators.

$$O_{S} = \alpha \left( \bar{d}(1+\gamma_{5})s \right) \left( \bar{\ell}^{-}\ell^{+} \right), \qquad O_{S}' = \alpha \left( \bar{d}(1-\gamma_{5})s \right) \left( \bar{\ell}^{-}\ell^{+} \right),$$
$$O_{P} = \alpha \left( \bar{d}(1+\gamma_{5})s \right) \left( \bar{\ell}^{-}\gamma_{5}\ell^{+} \right), \qquad O_{P}' = \alpha \left( \bar{d}(1-\gamma_{5})s \right) \left( \bar{\ell}^{-}\gamma_{5}\ell^{+} \right).$$

### SM operators and Feynman diagrams for $s \rightarrow d\mathcal{V}\overline{\mathcal{V}}$ and $s \rightarrow d\mu^+\mu^-$ decays





 $s \rightarrow d\mathcal{V}\overline{\mathcal{V}}$  transitions:



Wilson coefficient  $C_i(\mu)$  are calculated in PT at  $\mu = m_w$  and rescaled to  $\mu = 1$  GeV.  $\Box$  O<sub>T</sub> does not contribute to  $s \rightarrow d\mu^+\mu^-$  transitions PRL.113.241802.

**Decay mode 1:**  $B_1 \rightarrow B_2 \mathcal{V} \overline{\mathcal{V}}$ 



The total decay width in the presence of NP, expanded up to NLO in  $\delta,$  can be written as

$$\Gamma = \sum_{\ell=e,\mu,\tau} \frac{\alpha^2 G_F^2 |\lambda_t|^2 f_1(0)^2 \Delta^5}{60\pi^3} \cdot \left[ \left( 1 - \frac{3}{2}\delta \right) \left| C_{\nu_\ell}^L + C_{\nu_\ell}^R \right|^2 + 3\left( 1 - \frac{3}{2}\delta \right) \frac{g_1(0)^2}{f_1(0)^2} \left| C_{\nu_\ell}^L - C_{\nu_\ell}^R \right|^2 + O\left(\delta^2\right) \right]$$

□ These decay channels are sensitive to vectorial (parity even) and axial-vectorial (parity odd) couplings of the  $s \rightarrow d$  currents

A reliable determination of the form factors is necessary to better control uncertainties

### Form factors relevant to $B_1 \rightarrow B_2 \mathcal{V} \overline{\mathcal{V}}$

Following PRL114 (2015) 161802, the form factors are obtained from covariant baryon chiral perturbation theory up to one loop order, and thus providing model independent inputs

$$f_{1}(0)^{\Lambda n} = -\sqrt{\frac{3}{2}} \cdot \left(1 + \delta f_{1}(0)^{\Lambda n}\right),$$
  

$$f_{1}(0)^{\Sigma^{+}p} = -1 \cdot \left(1 + \delta f_{1}(0)^{\Sigma^{+}p}\right),$$
  

$$f_{1}(0)^{\Xi^{0}\Sigma^{0}} = -\sqrt{\frac{1}{2}} \cdot \left(1 + \delta f_{1}(0)^{\Xi^{0}\Sigma^{0}}\right),$$
  

$$f_{1}(0)^{\Xi^{0}\Lambda} = \sqrt{\frac{3}{2}} \cdot \left(1 + \delta f_{1}(0)^{\Xi^{0}\Lambda^{0}}\right),$$

	$\Lambda n$	$\Sigma^+ p$	$\Xi^0 \Sigma^0$	$\Xi^0\Lambda$
$\delta f_1(0)$	$0.001\substack{+0.013\\-0.010}$	$0.087^{+0.042}_{-0.031}$	$0.017\substack{+0.022\\-0.016}$	$0.040\substack{+0.028\\-0.021}$
$g_1(0)$	-0.89(2)	0.33(2)	-0.86(3)	0.24(4)

L. S. Geng et al., Phys. Rev. D 79, 094022 (2009) T. Ledwig et al., Phys. Rev. D 90, 054502 (2014)

### **Decay mode 2:** $K \rightarrow \pi \mathcal{V} \overline{\mathcal{V}}$

Isospin symmetry relate the form factors in the FCNC processes to those of the well-known charge-current decays

$$\langle \pi^+ | (\bar{s}d)_{V-A} | K^+ \rangle = \sqrt{2} \langle \pi^0 | (\bar{s}u)_{V-A} | K^+ \rangle,$$
$$\langle \pi^0 | (\bar{s}d)_{V-A} | K^0 \rangle = \langle \pi^0 | (\bar{s}u)_{V-A} | K^+ \rangle.$$



**D** Branching ratios of two  $K \rightarrow \pi \nu \overline{\nu}$  processes in the presence of NP are

$$BR(K^{+} \to \pi^{+} \nu \bar{\nu}) = \frac{2\alpha^{2} |\lambda_{t}|^{2} BR(K^{+} \to \pi^{0} e^{+} \nu_{e})}{|V_{us}|^{2}} \sum_{\ell=e,\mu,\tau} |C_{\nu_{\ell}}^{L} + C_{\nu_{\ell}}^{R}|^{2},$$
  
$$BR(K_{L} \to \pi^{0} \nu \bar{\nu}) = \frac{2\alpha^{2} \tau_{K_{L}} BR(K^{+} \to \pi^{0} e^{+} \nu_{e})}{\tau_{K^{+}} |V_{us}|^{2}} \sum_{\ell=e,\mu,\tau} \left( Im[(C_{\nu_{\ell}}^{L} + C_{\nu_{\ell}}^{R})\lambda_{t}^{*}]\right)^{2},$$

> The 3-body decay channels are only sensitive to **vectorial couplings** of the  $s \rightarrow d$  currents

> Uncertainties are mainly from the measurements of the charged current  $K^+ \rightarrow \pi^0 e^+ v$  decay.

# **Decay mode 3:** $K \rightarrow \pi \pi \mathcal{V} \overline{\mathcal{V}}$ (I)

Isospin symmetry relate the form factors in the FCNC processes to those of the wellknown charged-current decay

$$\langle \pi^+ \pi^0 | (\bar{s}d)_{V-A} | K^+ \rangle = -\sqrt{2} \langle (\pi^+ \pi^-)_{I=1} | (\bar{s}u)_{V-A} | K^+ \rangle$$

 $\langle \pi^0 \pi^0 | (\bar{s}d)_{V-A} | K^0 \rangle = \langle (\pi^+ \pi^-)_{I=0} | (\bar{s}u)_{V-A} | K^+ \rangle.$ 



- $\Box \text{ Four-body differential decay rate in terms of 9 angular coefficients}$   $\frac{d^5\Gamma}{ds_{\pi}ds_{\ell}d(\cos\theta_{\pi})d(\cos\theta_{\ell})d\phi} = \alpha^2 G_F^2 |\lambda_t|^2 N(s_{\pi}, s_{\ell}) J_5(s_{\pi}, s_{\ell}, \theta_{\pi}, \theta_{\ell}, \phi)$   $J_5 = I_1 + I_2 \cos 2\theta_{\ell} + I_3 \sin^2 \theta_{\ell} \cos 2\phi + I_4 \sin 2\theta_{\ell} \cos \phi + I_5 \sin \theta_{\ell} \cos \phi$   $+ I_6 \cos \theta_{\ell} + I_7 \sin \theta_{\ell} \sin \phi + I_8 \sin 2\theta_{\ell} \sin \phi + I_9 \sin^2 \theta_{\ell} \sin 2\phi,$
- □ After integrating out the angle  $\theta_{\ell}$  and  $\phi$ , only  $I_1$  and  $I_2$  contribute to the **total decay width**, i.e.,

$$\Gamma = \int_{4m_{\pi}^2}^{m_K^2} \int_0^{(m_K - \sqrt{s_{\pi}})^2} \int_{-1}^1 \alpha^2 G_F^2 |\lambda_t|^2 N(s_{\pi}, s_{\ell}) \cdot 4\pi (I_1 - \frac{1}{3}I_2) \cdot ds_{\pi} ds_{\ell} d(\cos \theta_{\pi}).$$

# **Decay mode 3:** $K \rightarrow \pi \pi \mathcal{V} \overline{\mathcal{V}}$ (II)

 $\Box$   $I_1$  and  $I_2$  in terms of helicity amplitudes

$$I_{1} = \frac{s_{\ell}}{2} \left( 3|H_{+}^{V}|^{2} + 3|H_{-}^{V}|^{2} + 2|H_{0}^{V}|^{2} + 3|H_{+}^{A}|^{2} + 3|H_{-}^{A}|^{2} + 2|H_{0}^{A}|^{2} \right),$$
  

$$I_{2} = \frac{s_{\ell}}{2} \left( |H_{+}^{V}|^{2} + |H_{-}^{V}|^{2} - 2|H_{0}^{V}|^{2} + |H_{+}^{A}|^{2} + |H_{-}^{A}|^{2} - 2|H_{0}^{A}|^{2} \right).$$

**\Box** Helicity amplitudes for  $K^+ \rightarrow \pi^+ \pi^0 v \overline{v}$ 

$$\begin{split} H_{0}^{V(A)} &= \frac{i(C_{\nu_{\ell}}^{L} - C_{\nu_{\ell}}^{R}) \left(4F \cdot m_{K}^{2} X + G \cdot \sigma_{\pi} \cos \theta_{\pi} \left(-(s_{l} - s_{\pi})^{2} + m_{K}^{4} + 4X^{2}\right)\right)}{4m_{K}^{3} \sqrt{s_{l}}}, \\ H_{+}^{V(A)} &= -\frac{i \sqrt{s_{\pi}} \sigma_{\pi} \sin \theta_{\pi} \left(G \cdot m_{K}^{2} \left(C_{\nu_{\ell}}^{L} - C_{\nu_{\ell}}^{R}\right) + H \cdot X \left(C_{\nu_{\ell}}^{L} + C_{\nu_{\ell}}^{R}\right)}{\sqrt{2}m_{K}^{3}}, \\ H_{-}^{V(A)} &= \frac{i \sqrt{s_{\pi}} \sigma_{\pi} \sin \theta_{\pi} \left(G \cdot m_{K}^{2} \left(C_{\nu_{\ell}}^{L} - C_{\nu_{\ell}}^{R}\right) - H \cdot X \left(C_{\nu_{\ell}}^{L} + C_{\nu_{\ell}}^{R}\right)}{\sqrt{2}m_{K}^{3}}, \end{split}$$

**\Box** Helicity amplitudes for  $K_L \rightarrow \pi^0 \pi^0 v \overline{v}$ 

$$H_0^{V(A)} = \frac{i\sqrt{2}X \cdot F \cdot \operatorname{Re}\left[\left(C_{\nu_\ell}^L - C_{\nu_\ell}^R \lambda_t^*\right)\right]}{m_K \sqrt{s_l}},$$
$$H_+^{V(A)} = 0,$$
$$H_-^{V(A)} = 0,$$

### Decay modes 4&5: $K_L \rightarrow \mu^+ \mu^-$ and $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ (I)

**D** Branching ratio of  $K_L \rightarrow \mu^+ \mu^-$  JHEP 08, 088 (2006)

$$BR(K_L \to \mu^+ \mu^-) = \left[ 6.7 + \left( \frac{0.08 \alpha \pi^2}{\sqrt{2} G_F m_s m_\mu} Im \left[ \lambda_t^* (C_S - C'_S) \right] \right)^2 + \left( 1.1 (C'_{10} - C_{10}) \right]^2 + \left( 1.1 (C'_{10} - C_{10}) \right)^2 + \left( 1.1 (C'_{10} - C_{10}) \right)^2$$

**D** For the  $K^+ \rightarrow \pi^+ \mu^+ \mu^-$  decay

$$\begin{aligned} \frac{d\Gamma}{dq^2 d\cos\theta_{\mu}} &= \Gamma_0 \beta_{\mu} \sqrt{\lambda(q^2)} \left[ a(q^2) + b(q^2)\cos\theta_{\mu} + c(q^2)\cos^2\theta_{\mu} \right] \\ a(q^2) &= q^2 \left( \beta_{\mu}^2 \left| F_S(q^2) \right|^2 + \left| F_P(q^2) \right|^2 \right) + \frac{\lambda(q^2)}{4} \left( \left| F_A(q^2) \right|^2 + \left| F_V(q^2) \right|^2 \right) \\ &+ 4m_{\mu}^2 m_{K^+}^2 \left| F_A(q^2) \right|^2 + 2m_{\mu} \left( m_{K^+}^2 - m_{\pi^+}^2 + q^2 \right) \operatorname{Re} \left[ F_P(q^2) F_A(q^2)^* \right], \\ b(q^2) &= 2m_{\mu} \beta_{\mu} \sqrt{\lambda(q^2)} \operatorname{Re} \left[ F_S(q^2) F_V(q^2)^* \right], \end{aligned}$$

$$c(q^2) = -\frac{\beta_{\mu}^2 \lambda(q^2)}{4} \left( \left| F_A(q^2) \right|^2 + \left| F_V(q^2) \right|^2 \right),$$

### **Decay modes 4&5:** $K_L \rightarrow \mu^+ \mu^-$ and $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ (II)

$$F_{V}(q^{2}) = \left(C_{9} + C_{9}'\right)f_{+}(q^{2}) + \frac{2m_{s}}{m_{K^{+}} + m_{\pi^{+}}}f_{T}(q^{2})C_{7} + F_{V\gamma}(q^{2}),$$

$$F_{A}(q^{2}) = \left(C_{10} + C_{10}'\right)f_{+}(q^{2}),$$

$$F_{S}(q^{2}) = \frac{m_{K^{+}}^{2} - m_{\pi^{+}}^{2}}{2(m_{s} - m_{d})}f_{0}(q^{2})\left(C_{S} + C_{S}'\right),$$

$$F_{P}(q^{2}) = \frac{m_{K^{+}}^{2} - m_{\pi^{+}}^{2}}{2(m_{s} - m_{d})}f_{0}(q^{2})\left(C_{P} + C_{P}'\right) - m_{\mu}\left(C_{10} + C_{10}'\right)\left[f_{+}(q^{2}) - \frac{m_{K^{+}}^{2} - m_{\pi^{+}}^{2}}{q^{2}}\left(f_{0}(q^{2}) - f_{+}(q^{2})\right)\right]$$
where  $\Gamma_{0} = \frac{G_{F}^{2}\alpha^{2}|\lambda|^{2}}{512\pi^{3}m_{K^{+}}^{3}}, \beta_{\mu} = \sqrt{1 - \frac{4m_{\mu}^{2}}{q^{2}}} \text{ and } \lambda(q^{2}) = q^{4} + m_{K^{+}}^{4} + m_{\pi^{+}}^{4} - 2(m_{K^{+}}^{2}m_{\pi^{+}}^{2} + m_{\pi^{+}}^{2}q^{2} + m_{\pi^{+}}^{2}q^{2})$ 
Long-distance contribution  $F_{V\gamma}(q^{2}) = -\left[\left(\alpha_{+} + \beta_{+}\frac{q^{2}}{m_{K^{+}}^{2}}\right) + \frac{1}{m_{K^{+}}^{2}G_{F}}W_{+}^{\pi\pi}(q^{2})\right]\frac{\sqrt{2}}{2\pi\lambda_{t}^{\pi}}, \text{ JHEP 08, 004 (1998)}$ 

#### The branching ratio and forward-backward asymmetry are defined as

$$BR = 2\Gamma_0 \int_{q_{\min}^2}^{q_{\max}^2} \beta_\mu \sqrt{\lambda(q^2)} \left( a(q^2) + \frac{1}{3}c(q^3) \right),$$
$$A_{FB} = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \beta_\mu \sqrt{\lambda(q^2)} b(q^2)}{2 \int_{q_{\min}^2}^{q_{\max}^2} \beta_\mu \sqrt{\lambda(q^2)} \left( a(q^2) + \frac{1}{3}c(q^3) \right)},$$

#### Helicity basis allows for an explicit separation of long and short range contributions μ $\frac{d\Gamma}{dq^2 d\cos\theta_\ell} = \mathcal{N}(q^2) \left[ I_1(q^2) + I_2(q^2)\cos\theta_\ell + I_3(q^2)\cos^2\theta_\ell \right]$ θ, Σ+ $I_{1}(q^{2}) = \left(|H_{\frac{1}{2},t}^{A}|^{2} + |H_{-\frac{1}{2},t}^{A}|^{2}\right) \cdot 8m_{\ell}^{2} + \left(|H_{\frac{1}{2},t}^{S}|^{2} + |H_{-\frac{1}{2},t}^{S}|^{2}\right) \cdot \left(2q^{2} - 5m_{\ell}^{2}\right)$ $+\left(|H_{\frac{1}{2}t}^{P}|^{2}+|H_{-\frac{1}{2}t}^{P}|^{2}\right)\cdot\left(2q^{2}-3m_{\ell}^{2}\right)-8m_{\ell}\sqrt{q^{2}}\cdot\operatorname{Re}\left[H_{\frac{1}{2}t}^{A*}H_{\frac{1}{2}t}^{P}+H_{-\frac{1}{2}t}^{A*}H_{-\frac{1}{2}t}^{P}\right]$ $+ \left( |H_{\frac{1}{2}0}^{V}|^{2} + |H_{-\frac{1}{2}0}^{V}|^{2} \right) \cdot \left( 8m_{\ell}^{2} + 2q^{2}\beta^{2} \right) + \left( |H_{\frac{1}{2}0}^{A}|^{2} + |H_{-\frac{1}{2}0}^{A}|^{2} \right) \cdot 2q^{2}\beta^{2}$ $+\left(|H_{\frac{1}{2},+}^{V}|^{2}+|H_{-\frac{1}{2},-}^{V}|^{2}\right)\cdot\left(8m_{\ell}^{2}+q^{2}\beta^{2}\right)+\left(|H_{\frac{1}{2},+}^{A}|^{2}+|H_{-\frac{1}{2},-}^{A}|^{2}\right)\cdot q^{2}\beta^{2},$ Short-distance $I_{2}(q^{2}) = -8m_{\ell}\sqrt{q^{2}\beta} \cdot \operatorname{Re}\left[H_{\frac{1}{2},t}^{S}H_{\frac{1}{2},0}^{V*} + H_{-\frac{1}{2},t}^{S}H_{-\frac{1}{2},0}^{V*}\right] - 4q^{2}\beta \cdot \operatorname{Re}\left[H_{\frac{1}{2},t}^{A}H_{\frac{1}{2},t}^{V*} - H_{-\frac{1}{2},-}^{A}H_{-\frac{1}{2},-}^{V*}\right]$ $I_{3}(q^{2}) = \left(|H_{\frac{1}{2}0}^{V}|^{2} + |H_{-\frac{1}{2}0}^{V}|^{2} + |H_{\frac{1}{2}0}^{A}|^{2} + |H_{-\frac{1}{2}0}^{A}|^{2}\right) \cdot \left(-2q^{2}\beta^{2}\right)$ *H<sup>V</sup>* includes long-distance contributions, and $H^{A,S,P}$ only + $\left(|H_{\frac{1}{2}+}^{V}|^{2} + |H_{-\frac{1}{2}-}^{V}|^{2} + |H_{\frac{1}{2}+}^{A}|^{2} + |H_{-\frac{1}{2}-}^{A}|^{2}\right) \cdot q^{2}\beta^{2},$ contain short-distance contributions $H_{\frac{1}{2},0}^{V} = -\frac{iC_{7}m_{s} \left[\sqrt{Q_{-}} \left(g_{T}(q^{2}) - g_{T}^{(1)}(q^{2})\frac{M_{1}+M_{2}}{M_{1}} - g_{T}^{(2)}(q^{2})\frac{Q_{+}}{M_{1}^{2}}\right) + \sqrt{Q_{+}} \left(g_{T5}(q^{2}) + g_{T5}^{(1)}(q^{2})\frac{M_{1}-M_{2}}{M_{1}} - g_{T}^{(2)}(q^{2})\frac{Q_{-}}{M_{1}^{2}}\right)\right]}{2\pi\sqrt{q^{2}}}$ $+\frac{\sqrt{Q_{-}}\left(C_{9}+C_{9}'\right)\left[f_{1}(q^{2})(M_{1}+M_{2})+f_{2}(q^{2})\frac{q^{2}}{M_{1}}\right]}{\sqrt{q^{2}}}+\frac{\sqrt{Q_{+}}\left(C_{9}-C_{9}'\right)\left[g_{1}(q^{2})(M_{1}-M_{2})-g_{2}(q^{2})\frac{q^{2}}{M_{1}}\right]}{\sqrt{q^{2}}}$ $+ \frac{4\sqrt{2}\pi[-a\sqrt{Q_{-}} - b\sqrt{Q_{+}} - c\sqrt{Q_{-}}(M_{1} + M_{2}) + d\sqrt{Q_{+}}(M_{1} - M_{2})]}{-}.$ Long-distance

### Decay mode 6: of $\Sigma^+ \rightarrow p \mu^+ \mu^-$ (l)

### Decay mode 6: $\Sigma^+ \rightarrow p \mu^+ \mu^-$ (II)

#### Decay width expanded in $\delta$ reads

$$\frac{d\Gamma}{d\cos\theta_{\ell}} = \mathcal{N}\left[I_1 + I_2\cos\theta_{\ell} + I_3\cos^2\theta_{\ell}\right]$$

$$I_{2} = (C_{S} + C_{S}^{*}) \operatorname{Re} \left[ (-0.08i) \frac{f_{S}(0)g_{T}(0)}{f_{1}(0)f_{1}(0)} \delta \cdot C_{7}^{*} - 0.26 \left\{ 1 - \frac{3}{2} \delta \right\} \frac{f_{S}(0)}{f_{1}(0)} \left( C_{9} + C_{9}^{*} \right)^{*}}{+ \left( \frac{2.32}{\Delta f_{1}(0)} \right) \frac{f_{S}(0)}{f_{1}(0)} \left( \frac{a}{a}_{i} \right)^{*} + \left( \frac{4.64}{f_{1}(0)} \right) \left( 1 - \frac{3}{2} \delta \right) \frac{f_{S}(0)}{f_{1}(0)} \left( \frac{a}{a}_{i} \right)^{*}}{f_{1}(0)f_{1}(0)} \delta \cdot C_{7}^{*} - 0.13\delta \frac{g_{F}(0)}{f_{1}(0)} \left( C_{9} - C_{9}^{*} \right)^{*}} + \left( \frac{2.32}{\Delta f_{1}(0)} \delta \right) \frac{g_{F}(0)g_{T5}(0)}{f_{1}(0)f_{1}(0)} \delta \cdot C_{7}^{*} - 0.13\delta \frac{g_{F}(0)}{f_{1}(0)} \left( C_{9} - C_{9}^{*} \right)^{*}}{+ \left( \frac{2.32}{\Delta f_{1}(0)} \delta \right) \frac{g_{F}(0)g_{T5}(0)}{f_{1}(0)} \left( \frac{b}{a}_{i} \right)^{*} - \left( \frac{2.32}{f_{1}(0)} \delta \right) \frac{g_{F}(0)}{f_{1}(0)} \left( \frac{d}{a}_{i} \right)^{*}} \right] + \left( C_{10} - C_{10}^{*} \right) \frac{g_{F}(0)g_{T5}(0)}{f_{1}(0)} \left( \frac{d}{a}_{i} \right)^{*} \right] + \left( C_{10} - C_{10}^{*} \right) \frac{g_{F}(0)g_{T5}(0)}{f_{1}(0)} \left( \frac{d}{a}_{i} \right)^{*}} \right) + \left( C_{10} - C_{10}^{*} \right) \frac{g_{F}(0)g_{T}(0)}{f_{1}(0)} \left( \frac{d}{a}_{i} \right)^{*} + \left( -0.23\delta \frac{f_{2}(0)g_{T5}(0)}{f_{1}(0)} \left( \frac{d}{a}_{i} \right)^{*} \right) + \left( -0.23\delta \frac{f_{2}(0)g_{T5}(0)}{f_{1}(0)} \left( \frac{d}{a}_{i} \right)^{*}} \right) + \left( -0.23\delta \frac{f_{2}(0)g_{T5}(0)}{f_{1}(0)f_{1}(0)} \delta \cdot C_{7}^{*} - 0.26\delta \frac{g_{1}(0)}{f_{1}(0)} \left( C_{9} - C_{9}^{*} \right)^{*}} + \left( \frac{g_{10}}{2.2167} \right) \left| \frac{d}{a}_{i}\right|^{2} + \left( \frac{g_{10}}{2.2167} \right) \left| \frac{d}{a}_{i}\right|^{2} + \left( \frac{g_{10}}{f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} - \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} - \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} \right) \left| \frac{d}{a}_{i}\right|^{2} - \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} \right|^{2} + \left( \frac{g_{10}}{2.2167} \right) \left| \frac{d}{a}_{i}\right|^{2} - \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} - \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} \right|^{2} \right|^{2} + \left( \frac{g_{10}}{2.2167} \right) \left| \frac{d}{a}_{i}\right|^{2} + \left( \frac{g_{10}}{2.2167} \right) \left| \frac{d}{a}_{i}\right|^{2} - \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} \right|^{2} \right|^{2} + \left( \frac{g_{10}}{2.4f_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} \right|^{2} + \left( \frac{g_{10}}{2.4g_{1}(0)^{2}} \right) \left| \frac{d}{a}_{i}\right|^{2} \right$$

BR = 
$$2\tau_{B_1}\mathcal{N}(I_1 + \frac{1}{3}I_3),$$
  
 $A_{FB} = \frac{I_2}{I_1 + \frac{1}{3}I_3}.$ 

 $f_2(0)$  is relevant for  $A_{FB}$ .

# Contents

- □ Background & purpose
  - >  $s \rightarrow dv\overline{v}$  &  $s \rightarrow d\ell^+\ell^-$
  - > Kaons vs. hyperons
- Theoretical framework
- Results and Discussions
- Summary and outlook



 $\Box \ \delta C_{vl}^{L} + C_{vl}^{R} \text{ is constrained more stringently by the kaon modes}$  $\Box B_{1} \rightarrow B_{2} \mathcal{V} \overline{\mathcal{V}} \text{ are better than their kaon siblings to constrain } \delta C_{vl}^{L} - C_{vl}^{R}$ 

#### Comparison of the SM predictions for $B_1 \rightarrow B_2 \mathcal{V} \overline{\mathcal{V}}$



[19] Jusak Tandean, JHEP 04, 104 (2019) [53] Xiao-Hui Hu et al., Chin. Phys. C 43, 093104 (2019)

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 $s \rightarrow d\mu^+\mu^-$ 

 $a (\text{GeV}^2) \times 10^{-3} b (\text{GeV}^2) \times 10^{-3} \text{ BR} \times 10^8 A_{FB} \times 10^5 \text{ BR} \times 10^8 [19, 20] A_{FB} \times 10^5 [19, 20]$ 

Case 1 13.	3 + 2.84i - 6.0 -	- 1.83 <i>i</i> 1.7	-1,7(2)	1.6	3.7
Case 2 -13	.3 + 2.84i $6.0 -$	1.83 <i>i</i> 3.5	0.3(1)	3.5	-1.4
Case 3 6.0	) + 2.84i - 13.3	- 1.83 <i>i</i> 5.5	0.4(0)	5.1	0.9
Case 4 -6.	0 + 2.84 <i>i</i> 13.3 -	-1.83 <i>i</i> 9.3	-0.4(0)	9.1	-0.3
			$\sqrt{10}$		
	$BR(K_L \to \mu^+ \mu^-)$	$ A_{FB} (K$	$\pi^+ \rightarrow \pi^+ \mu^+ \mu^-)$	$ A_{FB} (\Sigma^{+}$	$\rightarrow p\mu^+\mu^-)$
SM	$(7.64 \pm 1.22) 10^{-9}$		0	(-1.7~	0.4) 10 <sup>-5</sup>
Expt.	$(6.84 \pm 0.11) \cdot 10^{-9}$	< 2.3 10	) <sup>-2</sup> (90% C.L.)	< 2.3 10-	<sup>2</sup> (90% C.L.)
$C_S + C'_S$	×	(-3	.05, 3.05)	(-5.3,	$(5.3) \times 10^3$
$C_S - C'_S$	(-0.12, 0.12)		×	(-1.7,	$1.7) \times 10^3$
$\delta C_{10} + C_{10}'$	X		×	(-2.2, 2	$(2.2) \times 10^3$
$\delta C_{10} - C'_{10}$	(-2.35, 0.59)		×	(-1.4,	$1.4) \times 10^{3}$
10					· Olv

**The contribution of the form factor**  $f_2(0)$  can be relevant for AFB.

 $\Sigma^+ 
ightarrow p \mu^+ \mu^-$ 

Current kaon bounds except for the  $\delta C_{10} + C'_{10}$  scenario are a few orders of magnitude better than those of  $\Sigma^+ \rightarrow p\mu^+\mu^-$  if measured up to the same precision.

[19] X.G. He et al., PRD72, 074003 (2005) [20] X.G. He et al., JHEP 10, 040 (2018)

# Summary

□ For the  $s \to dv \overline{v}$  transitions,  $\delta C_{vl}^L + C_{vl}^R$  can be determined well by the kaon modes but the  $B_1 \to B_2 v \overline{v}$  modes are better than their kaon counterparts for the constraint on  $\delta C_{vl}^L - C_{vl}^R$ .

□ For the  $s \rightarrow d\mu^+\mu^-$  transitions, current kaon bounds are a few orders of magnitude better than those of  $\Sigma^+ \rightarrow p\mu^+\mu^-$  if they are measured up to the same precision, except for the  $\delta C_{10} + C'_{10}$ scenario. In addition, the contribution of the form factor  $f_2(0)$ is relevant for A<sub>FB</sub>.

# Outlook

- □ For the  $s \to dv \overline{\nu}$  transitions, measurements of  $B_1 \to B_2 \overline{\nu} \overline{\nu}$  decays can help better constrain the axial-vectorial coupling  $\delta C_{vl}^L - C_{vl}^R$ .
- □ For the  $\Sigma^+ \rightarrow p\mu^+\mu^-$  decay, a measurement of leptonic forwardbackward asymmetry  $A_{FB}$  can help constrain  $\delta C_{10} + C'_{10}$ .







# Thanks for your attention !

### Xiao-Gang He, Jusak Tandean, G. Valencia, PRD72, 074003 (2005)

TABLE I. Branching ratios of  $\Sigma^+ \rightarrow p\mu^+\mu^-$ ,  $pe^+e^-$  in the standard model. The unbracketed branching ratios receive contributions from all the form factors, with the expressions in Eq. (B2) [Eq. (B8)] for the imaginary parts contributing to the numbers in the first (last) four rows. Within each pair of square brackets, the first number has been obtained with c = d = 0, and the second with only the real parts of all the form factors.

Rea (MeV)	Reb (MeV)	$10^8 \mathcal{B}(\Sigma^+ \to p \mu^+ \mu^-)$	$10^6 \mathcal{B}(\Sigma^+ \rightarrow p e^+ e^-)$
13.3	-6.0	1.6 [2.2, 1.3]	9.1 [9.2, 8.6]
-13.3	6.0	3.4 [2.2, 3.1]	9.4 [9.2, 8.8]
6.0	-13.3	5.1 [6.7, 4.7]	9.6 [9.8, 9.0]
-6.0	13.3	9.0 [6.7, 8.6]	10.1 [9.8, 9.5]
11.1	-7.3	2.3 [2.9, 1.5]	9.3 [9.3, 7.2]
-11.1	7.3	4.5 [2.9, 3.7]	9.6 [9.3, 7.5]
7.3	-11.1	4.0 [5.1, 3.2]	9.5 [9.6, 7.4]
-7.3	11.1	7.3 [5.1, 6.4]	10.0 [9.6, 7.8]



# **Bright future ahead**

Channel	$\mathcal{R}$	$\epsilon_L$	$\epsilon_D$	$\sigma_L(\text{MeV}/c^2)$	$\sigma_D(\text{MeV}/c^2)$
$K_{\rm s}^0  o \mu^+ \mu^-$	1	1.0(1.0)	1.8 (1.8)	$\sim 3.0$	$\sim 8.0$
$K_{\rm s}^0 \to \pi^+\pi^-$	1	$1.1 \ (0.30)$	1.9(0.91)	$\sim 2.5$	$\sim 7.0$
$K_{\rm S}^0  ightarrow \pi^0 \mu^+ \mu^-$	1	$0.93\ (0.93)$	1.5(1.5)	$\sim 35$	$\sim 45$
$K_{\rm s}^0 \to \gamma \mu^+ \mu^-$	1	$0.85 \ (0.85)$	1.4(1.4)	$\sim 60$	$\sim 60$
$K^0_{\rm s} \to \mu^+ \mu^- \mu^+ \mu^-$	1	$0.37\ (0.37)$	1.1(1.1)	$\sim 1.0$	$\sim 6.0$
$K_{\rm L}^0 \to \mu^+ \mu^-$	$\sim 1$	$2.7~(2.7)~{ imes}10^{-3}$	$0.014 \ (0.014)$	$\sim 3.0$	$\sim 7.0$
$K^+ \to \pi^+ \pi^+ \pi^-$	$\sim 2$	9.0 (0.75) $\times 10^{-3}$	$41~(8.6)~\times 10^{-3}$	$\sim 1.0$	$\sim 4.0$
$K^+ \to \pi^+ \mu^+ \mu^-$	$\sim 2$	$6.3~(2.3)~{ imes}10^{-3}$	$0.030\ (0.014)$	$\sim 1.5$	$\sim 4.5$
$\Sigma^+ \to p \mu^+ \mu^-$	$\sim 0.13$	0.28(0.28)	0.64(0.64)	$\sim 1.0$	$\sim 3.0$
$\Lambda \to p\pi^-$	$\sim 0.45$	$0.41 \ (0.075)$	$1.3 \ (0.39)$	$\sim 1.5$	$\sim 5.0$
$\Lambda  o p \mu^- ar{ u_\mu}$	$\sim 0.45$	$0.32\ (0.31)$	$0.88 \ (0.86)$		
$\Xi^- \to \Lambda \mu^- \bar{\nu_{\mu}}$	$\sim 0.04$	$39~(5.7)~{ imes}10^{-3}$	0.27~(0.09)	—	—
$\Xi^- \to \Sigma^0 \mu^- \bar{\nu_{\mu}}$	$\sim 0.03$	$24~(4.9)~\times 10^{-3}$	$0.21 \ (0.068)$	—	—
$\Xi^- \rightarrow p \pi^- \pi^-$	$\sim 0.03$	0.41(0.05)	0.94~(0.20)	$\sim 3.0$	$\sim 9.0$
$\Xi^0 \to p\pi^-$	$\sim 0.03$	1.0(0.48)	2.0(1.3)	$\sim 5.0$	$\sim 10$
$\Omega^- \to \Lambda \pi^-$	$\sim 0.001$	95 (6.7) $\times 10^{-3}$	0.32(0.10)	$\sim 7.0$	$\sim 20$



**Table 1.** Acceptance scale factors  $\epsilon$ , and mass resolutions  $\sigma$ , for only long (L) and only downstream (D) tracks obtained from our simplified description of the LHCb Upgrade tracking system geometry. The production ratio of the strange hadron with respect to  $K_S^0$  is shown as  $\mathcal{R}$ . All efficiencies are normalised to that of fully reconstructed  $K_S^0 \to \mu^+ \mu^-$  and averaged over particles and anti-particles. Channels containing a photon, neutrino and  $\pi^0$  are partially reconstructed.



 $\pi^+$ 

 $10^{2}$ 



### Bright future ahead Super Tau-Charm/CEPC

Decay mode	Current data $\mathcal{B}(\times 10^{-6})$	Sensitivity $\mathcal{B}$ (90% C.L.) (×10 <sup>-6</sup> )	Type
$\Lambda \to n e^+ e^-$	_	< 0.8	
$\Sigma^+  ightarrow pe^+e^-$	< 7	< 0.4	
$\Xi^0 \to \Lambda e^+ e^-$	$7.6\pm0.6$	< 1.2	
$\Xi^0 \to \varSigma^0 e^+ e^-$	_	< 1.3	<b>T</b>
$\Xi^- \to \varSigma^- e^+ e^-$	_	< 1.0	Type A
$\Omega^-\to \Xi^- e^+ e^-$	_	< 26.0	
$\Sigma^+ \to p \mu^+ \mu^-$	$(0.09\substack{+0.09\\-0.08})$	< 0.4	
$\Omega^-\to \Xi^-\mu^+\mu^-$	_	< 30.0	
$\Lambda \to n \nu \bar{\nu}$	_	< 0.3	
$\Sigma^+ \to p \nu \bar{\nu}$	_	< 0.4	
$\Xi^0 \to A \nu \bar{\nu}$	_	< 0.8	
$\Xi^0 \to \Sigma^0 \nu \bar{\nu}$	_	< 0.9	Type B
$\Xi^- \to \Sigma^- \nu \bar{\nu}$	_	_*	
$\Omega^-\to \Xi^-\nu\bar\nu$	_	< 26.0	

Rare and forbidden hyperon decays and expected sensitivities with  $10^{10}$  events on the J/ $\psi$  peak and 3 ×  $10^{9}$  events on the  $\psi$ (2S) peak.