

# crystal ECAL granularity optimization and performance studies

LIU Chunxiu, LIU Yong, LV Janguang

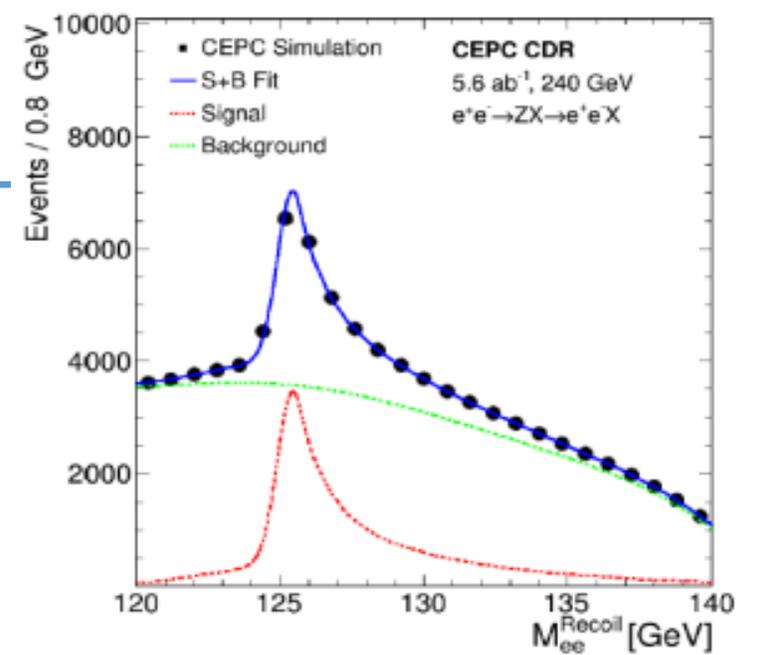
May 06, 2020

CEPC Physics&Detector meeting



# Overview: motivations

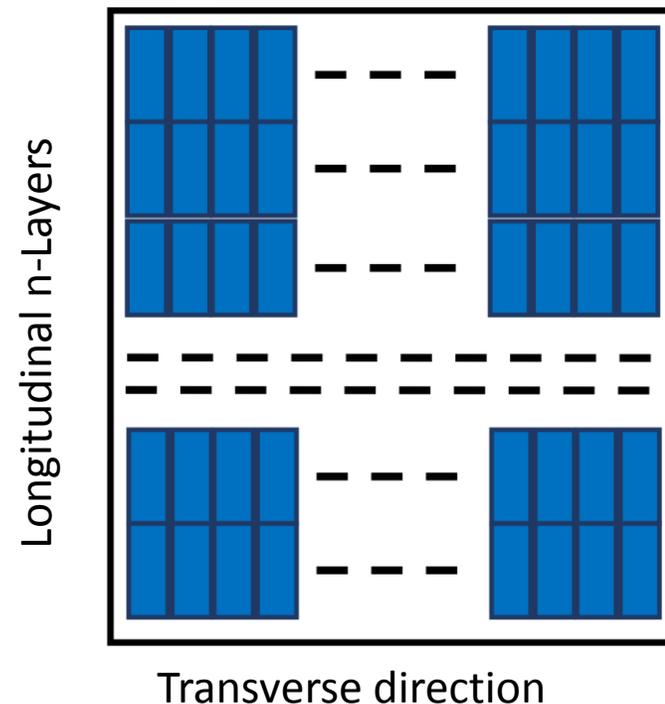
- Background: future lepton colliders (e.g. CEPC)
  - Precision measurements with Higgs and Z/W
- Why crystal calorimeter?
  - Homogeneous structure
    - Optimal intrinsic energy resolution:  $\sim 3\% / \sqrt{E} \oplus \sim 1\%$
  - High precision of electron energy : to improve Higgs recoil mass
    - Corrections to the Bremsstrahlung of electrons
  - Capability to trigger single photons
    - Flavour physics at Z-pole, potentials in search of new physics, ...
- Fine segmentation
  - Potential in PFA for precision measurements of jets





# New idea : High-granularity Crystal ECAL

- Homogeneous crystal structure:
  - Cell size:  $\sim$  moliere radius in transverse direction
  - N layers in longitudinal direction
- Key issues: optimization
  - Crystal options: BGO, PWO, etc.
  - Segmentation: in longitudinal and lateral directions
  - Performance: single particles and jets with PFA
  - Impacts from dead materials: upstream, services (cabling, cooling)
  - Costing
  - Fine timing information





# Study of the single particle performance

---

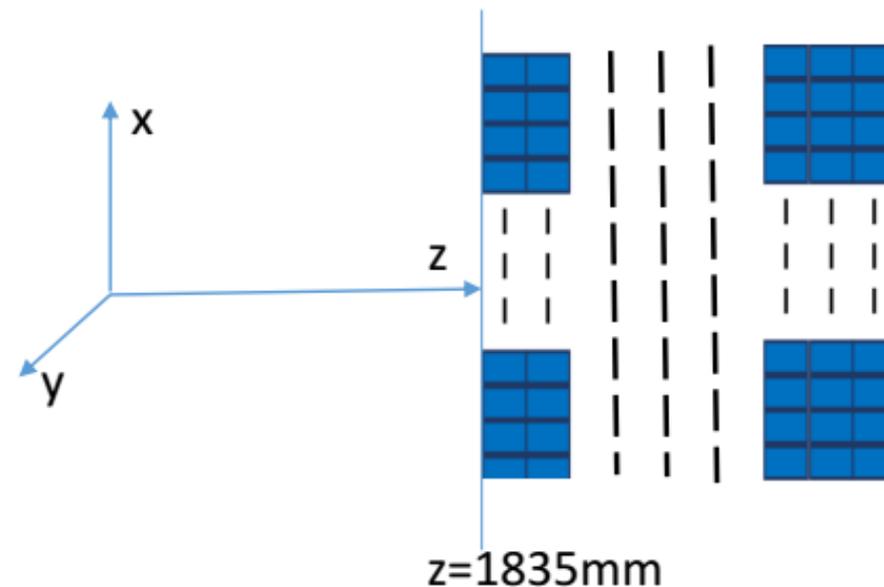
- Optimize the crystal granularity to realize the following performance
  - Whether the energy leakage can be corrected by the longitudinal profile of the cluster? (preliminary results presented)
  - Separation performance of 2  $\gamma$ 's from high energy  $\pi^0$  decay (preliminary results presented)
  - Separation performance of  $\gamma$  and merged  $\pi^0$  (preliminary results presented)
  - How to reconstruct the merged  $\pi^0$  (in processing)
  - Separate  $\gamma$  and  $K_L$  by time and profile of the cluster
- How to arrange the crystals
  - Cell size?
  - How many layers?
  - depth of each layer?



# Geometry construction in GEANT4 v10.5.0

## MC simulation of a simplified crystal calorimeter module for CEPC

- Construct the Matrix module in GEANT4 v10.5.0
  - Cell size:  $10 \times 10 \times 10 \text{mm}^3$ 
    - ✓ Easy to merge cells / layers
  - Construct a 3D BGO array with  $60 \times 60 \times 60$  cells
  - The front face of the array is  $1835 \text{mm}$  from zero (origin of coordinates), the inner radius of baseline ECAL Barrel.
  - Cell Size  $10 \text{mm}$  is  $\sim 0.31224^\circ$  solid angle at  $\theta = 90^\circ$  in Barrel
- Without any photodetector materials and wrappers
- Geant4 simulates the energy deposited in crystal cell.



BGO crystal material properties:  
Crystal radiation length:  $\sim 1.12 \text{cm}$ ;  
Moliere radius  $R_M$ :  $2.23 \text{cm}$ ;



# Generate the MC single $\gamma$ and $\pi^0$ samples

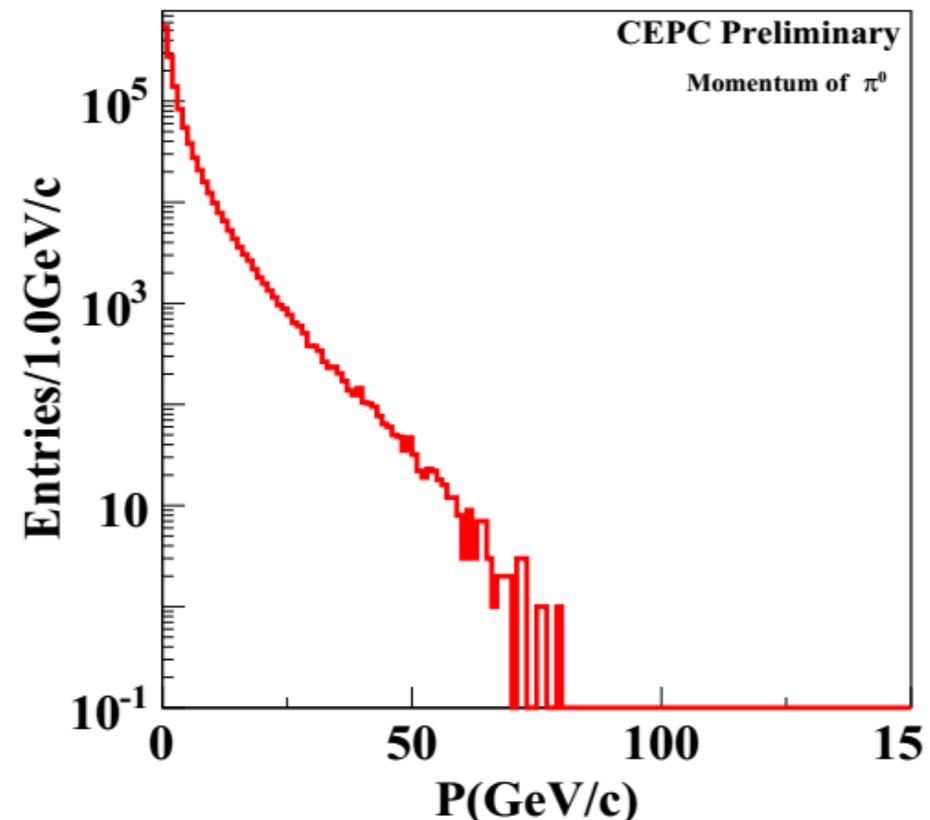
- Generate the MC single particles samples in the following:

- Gamma: 98GeV, 100GeV, 102GeV

- $\pi^0$ : 30GeV, 40GeV

- Momentum Direction:

It goes from the origin to the center of the crystal.





# The cluster reconstruction

---

- Cluster Reconstruction of each layer
  - According to the clusterisation procedure each local maximum originates the cluster. The local maximum cell with the energy deposition in excess of the energy deposition in each of its neighbouring cells.
  - To require the energy of local maximum to be in excess of 10MeV
  - The energy threshold of cell is 1MeV
- Cluster reconstruction after merging layers
- Reconstruction codes have been completed in root analysis( without any frame).

Study of the correction of the longitudinal  
shower energy leakage  
for high energy  $\gamma$  (e.g. 100GeV)



# The correction of the Longitudinal shower energy leakage

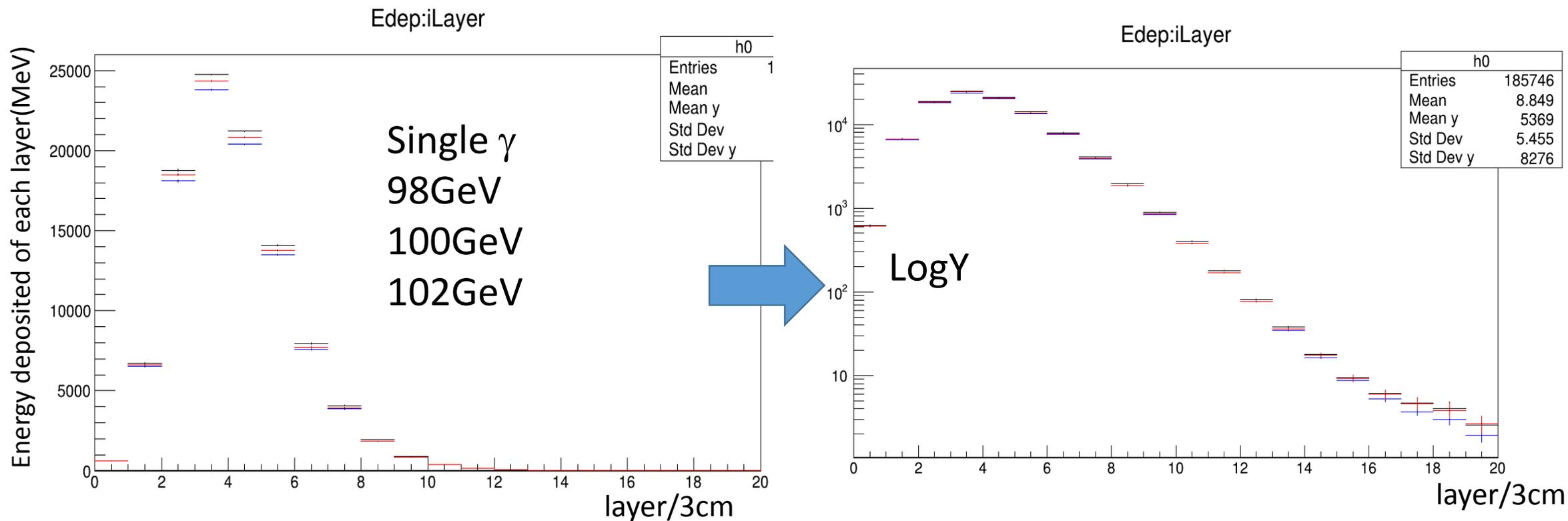
---

- Generate 98GeV, 100GeV, 102GeV single  $\gamma$
- The study based on the following ECAL detector.
  - Merge 3 layers into one layer, i.e., each layer/3cm depth
  - Consider the detector with the different length in the longitudinal direction
    - ✓ With 30cm ( $\sim 26.8X_0$ ) length BGO (a total of 10 layers)
    - ✓ With 27cm ( $\sim 24.1X_0$ ) length BGO (a total of 9 layers)
    - ✓ With 24cm ( $\sim 21.4X_0$ ) length BGO (a total of 8 layers)
- Study the correction of the Longitudinal shower energy leakage according to the longitudinal shower profile



# the Longitudinal shower profile

Energy deposited (MeV) versus iLayer with each layer(3cm)



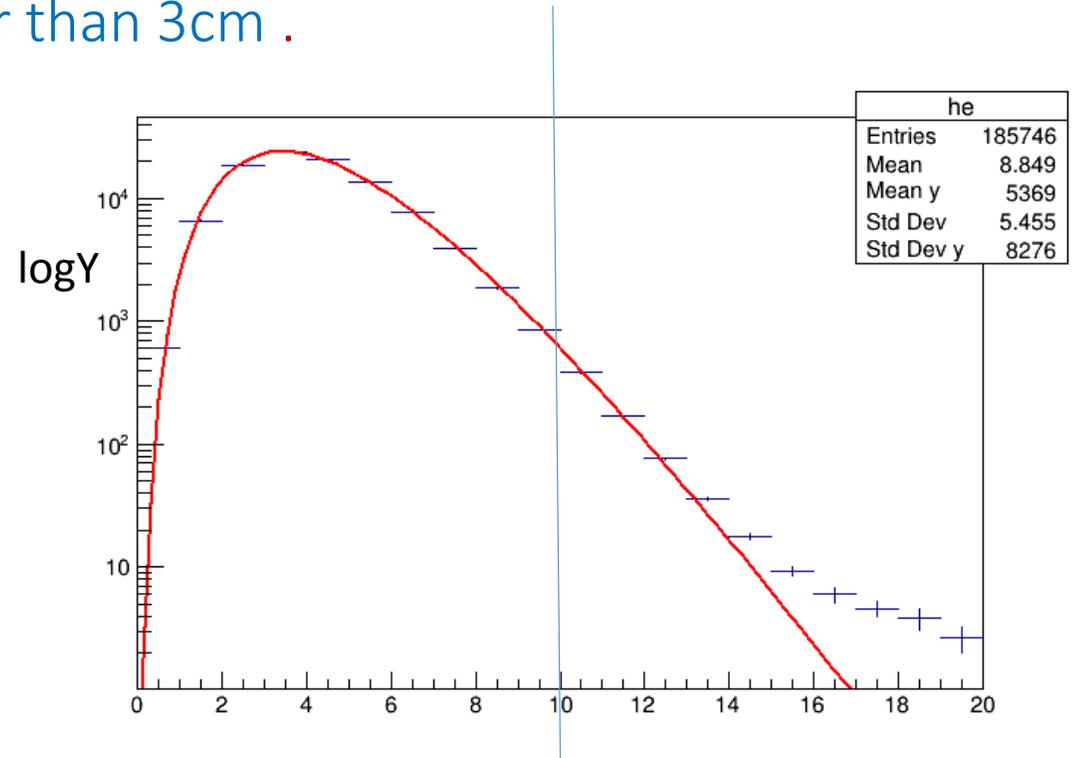
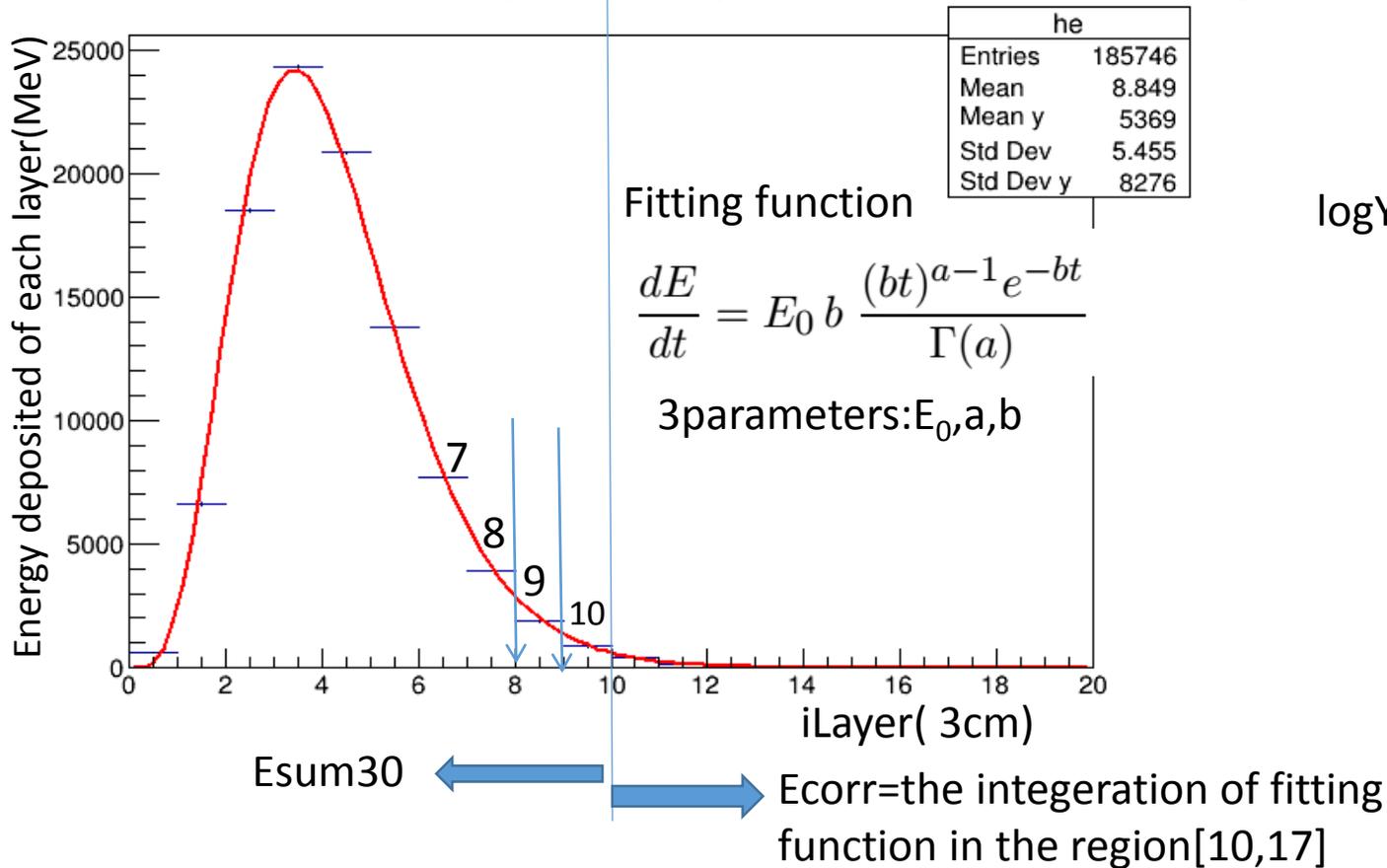
The shower maximum happens in around 10 to 12cm depth in longitudinal direction.



# The method of the correction of longitudinal leakage

The fewer the data points, the greater the correction error.

The correction needs at least 7-8 data points ,  
and the depth of layer should not be larger than 3cm .



The fit function needs to be improved

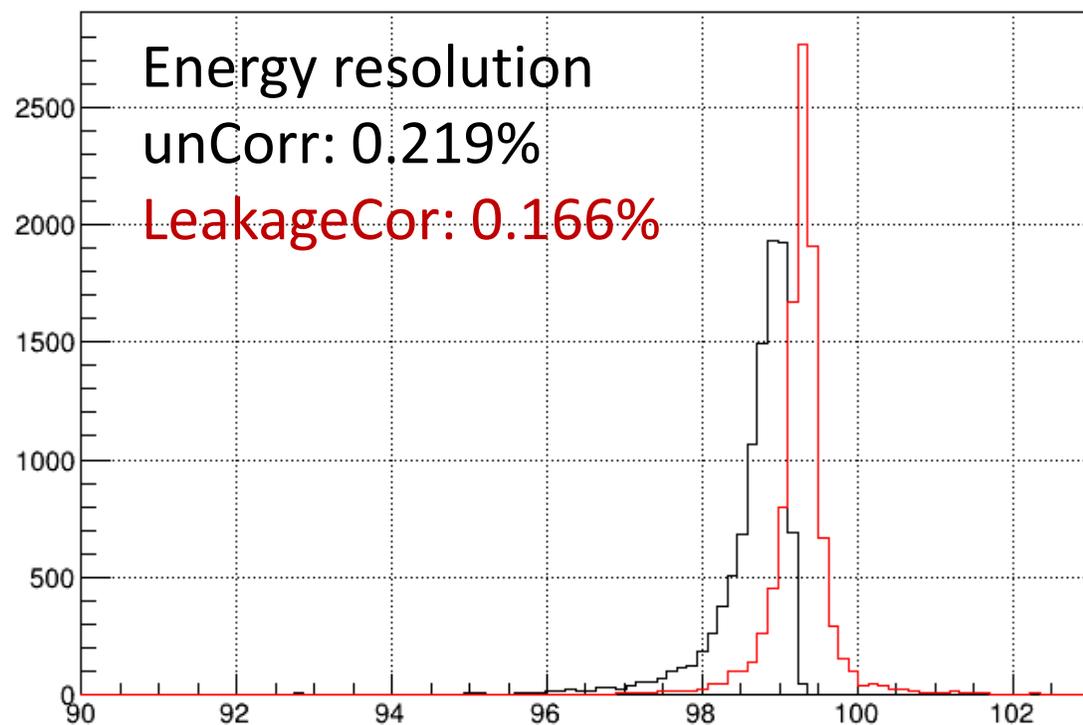


# Energy measurement of 100GeV $\gamma$ with 30cm depth crystal

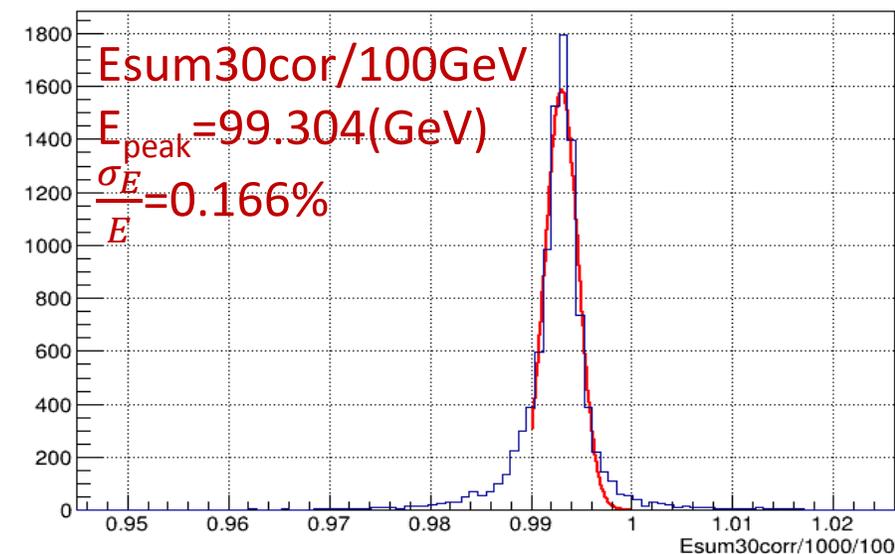
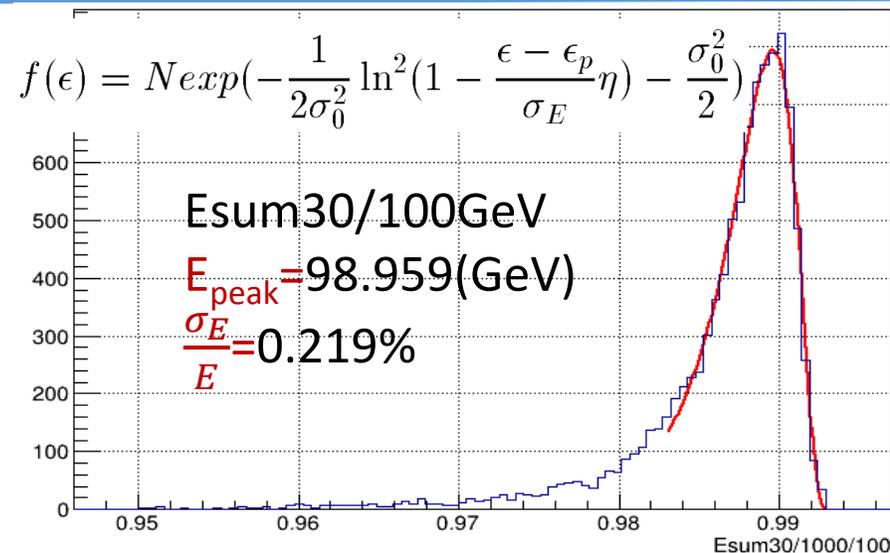
30cm( $\sim 26.8X_0$ ) length BGO

10 layers/3cm

Cell size 1x1cm<sup>2</sup>



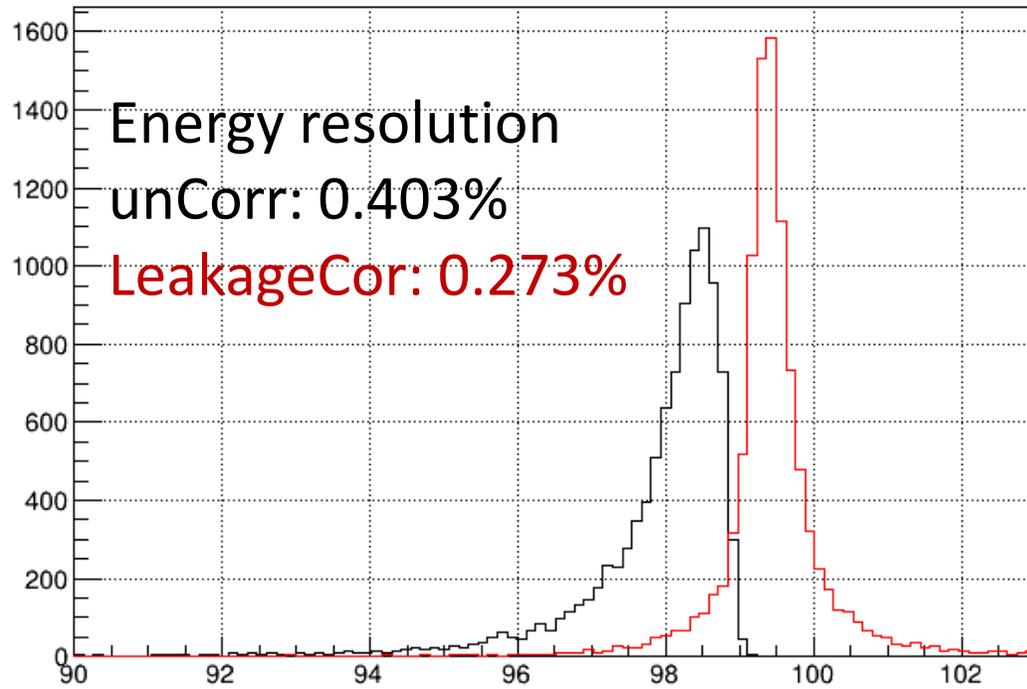
The energy resolution is optimized around 24%



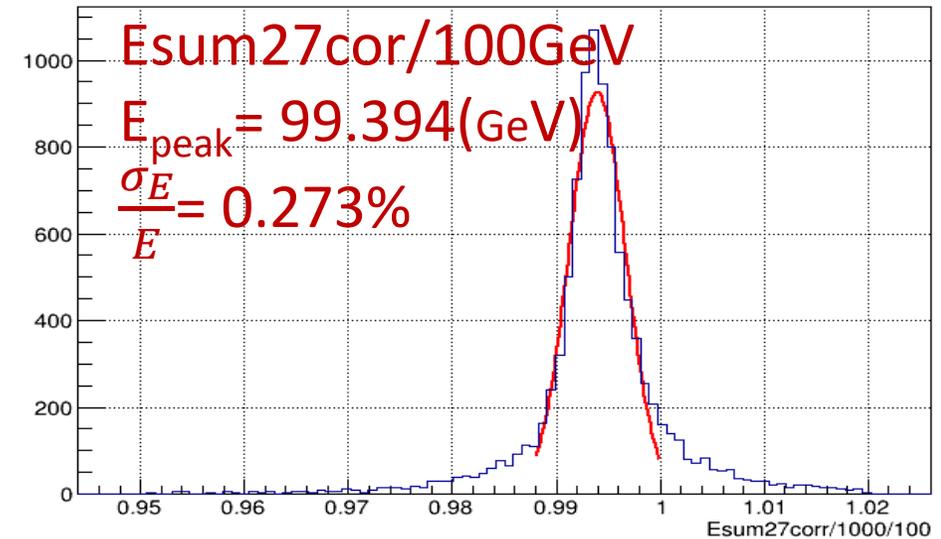
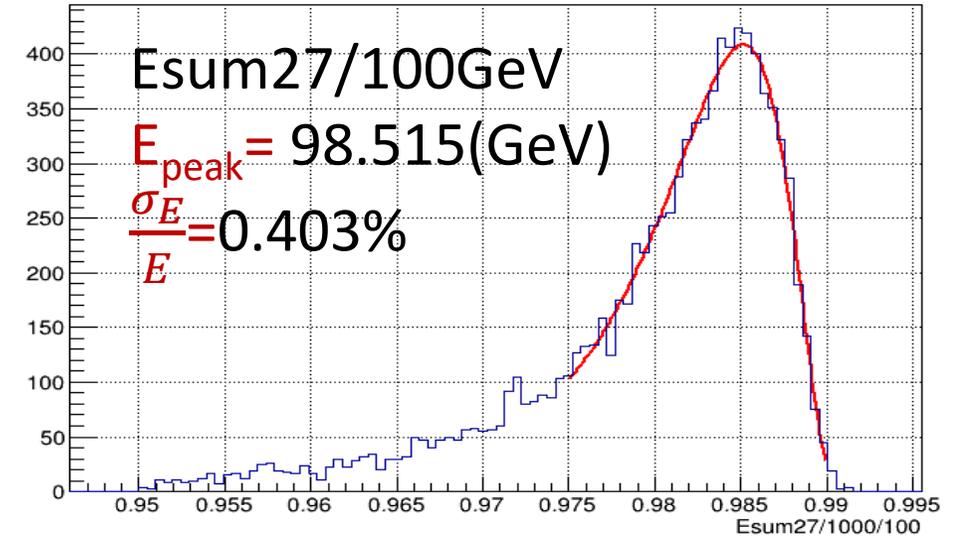


# Energy measurement of 100GeV $\gamma$ with 27cm depth crystal

27cm( $\sim 24.1X_0$ ) length BGO  
9 layers/3cm  
Cell size 1x1cm<sup>2</sup>



The energy resolution is optimized around 32%



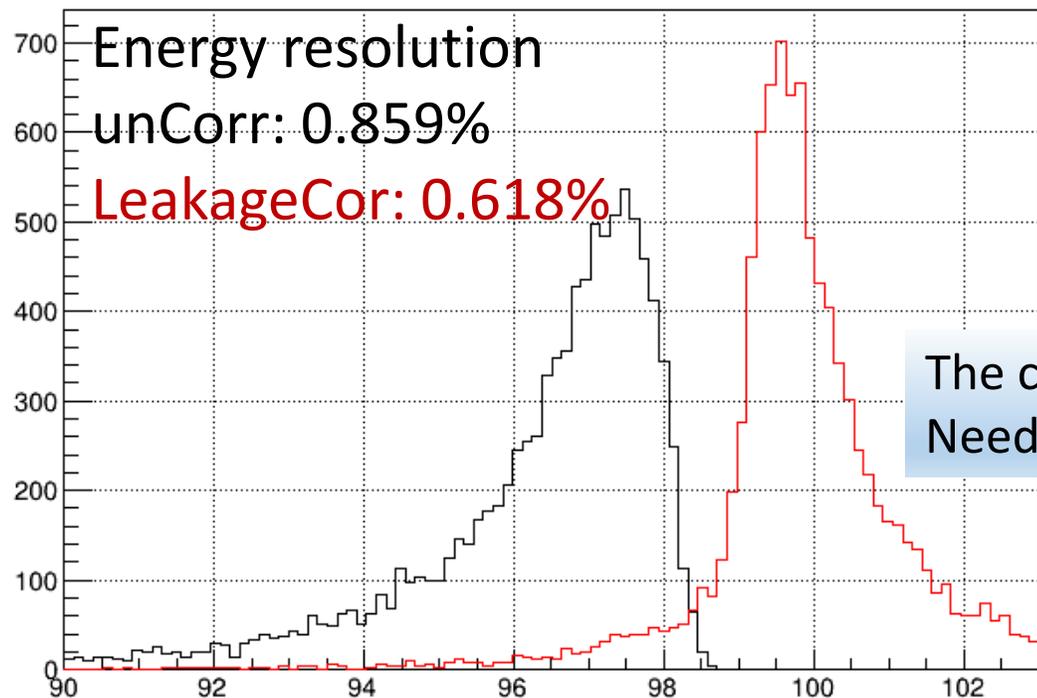


# Energy measurement of 100GeV $\gamma$ with 24cm depth crystal

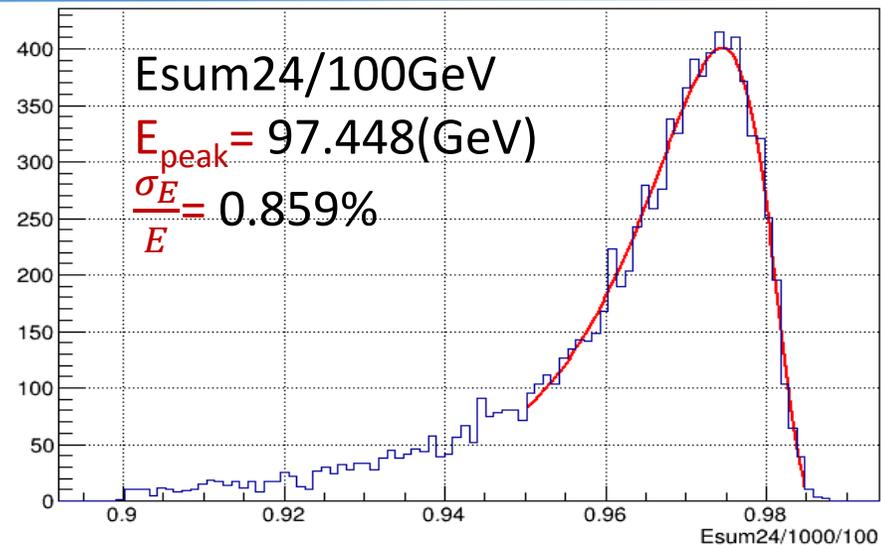
24cm( $\sim 21.4X_0$ ) length BGO

8 layers/3cm

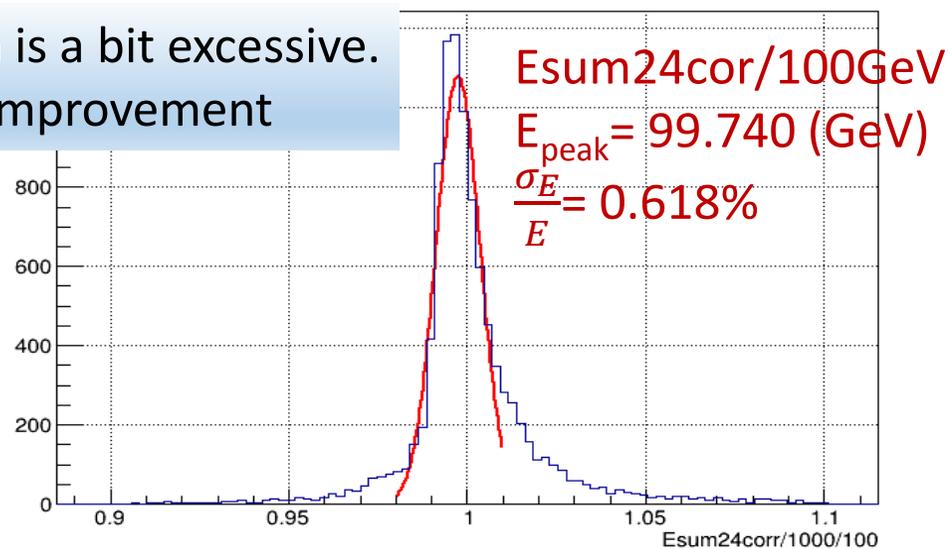
Cell size 1x1cm<sup>2</sup>



The energy resolution is optimized around 30%



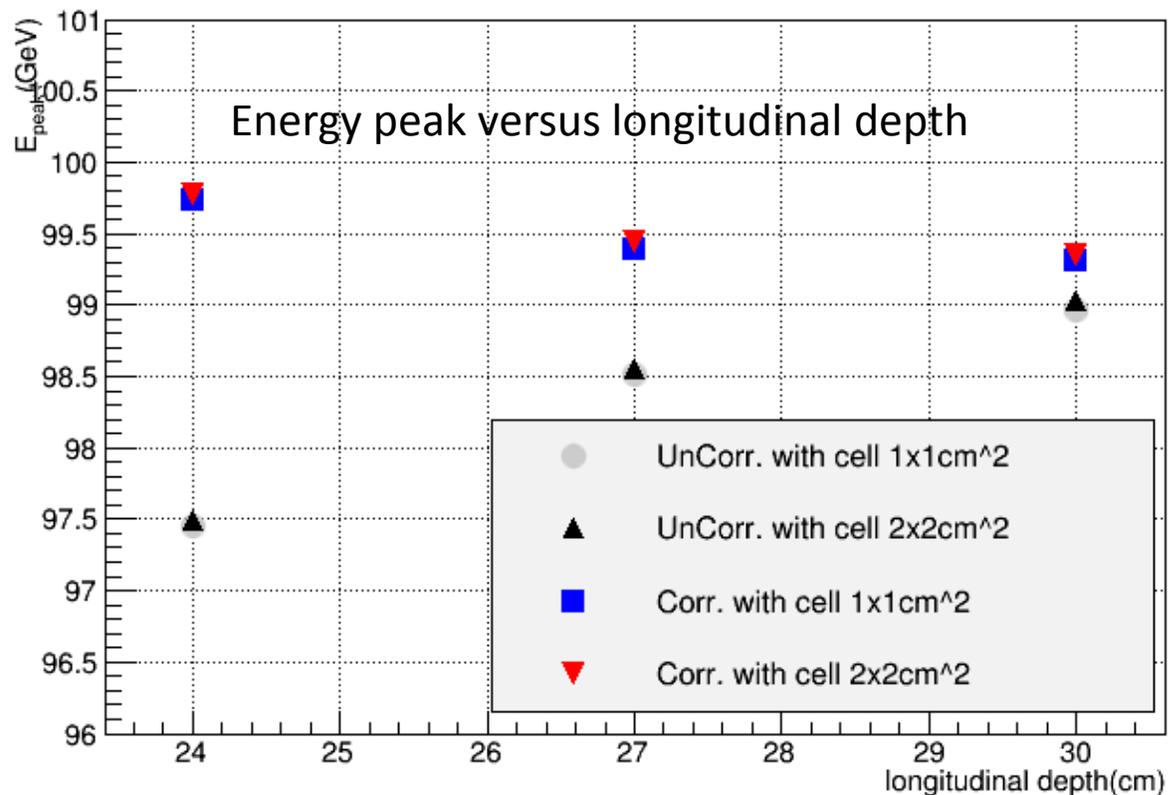
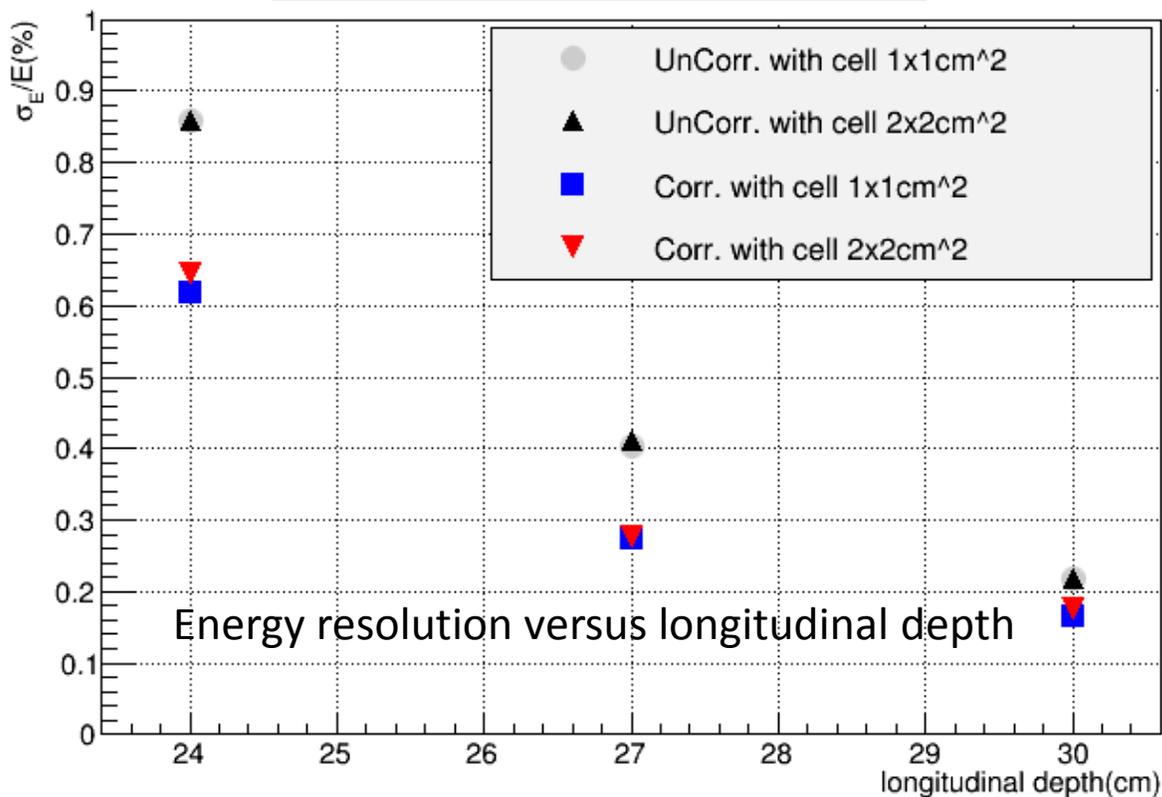
The correction is a bit excessive.  
Need further improvement





# The correction of the Longitudinal shower energy leakage

## Preliminary results



The energy peak has been corrected to 99.5%.  
The energy resolution is also optimized around 20% to 30%

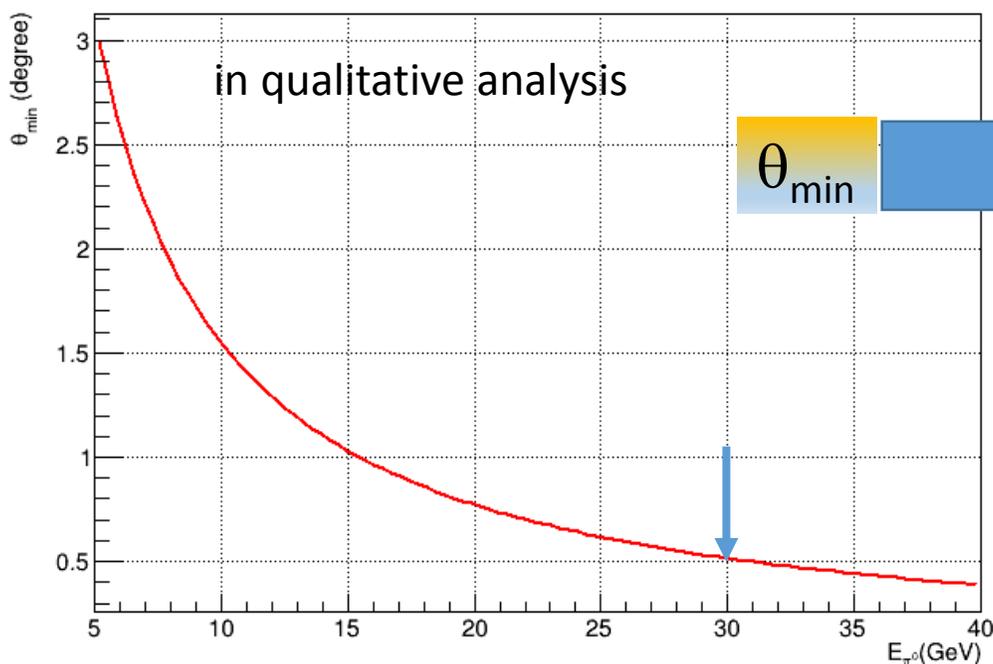
# Study of the separation performance of $\gamma$ and merged $\pi^0$



# Separation performance of $2\gamma$ 's from the high energy $\pi^0$ decay

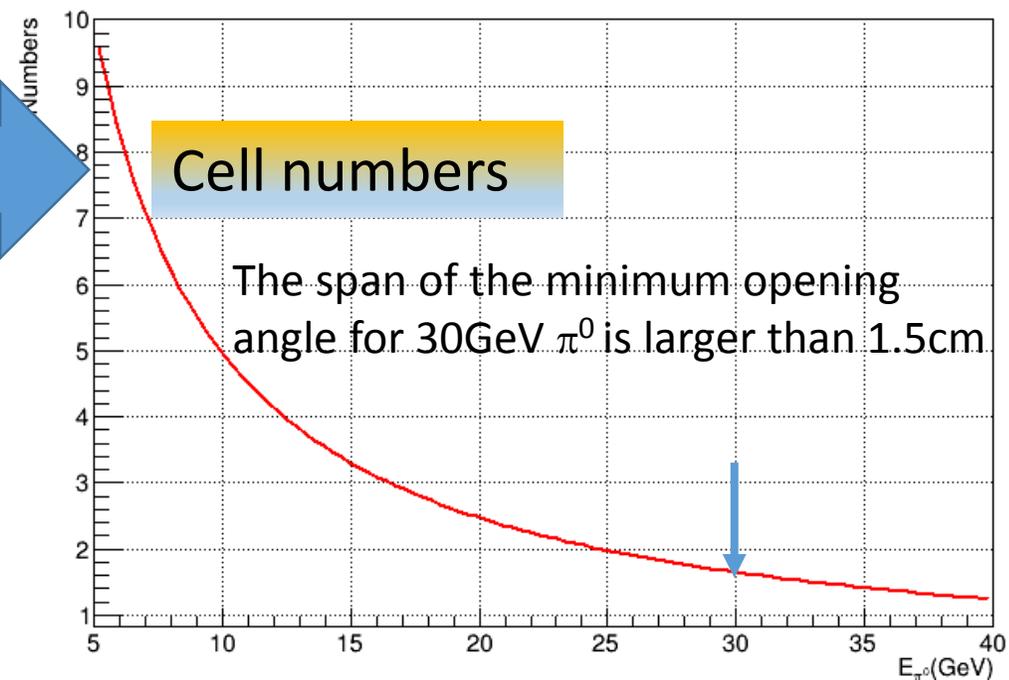
- Convert the  $\theta_{\min}$  into the cell numbers at  $\theta=90^\circ$  for CEPC with Radius(1.835m) and the cell size 10mm.
- One crystal has the maximum angle  $\sim 0.31224^\circ$  at  $\theta=90^\circ$  in barrel.

$\theta_{\min}$  of two gammas from  $\pi^0$  decay



$\theta_{\min}$  versus  $\pi^0$  momentum

cell Numbers at  $\theta=90^\circ$  for CEPC with Radius(1.835m) and cell size 10mm

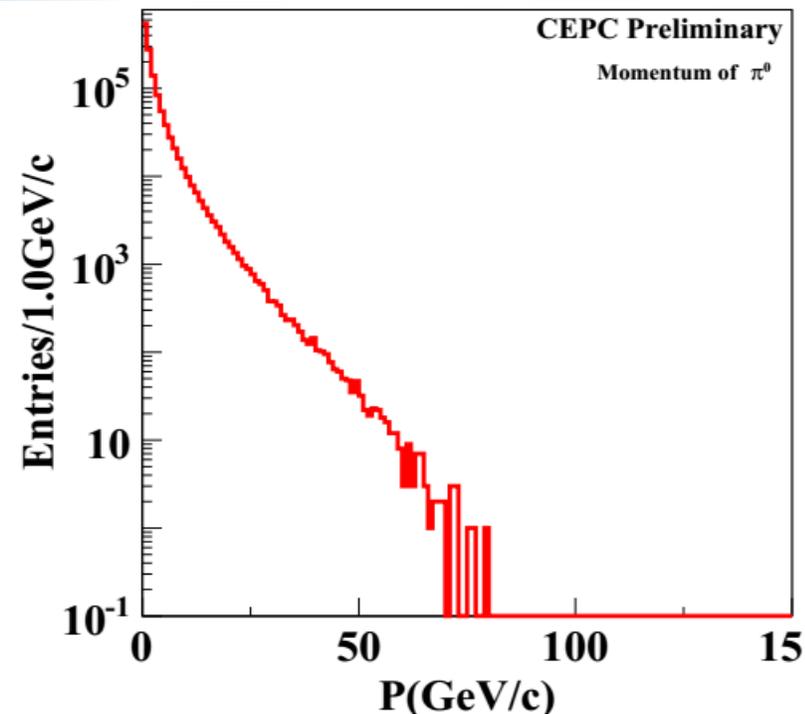


Cell numbers versus  $\pi^0$  momentum



# Separation Performance of $2\gamma$ 's from high energy $\pi^0$ decay

- For the purpose the decay events with the small opening angle are selected.
- There are two types of  $\pi^0$  event in ECAL reconstruction
  - One type is the “resolved”  $\pi^0$  from pair of photons.
  - Another type is the “merged”  $\pi^0$  from single cluster.
  - Their proportions are shown in the right table.
- So in the following the study of the separation performance of  $\gamma$  and merged  $\pi^0$  will use 40GeV  $\pi^0$  samples.

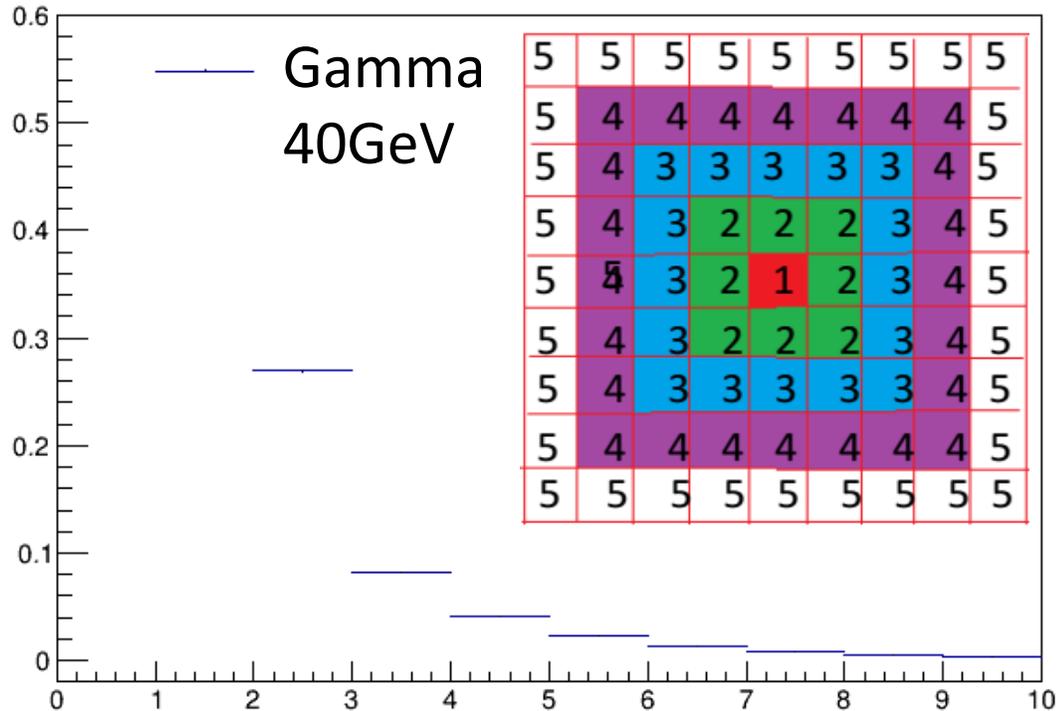


	$\pi^0$ Momentum	Cell 1x1cm <sup>2</sup>	Cell 2x2cm <sup>2</sup>
Resolved $\pi^0$	30GeV	~100%	0%
	40GeV	~60%	0%
Merged $\pi^0$	30GeV	0%	100%
	40GeV	~40%	100%



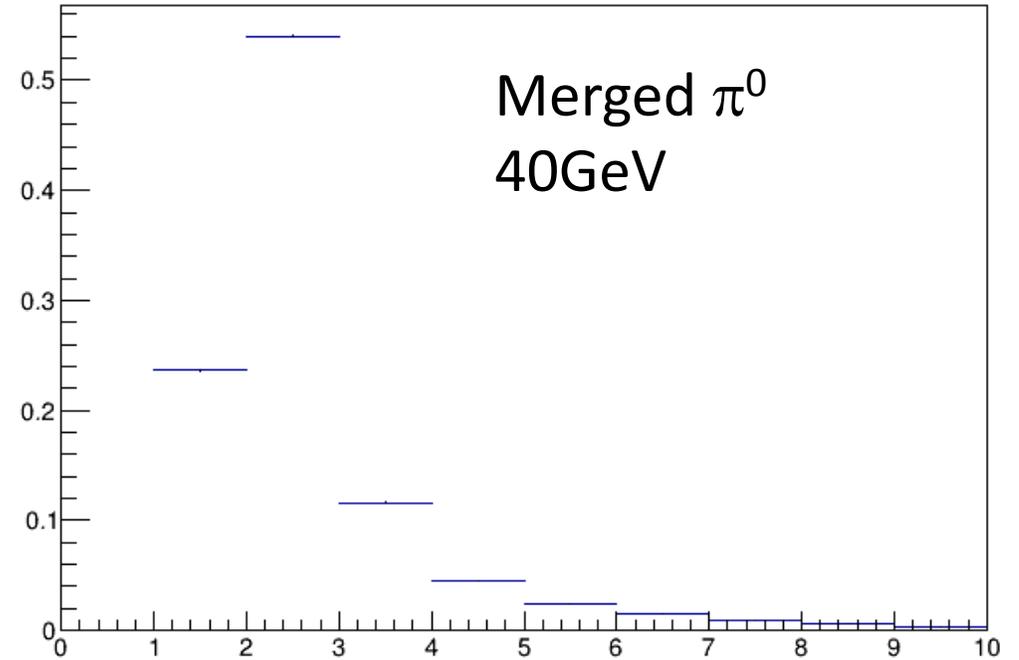
# Lateral shower energy distribution for Cell 1x1x30cm<sup>3</sup>

ECircle:ICircle



Energy of each circle versus circle number

ECircle:ICircle



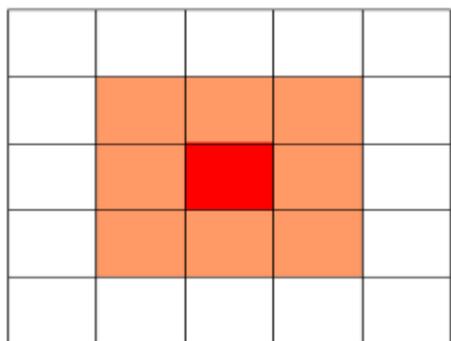
For single  $\gamma$ , the lateral shower energy is symmetric at the shower center.  
For merged  $\pi^0$ , the lateral shower is asymmetric.



# The shower shape variables

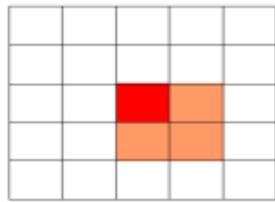
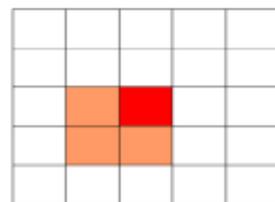
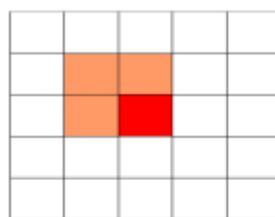
Study the separation performance of  $\gamma$  and merged  $\pi^0$  by using the shower lateral shape variables

- $S1/S4$ ,  $S1/S9$ ,  $S1/S25$ ,  $S9/S25$ ,  $S4/S9$ ,  $F9$ ,  $F16$

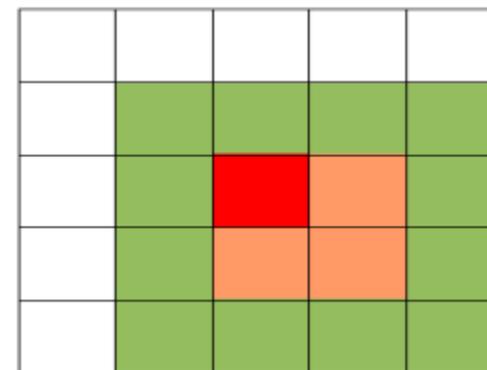


$S1, S9, S25$

$$F_9 = \frac{S9 - S1}{S9}$$



$S4$  the energy maximum in the four  $2 \times 2$  arrays



$S16$

$$F_{16} = \frac{S16 - S4}{S16}$$



# Study the 40GeV $\gamma$ /merged $\pi^0$ separation in three ways in the following

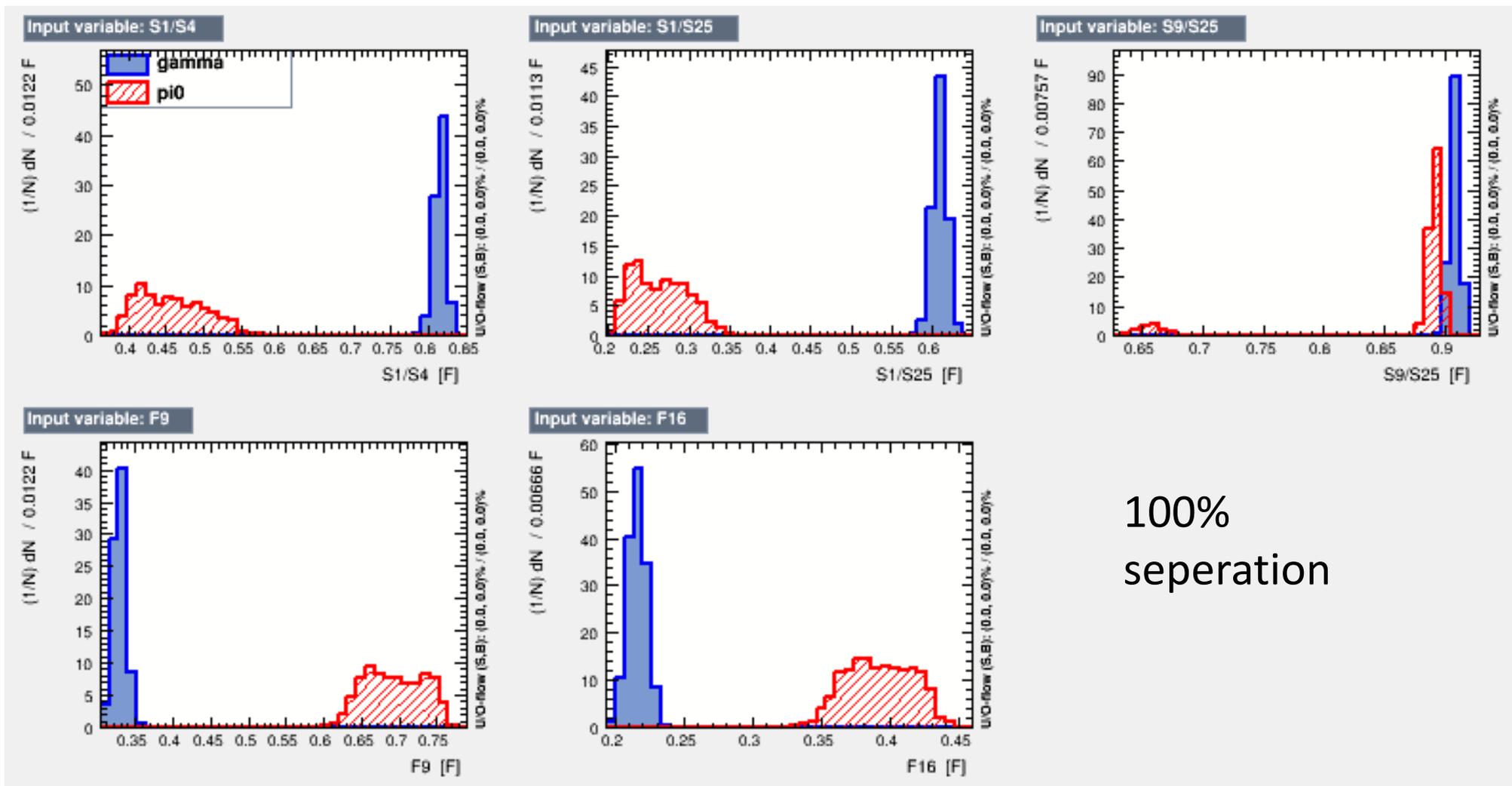
---

- Using the whole reconstruction of 30cm Depth (merge 10Layers)
- Using the whole reconstruction of 24cm Depth (merge 8Layers)
- Using alone the energy information of each layer with 3cm Depth
- In the each way we consider two types of cell size.
  - Cell size 1x1 cm<sup>2</sup>
  - Cell size 2x2 cm<sup>2</sup>



# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

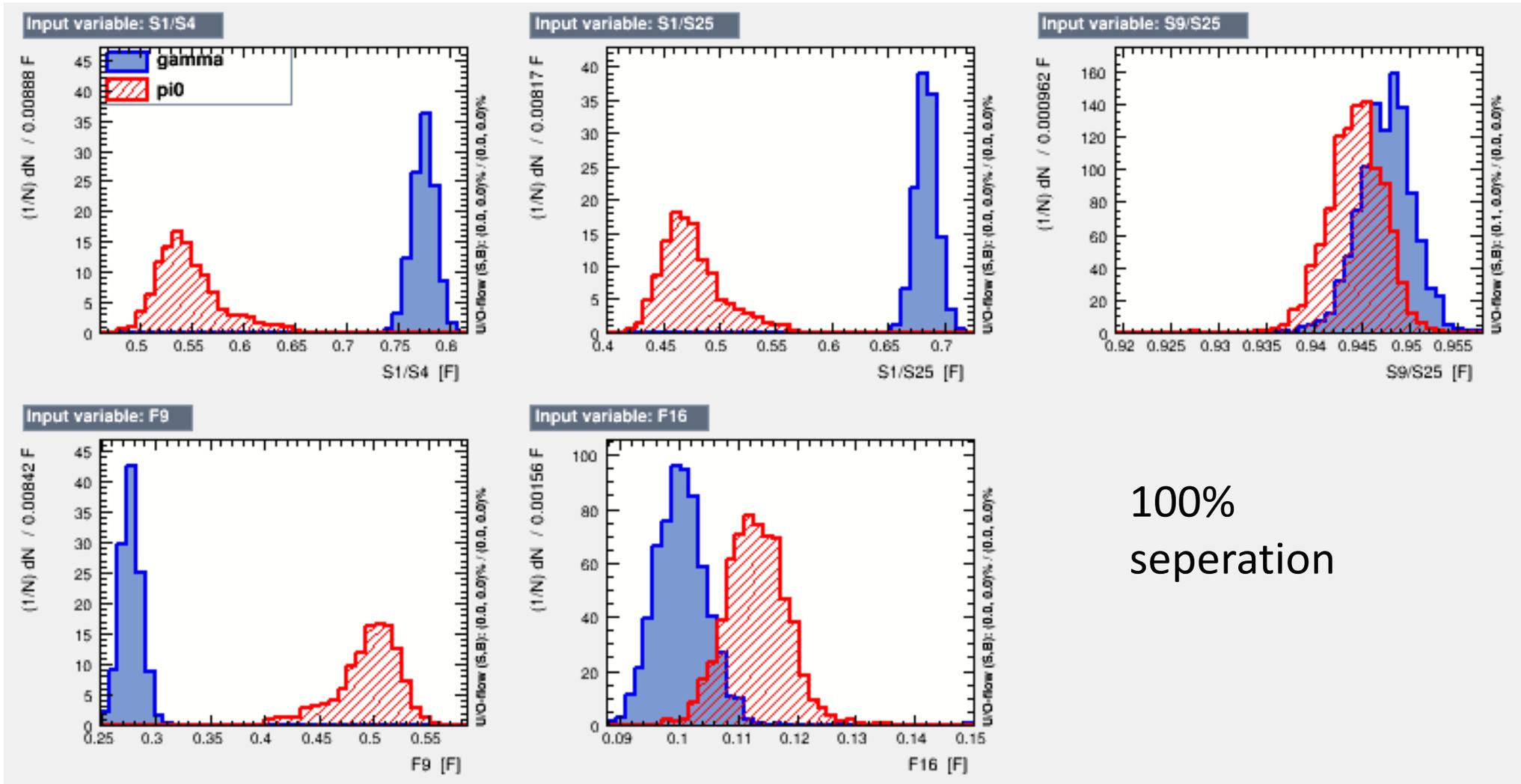
- the whole reconstruction of 30cm Depth with Cell 1x1cm<sup>2</sup>





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

- the whole reconstruction of 30cm Depth with Cell 2x2cm<sup>2</sup>

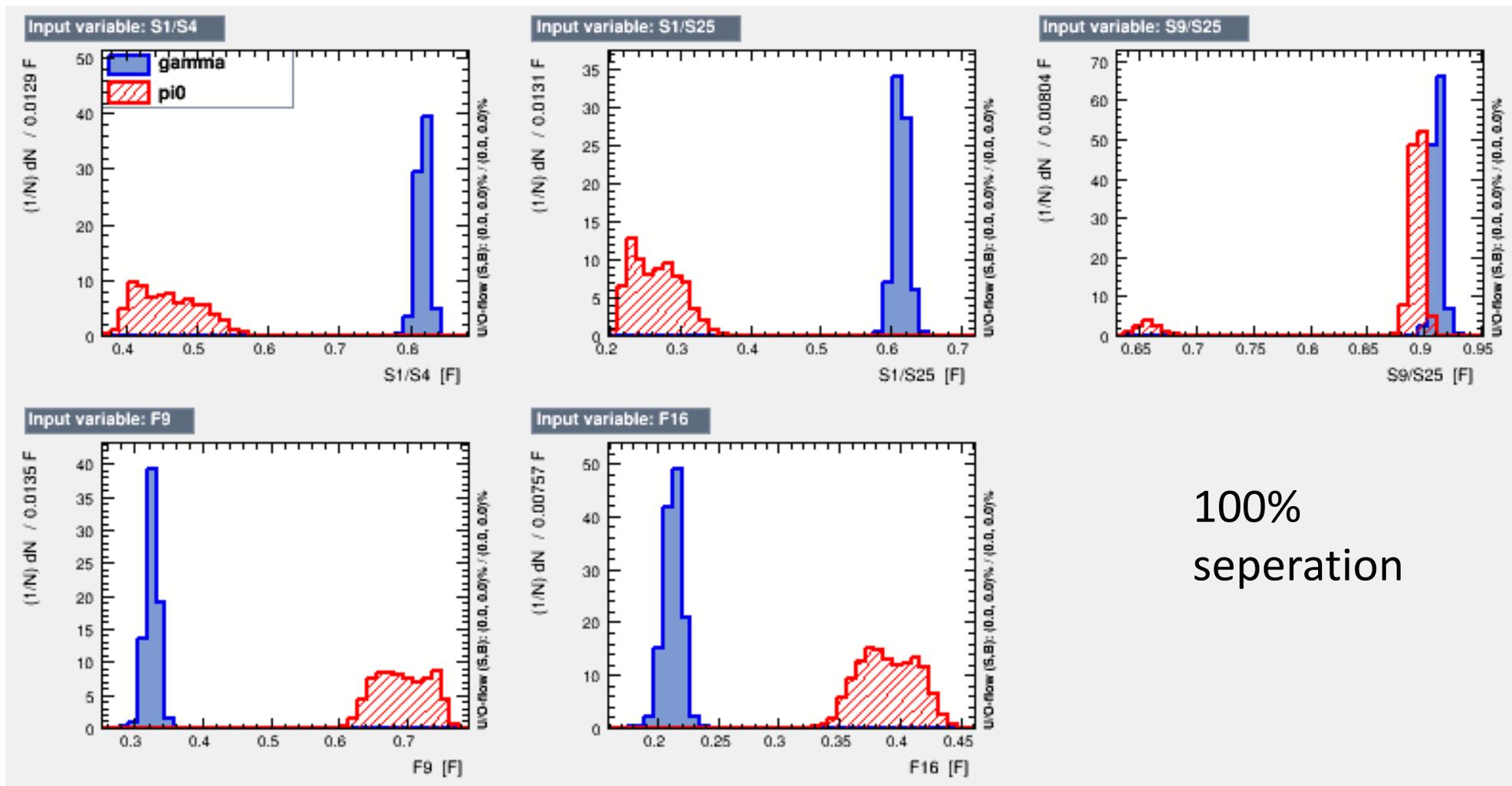


100%  
seperation



# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

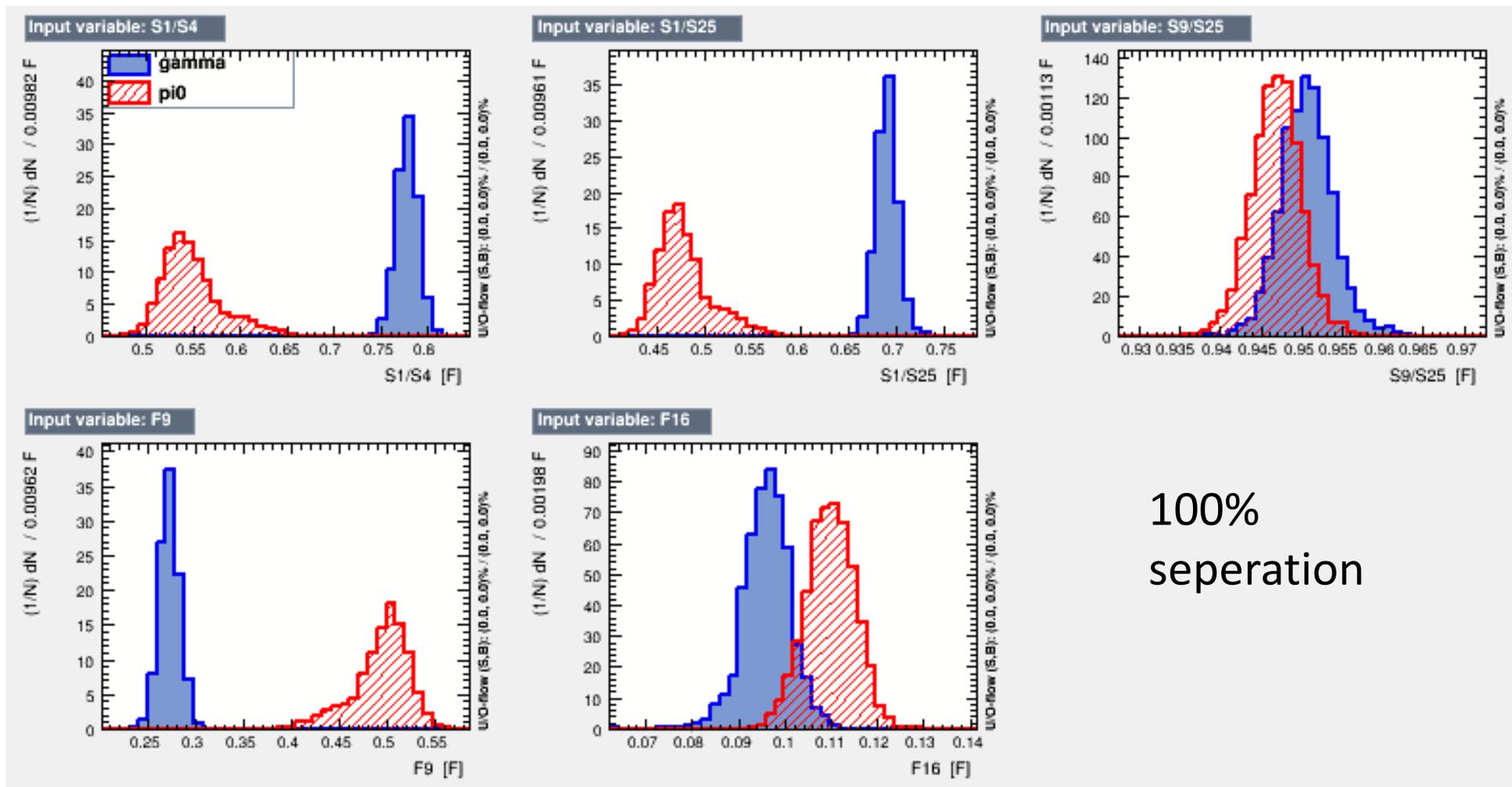
- the whole reconstruction of 24cm Depth with Cell 1x1cm<sup>2</sup>





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

- the whole reconstruction of 24cm Depth with Cell 2x2cm<sup>2</sup>

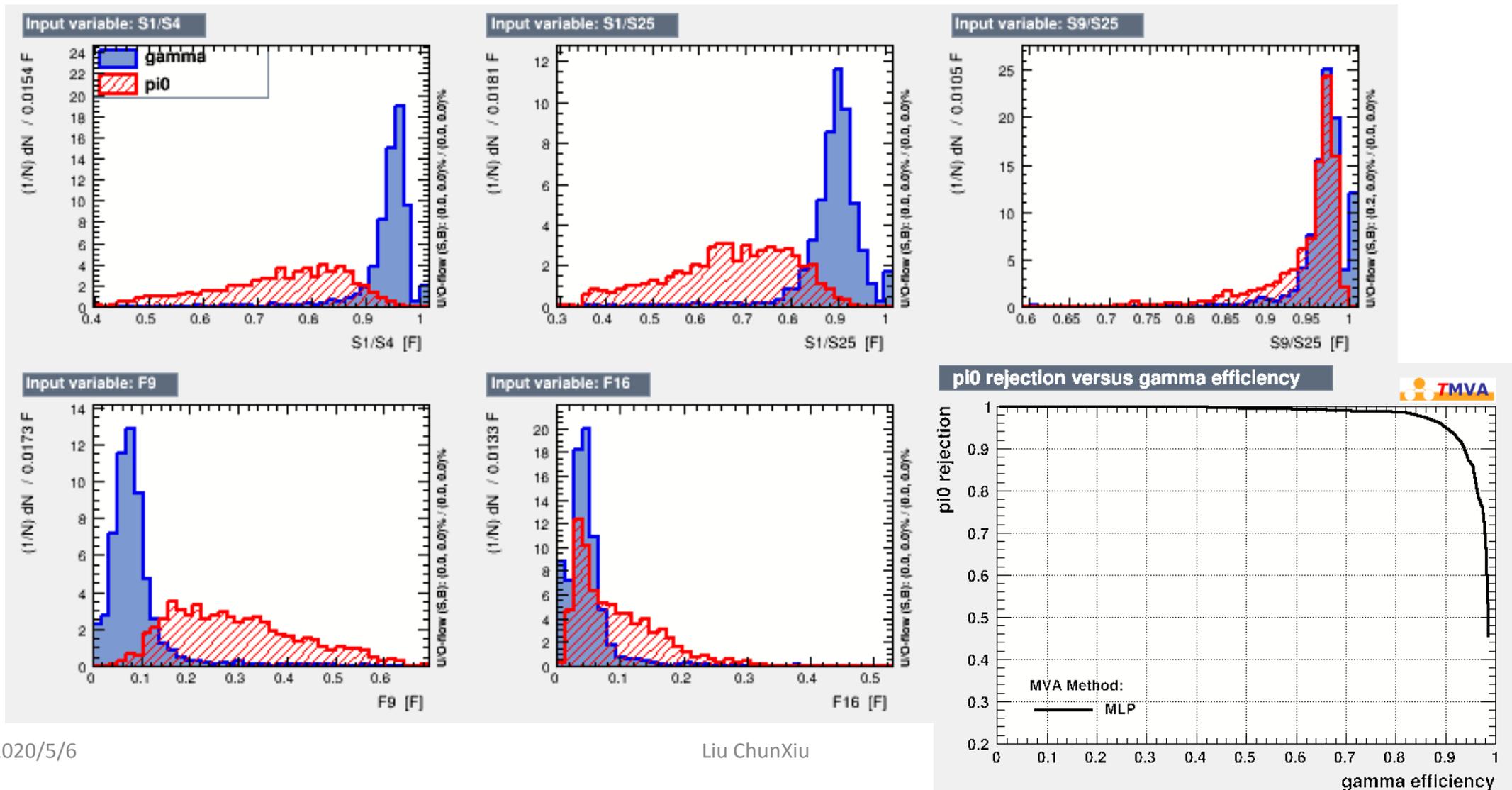


100%  
seperation



# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

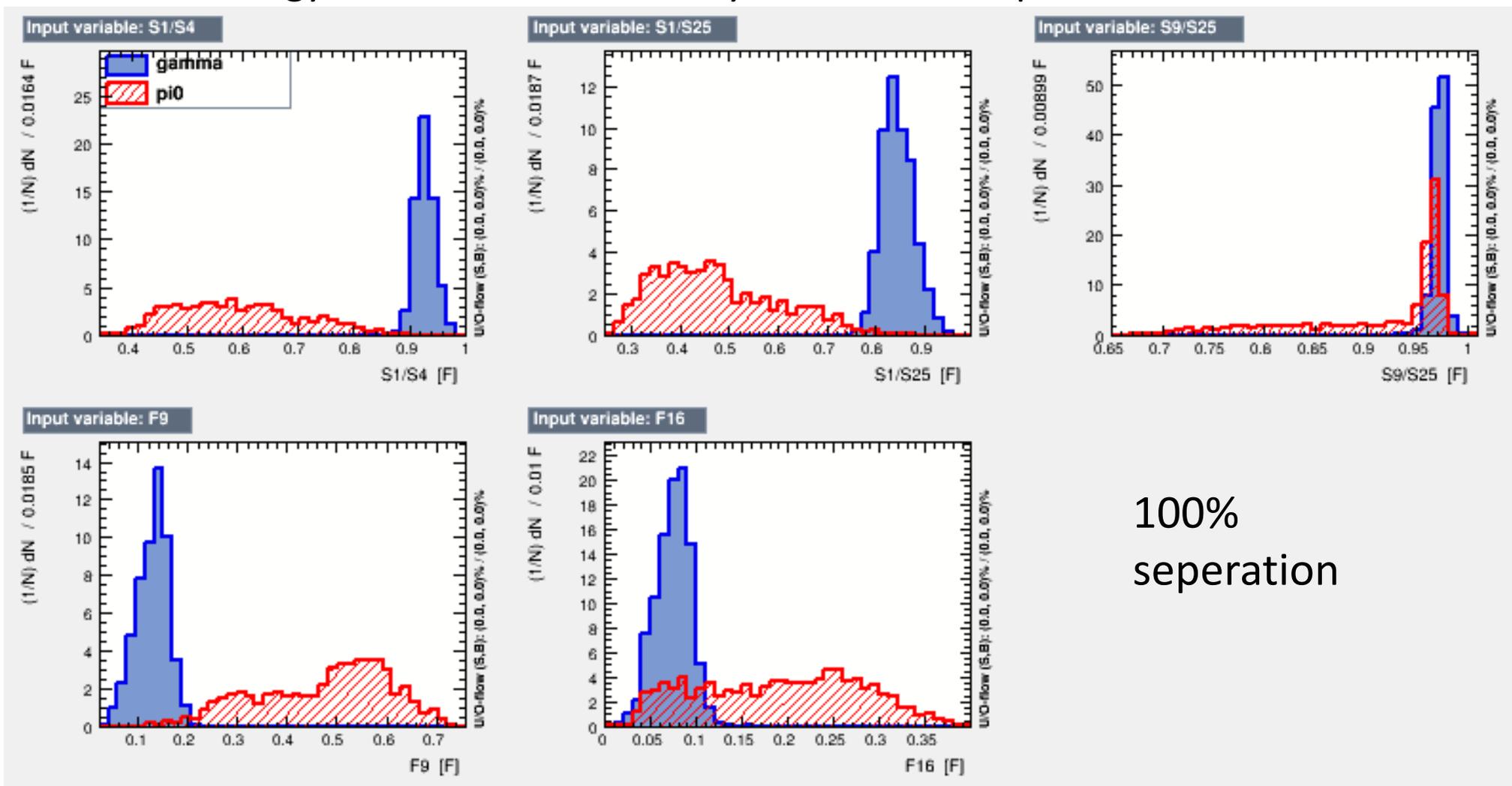
- alone the energy information of each layer with 3cm Depth with Cell  $1 \times 1 \text{cm}^2$  :1st layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

- alone the energy information of each layer with 3cm Depth with Cell  $1 \times 1 \text{cm}^2$  :2nd layer

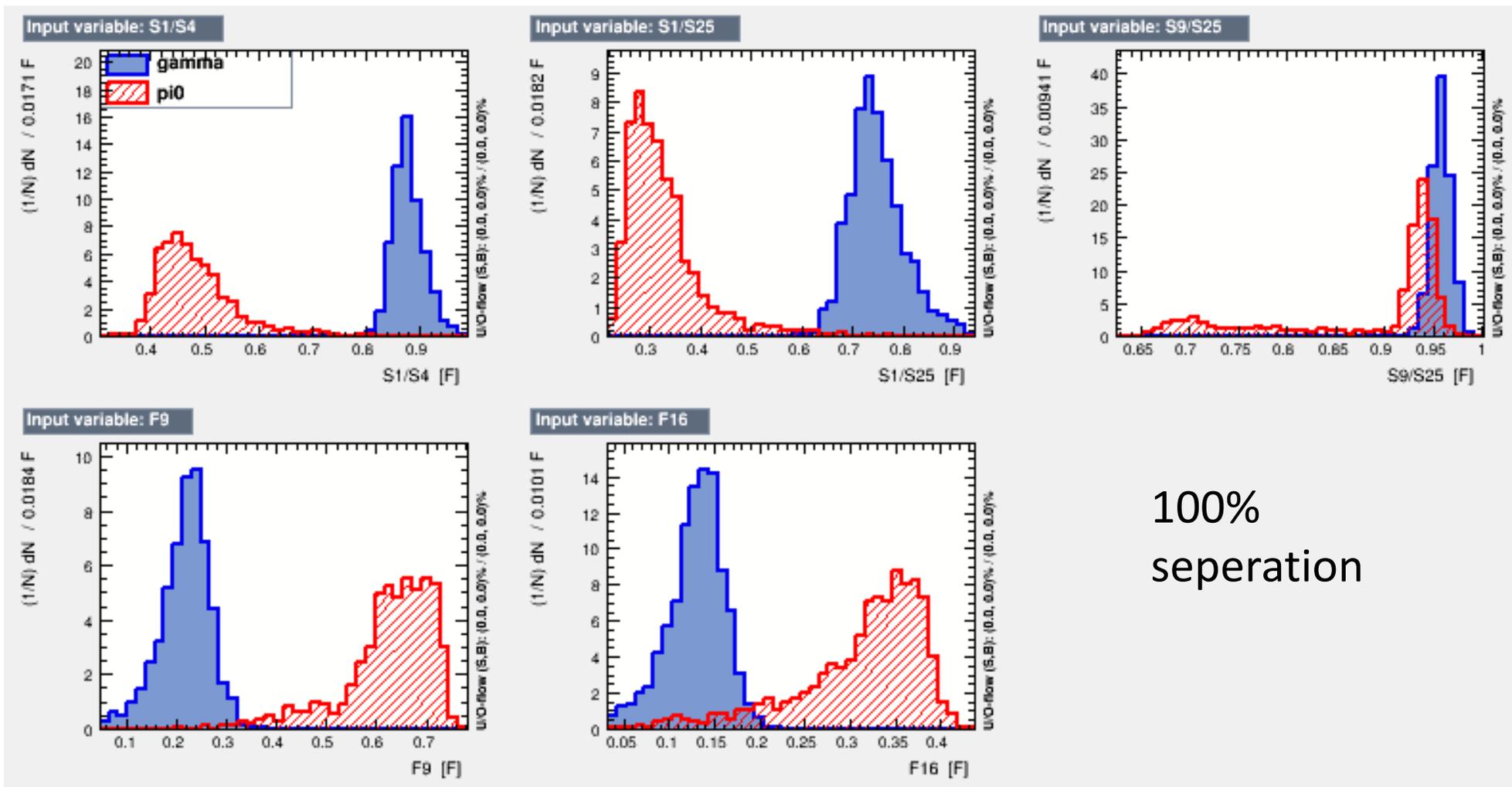


100%  
seperation



# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

- alone the energy information of each layer with 3cm Depth with Cell  $1 \times 1 \text{cm}^2$  :3rd layer

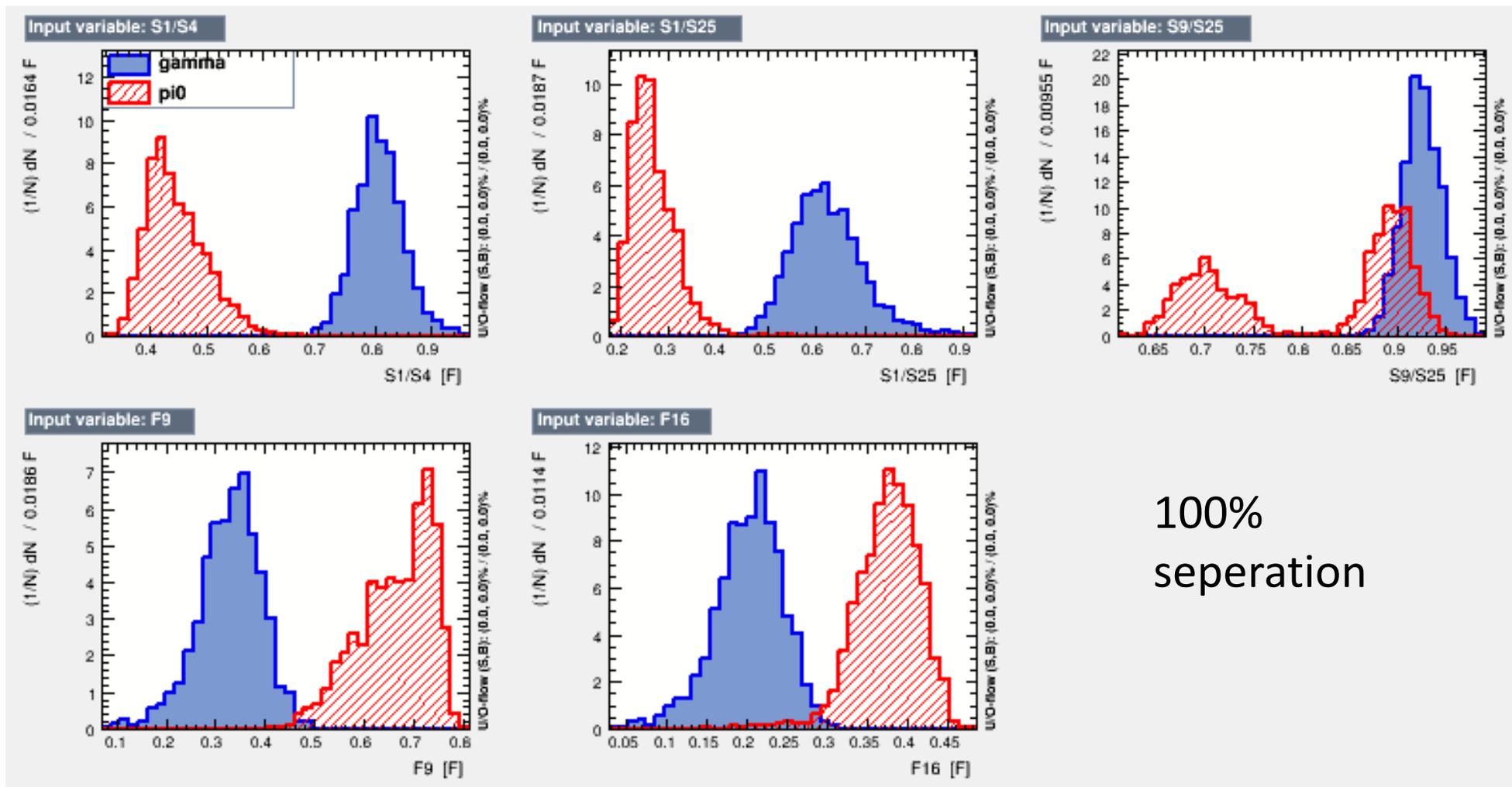


100%  
seperation



# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

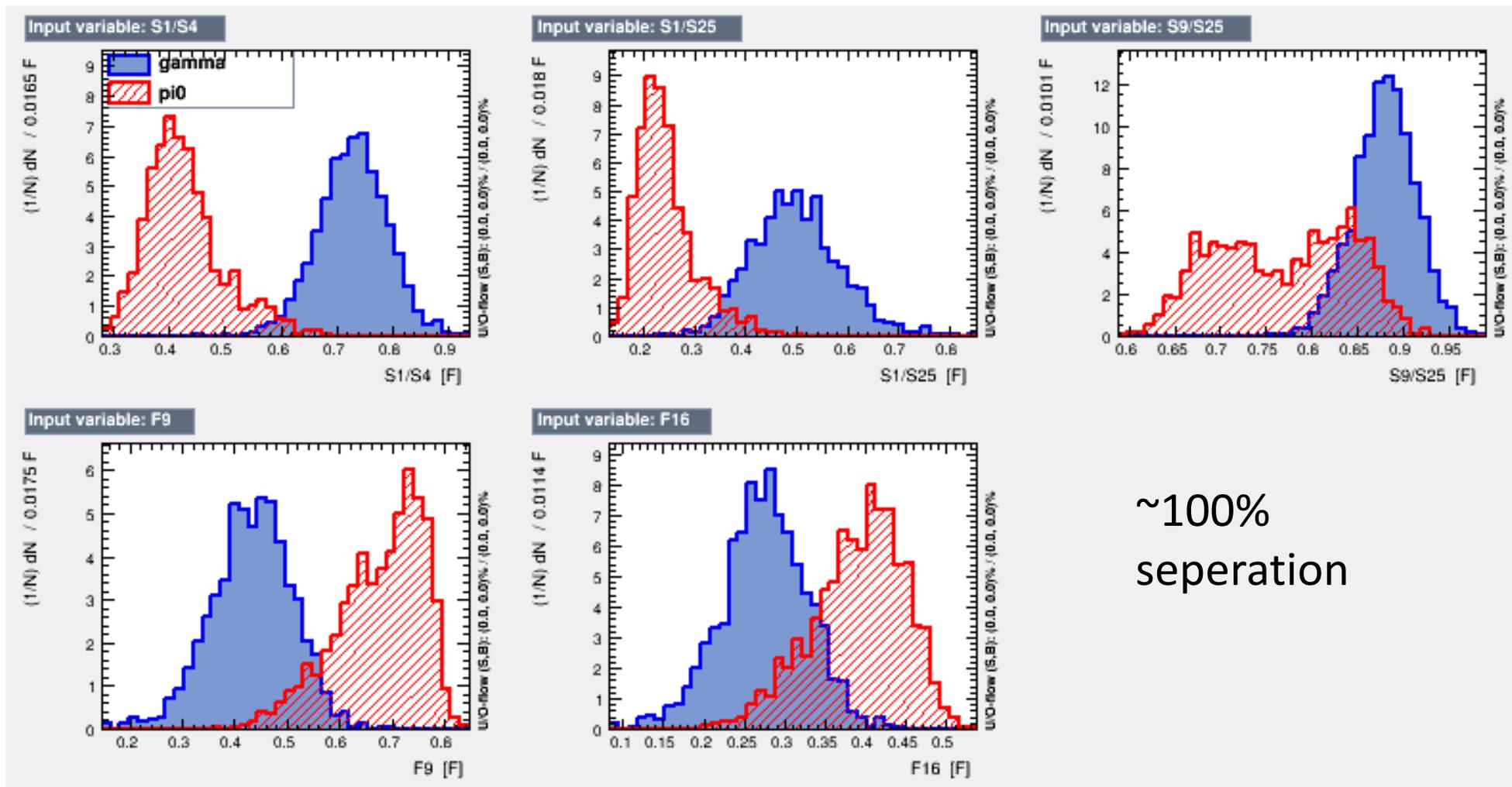
- alone the energy information of each layer with 3cm Depth with Cell  $1 \times 1 \text{cm}^2$  :4th layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

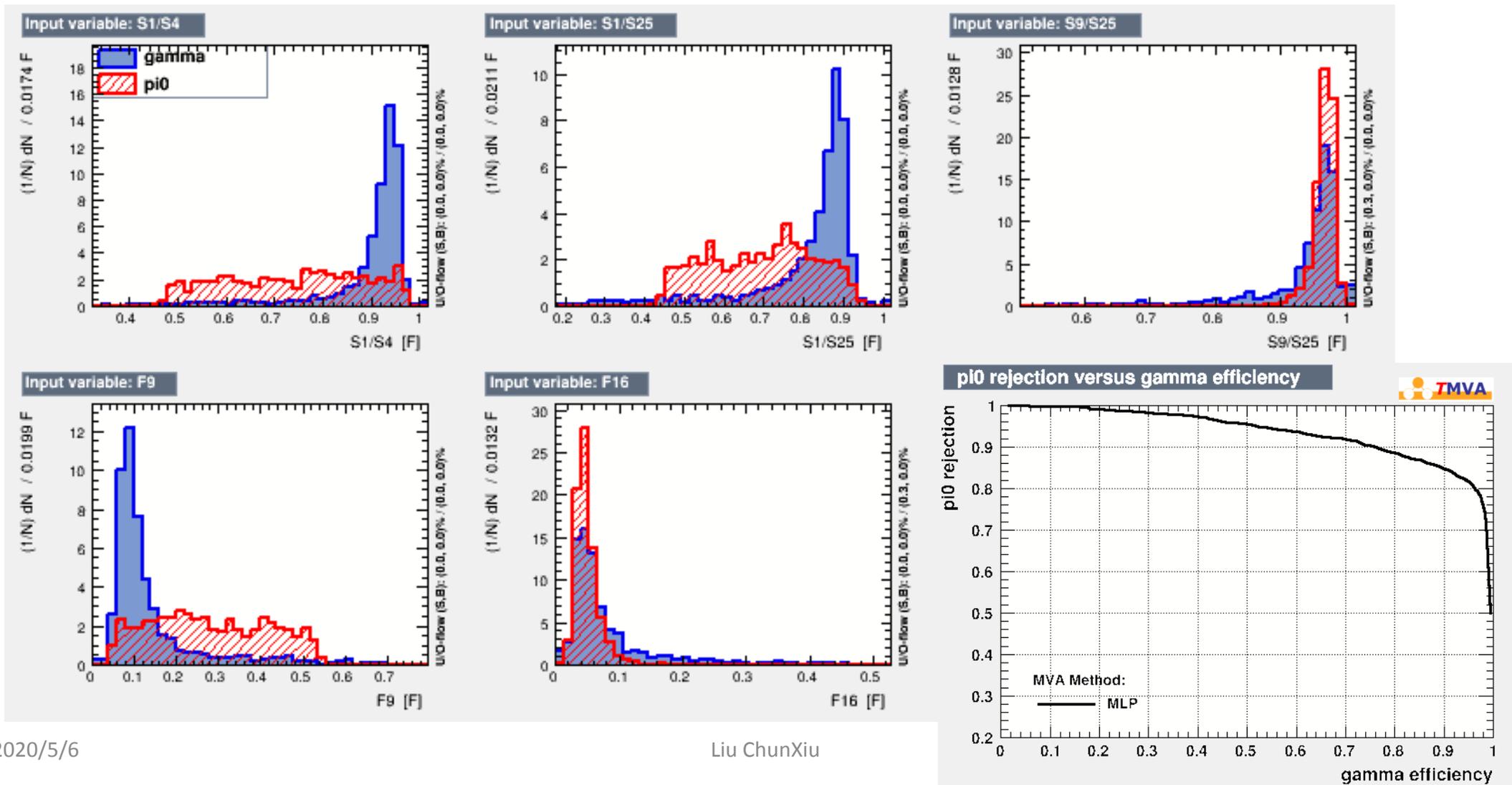
- alone the energy information of each layer with 3cm Depth with Cell  $1 \times 1 \text{cm}^2$  :5th layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

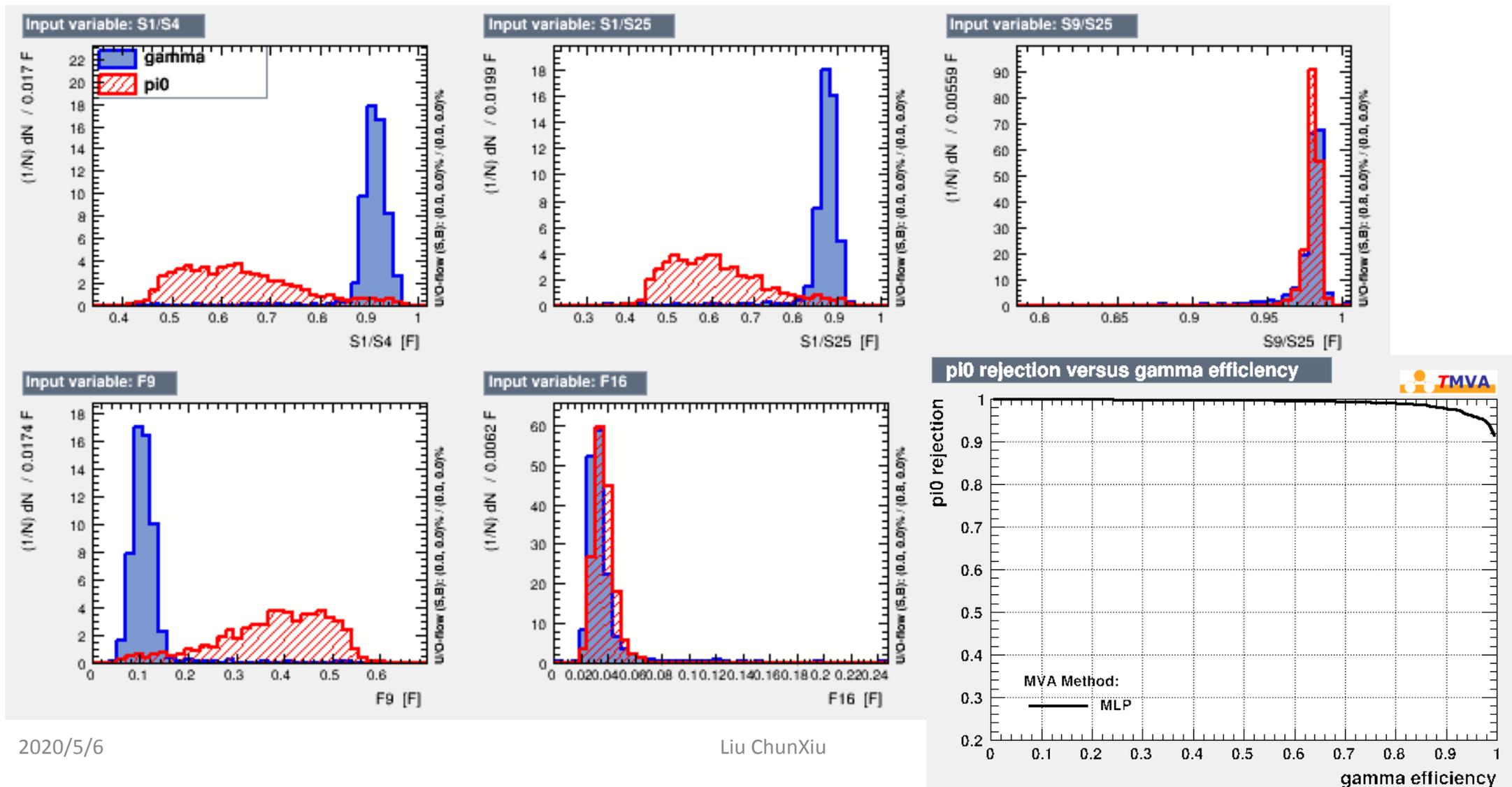
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :1st layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

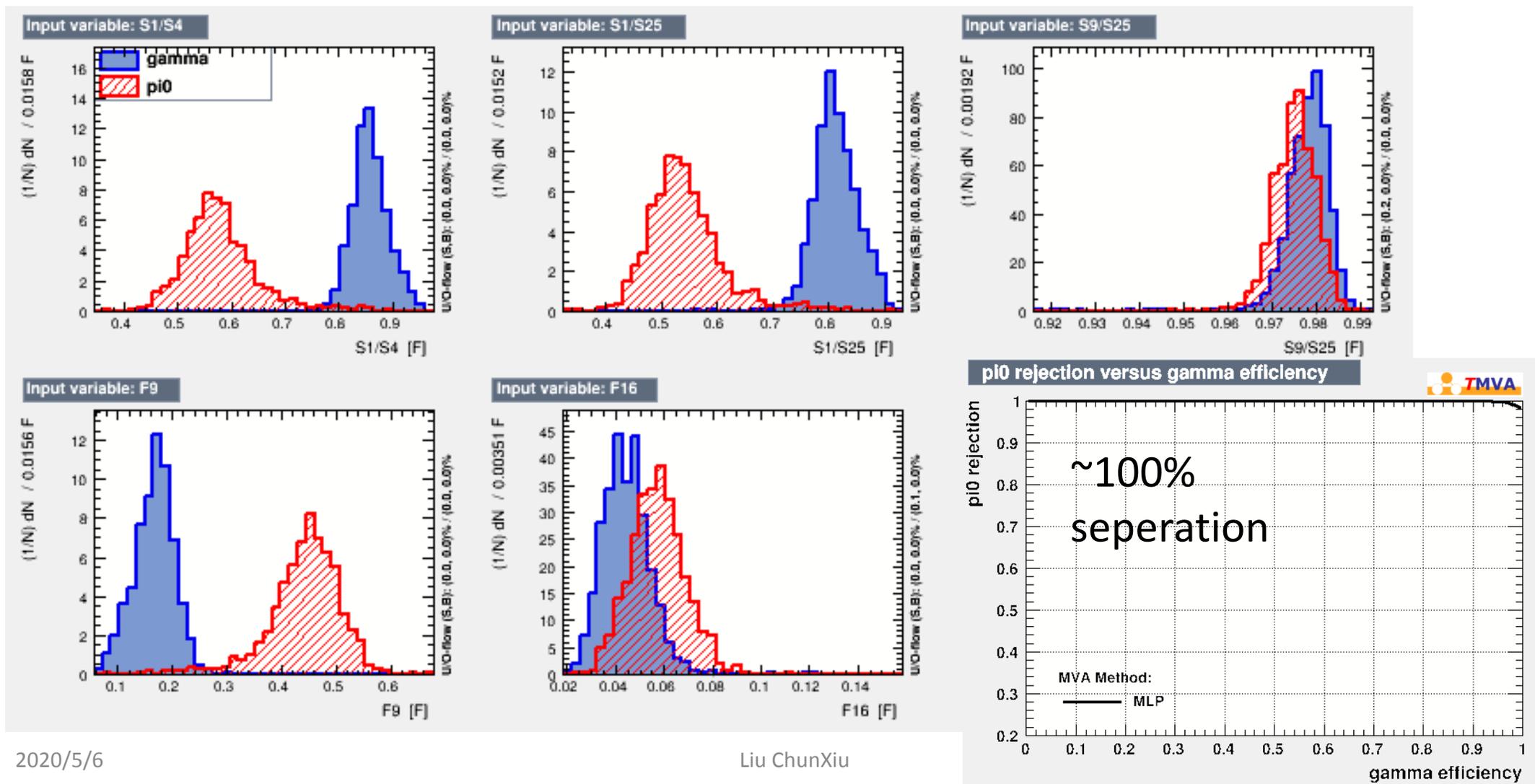
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :2nd layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

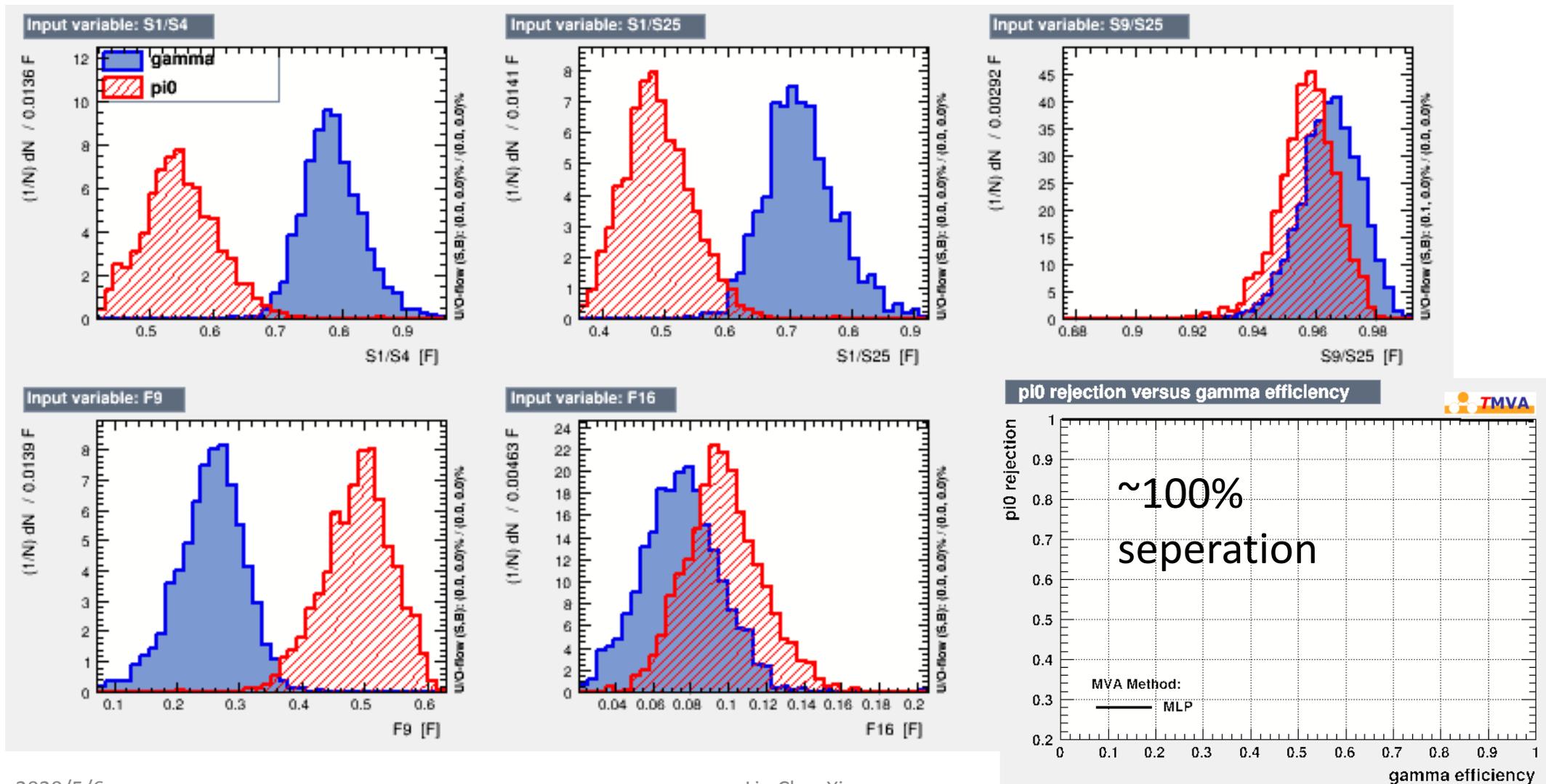
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :3rd layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

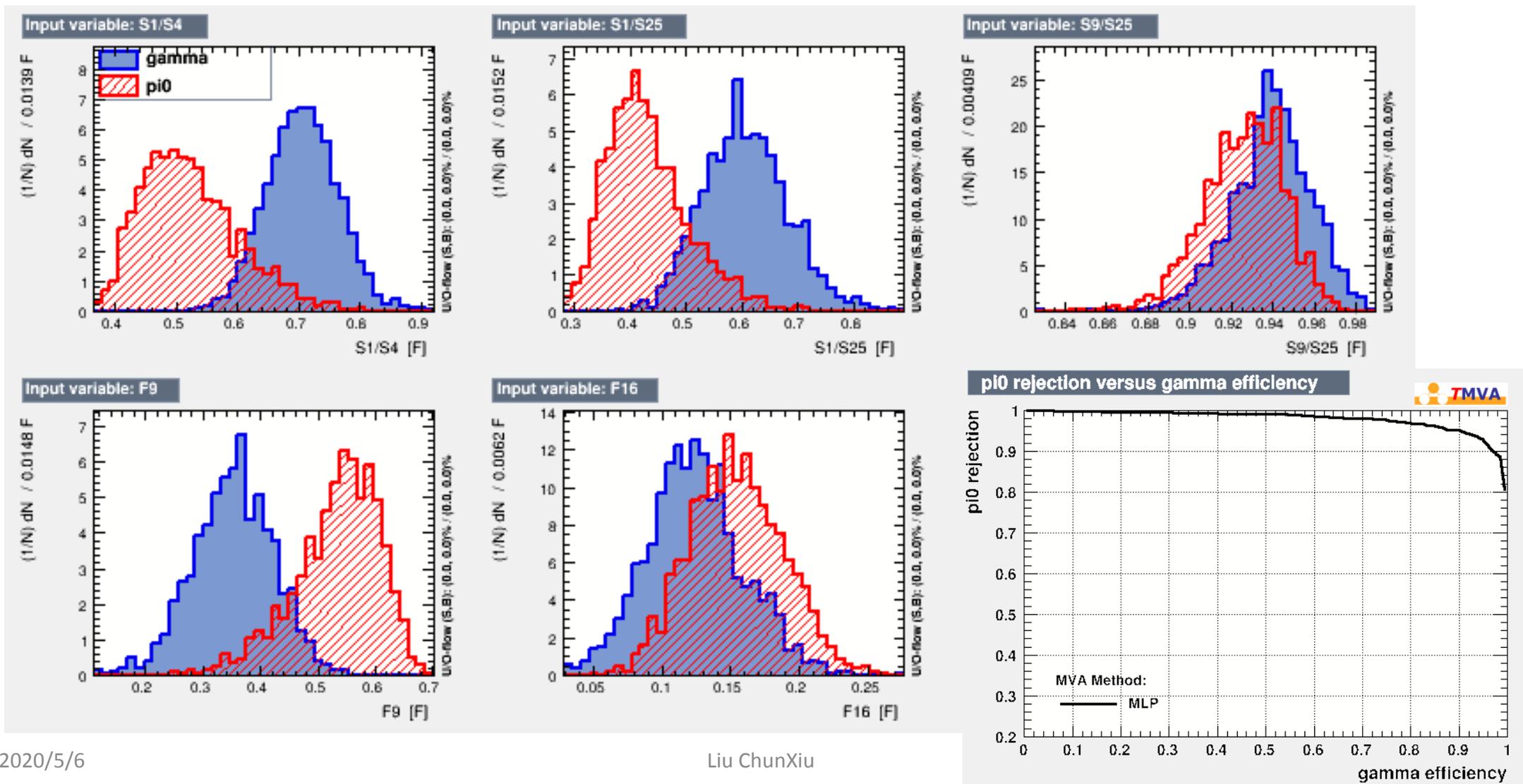
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :4th layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

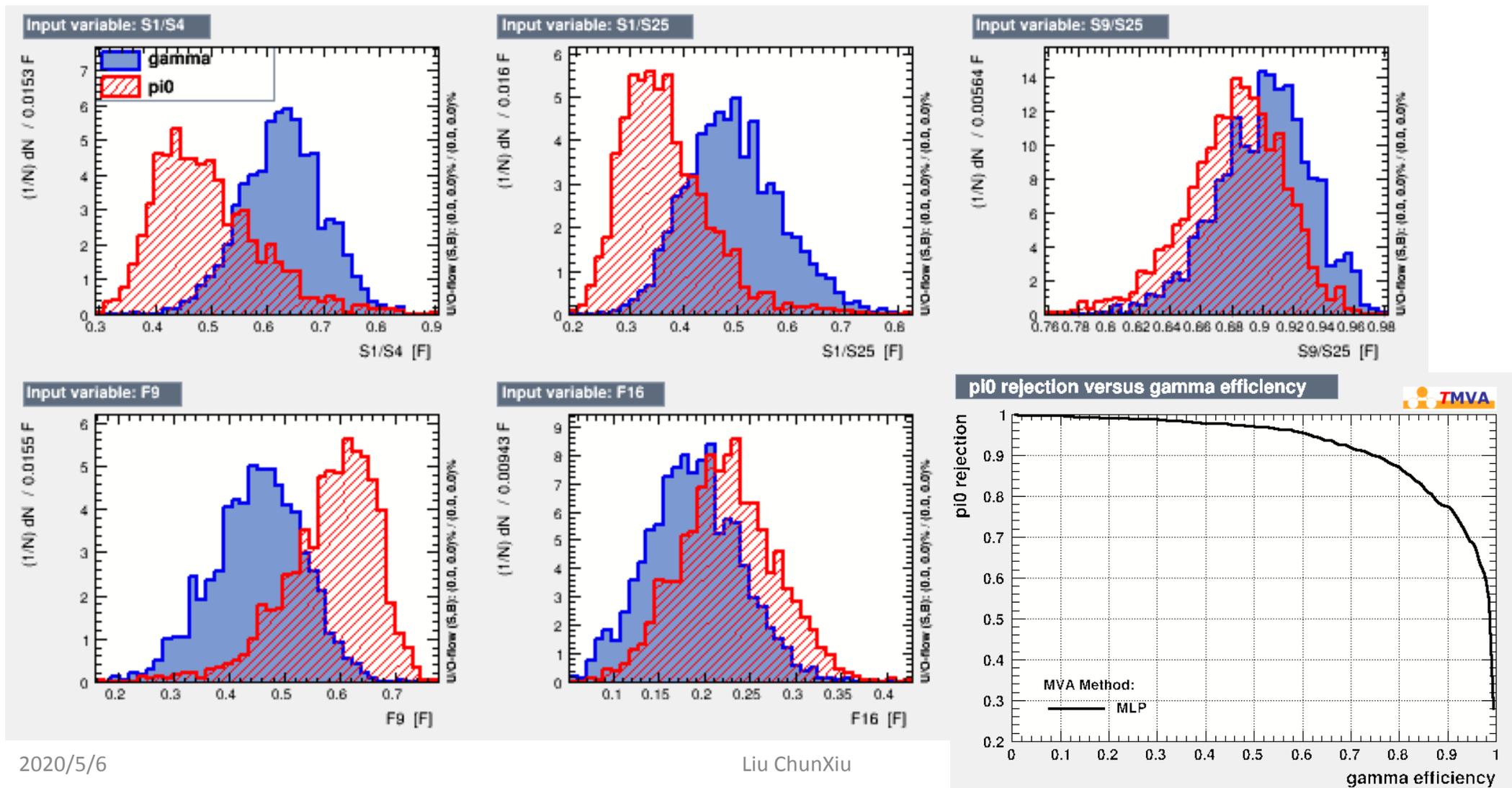
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :5th layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

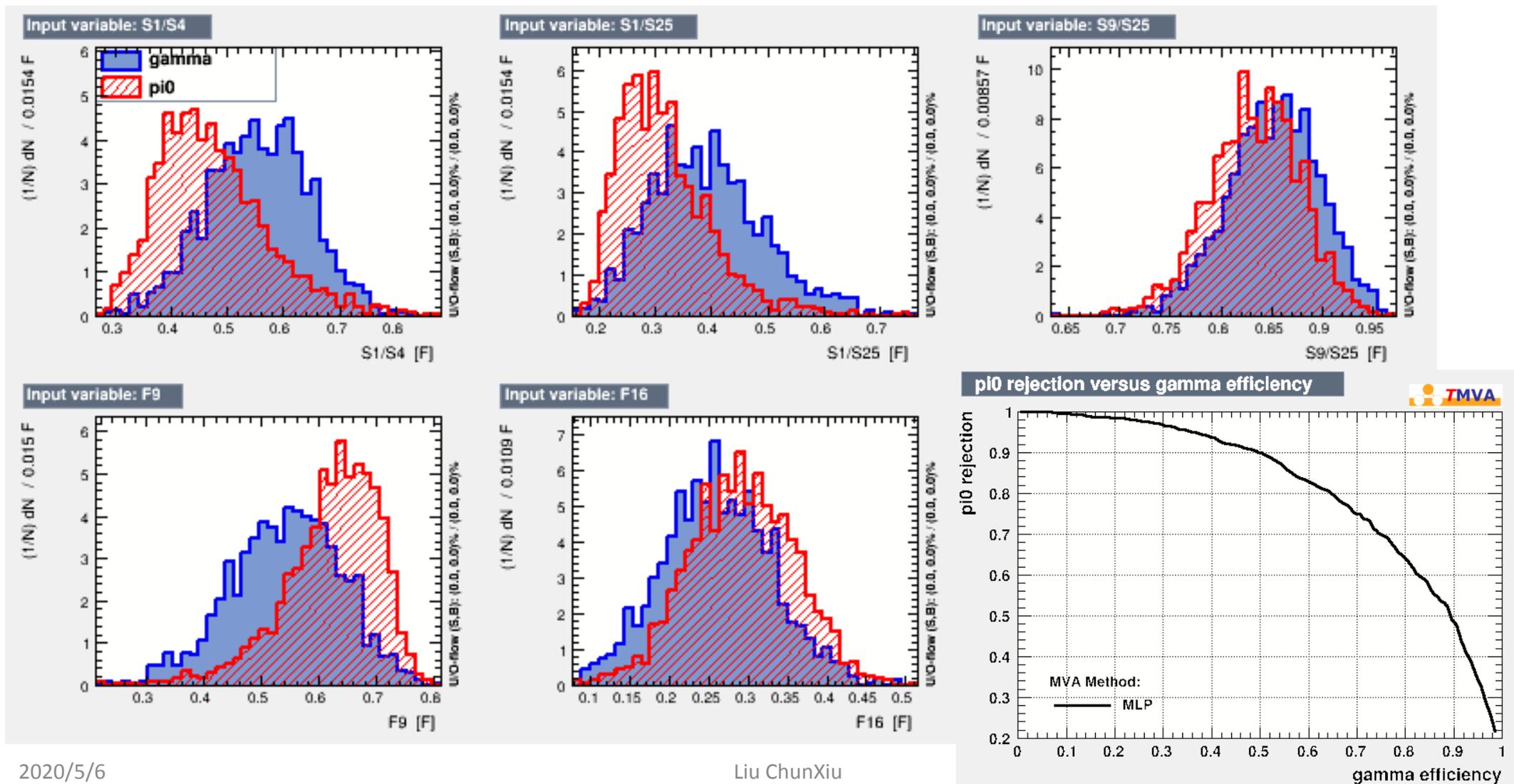
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :6th layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

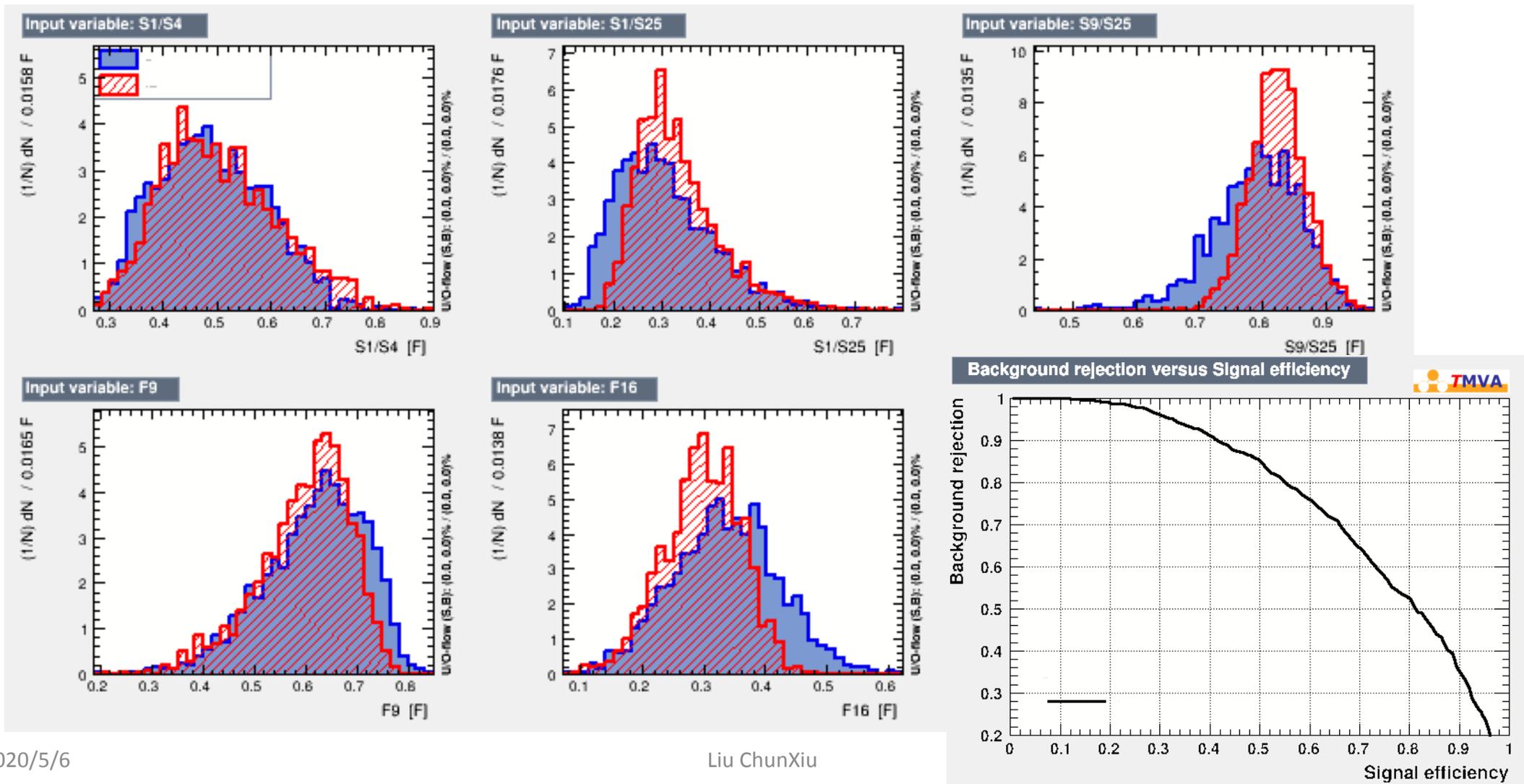
- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :7th layer





# separation performance of the 40GeV $\gamma$ and merged $\pi^0$

- alone the energy information of each layer with 3cm Depth with Cell  $2 \times 2 \text{cm}^2$  :8th layer





## separation performance of the 40GeV $\gamma$ and merged $\pi^0$

---

- 30cm Depth (merge 10Layers), and 24cm Depth (merge 8Layers)
  - separation performance is 100% for cell 1x1cm<sup>2</sup> and 2x2cm<sup>2</sup>
- using alone the reconstruction of each layer with 3cm Depth
  - In the maximum shower layer, the separation performance is best, especially, for cell 2x2 cm<sup>2</sup>.



# Summary

---

- Construct the BGO matrix module with  $60 \times 60 \times 60 \text{cm}^3$  in Geant4
- Complete the cluster reconstruction of each layer
- Give some preliminary study results
  - Study the correction of the longitudinal energy leakage, the energy resolution can be improved by  $\sim 20\%$ - $30\%$ . The preliminary results show that longitudinal direction needs at least 7~8 layers, and each layer depth should not be larger than 3cm.
  - Separation performance of  $2\gamma$ 's from high energy  $\pi^0$  decay,
    - For cell  $1 \times 1 \text{cm}^2$ , "resolved"  $\pi^0$  is  $\sim 100\%$  for 30GeV and  $\sim 60\%$  for 40GeV
    - For cell  $2 \times 2 \text{cm}^2$ , "resolved"  $\pi^0$  is 0%.
  - Separation performance of 40GeV  $\gamma$  and merged  $\pi^0$  is  $\sim 100\%$ , for cell  $1 \times 1 \text{cm}^2$  and  $2 \times 2 \text{cm}^2$ .
  - Need to further study



# merged $\pi^0$ reconstruction in processing

---

Next to work:

- Investigate the methods of merged  $\pi^0$  reconstruction
  - Two second moment methods:
    - to estimate the invariant mass of the  $\pi^0$  system based on the shape of the merged cluster
  - The third method:
    - the single cluster of the merged  $\pi^0$  is split into two interleaved 3x3 subclusters built around the two main cells in the original cluster.
- .....

Thank you!