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# SNRs – Particle escape and gamma-ray halo formation

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TeVPa, 25-29 October 2021

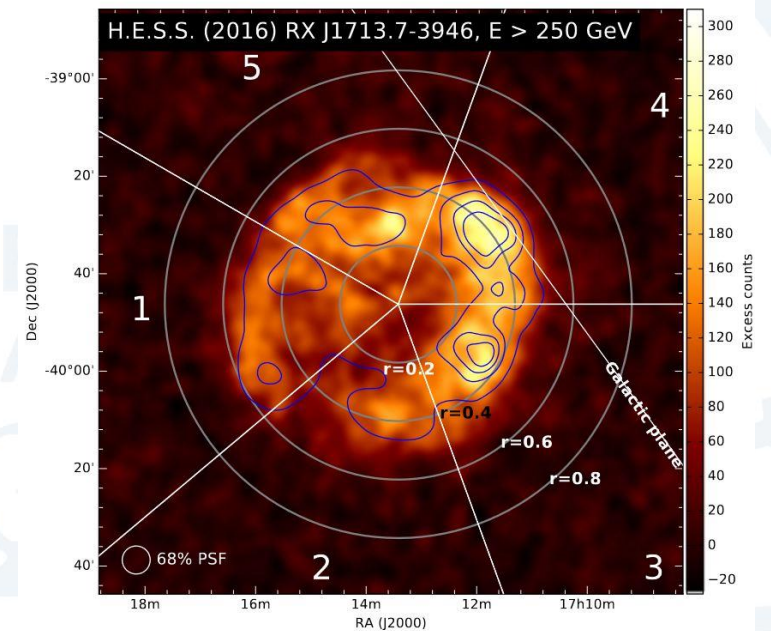


# The cosmic-ray spectrum

## Experimental evidence

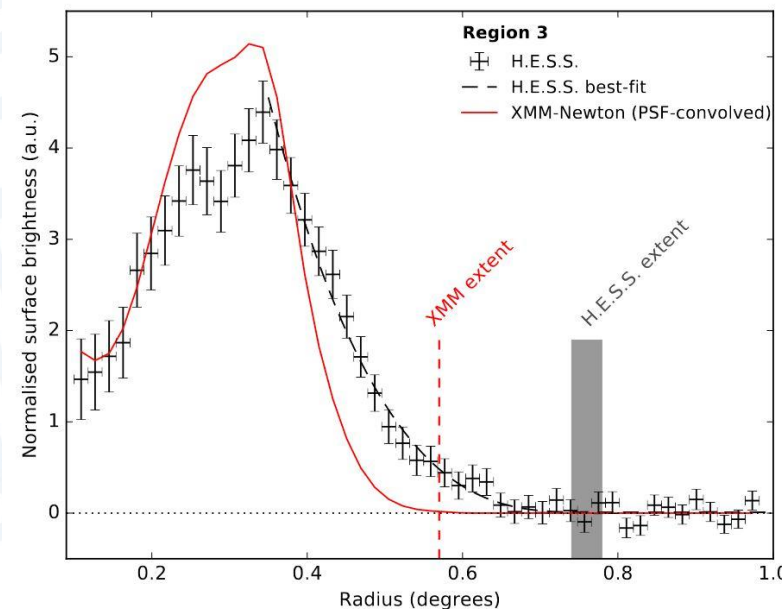
More and more observational constrains:

Models need to account for spectral evolution and morphology

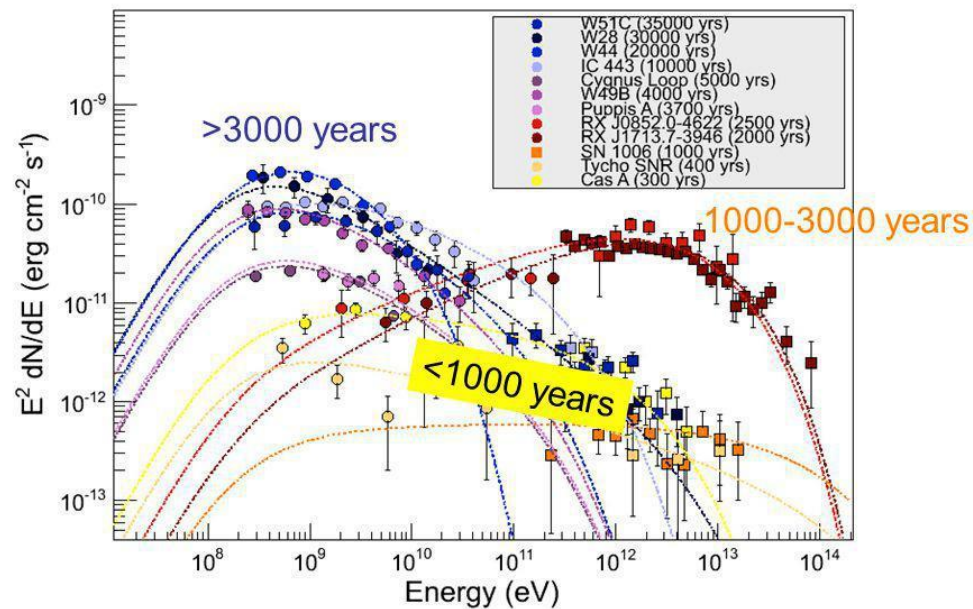


Figures:  
(Top) Excess-count map of RX J1713.7-3946

(Left) Gamma-ray and X-ray profiles of RX J1713.7-3946 (H.E.S.S. 2018)



Evolution of particle acceleration in the shell-type SNRs



Stefan Funk, August 5th 2011, TeVPA

Figure: Gamma-ray flux from various SNRs (Funk, TeVPA 2011)

# Fermi acceleration

## Coupled equations

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Powered by



Cosmic-ray  
transport equation

Hydro equations

Magnetic Turbulence

Magnetic field

Other contributions  
using RATPaC:

[8] Young SNRs in dense  
environments

[88] Spectral softening in  
CC-SNRs

Standard DSA

Non-linear DSA

NDSA + high MF



# Fermi acceleration

## The equations

$$\frac{\partial N}{\partial t} = \underbrace{\nabla D_r \nabla N}_{\text{Diffusion}} - \underbrace{\nabla v N}_{\text{Advection}} - \underbrace{\frac{\partial}{\partial p} \left( N \dot{p} - \frac{v}{3} N p \right)}_{\text{Cooling Acceleration}} + \underbrace{Q}_{\text{Injection}}$$

$$\frac{\partial E_W}{\partial t} = - \underbrace{(v \nabla_r E_W + c \nabla_r v E_W)}_{\text{Advection + Compression}} + \underbrace{k^3 \nabla_k D_k \nabla_k \frac{E_W}{k^3}}_{\text{Cascading}} + \underbrace{2(\Gamma_g - \Gamma_d) E_W}_{\text{Growth + Damping}}$$

$$\frac{\partial}{\partial t} \begin{pmatrix} \rho \\ \mathbf{m} \\ E \end{pmatrix} + \nabla \begin{pmatrix} \rho \mathbf{v} \\ \mathbf{m} \mathbf{v} + P \mathbf{I} \\ (E + P) \mathbf{v} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ L \end{pmatrix} \quad \frac{\rho v^2}{2} + \frac{P}{\gamma - 1} = E$$

**The equations are solved:**

- One dimensional
- Assuming spherical symmetry
- Including Synchrotron cooling for electrons
- On a comoving, expanding grid for turbulence and CRs → no free escape boundary
- Type-Ia,  $B_0 = 5 \mu G$

# Fermi acceleration

## Turbulence setup

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Initial turbulence derived from 1/10<sup>th</sup>  
of the Galactic diffusion coefficient

$$\rightarrow D_r(t = 0) = 10^{28} \left( \frac{pc}{10 GeV} \right)^{1/3} \left( \frac{B_0}{3 \mu G} \right)^{-1/3} cm^2/s$$

Growth rate based on pressure  
gradient of CRs (resonant CR-  
instability x10)

$$\rightarrow \Gamma_r = \mathbf{10} \frac{v_A p^2 v}{3 E_W} \left| \frac{\partial N}{\partial r} \right|$$

Damping as diffusion in  
wavenumber space

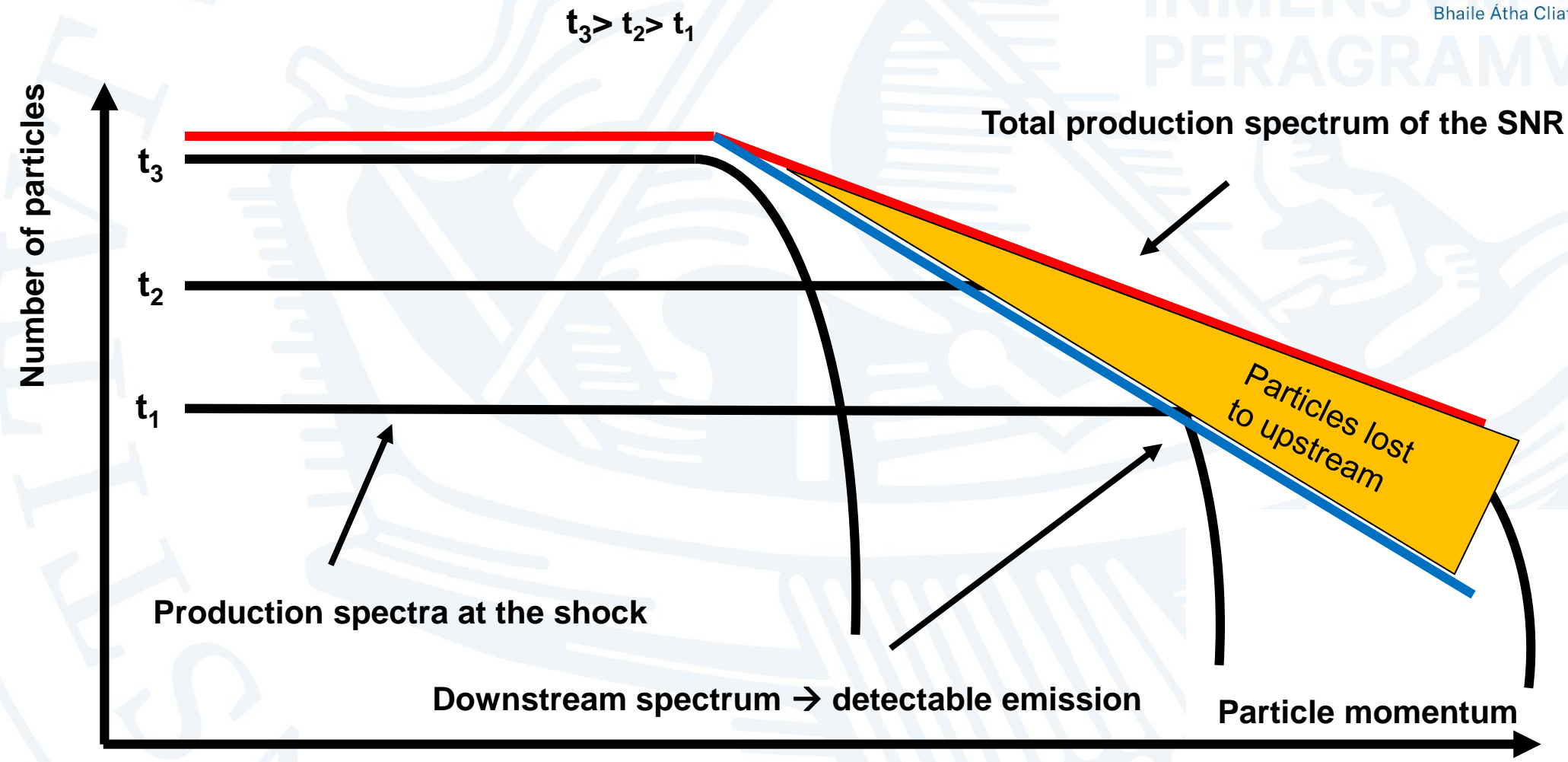
$$\rightarrow D_k = k^3 v_A \sqrt{\frac{E_W}{2 B_0^2}}$$



# Results

# Cosmic-ray escape

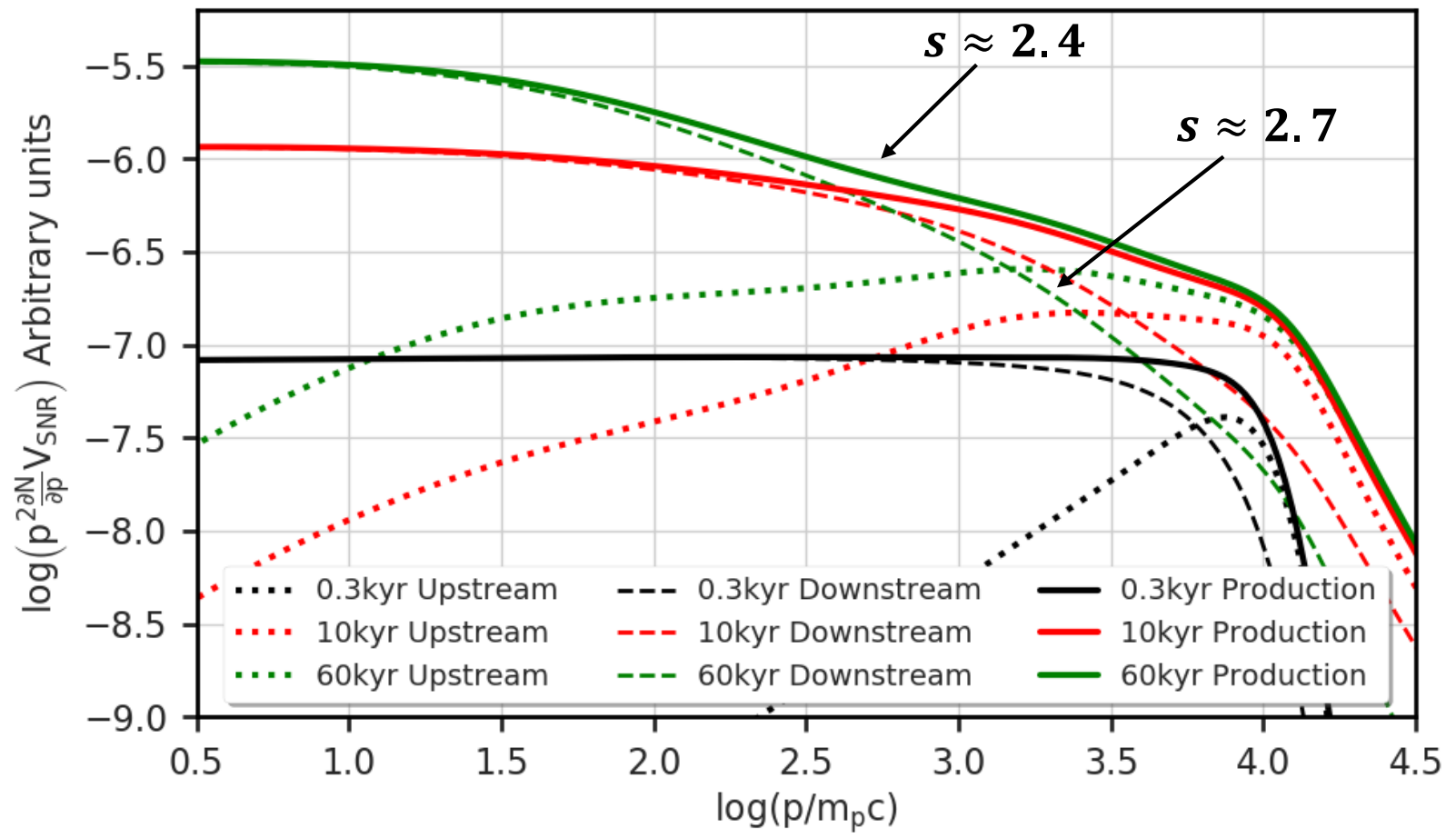
## The mechanism



# Cosmic-ray escape

## Production spectra

- The production spectrum agrees roughly with galactic propagation models
- The downstream spectra are softer than the production spectra
- Particles “escape” from deep downstream to upstream



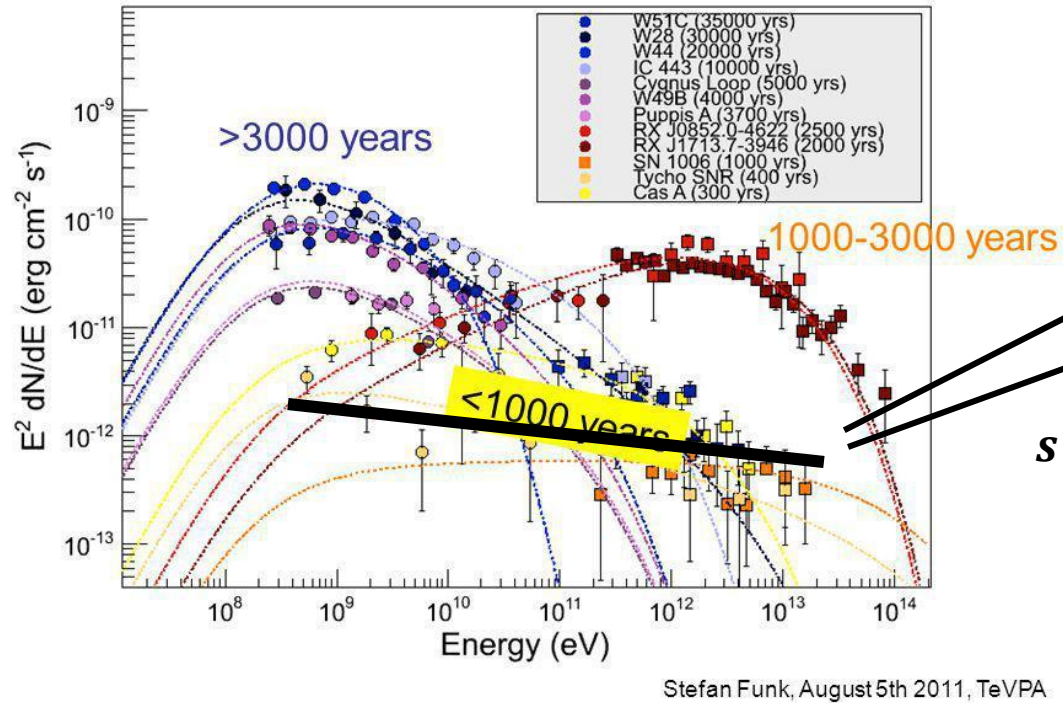
From: A&A, 634 (2020) A59



# Gamma-ray spectra

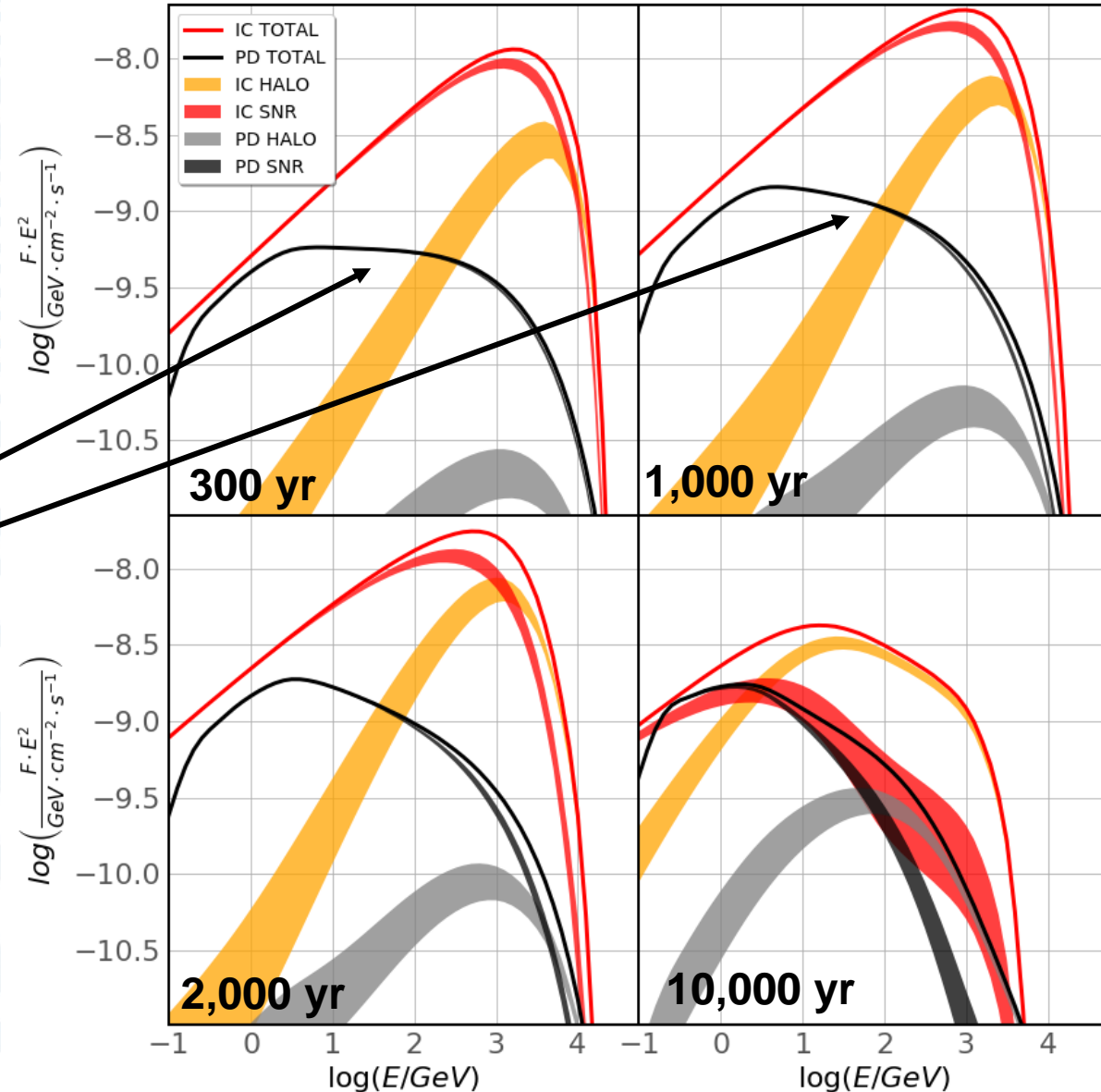
## Spectral evolution: very young SNRs

### Observation:



**Figure: Gamma-ray flux from various SNRs**  
(Funk, TeVPA 2011)

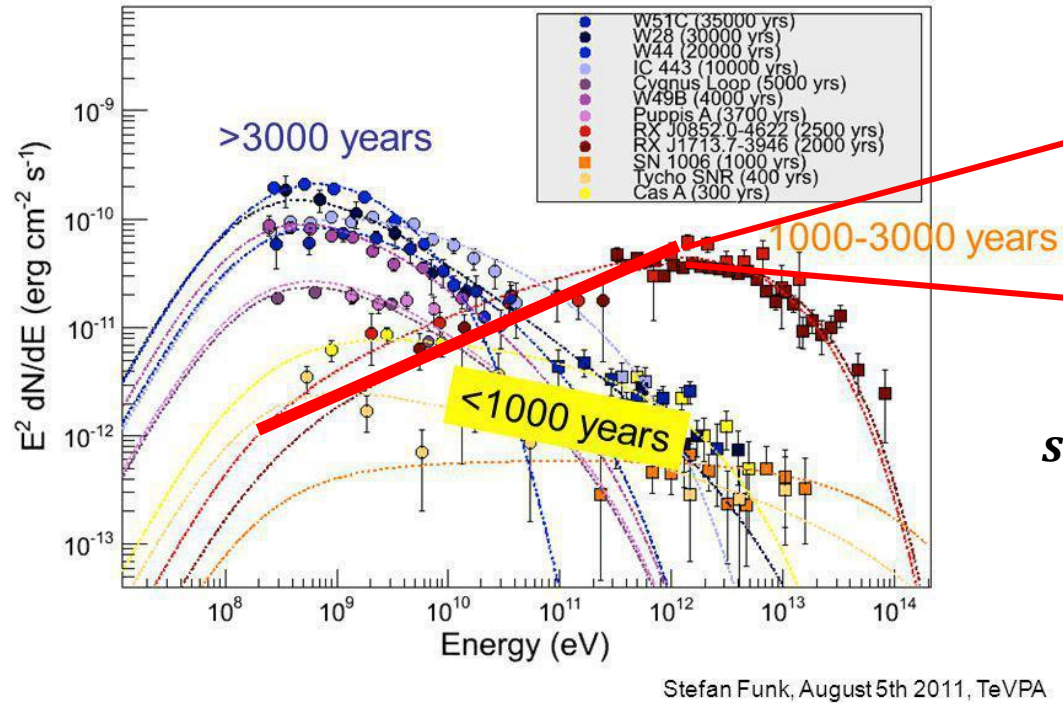
### Model prediction:



# Gamma-ray spectra

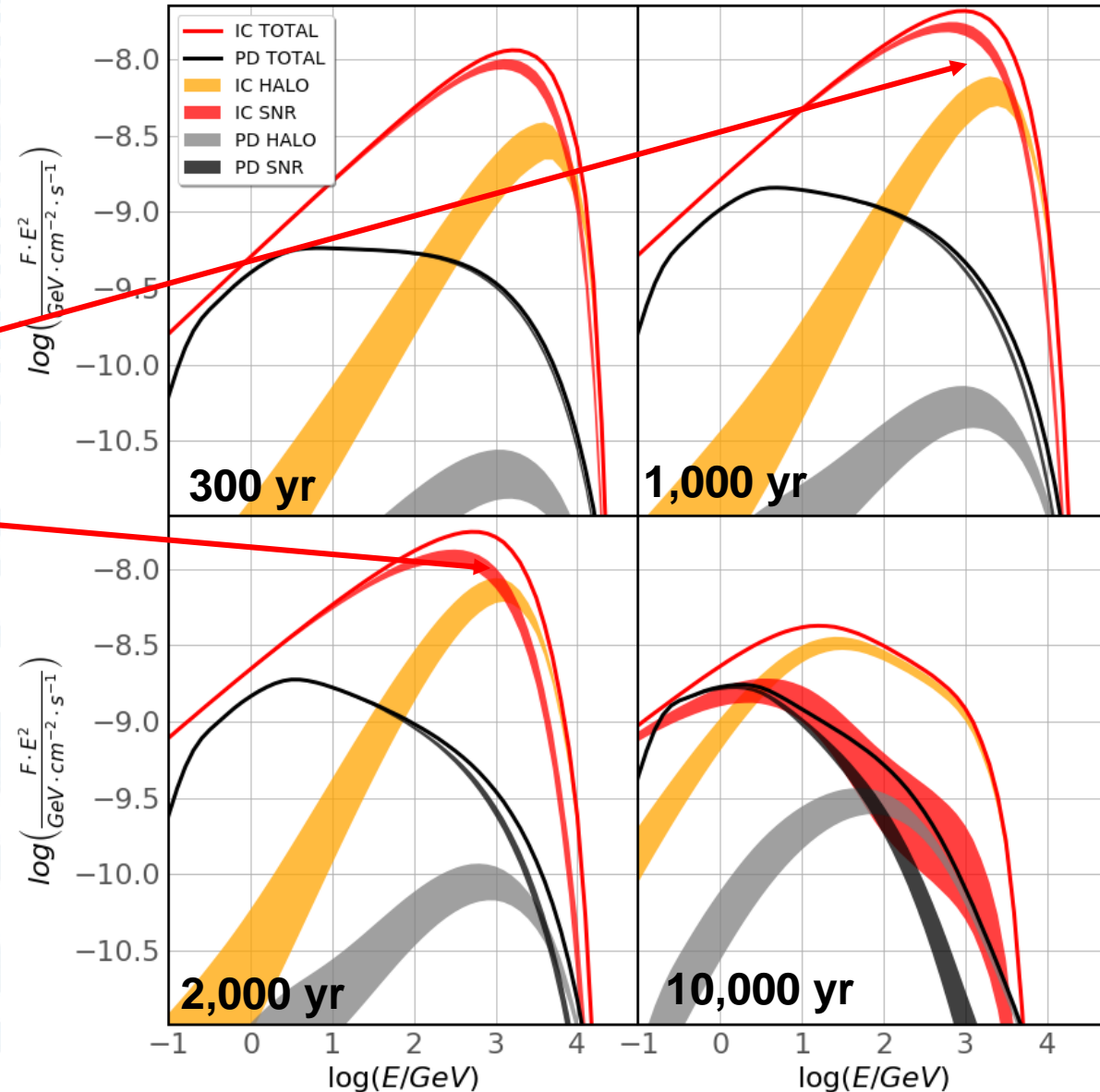
## Spectral evolution: young SNRs

### Observation:



**Figure: Gamma-ray flux from various SNRs**  
(Funk, TeVPA 2011)

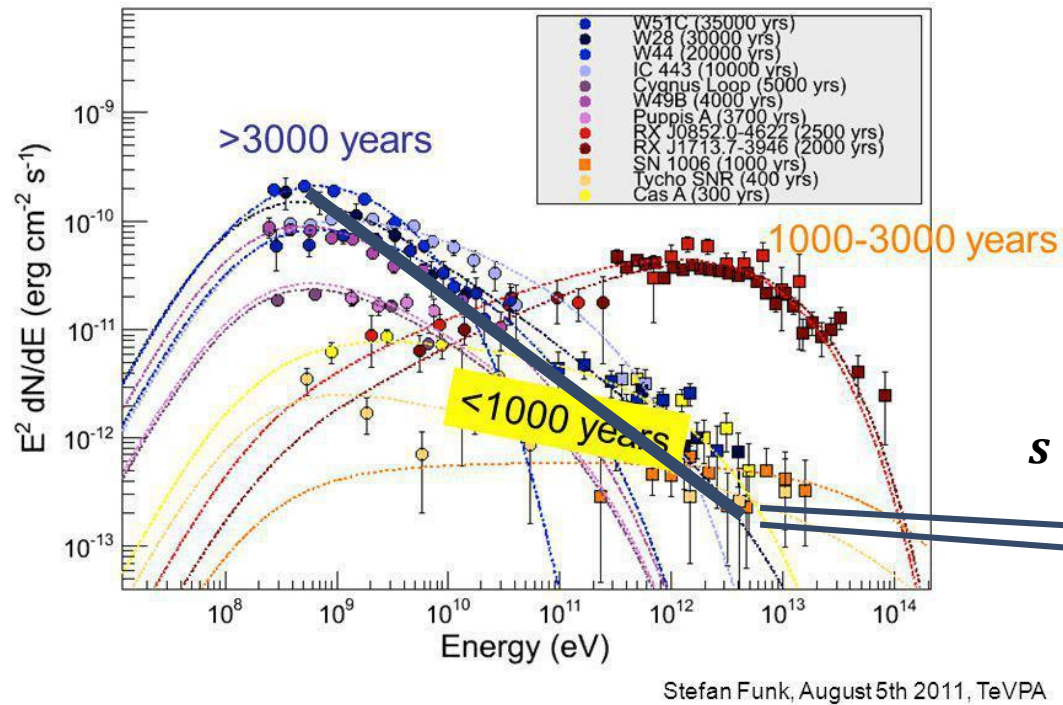
### Model prediction:



# Gamma-ray spectra

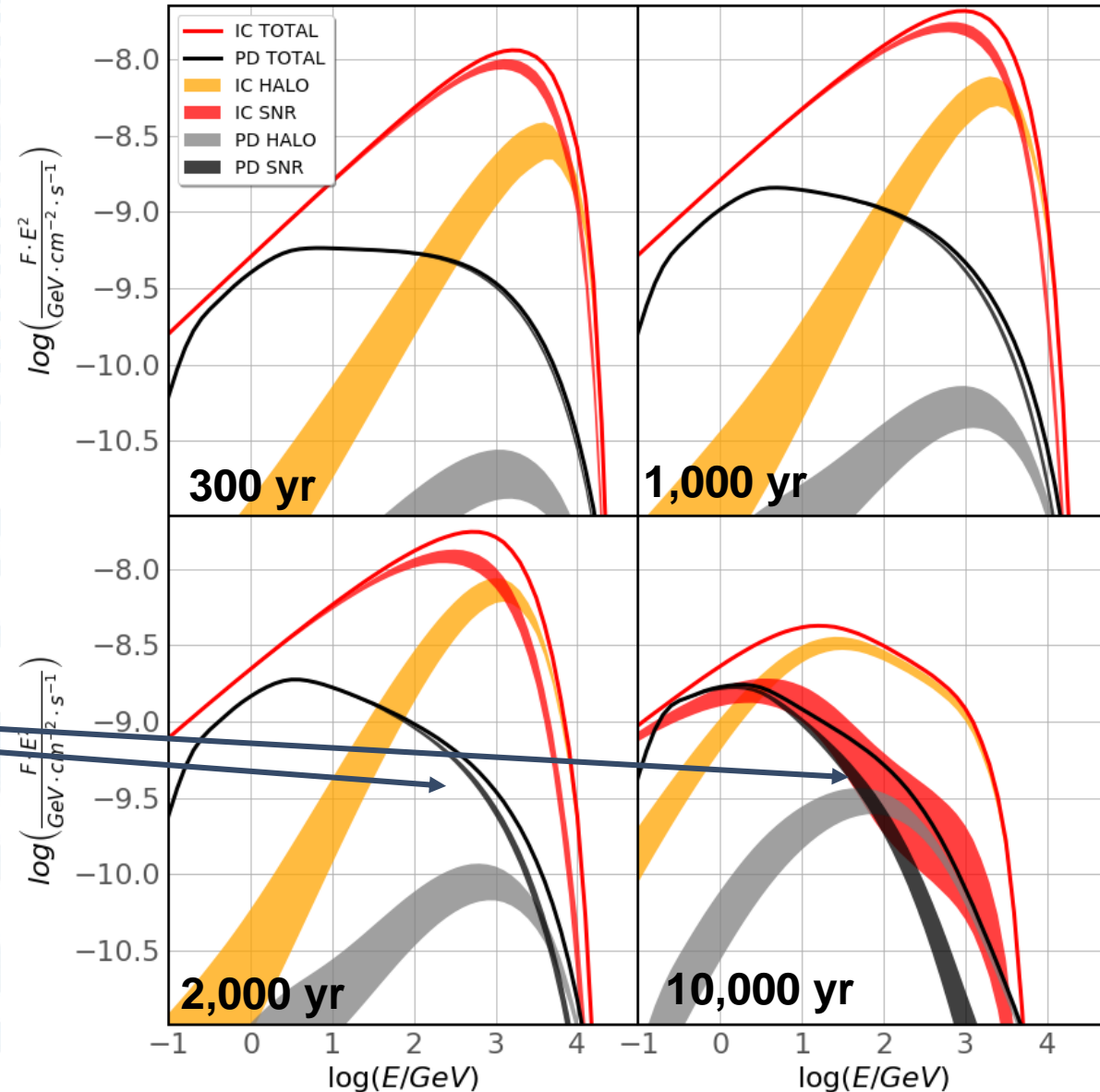
## Spectral evolution: evolved SNRs

### Observation:



**Figure: Gamma-ray flux from various SNRs**  
(Funk, TeVPA 2011)

### Model prediction:



# Gamma-ray morphology

## Emission and spectral index maps

### PD-emission:

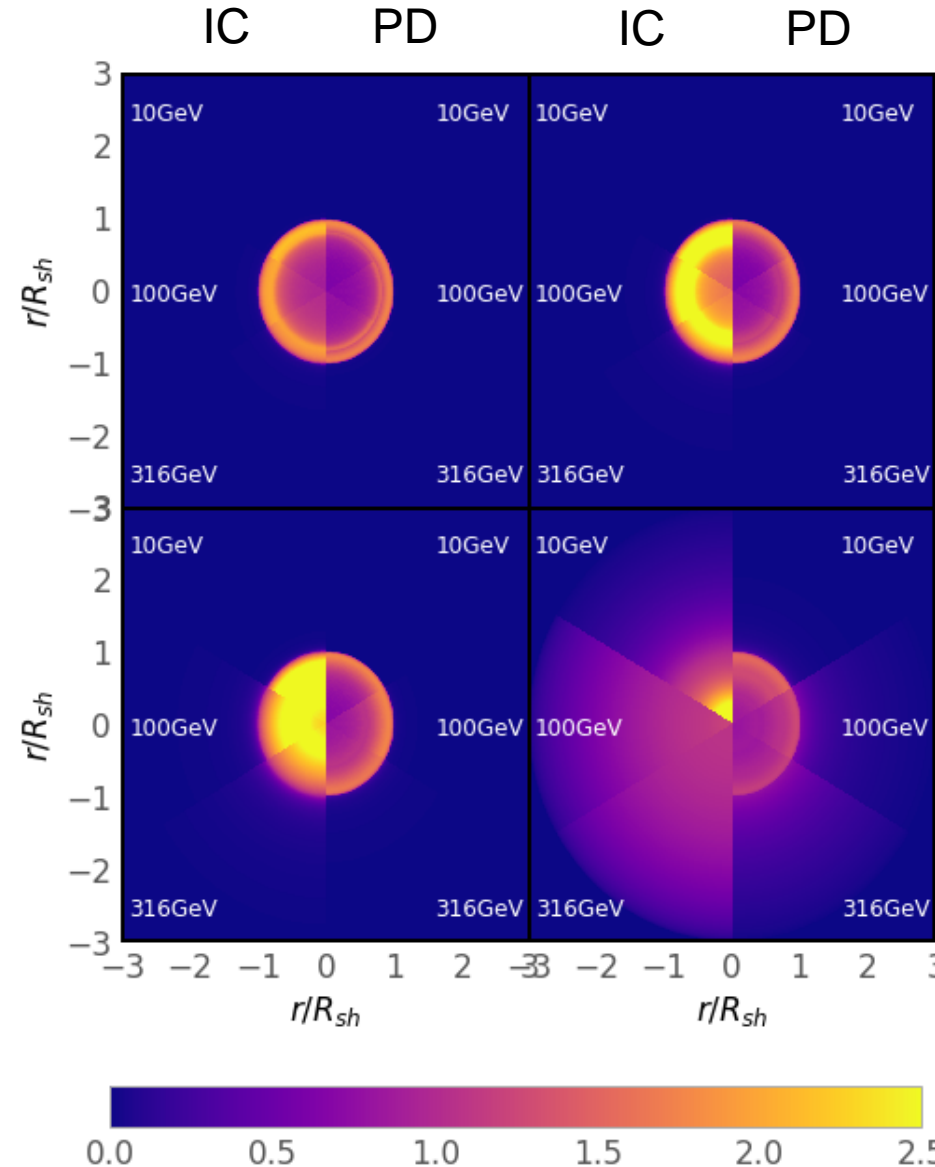
- Shell-like morphology throughout all phases and energies
- Faint halo emission

### IC-emission:

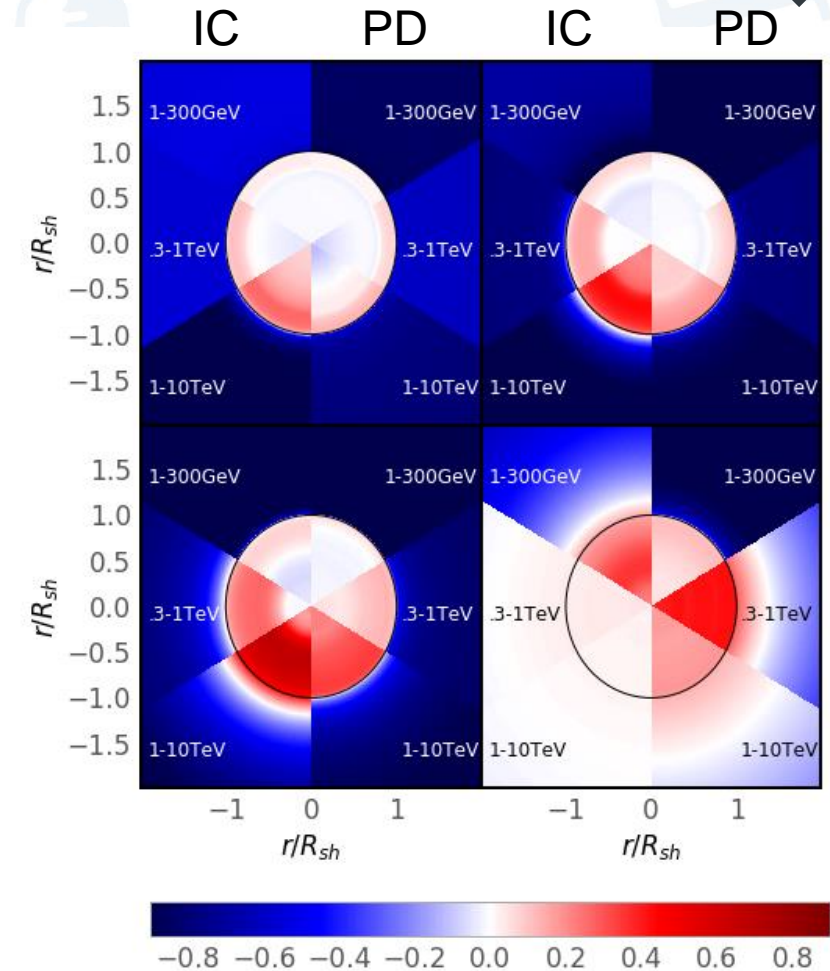
- Initially shell like morphology
- Transition to center-filled morphology
- Halo emission already after 2kyr

### Spectral index distribution:

- No significant deviation from regions of brightest emission



← Emission maps  
Spectral index deviation maps ↓

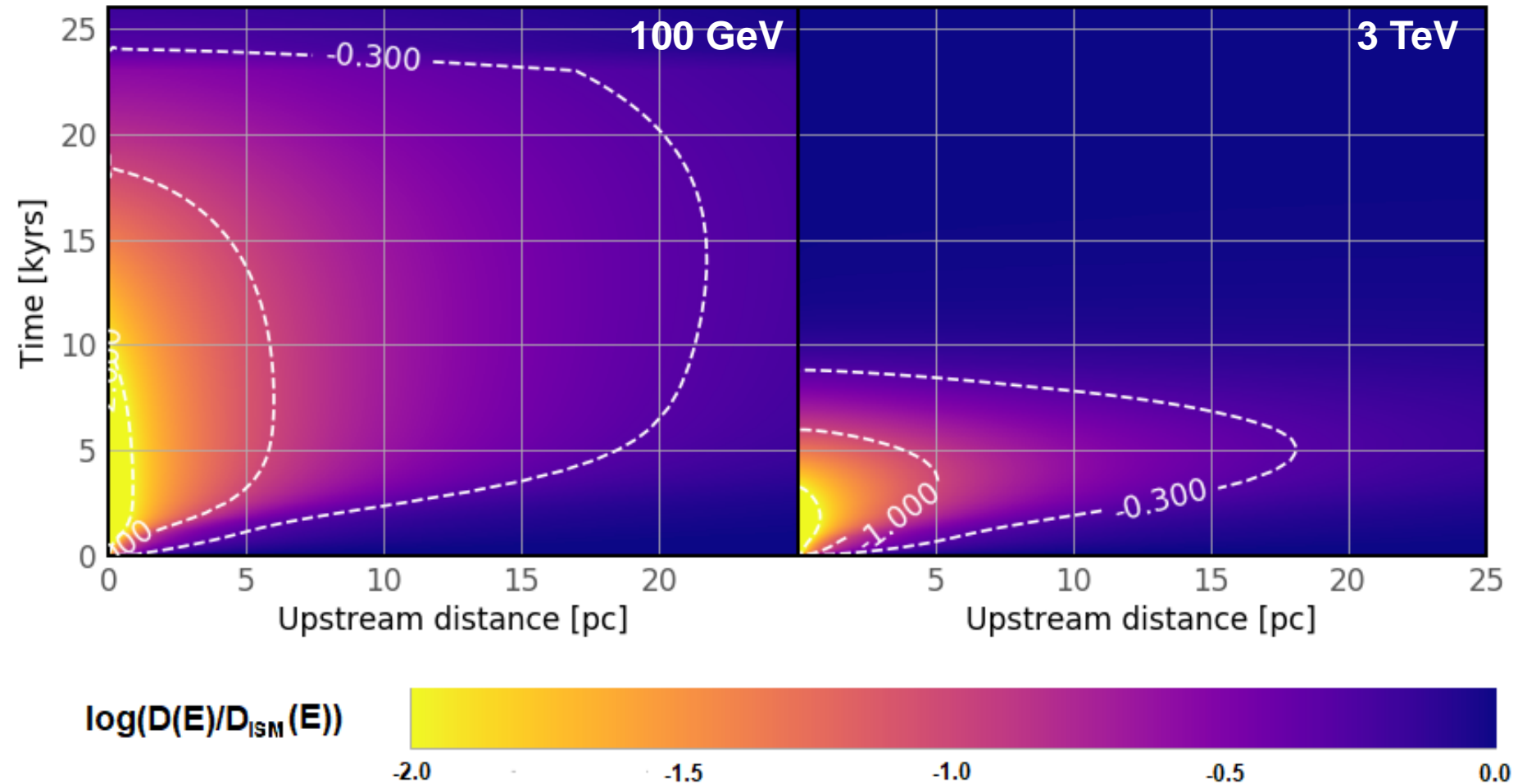


# Halo diffusion coefficient

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- Diffusion coefficient gets reduced up to ~20pc into the upstream
- Rise time similar across energies → down cascading
- Escaping CRs govern diffusion for low-energetic CRs



From: A&A, 654 (2021) A139

# Conclusions

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- A strong evolution of  $E_{\max}$  results in **soft production spectra** even if the acceleration mechanism is standard DSA
- The spectral index of the production spectra is  $s \approx 2.4$  is **close to the predictions by galactic propagation models** ( $s = 2.2 - 2.4$ )
- Particle **escape** of the highest energetic CRs **forms soft spectra at high energies** and spectral breaks between 1-10GeV
- **Reduced diffusion coefficient in the upstream**; strong spatial and temporal evolution
- The gamma-ray morphology depends strongly on the emission mechanism:
  - Persistent **shell-like** structure for **hadronic emission**
  - **Shell-like to center filled** evolution for **leptonic emission**
- Stronger **halo-emission** for the leptonic channel → **potentially detectable** by current-generation IACTs
- No significant spectral-index deviation expected due to projection effects

Thank you for your attention!