

# Differential **Jet** Performance



Pei-Zhu Lai



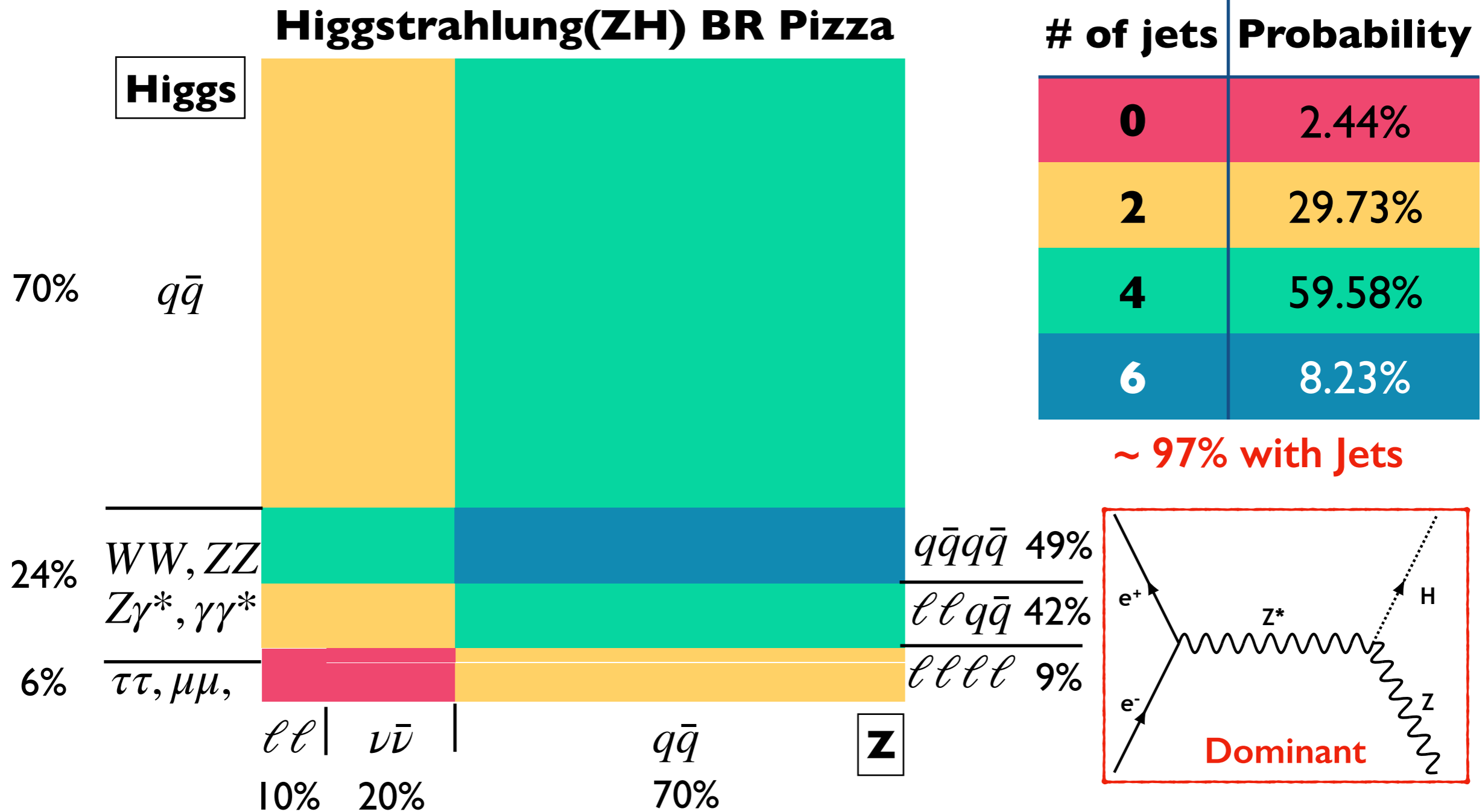
NCU (Taiwan)

On the behalf of the CEPC Collaboration

Online mini-workshop, National Central University (NCU), Chung-li Taiwan

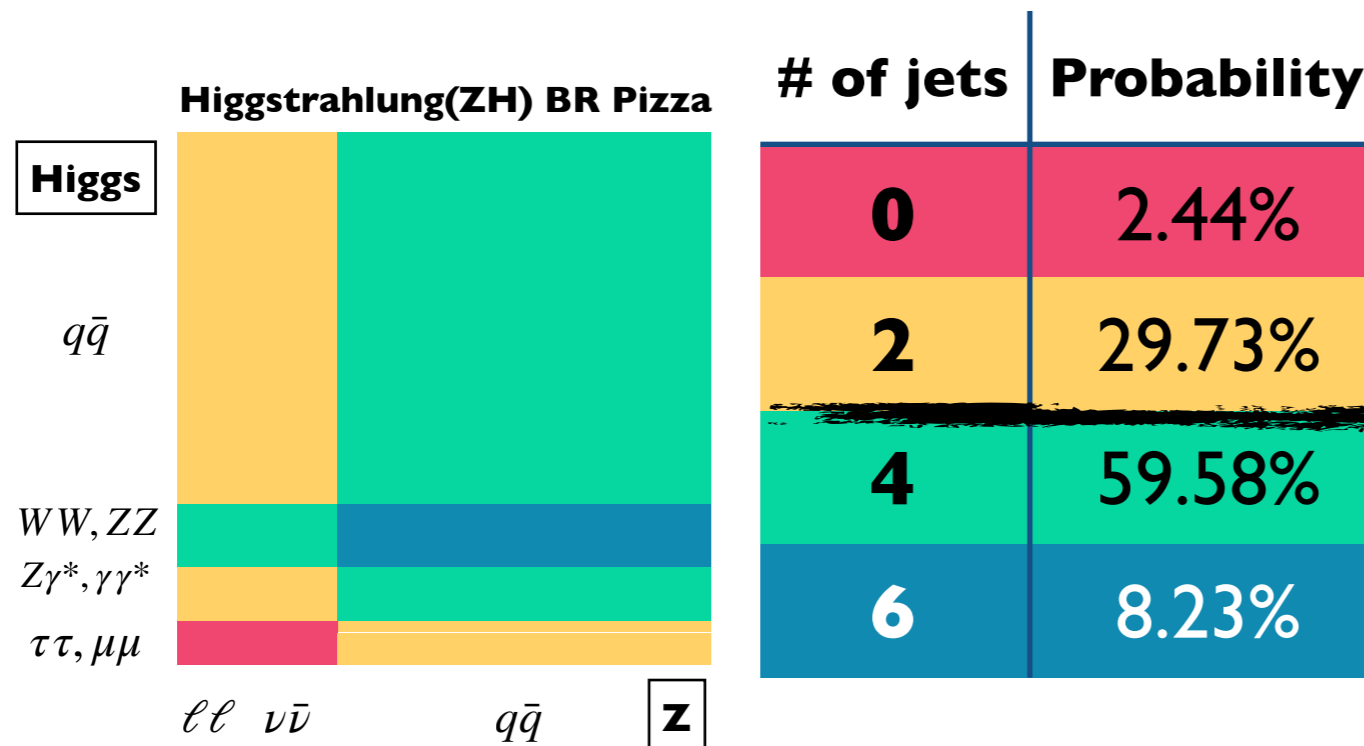
July 23, 2020

# Jets at the Higgs Signal



- Up to **97%** of Higgstrahlung(ZH) final-states are associated to jets.
- Jets are also critical for many EW precision measurements.

# Jets at the Higgs Signal



# of jets	Probability
0	2.44%
2	29.73%
4	59.58%
6	8.23%

**1/3** of ZH events

- Major SM Higgs decay mode.
- One color singlet could be identified. (Z or Higgs boson)

**2/3** of ZH events

- $ZH \rightarrow q\bar{q}q\bar{q}$  is dominant.
- Wrong jet pairing is a major uncertainty.

**(Potential huge impact)**

■ **2/3** of ZH events need dedicated **color-singlet identification** (Z, W, H,  $\gamma^*$ ) → Via jet **clustering** and **pairing**.

■ **Jet clustering** is also essential for differential & EW precision measurements (e.g. TGCs).

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invariant mass resolutions

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BM2: Jet energy and angular  
differential response

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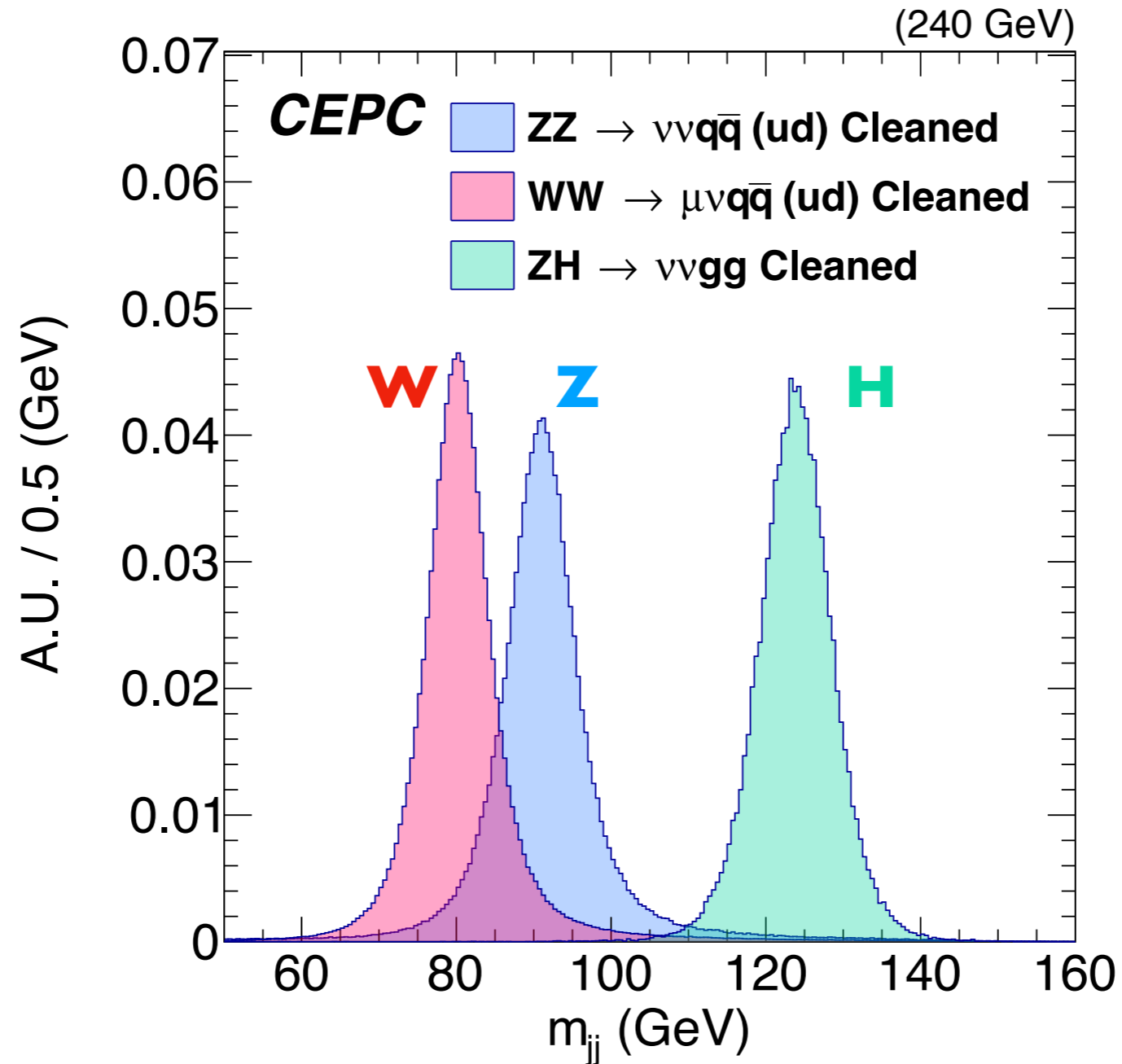
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# BMI: Massive Boson Mass Resolution



- W-, Z-, and Higgs-boson dijet masses are **well separated** at CEPC.
- Z- and W-boson could be separated  $\approx 2\sigma$ .
- **Higgs Boson Mass Resolution = 3.8%** is reached the CEPC baseline.

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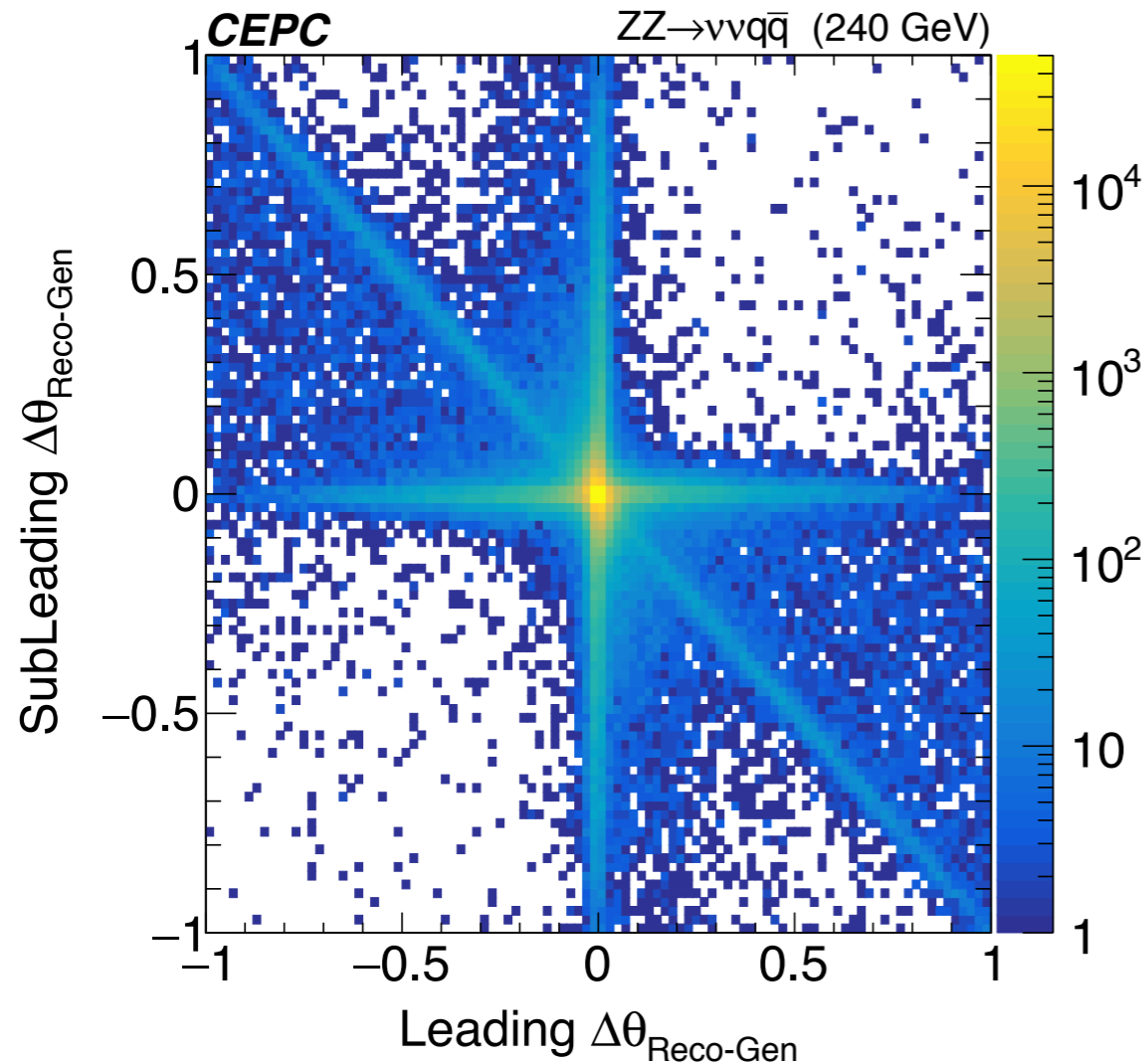
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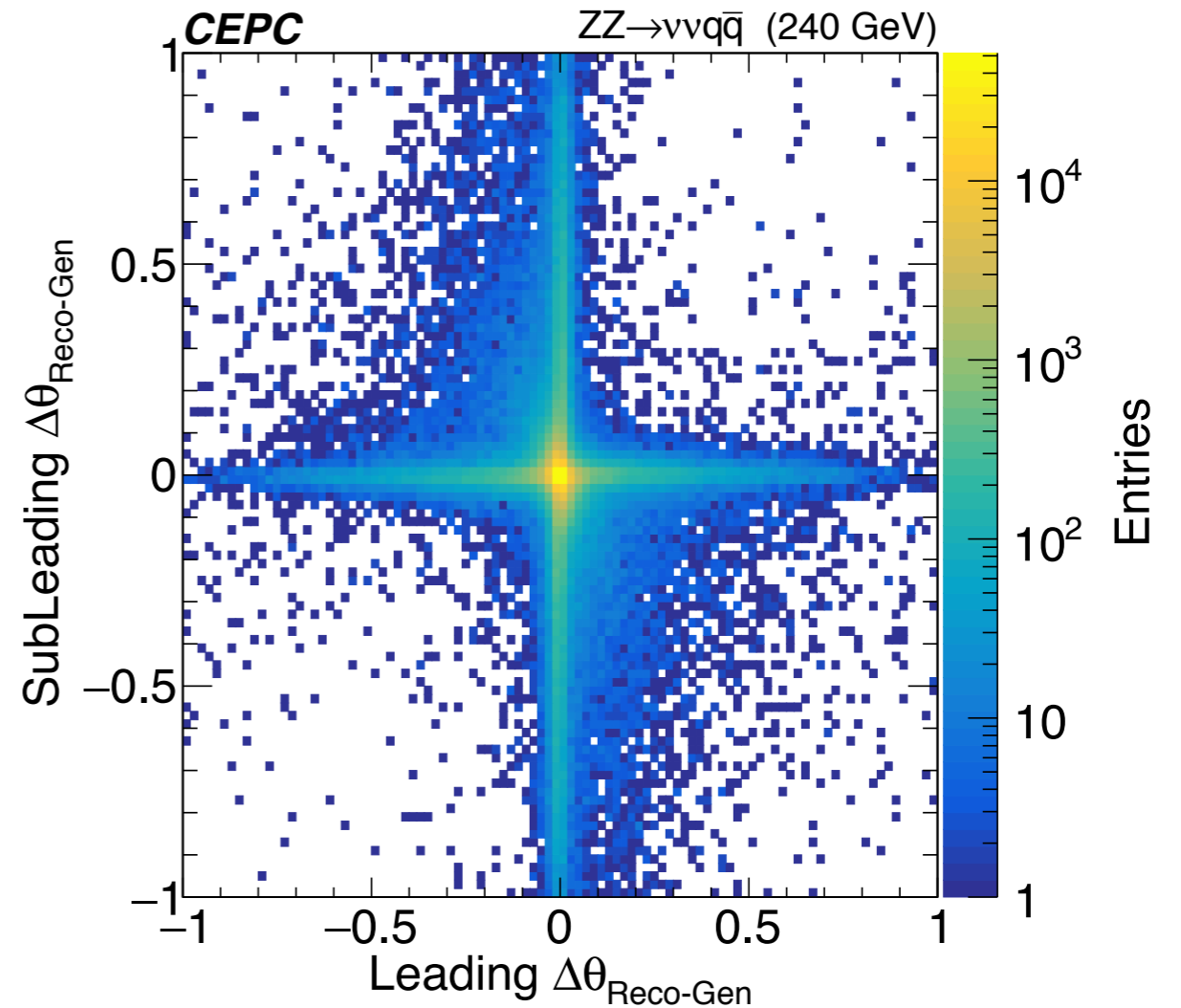
BM2: Jet energy and angular differential response

# Matching RecoJet & GenJet

Poor Matching



Good Matching

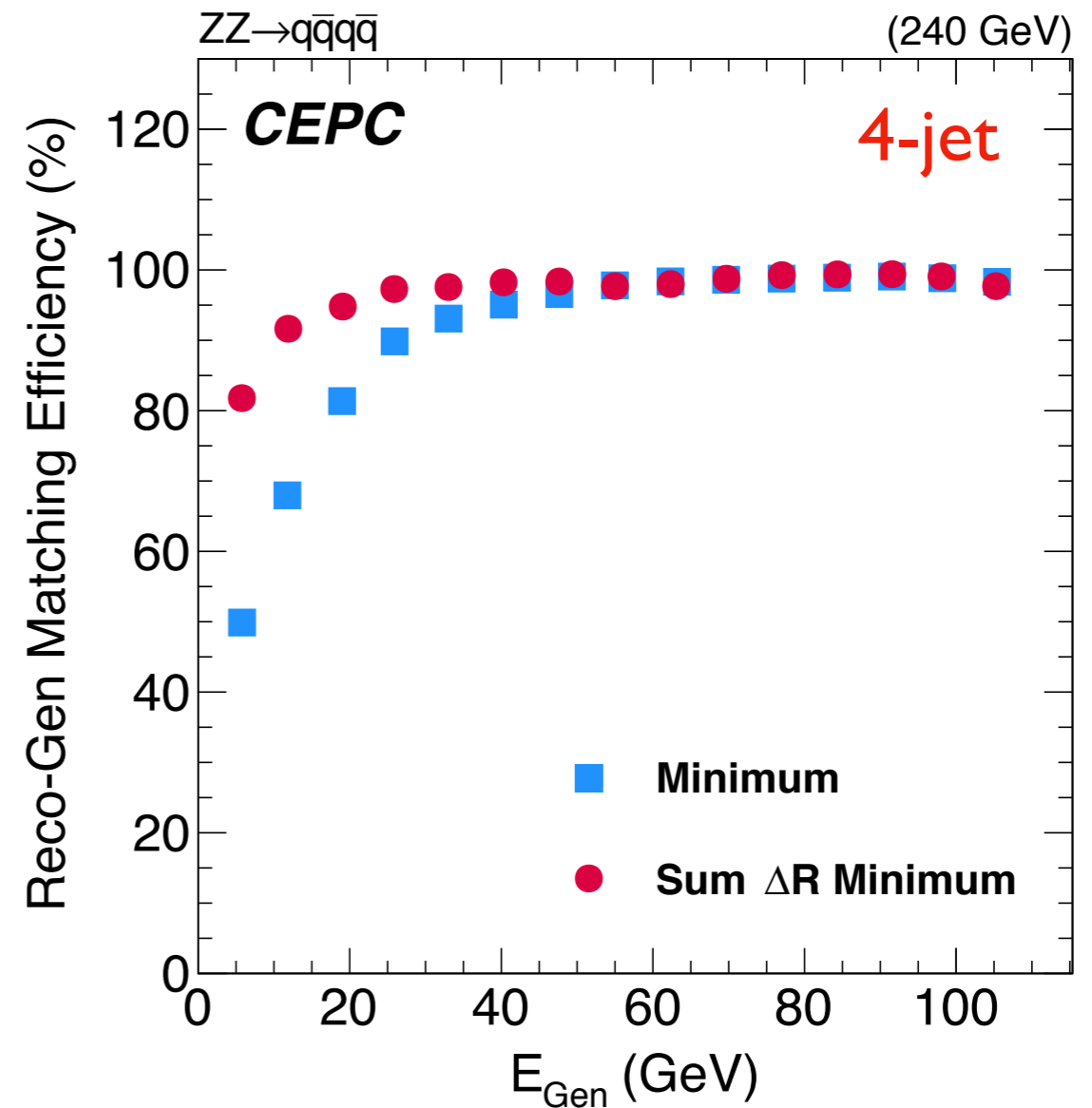
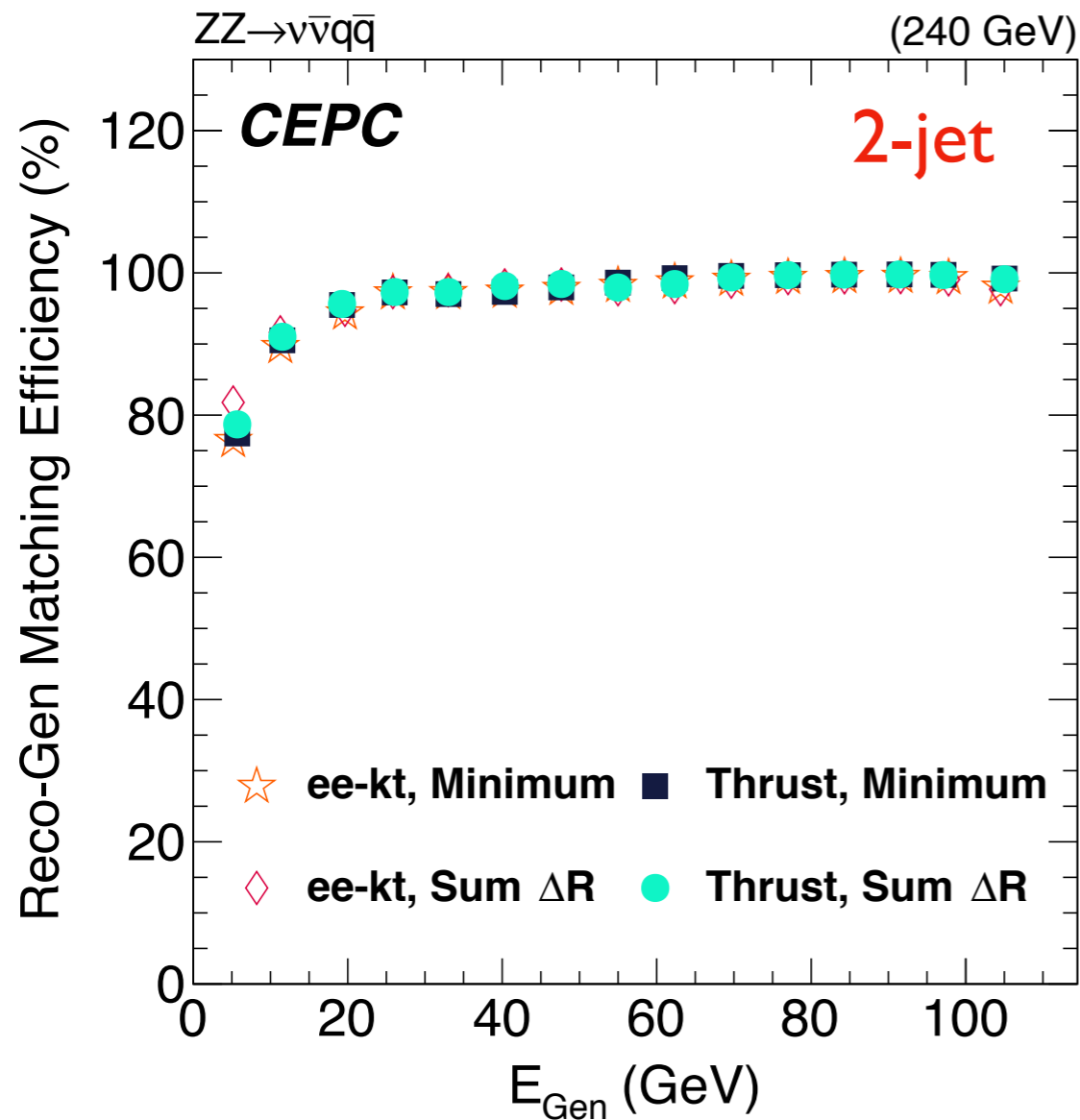


■ Two matching methods are studied:

- I. Matching energetic RecoJet to minimum  $\Delta R$  GenJet.
- II. Minimum combination  $\Delta R$  ( $= \sqrt{\Delta\theta^2 + \Delta\phi^2}$ ) of RecoJet and GenJet. (Adopted)

$$\text{Matching Efficiency} \equiv \frac{N_{\Delta R < 0.4}}{N}$$

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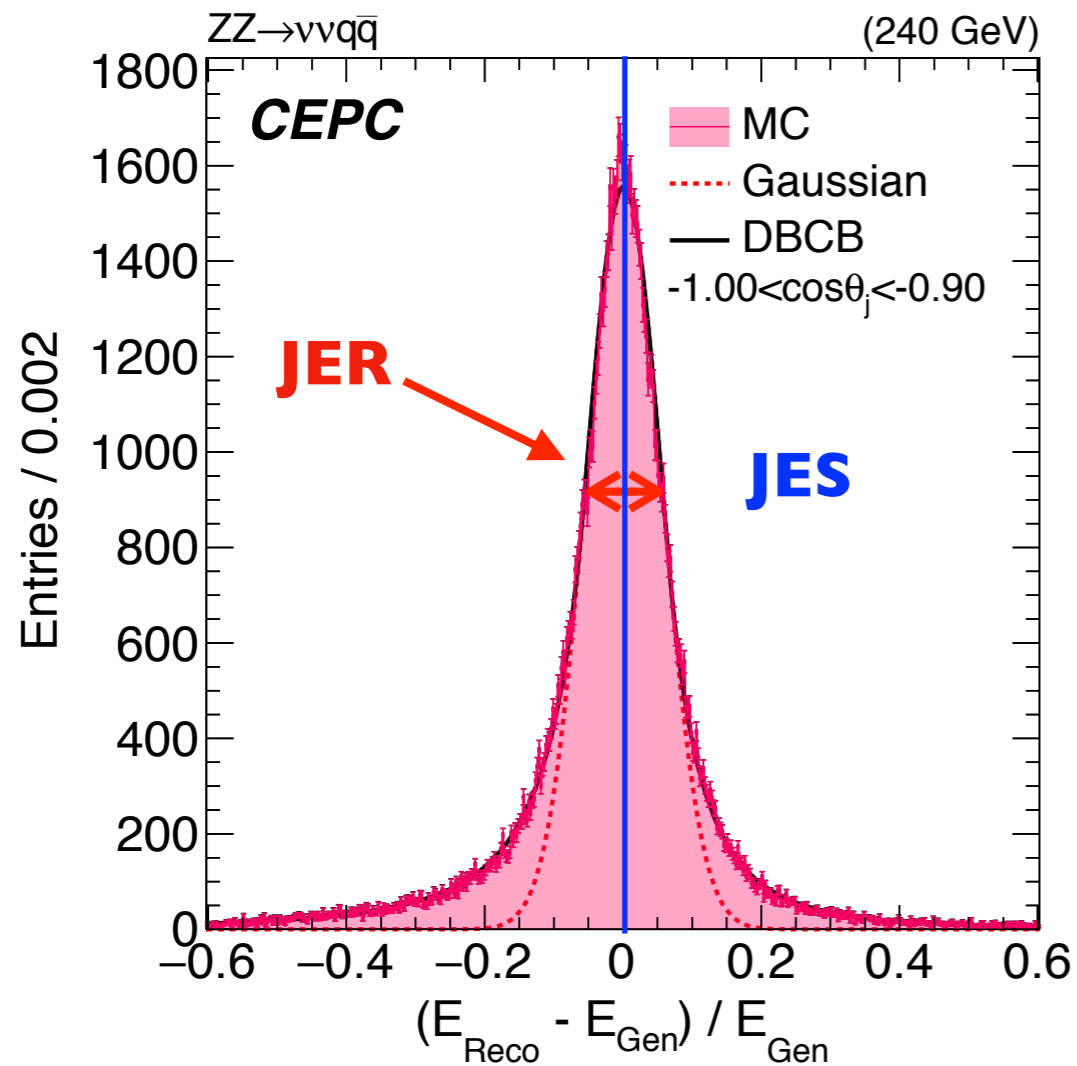
$$\text{Matching Efficiency} \equiv \frac{N_{\Delta R < 0.4}}{N}$$

# Quantify the Performance

- Double-sided crystal ball (DBCBCB) function is used to extract energy resolution/scale; Gaussian is used to extracted angular ( $\theta$ ,  $\phi$ ) resolution/scale.

Jet Energy Resolution (JER)

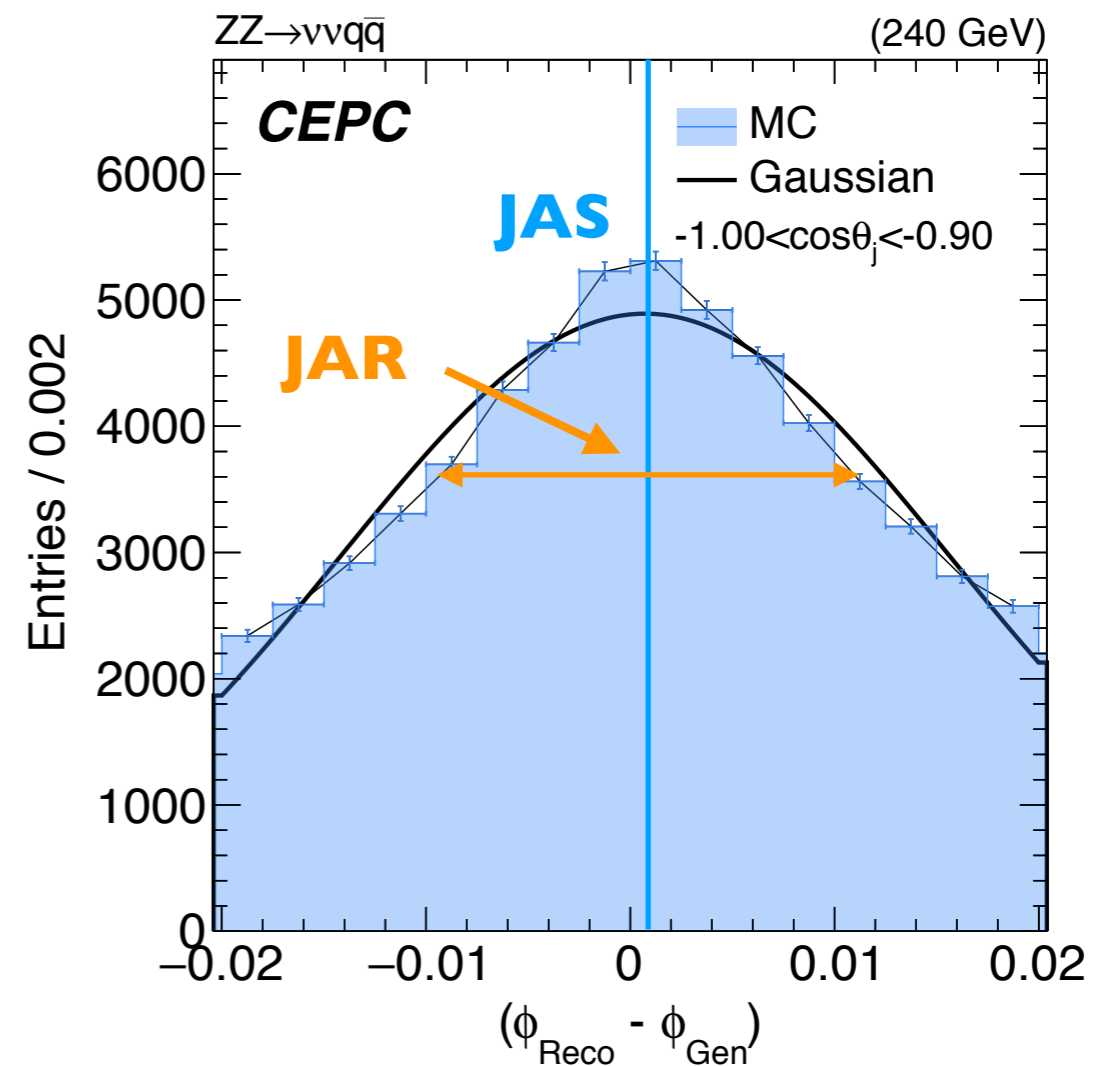
Jet Energy Scale (JES)



Energy Relative Difference : 
$$\frac{E_{RecoJet} - E_{GenJet}}{E_{GenJet}}$$

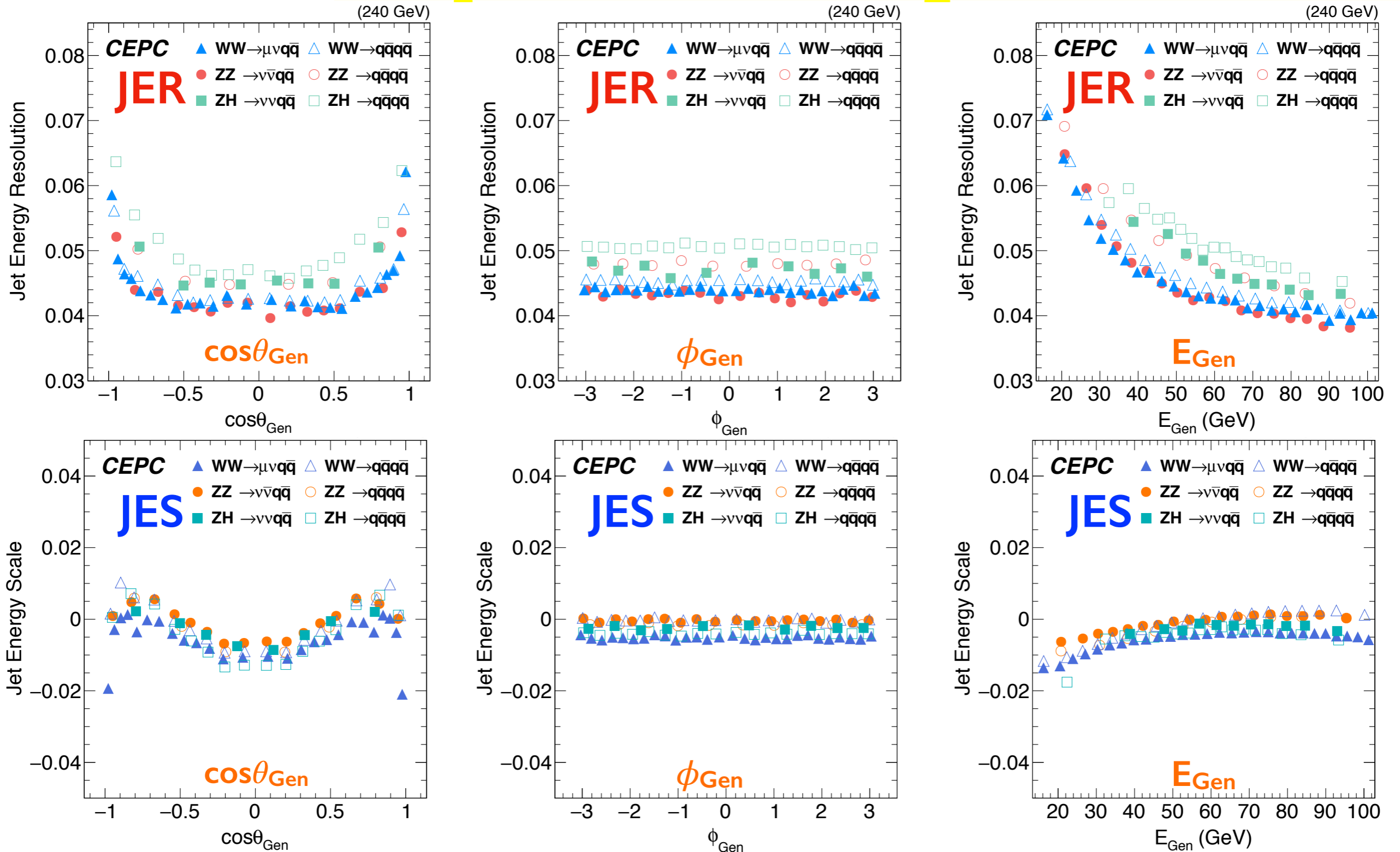
Jet Angular Resolution (JAR)

Jet Angular Scale (JAS)



Angular Difference : 
$$\phi_{RecoJet} - \phi_{GenJet}$$

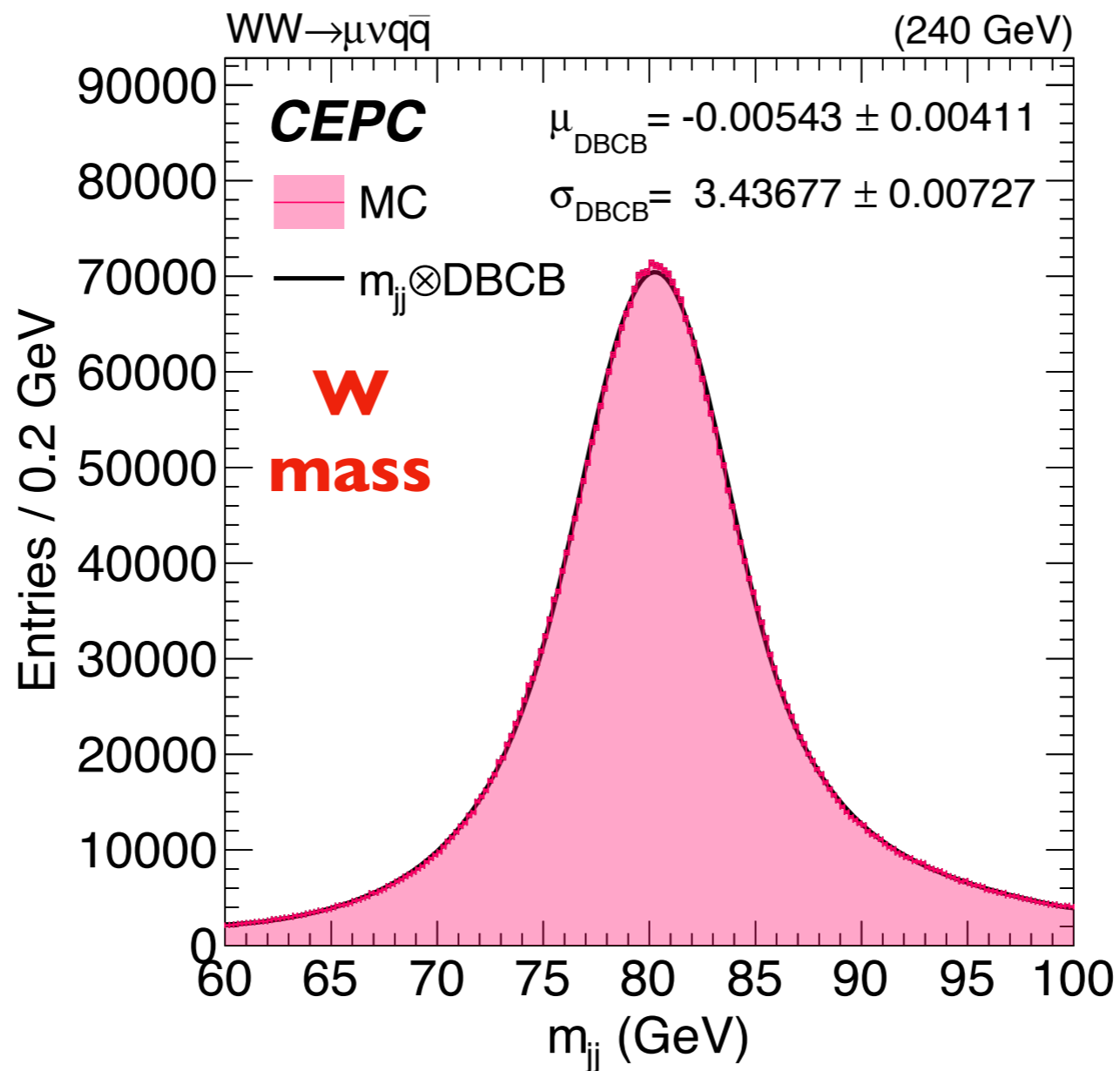
# BM3: JER & JES (Reco-Gen)



■ JER is around **4.5%** in barrel region; JES is around **1%**.

■ The difference between 2 and 4 jets final-state is controlled within **1%** level.

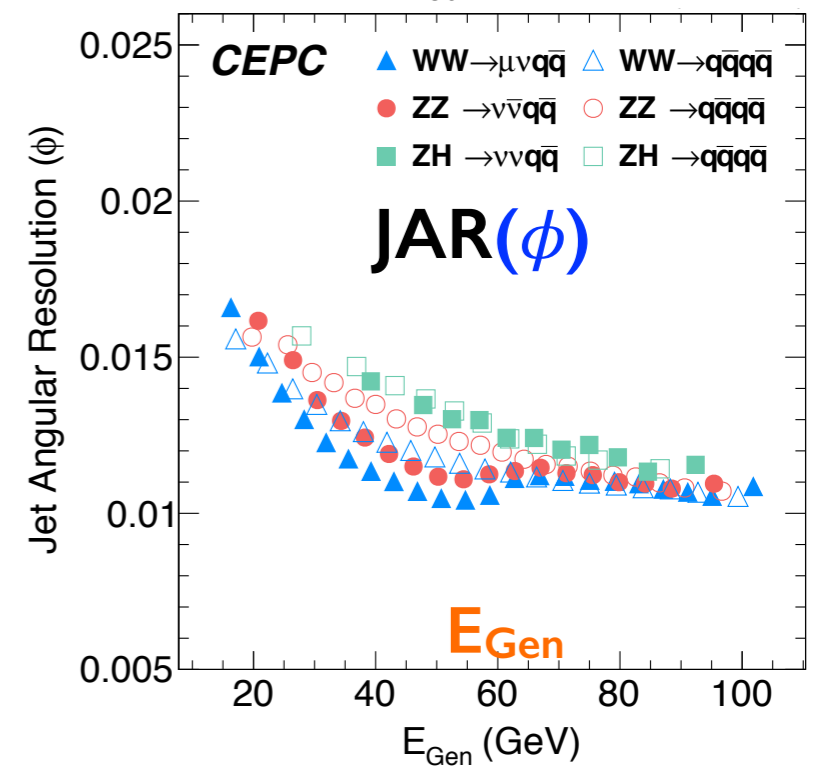
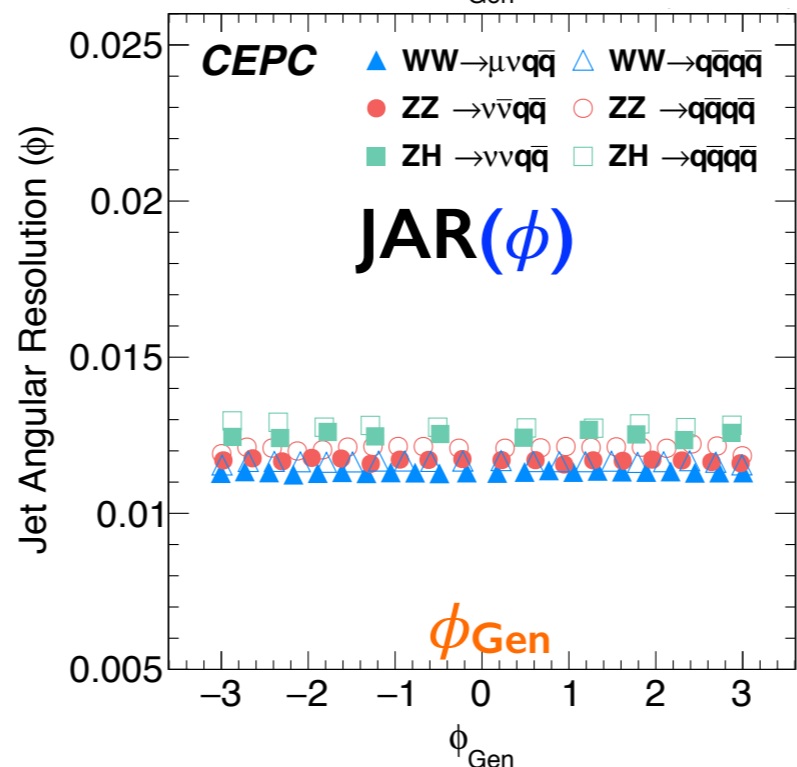
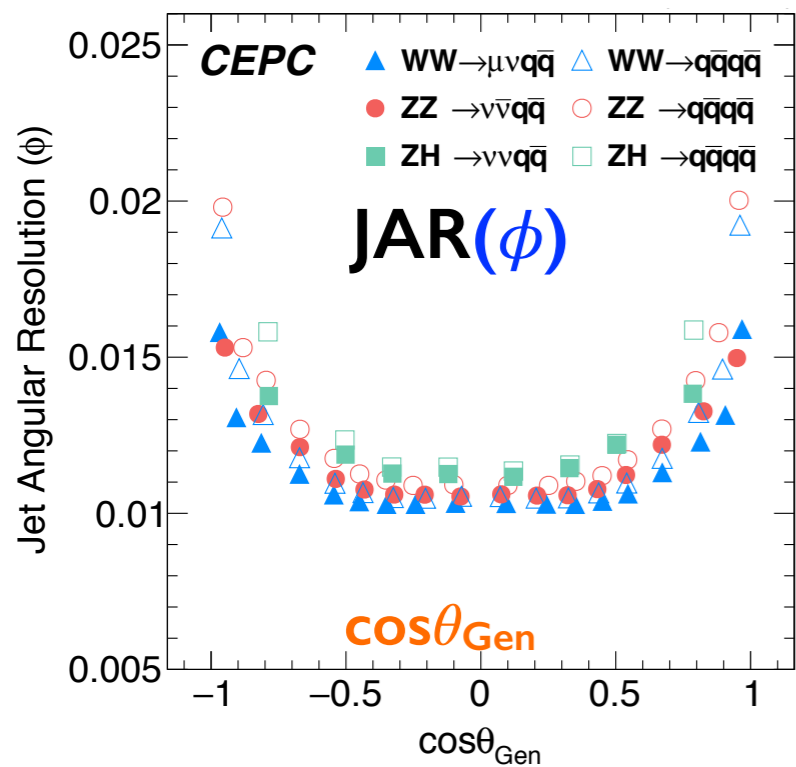
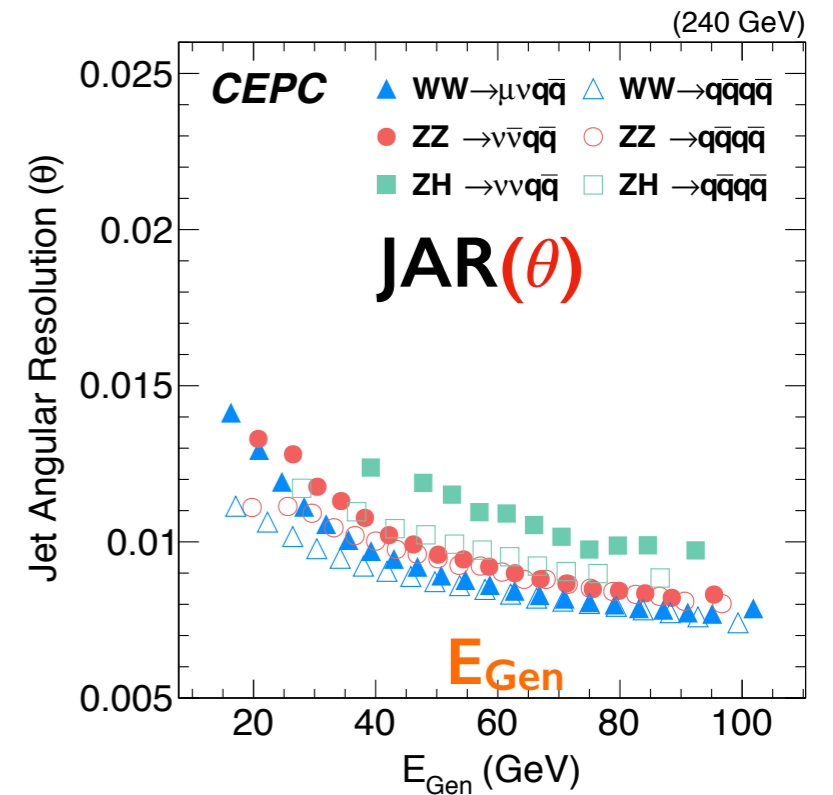
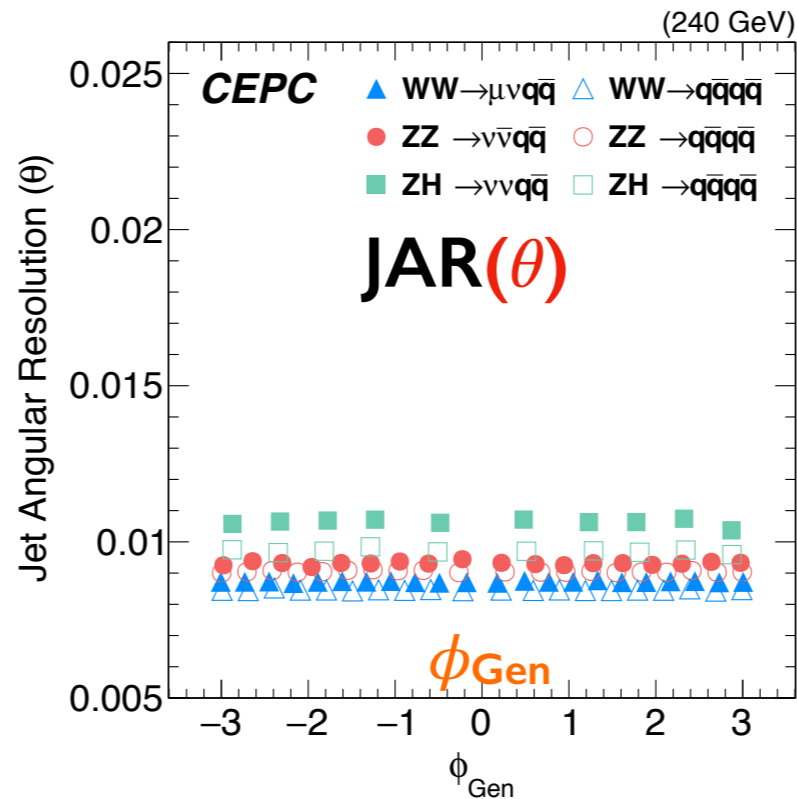
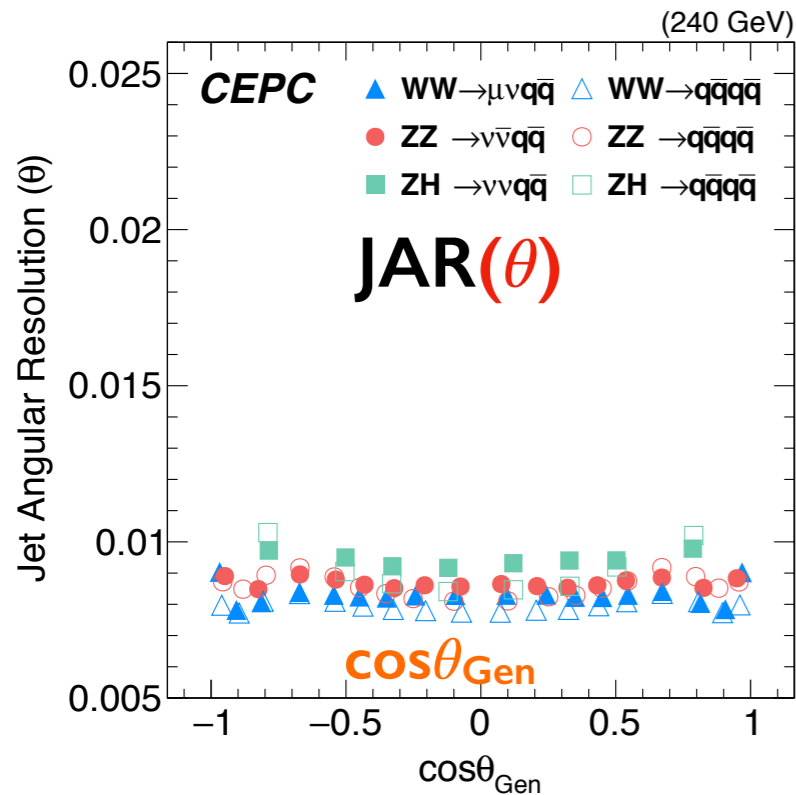
# BM3: JES Calibration



**Challenge  
but  
Important!**

- Multi-differential JES calibration ( $\cos\theta$ , energy, flavor tagging).
- Preliminary W-boson mass uncertainty already at **very small level**.
- Further control the systematic using differential information?

# BM3: JAR (Reco-Gen)

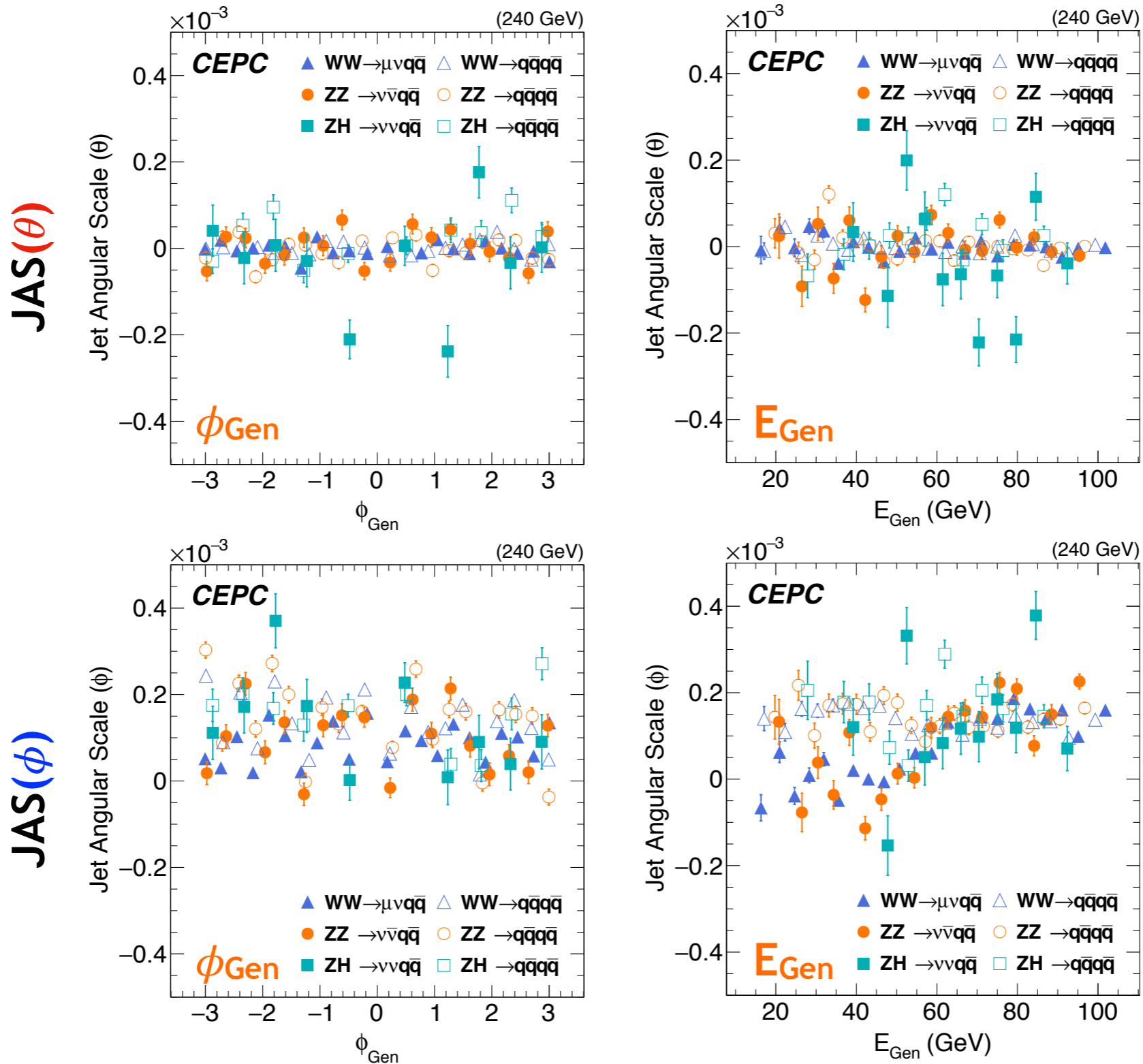


■ JAR is around 1% in barrel region; JAS is **independent** of  $\phi$ .

■ The difference between 2 and 4 jets final-state is controlled within 1% level.

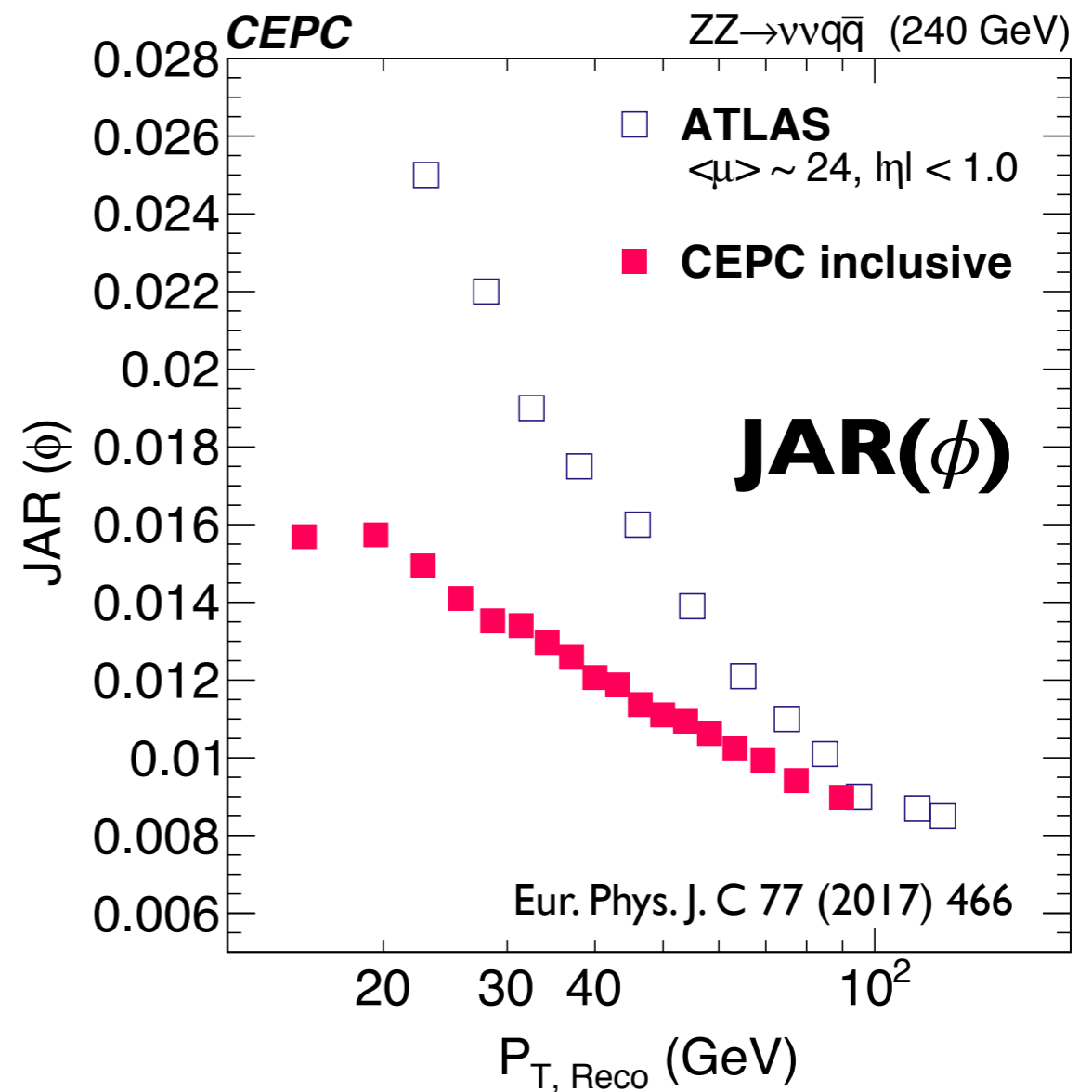
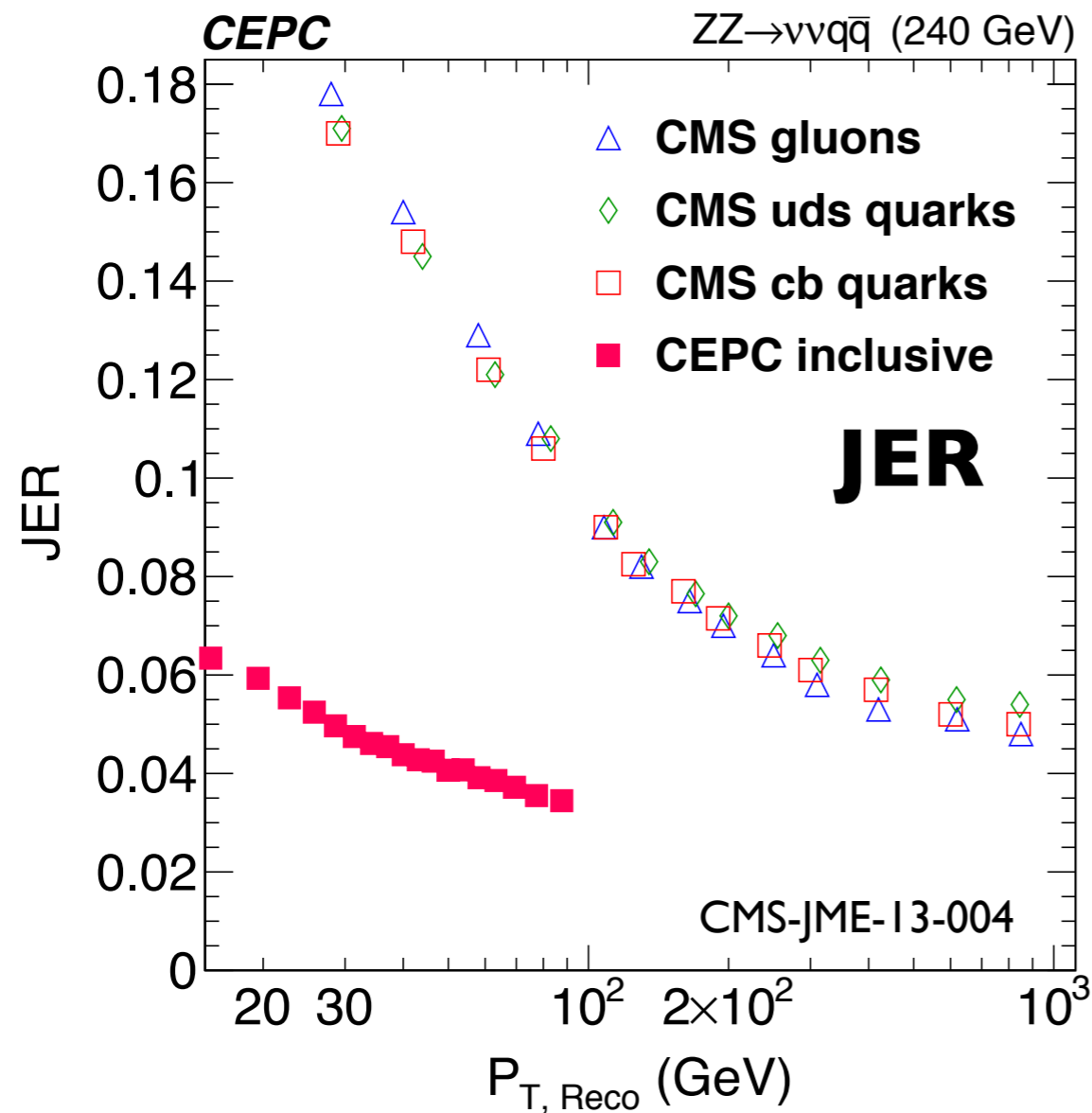


# BM3: JAS (Reco-Gen)



- JAS( $\theta$ ) is controlled to be near **0.02%** and JAS( $\phi$ ) is around **0.04%**.
- RMS of JAS( $\theta$ ) and JAS( $\phi$ ) is around  **$10^{-5}$** .

# Compare to CMS & ATLAS at LHC



■ **JER** at CEPC is better than **CMS** as it should be; **3-4 times** better in the same  $p_T$  region.

■ **JAR( $\phi$ )** at CEPC is better than **ATLAS** as it should be; **1.0-1.6 times** better in the same  $p_T$  region.

■ Free from: QCD Background, Underlying Event, Pile Up.

■ Benefit from: PFA (Arbor), Fine-segments of Calorimeter

# Physical Benchmarks

# of jets	Probability
0	2.44%
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BM3: # of jet identification & thrust based algorithm

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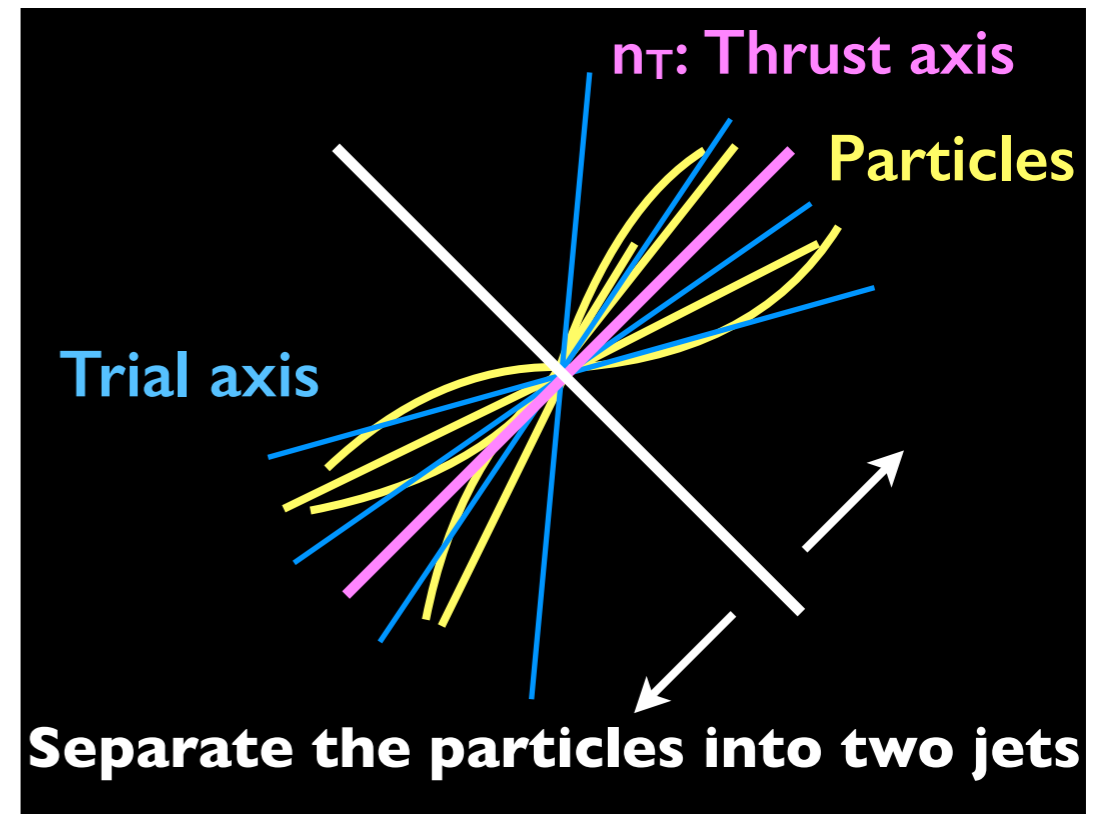
- 2/3 of ZH events need dedicated **color-singlet identification** (Z, W, H,  $\gamma^*$ ) → Via jet **clustering** and **pairing**.
- **Jet clustering** is also essential for differential & EW precision measurements (e.g. TGCs).

# BM2: Thrust Jet Clustering Method

$$T \equiv \max \frac{\sum_j^N |P_j \cdot n_T|}{\sum_i^N |P_i|}$$

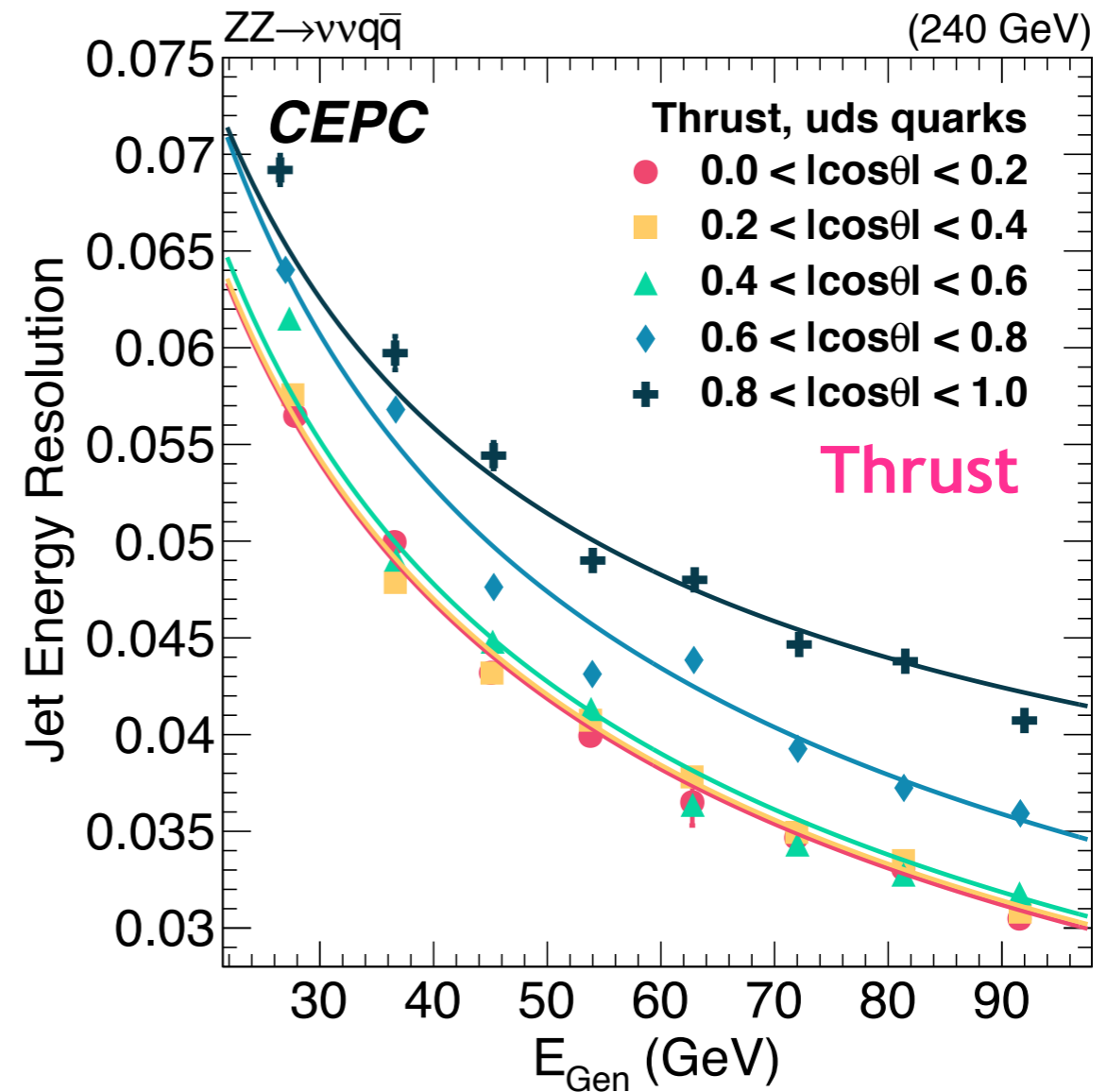
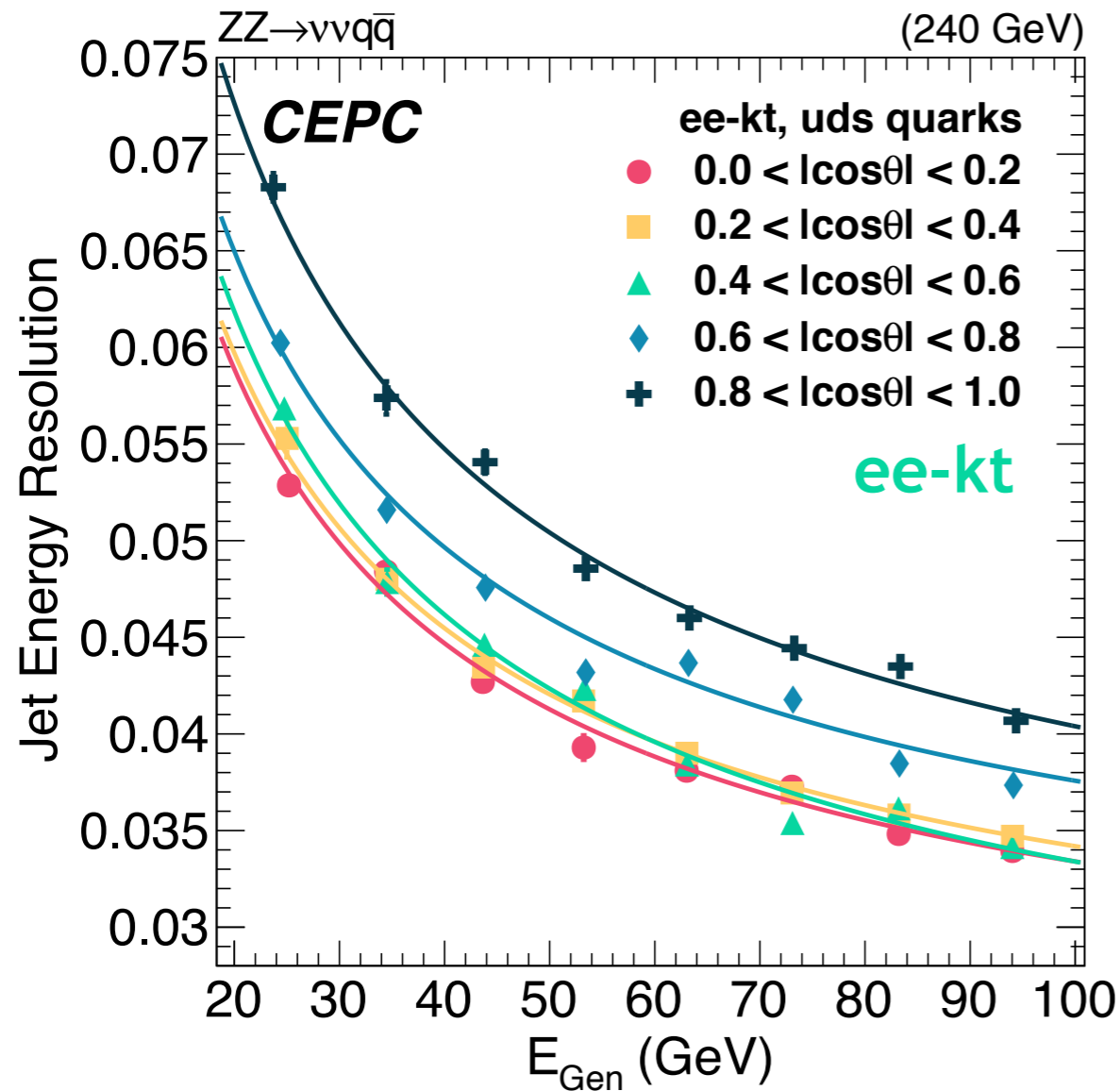
$P_i$  or  $P_j$ : Momentum of each particle

$n_T$ : A unit vector (  $\sin\theta \times \cos\phi$ ,  $\sin\theta \times \sin\phi$ ,  $\cos\theta$  )



- Thrust is one kind of event-shape variable.
- The nature of the clustering idea for the **single boson to 2-jet events**.
  1. Boosting the system back to the rest frame.
  2. Find out a vector in the  $\theta$  and  $\phi$  phase space with highest momentum flux.
  3. Divide the system into 2 hemispheres with the thrust axis, and each identified as a jet. (Only applicable to **2 jets event**)

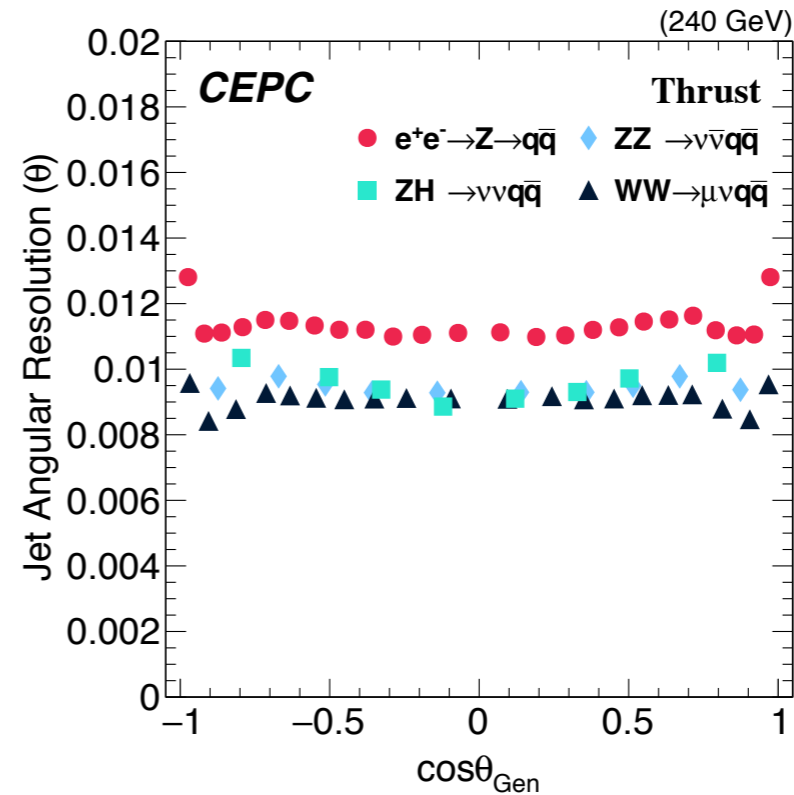
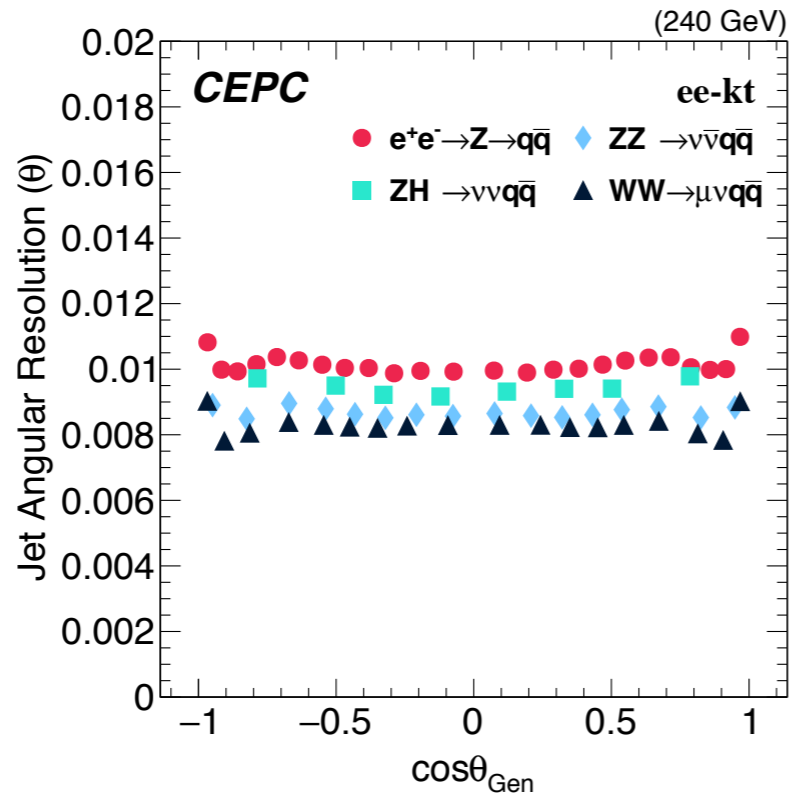
# BM3: JER (ee-kt—Thrust)



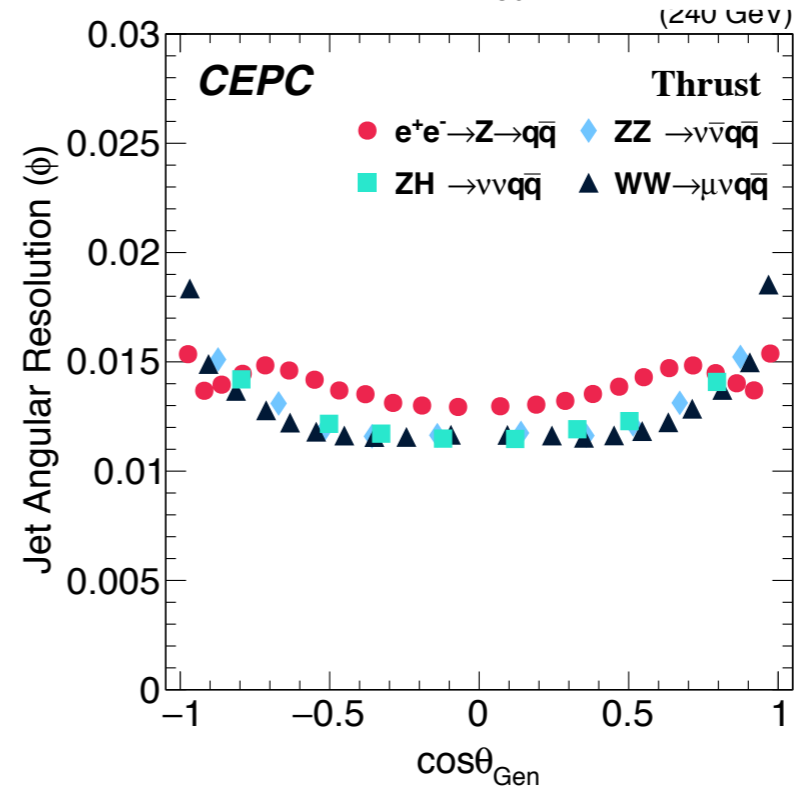
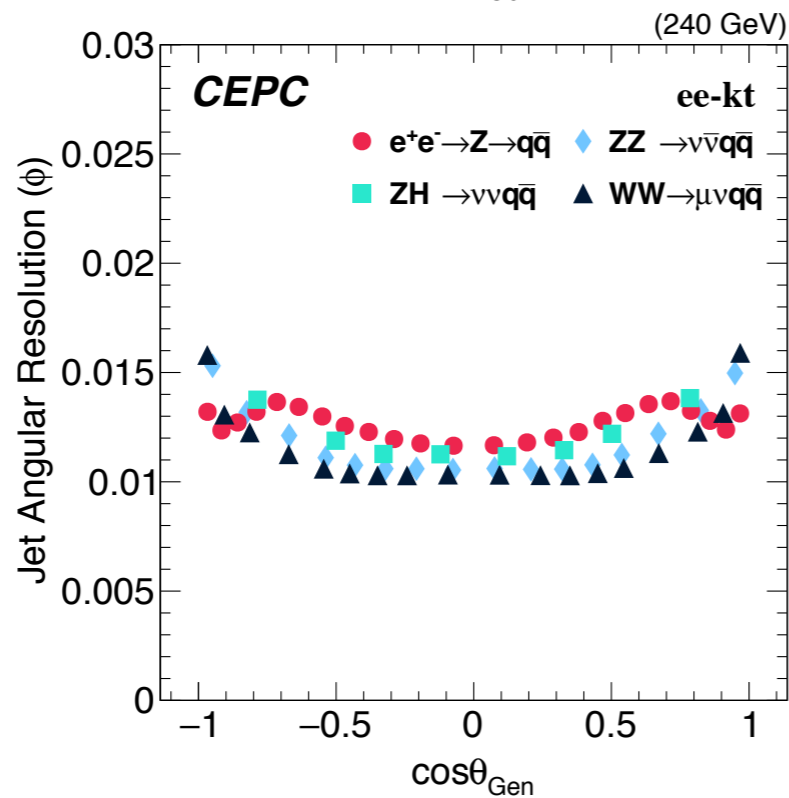
- The improvement brought from thrust based algorithm is significant at high energy region ( $E_j > 60$  GeV) and central detector region ( $|\cos\theta_j| < 0.6$ ).
- Improvement comes from boosted object separation in thrust based algorithm.

# BM3: JAR (ee-kt—Thrust)

JAR( $\theta$ )



JAR( $\phi$ )

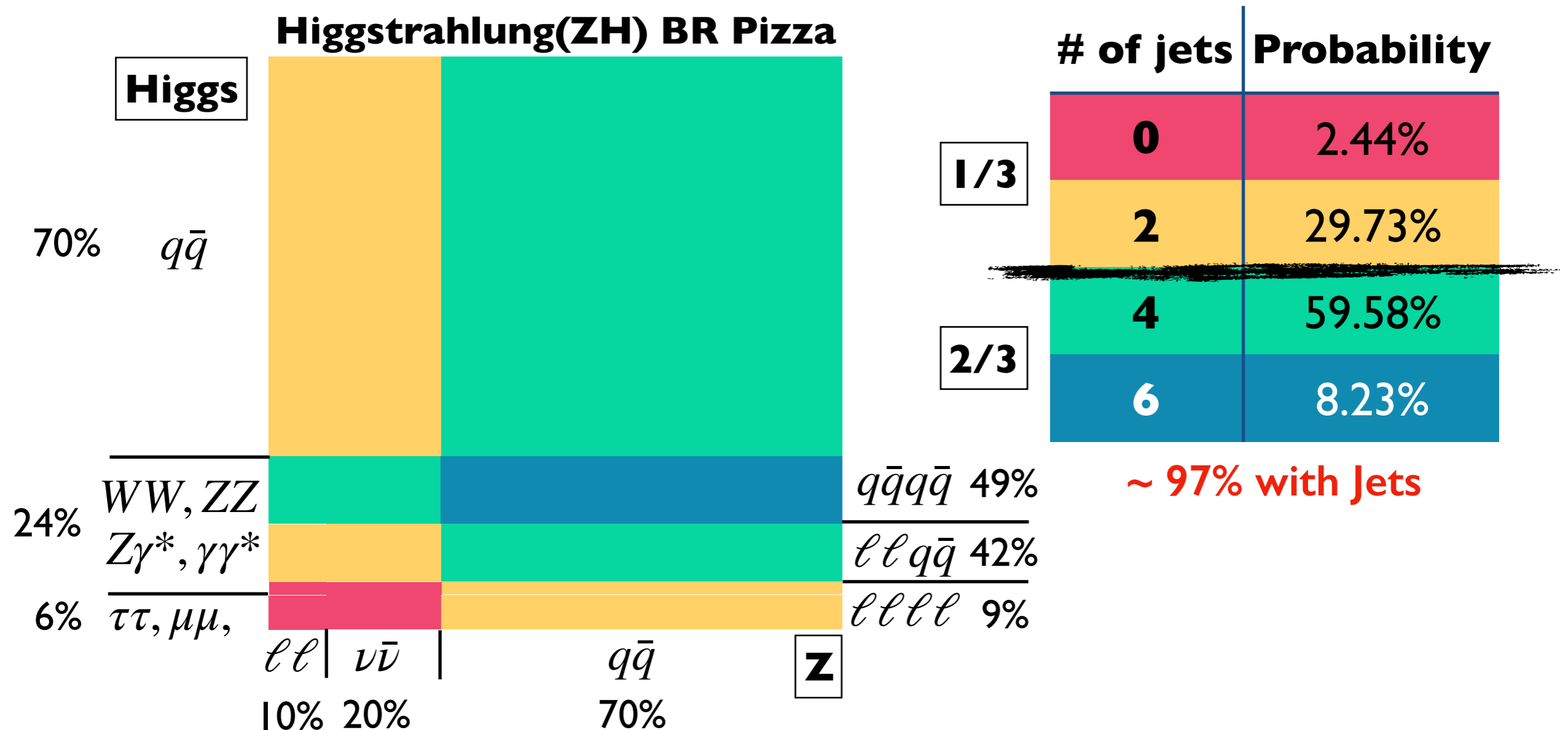


■ Both of jet  $\theta$  and  $\phi$  angular resolution are degraded by thrust method around 10%.

# Summary(1/2)

## ■ Jets are crucial for the CEPC Higgs physics and EW physics

- **97%** of ZH events involve jets
- **1/3** of ZH events come from only single Z or Higgs boson.
- **2/3** of ZH events have more than one boson (e.g.  $ZH \rightarrow q\bar{q}q\bar{q}$ )  
 → Need **color singlet identification algorithm**.



# Summary(2/2)

- I. **BMR < 4% (3.8%) is critical. Achieved at the CEPC baseline**
  - \* W, Z, Higgs boson can be efficiently separated at both semi-leptonic & full hadronic final-state.
  - \* Exploit Z-boson di-jet recoil mass to distinguish the ZH from ZZ process (main background).
  
- II. **Jet energy resolution ~ 3-5% & Jet angular resolution ~ 1%.**
  - \* All of the dominant jet processes have been studied.
  
- III. **2-jet final-states could be identified with  $\text{efficiency} \times \text{purity} = 88.4\%$ .**
  - \* Have designed a dedicatedly algorithm, **thrust based algorithm**.
  - \* JER is improved ~ **10%** in  $|\cos\theta_j| < 0.6$ ; JAR is degraded ~ **10%**.

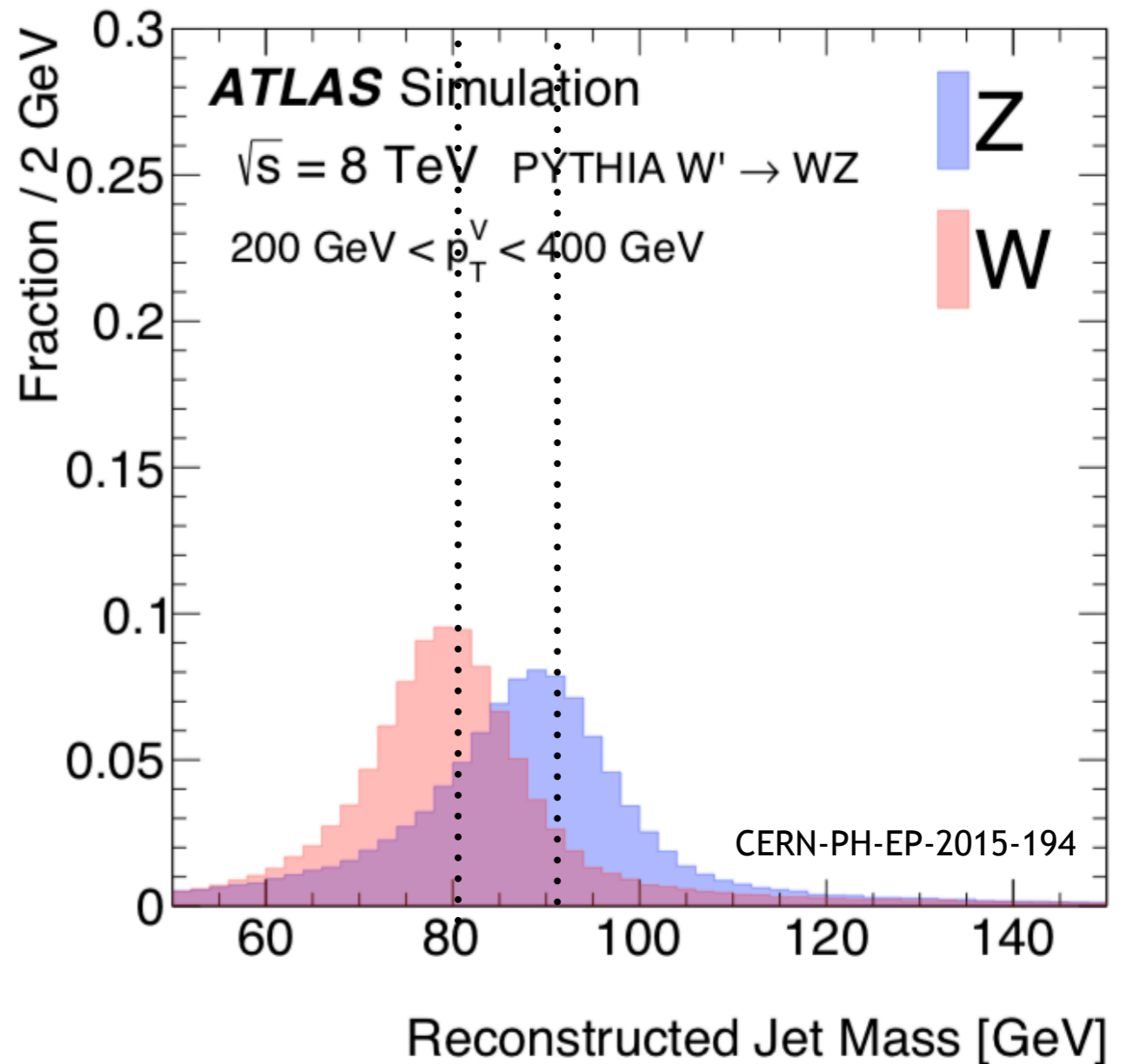
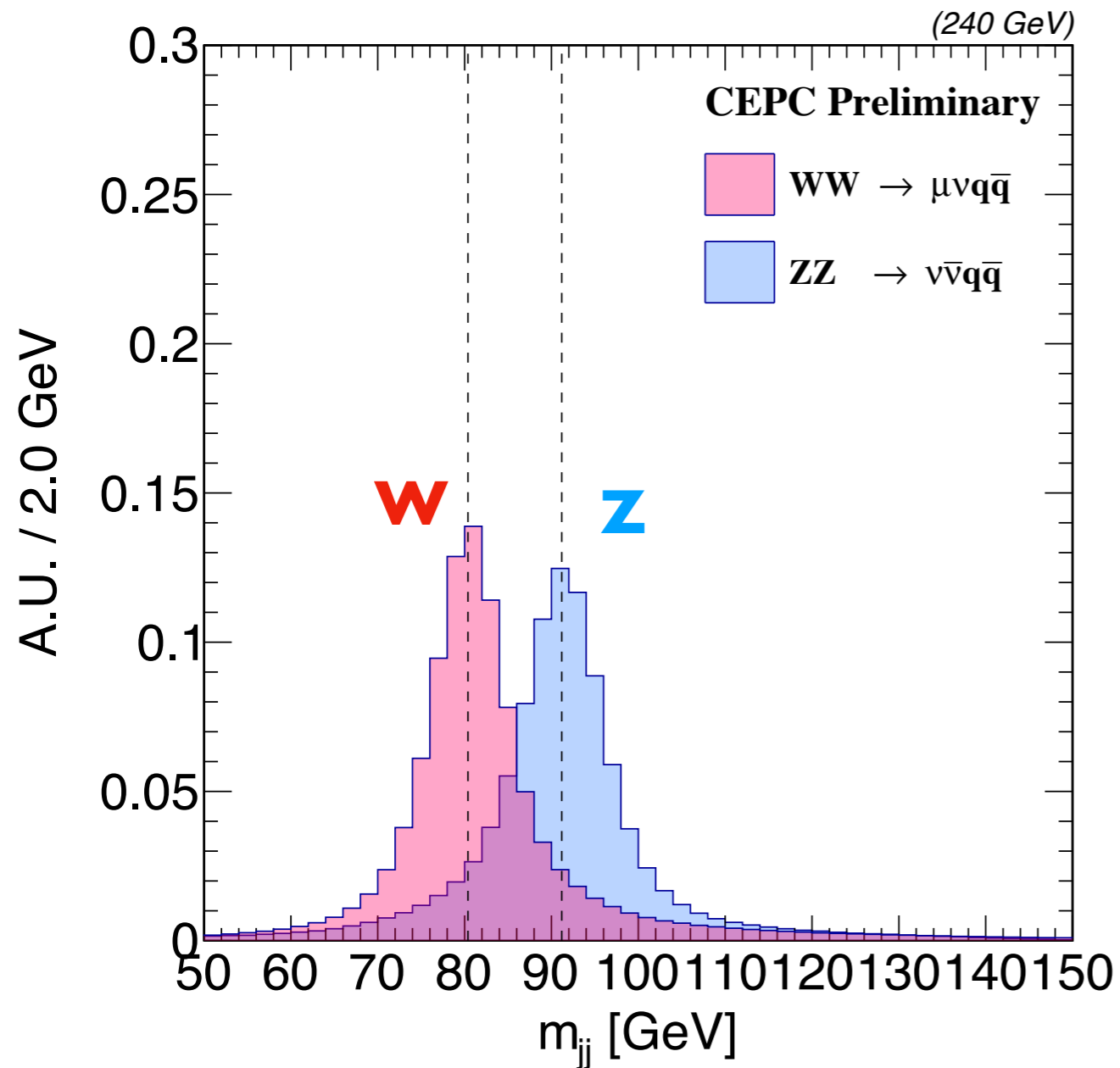


**Thank for your attention**



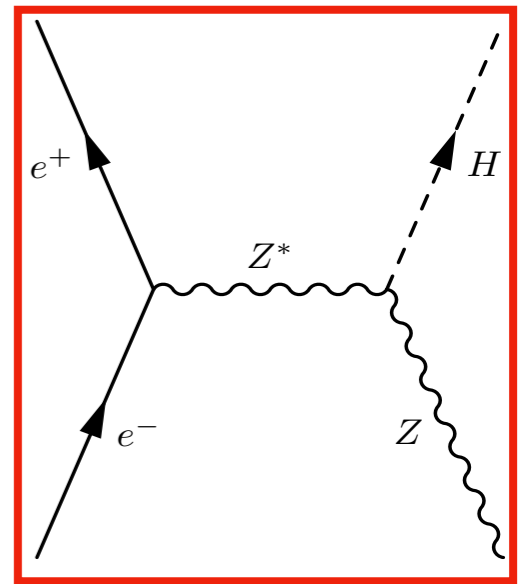
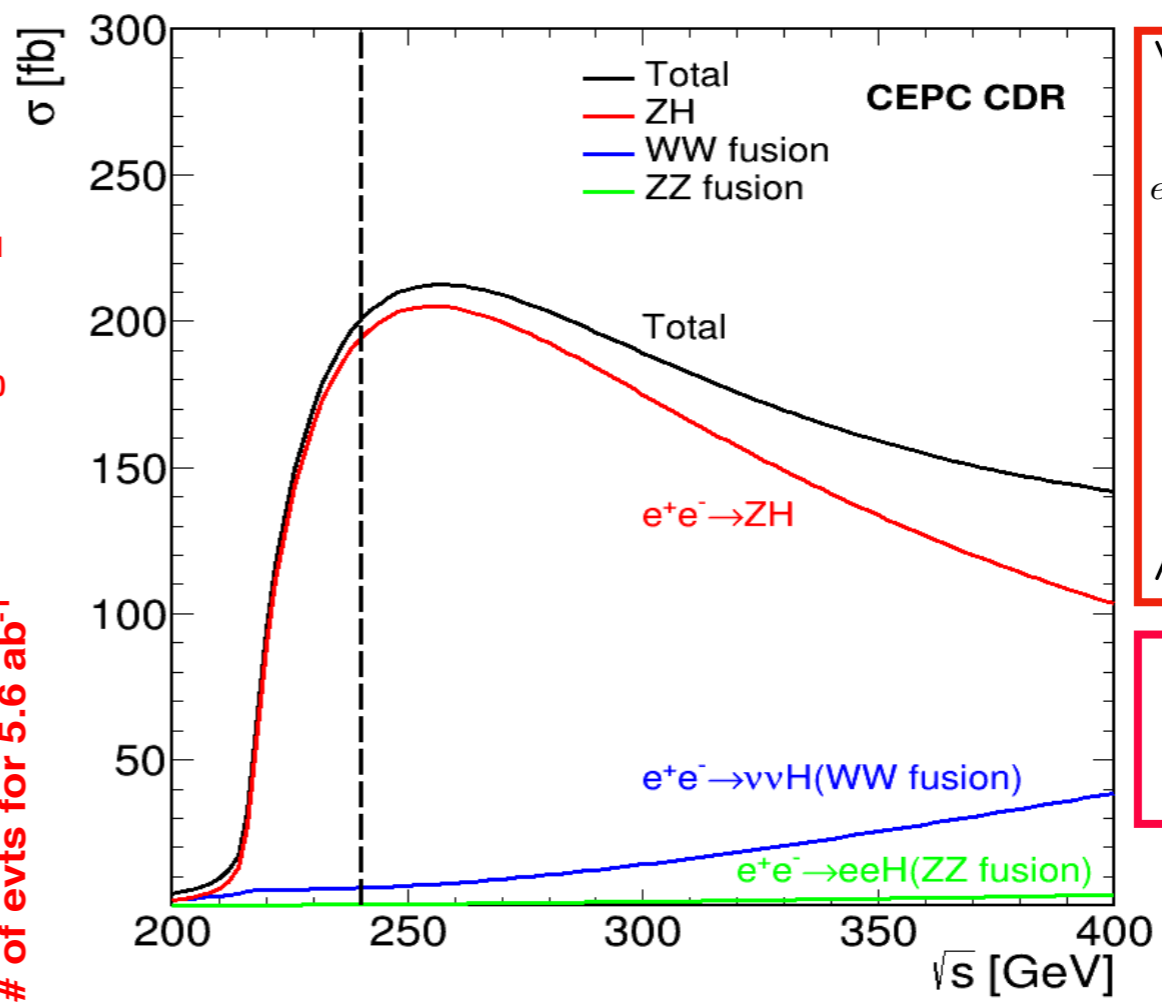
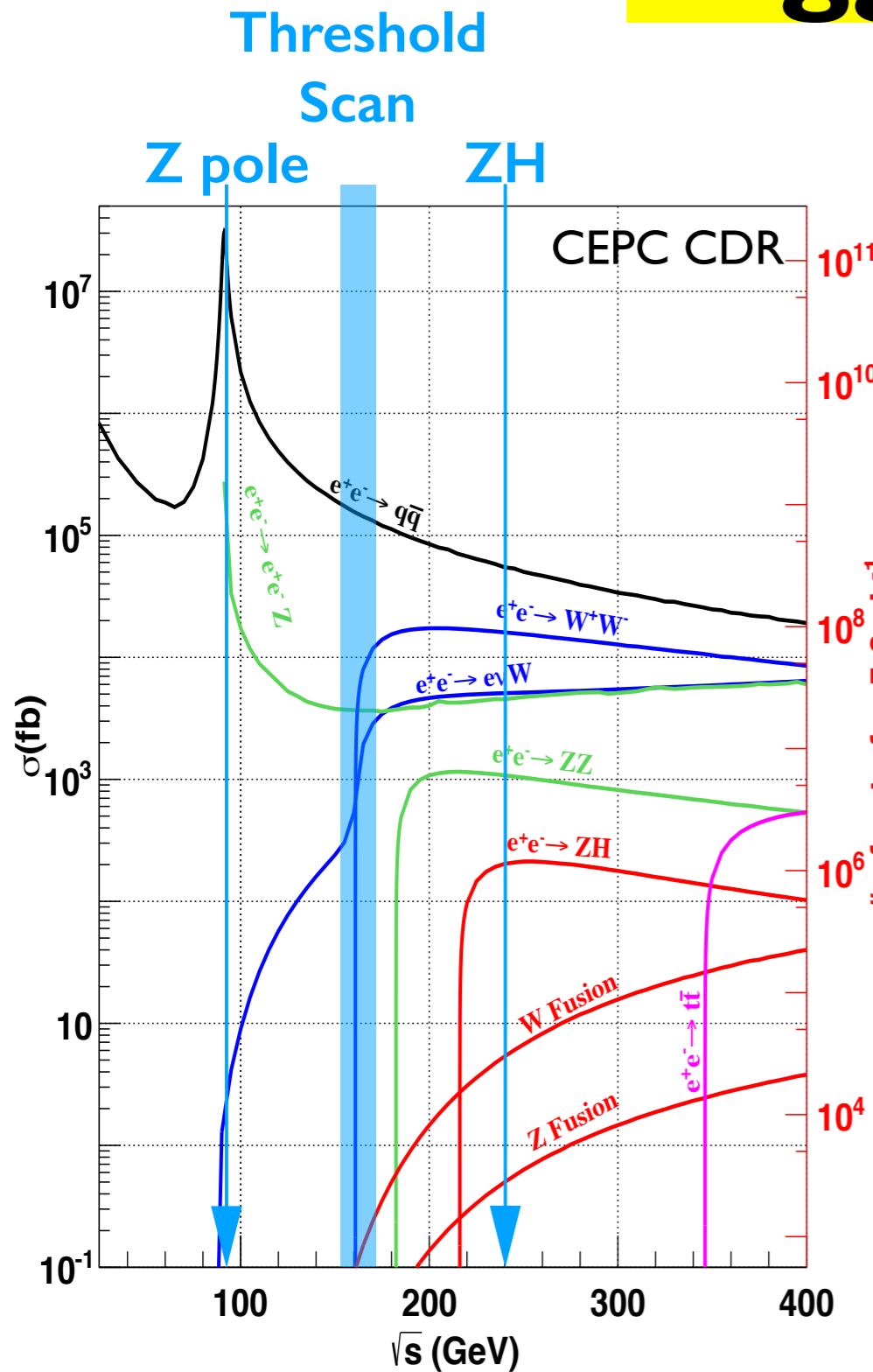
**Back up**

# BM I: Massive Boson Mass Resolution



- The separation of Z- and W-boson at CEPC is better than ATLAS as it should be.
  - Better collision environment and dedicatedly designed PFA and detector.

# Higgs Production at CEPC



**S : B =**  
**1 : (100 ~ 1000)**

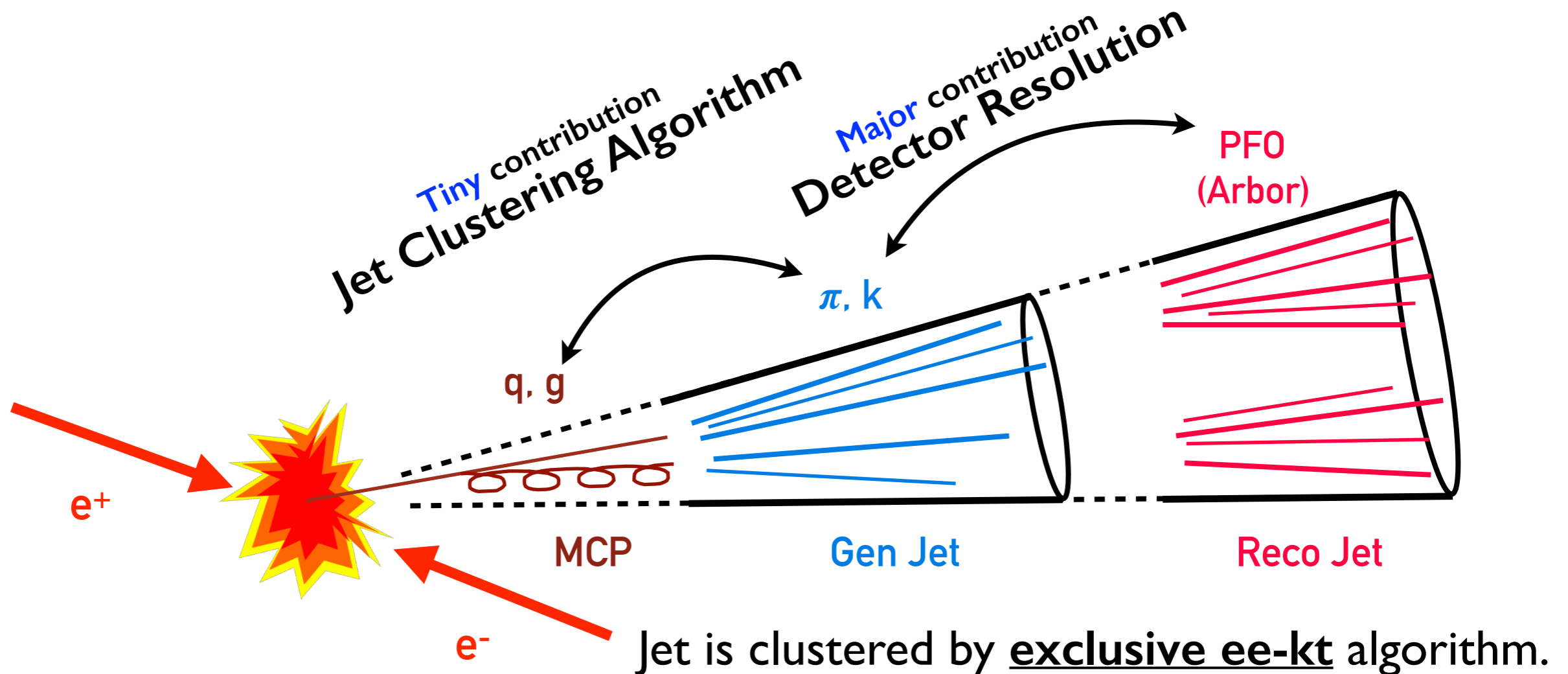
Process	Cross section(fb)	Events in 5.6 ab <sup>-1</sup>
$e^+e^- \rightarrow ZH$	196.2	$1.10 \times 10^6$
$e^+e^- \rightarrow \nu_e \bar{\nu}_e H$	6.19	$3.47 \times 10^4$
$e^+e^- \rightarrow e^+e^- H$	0.28	$1.57 \times 10^3$
<b>Total</b>	<b>203.7</b>	<b><math>1.14 \times 10^6</math></b>

■ Observables: Higgs mass,  $\sigma(\mathbf{ZH})$ , event rate ( $\sigma(\mathbf{ZH}, \nu\nu H) \times \text{Br}(H \rightarrow X)$ ), Diff.

→ **Absolute Higgs width**, branching ratio, **couplings**

# Objects Definition

- **MCPs** represents initial parton of MC quark. The original state of quark.
- **GenJets** are all MC particles grouped with  $c\tau > 1\text{cm}$  except neutrinos through exclusive ee-kt jet clustering algorithm.
- **RecoJets** are grouped with the particle flow objects by exclusive ee-kt jet clustering algorithm.



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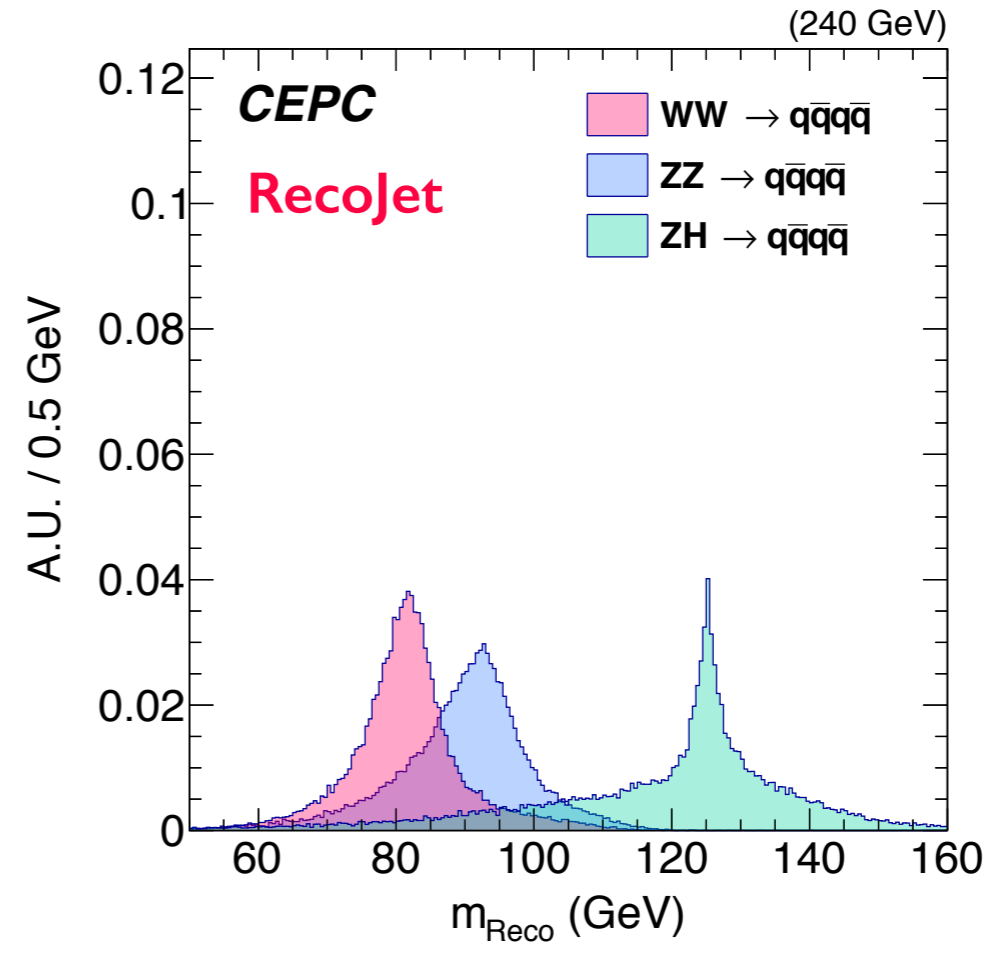
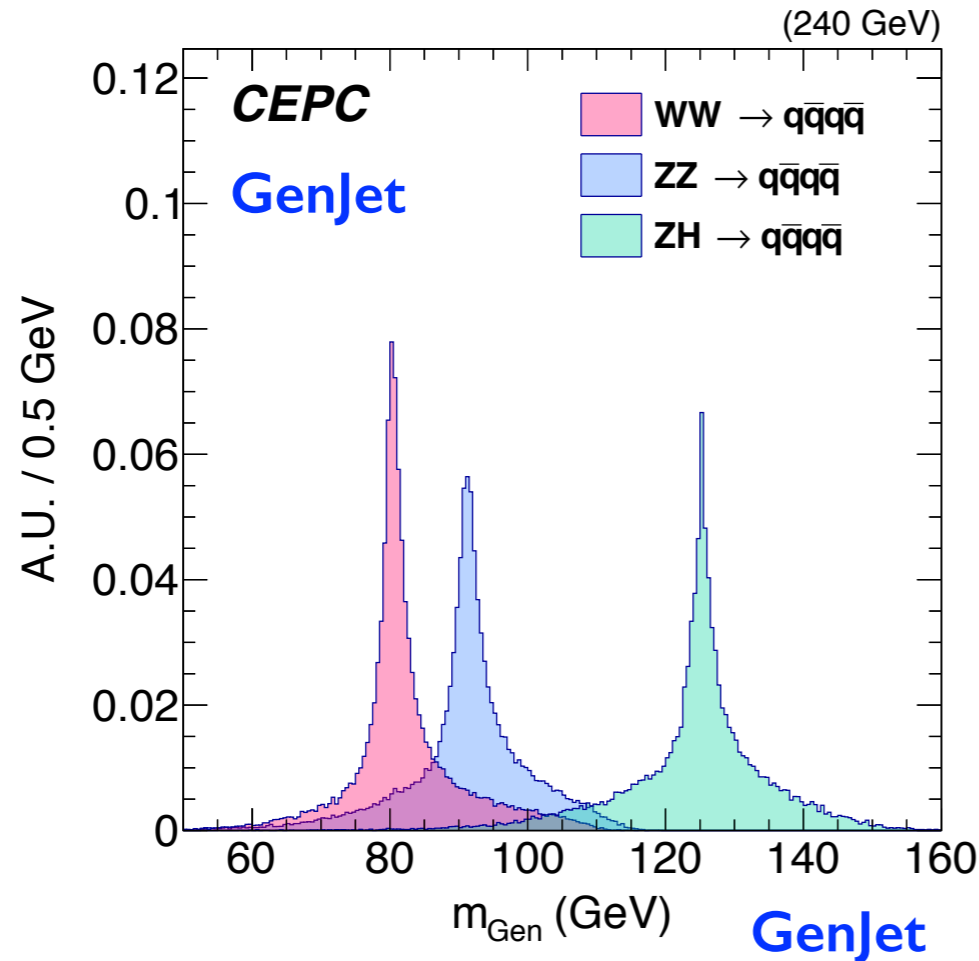
- $ZH \rightarrow q\bar{q}q\bar{q}$  is dominant.
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**(Potential huge impact)**

BM4: Separation of  $WW$ ,  $ZZ$ , and  $ZH \rightarrow qqqq$  final state

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# BM4: WW, ZZ, ZH to 4-jet Separation

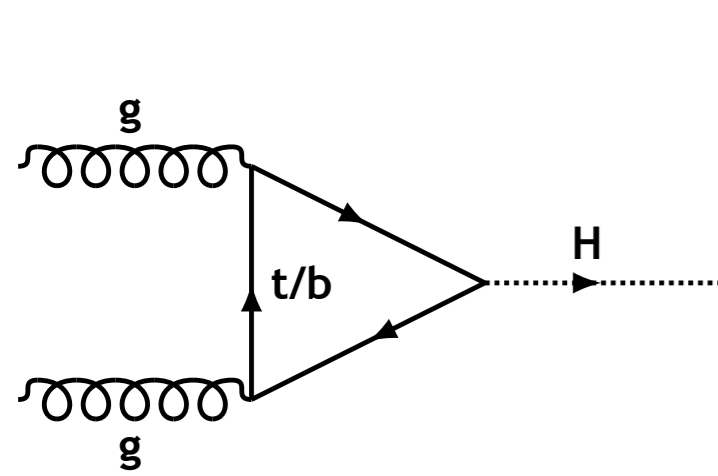


Sample \ Assignment(%)	WW	ZZ	ZH
WW	63.24	18.95	17.81
ZZ	16.09	57.89	26.02
ZH	9.99	13.84	<b>76.17</b>

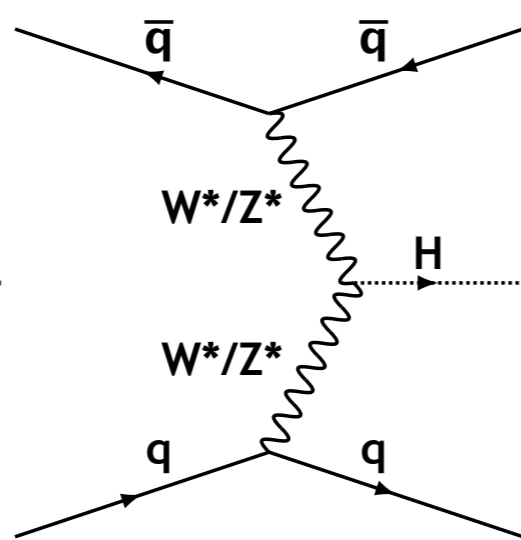
Sample \ Assignment(%)	WW	ZZ	ZH
WW	64.98	19.07	15.94
ZZ	26.51	50.54	22.96
ZH	20.29	22.93	<b>56.77</b>

- The **Efficiency x Purity** of ZH identification is reached **18%** in the 5 ab<sup>-1</sup> statistic.
- The **statistical uncertainty** of ZH to full hadronic final-state could achieve **0.25%** after considering the major bkg, WW and ZZ.

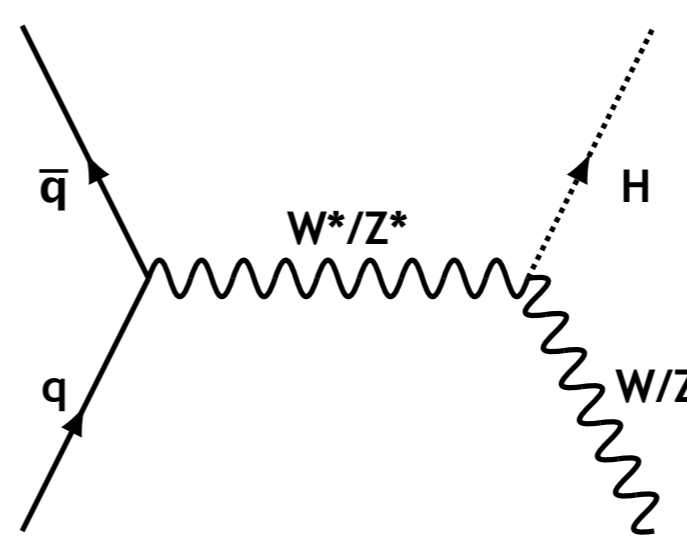
# Higgs Production @ Hadron Collider



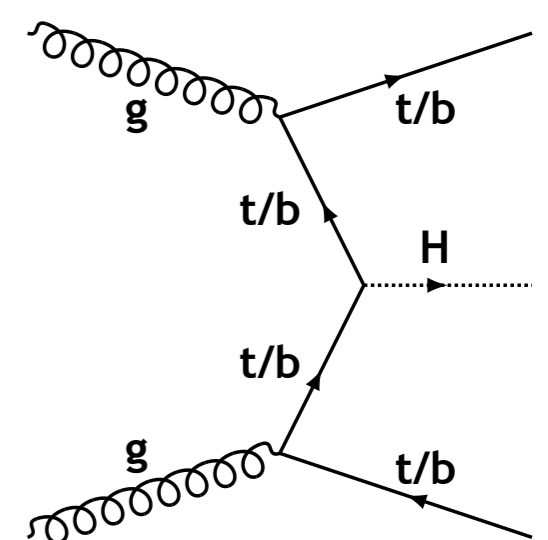
**ggF**  
Gluon-gluon Fusion



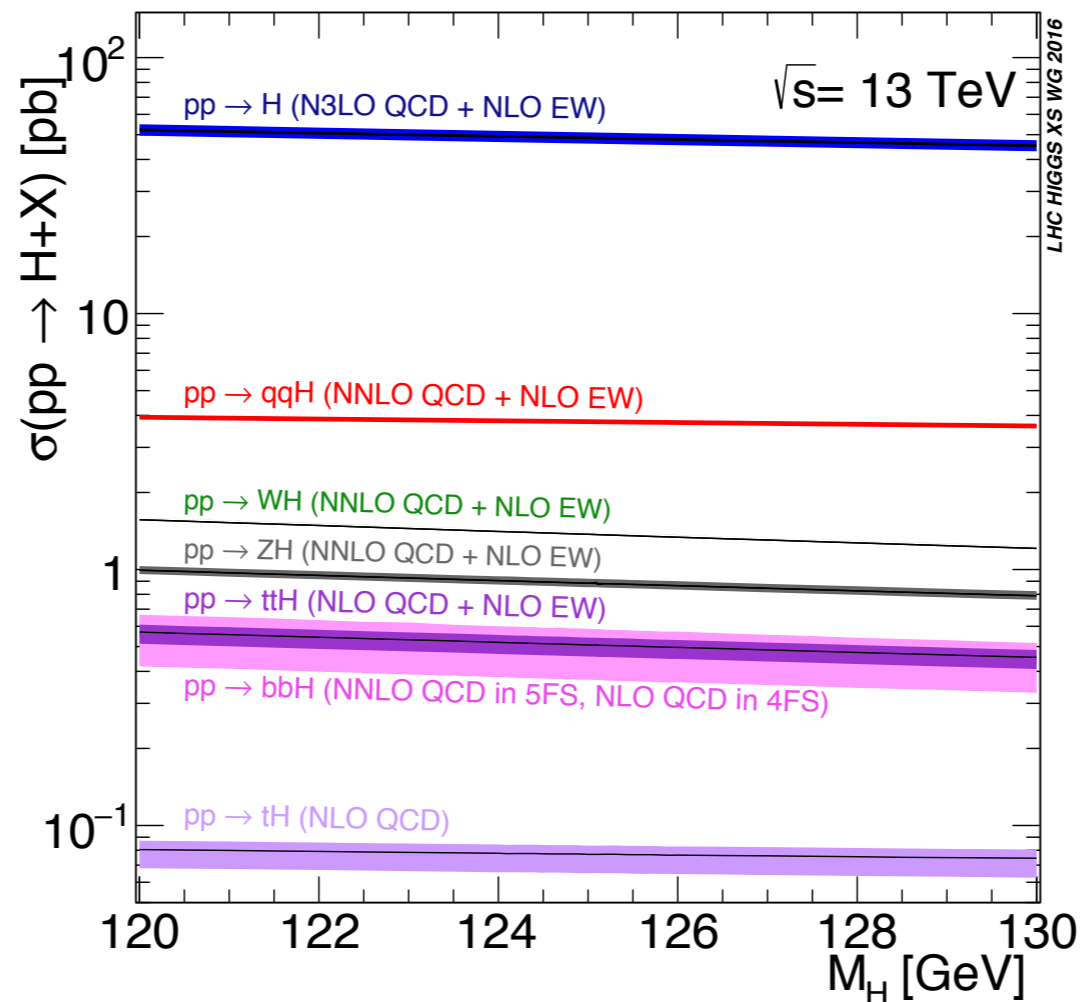
**VBF**  
Vector boson fusion



**WH/ZH**  
Associated vector boson fusion

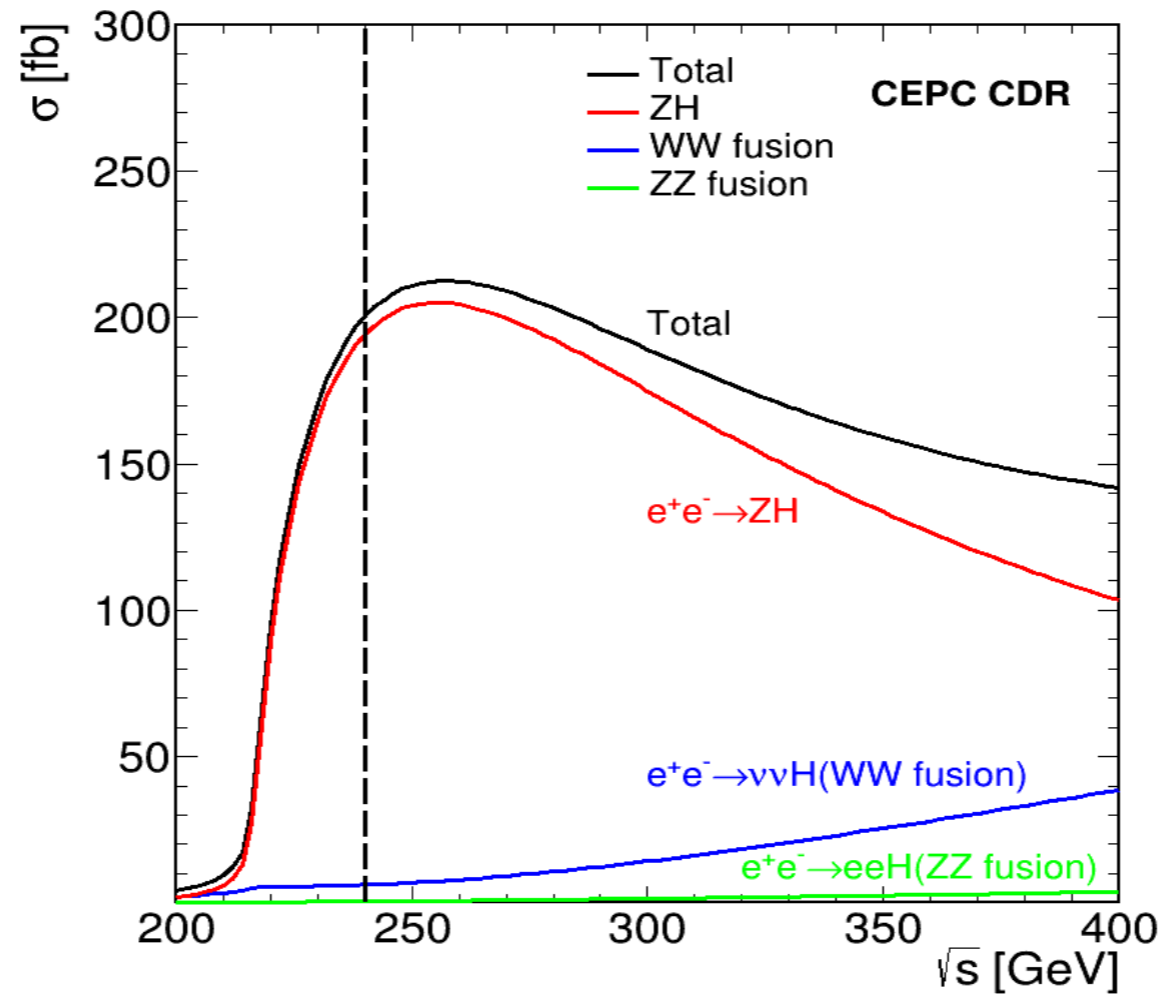
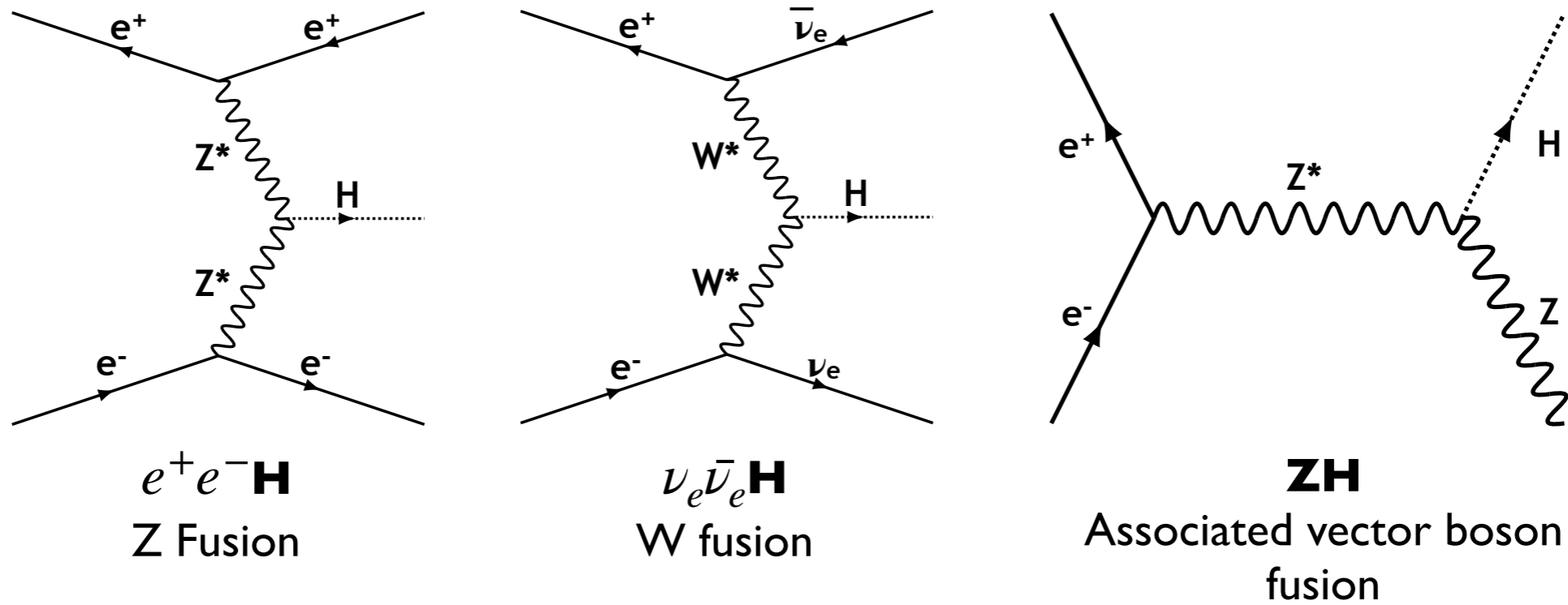


**ttH**  
Associated top-quark pair production





# Higgs Production @ Lepton Collider



# SM Production @ Lepton Collider

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Higgs boson production, cross section in fb		
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<b>Total</b>	<b>203.7</b>	<b><math>1.14 \times 10^6</math></b>
Background production, cross section in pb		
$e^+e^- \rightarrow e^+e^+(\gamma)$ (Bhabha)	930	$5.2 \times 10^9$
$e^+e^- \rightarrow q\bar{q}(\gamma)$	54.1	$3.0 \times 10^8$
$e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ [or $\tau^+\tau^-(\gamma)$ ]	5.3	$3.0 \times 10^7$
$e^+e^- \rightarrow WW$	16.7	$9.4 \times 10^7$
$e^+e^- \rightarrow ZZ$	1.1	$6.2 \times 10^6$
$e^+e^- \rightarrow e^+e^-ZZ$	4.54	$2.5 \times 10^7$
$e^+e^- \rightarrow e^+\nu W^-/e^-\bar{\nu}W^+$	5.09	$2.6 \times 10^7$

$Z \rightarrow \ell^+\ell^-$ : **10%**

$Z \rightarrow \nu\nu$ : **20%**

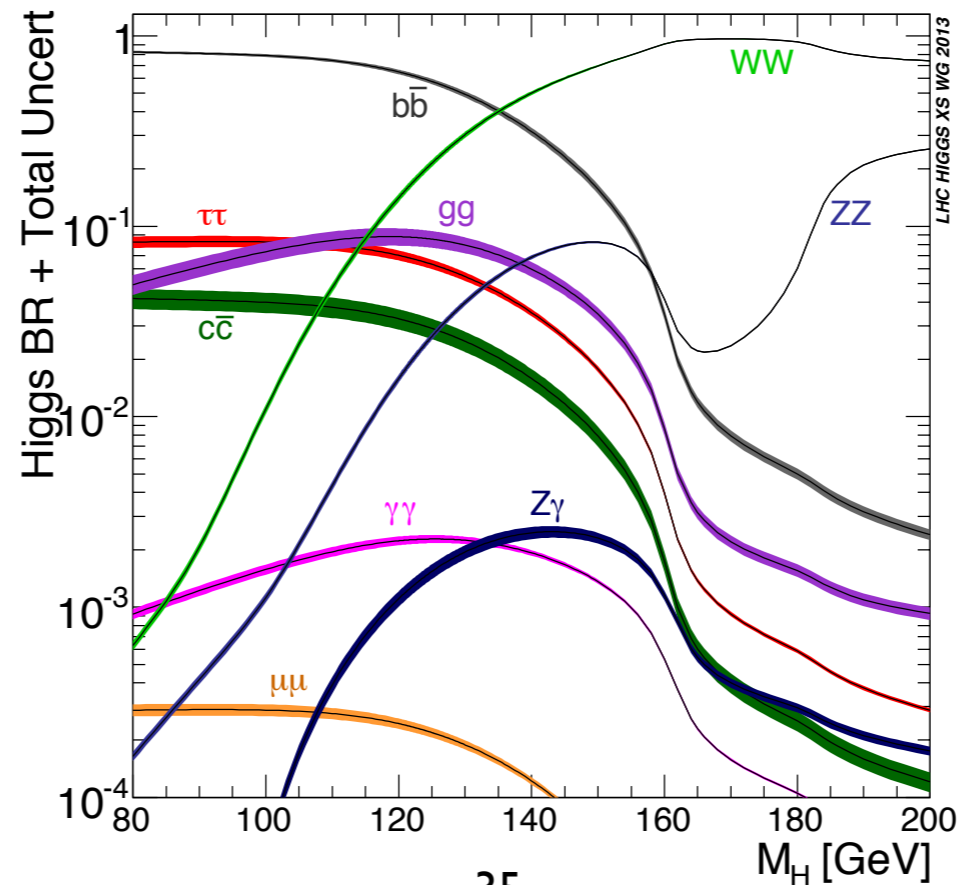
$Z \rightarrow q\bar{q}$ : **70%**

$W \rightarrow \ell\nu$ : **30%**

$W \rightarrow q\bar{q}$ : **70%**

# Higgs Decay Modes

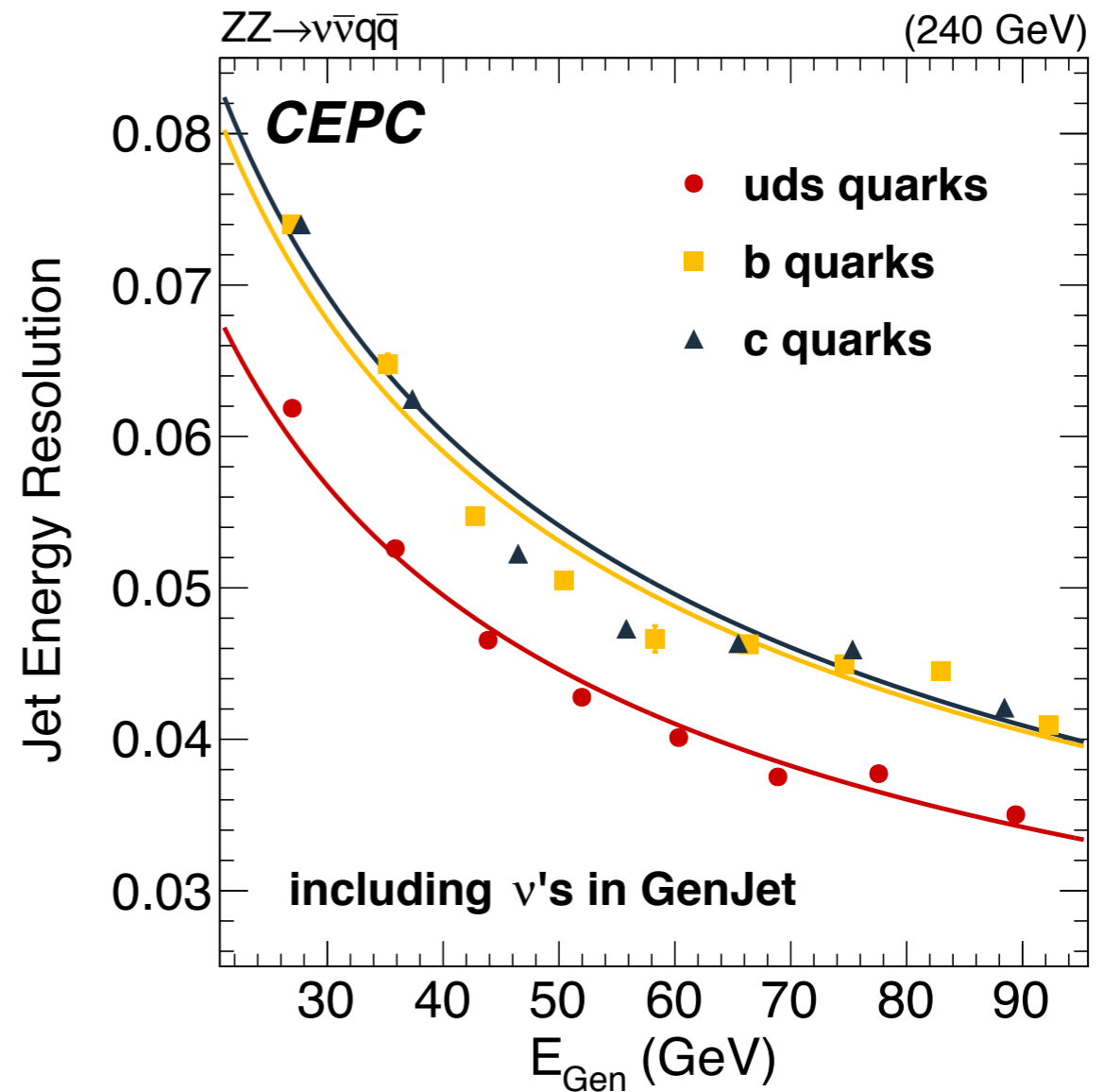
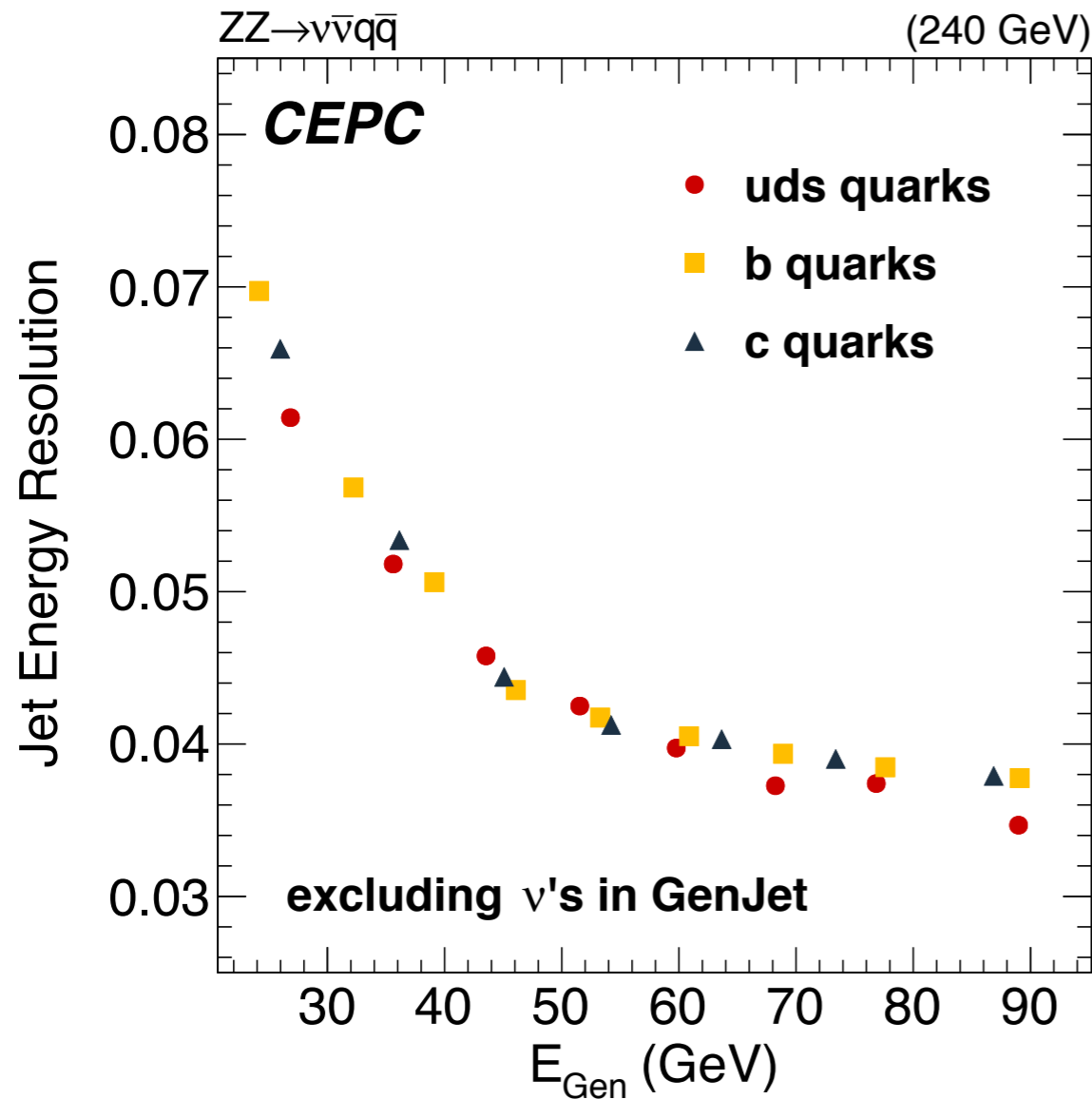
Decay mode	Branching ratio	Relative uncertainty (%)
$H \rightarrow b\bar{b}$	57.7%	(+3.2, -3.3)
$H \rightarrow c\bar{c}$	2.91%	(+12, -12)
$H \rightarrow gg$	8.57%	(+10, -10)
$H \rightarrow \tau^+\tau^-$	6.32%	(+5.7, -5.7)
$H \rightarrow \mu^+\mu^-$	$2.19 \times 10^{-4}$	(+6.0, -5.9)
$H \rightarrow WW^*$	21.5%	(+4.3, -4.2)
$H \rightarrow ZZ^*$	2.64%	(+4.3, -4.2)
$H \rightarrow \gamma\gamma$	$2.28 \times 10^{-3}$	(+5.0, -4.9)
$H \rightarrow Z\gamma$	$1.53 \times 10^{-3}$	(+9.0, -8.8)
$\Gamma_H$	4.07 MeV	(+4.0, -4.0)



# Physics Object Performances

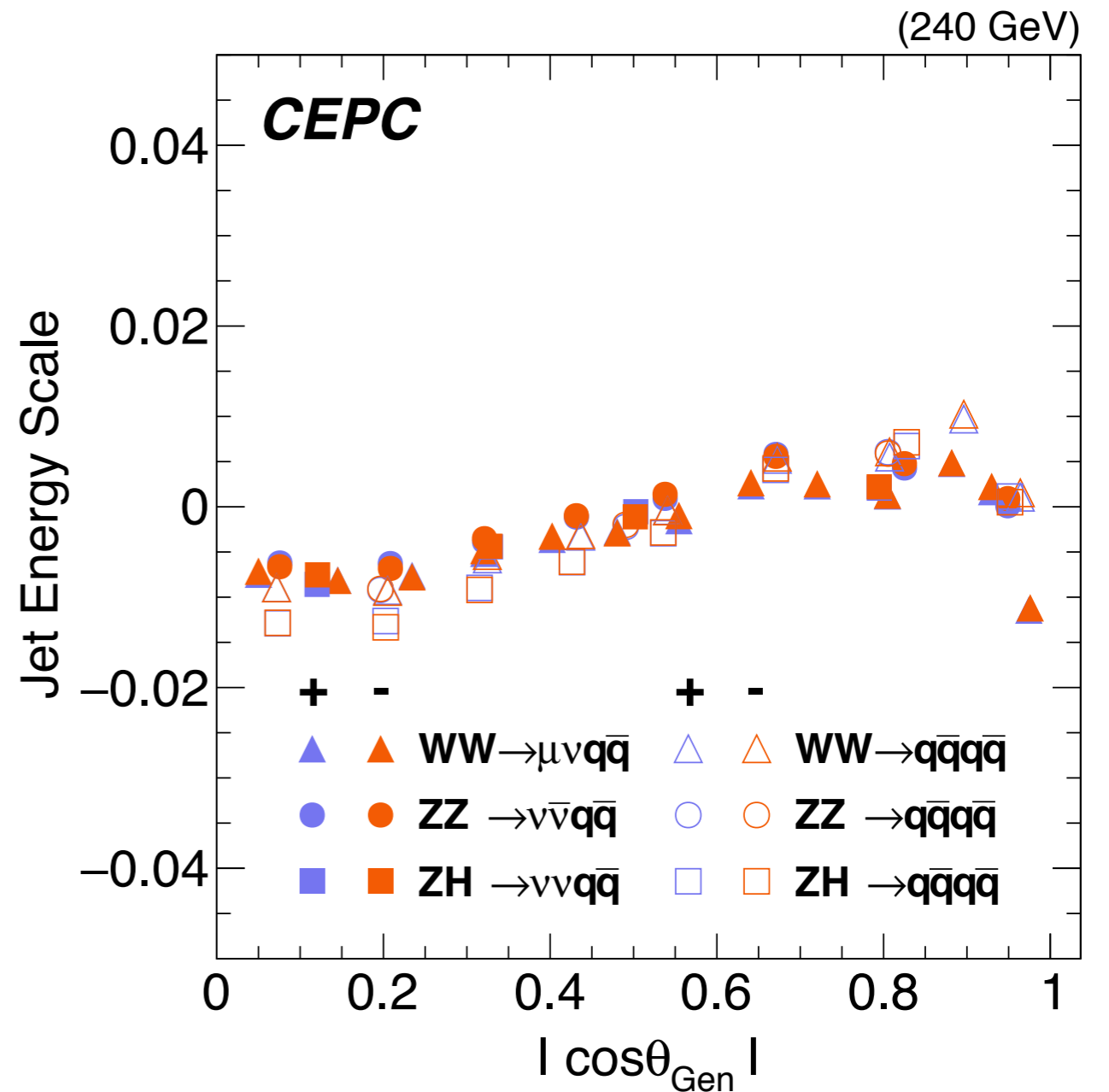
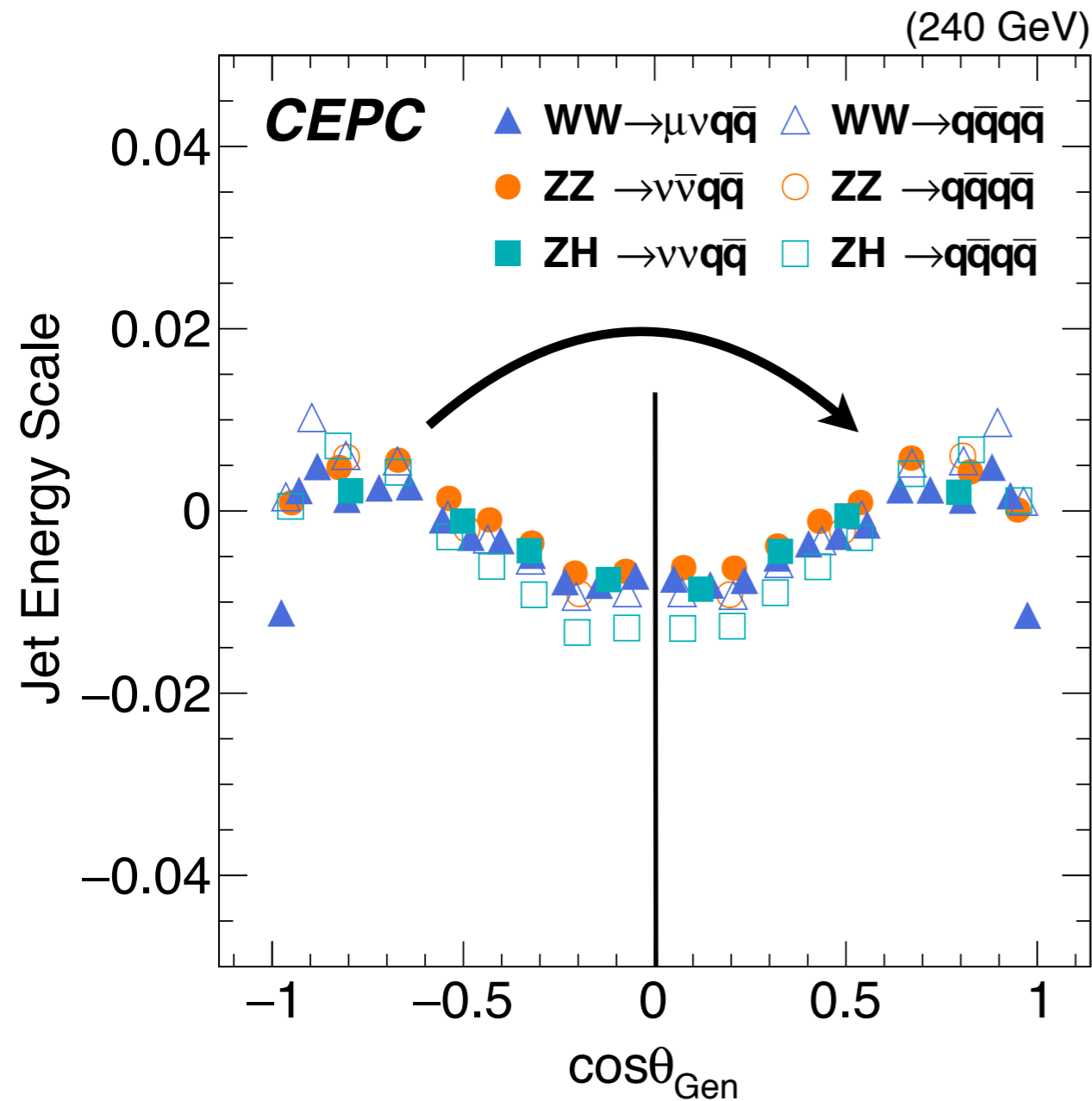
- **Leptons:** Above 2 GeV, the reconstruction efficiency  $> 99.5\%$  with misidentification rate  $< 1\%$ ; A relative mass resolution  $0.19\%$  of  $H \rightarrow \mu^+ \mu^-$ .
- **Photons:** Above 5 GeV, the reconstruction efficiency  $\sim 100\%$  with no misidentification rate from hadronic jet; A relative mass resolution  $2.5\%$  of  $H \rightarrow \gamma\gamma$
- **$\tau$ -leptons:** The reconstruction efficiency  $\sim 80\%$  with a purity  $\sim 90\%$  measured from  $ZH \rightarrow \tau\tau q\bar{q}$  event at  $\sqrt{s} = 240 \text{ GeV}$ .
- **Jet flavor tagging:** The b-tagging efficiency/purity of  $80\%/90\%$  and c-tagging efficiency/purity  $60\%/60\%$  are extracted from  $Z \rightarrow q\bar{q}$  at Z-pole.
- $K^\pm$ :  $K/\pi$  separation  $2\sigma$  with proposed ToF, achieving the accumulated efficiency/purity of  $95\%/95\%$  for kaons ID in  $Z \rightarrow q\bar{q}$  from momentum  $2\sim 20 \text{ GeV}$ .

# BM3: JER (Reco-Gen)



- JER depends on the jet flavors since the semi-leptonic decay of heavy flavor jet.  
→ **Consistent JER when excluding neutrinos in GenJets**
- For light-flavor jets with higher energy ( $E_j \sim 90$ ), JER could reach **3.4%**.

# BM3: JES Symmetry (Reco-Gen)



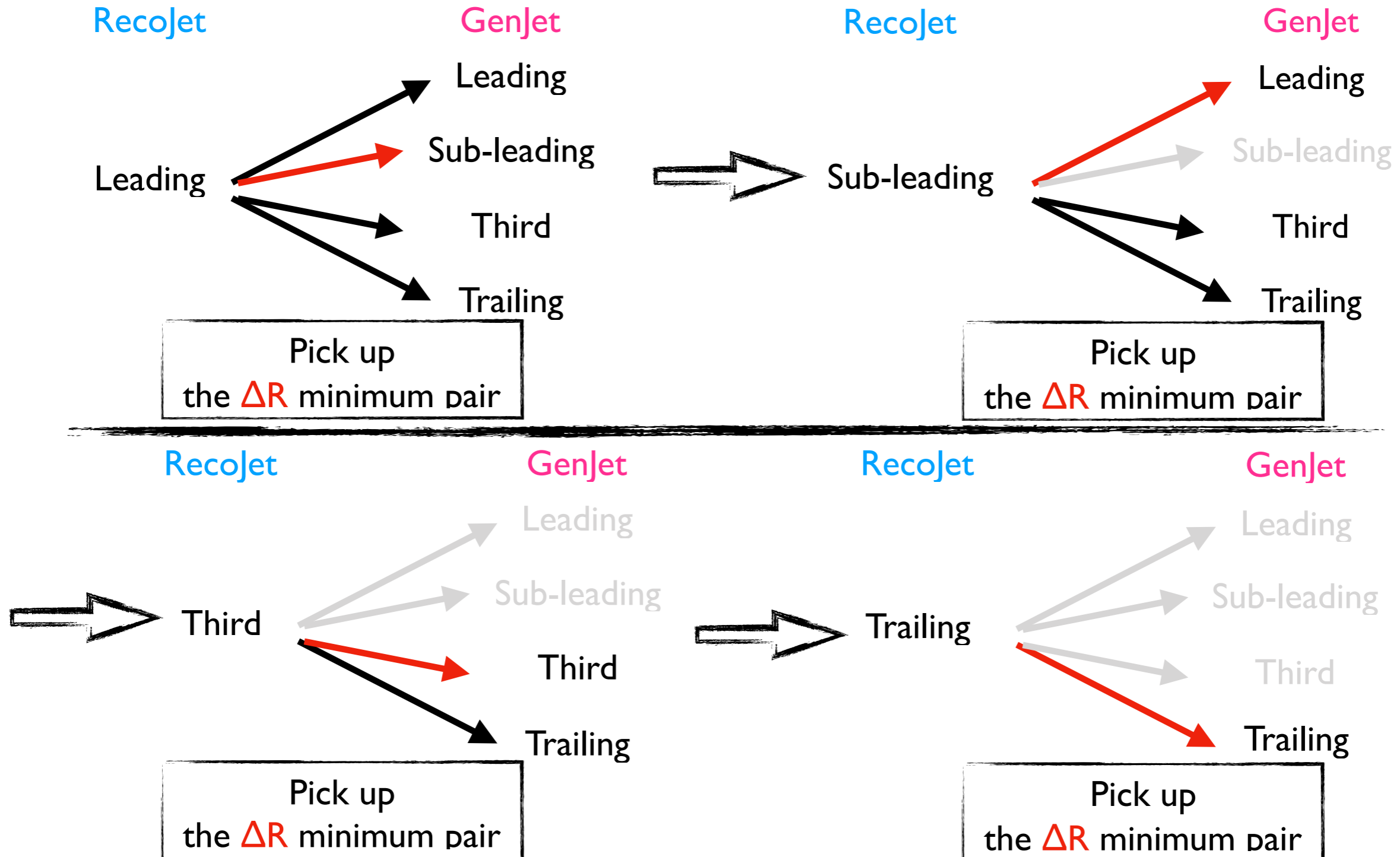
■ The results show very nice agreement between  $\cos\theta > 0$  and  $\cos\theta < 0$

# Double-sided Crystal Ball Function

$$f(x|\alpha_1, \alpha_2, n_1, n_2, \bar{x}, \sigma) = \begin{cases} \left(\frac{n_1}{|\alpha_1|}\right)^{n_1} e^{-\frac{|\alpha_1|^2}{2}} \left(\frac{n_1}{|\alpha_1|} - |\alpha_1| - \frac{x - \bar{x}}{\sigma}\right)^{-n_1} & \frac{x - \bar{x}}{\sigma} < -\alpha_1 \\ e^{-\frac{1}{2}\left(\frac{x - \bar{x}}{\sigma}\right)^2} & -\alpha_1 < \frac{x - \bar{x}}{\sigma} < \alpha_2 \\ \left(\frac{n_2}{|\alpha_2|}\right)^{n_2} e^{-\frac{|\alpha_2|^2}{2}} \left(\frac{n_2}{|\alpha_2|} - |\alpha_2| - \frac{x + \bar{x}}{\sigma}\right)^{-n_2} & \alpha_2 < \frac{x - \bar{x}}{\sigma} \end{cases}$$

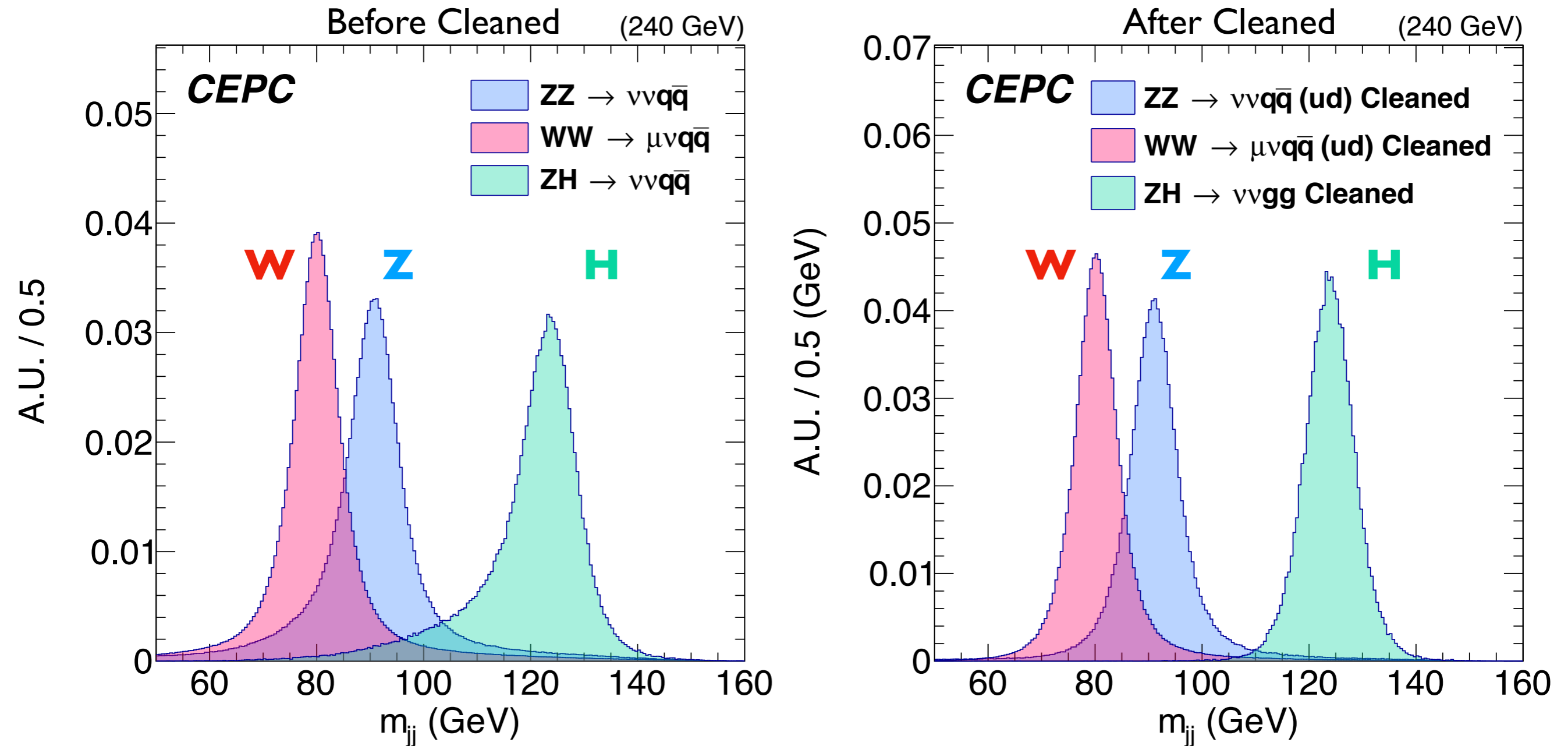
# Minimum Matching Method

- Only **1.28%** of events have  $dR < 0.4$  between Lead Recojet to more than 2 Genjets; **1.79%** for Sub-leading one; **0.7%** for Third one.
- When  $\#(\Delta R_{\text{Reco-Gen}} < 0.4) > 2$ , matched GenJet is decided by  $|\Delta E/E|$ .





# BM I: Massive Boson Mass Resolution

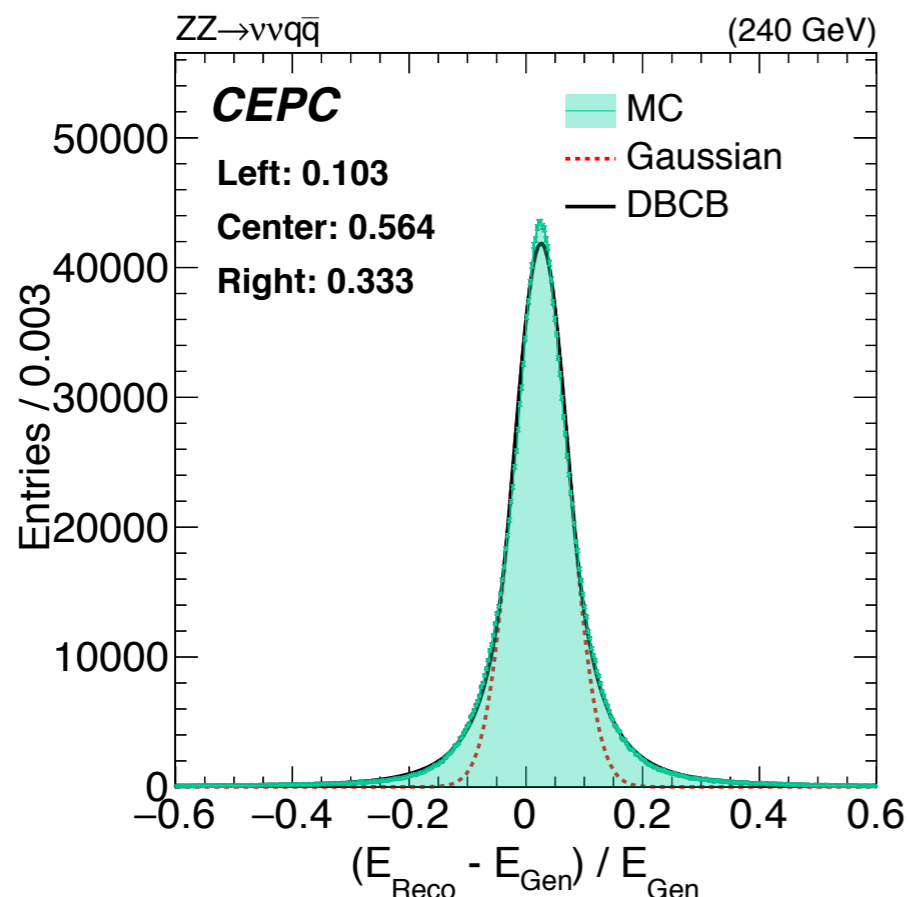


- W-, Z-, and Higgs-boson dijet masses are **well separated** at CEPC.
- After cleaned, Z- and W-boson could be separated  $\approx 2\sigma$ .
- **Higgs Boson Mass Resolution = 3.8%** is reached the CEPC baseline.

Cleaned: Select the light flavor jet event with low energy ISR, low energy neutrino inside jet, and within  $|\cos\theta| < 0.85$ .

# BM3: JER, JAR( $\theta$ ), and JAR( $\phi$ ) Cover Fraction

Operation mode	Process	JER(%)	JAR( $\theta$ ) (%)	JAR( $\phi$ ) (%)
<b>Z</b>	$e^+e^- \rightarrow Z \rightarrow q\bar{q}$	57.6	52.5	44.7
	$e^+e^- \rightarrow Z\gamma \rightarrow q\bar{q}\gamma$	56.2	51.0	47.9
	$e^+e^- \rightarrow WW \rightarrow \mu\nu q\bar{q}$	49.1	46.7	46.9
	$e^+e^- \rightarrow WW \rightarrow q\bar{q}q\bar{q}$	58.2	50.9	49.9
<b>H</b>	$e^+e^- \rightarrow ZZ \rightarrow \nu\bar{\nu}q\bar{q}$	56.4	48.3	40.6
	$e^+e^- \rightarrow ZZ \rightarrow q\bar{q}q\bar{q}$	61.4	47.9	48.3
	$e^+e^- \rightarrow ZH \rightarrow \nu\bar{\nu}(q\bar{q} \text{ or } gg)$	62.5	44.1	48.5
	$e^+e^- \rightarrow ZH \rightarrow q\bar{q}(q\bar{q} \text{ or } gg)$	63.3	43.5	44.8



~60%

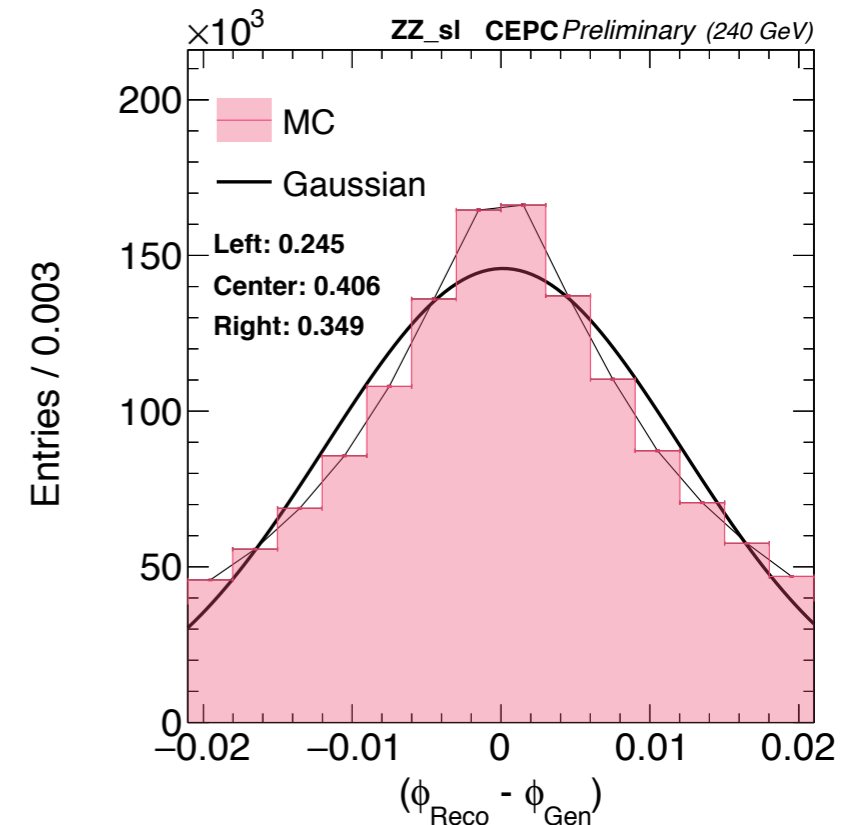
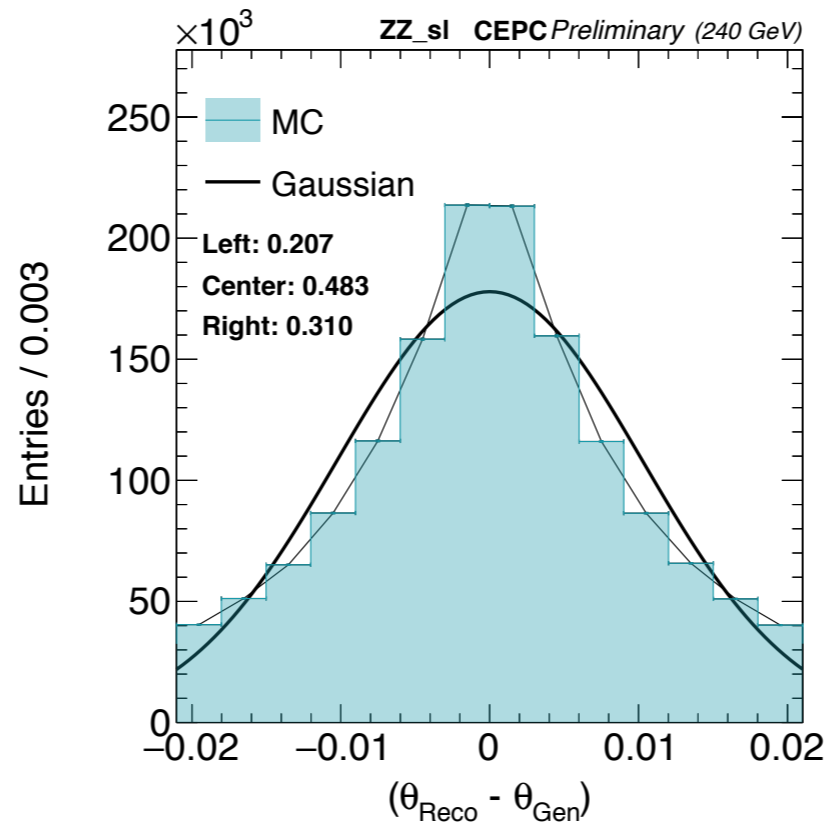
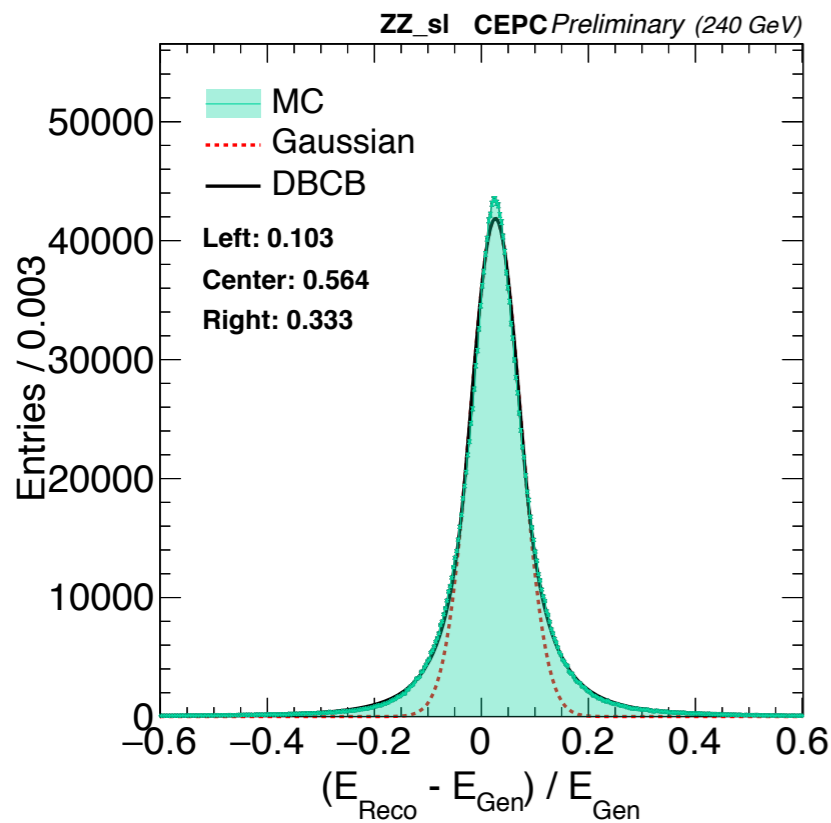
~50%

~50%

$$\text{Cover Fraction: } = \frac{N_{\sigma \text{ covered}}}{N}$$

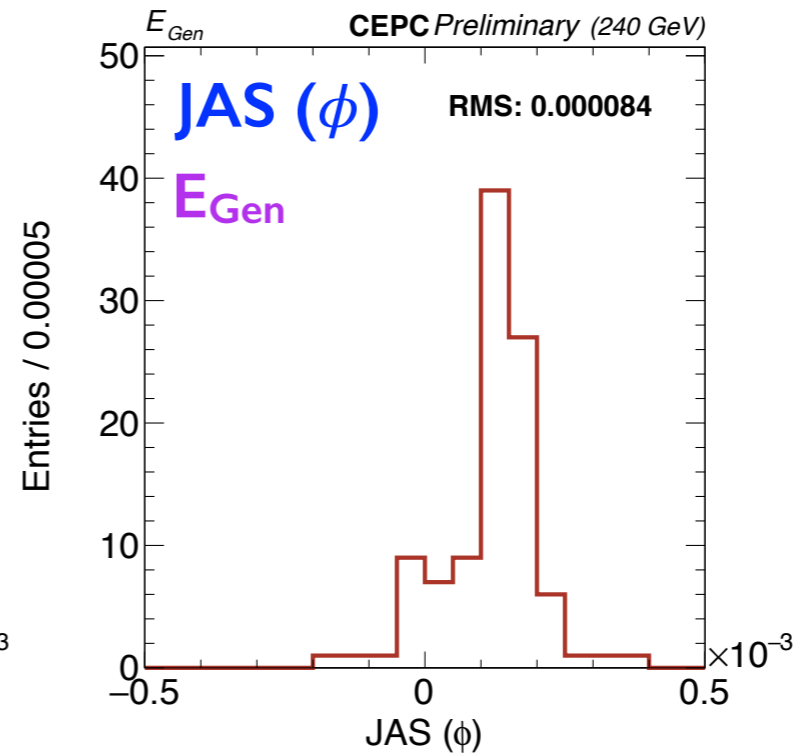
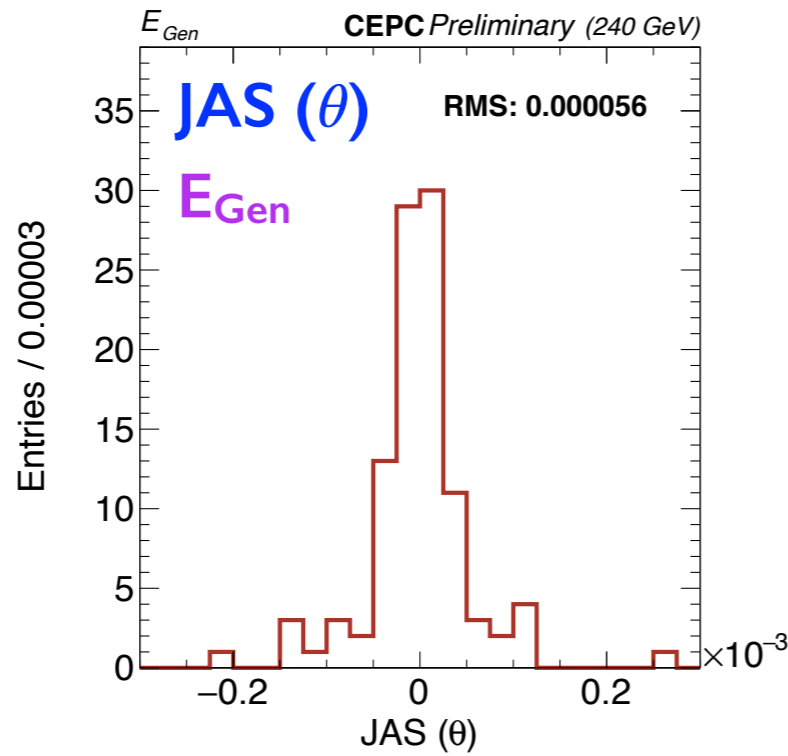
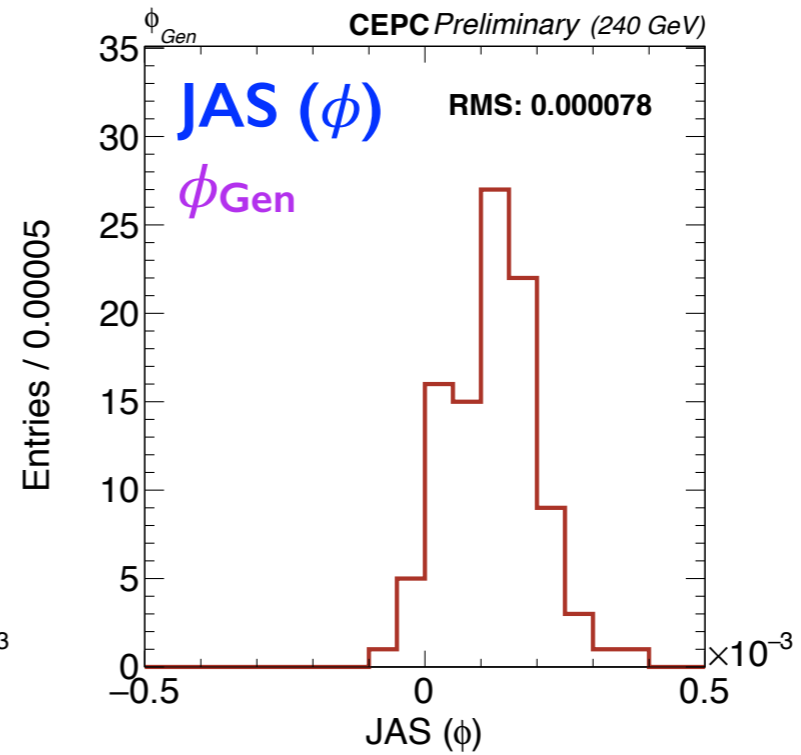
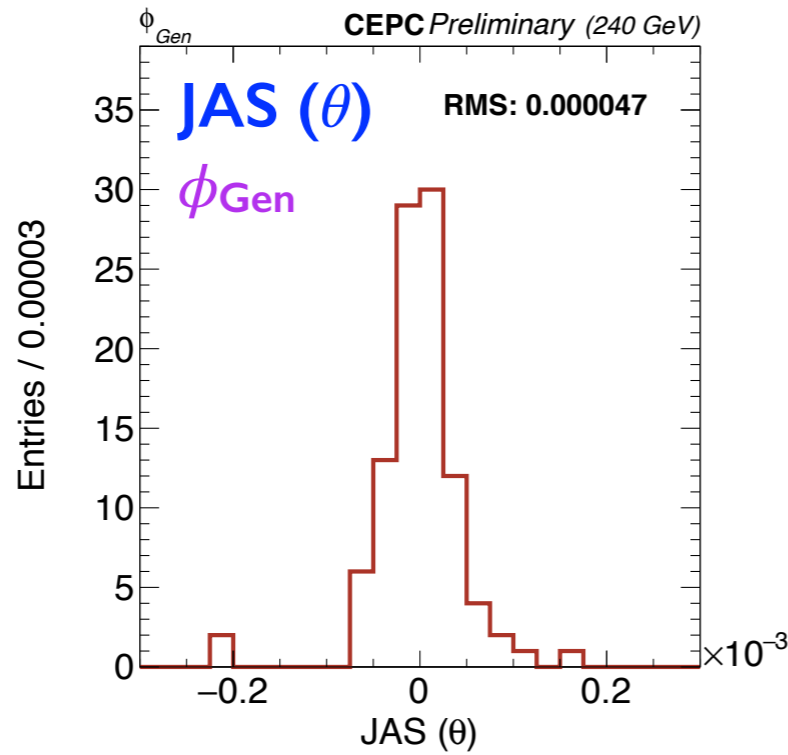
- The cover fraction is close to a Gaussian distribution, **68%**.  
→ **Well-controlled tail**

# BM3: JER, JAR( $\theta$ ), and JAR( $\phi$ ) Cover Fraction

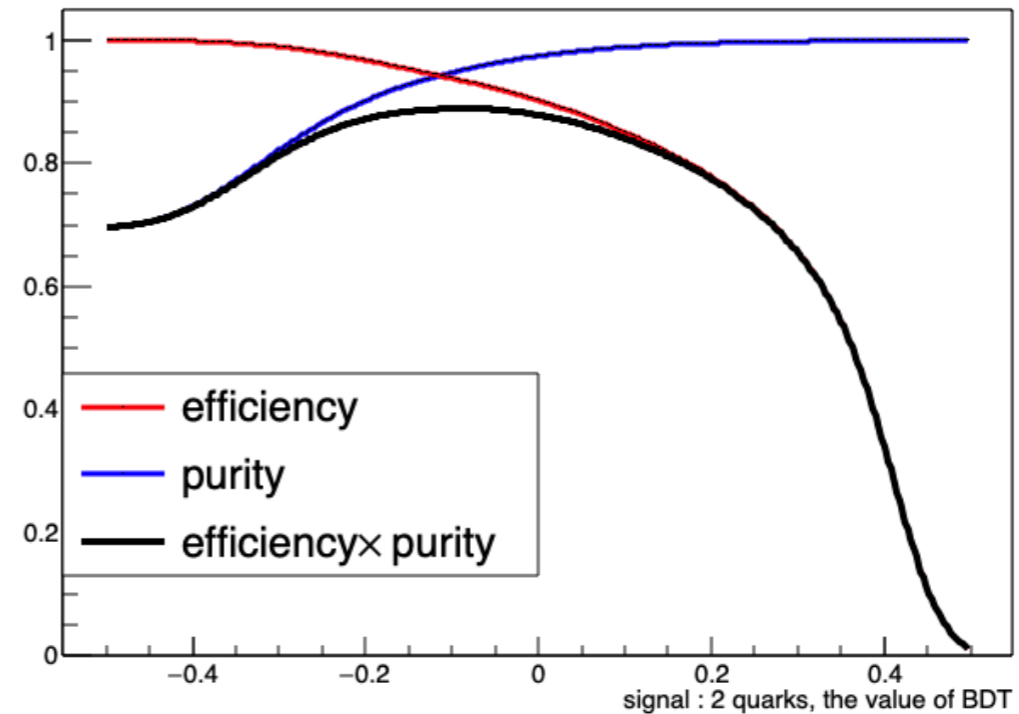
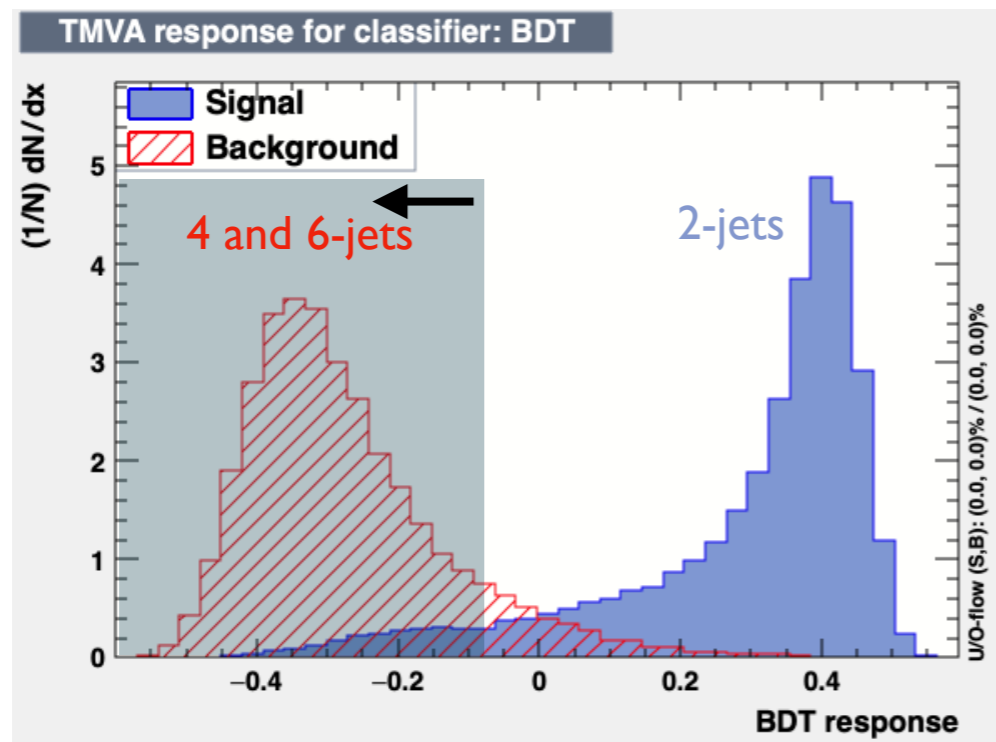


Operation mode	Process	JER(%)	JAR( $\theta$ )(%)	JAR( $\phi$ )(%)
<b>Z</b>	$e^+e^- \rightarrow Z \rightarrow q\bar{q}$	57.6	52.5	44.7
	$e^+e^- \rightarrow Z\gamma \rightarrow q\bar{q}\gamma$	56.2	51.0	47.9
	$e^+e^- \rightarrow WW \rightarrow \mu\nu q\bar{q}$	49.1	46.7	46.9
	$e^+e^- \rightarrow WW \rightarrow q\bar{q}q\bar{q}$	58.2	50.9	49.9
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	$e^+e^- \rightarrow ZZ \rightarrow q\bar{q}q\bar{q}$	61.4	47.9	48.3
	$e^+e^- \rightarrow ZH \rightarrow \nu\bar{\nu}(q\bar{q} \text{ or } gg)$	62.5	44.1	48.5
	$e^+e^- \rightarrow ZH \rightarrow q\bar{q}(q\bar{q} \text{ or } gg)$	63.3	43.5	44.8

# JAS Projection



# BM2: Preliminary Number of Jet Identification



## Samples:

$e^+e^- \rightarrow q\bar{q}$  (2 jets)  
 $ZZ \rightarrow q\bar{q}q\bar{q}$  (4 jets)  
 $W^+W^- \rightarrow q\bar{q}q\bar{q}$  (4 jets)  
 $ZH \rightarrow q\bar{q}q\bar{q}$  (4 jets)  
 $ZH \rightarrow q\bar{q}H \rightarrow q\bar{q}q\bar{q}q\bar{q}$  (6 jets)

Signal	Efficiency × purity
2 jets	88.4%
6 jets	1.8%

20 event-shape variables are combined with the multi-variate analysis to separate 2, 4, and 6 jets final-states.

# Event Shape Variables

## Heavy Jet Mass

$$M_1^2 = \frac{1}{(\sqrt{s})^2} \left( \sum_i^N P_i \right)^2$$

$$M_2^2 = \frac{1}{(\sqrt{s})^2} \left( \sum_i^N P_i \right)^2$$

## Jet Broadening

$$B_1 = \frac{1}{2 \sum_{j=1}^N |P_j|} \sum_{i=1}^N |P_i \times n_T|, (P_i \times n_T) > 0$$

$$B_2 = \frac{1}{2 \sum_{j=1}^N |P_j|} \sum_{i=1}^N |P_i \times n_T|, (P_i \times n_T) < 0$$

## Jet Transition variable, $y_{23}$ , $y_{45}$ , $y_{67}$

ee-kt jet clustering algorithm

$$d_{ij} = 2 \min(E_i^2, E_j^2) (1 - \cos \theta_{ij})$$

## C and D Parameter

$$L^{ab} = \frac{1}{\sum_{j=1}^N |P_j|} \sum_{i=1}^N \frac{P_i^a P_i^b}{|P_i|}$$

$$C = 3(\lambda_1 \lambda_2 + \lambda_1 \lambda_3 + \lambda_2 \lambda_3)$$

$$D = 27 \lambda_1 \lambda_2 \lambda_3$$

## Energy-Energy Correlation

$$EEC = \frac{1}{\sigma_{tot}} \sum_{ij} \int d\sigma \frac{E_i E_j}{Q^2} \delta(\cos \chi - \cos \theta_{ij})$$

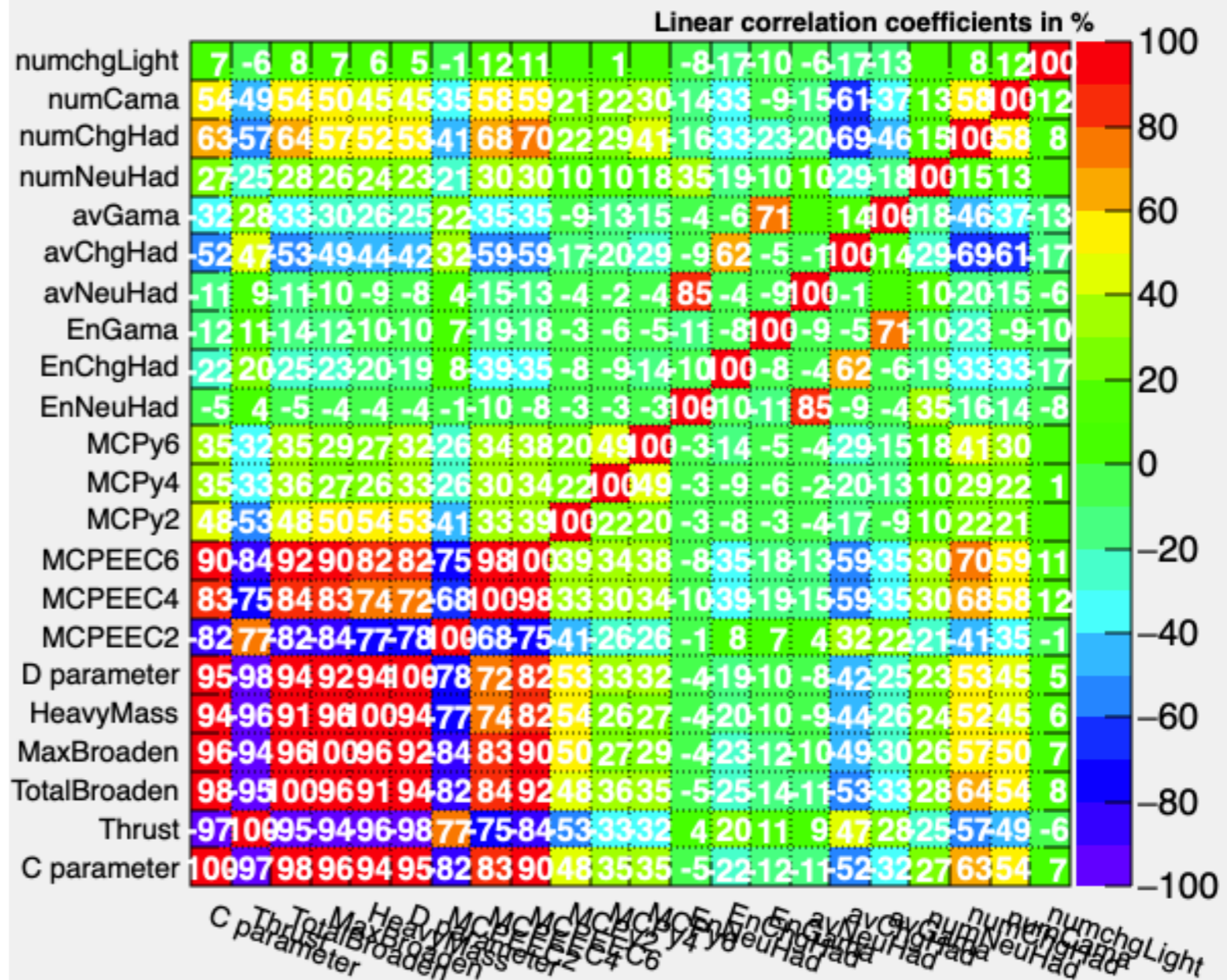
$$likelihood = \frac{\sum (P1_i) \times P2_i}{\sqrt{\sum (P1_i \times P2_i) \times \sum (P2_i \times P2_i)}}$$

# BM2: Number of Jet Identification

**20 Variables**

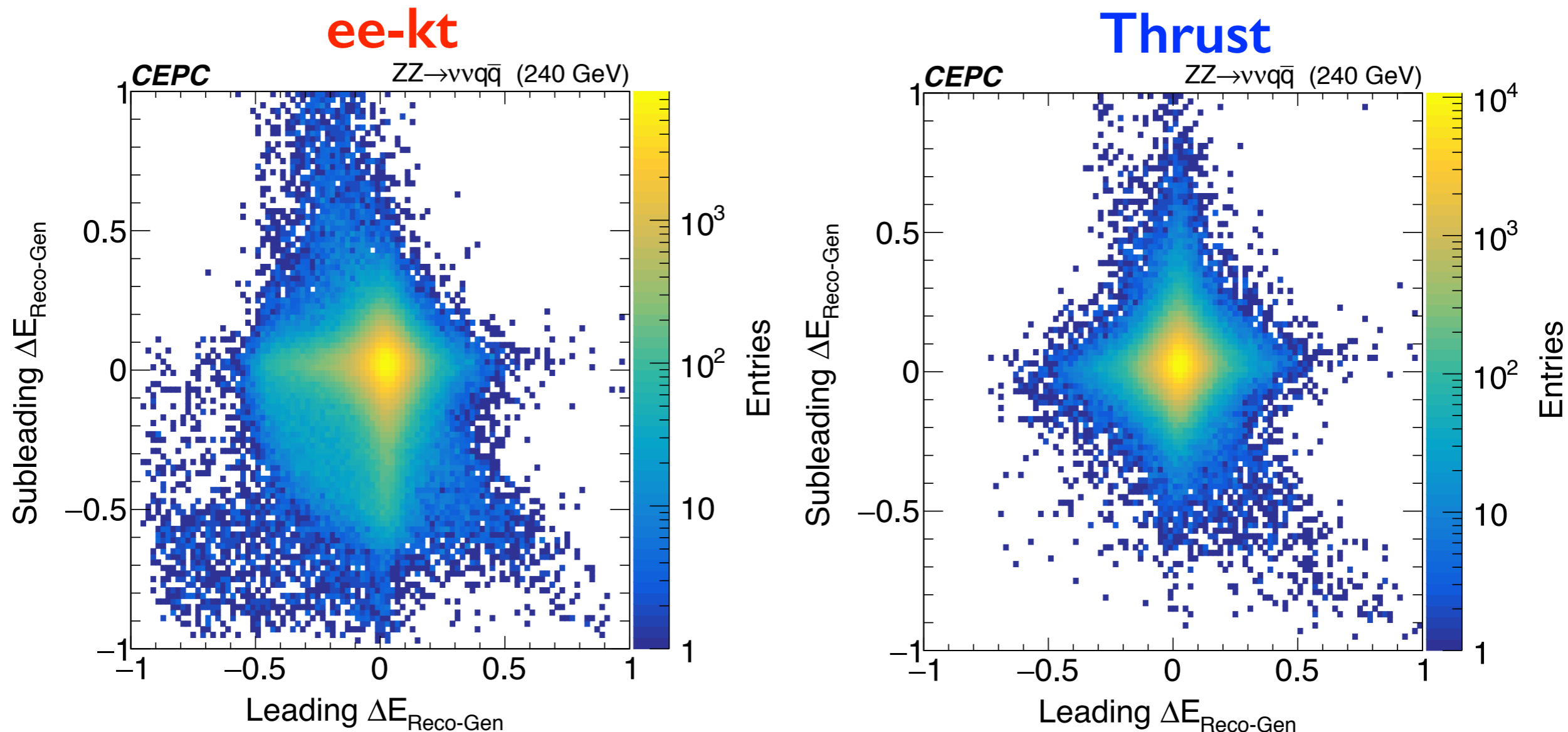
# of charge lepton	EEC 6
# of $\gamma$	EEC 4
# of charge hadron	EEC 2
# of neutro hadron	C parameter
$\bar{E}_\gamma$	D parameter
$\bar{E}_{\text{Charge hadron}}$	Heavy Mass
$\bar{E}_{\text{Neutro hadron}}$	Max Broaden
$E_\gamma$	Total Broaden
$E_{\text{Charge hadron}}$	Thrust
$E_{\text{Neutro hadron}}$	$y_{23}, y_{45}, y_{67}$

Correlation Matrix (signal)



- Event-shape variables basic multi-variable analysis to separate 2, 4, and 6 jets final-state.

# BM3: Thrust Jet Clustering Method



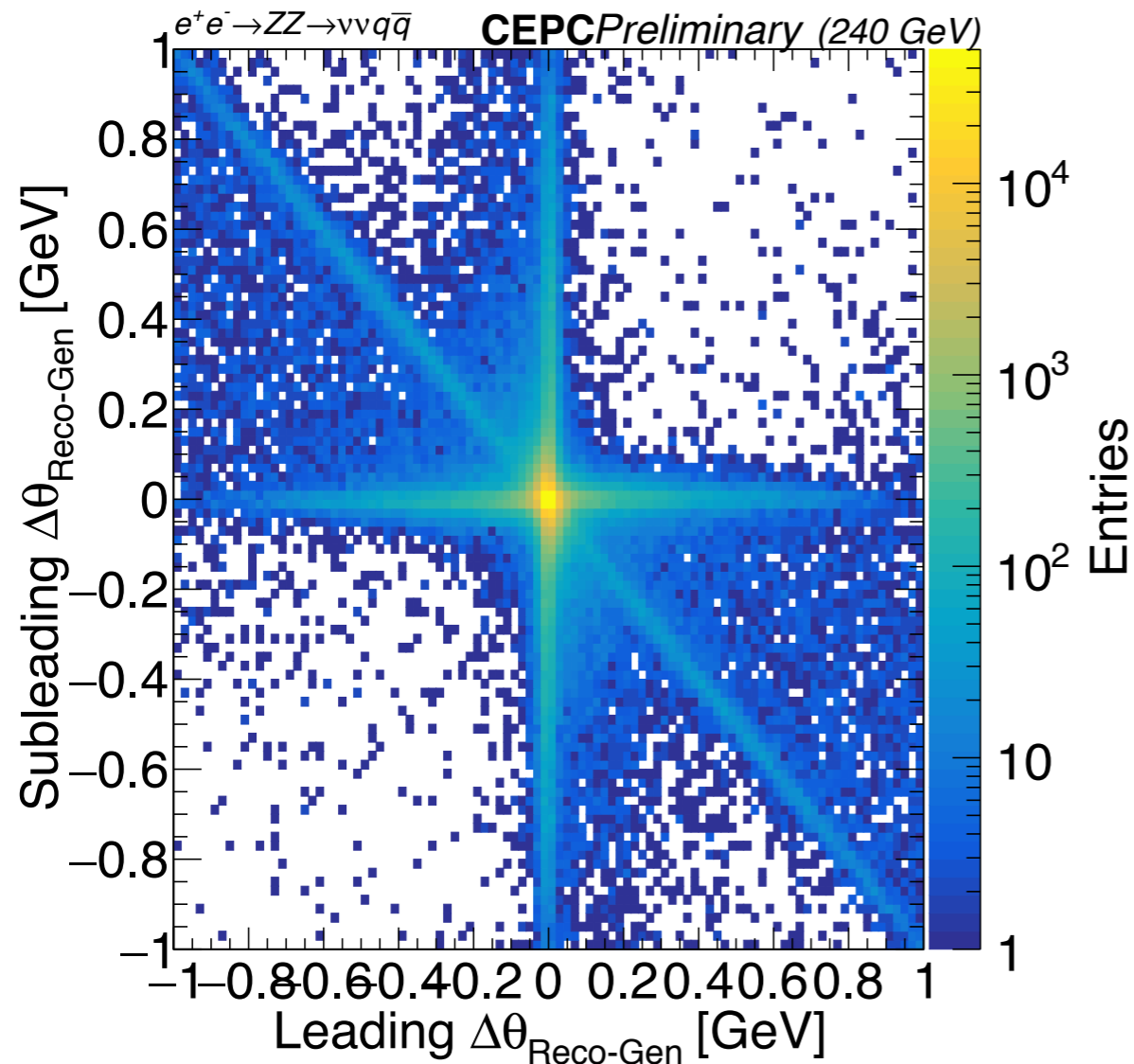
- Identify the 2 jets event with (efficiency x purity) = **88.4%**
  - The thrust jet clustering method
- After “cleaned” selection, the thrust method has **suppressed the tail significantly**
  - Expected to have improvement on jet energy and angular response.

Cleaned: Select the light flavor jet event with low energy ISR, low energy neutrino inside jet, and within  $|\cos\theta| < 0.85$ .

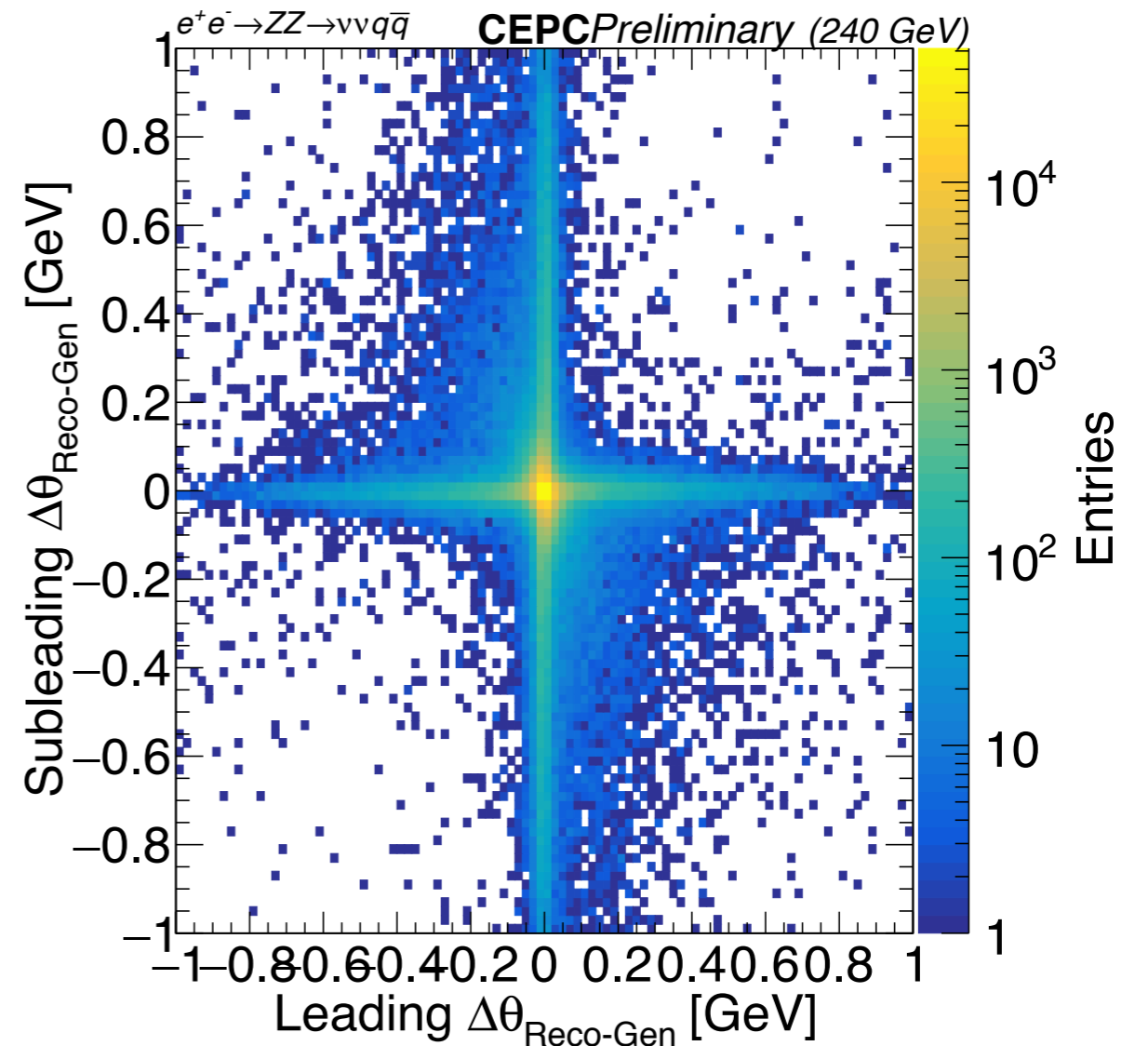


# Matching Impact

## Energy Matching

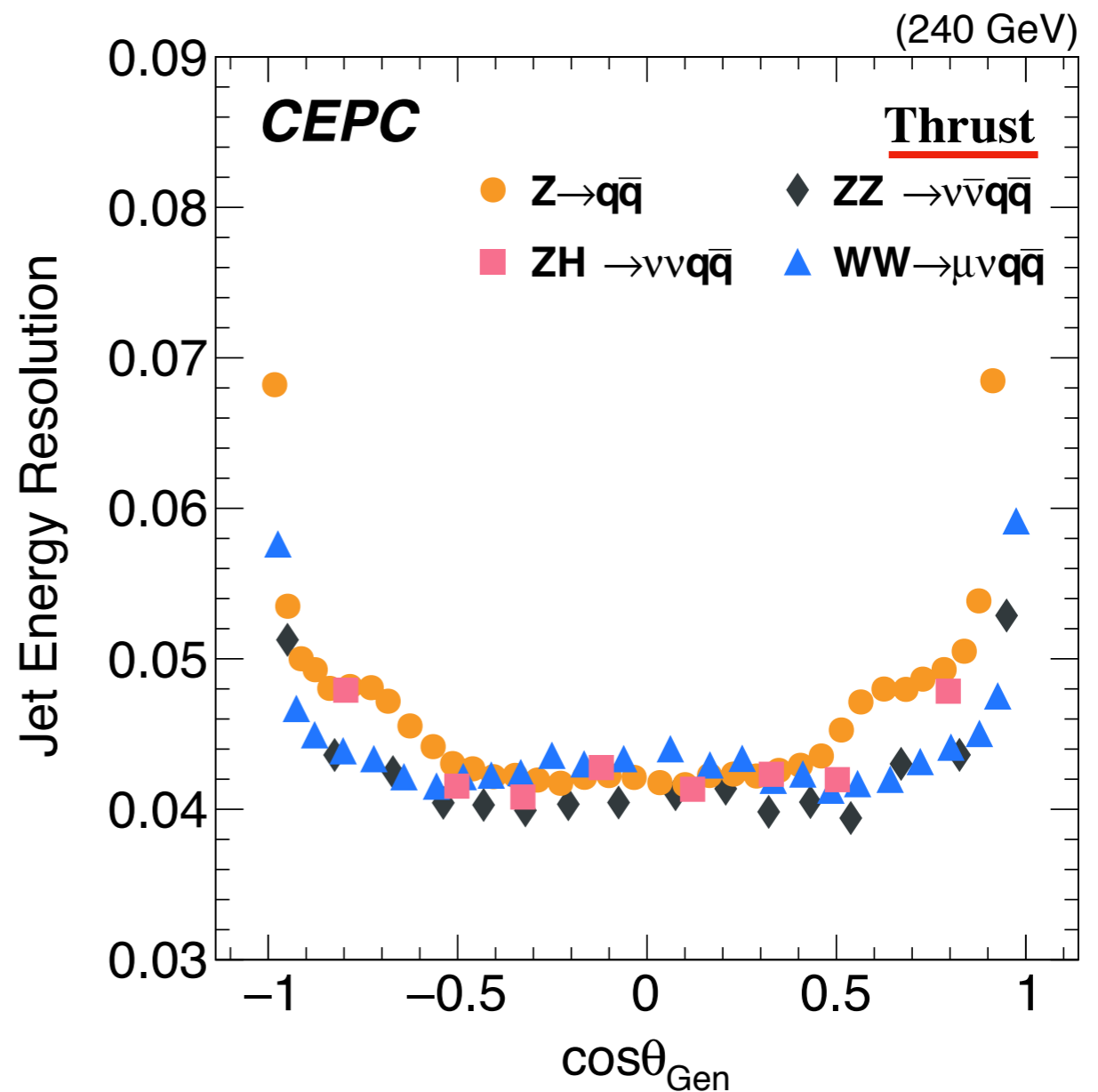
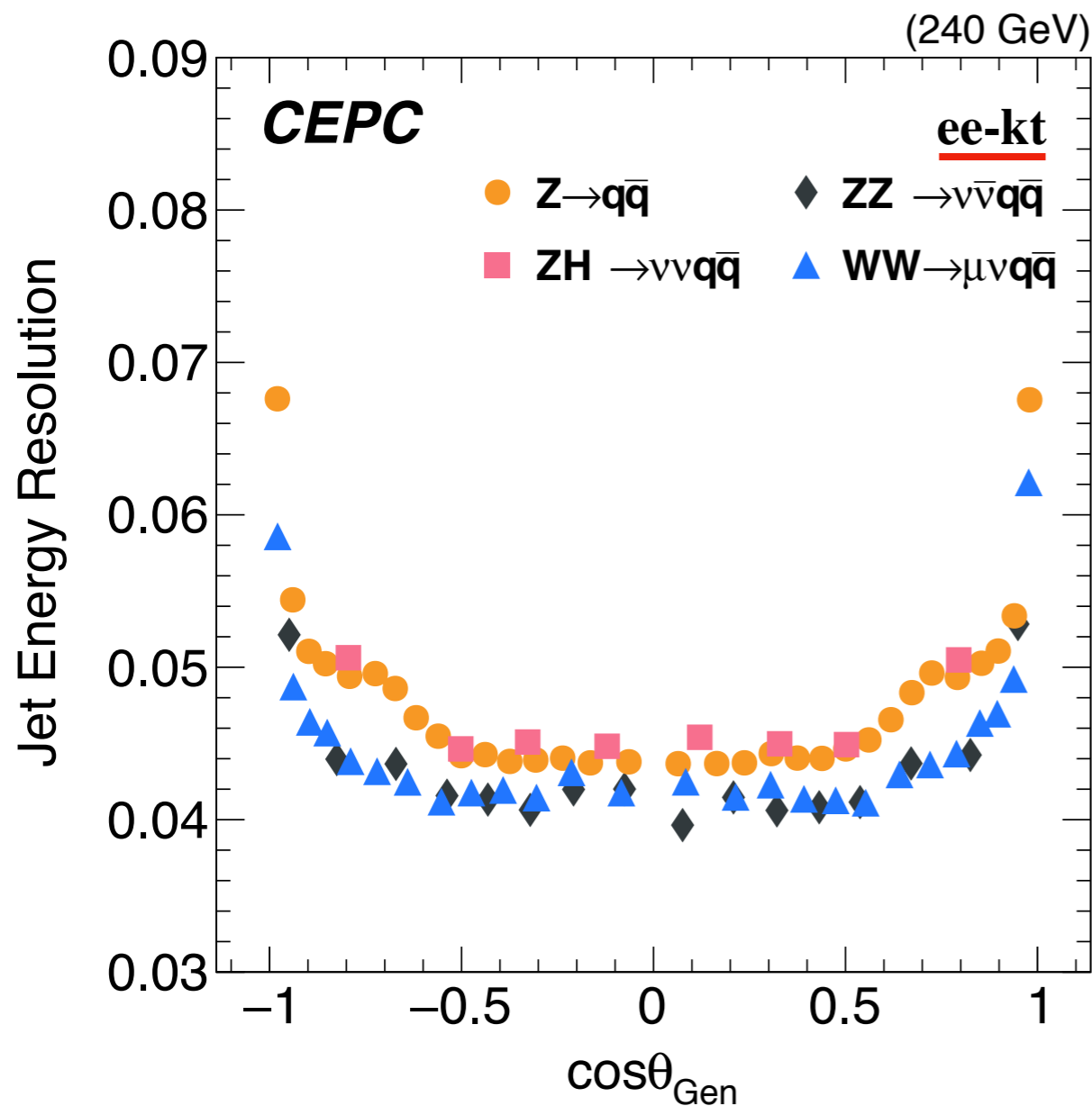


## $\Delta R$ Matching



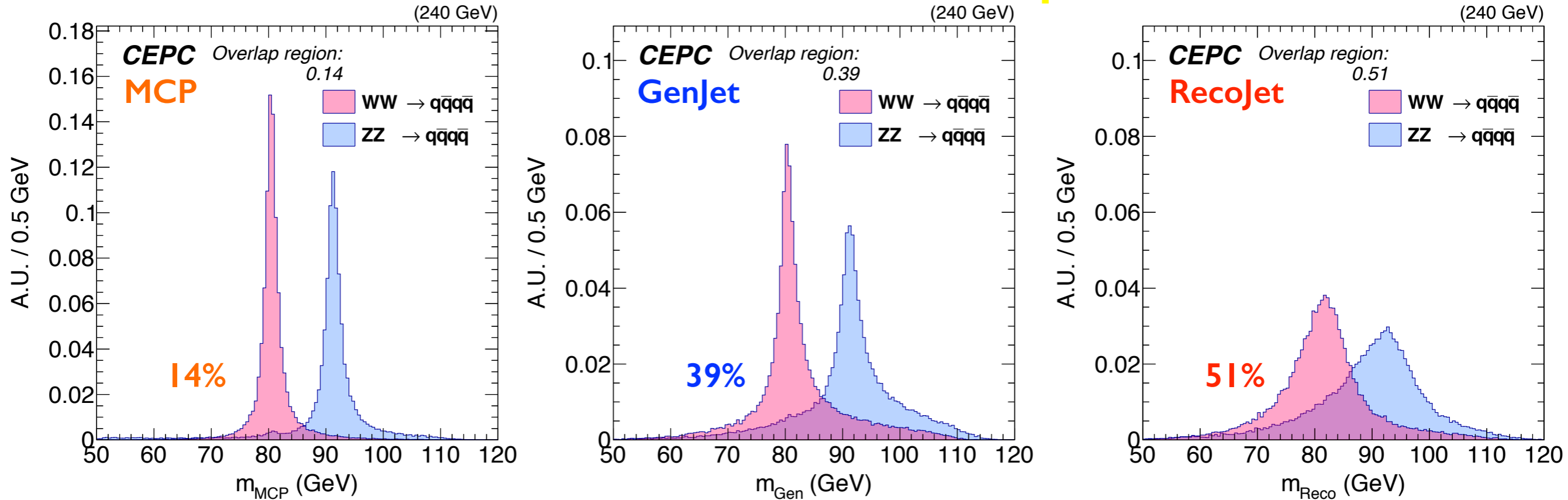
Both after being applied the cleaned selection

# BM3: JER (ee-kt—Thrust)



- ZH and Z-pole processes are improved  $\sim 10\%$  in  $|\cos\theta| < 0.5$ , while ZZ and WW are degraded by thrust based algorithm. (**Need more investigation**)

# BM4: WW & ZZ to 4-jet Separation



■  $E_j \sim (20 \sim 120 \text{ GeV}) \rightarrow$  Low energy

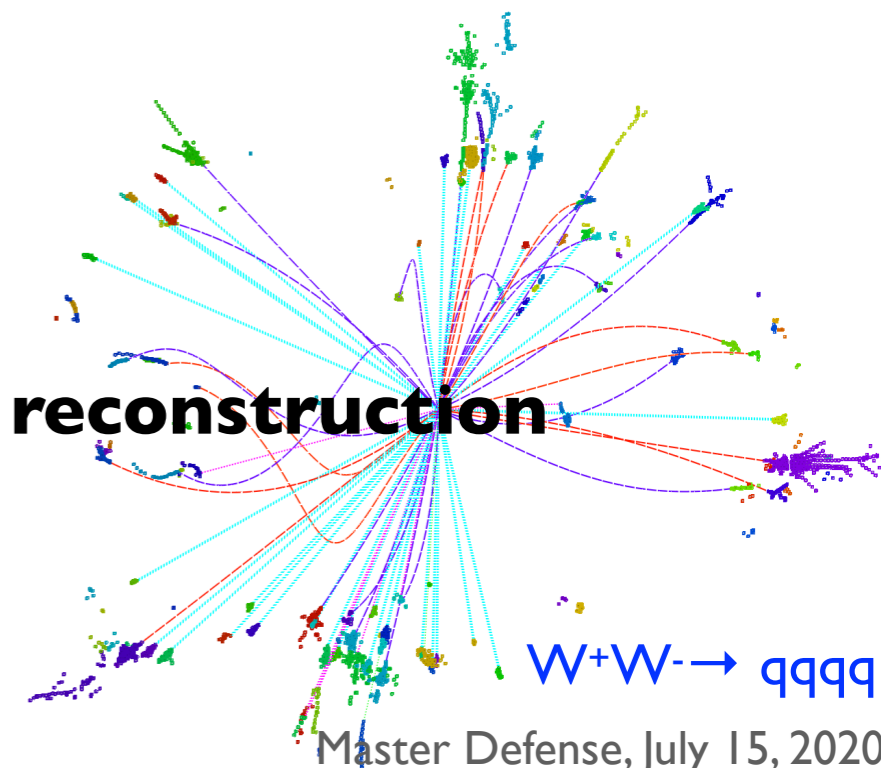
■ Typical multiplicity  $\rightarrow$  Up to  $10^2$

■ Jets are clustered by ee-kt and paired by  $\chi^2$ .

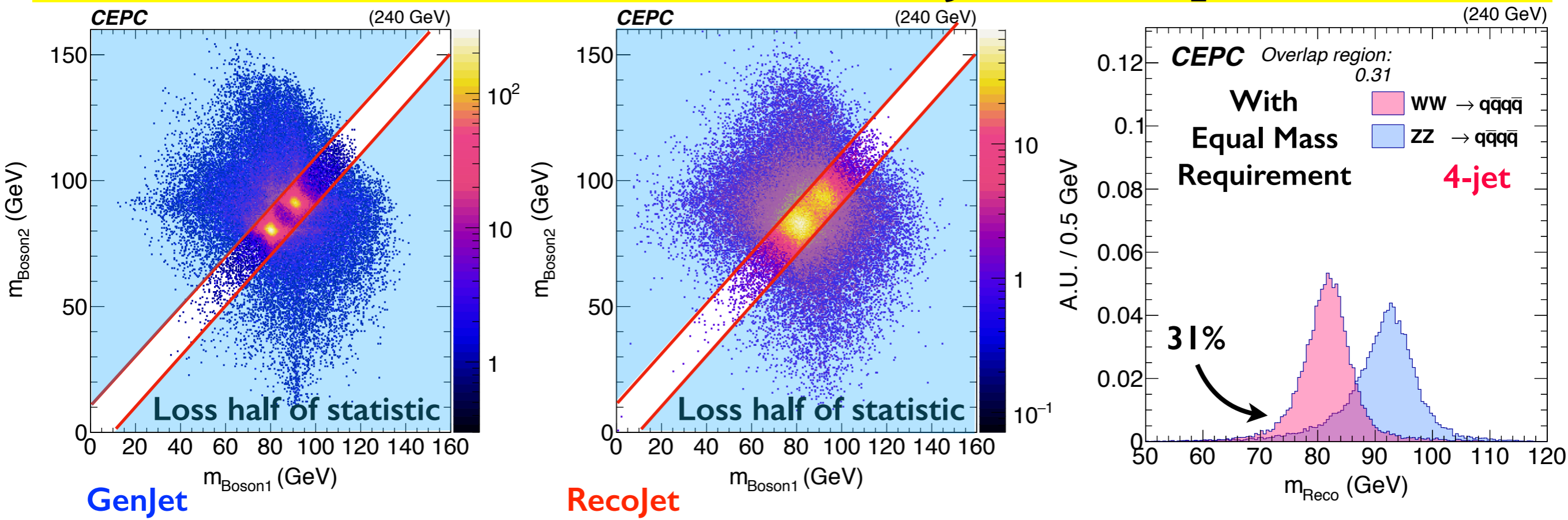
■ Separation of WW & ZZ to 4 jets is determined by:

- 25%  $\rightarrow$  1. (14%) Intrinsic boson mass/width (10 GeV)
- 2. (39%) **Wrong jet pairing for color singlet reconstruction**
- $\rightarrow$  **Jet Clustering & Pairing**
- 12%  $\rightarrow$  3. (51%) Detector response

$$\chi^2 = |(m_1 - m_{boson})| + |(m_2 - m_{boson})|$$



# BM4: WW & ZZ to 4-jet Separation

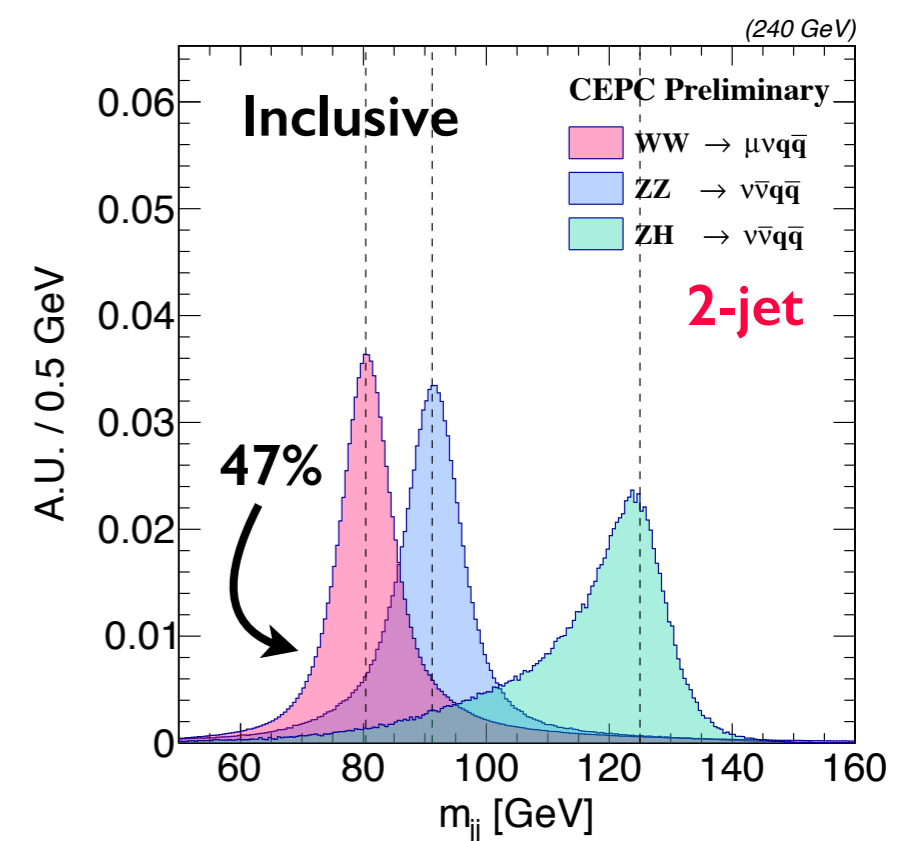


■ **Equal mass requirement:**  $|M_{12} - M_{34}| < 10 \text{ GeV}$

- Cost half of the statistic.
- Overlapping region can be reduced from 51%/39% to 31%/15% for the RecoJet/GenJet.

■ **CEPC baseline could separate WW & ZZ with full hadronic final-state**

■ Need to improve the naive jet pairing method.



# ZH Full Hadronic Statistical Uncertainty

- According to the final results, the following estimation could be declared:  
The identified efficiency of ZH signal is 60% with background, 20% ZZ and 10% WW.  
The cross section of ZZ is 5 times amount than ZH, 10 times from WW.

	Efficiency	XS			
WW	10%	10	→	100	Purity → $60/200$ = 30%
ZZ	20%	5	→	100	
ZH	60%	1	→	60	

Efficiency x Purity

$$60\% \times 30\% = 18\%$$

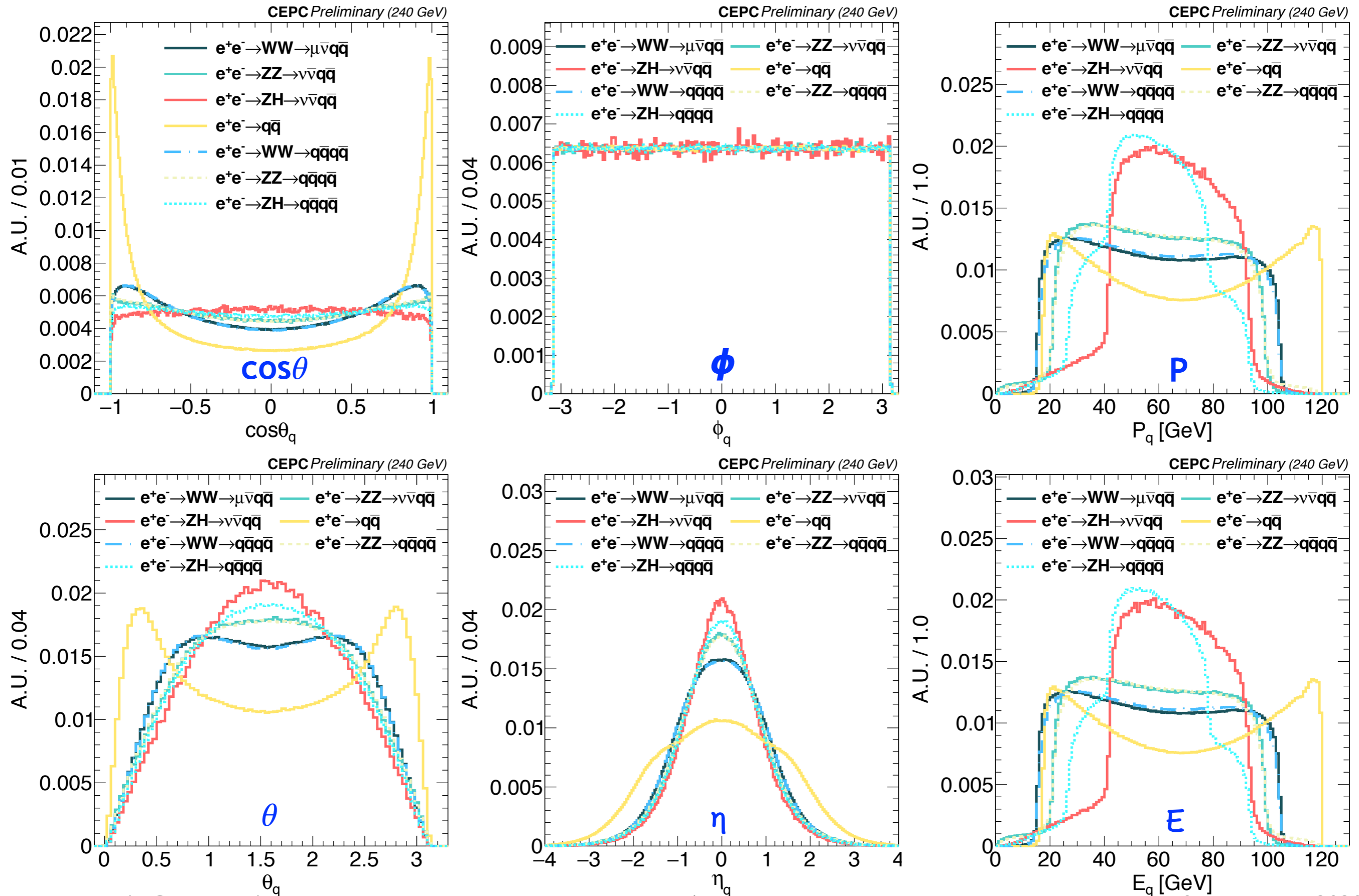


# of ZH = 500,000 in the 5 ab<sup>-1</sup>

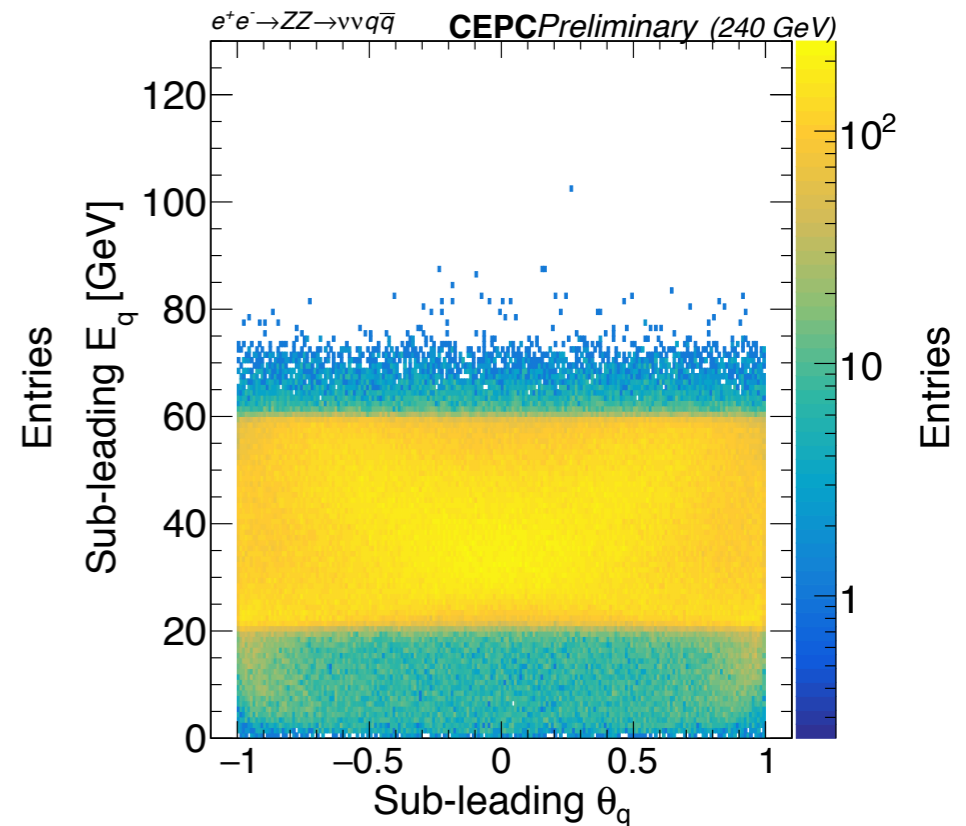
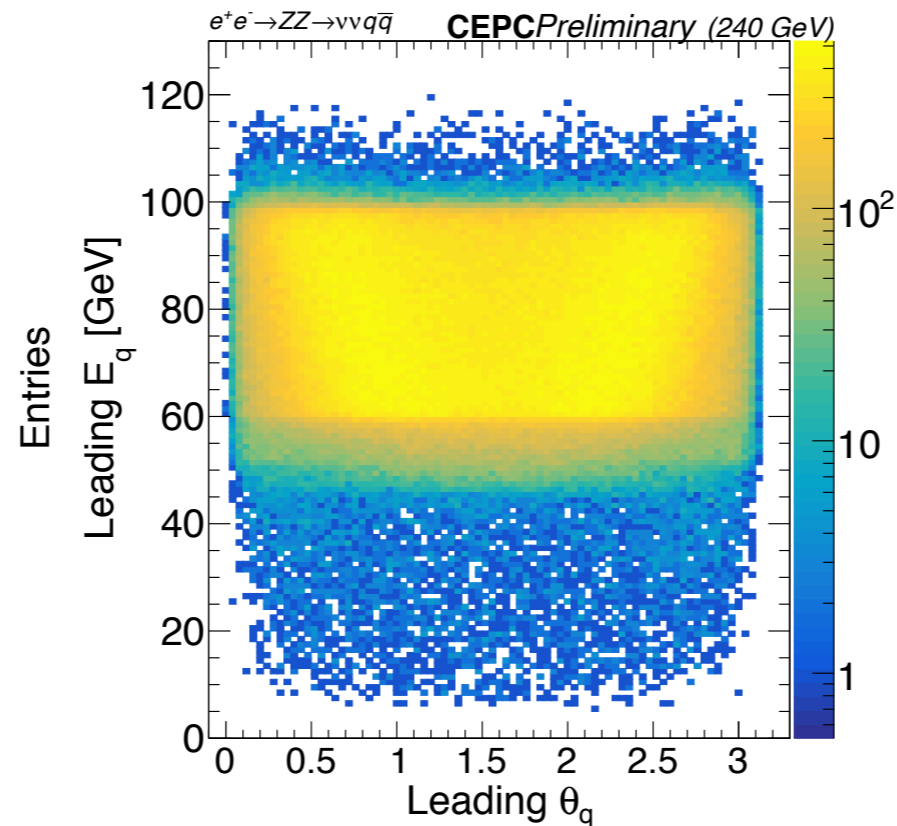
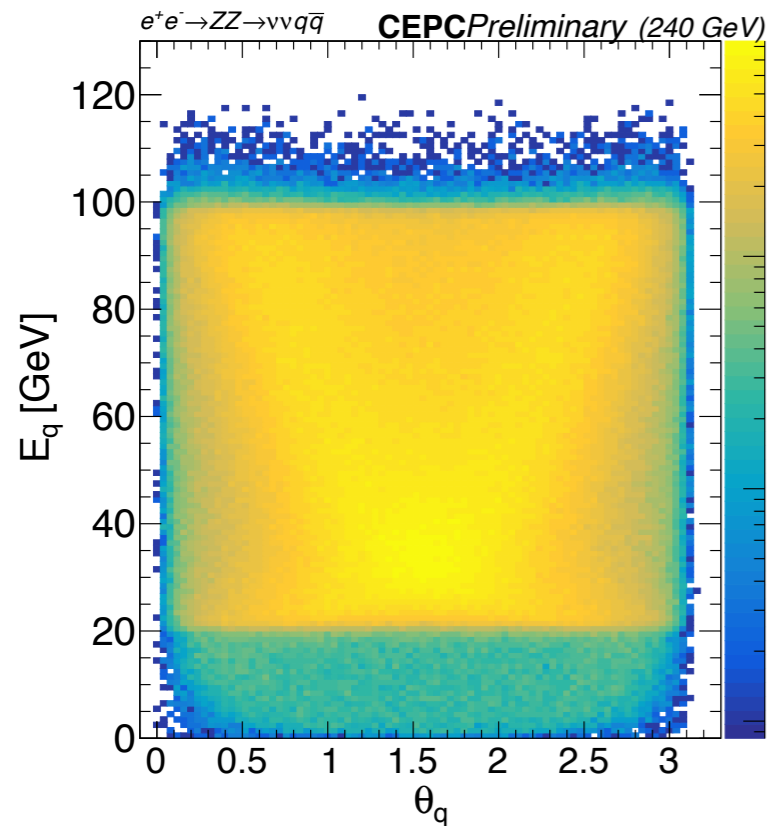
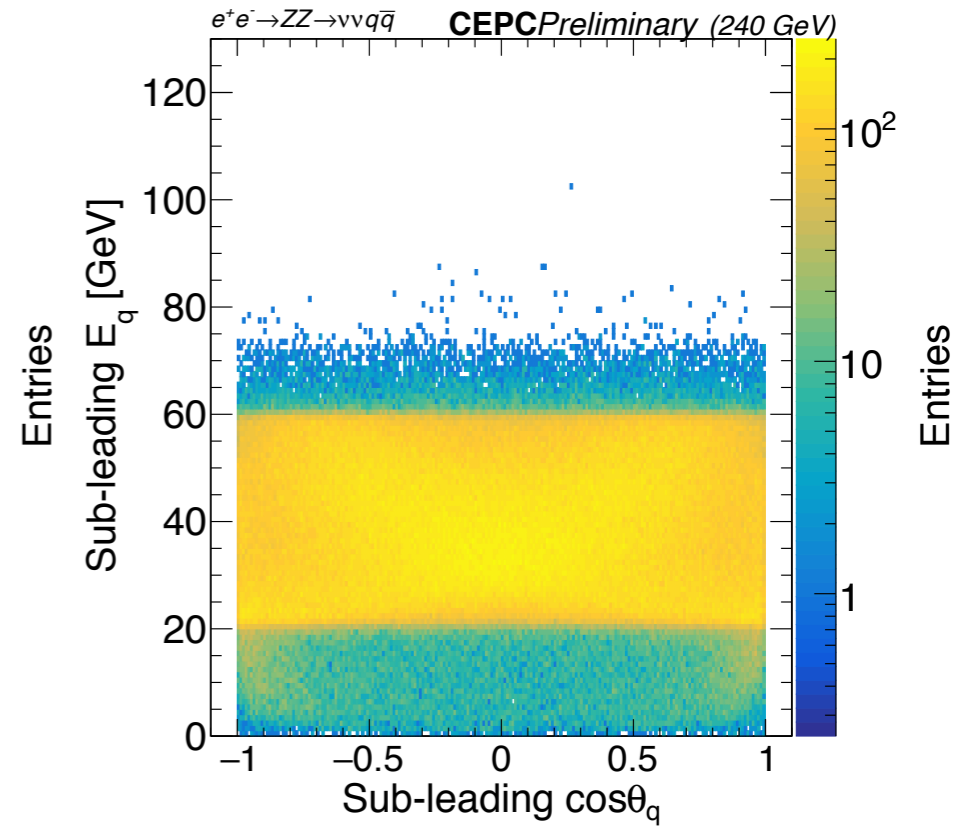
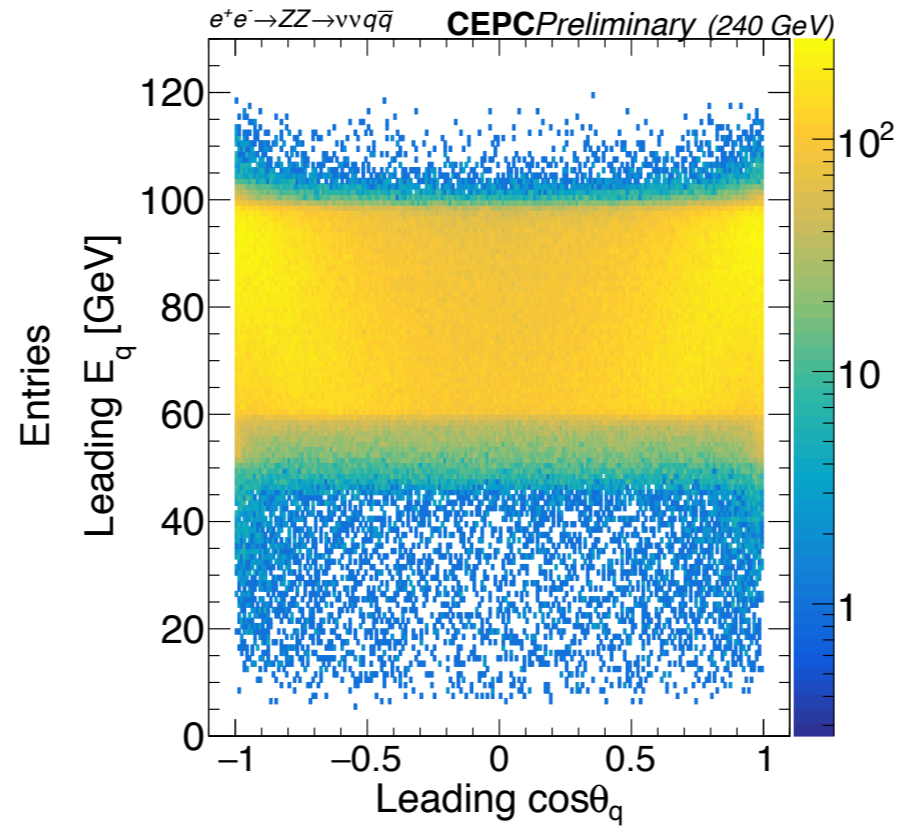
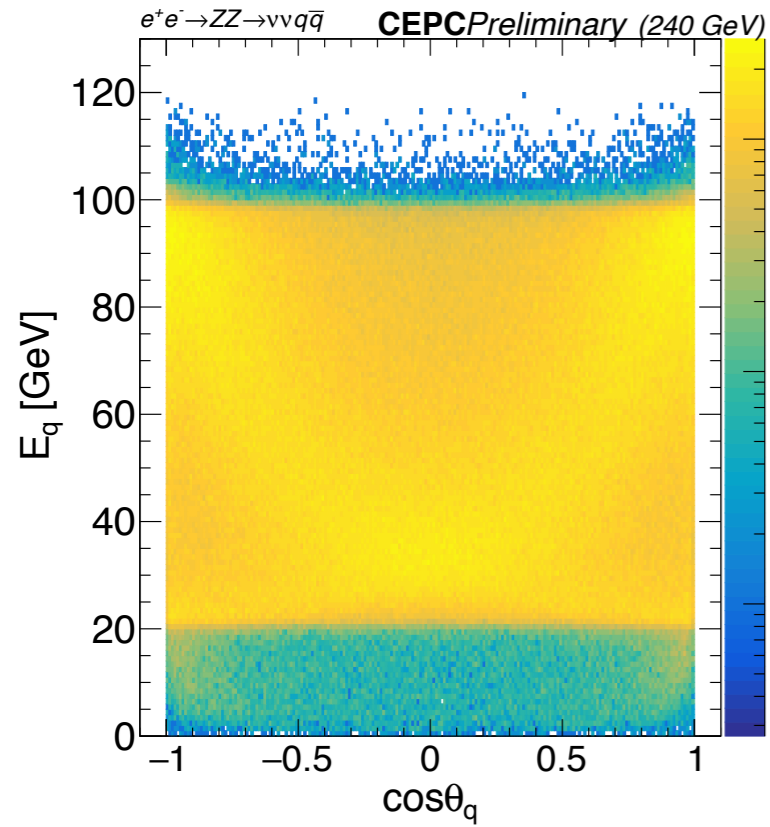
500,000 x 18% = 150,000 could be identified

$$1 / \text{sqrt}(150,000) = 0.25\%$$

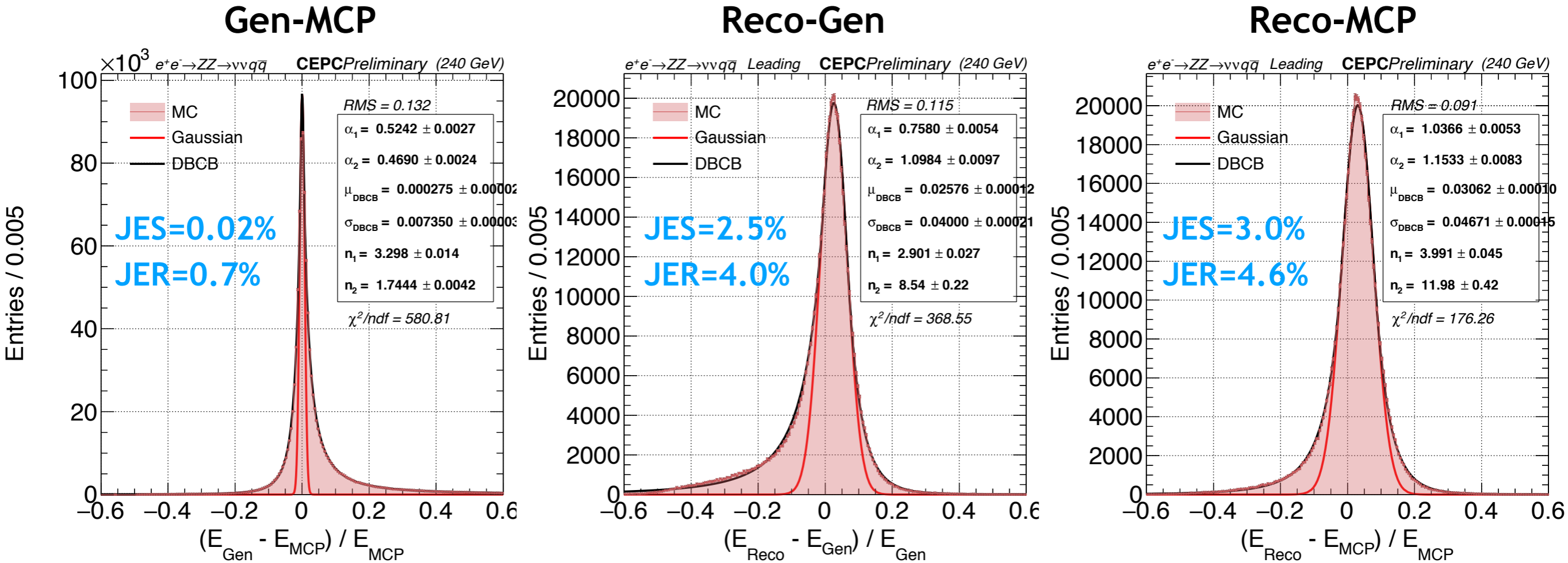
# Kinematic Summary Plots (Parton level)



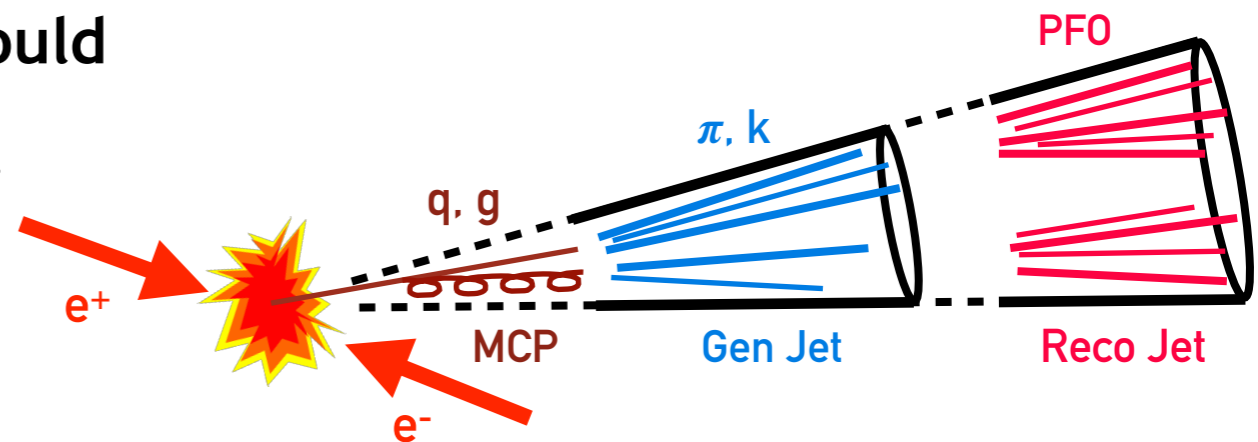
# E as a Function of the Polar Angle



# Leading JER & JES



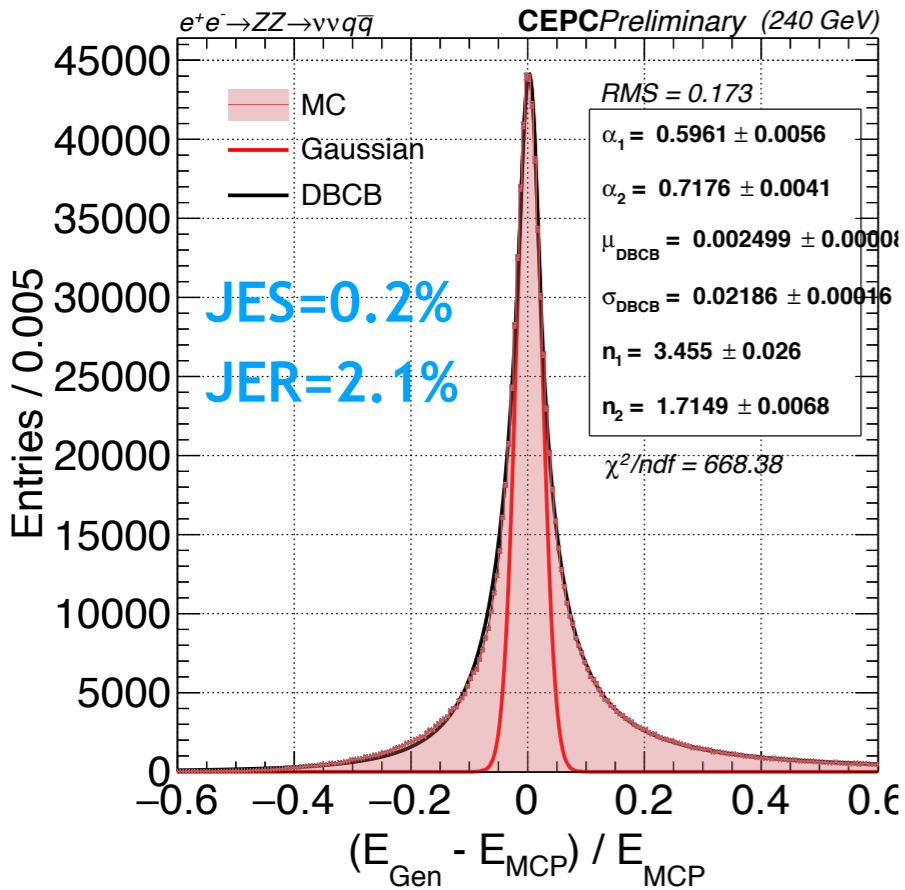
■ JER/JES between Reco jet and MCP would combine the effects of two previous stages.



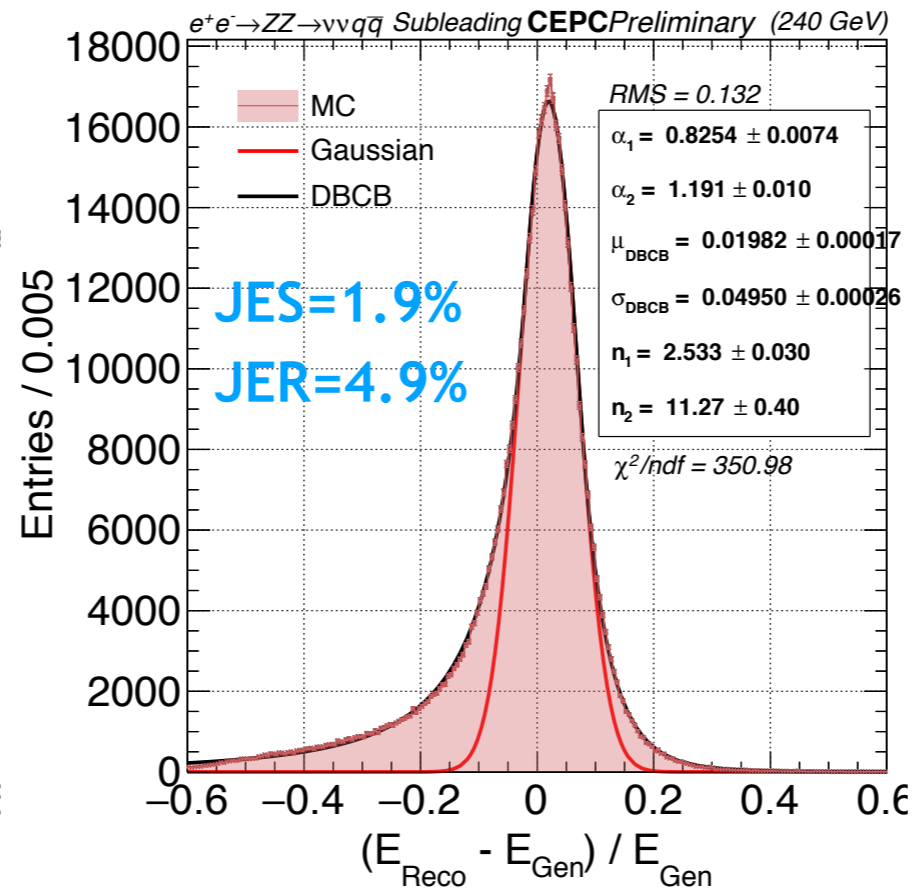


# Sub-leading JER & JES

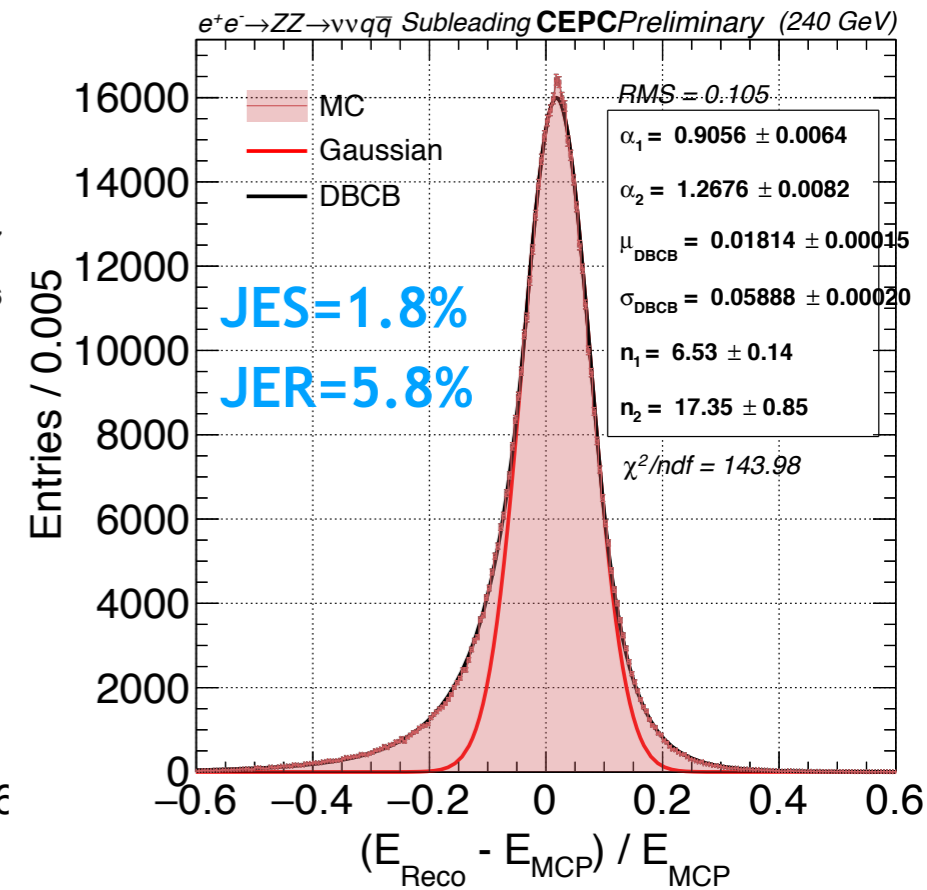
## Gen-MCP



## Reco-Gen



## Reco-MCP



■ JER/JES between Reco jet and MCP would combine the effects of two previous stages.

