

$QQ\bar{Q}\bar{Q}$ tetraquark states

Hua-Xing Chen

Beihang University & Southeast University

Based on: Wei Chen, Hua-Xing Chen, Xiang Liu, T. G. Steele, and Shi-Lin Zhu, Phys.Lett. B773, 247-251 (2017)

Doubly hidden-flavor tetraquarks: $QQ\bar{Q}\bar{Q}$

$QQ\bar{Q}\bar{Q}$ Tetraquarks:

- They are far away from the mass range of the observed conventional $q\bar{q}$ hadrons.
- Can be clearly distinguished experimentally from the normal states.
- The light mesons ($\pi, \rho, \omega, \sigma \dots$) can not be exchanged between two charmonia/bottomonia.
- The binding force comes from the short-range gluon exchange.
- A molecule configuration is not favored and thus the $QQ\bar{Q}\bar{Q}$ is a good candidate for compact tetraquark.



Theoretical works:

- Quark-Gluon models: *Prog. Theor. Phys.* 54, 492 (1975); *Zeit. Phys.* C7, 317 (1981).
- Potential model: *Phys.Rev.* D25, 2370 (1982); *Phys. Lett.* B123, 449 (1983).
- MIT bag model: *Phys. Rev.* D32, 755 (1985).
- Hyperspherical harmonic formalism: *Phys. Rev.* D73, 054004 (2006).
- BS or Schroedinger Eqs: *Phys.Rev.*D86, 034004 (2012); *Phys.Lett.*B718, 545 (2012).
- Recent studies: [arXiv:1605.01134](https://arxiv.org/abs/1605.01134); [1605.01647](https://arxiv.org/abs/1605.01647); [1612.00012](https://arxiv.org/abs/1612.00012); *PRD*95, 034011 (2017); *EPJC*77, 432 (2017); [arXiv:1706.07553](https://arxiv.org/abs/1706.07553).

Experiments:

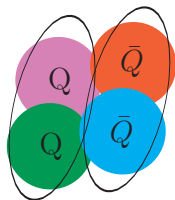
- $J/\psi J/\psi$ pairs: *Phys. Lett.* B707, 52 (2012) (LHCb); *JHEP* 1409, 094(2014) (CMS); *Phys. Rev.* D90, 111101 (2014) (D0).
- $J/\psi \Upsilon(1S)$ events: *Phys. Rev. Lett.* 116, 082002 (2016) (D0); K. Dilsiz's talk at APS April Meeting 2016 on behalf of CMS, see <https://absuploads.aps.org/presentation.cfm?pid=11931>.
- $\Upsilon(1S)\Upsilon(1S)$ pairs: *JHEP* 05, 013 (2017) (CMS).

Tetraquark Sum Rules

- Study **two-point correlation function** of current $J(x)$ with the same quantum numbers with hadron state:

$$\Pi(q^2) = i \int d^4x e^{iq \cdot x} \langle \Omega | T[J(x) J^\dagger(0)] | \Omega \rangle$$

- Classify states $|X\rangle$ by coupling to current $\langle \Omega | J(x) | X \rangle \neq 0$
- Currents are **probes of spectrum** and might not overlap with state



Interpolating currents with $J^{PC} = 0^{++}$:

$$J_1 = Q_a^T C \gamma_5 Q_b \bar{Q}_a \gamma_5 C \bar{Q}_b^T,$$

$$J_2 = Q_a^T C \gamma_\mu \gamma_5 Q_b \bar{Q}_a \gamma^\mu \gamma_5 C \bar{Q}_b^T,$$

$$J_3 = Q_a^T C \sigma_{\mu\nu} Q_b \bar{Q}_a \sigma^{\mu\nu} C \bar{Q}_b^T,$$

$$J_4 = Q_a^T C \gamma_\mu Q_b \bar{Q}_a \gamma^\mu C \bar{Q}_b^T,$$

$$J_5 = Q_a^T C Q_b \bar{Q}_a C \bar{Q}_b^T,$$

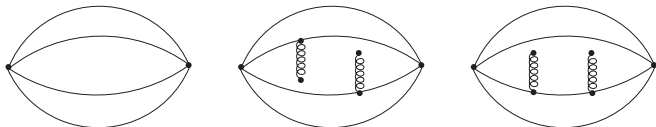
- **Hadron level:** described by the **dispersion relation**

$$\Pi(q^2) = \frac{(q^2)^N}{\pi} \int \frac{\text{Im}\Pi(s)}{s^N(s - q^2 - i\epsilon)} ds + \sum_{n=0}^{N-1} b_n (q^2)^n,$$

$$\begin{aligned} \rho(s) &= \frac{1}{\pi} \text{Im}\Pi(s) = \sum_n \delta(s - m_n^2) \langle 0 | J | n \rangle \langle n | J^\dagger | 0 \rangle \\ &= f_X^2 \delta(s - m_X^2) + \text{continuum}, \end{aligned}$$

- **Quark-gluon level:** evaluated via **operator product expansion(OPE)**

$$\Pi(s) = \Pi^{\text{pert}}(s) + \Pi^{\langle GG \rangle}(s) + \dots,$$



- Define **moments** in Euclidean region $Q^2 = -q^2 > 0$:

$$\begin{aligned}
 M_n(Q_0^2) &= \frac{1}{n!} \left(-\frac{d}{dQ^2} \right)^n \Pi(Q^2) |_{Q^2=Q_0^2} \\
 &= \int_{m_H^2}^{\infty} \frac{\rho(s)}{(s + Q_0^2)^{n+1}} ds = \frac{f_X^2}{(m_X^2 + Q_0^2)^{n+1}} [1 + \delta_n(Q_0^2)],
 \end{aligned}$$

where $\delta_n(Q_0^2)$ contains the higher states and continuum.

- Ratio of the moments

$$r(n, Q_0^2) \equiv \frac{M_n(Q_0^2)}{M_{n+1}(Q_0^2)} = (m_X^2 + Q_0^2) \frac{1 + \delta_n(Q_0^2)}{1 + \delta_{n+1}(Q_0^2)}.$$

- Predict **hadron mass**

$$m_X = \sqrt{r(n, Q_0^2) - Q_0^2}$$

for sufficiently large n when $\delta_n(Q_0^2) \cong \delta_{n+1}(Q_0^2)$ for convergence.

Limitations for (n, ξ) parameter space:

$$\xi = Q_0^2/16m_c^2, \text{ for } cc\bar{c}\bar{c} \text{ system};$$

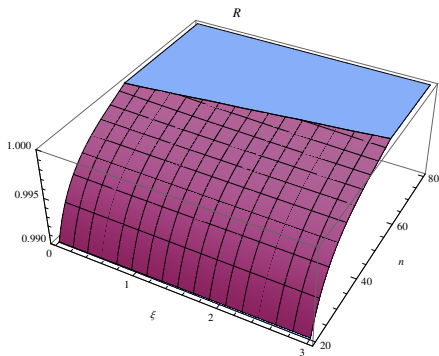
$$\xi = Q_0^2/m_b^2, \text{ for } bb\bar{b}\bar{b} \text{ system.}$$

- **Small ξ** : higher dimensional condensates give large contributions to $M_n(Q_0^2)$, leading to bad OPE convergence.
- **Large ξ** : slower convergence of $\delta_n(Q_0^2)$. This can be compensated by taking higher derivative n for the lowest lying resonance to dominate.
- **Large n** : moving further away from the asymptotically free region. The OPE convergence would also become bad.
- Requiring $\Pi^{(GG)}(s) \leq \Pi^{pert}(s)$ to obtain an upper limit n_{max} , which will increase with respect to ξ .
- **Good (n, ξ) region**: the lowest lying resonance dominates the moments while the OPE series has good convergence.

$$n_{max} = 75, 76, 77, 78 \text{ for } \xi = 0.2, 0.4, 0.6, 0.8$$

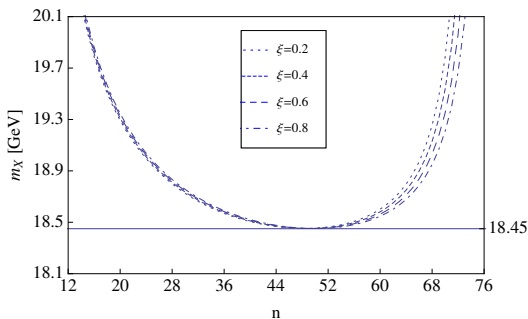
Hölder's inequality:

$$R = \frac{M_n(Q_0^2)^2}{M_r(Q_0^2)M_{2n-r}(Q_0^2)} \leq 1,$$



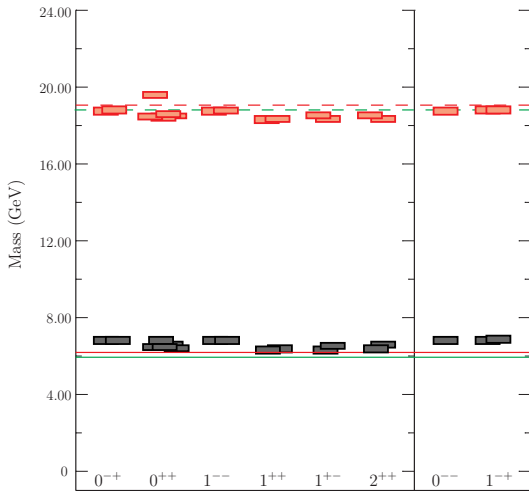
The boundary gives $(n, \xi) = (48, 0.2), (49, 0.4), (49, 0.6), (50, 0.8)$.

Mass for scalar $bb\bar{b}\bar{b}$ tetraquark: mass curves have plateaus at
 $(n, \xi) = (48, 0.2), (49, 0.4), (49, 0.6), (50, 0.8)$



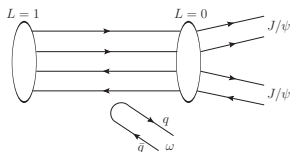
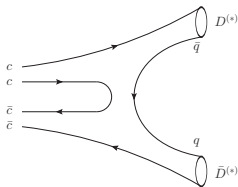
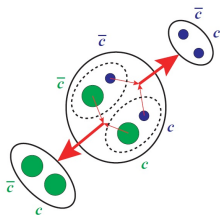
$$m_{X_b} = (18.45 \pm 0.15) \text{ GeV.}$$

J^{PC}	Currents	$m_{X_c}(\text{GeV})$	$m_{X_b}(\text{GeV})$
0^{++}	J_1	6.44 ± 0.15	18.45 ± 0.15
	J_2	6.59 ± 0.17	18.59 ± 0.17
	J_3	6.47 ± 0.16	18.49 ± 0.16
	J_4	6.46 ± 0.16	18.46 ± 0.14
	J_5	6.82 ± 0.18	19.64 ± 0.14
1^{++}	$J_{1\mu}^+$	6.40 ± 0.19	18.33 ± 0.17
	$J_{2\mu}^+$	6.34 ± 0.19	18.32 ± 0.18
1^{+-}	$J_{1\mu}^-$	6.37 ± 0.18	18.32 ± 0.17
	$J_{2\mu}^+$	6.51 ± 0.15	18.54 ± 0.15
2^{++}	$J_{1\mu\nu}$	6.51 ± 0.15	18.53 ± 0.15
	$J_{2\mu\nu}$	6.37 ± 0.19	18.32 ± 0.17
0^{-+}	J_1^+	6.84 ± 0.18	18.77 ± 0.18
	J_2^+	6.85 ± 0.18	18.79 ± 0.18
0^{--}	J_1^-	6.84 ± 0.18	18.77 ± 0.18
1^{-+}	$J_{1\mu}^+$	6.84 ± 0.18	18.80 ± 0.18
	$J_{2\mu}^+$	6.88 ± 0.18	18.83 ± 0.18
1^{--}	$J_{1\mu}^-$	6.84 ± 0.18	18.77 ± 0.18
	$J_{2\mu}^-$	6.83 ± 0.18	18.77 ± 0.16



Decay behavior: $cc\bar{c}\bar{c}$ tetraquarks

- $cc\bar{c}\bar{c} \rightarrow (c\bar{c}) + (c\bar{c})$: charm quark pair **rearrangement** or annihilation.
- $cc\bar{c}\bar{c} \rightarrow (q\bar{c}) + (c\bar{q})$: **possible** via a heavy quark pair annihilation and a light quark pair creation.
- $cc\bar{c}\bar{c} \rightarrow (cq\bar{q}) + (\bar{c}\bar{q}\bar{q})$: **suppressed** by two light quark pair creation.
- $cc\bar{c}\bar{c}(L=1) \rightarrow cc\bar{c}\bar{c}(L=0) + (q\bar{q})_{J=0}$: **OZI forbidden**.
- These $cc\bar{c}\bar{c}$ states may not be very narrow.



The $bb\bar{b}\bar{b}$ tetraquarks lie below two bottomonium thresholds:

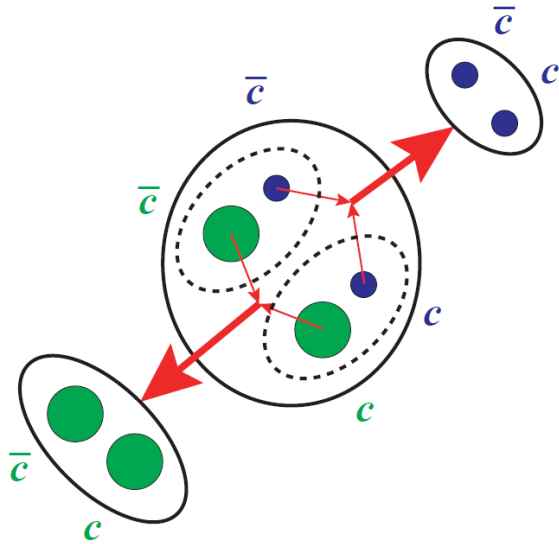
- $bb\bar{b}\bar{b} \rightarrow (b\bar{b}) + (b\bar{b})$: kinematically forbidden.
- $bb\bar{b}\bar{b} \rightarrow (q\bar{b}) + (b\bar{q})$: possible via a heavy quark pair annihilation and a light quark pair creation.
- $bb\bar{b}\bar{b} \rightarrow (b\bar{b}) + \gamma$: electromagnetic decay via $b\gamma_\mu\bar{b} \rightarrow \gamma$ photon production process.
- These $bb\bar{b}\bar{b}$ states are expected to be very narrow.

Preliminary

The interpolating currents with $J^{PC} = 0^{-+}$ are

$$J_1 = Q_a^T C Q_b \bar{Q}_a \gamma_5 C \bar{Q}_b^T + Q_a^T C \gamma_5 Q_b \bar{Q}_a C \bar{Q}_b^T ,$$

$$J_2 = Q_a^T C \sigma_{\mu\nu} Q_b \bar{Q}_a \sigma^{\mu\nu} \gamma_5 C \bar{Q}_b^T ,$$

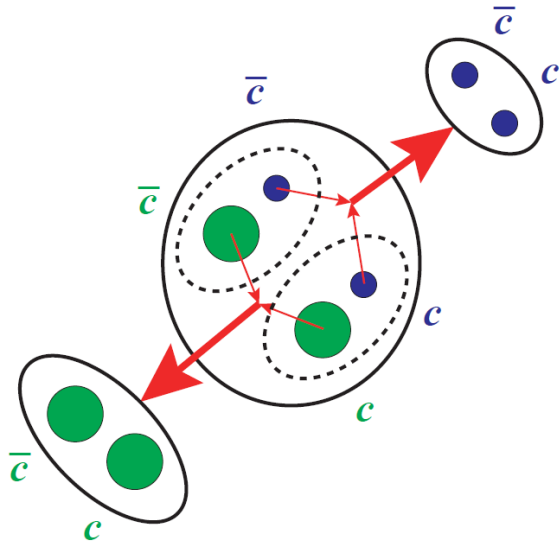


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$$J_1 = 0^- \quad 0^+ \quad + Q_a^T C \gamma_5 Q_b \bar{Q}_a C \bar{Q}_b^T ,$$

$$J_2 = 1^\pm \quad 1^{\mp} ,$$

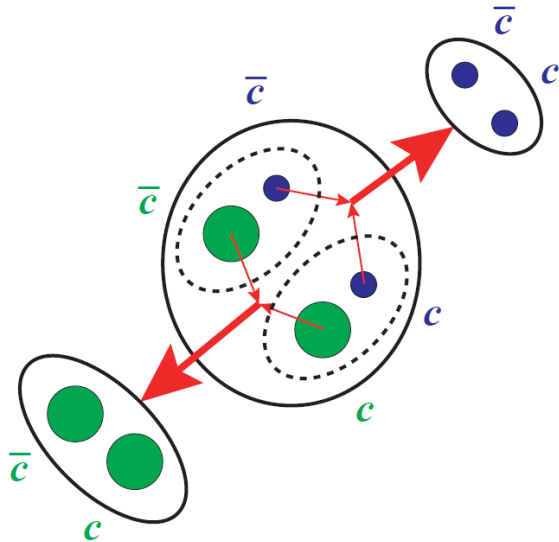


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$$J_2 = Q_a^T C \sigma_{\mu\nu} Q_b \bar{Q}_a \sigma^{\mu\nu} \gamma_5 C \bar{Q}_b^T ,$$



After applying the Fierz transformation, we obtain

$$J_1 \rightarrow -\bar{Q}_a Q_a \bar{Q}_b \gamma_5 Q_b + \frac{1}{4} \bar{Q}_a \sigma_{\mu\nu} Q_a \bar{Q}_b \sigma^{\mu\nu} \gamma_5 Q_b$$

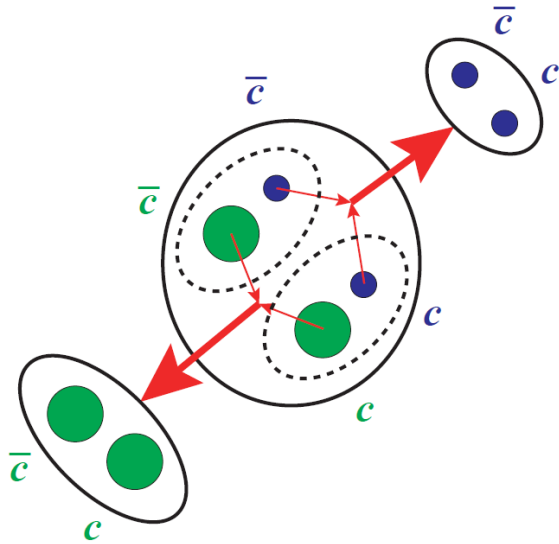
$$J_2 \rightarrow 6 \bar{Q}_a Q_a \bar{Q}_b \gamma_5 Q_b - \frac{1}{2} \bar{Q}_a \sigma_{\mu\nu} Q_a \bar{Q}_b \sigma^{\mu\nu} \gamma_5 Q_b$$

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After applying the Fierz transformation, we obtain

$$J_1 \rightarrow - \mathbf{0}^+ \quad \mathbf{0}^- \quad \frac{1}{4} \quad \mathbf{1}^\pm \quad \mathbf{1}^\mp$$

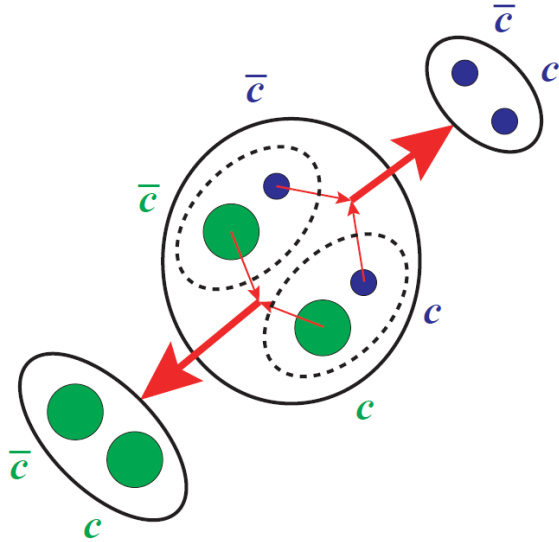
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$\chi_{c0} \eta_c$



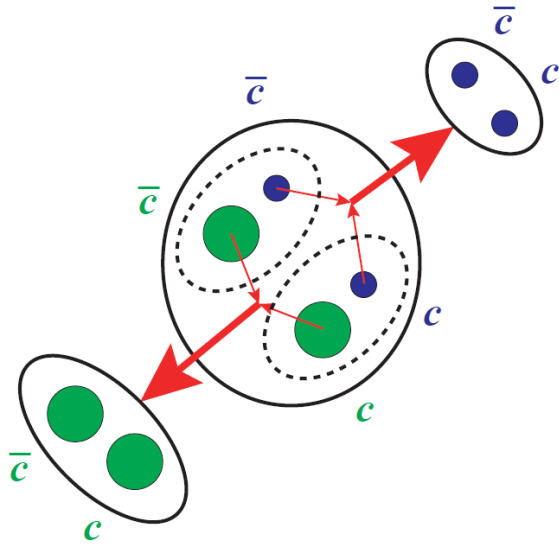
$J/\psi J/\psi, J/\psi h_c, h_c h_c$

Preliminary

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$$J_1 = Q_a^T C Q_b \bar{Q}_a \gamma_5 C \bar{Q}_b^T + Q_a^T C \gamma_5 Q_b \bar{Q}_a C \bar{Q}_b^T ,$$

$$J_2 = Q_a^T C \sigma_{\mu\nu} Q_b \bar{Q}_a \sigma^{\mu\nu} \gamma_5 C \bar{Q}_b^T ,$$



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$$J_2 \rightarrow 6 \bar{Q}_a Q_a \bar{Q}_b \gamma_5 Q_b - \frac{1}{2} \bar{Q}_a \sigma_{\mu\nu} Q_a \bar{Q}_b \sigma^{\mu\nu} \gamma_5 Q_b$$



$\chi_{c0} \eta_c$



$J/\psi J/\psi, J/\psi h_c, h_c h_c$

$$Br(|0^{-}0^{+} \rangle \rightarrow J/\psi J/\psi : J/\psi h_c : \chi_{c0} \eta_c) = 6.3 : 1.3 : 4.3$$

$$Br(|1^{\pm}1^{\mp} \rangle \rightarrow J/\psi J/\psi : J/\psi h_c : \chi_{c0} \eta_c) = 6.3 : 1.3 : 39$$

Summary

- Many new charmonium-like states were observed experimentally. They are good candidates for $cq\bar{c}\bar{q}$ states.
- Hidden-charm pentaquark states were observed by LHCb.
- Doubly hidden-charm/bottom $QQ\bar{Q}\bar{Q}$ states favor the compact tetraquark configuration than the hadron molecule.
- We have calculated the mass spectra for the $cc\bar{c}\bar{c}$ and $bb\bar{b}\bar{b}$ tetraquark states. Our results show that the $cc\bar{c}\bar{c}$ states lie above two charmonium thresholds and thus mainly decay via spontaneous dissociations. The $bb\bar{b}\bar{b}$ states are expected to be very narrow.
- The recent observations of the J/ψ pair, $J/\psi\Upsilon(1S)$ and $\Upsilon(1S)\Upsilon(1S)$ events shed some light for the production of these doubly hidden-charm/bottom tetraquarks.

Thank you for your attention!