Part 3 - Vertex reconstruction, analysis & reality



SUMMARY

Recap of yesterday

- We've found tracks
 - global and local pattern recognition algorithms
- We've fitted those tracks
 - least squares estimator fit, e.g. global χ^2 minimazation, Kalman filter
- Discussed the fit output
- Touched upon "ghost tracks"
 - we will hear a bit more about that though
- Dedicated electron fitting



Dedicated electron fitting



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So far we discussed "fakes" (ghost tracks) at seed level

good track not so good track



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many compatible hits

completeness

uniqueness

low χ^2 /ndf

small impact parameter (for primaries)



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shared hits bad fit quality,





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not so good track

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short tracks

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Can we be sure ?

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Can we be sure ?

 Some of the characteristics can only be checked after all track candidates are found



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give scores and rank the tracks!

Vertex reconstruction

- We've found tracks, let's use them: vertex reconstruction
- Similar problem to track reconstruction
 - consists of vertex finding and vertex fitting, (primary) input are tracks

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J

$$q_{i} = h_{i}(v, p_{i}) + \varepsilon_{i}$$
with: $h_{i} =$ dependency of track parameters on
vertex and parameters at vertex
$$\varepsilon_{i} = \text{error of } q_{i}$$
Jacobians: $A_{i} = \frac{\partial h_{i}(v, p_{i})}{\partial v}$ $B_{i} = \frac{\partial h_{i}(v, p_{i})}{\partial p_{i}}$

$$h_{i} = f \circ \tilde{q}(v, p_{i}) \quad \text{with:} \quad \begin{array}{l} v = (v_{x}, v_{y}, v_{z}) \\ p_{i} = (\theta_{i}, \phi_{i}, Q_{i}/P_{i}) \end{array}$$



Vertex reconstruction

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Vertex fitting

• And again, you can do a straight forward global χ^2 minimisation

 $\chi^{2} = \sum_{i} \Delta q_{i}^{T} G_{i} \Delta q_{i} \quad \text{with:} \quad \Delta q_{i} = q_{i} - h_{i}(v, p_{i})$ $V_{i} = G_{i}^{-1} \quad \text{covariance of the measured } q_{i}$ linearize the problem: $v \rightarrow v_{0} + \delta v \text{ and } p_{i} \rightarrow p_{i,0} + \delta p_{i}$

 $h_i(v, p_i) \cong h_i(v_0, p_{i,0}) + A_i \delta v + B_i \delta p_i + \text{higher terms}$

this yields:

$$\chi^{2} = \sum_{i} \left(h_{i}(v_{0}, p_{i,0}) + A_{i}\delta v + B_{i}\delta p_{i} \right)^{T} G_{i} \left(h_{i}(v_{0}, p_{i,0}) + A_{i}\delta v + B_{i}\delta p_{i} \right)$$

minimizing the linearized χ^2 gives the following set of equations:

$$\frac{\partial \chi^2}{\partial v} = 0 \quad \Rightarrow \quad \left[\left(\sum_i A_i^T G_i A_i \right) \cdot \delta v + \sum_i A_i^T G_i B_i \cdot \delta p_i = \sum_i A_i^T G_i \cdot \Delta q_{i,0} \right] \\ \frac{\partial \chi^2}{\partial p_i} = 0 \quad \Rightarrow \quad B_i^T G_i A_i \cdot \delta v + B_i^T G_i B_i \cdot \delta p_i = B_i^T G_i \cdot \Delta q_{i,0} \\ \text{with: } \Delta q_{i,0} = q_i - h_i(v_0, p_{i,0}) \right]$$

Vertex fitting

Or, you apply a Kalman filter technique

$$\delta v_{i} = C_{i}^{-1} \cdot \left[C_{i-1} \delta v_{i-1} + A_{i}^{T} G_{i}^{B} \cdot \Delta q_{i,i-1} \right]$$
$$C_{i} = \left(C_{i-1}^{-1} + A_{i}^{T} G_{i}^{B} A_{i} \right)^{-1}$$

$$\delta p_{i,i} = W_i B_i^T G_i \cdot \left(\Delta q_{i,i-1} - A_i \delta v_i \right)$$
$$D_i = W_i + W_i B_i^T G_i A_i C_i A_i^T G_i B_i W_i$$

and the smoother becoming the re-evaluation of the parameters $q_{i,n}$ depending on the fitted vertex after inclusion of n tracks

$$q_{i,n} = h_i(v_0 + \delta v_n, p_{i,0} + \delta p_{i,n})$$

with: $\operatorname{cov}(q_{i,n}) = B_i W_i B_i^T + V_i^B G_i A_i C_n A_i^T G_i V_i^B$ and $V_i^B = V_i - B_i W_i B_i^T$



What about the initial seed ?



salzburg\$ ipython -i --matplotlib=osx VertexFinding.py
In [1]: fig, plots = buildDetector()

```
In [2]: hits = shoot(fig, plots, nvertices=1, number=25, seed=12345)
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In [3]: findVertices(fig,plots,hits)
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- Part 3 - HCPSS Aug 11-22, 2014 Reconstruction and Track A. Salzburger

Enemy No. 3: pile-up









To maximise the physics potential, LHC was running (and will keep on running) with multiple instantaneous collisions: <u>pile-up</u>



 More "fun" for track reconstruction



- Pile-up let's combinatorics explode
- This is bad from many angles:
 - CPU time explodes
 - Iow track fake rate is at risk (make more stringent requirements)
 - track finding becomes more difficult (risk of losing tracks)
 - vertex reconstruction suffers from multiple problems:
 - fake vertices
 - merged vertices
 - split vertices

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Track reconstruction in analysis

The first published analyses of all LHC experiments were tracking based



Prompt K_{S^0} production in pp collisions at $\sqrt{s} = 0.9$ TeV

 A three-step master plan to a Soft QCD paper : (might be "slightly" simplified)

- 1. take data from generic p-p collisions without bias towards some signature ("Minimum bias measurement")
- 2. count how many primary tracks you find (e.g. vs η , vs p_T)
- 3. correct for tracks you have not found and publish

Let's do it !

Let's roll the dice ourselves





And that's what the track reconstruction gives us





And that's what the track reconstruction gives us



And that's what the track reconstruction gives us



We need to define a tracking efficiency

- There is no such thing as a tracking efficiency
 - restricted to phase-space
 - restricted to your definitions of a track (requirements and cuts)
 - different for different particles
- For checking the algorithmic performance
 - define a "reconstructable track" in Monte Carlo and check how often you can find it
 - can we do that in data ?



Tracking efficiency

- Material is the main source of inefficiency in the tracker
 - majority of particles are hadrons: nuclear interaction dominates
 - for electrons also bremsstrahlung needs to be considered
- Tracking efficiency for hadrons is usually taken from Monte Carlo
 - defined by :

E =

Number of found tracks*and matched to a truth particle Number of generated stable charged particles**

**satisfying my phase space

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Perfect ! Now we can measure it ...

*satisfying my track cuts

**satisfying my phase space

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remember ?

- " ... rather constant in p ..."
- ' ... defined by nuclear interaction length $arLapha_0$..."

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our built-up material map ...

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both ionisation loss and multiple scattering act most at low $p_{T} \, \mbox{in the minimum bias}$ regime

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INTERLUDE

Tracking efficiency

-*dE/dx* [MeV/mm]

10

1

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Measuring your detector material

 Hundreds of pages of TDRs and technical drawings before detector construction



- ATLAS has actually weighted the detector before installing it and compared the weight to the one in simulation
- Best: measure the material in situ !

Using photon conversions

- Photons can convert into e⁺e⁻ when hitting detector material
- 2-track vertices with electron PID
 - very clear signal
- Count conversion vertices in data and MC and compare
 - Is this really measuring the material ?
 - Are we just seeing an artefact of non-ideal simulation (cross-section ...) ?



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- Try to find a standard candle,
 i.e. a piece of material you
 know very well in reality and
 simulation



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remember ?

"... ATLAS is trying to measure the old beam pipe again ... "



Using photon conversions



400

23

400

R (mm)

Using hadronic Interactions

- The straight-forward way
 - measure how often tracks "survive" when passing material



Using hadronic Interactions

- The straight-forward way
 - measure how often tracks "survive" when passing material



INTERLUDE
- The more sophisticated way
 - assume we can configure our track reconstruction to also reconstruct the charged particles coming out of a hadronic interaction
 - let's try to use our vertex reconstruction skills and try to reconstruct the vertices from hadronic interactions



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What do you need to be very careful about ?



INTERLUDE

INTERLUDE

Using hadronic Interactions 5

- Both CMS & ATLAS have achieved astonishing results with this technique
 - offset of nominal beam pipe seen for both experiments
 - accuracy of material measurement for ATLAS ~8 %





Let's finish the analysis











• Let's finish the analysis: done.





Example: Higgs mass from $H \to Z Z^* \to 4 \mu$

 A three-step master plan to a Higgs mass paper : (might be even more "slightly" simplified)

- 1. take data with some sort of muon trigger and find events with 4 muons in the final state (2 oppositely charged muon pairs)
- 2. use their track momentum measurement and combine them to a common Higgs mass
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Let's do it !





















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Enemy No. 4: misalignment

- No one said the detector elements are actually exactly where you expect them
 - you need to find out where they are !
- Major feature: random module misalignment
 - can be corrected for using alignment algorithms
 - most commonly used: a global χ^2 minimisation using tracks and varying the module positions
 - many many degrees of freedom (ATLAS: 36 k matrix inversion, CMS even more)
- It works !



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Level 1 alignment




















Calibrate your detector

• use known resonances to calibrate your detector



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Calibrate your detector

use known resonances to calibrate your detector



Example: Higgs mass from $H \to Z Z^* \to 4 \mu$

• Let's finish our analysis and get out of there ...



Example: Higgs mass from $H \to Z Z^* \to 4 \mu$

• Let's finish our analysis and get out of there ...



The take aways

Actually, you should fill this page !

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What I could not cover ...

- ▶ A lot ...
- Track/vertex finding: there are way more methods
- Track fitting: there are way more methods
- Track reconstruction in very dense environments
 - e.g. in core of very dense jets
- Combined reconstruction
 - combined μ fitting, decay chain fitting, constraint fitting \ldots
- Computing aspect
 - CPU time optimisation (very important for high pile-up)

And finally

- Thanks to you for being such a great audience !
- To the school organisers and other lecturers to make this such a great school

• A special thank to Markus Elsing for some of the material.

Aug

Reconstruct

and

A. Salzburge