

# Novel method to reliably determine the photon helicity in $b \rightarrow s\gamma$

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*WYZ: Phys.Rev.Lett. 125 (2020) 5, 051802*

@ 6th China LHC Physics Workshop

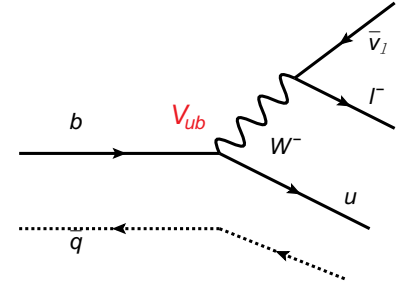
# Outline

- Heavy Flavor Physics
- Photon polarization in  $b \rightarrow s\gamma$ :  
$$B \rightarrow K_1(\rightarrow K\pi\pi)\gamma$$
- Model-independent extraction using  
$$D \rightarrow K_1(\rightarrow K\pi\pi)e^+\nu$$
- Summary

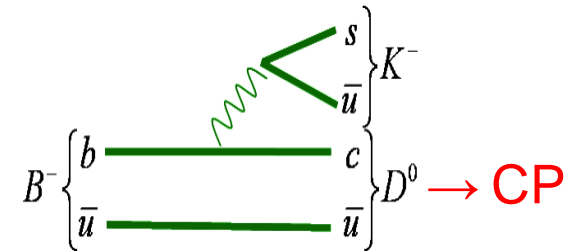
# Heavy Flavor Physics

# Heavy Flavor Bottom Physics

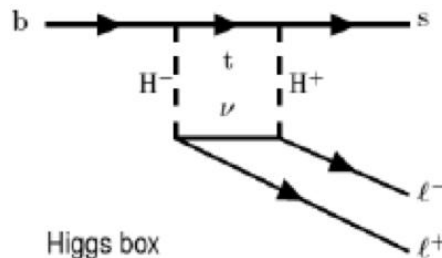
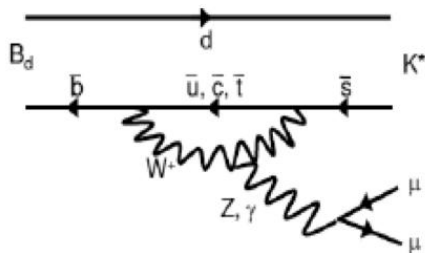
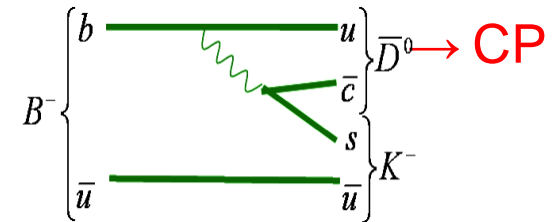
- Extract the SM parameters:  
 $V_{ub}$ ,  $V_{cb}$ , Weak Phases



- Test SM: unitary triangle



- Hunt for NP: Rare Decays

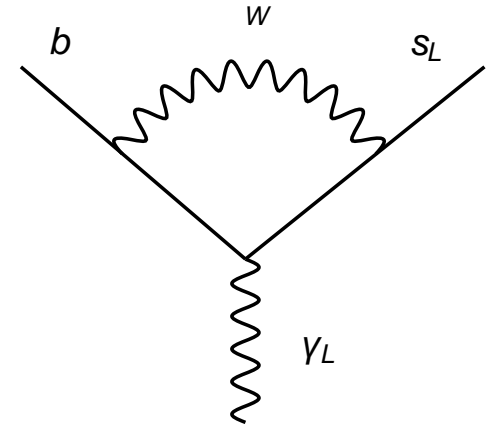


Photon polarization in  $b \rightarrow s\gamma$ :

$$B \rightarrow K_1(\rightarrow K\pi\pi)\gamma$$

# Photon polarization of $b \rightarrow s\gamma$

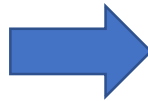
- An unique sensitivity to BSM with right-handed couplings
- Never been measured at a **high precision**: an important challenge for LHCb (and its upgrade) and Belle II



$$\mathcal{H}_{\text{eff}}^{\text{SM}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* C_{7\gamma} O_{7\gamma}$$

$$O_{7\gamma} = \frac{em_b}{16\pi^2} \bar{s} \sigma_{\mu\nu} \frac{1 + \gamma_5}{2} b F^{\mu\nu}$$

SM



$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* (C_{7L} O_{7L} + C_{7R} O_{7R})$$

$$O_{7L,R} = \frac{em_b}{16\pi^2} \bar{s} \sigma_{\mu\nu} \frac{1 \pm \gamma_5}{2} b F^{\mu\nu}$$

New Physics

# How do we measure the polarization?

## ➤ Time-dependent measurements:

- ✓  $B_d \rightarrow K_s \pi^0 \gamma$

- ✓  $B_d \rightarrow K_s \pi^+ \pi^- \gamma$

- ✓  $B_s \rightarrow K^+ K^- \gamma$

## ➤ Angular distribution:

- ✓ Baryonic decays:  $\Lambda_b \rightarrow \Lambda \gamma$

request to the polarization of  $\Lambda_b$  or  $\Lambda$

- ✓  $B \rightarrow K_{res}(\rightarrow K\pi\pi)\gamma$

# Photon polarization of $B \rightarrow K_1 (\rightarrow K\pi\pi)\gamma$

$$\lambda_\gamma \equiv \frac{|\mathcal{A}(\bar{B} \rightarrow \bar{K}_{1R}\gamma_R)|^2 - |\mathcal{A}(\bar{B} \rightarrow \bar{K}_{1L}\gamma_L)|^2}{|\mathcal{A}(\bar{B} \rightarrow \bar{K}_{1R}\gamma_R)|^2 + |\mathcal{A}(\bar{B} \rightarrow \bar{K}_{1L}\gamma_L)|^2} \\ \simeq \frac{|C_{7R,NP}|^2 - |C_{7L,SM}|^2}{|C_{7R,NP}|^2 + |C_{7L,SM}|^2}$$

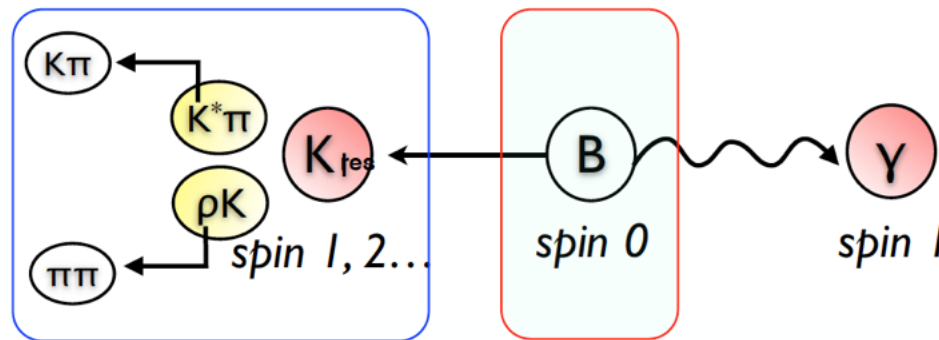
In the SM,  $\lambda_\gamma \simeq -1$



# Angular distribution method

Gronau, Grossman, Pirjol, Ryd PRL88('01)

- Photon polarization  
= Recoiling  $K_1$  polarization  
=> measure it from  $K_1$  decay angular distribution



# **$K_1(1270)$**

$$I(J^P) = \frac{1}{2}(1^+)$$

Mass  $m = 1272 \pm 7$  MeV [1]

Full width  $\Gamma = 90 \pm 20$  MeV [1]

<b><math>K_1(1270)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K \rho$	(42 $\pm$ 6 ) %	46
$K_0^*(1430) \pi$	(28 $\pm$ 4 ) %	†
$K^*(892) \pi$	(16 $\pm$ 5 ) %	302
$K \omega$	(11.0 $\pm$ 2.0) %	†
$K f_0(1370)$	( 3.0 $\pm$ 2.0) %	†
$\gamma K^0$	seen	539

# Up-down asymmetry for $K_1$

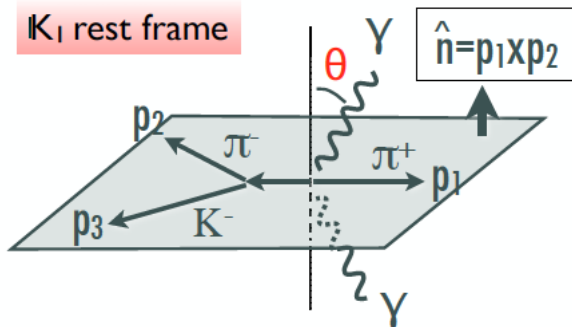
Angular distribution:

Gronau, Grossman, Pirjol, Ryd PRL88('01)

$$\frac{d\Gamma_{K_1\gamma}}{d\cos\theta_K} = \frac{|A|^2|\vec{J}|^2}{4} \times \left[ 1 + \cos^2\theta_K + 2\lambda_\gamma \cos\theta_K \frac{\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)]}{|\vec{J}|^2} \right].$$

Up-down asymmetry for  $K_1$

$$\begin{aligned} \mathcal{A}_{\text{UD}} &\equiv \frac{\left[ \int_0^1 - \int_{-1}^0 \right] d\cos\theta_K \frac{d\Gamma(B \rightarrow K_1\gamma)}{d\cos\theta_K}}{\left[ \int_0^1 + \int_{-1}^0 \right] d\cos\theta_K \frac{d\Gamma(B \rightarrow K_1\gamma)}{d\cos\theta_K}} \\ &= \lambda_\gamma \frac{3}{4} \frac{\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)]}{|\vec{J}|^2} \end{aligned}$$



To measure  $\lambda_\gamma$ , we need to know *the decay factor*

# LHCb result on up-down asymmetry

LHCb PRL ('14)

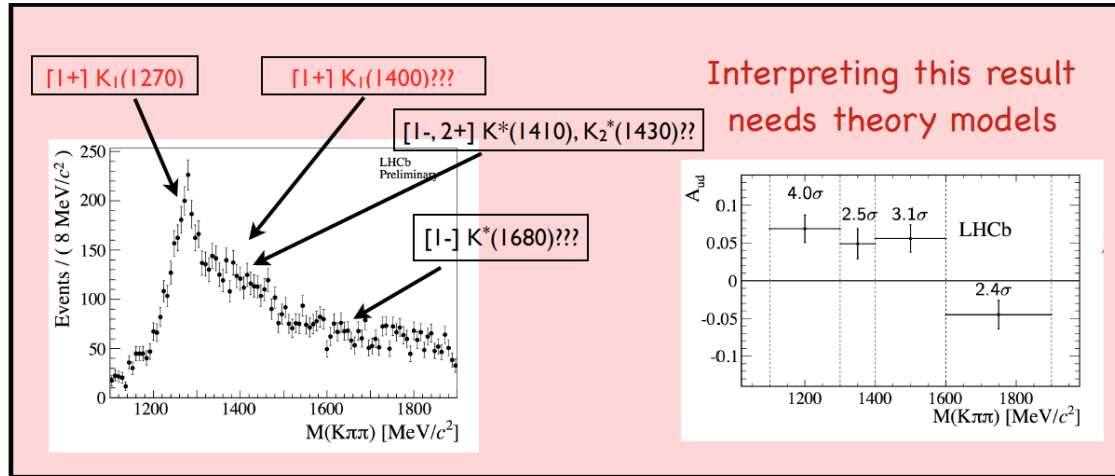
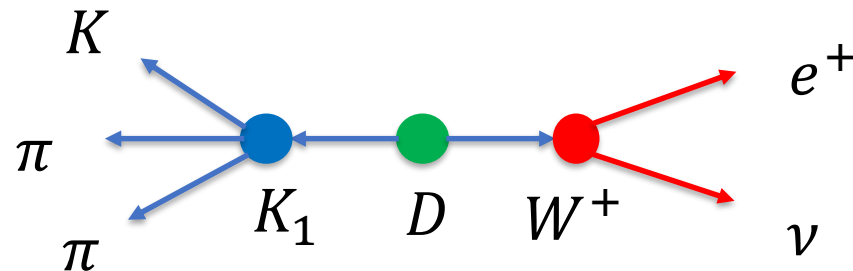


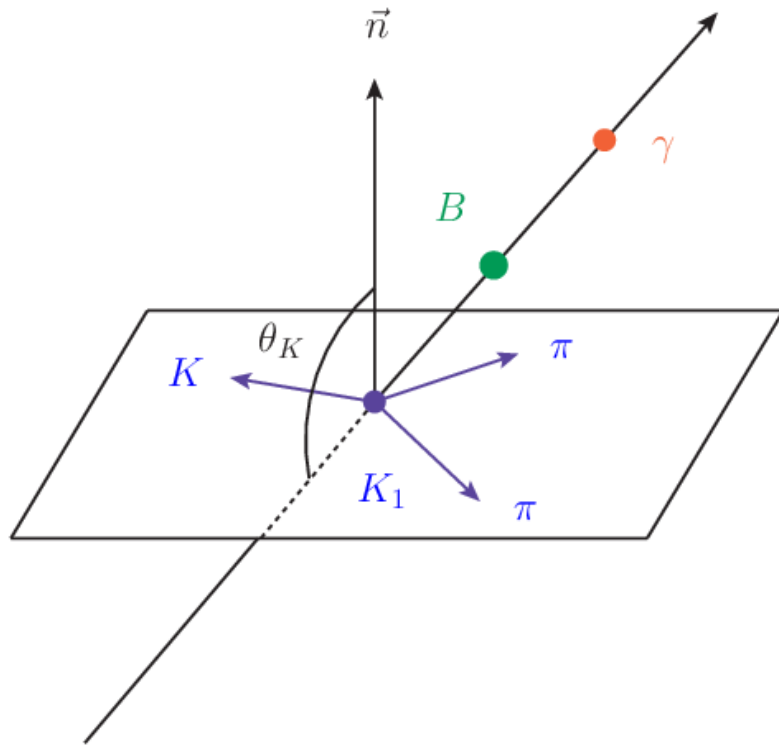
TABLE I. Legendre coefficients obtained from fits to the normalized background-subtracted  $\cos \hat{\theta}$  distribution in the four  $K^+\pi^-\pi^+$  mass intervals of interest. The up-down asymmetries are obtained from Eq. (4). The quoted uncertainties contain statistical and systematic contributions. The  $K^+\pi^-\pi^+$  mass ranges are indicated in  $\text{GeV}/c^2$  and all the parameters are expressed in units of  $10^{-2}$ . The covariance matrices are given in Ref. [22].

	[1.1,1.3]	[1.3,1.4]	[1.4,1.6]	[1.6,1.9]
$c_1$	$6.3 \pm 1.7$	$5.4 \pm 2.0$	$4.3 \pm 1.9$	$-4.6 \pm 1.8$
$c_2$	$31.6 \pm 2.2$	$27.0 \pm 2.6$	$43.1 \pm 2.3$	$28.0 \pm 2.3$
$c_3$	$-2.1 \pm 2.6$	$2.0 \pm 3.1$	$-5.2 \pm 2.8$	$-0.6 \pm 2.7$
$c_4$	$3.0 \pm 3.0$	$6.8 \pm 3.6$	$8.1 \pm 3.1$	$-6.2 \pm 3.2$
$\mathcal{A}_{ud}$	$6.9 \pm 1.7$	$4.9 \pm 2.0$	$5.6 \pm 1.8$	$-4.5 \pm 1.9$

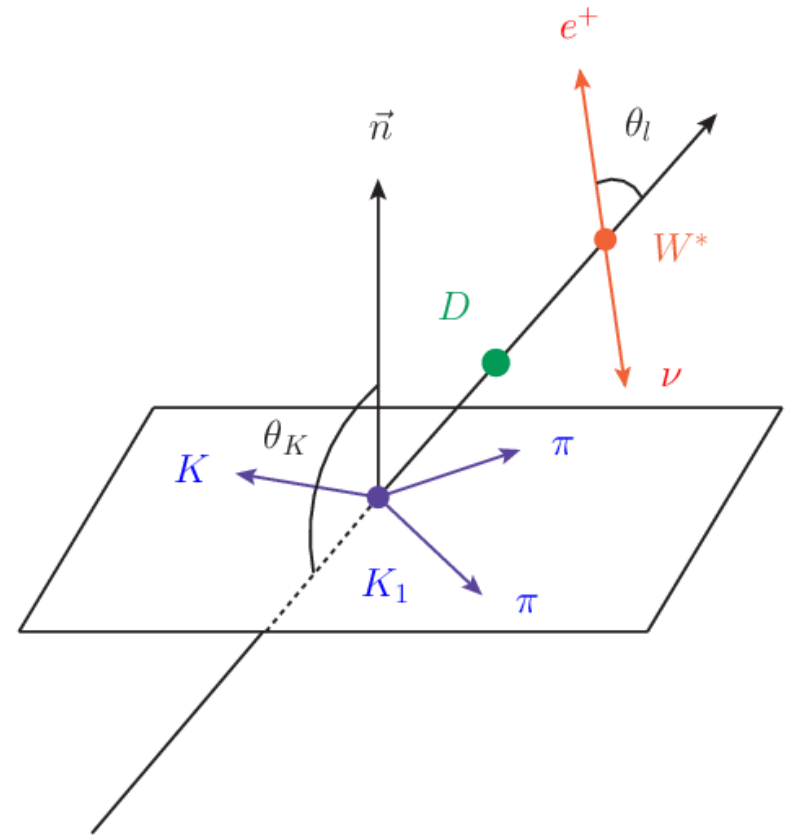
# Model-independent extraction using $D \rightarrow K_1(\rightarrow K\pi\pi)e^+\nu$



$$B \rightarrow K_1(K\pi\pi)\gamma \text{ vs } D \rightarrow K_1(K\pi\pi)e^+\nu$$



Polarization of  $\gamma$ : +, -



Polarization of  $W$ : +, -, 0, t

t: timelike,  $\epsilon^\mu(t) \sim p_W^\mu$

# Angular Distribution of $D \rightarrow K_1(\rightarrow K\pi\pi)e^+\nu$

$$\begin{aligned}\frac{d\Gamma_{K_1 e \nu_e}}{d\cos\theta_K d\cos\theta_l} = & d_1[1 + \cos^2\theta_K \cos^2\theta_l] \\ & + d_2[1 + \cos^2\theta_K] \cos\theta_l + d_3 \cos\theta_K [1 + \cos^2\theta_l] \\ & + d_4 \cos\theta_K \cos\theta_l + d_5[\cos^2\theta_K + \cos^2\theta_l].\end{aligned}$$

The angular coefficients are given as:

$$\begin{aligned}d_1 &= \frac{1}{2}|\vec{J}|^2(4c_0^2 + c_-^2 + c_+^2), d_2 = -|\vec{J}|^2(c_-^2 - c_+^2), \\ d_3 &= -\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)](c_-^2 - c_+^2), \\ d_4 &= 2\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)](c_-^2 + c_+^2), \\ d_5 &= -\frac{1}{2}|\vec{J}|^2(4c_0^2 - c_-^2 - c_+^2).\end{aligned}$$

# Up-down asymmetries

$$D \rightarrow K_1(\rightarrow K\pi\pi)e^+\nu$$

$$\mathcal{A}'_{\text{UD}} \equiv \frac{\left[ \int_0^1 - \int_{-1}^0 \right] d \cos \theta_K \frac{d\Gamma_{K_1 e \nu e}}{d \cos \theta_K}}{\left[ \int_0^1 - \int_{-1}^0 \right] d \cos \theta_l \frac{d\Gamma_{K_1 e \nu e}}{d \cos \theta_l}}$$

$$\mathcal{A}'_{\text{UD}} = \frac{\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)]}{|\vec{J}|^2}$$

$$B \rightarrow K_1(\rightarrow K\pi\pi)\gamma$$

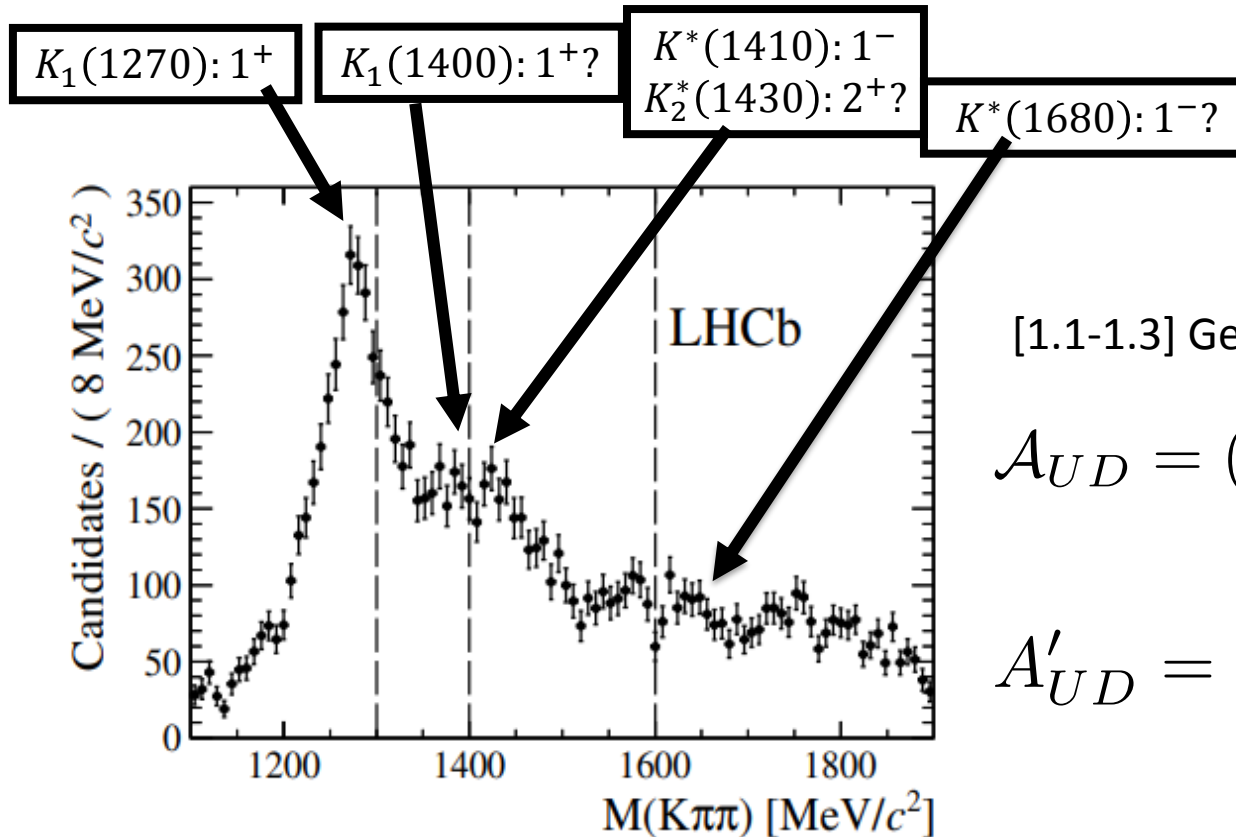
$$\mathcal{A}_{UD} \equiv \frac{\left[ \int_0^1 - \int_{-1}^0 \right] d \cos \theta_K \frac{d\hat{\Gamma}_{K_1 \gamma}}{d \cos \theta_K}}{\left[ \int_0^1 + \int_{-1}^0 \right] d \cos \theta_K \frac{d\hat{\Gamma}_{K_1 \gamma}}{d \cos \theta_K}}$$

$$= \lambda_\gamma \frac{3}{4} \frac{\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)]}{|\vec{J}|^2}$$



# Prospect at BESIII & BelleII

LHCb: PRL112.161801(2014)



[1.1-1.3] GeV:

$$\mathcal{A}_{UD} = (6.9 \pm 1.7) \times 10^{-2}$$

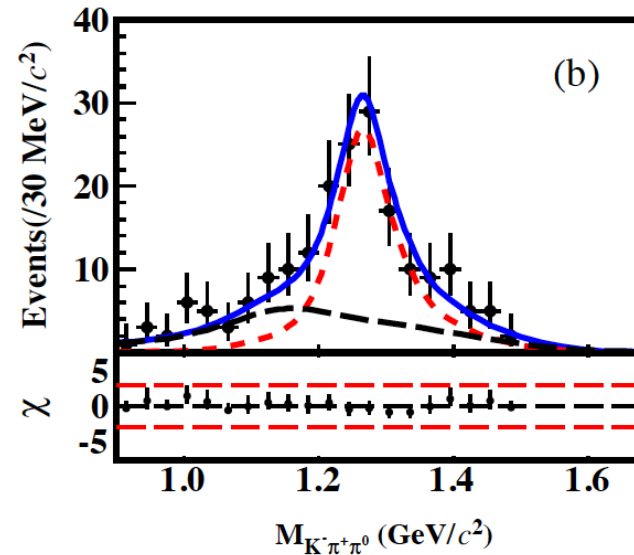


$$A'_{UD} = (9.2 \pm 2.3) \times 10^{-2}$$

A significant deviation from the above value would be a clear signal for new physics beyond SM.

# $D \rightarrow K_1(\rightarrow K\pi\pi)e^+\nu$ from BESIII

BESIII: 1907.11370



$$\mathcal{B}(D^+ \rightarrow \bar{K}_1^0 e^+ \nu) = (2.3 \pm 0.26 \pm 0.18 \pm 0.25) \times 10^{-3}.$$

BESIII, BelleII, LHCb, Super Tau-Charm, CEPC in future?

# Summary

- Heavy Flavor Physics: indirect search for NP
- Photon polarization in  $b \rightarrow s\gamma$ : unique to probe right-handed couplings
- Model-independent extraction using  $D \rightarrow K_1(\rightarrow K\pi\pi)e^+\nu$ 
  - ✓ Hadron inputs
  - ✓ Photon polarization in a model-independent way: NP?
  - ✓ BESIII, BelleII, LHCb, Super Tau-Charm, CEPC in future?

Thank you very much!

# Backup

# Including more $K_J$ resonances

The angular distribution for  $D \rightarrow K_{res}(\rightarrow K\pi\pi)e^+\nu$

$$\frac{d\hat{\Gamma}}{d\cos\theta_K d\cos\theta_l} = \sum_{K_J=K_1, K_1^*, K_2, K_{12}^I} \frac{d\hat{\Gamma}_{K_J l \nu}}{d\cos\theta_K d\cos\theta_l}$$

➤ For  $K^*(1410)$

$$\begin{aligned} \frac{d\hat{\Gamma}_{K_1^* l \nu}}{d\cos\theta_K d\cos\theta_l} &= (|c_+''|^2 + |c_-''|^2) \sin^2\theta_K (1 + \cos^2\theta_l) \\ &+ 2(|c_+''|^2 - |c_-''|^2) \sin^2\theta_K \cos\theta_l + 4|c_0''|^2 \cos^2\theta_K \sin^2\theta_l \end{aligned}$$

# Including more $K_J$ resonances

➤ For  $K_2^*(1430)$

$$\begin{aligned} \frac{d\hat{\Gamma}_{K_2 l \nu}}{d \cos \theta_K d \cos \theta_l} &= |c'_0|^2 \frac{3}{2} \sin^2(2\theta_K) \sin^2 \theta_l |\vec{K}|^2 \\ &+ 2|c'_1|^2 \cos^4 \frac{\theta_l}{2} \left\{ |\vec{K}|^2 (\cos^2 \theta_K + \cos^2 2\theta_K) \right. \\ &\quad \left. + 2 \cos \theta_K \cos 2\theta_K \operatorname{Im}[\vec{n} \cdot (\vec{K} \times \vec{K}^*)] \right\} \\ &+ 2|c'_{-1}|^2 \sin^4 \frac{\theta_l}{2} \left\{ |\vec{K}|^2 (\cos^2 \theta_K + \cos^2 2\theta_K) \right. \\ &\quad \left. - 2 \cos \theta_K \cos 2\theta_K \operatorname{Im}[\vec{n} \cdot (\vec{K} \times \vec{K}^*)] \right\} \end{aligned}$$

➤  $K_1 - K_2$  interference

$$\begin{aligned} &\frac{d\hat{\Gamma}_{K_{12}^I l \nu}}{d \cos \theta_K d \cos \theta_l} \\ &= -4\sqrt{3} \sin^2(\theta_K) \cos \theta_K \sin^2 \theta_l \operatorname{Re}[c_0(c'_0)^* \vec{J} \cdot \vec{K}^*] \\ &\quad - 8 \cos^4 \frac{\theta_l}{2} \left\{ \frac{1}{2} (3 \cos^2 \theta_K - 1) \operatorname{Im}[c_+(c'_+)^* \vec{n} \cdot (\vec{J} \times \vec{K}^*)] \right. \\ &\quad \left. + \cos^3 \theta_K \operatorname{Re}[c_1(c'_1)^* (\vec{J} \cdot \vec{K}^*)] \right\} \\ &\quad - 8 \sin^4 \frac{\theta_l}{2} \left\{ \frac{1}{2} (1 - 3 \cos^2 \theta_K) \operatorname{Im}[c_-(c'_-)^* \vec{n} \cdot (\vec{J} \times \vec{K}^*)] \right. \\ &\quad \left. + \cos^3 \theta_K \operatorname{Re}[c_{-1}(c'_{-1})^* (\vec{J} \cdot \vec{K}^*)] \right\}. \end{aligned}$$