

# Discovery of the real and complex triplet models at the LHC and future colliders

**Yong Du**

email: [yongdu@umass.edu](mailto:yongdu@umass.edu)

based on arXiv: 2003.07867,  
and JHEP 01(2019)101

CLHCP2020, November 6, Tsinghua University

Disclaimer: Apologize for missing your work here

# The real triplet model

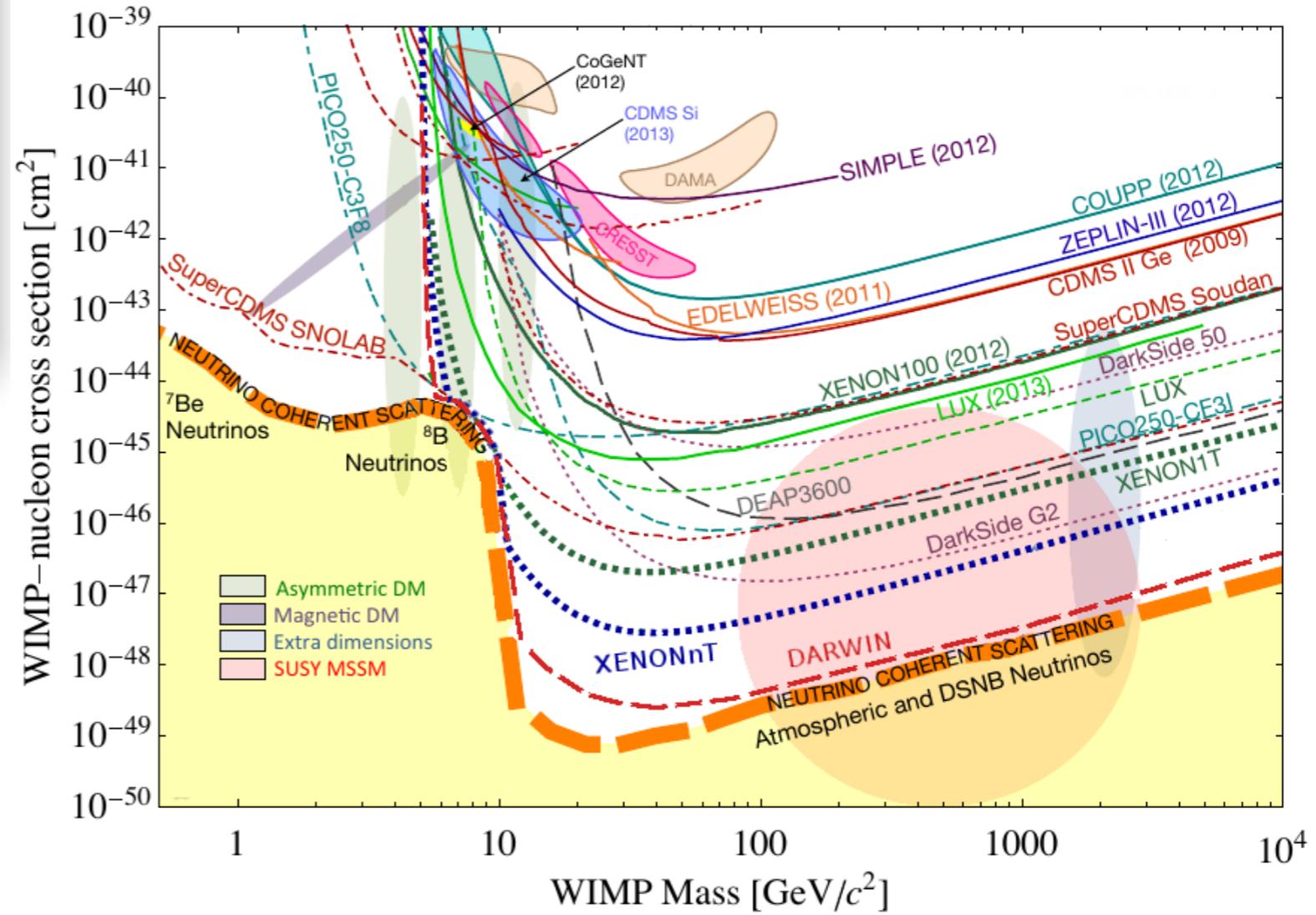
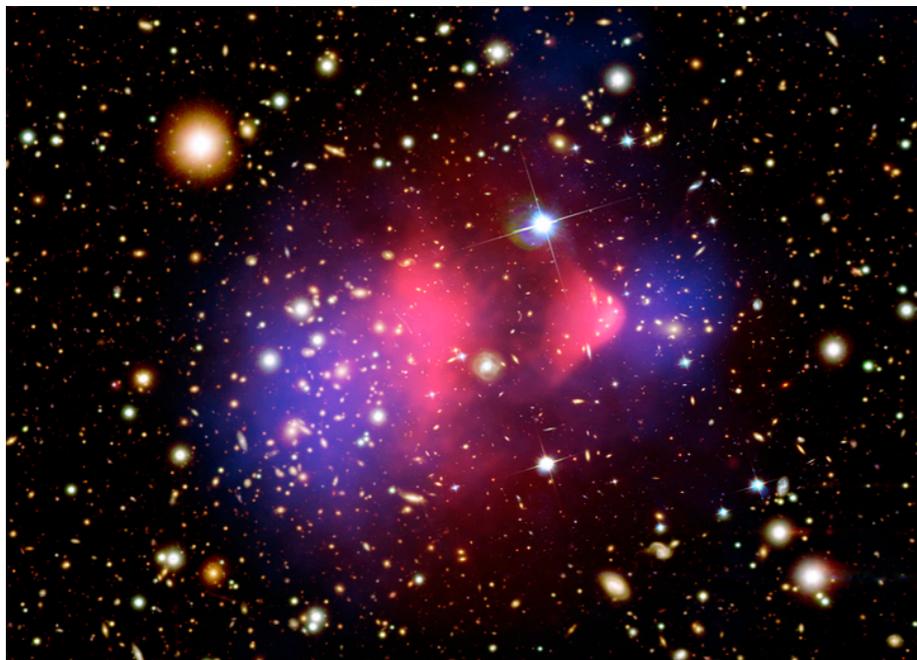
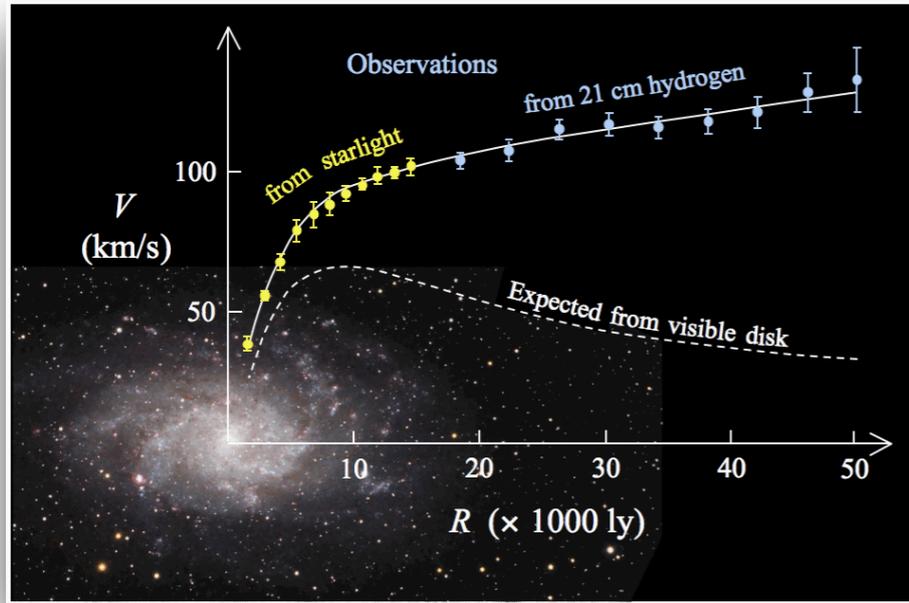
In collaboration with Cheng-Wei Chiang, Giovanna Cottin, Kaori Fuyuto, Michael Ramsey-Musolf

based on arXiv: 2003.07867,

# Dark matter: Background

Yong Du, F. Huang, H.L. Li, J.H. Yu,  
arXiv: 2005.01717

(SIDM from freeze-in)



Klasen et al, arXiv: 1507.03800

# Dark matter: Background

*The real triplet model!*



KAVLI  
IPMU

## new sociology

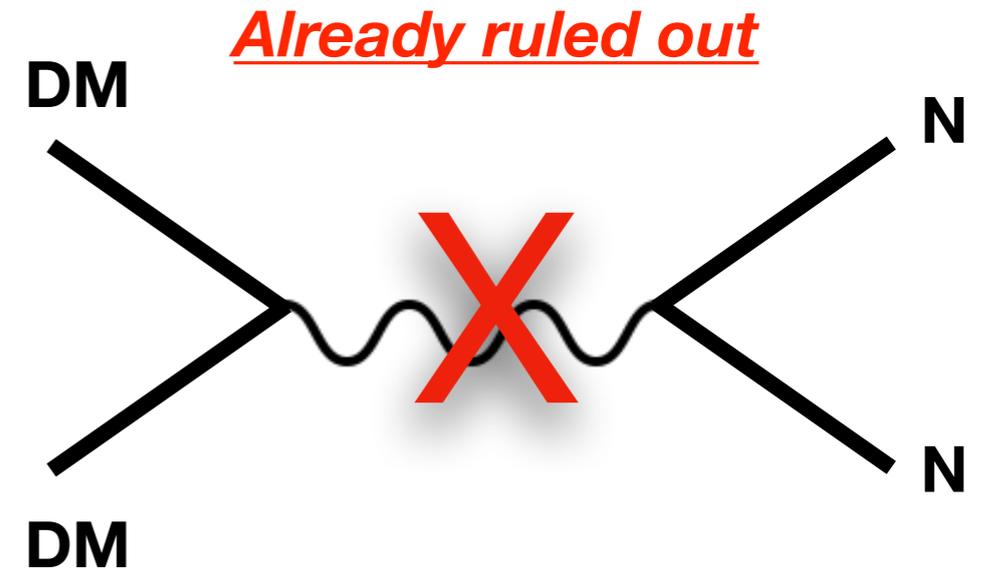
- WIMP should be explored at least down to the **neutrino floor**
  - heavier! e.g., wino @ 3 TeV  $\Rightarrow$  CIA
  - dark matter definitely exists
  - hierarchy problem may be optional?
  - need to explain dark matter on its own
  - perhaps we should decouple these two
  - do we really need big ideas like SUSY?
  - perhaps not necessarily heavier but rather **lighter and weaker coupling?**

*Slide from H. Murayama*

# Brief model introduction

$\Sigma :=$  Real triplet (1, 3, 0)

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2}\Sigma^+ \\ \sqrt{2}\Sigma^- & -\Sigma^0 \end{pmatrix}$$



# Brief model introduction

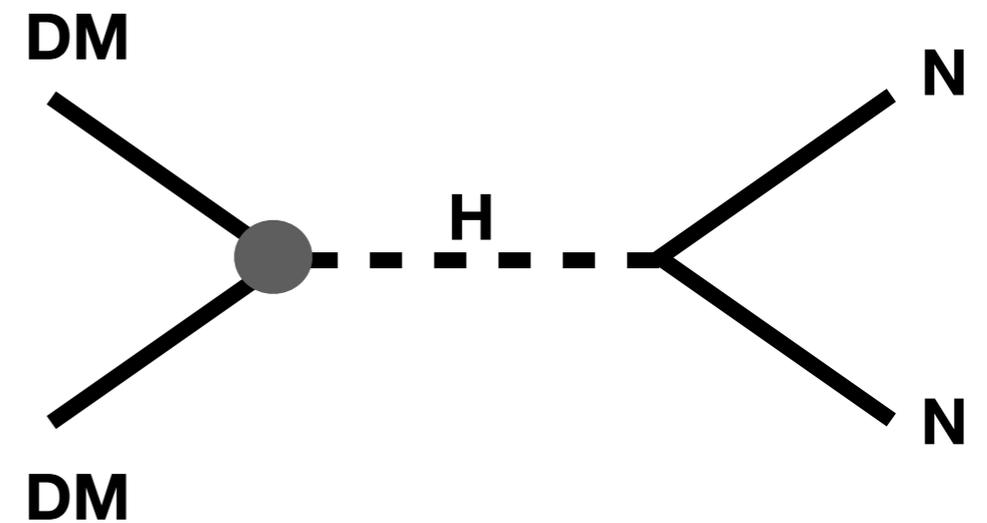
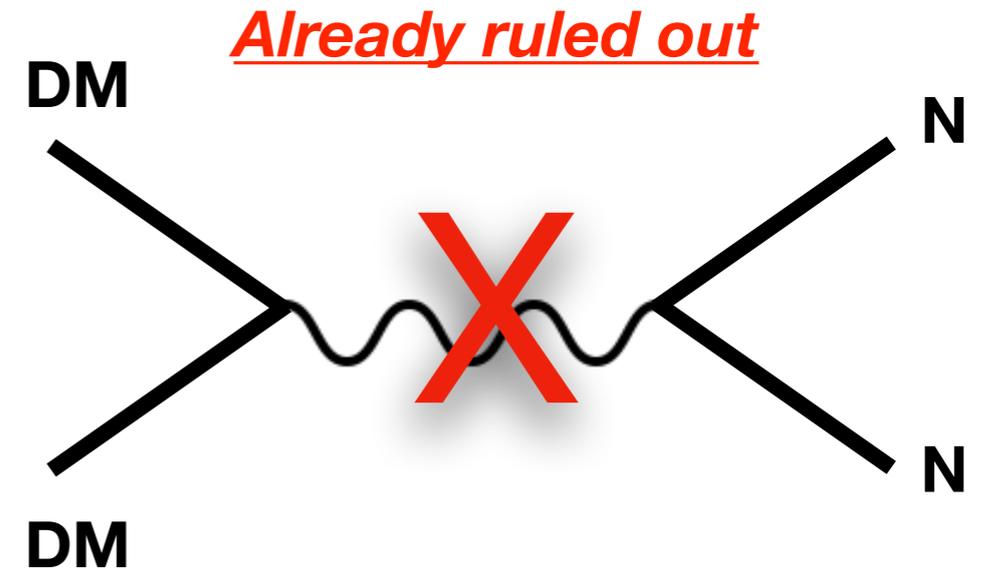
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$$V(\mathbf{H}, \Sigma) = -\mu^2 \mathbf{H}^\dagger \mathbf{H} + \lambda_0 (\mathbf{H}^\dagger \mathbf{H})^2$$

$$-\frac{1}{2} M_\Sigma^2 \mathbf{F} + \frac{b_4}{4} \mathbf{F}^2 + \frac{a_2}{2} \mathbf{H}^\dagger \mathbf{H} \mathbf{F}$$

$$\mathbf{F} = (\Sigma^0)^2 + 2\Sigma^+ \Sigma^-$$



# Brief model introduction

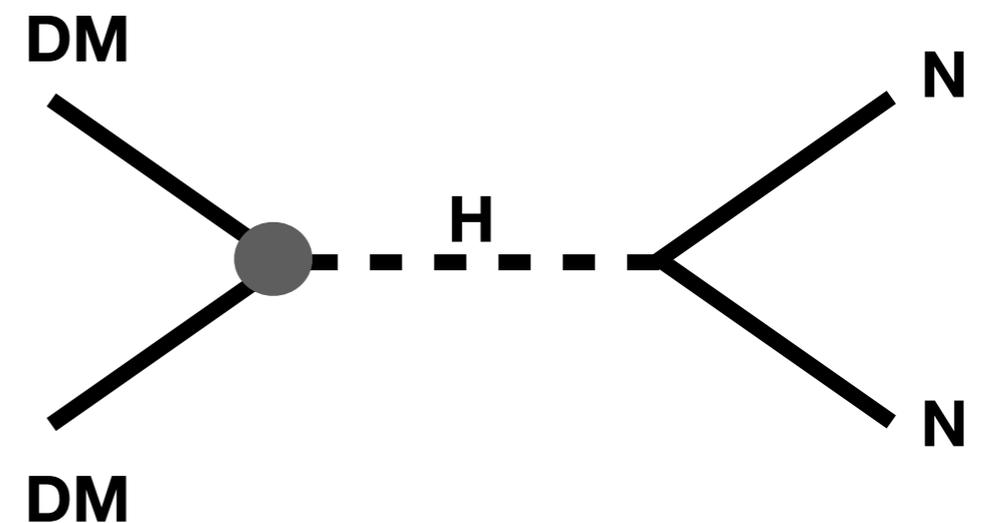
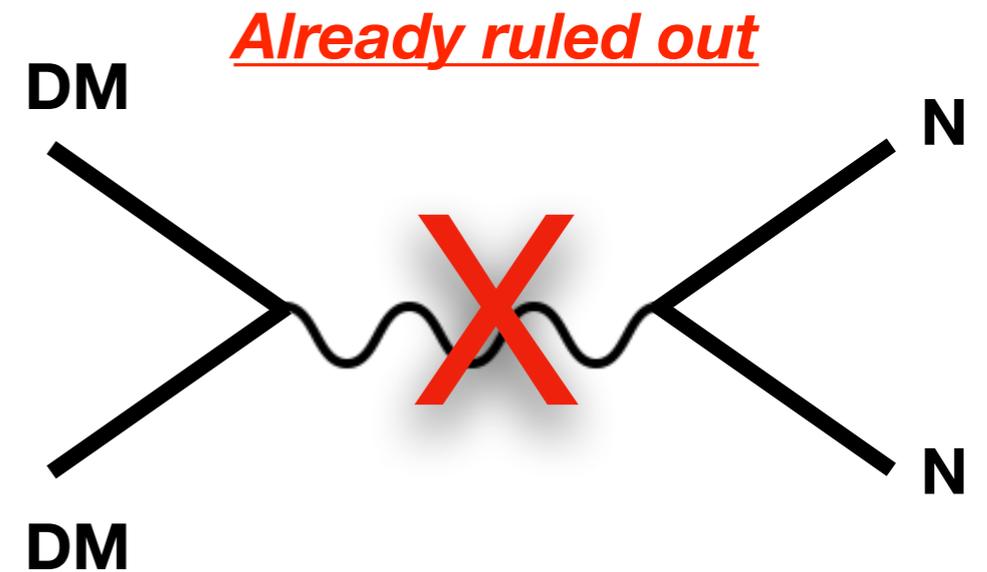
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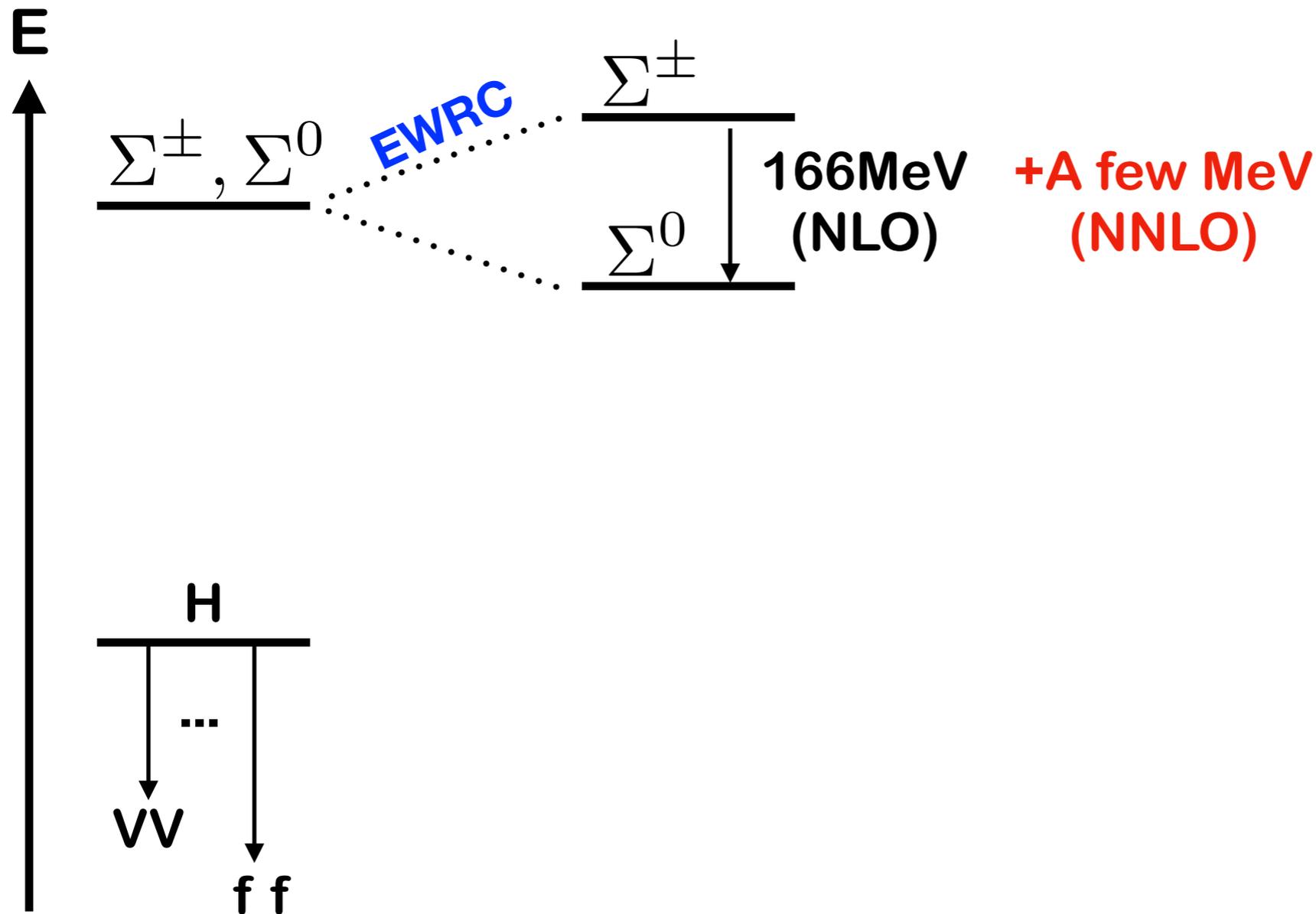
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*Collider phenomenologies?*

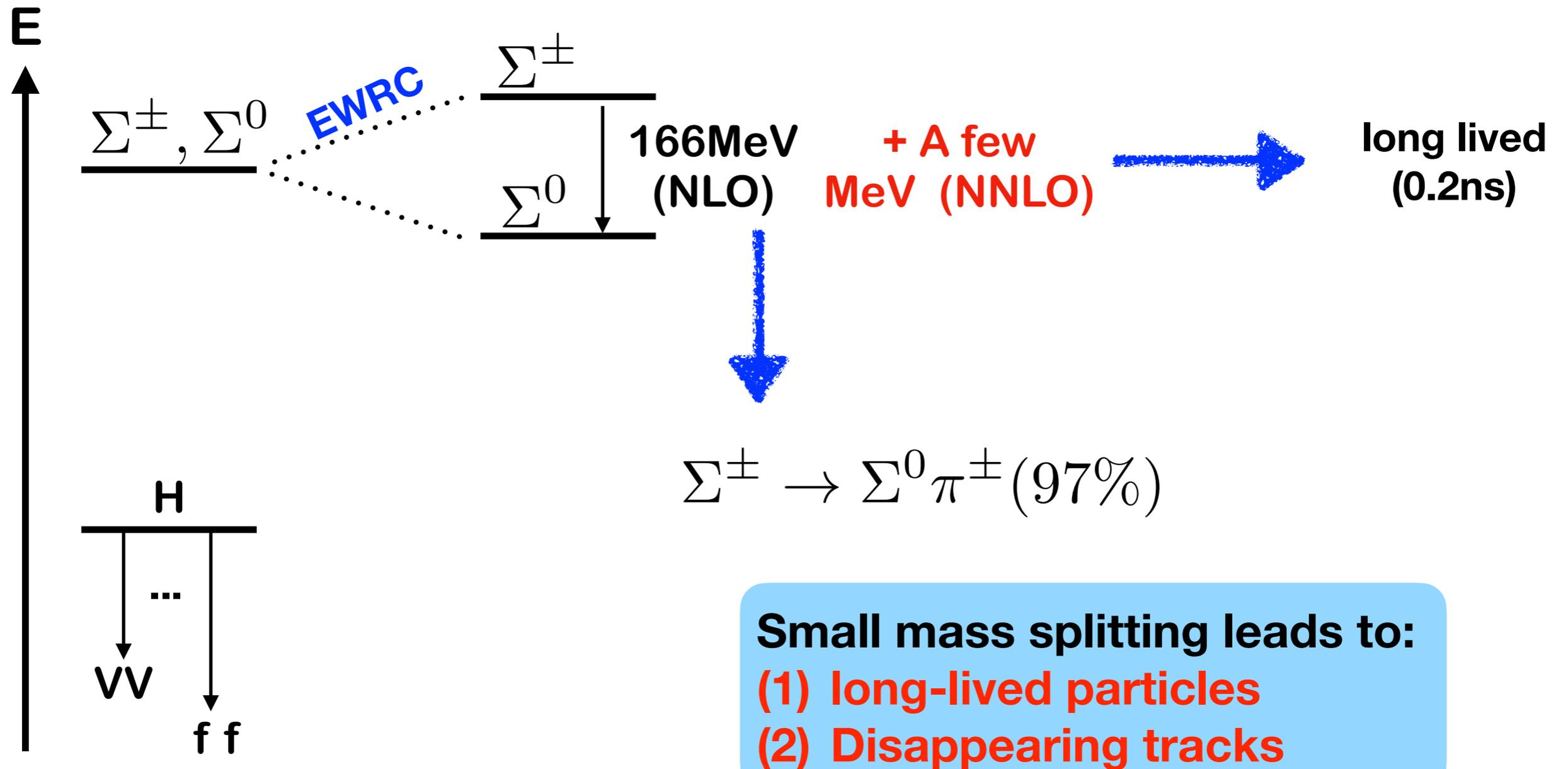
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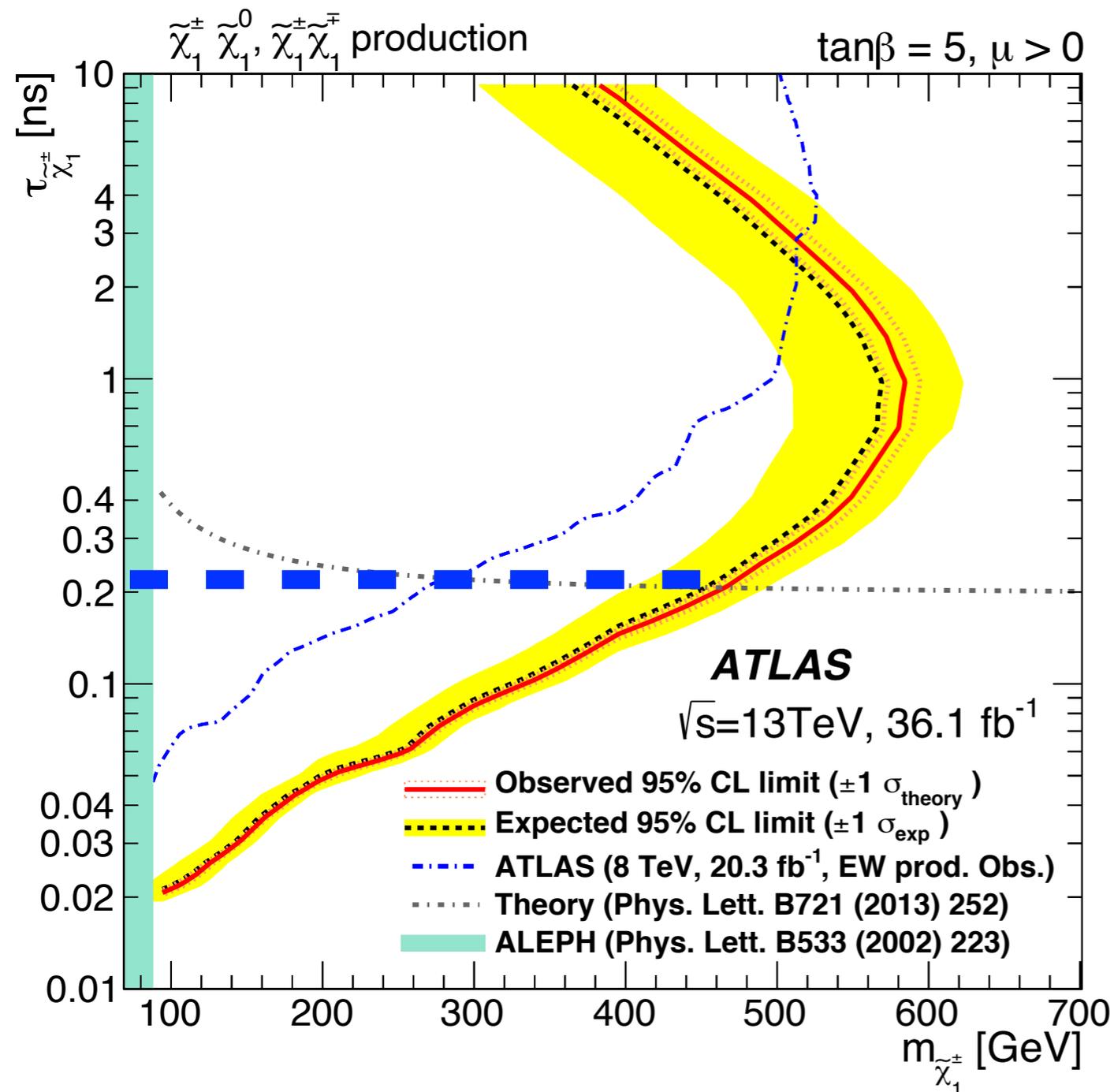


**Small mass splitting leads to:**  
**(1) long-lived particles**  
**(2) Disappearing tracks**

J. Alimena et al., 2019; T. Hambye et al, 2009; R. Mahbubani et al 2017  
 Q.H. Cao et al., 2018; L.D. Luzio et al. 2018; Abe et al. 2018; Kuramotoa et al 2019;  
 ...

# Reproduction of ATLAS result

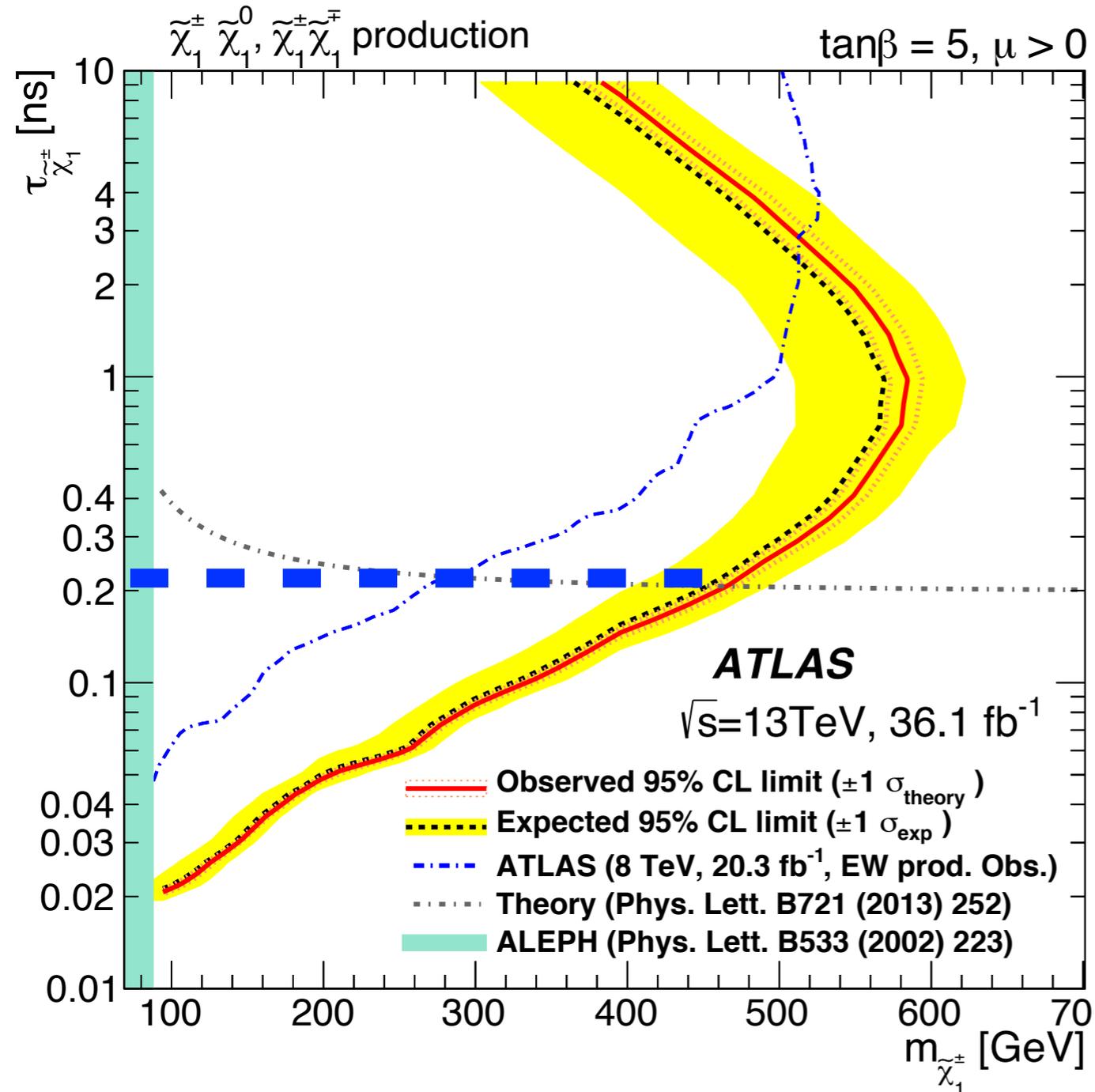
C.W. Chiang, G. Cottin, [Yong Du](#),  
K. Fuyuto, M.J. Ramsey-Musolf  
arXiv: 2003.07867



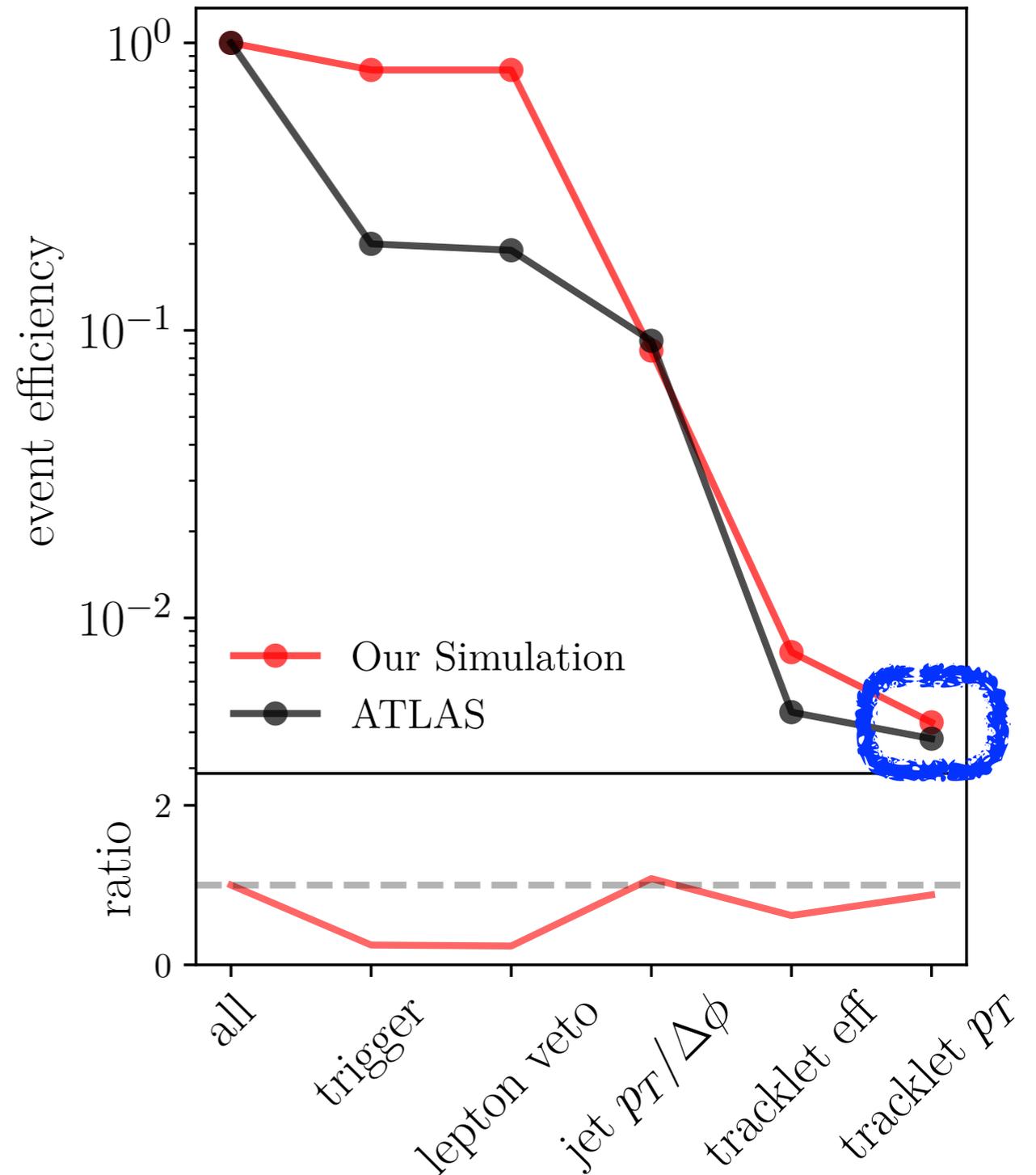
ATLAS collaboration,  
arXiv:1712.02118

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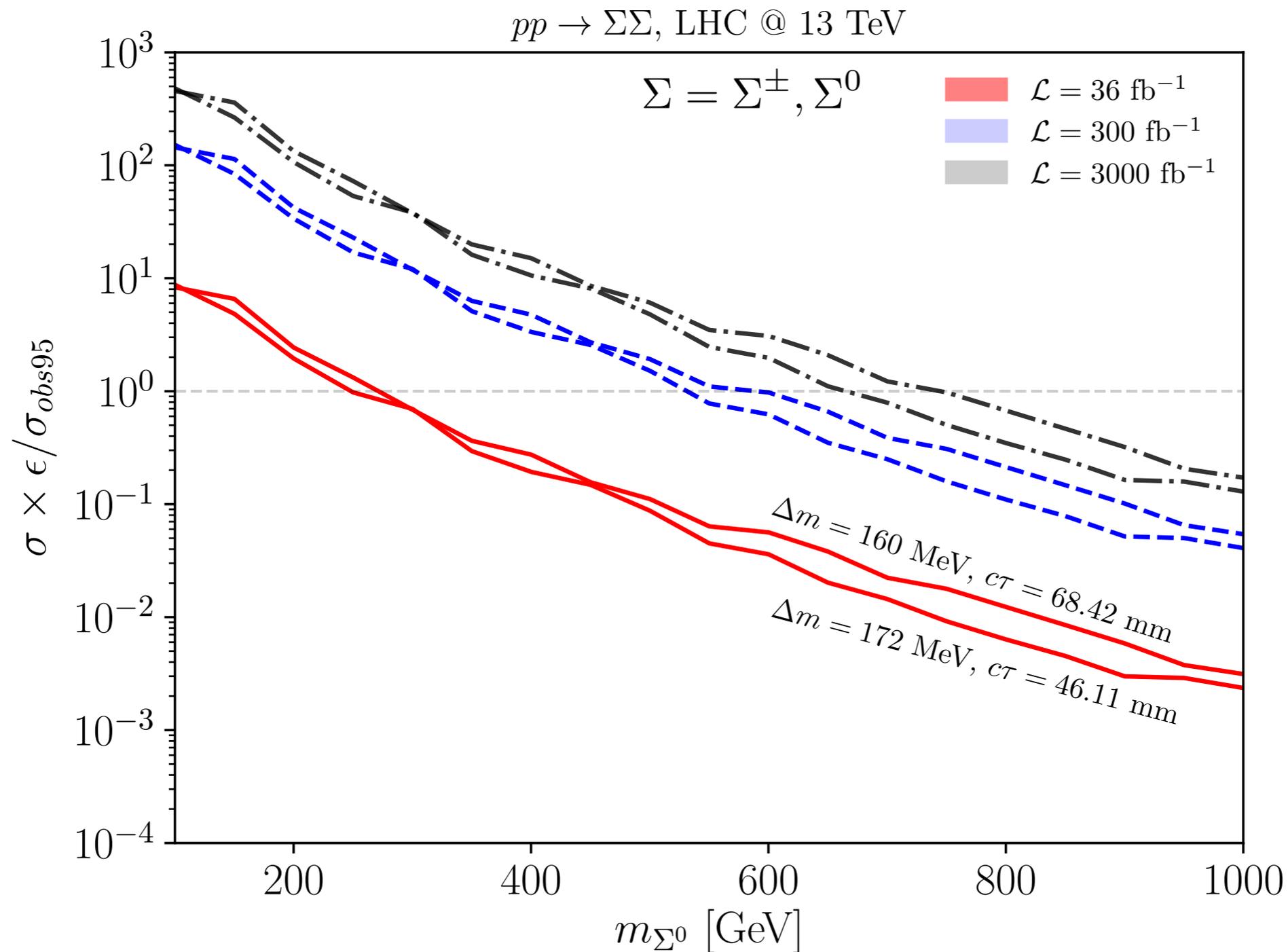
ATLAS collaboration,  
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# What we find... Collider part

C.W. Chiang, G. Cottin, [Yong Du](#),  
K. Fuyuto, M.J. Ramsey-Musolf  
arXiv: 2003.07867

## (HL-)LHC exclusion from cross section



# What we find... Collider part

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## FCC-pp discovery with different pileup control

M. Saito, R. Sawada, K. Terashi and S. Asai, 2019

Benchmark	$\sigma$ [pb]	$\epsilon$	$S$	$B$	$S/\sqrt{B}$
$m_{\Sigma^\pm} = 1.1 \text{ TeV}, \bar{\mu} = 200$	$5.8 \times 10^{-2}$	$3.17 \times 10^{-4}$	553	673	21.3
$m_{\Sigma^\pm} = 1.1 \text{ TeV}, \bar{\mu} = 500$	$5.8 \times 10^{-2}$	$3.17 \times 10^{-4}$	553	8214	6
$m_{\Sigma^\pm} = 3.1 \text{ TeV}, \bar{\mu} = 200$	$9.4 \times 10^{-4}$	$4.69 \times 10^{-4}$	13.3	1.9	9.6
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**3TeV** triplet DM could be discoverable at FCC-pp

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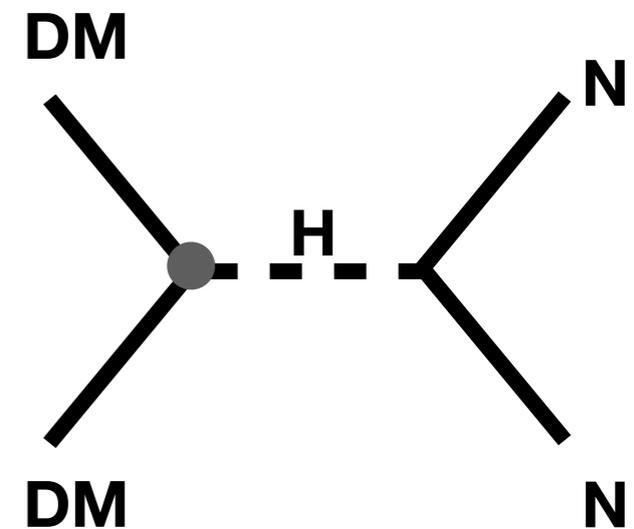
**3TeV** triplet DM could be discoverable at FCC-pp

**Collider searches are a2 insensitive!**

# What we find... **Combination**

C.W. Chiang, G. Cottin, [Yong Du](#),  
K. Fuyuto, M.J. Ramsey-Musolf  
arXiv: 2003.07867

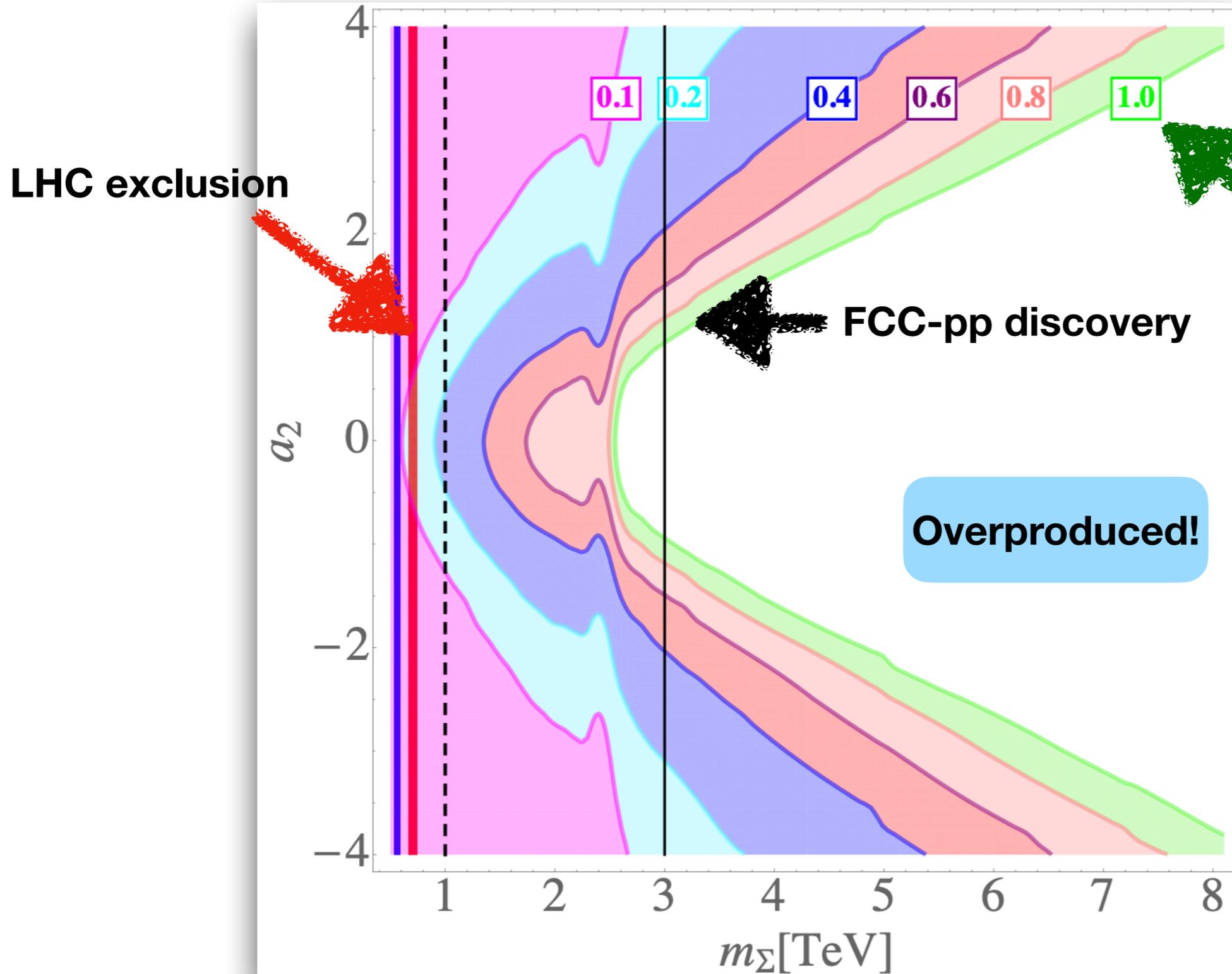
Colliders+relic abundance



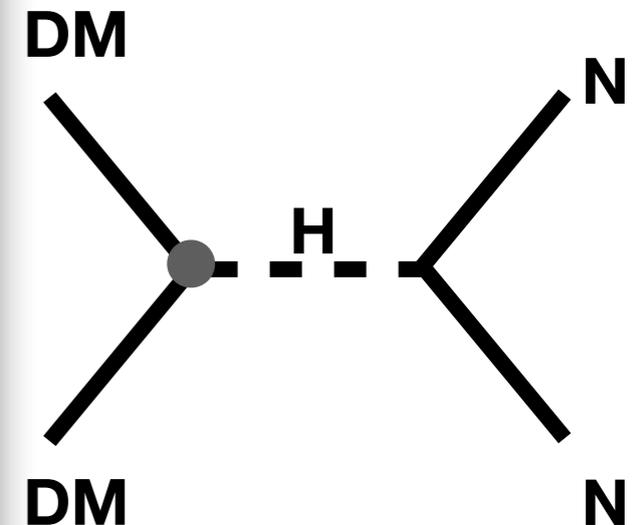
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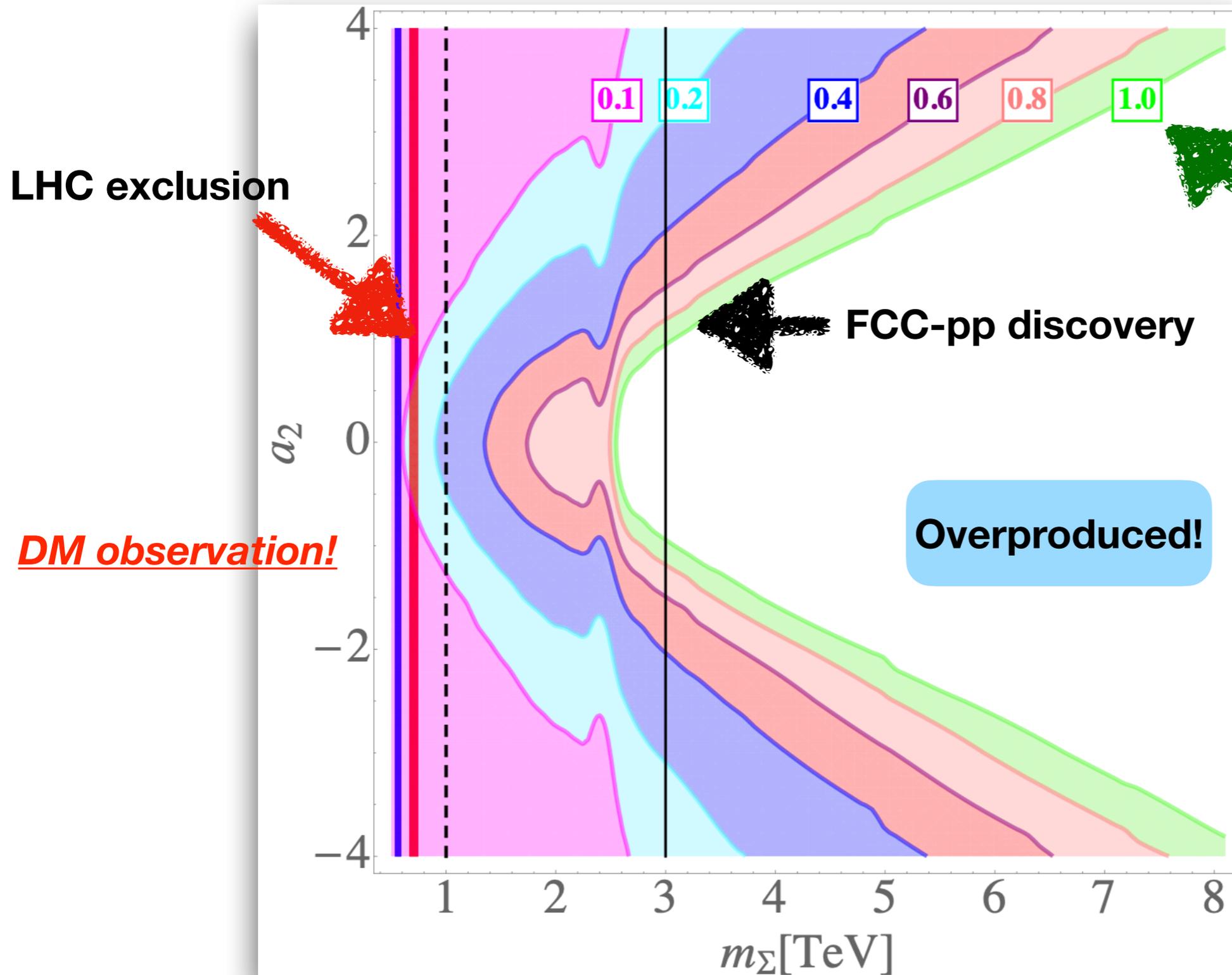
$$\mathcal{R} = \frac{\Omega_\Sigma}{\Omega_{\text{DM}}}$$



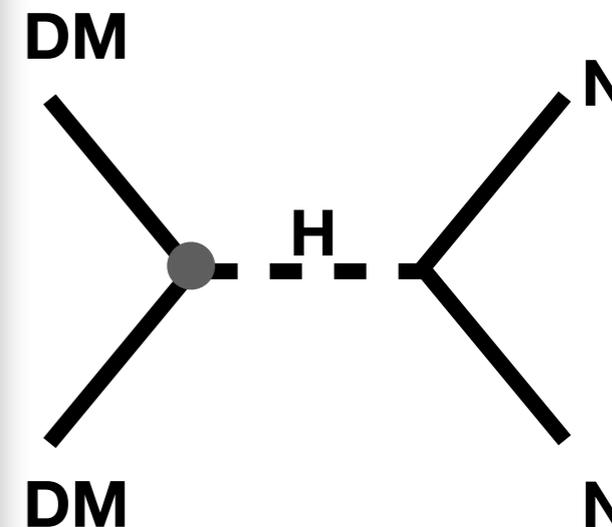
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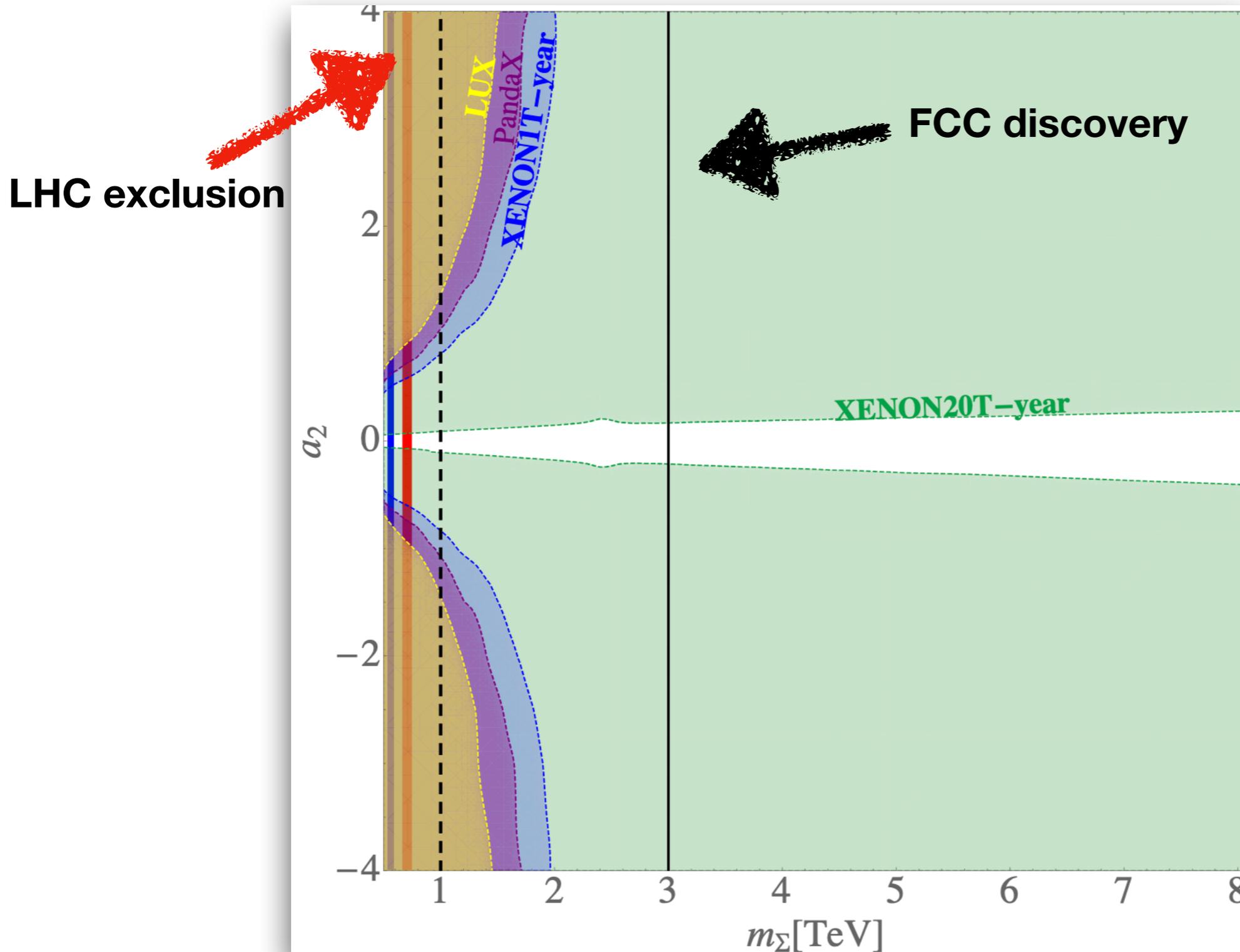


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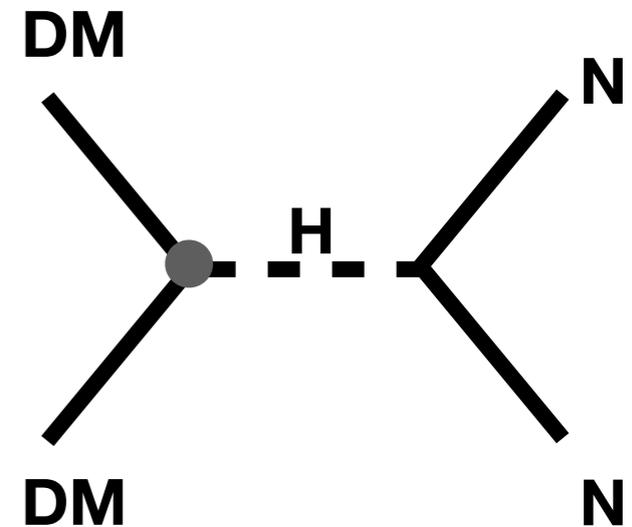


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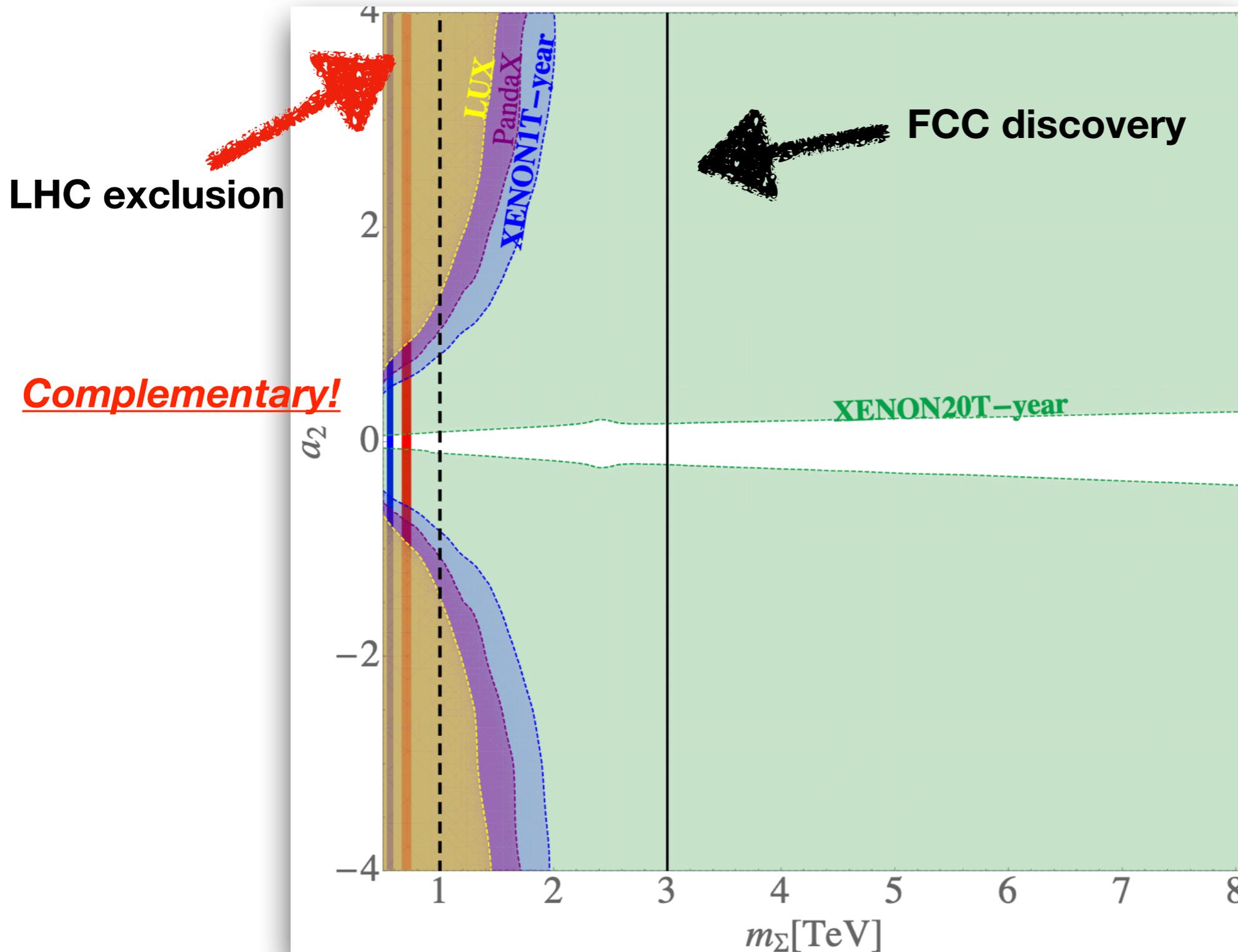


$$\sigma_{\text{SI}}^{\text{scaled}} \equiv \frac{\sigma_{\text{SI}} \Omega h^2}{(\Omega h^2)_{\text{Planck}}}$$

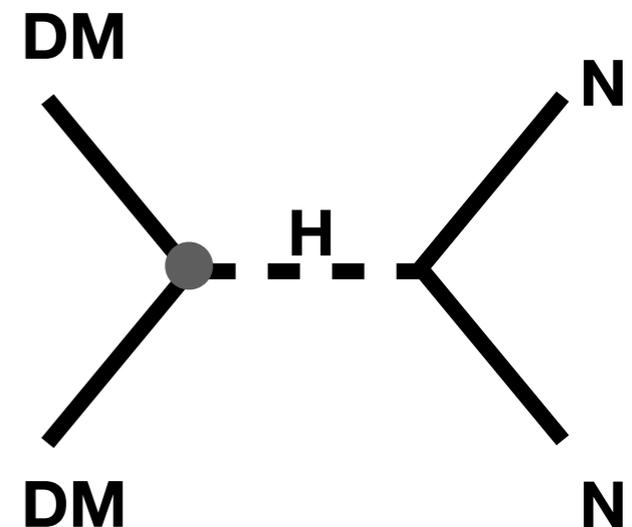


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# The complex triplet model

In collaboration with Aaron Dunbrack, Michael Ramsey-Musolf, Jiang-Hao Yu

Based on JHEP 01(2019)101

# The Complex triplet model

(1) Neutrino masses (type-II seesaw); (2) BAU (EWBG)

SM Higgs Doublet

$$\Phi = \begin{bmatrix} \varphi^+ \\ \frac{1}{\sqrt{2}}(\varphi + i\chi) \end{bmatrix}$$

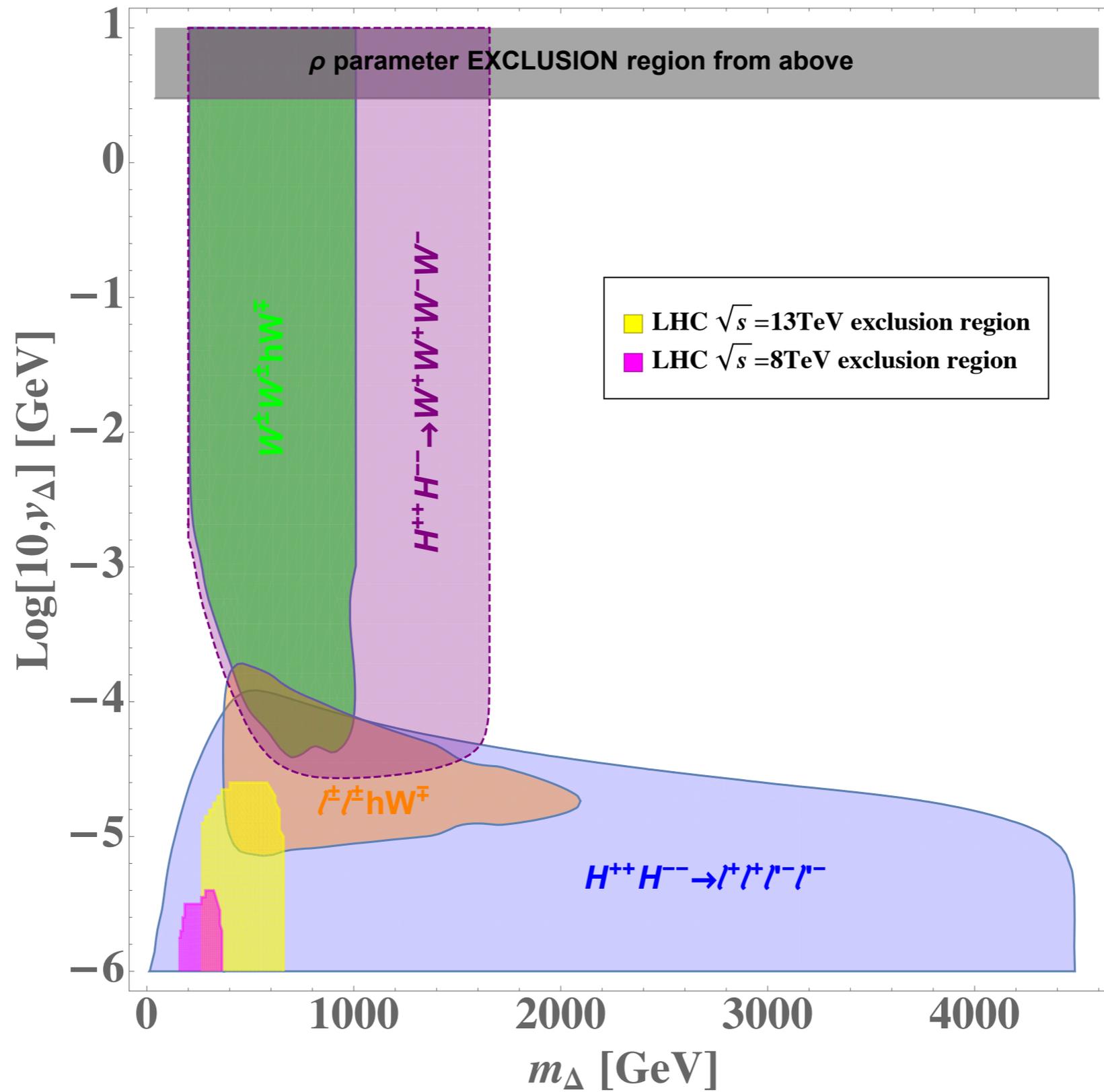
Complex triplet

$$\Delta = \begin{bmatrix} \frac{\Delta^+}{\sqrt{2}} & H^{++} \\ \frac{1}{\sqrt{2}}(\delta + i\eta) & -\frac{\Delta^+}{\sqrt{2}} \end{bmatrix}$$

$$\Delta(1, 3, 2)$$

$$V(\Phi, \Delta) = -m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu \Phi^T i\tau_2 \Delta^\dagger \Phi + \text{h.c.}] + \lambda_1 (\Phi^\dagger \Phi)^2 \\ + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[\Delta^\dagger \Delta \Delta^\dagger \Delta] + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi$$

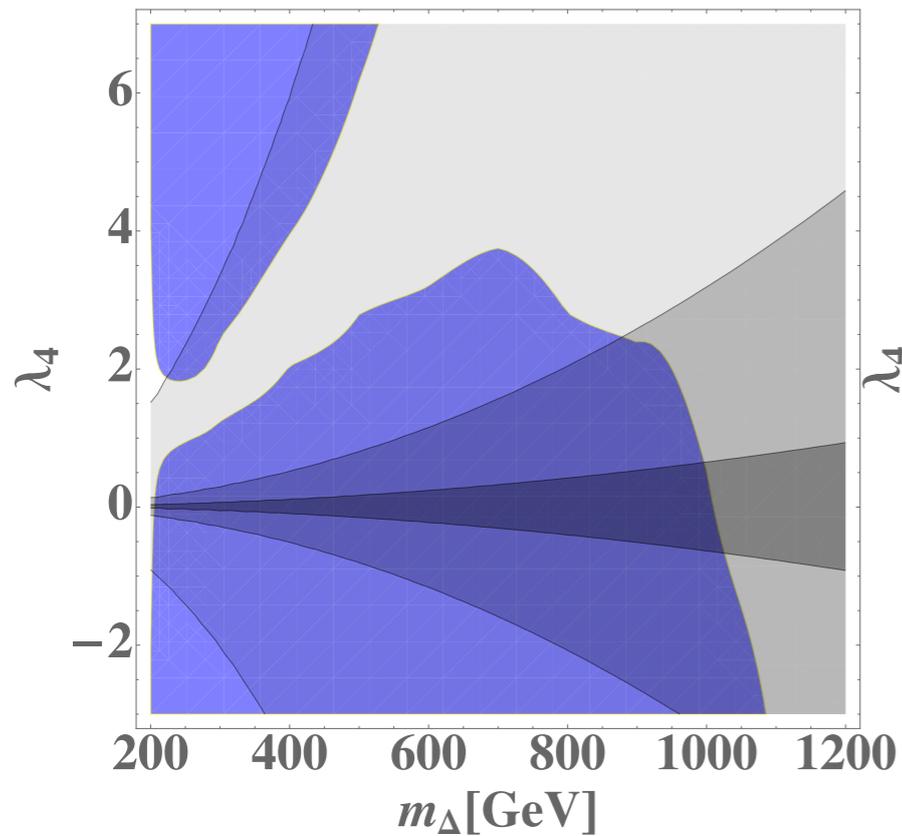
# The Complex triplet model



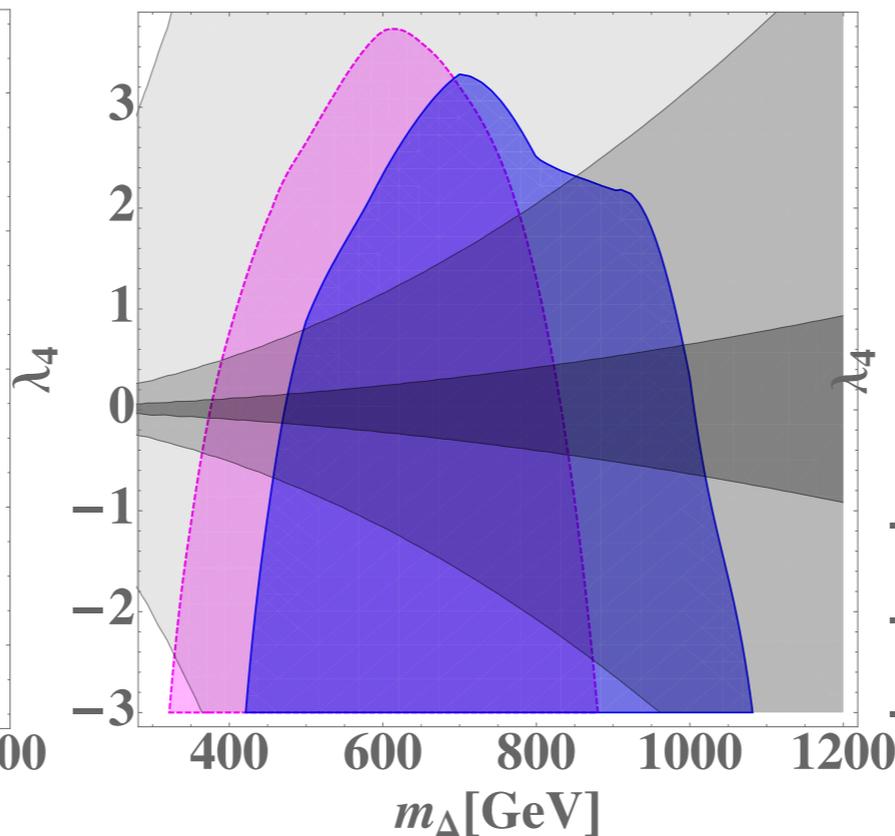
# Higgs portal parameter determination

$hW^\pm W^\mp W^\mp$

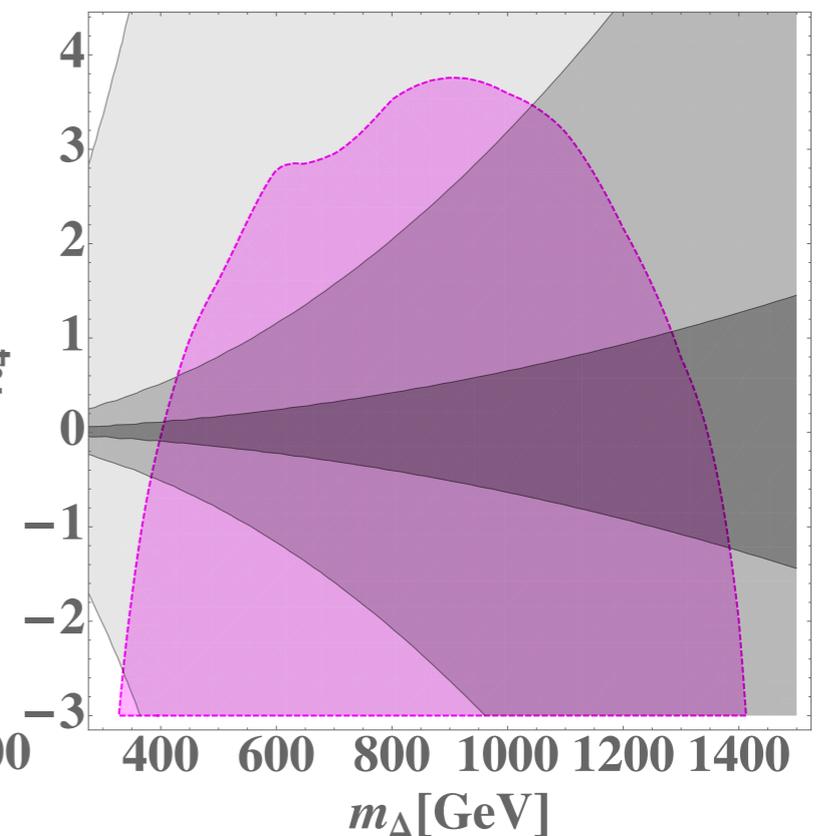
$hW^\pm \ell^\mp \ell^\mp$



$v_\Delta = 10^{-1} \text{ GeV}$



$v_\Delta = 10^{-4} \text{ GeV}$



$v_\Delta = 10^{-5} \text{ GeV}$

$R_{h\gamma\gamma} = 1.16^{+0.20}_{-0.18}$  (LHC)  
 $R_{h\gamma\gamma} = 1 \pm 0.05$  (FCC-ee)  
 $R_{h\gamma\gamma} = 1 \pm 0.01$  (FCC-hh)

ATLAS&CMS, JHEP08, 045 (2016)

Contino et al, CERN Yellow Report (2017)

# Summary

\* The real triplet (1,3,0) model in the dark matter scenario:

1. could be discovered up to  $\sim(300) 800\text{GeV}$  at (HL-)LHC. FCC-pp could **discover 3 TeV** triplet depending on pileup control.
2. XENON1T rules out 1~2TeV triplet (depending on  $a_2$ ), XENON20T would cover **almost the entire parameter space**.
3. Collider and dark matter direct detection are **complementary**.

\* The complex triplet (1,3,2) model:

1. FCC-pp could cover **a significant portion** of its parameter space up to 4TeV.
2. Precision measurements of  $h \rightarrow \gamma\gamma$  help indirectly the Higgs portal parameter determination.

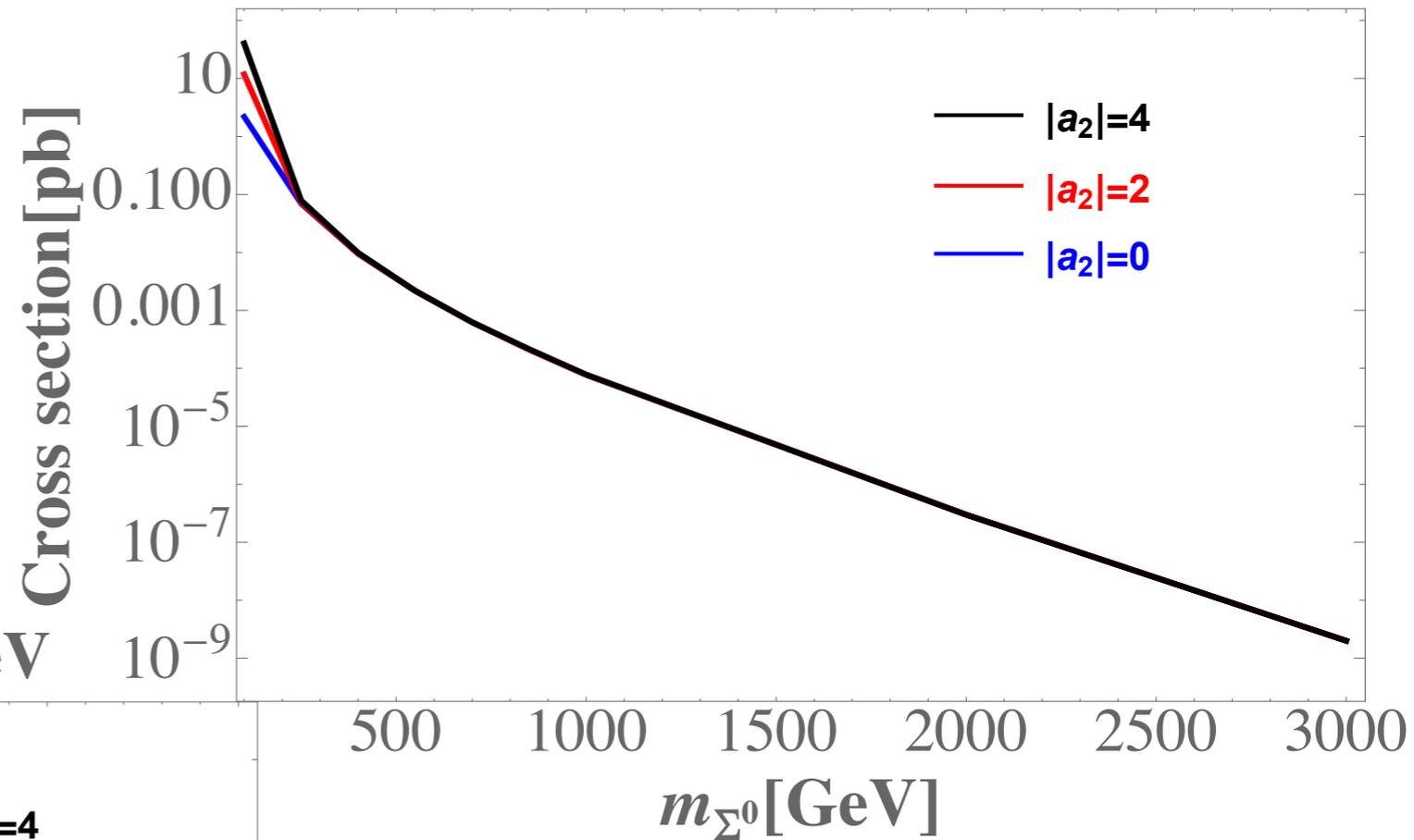
**Backup**

# Production cross section: $a_2$ dependence

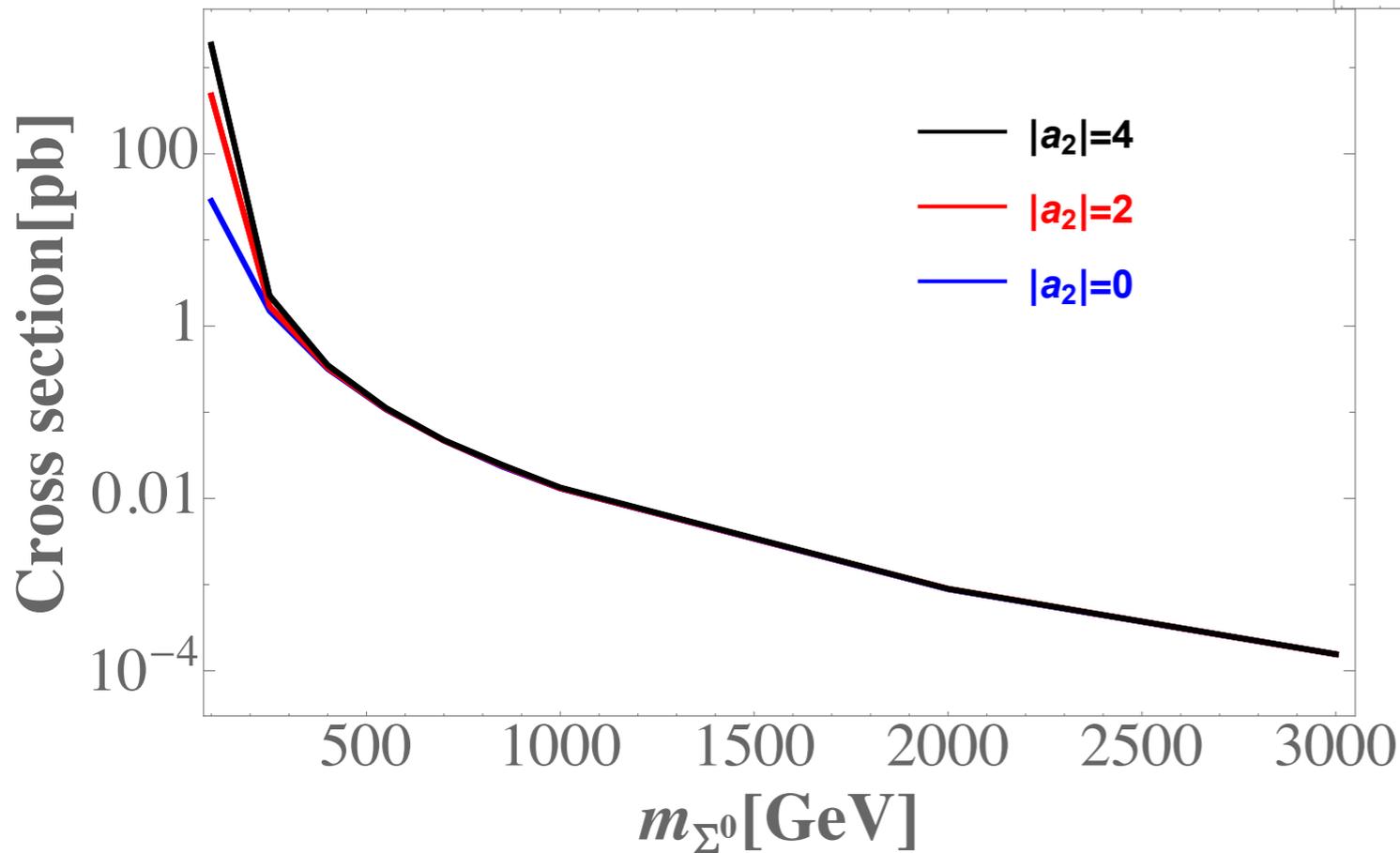
13 TeV



$pp \rightarrow \Sigma \Sigma$  at  $\sqrt{s}=13\text{TeV}$



$pp \rightarrow \Sigma \Sigma$  at  $\sqrt{s}=100\text{TeV}$



100 TeV

C.W. Chiang, G. Cottin, [Yong Du](#),  
K. Fuyuto, M.J. Ramsey-Musolf  
arXiv: 2003.07867

# Cuts applied for the (HL-)LHC

- Trigger :  $\cancel{p}_T > 140 \text{ GeV}$
- Lepton veto : no electrons or muons
- Jet  $p_T/\Delta\phi$  : at least one jet with  $p_T > 140 \text{ GeV}$ , and  $\Delta\phi$  between the  $\cancel{p}_T$  vector and each of the up to four hardest jets with  $p_T > 50 \text{ GeV}$  to be bigger than 1.0
- Tracklet selection : at least one tracklet (generator-level chargino) with :
  - $p_T > 20 \text{ GeV}$  and  $0.1 < |\eta| < 1.9$
  - $122.5 \text{ mm} < \text{decay position} < 295 \text{ mm}$
  - $\Delta R$  distance between the tracklet and each of the up to four highest- $p_T$  jets with  $p_T > 50 \text{ GeV}$  to be bigger than 0.4
  - we apply the tracklet acceptance  $\times$  efficiency map<sup>6</sup> provided by ATLAS, which is based on the decay position and  $\eta$ . This is applied to selected tracklets passing the above selections.
- Tracklet  $p_T$  : Select tracklets with  $p_T > 100 \text{ GeV}$ .

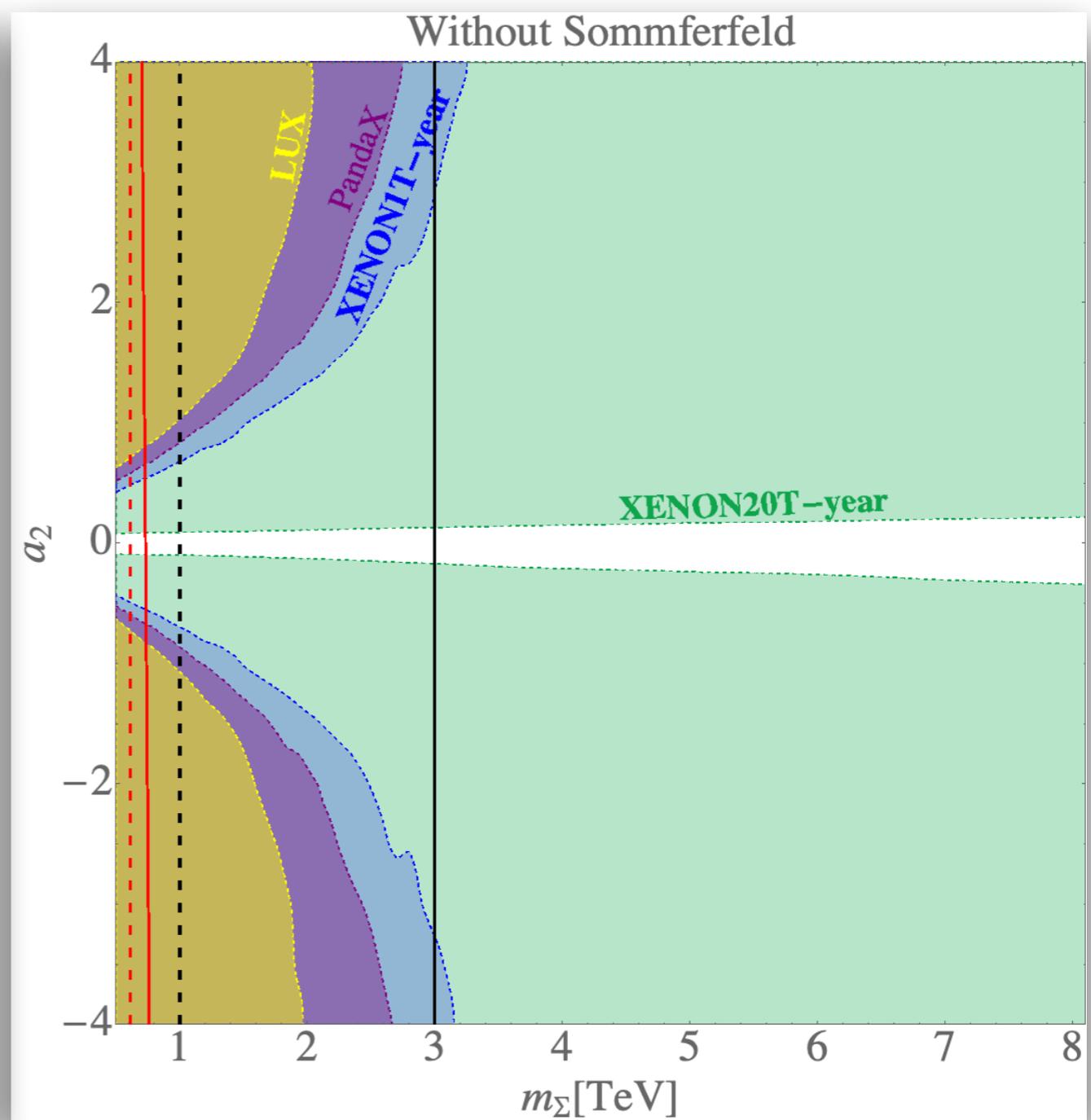
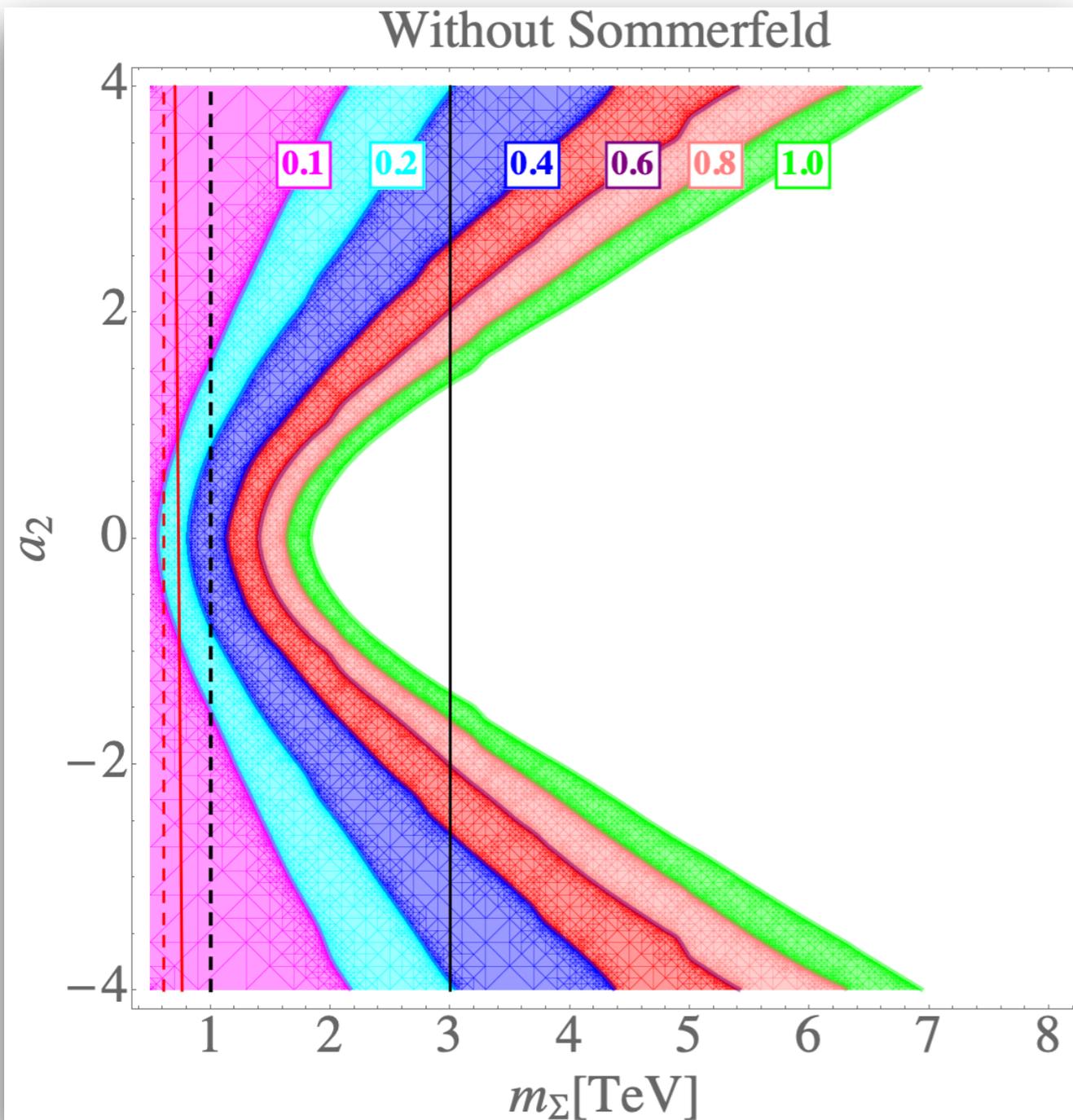
C.W. Chiang, G. Cottin, [Yong Du](#),  
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# Cuts applied for a 100TeV collider

- Trigger :  $\cancel{p}_T > 1 \text{ TeV}$  or  $\cancel{p}_T > 4 \text{ TeV}$  depending on the benchmark as discussed below.
- Lepton veto : no electrons or muons.
- Jet  $p_T/\Delta\phi$  : at least one jet with  $p_T > 1 \text{ TeV}$ , and  $\Delta\phi$  between the  $\cancel{p}_T$  vector and each of the up to four hardest jets with  $p_T > 50 \text{ GeV}$  to be bigger than 1.0.

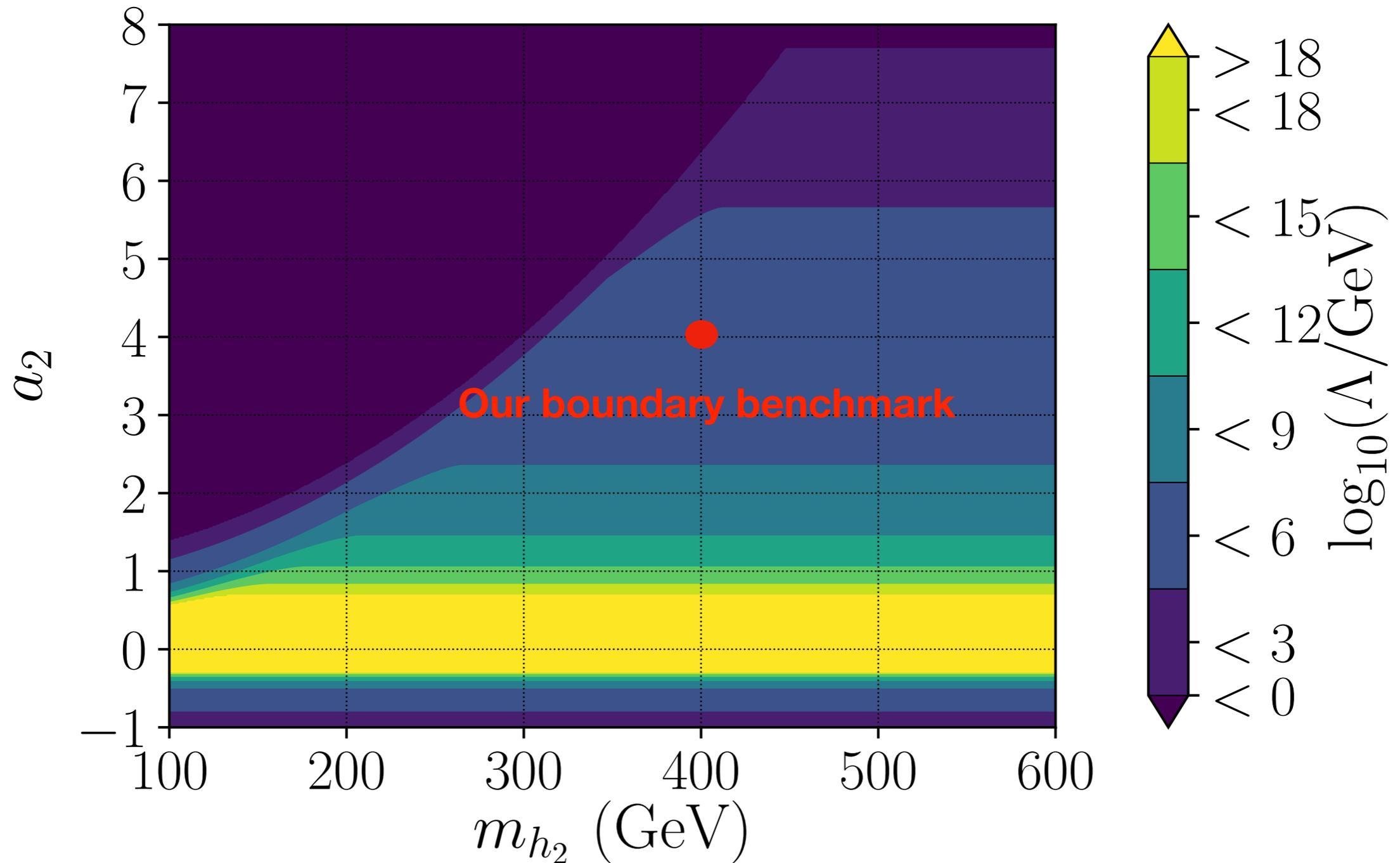
C.W. Chiang, G. Cottin, [Yong Du](#),  
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# Constraints w/o including the Sommerfeld



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K. Fuyuto, M.J. Ramsey-Musolf  
arXiv: 2003.07867

# Constraints from perturbativity and perturbative unitarity



**Complex triplet**

# Model key features

$\Delta(1, 3, 2)$

$$V(\Phi, \Delta) = -m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu \Phi^T i\tau_2 \Delta^\dagger \Phi + \text{h.c.}] + \lambda_1 (\Phi^\dagger \Phi)^2 \\ + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[\Delta^\dagger \Delta \Delta^\dagger \Delta] + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi$$

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = \frac{1 + \frac{2v_\Delta^2}{v_\Phi^2}}{1 + \frac{4v_\Delta^2}{v_\Phi^2}}$$

$$\rho = 1.0006 \pm 0.0009$$

PDG, 2016

$$0 \leq v_\Delta \lesssim 3.0 \text{ GeV}$$

$$v_\Delta \ll v_\Phi \simeq v$$

$$v = \sqrt{v_\Delta^2 + v_\Phi^2} = 246 \text{ GeV}$$

$$\sin \beta_\pm \sim \sin \beta_0 \sim \sin \alpha \sim \frac{v_\Delta}{v_\Phi} \sim 0$$

# Model key features

$$\Delta m = |m_{H^{\pm\pm}} - m_{H^\pm}| \approx |m_{H^\pm} - m_{H,A}| \approx \frac{|\lambda_5| v_\Phi^2}{8m_\Delta} \approx \frac{|\lambda_5| v^2}{8m_\Delta}$$

Determined by mass splitting

$$m_h^2 \simeq 2v_\Phi^2 \lambda_1 \simeq 2v^2 \lambda_1, \quad m_H \simeq m_\Delta \simeq m_A, \quad m_{H^\pm}^2 \simeq m_\Delta^2 - \frac{\lambda_5}{4} v_\Phi^2, \quad m_{H^{\pm\pm}}^2 \simeq m_\Delta^2 - \frac{\lambda_5}{2} v_\Phi^2$$

Fixed by SM  
Higgs mass  
 $\lambda_1 \simeq 0.129$

Basically the mass  
scale of the triplet

# Model key features

$$m_h^2 \simeq 2v_\Phi^2 \lambda_1 \simeq 2v^2 \lambda_1, \quad m_H \simeq m_\Delta \simeq m_A, \quad m_{H^\pm}^2 \simeq m_\Delta^2 - \frac{\lambda_5}{4} v_\Phi^2, \quad m_{H^{\pm\pm}}^2 \simeq m_\Delta^2 - \frac{\lambda_5}{2} v_\Phi^2$$

Also determines the mass hierarchy

$$\lambda_5 \leq 0 : m_h < m_H \simeq m_A \leq m_{H^\pm} \leq m_{H^{\pm\pm}}$$

# Model key features

$$V(\Phi, \Delta) = -m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu \Phi^T i\tau_2 \Delta^\dagger \Phi + \text{h.c.}] + \lambda_1 (\Phi^\dagger \Phi)^2 \\ + \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[\Delta^\dagger \Delta \Delta^\dagger \Delta] + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi$$

How determine?

$$\text{Br}(A \rightarrow hZ, H \rightarrow ZZ, H \rightarrow W^+ W^-, H^\pm \rightarrow hW^\mp) = F(\lambda_4, \lambda_5, \dots)$$

# Model key features

## Brief summary

$$V(\Phi, \Delta) = -m^2 \Phi^\dagger \Phi + M^2 \text{Tr}(\Delta^\dagger \Delta) + [\mu \Phi^T i\tau_2 \Delta^\dagger \Phi + \text{h.c.}] + \lambda_1 (\Phi^\dagger \Phi)^2$$
$$+ \lambda_2 [\text{Tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{Tr}[\Delta^\dagger \Delta \Delta^\dagger \Delta] + \lambda_4 (\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi$$

Fixed by SM Higgs mass

From the BRs

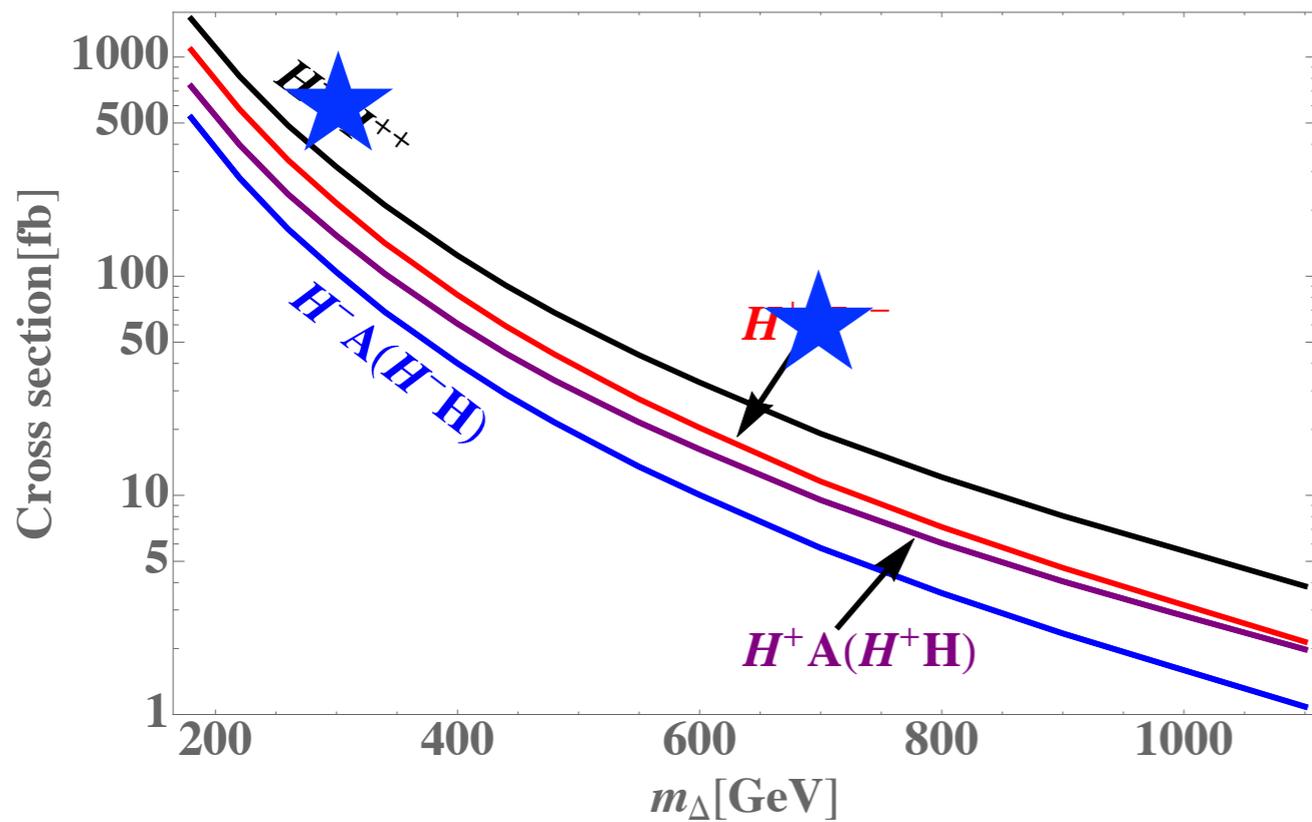
Determined by mass splitting

Remain unknown

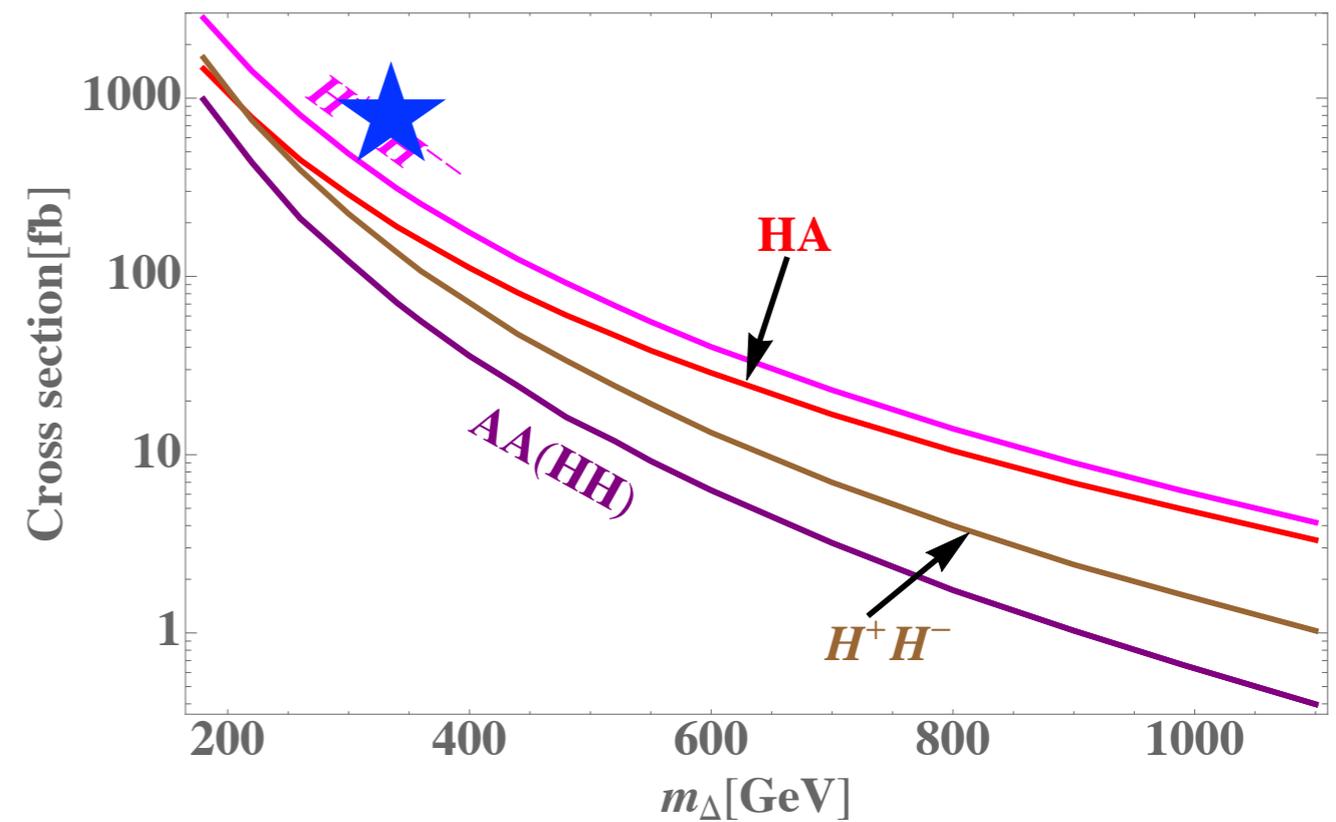
# Model discovery

$$\lambda_1 = 0.129, \lambda_2 = 0.2, \lambda_3 = 0, \lambda_4 = 0, \lambda_5 = -0.1$$

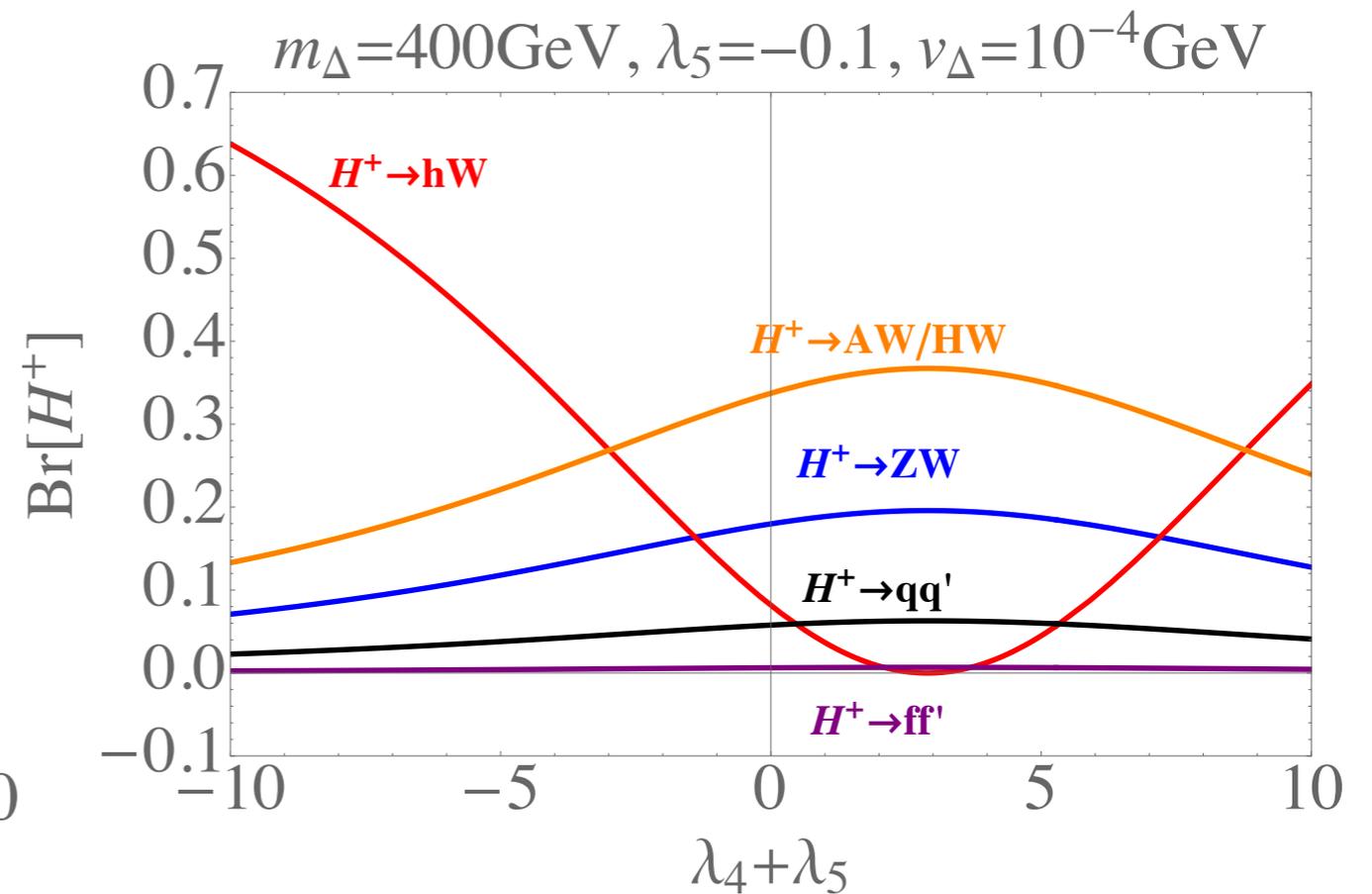
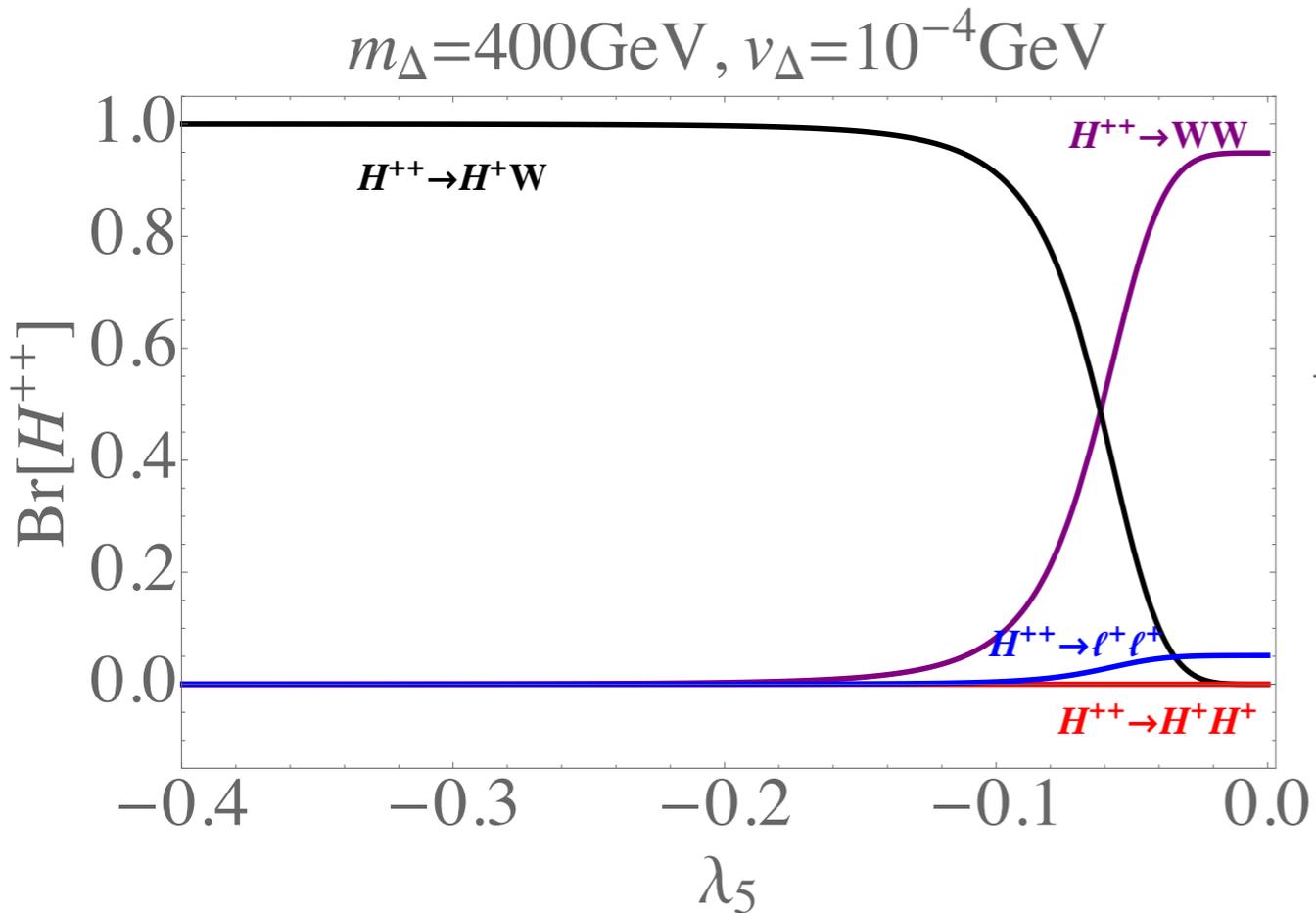
Production cross section at  $\sqrt{s} = 100\text{TeV}$



Production cross section at  $\sqrt{s} = 100\text{TeV}$



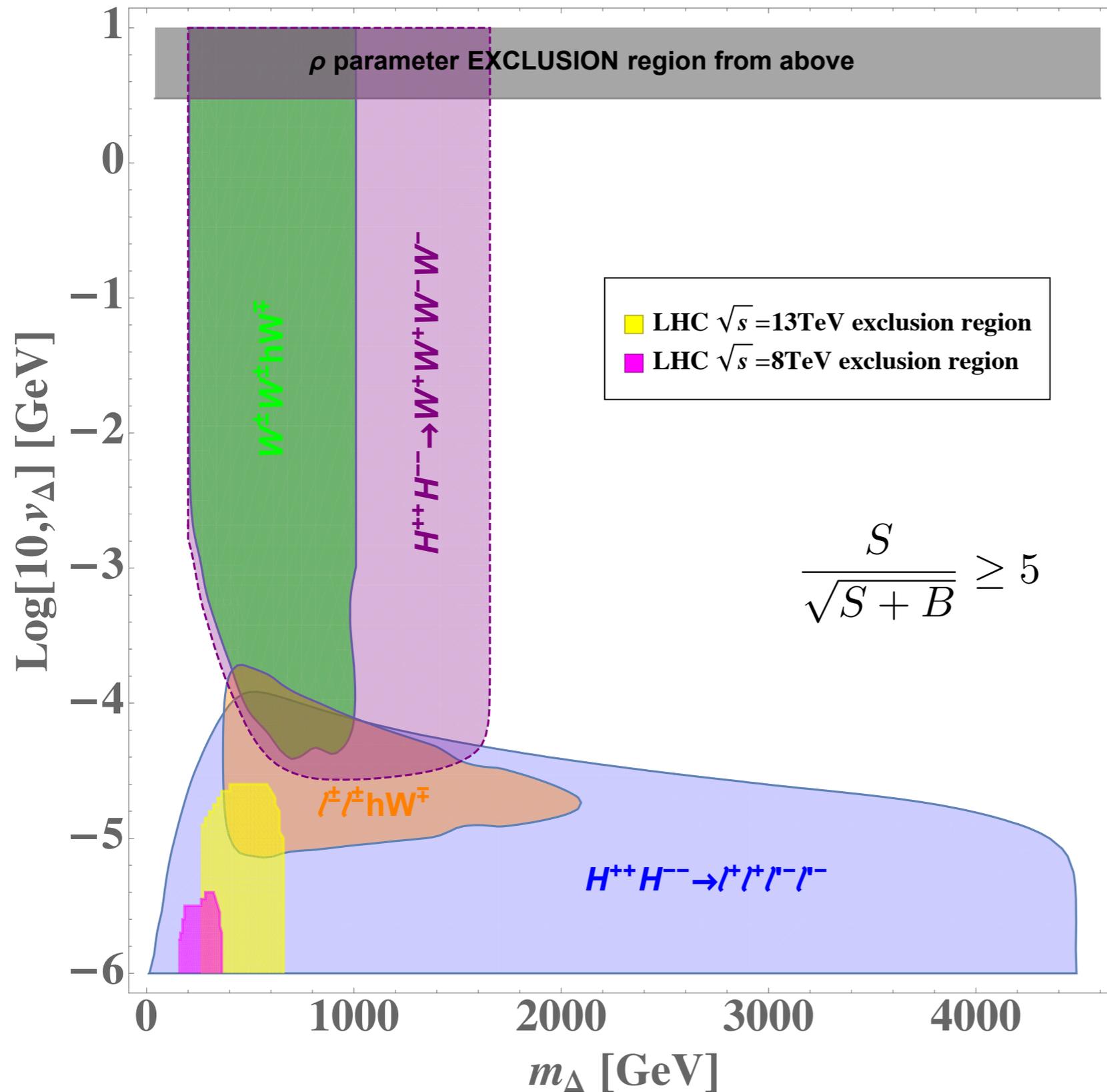
# Model discovery



$pp \rightarrow H^{++} H^{--}$  and  $pp \rightarrow H^{\pm\pm} H^{\mp}$   
 $H^{\pm\pm} \rightarrow \ell^{\pm} \ell^{\pm}$  ( $W^{\pm} W^{\pm}$ ) and  $H^{\mp} \rightarrow hW^{\mp}$

↓ **small  $v_{\Delta}$** 
↓ **large  $v_{\Delta}$**

# Model discovery



$$\lambda_2 = 0.2$$

$$\lambda_3 = 0$$

$$\lambda_4 = 0$$

$$\lambda_5 = -0.1$$

ATLAS, JHEP03, 041(2015)

ATLAS, Eur. Phys. J C 78 (2018)

$$m_{H^{\pm\pm}}^2 \simeq m_\Delta^2 - \frac{\lambda_5}{2} v_\Phi^2$$

$$m_\Delta \geq 0 \text{ GeV}$$

$$\Leftrightarrow m_{H^{\pm\pm}} \geq 54.78 \text{ GeV}$$

**LEP constraints  
automatically satisfied**

OPAL (1992, 2002)

# Higgs portal parameter determination

$$\Delta m = |m_{H^{\pm\pm}} - m_{H^\pm}| \approx |m_{H^\pm} - m_{H,A}| \approx \frac{|\lambda_5|v_\Phi^2}{8m_\Delta} \approx \frac{|\lambda_5|v^2}{8m_\Delta}$$

Upon discovery,  $\lambda_5$  can be determined readily by the mass splitting.

Can determine  $\lambda_4$  from precise measurements on  $\text{Br}(H^\pm \rightarrow hW^\pm)$  after discovery.

Parameter scan on the  $v_\Delta$ - $m_\Delta$  plane and BDT analysis for

$$pp \rightarrow H^{\pm\pm} H^\mp \rightarrow \ell^\pm \ell^\pm hW^\mp / W^\pm W^\pm hW^\mp$$