

# Rare charm decays

# 稀有魅力衰減

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Overview

SM in rare charm decays

NP

NP in D meson in rare charm decays

NP in B anomalies  $\rightarrow$  NP in charm  
Impact of  $D^0 - \bar{D}^0$  on rare charm decays  
Signatures of NP in FCNC charm decays

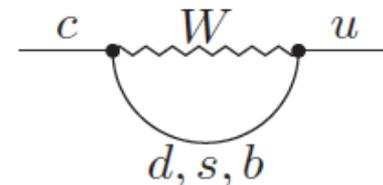
$D \rightarrow V \gamma$   
 $D \rightarrow P_1 P_2 \gamma$   
 $D \rightarrow P l^+ l^-$   
 $D \rightarrow l^+ l^-$   
 $D \rightarrow P_1 P_2 l^+ l^-$   
 $D \rightarrow$  invisibles

Summary and Outlook

# SM effective Hamiltonian for rare charm decays -FCNC

$$\mathcal{H}_{\text{eff}} = \lambda_d \mathcal{H}^d + \lambda_s \mathcal{H}^s - \frac{4G_F \lambda_b}{\sqrt{2}} \sum_{i=3, \dots, 10, S, P, \dots} C_i \mathcal{O}_i$$

$$\lambda_q = V_{uq} V_{cq}^*$$



Tree-level 4-quark operators      (Short-distance) penguin operators

- 1) At scale  $m_W$  all penguin contributions vanish due to GIM;
- 2) SM contributions to  $C_{7\dots 10}$  at scale  $m_c$  entirely due to mixing of tree-level operators into penguin ones under QCD
- 3) SM values at  $m_c$

# Effective weak Lagrangian

$$\mathcal{L}_{\text{eff}}^{\text{weak}} = \frac{4G_F}{\sqrt{2}} \left( \sum_{q \in \{d,s\}} V_{cq}^* V_{uq} \sum_{i=1}^2 C_i Q_i^{(q)} + \sum_{i=3}^6 C_i Q_i + \sum_{i=7}^8 (C_i Q_i + C'_i Q'_i) \right)$$

$$Q_1^{(q)} = (\bar{u}_L \gamma_{\mu_1} T^a q_L) (\bar{q}_L \gamma^{\mu_1} T^a c_L),$$

$$Q_2^{(q)} = (\bar{u}_L \gamma_{\mu_1} q_L) (\bar{q}_L \gamma^{\mu_1} c_L),$$

$$Q_3 = (\bar{u}_L \gamma_{\mu_1} c_L) \sum_{\{q:m_q < \mu_c\}} (\bar{q} \gamma^{\mu_1} q),$$

$$Q_4 = (\bar{u}_L \gamma_{\mu_1} T^a c_L) \sum_{\{q:m_q < \mu_c\}} (\bar{q} \gamma^{\mu_1} T^a q),$$

$$Q_5 = (\bar{u}_L \gamma_{\mu_1} \gamma_{\mu_2} \gamma_{\mu_3} c_L) \sum_{\{q:m_q < \mu_c\}} (\bar{q} \gamma^{\mu_1} \gamma^{\mu_2} \gamma^{\mu_3} q),$$

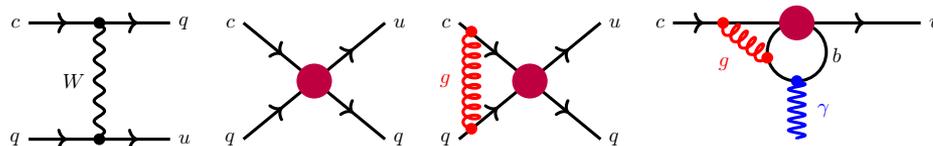
$$Q_6 = (\bar{u}_L \gamma_{\mu_1} \gamma_{\mu_2} \gamma_{\mu_3} T^a c_L) \sum_{\{q:m_q < \mu_c\}} (\bar{q} \gamma^{\mu_1} \gamma^{\mu_2} \gamma^{\mu_3} T^a q),$$

$$Q_7 = \frac{e m_c}{16\pi^2} (\bar{u}_L \sigma^{\mu_1 \mu_2} c_R) F_{\mu_1 \mu_2},$$

$$Q'_7 = \frac{e m_c}{16\pi^2} (\bar{u}_R \sigma^{\mu_1 \mu_2} c_L) F_{\mu_1 \mu_2},$$

$$Q_8 = \frac{g_s m_c}{16\pi^2} (\bar{u}_L \sigma^{\mu_1 \mu_2} T^a c_R) G_{\mu_1 \mu_2}^a,$$

$$Q'_8 = \frac{g_s m_c}{16\pi^2} (\bar{u}_R \sigma^{\mu_1 \mu_2} T^a c_L) G_{\mu_1 \mu_2}^a,$$

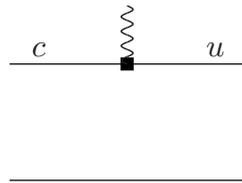


- matching of SM contributions onto Weak Effective Theory at  $\mu = M_W$  ;
- RG-evolution of Wilson coefficients from  $M_W$  to  $m_b$ ,
- integrating out the b quark and second matching at  $\mu = m_b$ ,
- RG-evolution of Wilson coefficients from  $m_b$  to the charm scale  $\mu_c$ .

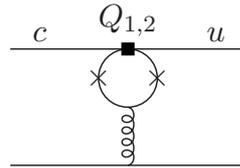
(recent results: Gisbert et al. 2011.09478, de Boer, Hiller, 1510.00311, 1701.06392, De Boer et al, 1606.05521, 1707.00988

SF& Singer, hep-ph/9705327, hep-ph/9901252, SF, Prelovsek & Singer hep-ph/9801279)

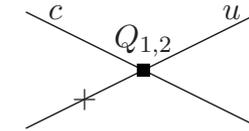
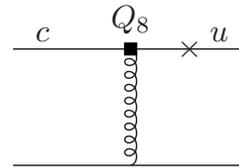
## SM Corrections: hard spectator and weak annihilation



spectating



hard spectator interaction



weak annihilation

Leading hard spectator within QCD factorization adopted from B physics

$$\lambda_D \sim \Lambda_{\text{QCD}} \sim \mathcal{O}(0.1 \text{ GeV})$$

scale dependence varied  $\mu_c \in [m_c/\sqrt{2}, \sqrt{2}m_c]$

$$C_7^{\text{HSI},\rho} \in [0.00051 + 0.0014i, 0.00091 + 0.0020i] \cdot \frac{\text{GeV}}{\lambda_D}, \quad C_7^{\text{WA},\rho^0} \in [-0.010, -0.0011] \cdot \frac{\text{GeV}}{\lambda_D}$$

$$C_7^{\text{HSI},\omega} \in [0.00030 + 0.0010i, 0.00098 + 0.0020i] \cdot \frac{\text{GeV}}{\lambda_D}, \quad C_7^{\text{WA},\omega} \in [0.0097, 0.0011] \cdot \frac{\text{GeV}}{\lambda_D},$$

$$C_7^{\text{HSI},K^{*+}} \in [0.00032 + 0.0013i, 0.00096 + 0.0022i] \cdot \frac{\text{GeV}}{\lambda_D}, \quad C_7^{\text{WA},\rho^+} \in [0.029, 0.038] \cdot \frac{\text{GeV}}{\lambda_D},$$

$$C_7^{\text{WA},K^{*+}} \in [-0.034, -0.047] \cdot \frac{\text{GeV}}{\lambda_D}$$

hard spectator interaction- adopted from B

DeBoer & Hiller 1701.06392

SD contributions C. Greub et al., PLB 382 (1996) 415;

D → Vγ

branching ratio	$D^0 \rightarrow \rho^0 \gamma$	$D^0 \rightarrow \omega \gamma$	$D^+ \rightarrow \rho^+ \gamma$	$D_s \rightarrow K^{*+} \gamma$
two-loop QCD	$(0.14 - 2.0) \cdot 10^{-8}$	$(0.14 - 2.0) \cdot 10^{-8}$	$(0.75 - 1.0) \cdot 10^{-8}$	$(0.32 - 5.5) \cdot 10^{-8}$
HSI+WA	$(0.11 - 3.8) \cdot 10^{-6}$	$(0.078 - 5.2) \cdot 10^{-6}$	$(1.6 - 1.9) \cdot 10^{-4}$	$(1.0 - 1.4) \cdot 10^{-4}$
hybrid	$(0.041 - 1.17) \cdot 10^{-5}$	$(0.042 - 1.12) \cdot 10^{-5}$	$(0.017 - 2.33) \cdot 10^{-4}$	$(0.053 - 1.54) \cdot 10^{-4}$
*	$(0.1 - 1) \cdot 10^{-5}$	$(0.1 - 0.9) \cdot 10^{-5}$	$(0.4 - 6.3) \cdot 10^{-5}$	$(1.2 - 5.1) \cdot 10^{-5}$
**	$(0.1 - 0.5) \cdot 10^{-5}$	$0.2 \cdot 10^{-5}$	$(2 - 6) \cdot 10^{-5}$	$(0.8 - 3) \cdot 10^{-5}$
***	$3.8 \cdot 10^{-6}$	–	$4.6 \cdot 10^{-6}$	–
data <sup>†</sup>	$(1.77 \pm 0.31) \cdot 10^{-5}$	$< 2.4 \cdot 10^{-4}$	–	–

Hiller & De Boer 1701.06392

\* SF& Singer, hep-ph/9705327, hep-ph/9901252, SF, Prelovsek & Singer hep-ph/9801279

\*\* Burdman et al. hep-ph/9502329,

\*\*\* Khodjamirian et al., hep-ph/9506242

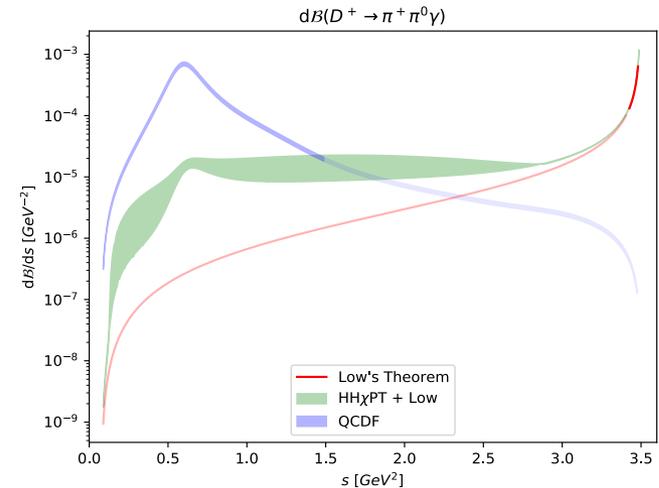
Hybrid model: LD effects included in form-factors for D → Vγ

“poor convergence of the  $1/m_c$  and  $\alpha_s$ -expansion prohibits a sharp conclusion without further study “

Note: all SM th. predictions for  
BR( $D^0 \rightarrow \rho^0 \gamma$ ) smaller than exp. rates!

$$D \rightarrow P_1 P_2 \gamma$$

- CF:  $D_s \rightarrow \pi^+ \pi^0 \gamma$ ,  $D_s \rightarrow K^+ \bar{K}^0 \gamma$ ,  $D^+ \rightarrow \pi^+ \bar{K}^0 \gamma$ , ( $D^0 \rightarrow \pi^0 \bar{K}^0 \gamma$ ,
- SCS:  $D^+ \rightarrow \pi^+ \pi^0 \gamma$ ,  $D_s \rightarrow \pi^+ K^0 \gamma$ ,  $D_s \rightarrow K^+ \pi^0 \gamma$ ,  
 $D^+ \rightarrow K^+ \bar{K}^0 \gamma$ , ( $D^0 \rightarrow \pi^+ \pi^- \gamma$ ,  $D^0 \rightarrow K^+ K^- \gamma$ )
- DCS:  $D^+ \rightarrow \pi^+ K^0 \gamma$ ,  $D^+ \rightarrow K^+ \pi^0 \gamma$ ,  $D_s \rightarrow K^+ K^0 \gamma$



”sizable effects of the dipole operators can be seen for differential branching ratios and forward backward asymmetries – it is difficult to claim sensitivity to NP due to the uncertainties of the leading order calculation and the intrinsic uncertainty of the Breit-Wigner contributions.” – Adolph & Hiller 2104.08287, Adolph et al., 2009.14212, SF et al., hep-ph/0204306, [hep-ph/0210423.

## CP asymmetry in charm radiative decays

CP asymmetries in  $c \rightarrow u\gamma$  transitions constitute SM null tests

$$A_{CP}(D \rightarrow V\gamma) = \frac{\Gamma(D \rightarrow V\gamma) - \Gamma(\bar{D} \rightarrow \bar{V}\gamma)}{\Gamma(D \rightarrow V\gamma) + \Gamma(\bar{D} \rightarrow \bar{V}\gamma)}$$

$$|A_{CP}^{\text{SM}}| < 2 \cdot 10^{-3}$$

large uncertainties!

Experiment

Belle, 1603.03257

$$A_{CP}(D^0 \rightarrow \rho^0\gamma) = 0.056 \pm 0.152 \pm 0.006,$$

$$A_{CP}(D^0 \rightarrow \phi\gamma) = -0.094 \pm 0.066 \pm 0.001$$

$$A_{CP}(D^0 \rightarrow \bar{K}^{*0}\gamma) = -0.003 \pm 0.020 \pm 0.000$$

Hiller& de Boer 1701. 06392

LQs might give as large

contributions as SM

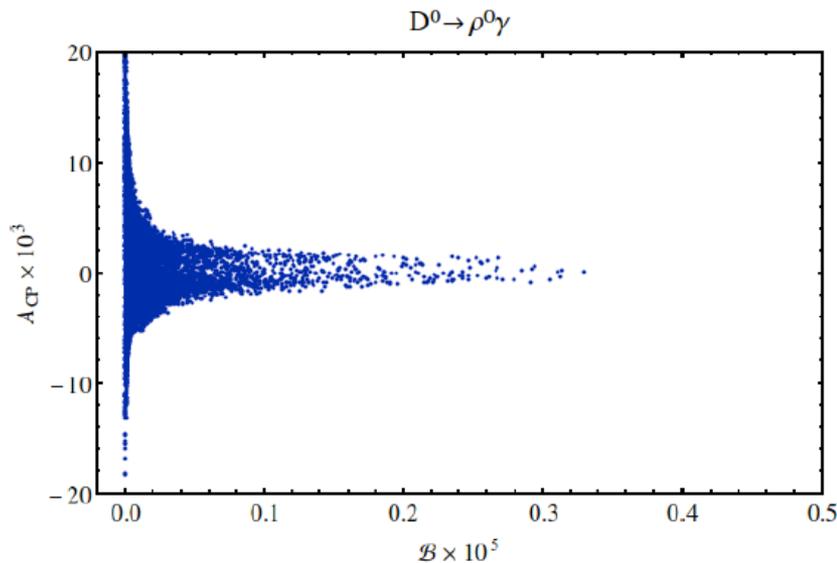
$D^0 \rightarrow \phi\gamma$  or  $D^0 \rightarrow K^{*0}\gamma$  decays (SM-dominated)

the polarization fraction  $r$

$$A_{L,R}^{\text{SM}}(\rho^0) = A_{L,R}(\bar{K}^{*0}) \times [\text{U-spin corrections}]$$

$D^0 \rightarrow \rho^0\gamma$

the photon polarization and therefore  $A_\Delta$  in  $D^0 \rightarrow \rho^0(\rightarrow \pi^+\pi^-)\gamma$  becomes a null test of the SM.



Authors varied the form factor, the two-loop QCD and hard spectator interaction plus weak annihilation within uncertainties, where  $\lambda_D \in [0.1, 0.6]$  GeV,  $A_{7-}$  contributions and relative strong phases.

Chromo-magnetic operator important for the CP asymmetry

$$A_{CP}|_{\langle Q_8, Q'_8 \rangle} \sim -\text{Im} \left[ 2C_8 + \frac{1}{2}C'_8 \right]$$

$$D \rightarrow \pi l^+ l^-$$

SD dynamics  
SM

$$\mathcal{C}_7^{\text{eff}}(q^2 \approx 0) \simeq -0.0011 - 0.0041 i$$

$$\mathcal{C}_9^{\text{eff}}(q^2) \simeq -0.021 \left[ V_{cd}^* V_{ud} L(q^2, m_d, \mu_c) + V_{cs}^* V_{us} L(q^2, m_s, \mu_c) \right],$$

$$\mathcal{C}_{10}^{\text{SM}} = 0 \quad \text{Only for D, different for B and K in SM}$$

$$\mathcal{C}_i^{\prime \text{SM}} = \mathcal{C}_S^{\text{SM}} = \mathcal{C}_T^{\text{SM}} = \mathcal{C}_{T5}^{\text{SM}} = \mathcal{C}_{10}^{\text{SM}} = 0$$

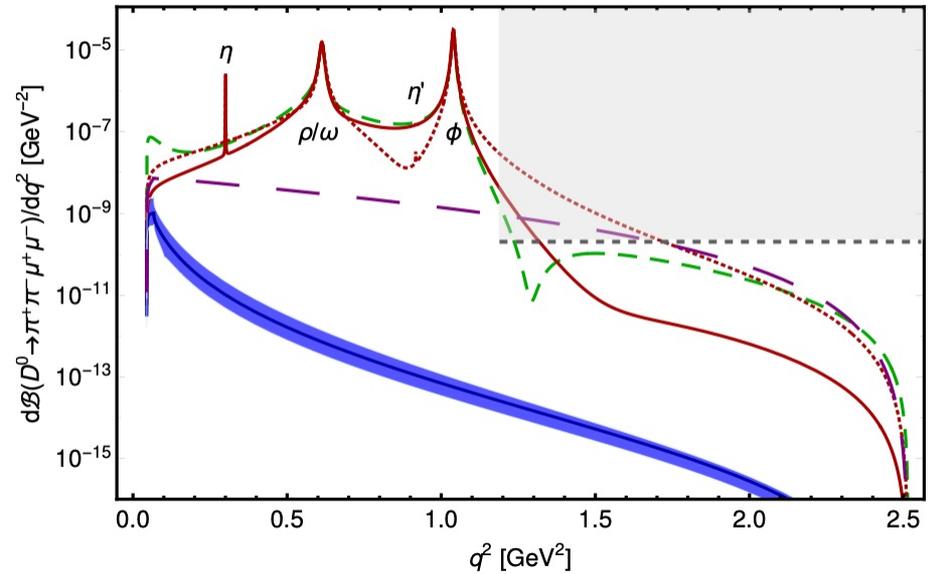
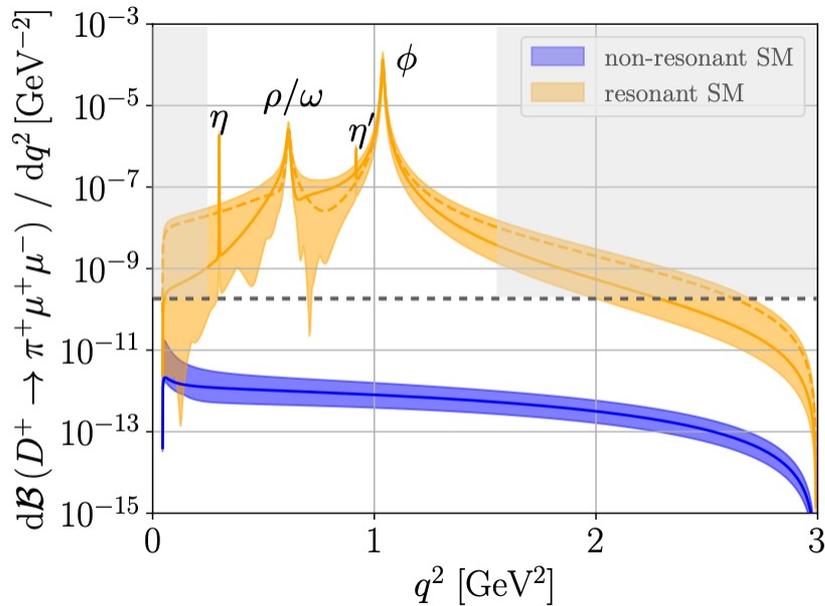
Gisbert et al. 2011.09478,

LD dynamics: Resonance contributions

$$\mathcal{C}_9^R = a_{\rho^0} e^{i\delta_{\rho^0}} \left( \frac{1}{q^2 - m_{\rho^0}^2 + i m_{\rho^0} \Gamma_{\rho^0}} - \frac{1}{3} \frac{1}{q^2 - m_{\omega}^2 + i m_{\omega} \Gamma_{\omega}} \right) + \frac{a_{\phi} e^{i\delta_{\phi}}}{q^2 - m_{\phi}^2 + i m_{\phi} \Gamma_{\phi}}$$

$$\mathcal{C}_P^R = \frac{a_{\eta} e^{i\delta_{\eta}}}{q^2 - m_{\eta}^2 + i m_{\eta} \Gamma_{\eta}} + \frac{a_{\eta'}}{q^2 - m_{\eta'}^2 + i m_{\eta'} \Gamma_{\eta'}}$$

$$D \rightarrow \pi l^+ l^-$$



SM prediction: Long distance contributions most important!

peaks at  $\rho, \omega, \phi$  and  $\eta$  resonances

Gisbert et al., 2011.09478  
 de Boer, Hiller, 1510.00311,  
 SF and Kosnik, 1510.00965  
 Bause et al, 1909.11108

Lattice for form factors  
 HFLAV, 1909.12524

SM in  $D \rightarrow \ell^+ \ell^-$

Belle & LHCb Experiment:

$$\mathcal{B}(D^0 \rightarrow e^+ e^-) < 7.9 \times 10^{-8}$$

$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) < 6.2 \times 10^{-9}$$

$$\mathcal{B}(D^0 \rightarrow \mu^\pm e^\mp) < 1.3 \times 10^{-8}$$

Helicity suppression

$$\begin{aligned} \mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) = & \frac{G_F^2 \alpha_e^2 m_D^5 f_D^2}{64 \pi^3 m_c^2 \Gamma_D} \sqrt{1 - \frac{4 m_\mu^2}{m_D^2}} \left[ \left(1 - \frac{4 m_\mu^2}{m_D^2}\right) \left| \mathcal{C}_S^{(\mu)} - \mathcal{C}_S^{(\mu)'} \right|^2 \right. \\ & \left. + \left| \mathcal{C}_P^{(\mu)} - \mathcal{C}_P^{(\mu)'} + \frac{2 m_\mu m_c}{m_D^2} \left( \mathcal{C}_{10}^{(\mu)} - \mathcal{C}_{10}^{(\mu)'} \right) \right|^2 \right], \end{aligned}$$

$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-)_{\text{LD}} \approx 8 \alpha^2 \cdot \left( \frac{m_\mu^2}{m_D^2} \right) \cdot \log^2 \left( \frac{m_\mu^2}{m_D^2} \right) \cdot \mathcal{B}(D^0 \rightarrow \gamma \gamma) \sim 10^{-11}$$

Gisbert et al. 2011.09478,

# NP in rare charm decays – from B to D

Search for NP in up sector

}

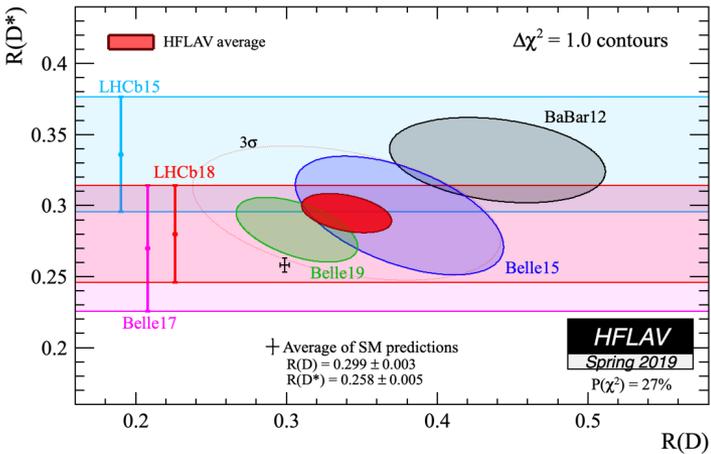
at low energies (charm factories)  
at high energies LHC

B anomalies explained by NP

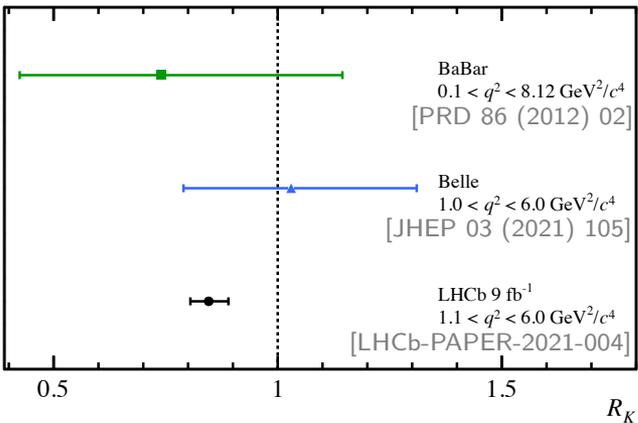
Can this NP be seen in charm rare decays,  $D^0 - \bar{D}^0$  oscillations ...

Unfortunately GIM mechanism is in the action for FCNC in charm physics !

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})} \Big|_{\ell \in (e, \mu)}$$



$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu \mu)}{\mathcal{B}(B \rightarrow K^{(*)} ee)} \Big|_{q^2 \in [q_{\min}^2, q_{\max}^2]}$$



NP explaining both B anomalies

$$R_{D^{(*)}}^{exp} > R_{D^{(*)}}^{SM}$$

$$\mathcal{L}_{NP} = \frac{1}{(\Lambda^D)^2} 2 \bar{c}_L \gamma_\mu b_L \bar{\tau} \gamma^\mu \nu_L$$

$$\Lambda^D \simeq 3 \text{ TeV}$$

$$R_{K^{(*)}}^{exp} < R_{K^{(*)}}^{SM}$$

$$\mathcal{L}_{NP} = \frac{1}{(\Lambda^K)^2} \bar{s}_L \gamma_\mu b_L \bar{\mu}_L \gamma^\mu \mu_L$$

$$\Lambda^K \simeq 30 \text{ TeV}$$

$$\Lambda^D \simeq \Lambda^K \equiv \Lambda$$

NP in FCNC  $B \rightarrow K^{(*)} \mu^+ \mu^-$   
has to be suppressed

$$\frac{1}{(\Lambda^K)^2} = \frac{C_K}{\Lambda^2} \quad C_K \simeq 0.01$$

suppression factor

## Charged current charm meson decays and New Physics

$$\mathcal{L}_{SM} = \frac{4G_F}{\sqrt{2}} V_{cs} \bar{s}_L \gamma^\mu c_L \bar{\nu}_l \gamma_\mu l$$

PDG 2020

$$f_{D^+} = 212.6(7) \text{ MeV}$$

$$f_{D_s} = 249.9(5) \text{ MeV}$$

$$\frac{f_{D_s}}{f_{D^+}} = 1.175(2)$$

$$|V_{cs}| = 0.983(13)(14)(2)$$

Electro-magnetic correction 1-3%

$$\mathcal{L}_{NP} = \frac{2}{\Lambda_c^2} \bar{s}_L \gamma^\mu c_L \bar{\nu}_l \gamma_\mu l$$

1 % error in

$$\Gamma(D_s^+ \rightarrow l^+ \nu_l)$$

$$\Lambda_c \sim 2.5 \text{ TeV}$$

Message:

Even if there is NP at 3 TeV scale  
the effect on charm leptonic decay  
can be  $\sim 1\%$ !

# New Physics in charm processes



NP in charm

Constraints from K, B physics

Constraints from EW physics,  
oblique corrections,  $Z \rightarrow b\bar{b}$

Constraints from LHC

Up-quark in weak doublet “talks” to down quarks via CKM!

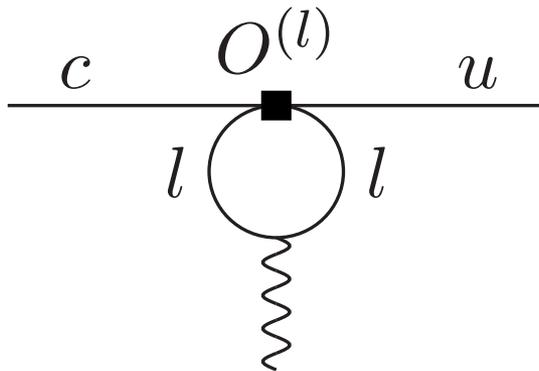
Effects of NP in charm suppressed by  $V_{cb}^* V_{ub}$ !

$$Q_{iL} = \begin{bmatrix} V_{il}^* u_j \\ d_i \end{bmatrix}_L$$

# New Physics in FCNC charm decays

Leptoquarks in  $c \rightarrow uy$

Hiller& de Boer 1701. 06392  
SF and Košnik, 1510.00965



Constraints from

$$\tau^- \rightarrow \pi^- \nu_\tau$$

$$\tau^- \rightarrow K^- \nu_\tau$$

$$\Delta m_D$$

$$D^+ \rightarrow \tau^+ \nu_\tau$$

$$D_s^+ \rightarrow \tau^+ \nu_\tau$$

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

Even for  $\tau$  in the loop too small contribution  
( $m_\tau/m_{LQ}$ )<sup>2</sup> suppression!

Within LQ models the  $c \rightarrow uy$  branching ratios are SM-like with CP asymmetries at (0.01) for  $S_{1,2}$  and  $V_{-2}$  and SM-like for  $S_3$ .

Vector LQ  $V_1$   $A_{CP} \sim O(10\%)$ . The largest effects arise from  $\tau$ -loops.

$S_3$  can explain  
 $R_{K^{(*)}}$  !

# Angular distributions in $D \rightarrow P_1 P_2 l^+ l^-$

LHCb, 1707.08377

$$\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-)|_{[0.565-0.950] \text{ GeV}} = (40.6 \pm 5.7) \times 10^{-8}$$

$$\mathcal{B}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-)|_{[0.950-1.100] \text{ GeV}} = (45.4 \pm 5.9) \times 10^{-8}$$

$$\mathcal{B}(D^0 \rightarrow K^+ K^- \mu^+ \mu^-)|_{[>0.565] \text{ GeV}} = (12.0 \pm 2.7) \times 10^{-8}$$

De Beor and Hiller, 1805.08516

- study of angular distributions  $\rightarrow$  SM – null tests
- simpler than in B decays due to dominance of long distance physics (resonances)
- NP induced integrated CP asymmetries can reach few percent
- sensitive on  $C_{10}^{(\prime)}$

$$A_{\text{FB}}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-) = (3.3 \pm 3.7 \pm 0.6)\%$$

$$A_{2\phi}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-) = (-0.6 \pm 3.7 \pm 0.6)\%$$

$$A_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-) = (4.9 \pm 3.8 \pm 0.7)\%$$

$$A_{\text{FB}}(D^0 \rightarrow K^+ K^- \mu^+ \mu^-) = (0 \pm 11 \pm 2)\%$$

$$A_{2\phi}(D^0 \rightarrow K^+ K^- \mu^+ \mu^-) = (9 \pm 11 \pm 1)\%$$

$$A_{\text{CP}}(D^0 \rightarrow K^+ K^- \mu^+ \mu^-) = (0 \pm 11 \pm 2)\%$$

LHCb, 1806.10793  
consistent with SM

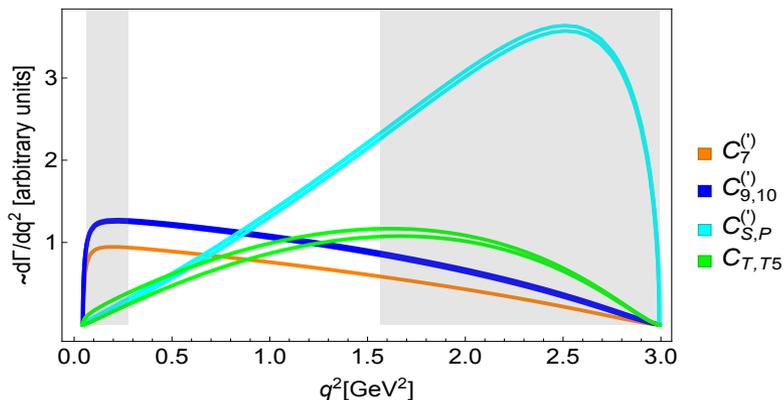
## Tests of LFU

$$R_{P_1 P_2}^D = \frac{\int_{q_{\min}^2}^{q_{\max}^2} d\mathcal{B}/dq^2(D \rightarrow P_1 P_2 \mu^+ \mu^-)}{\int_{q_{\min}^2}^{q_{\max}^2} d\mathcal{B}/dq^2(D \rightarrow P_1 P_2 e^+ e^-)}$$

$$R_{\pi\pi}^{D \text{ SM}} = 1.00 \pm \mathcal{O}(\%)$$

$$R_{KK}^{D \text{ SM}} = 1.00 \pm \mathcal{O}(\%)$$

NP bounds from  $D \rightarrow \pi l^+ l^-$  and  $D \rightarrow l^+ l^-$



Maximally allowed values of the Wilson coefficients in the low and high energy bins, according to LHCb 1304.6365 :

$$q^2 \in [0.0625, 0.276] \text{ GeV}^2$$

$ \tilde{C}_i  =  V_{ub}V_{cb}^* C_i $	$ \tilde{C}_i _{\text{max}}$		
	BR( $\pi\mu\mu$ ) <sub>I</sub>	BR( $\pi\mu\mu$ ) <sub>II</sub>	BR( $D^0 \rightarrow \mu\mu$ )
$\tilde{C}_7$	2.4	1.6	-
$\tilde{C}_9$	2.1	1.3	-
$\tilde{C}_{10}$	1.4	0.92	0.56
$\tilde{C}_S$	4.5	0.38	0.043
$\tilde{C}_P$	3.6	0.37	0.043
$\tilde{C}_T$	4.1	0.76	-
$\tilde{C}_{T5}$	4.4	0.74	-
$\tilde{C}_9 = \pm \tilde{C}_{10}$	1.3	0.81	0.56

0.043

region II

$$q^2 \in [1.56, 4.00] \text{ GeV}^2$$

Best bounds from

$$D^0 \rightarrow \mu^+ \mu^-$$

Model of NP	Effect on W.c.	Size of the effect
Scalar leptoquark (3,2,7/6)	$C_S, C_P, C_S', C_P', C_T, C_{T5},$ $C_9, C_{10}, C_9', C_{10}'$	$V_{cb}V_{ub}  C_9, C_{10}  < 0.34$
Vector leptoquark (3,1,5/3)	$C_9' = C_{10}'$	$V_{cb}V_{ub}  C_9', C_{10}'  < 0.24$
Two Higgs doublet Model type III	$C_S, C_P, C_S', C_P'$	$V_{cb}V_{ub}  C_S - C_S'  < 0.005$ $V_{cb}V_{ub}  C_P - C_P'  < 0.005$
Z' model	$C_9', C_{10}'$	$V_{cb}V_{ub}  C_9'  < 0.001$ $V_{cb}V_{ub}  C_{10}'  < 0.014$

# Lepton flavor violation

$$c \rightarrow u\mu^\pm e^\mp$$

1510.00311 (de Beor and Hiller)  
1705.02251 (Sahoo and Mohanta)

$$\mathcal{L}_{\text{eff}}^{\text{weak}}(\mu \sim m_c) = \frac{4G_F}{\sqrt{2}} \frac{\alpha_e}{4\pi} \sum_i \left( K_i^{(e)} O_i^{(e)} + K_i^{(\mu)} O_i^{(\mu)} \right)$$

$$O_9^{(e)} = (\bar{u}\gamma_\mu P_L c) (\bar{e}\gamma^\mu \mu)$$

$$O_9^{(\mu)} = (\bar{u}\gamma_\mu P_L c) (\bar{\mu}\gamma^\mu e)$$

LHCb bound, 1512.00322

$$BR(D^0 \rightarrow e^+ \mu^- + e^- \mu^+) < 2.6 \times 10^{-7}$$

$$BR(D^+ \rightarrow \pi^+ e^+ \mu^-) < 2.9 \times 10^{-6}$$

$$BR(D^+ \rightarrow \pi^+ e^- \mu^+) < 3.6 \times 10^{-6}$$

$$BR(D^0 \rightarrow e^\pm \tau^\mp) < 7 \times 10^{-15}$$

$$\left| K_{S,P}^{(l)} - K_{S,P}^{(l)'} \right| \lesssim 0.4,$$

$$\left| K_{9,10}^{(l)} - K_{9,10}^{(l)'} \right| \lesssim 6, \quad \left| K_{T,T5}^{(l)} \right| \lesssim 7,$$

$$l = e, \mu$$

$$\Lambda_c \rightarrow p\gamma$$

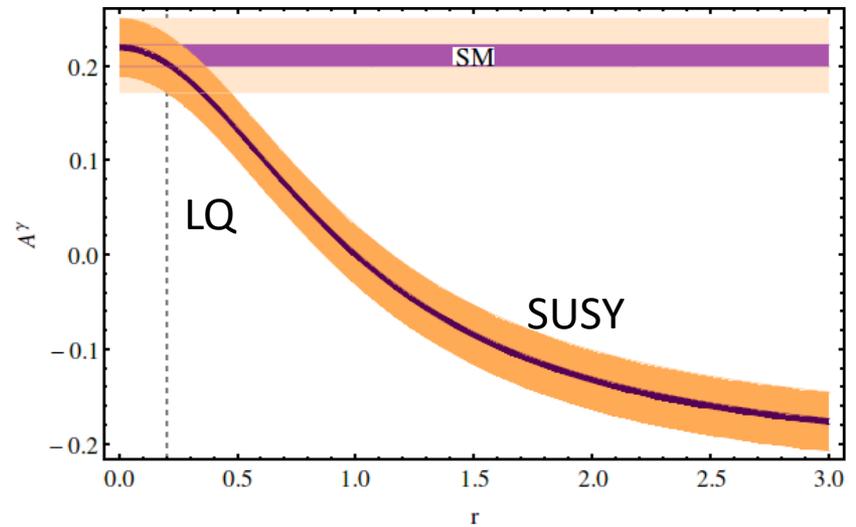
$$\mathcal{B}(\Lambda_c \rightarrow p\gamma) \sim \mathcal{O}(10^{-5})$$

Hiller& de Boer 1701. 06392

If  $\Lambda_c$ -baryons are produced polarized, such as at Z,  
angular asymmetries in  $\Lambda_c \rightarrow p\gamma$  can probe  
chirality-flipped contributions

$$A^\gamma = -\frac{P_{\Lambda_c}}{2} \frac{1 - |r|^2}{1 + |r|^2}$$

$$P_{\Lambda_c} = -0.44.$$



## Charm meson decays to invisible fermions

Bause et al. 2010.02225 predicted rather large branching ratios for D decays to  $\pi$  and invisibles, based on Belle result

$$BR(D^0 \rightarrow \text{invisibles}) < 9.4 \times 10^{-5}$$

$$\text{SM } \mathcal{B}(D^0 \rightarrow \nu\bar{\nu}) = 1.1 \times 10^{-31}$$

$$D^0 \rightarrow \nu\bar{\nu}\nu\bar{\nu} \quad \text{dominates over two-body decay}$$

Bhattacharaya et al., 1809.04606

Improvements are expected at BESIII and FCC-ee

But models in 2010.02225 do not consider a “realistic” models in which flavour observables define the parameter space.

# Dinuetrino charm meson decays

Bause et al., 2007.05001

Bause et al., 2010.02225

$$\mathcal{L}_{\text{eff}} \supset \frac{4 G_F}{\sqrt{2}} \frac{\alpha_e}{4\pi} \left( c_L^{Uij} Q_L^{ij} + c_R^{Uij} Q_R^{ij} \right) + \text{H.c.}$$

$$Q_{L(R)}^{ij} = (\bar{u}_{L(R)} \gamma_\mu c_{L(R)}) (\bar{\nu}_{jL} \gamma^\mu \nu_{iL})$$

$$\mathcal{B}(c \rightarrow u \nu \bar{\nu}) = \sum_{i,j} \mathcal{B}(c \rightarrow u \nu_j \bar{\nu}_i)$$

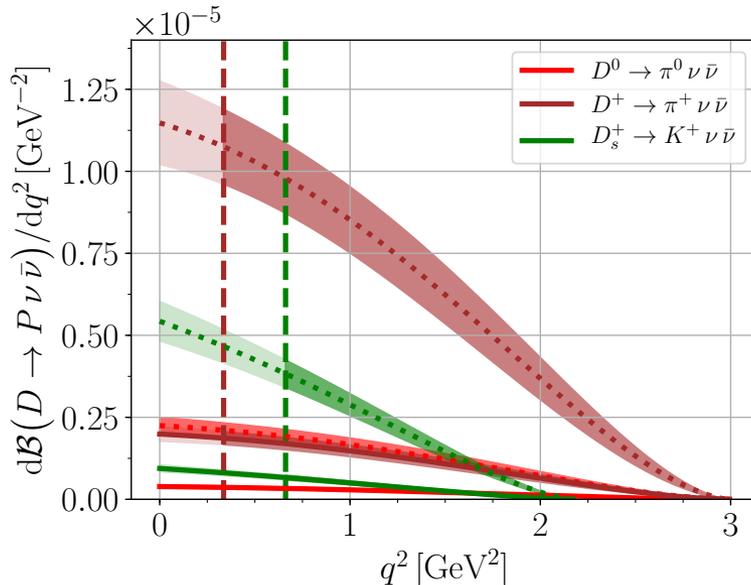
$$x_U^\pm = \sum_{i,j} |c_L^{Uij} \pm c_R^{Uij}|^2$$

From charged leptons  $D \rightarrow P l^+ l^-$

$$x_U \lesssim 34, \quad (\text{LU}) \quad \text{diag}(k,k,k)$$

$$x_U \lesssim 196, \quad (\text{cLFC}) \quad \text{diag}(k_1,k_2,k_2)$$

$$x_U \lesssim 716, \quad (\text{general}) \quad \text{matrix } 3 \times 3$$

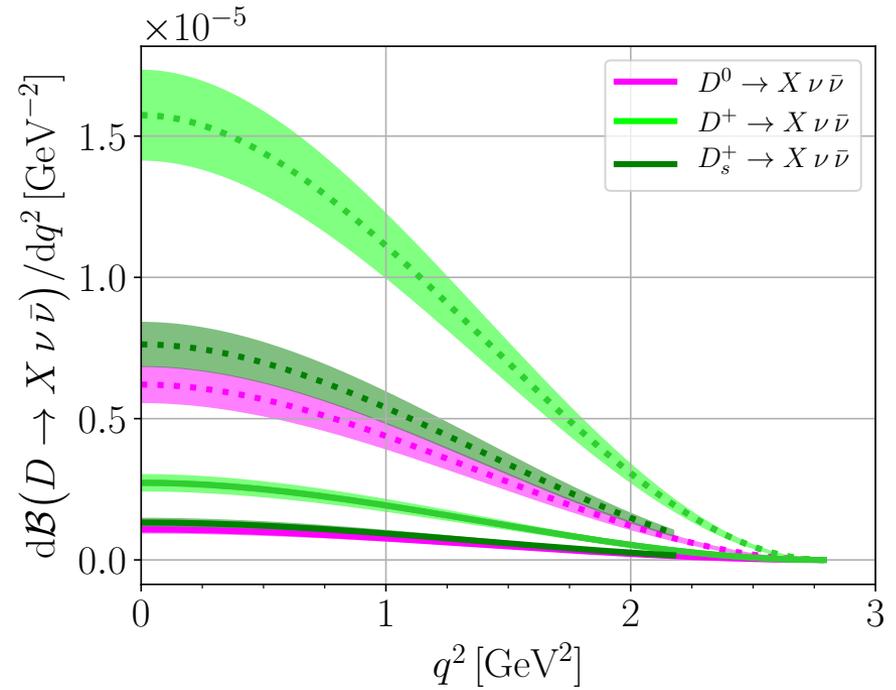
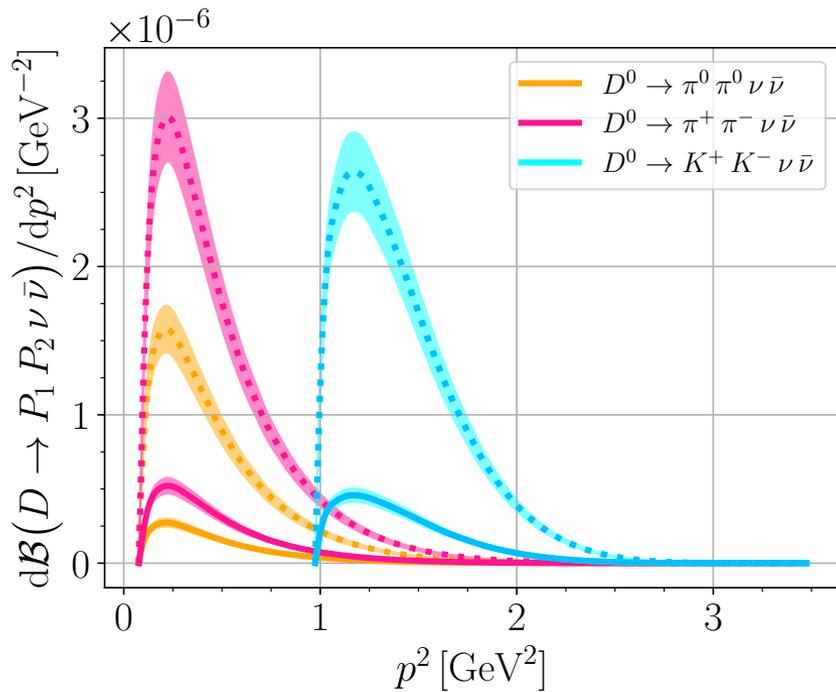


Bounds from LHC Drell-Yan study  $pp \rightarrow l_1 l_2$  (charged leptons)

Fuentes-Martin et al., 2003.12421,

Angelescu et al, 2002.05684;

In down sector rare decays are more constraining.



With massless  $\nu_R$   $\mathcal{B}(D^0 \rightarrow \text{inv.}) \lesssim 2 \cdot 10^{-6}$

These limits are data-driven and will go down if improved bounds from charged leptons become available!

# Invisible fermions and scalar leptoquarks

SF &A. Novosel, 2101.10712

Cloured Scalar	Invisible fermion
$S_1 = (\bar{3}, 1, 1/3)$	$\bar{d}_R^C{}^i \chi^j S_1$
$\bar{S}_1 = (\bar{3}, 1, -2/3)$	$\bar{u}_R^C{}^i \chi^j \bar{S}_1$
$\tilde{R}_2 = (\bar{3}, 2, 1/6)$	$\bar{u}_L^i \chi^j \tilde{R}_2^{2/3}$
$\tilde{R}_2 = (\bar{3}, 2, 1/6)$	$\bar{d}_L^i \chi^j \tilde{R}_2^{-1/3}$

coloured singlet  $\mathcal{L}(\bar{S}_1) \supset \bar{y}_{1ij}^{RR} \bar{u}_R^C{}^i \chi_R^j \bar{S}_1 + \text{h.c.}$

$$\mathcal{L}_{\text{eff}} = \sqrt{2} G_F c^{RR} (\bar{u}_R \gamma_\mu c_R) (\bar{\chi}_R \gamma^\mu \chi_R)$$

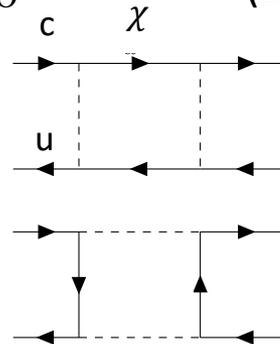
$$c^{RR} = \frac{v^2}{2M_{\bar{S}_1}^2} \bar{y}_{1c\chi}^{RR} \bar{y}_{1u\chi}^{RR*}$$

Constraints from charm mixing

$$\left| \bar{y}_{1c\chi}^{RR} \bar{y}_{1u\chi}^{RR*} \right| < 1.2 \times 10^{-5} M_{\bar{S}_1} / \text{GeV}$$

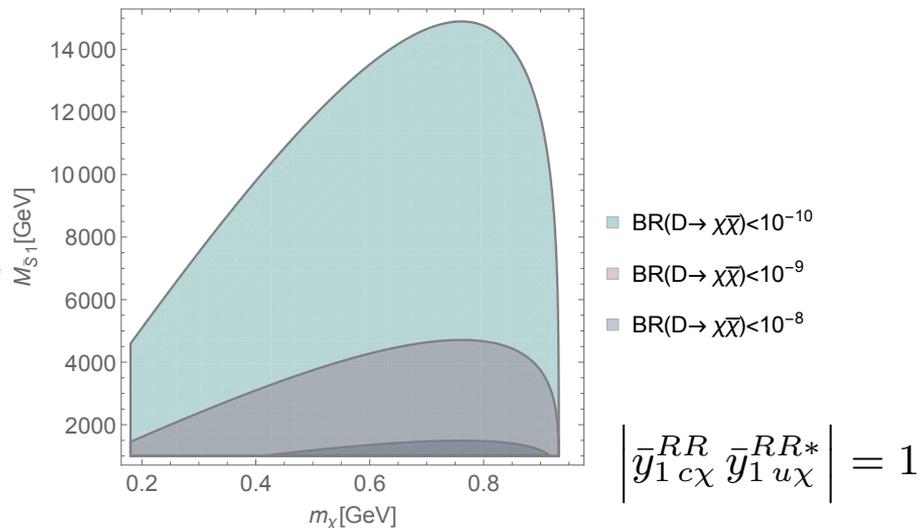
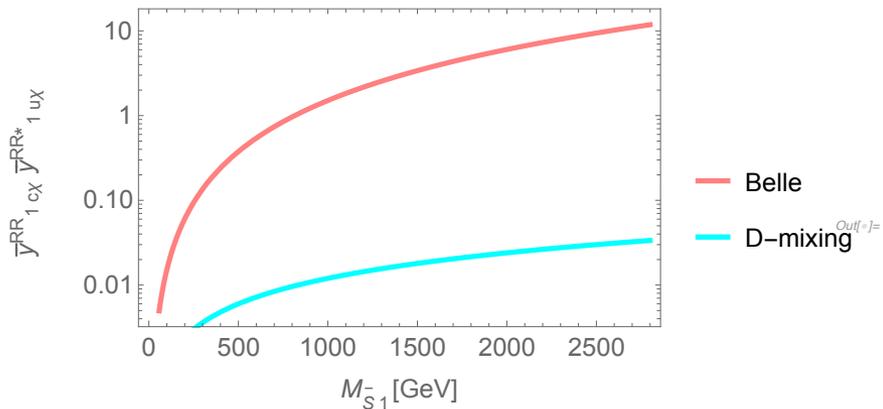
$BR(D^0 \rightarrow \text{invisibles}) < 9.4 \times 10^{-5}$  (Belle, 1611.09455)

$m_\chi$ (GeV)	$\mathcal{B}(D^0 \rightarrow \chi \bar{\chi})_{D-\bar{D}}$
0.18	$< 1.1 \times 10^{-9}$
0.50	$< 7.4 \times 10^{-9}$
0.80	$< 1.1 \times 10^{-8}$



Massive  $\chi = \nu_R$   
model allows to use  
charm mixing

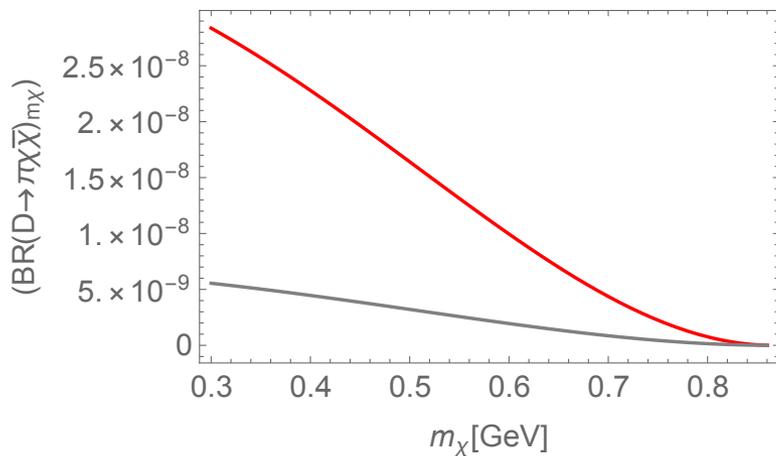
Main message: charm mixing leads to strong constraints



$$\left| \bar{y}_{1c\chi}^{RR} \bar{y}_{1u\chi}^{RR*} \right| = 1$$

$m_\chi$ (GeV)	$\mathcal{B}(D^0 \rightarrow \chi\bar{\chi}\gamma)_{D-\bar{D}}$	$\mathcal{B}(D^0 \rightarrow \chi\bar{\chi}\gamma)_{Belle}$
0.18	$< 2.1 \times 10^{-11}$	$< 1.3 \times 10^{-7}$
0.50	$< 6.9 \times 10^{-12}$	$< 6.3 \times 10^{-9}$
0.80	$< 8.4 \times 10^{-14}$	$< 2.2 \times 10^{-10}$

$m_\chi$ (GeV)	$\mathcal{B}(D^0 \rightarrow \pi^0 \chi\bar{\chi})_{D-\bar{D}}$	$\mathcal{B}(D^+ \rightarrow \pi^+ \chi\bar{\chi})_{D-\bar{D}}$
0.18	$< 5.9 \times 10^{-9}$	$< 3.0 \times 10^{-8}$
0.50	$< 3.2 \times 10^{-9}$	$< 1.6 \times 10^{-8}$
0.80	$< 1.5 \times 10^{-10}$	$< 7.6 \times 10^{-10}$

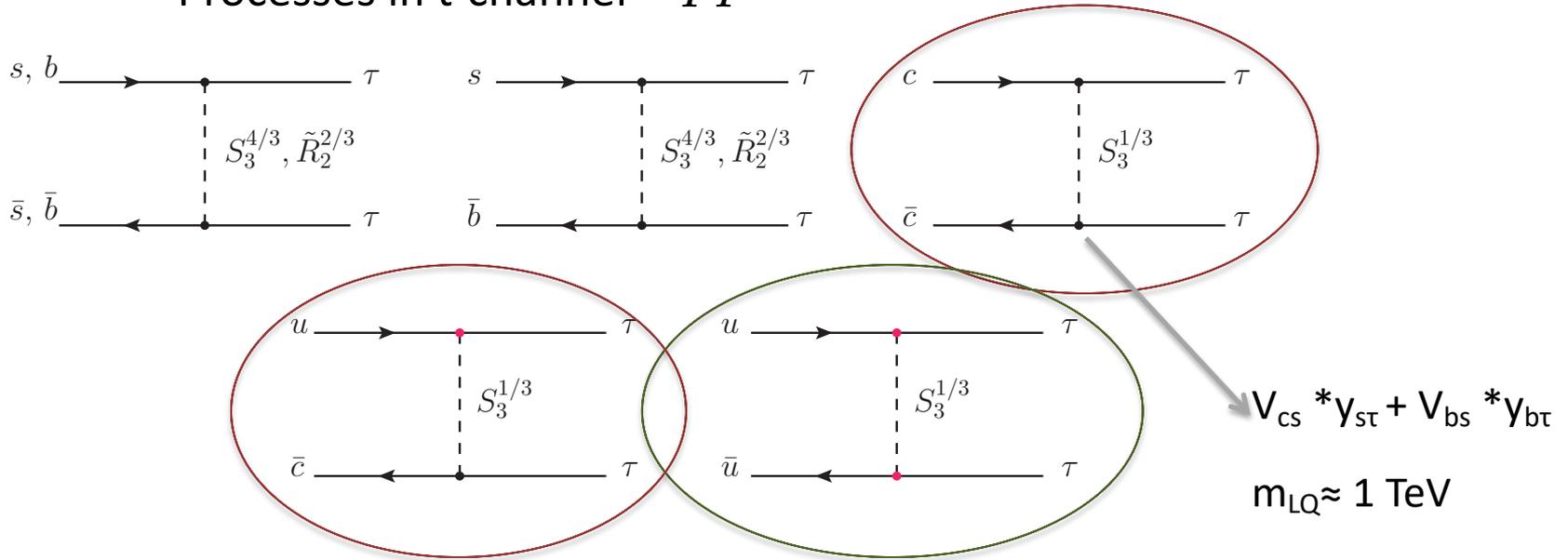


—  $\text{BR}(D^+ \rightarrow \pi^+ \chi\bar{\chi})$   
 —  $\text{BR}(D^0 \rightarrow \pi^0 \chi\bar{\chi})$

Mass of scalar leptoquark is within LHC reach!

# LHC constraints on charm coupling to LQs: high-mass $\tau\tau$ production

Processes in t-channel  $pp \rightarrow \tau^+ \tau^-$



Flavour anomalies generate  $s\tau$ ,  $b\tau$  and  $c\tau$  relatively large couplings.

$s$  quark pdf function for protons are  $\sim 3$  times larger contribution than for  $b$  quark.

1706.07779, Doršner, SF, Faroughy, Košnik

## Summary & Outlook

- SM effective weak Lagrangian very precisely known – SD dynamics, (LD dynamics difficult to explain, without huge involvement of Lattice QCD).
- New physics explaining B anomalies, leads to rather small effects in charge current transitions;
- FCNC transition in charm rare decays suffer from strong GIM suppression, makes search for NP demanding;
- LHC offers tests of FCNC at high energies;
- Few proposals to test DM in charm physics scalar LQ mass in TeV region;
- Charm physics complement any search for NP at low and high energies!

# 瓦拉



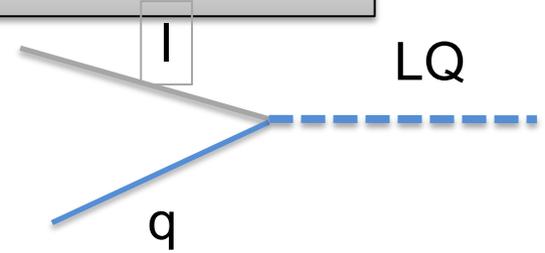
HVALA

Popular scenario: Leptoquarks as a resolution of B anomalies:

$$LQ = (SU(3)_c, SU(2)_L)_Y$$

$$\text{or } LQ = (SU(3)_c, SU(2)_L, Y)$$

$$Q = I_3 + Y$$



no proton decay  
at tree level

Model	$R_{D^{(*)}}$	$R_{K^{(*)}}$	$R_{D^{(*)}}$ & $R_{K^{(*)}}$
$S_1 = (\bar{3}, 1)_{1/3}$	✓	✗	✗
$R_2 = (3, 2)_{7/6}$	✓	✗*	✗
$S_3 = (\bar{3}, 3)_{1/3}$	✗	✓	✗
$U_1 = (3, 1)_{2/3}$	✓	✓	✓
$V_2 = (3, 1)_{2/3}$	✗	✗	✗
$\widetilde{V}_2 = (\bar{3}, 2)_{-1/6}$	✗	✗	✗
$U_3 = (3, 3)_{2/3}$	✗	✓	✗

Spin 0

Spin 1

No single scalar LQ to solve simultaneously both anomalies! Doršner, SF, Greljo,  
 Scalar LQ  $\longrightarrow$  simpler UV completion; Kamenik, Košnik, 1603.04993

Only  $R_2$  and  $S_1$  might explain  $(g-2)_\mu$  (both chiralities are required with the enhancement factor  $m_t/m_\mu$ ) Muller 1801.0338, Doršner, SF & Sumensari, 1910.03877.

# Charm Physics Confronts High- $p_T$ Lepton Tails

Fuentes-Martin et al., 2003.12421

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

$$\mathcal{L}_{\text{SMEFT}} \supset \frac{1}{v^2} \sum_k \mathcal{C}_k \mathcal{O}_k$$

$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L) (\bar{q}_L \gamma^\mu \tau^I q_L),$$

$$\mathcal{O}_{lequ}^{(1)} = (\bar{l}_L^p e_R) \epsilon_{pr} (\bar{q}_L^r u_R),$$

$$\mathcal{O}_{\phi q}^{(3)} = (\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\bar{q}_L \gamma^\mu \tau^I q_L),$$

$$\mathcal{O}_{ledq} = (\bar{l}_L e_R) (\bar{d}_R q_L),$$

$$\mathcal{O}_{lequ}^{(3)} = (\bar{l}_L^p \sigma_{\mu\nu} e_R) \epsilon_{pr} (\bar{q}_L^r \sigma^{\mu\nu} u_R)$$

$$\mathcal{O}_{\phi ud} = (\tilde{\phi}^\dagger i D_\mu \phi) (\bar{u}_R \gamma^\mu d_R).$$

$$\mathcal{L}_{\text{CC}} = -\frac{4G_F}{\sqrt{2}} V_{ci} \left[ (1 + \epsilon_{V_L}^{\alpha\beta i}) \mathcal{O}_{V_L}^{\alpha\beta i} + \epsilon_{V_R}^{\alpha\beta i} \mathcal{O}_{V_R}^{\alpha\beta i} + \epsilon_{S_L}^{\alpha\beta i} \mathcal{O}_{S_L}^{\alpha\beta i} + \epsilon_{S_R}^{\alpha\beta i} \mathcal{O}_{S_R}^{\alpha\beta i} + \epsilon_T^{\alpha\beta i} \mathcal{O}_T^{\alpha\beta i} \right] + \text{h.c.},$$

## Tree level matching

$$\epsilon_{V_L}^{\alpha\beta i} = -\frac{V_{ji}}{V_{ci}} [\mathcal{C}_{lq}^{(3)}]_{\alpha\beta 2j} + \delta_{\alpha\beta} \frac{V_{ji}}{V_{ci}} [\mathcal{C}_{\phi q}^{(3)}]_{2j},$$

$$\epsilon_{S_L}^{\alpha\beta i} = -\frac{V_{ji}}{2V_{ci}} [\mathcal{C}_{lequ}^{(1)}]_{\beta\alpha j 2}^*,$$

$$\epsilon_T^{\alpha\beta i} = -\frac{V_{ji}}{2V_{ci}} [\mathcal{C}_{lequ}^{(3)}]_{\beta\alpha j 2}^*,$$

$$\epsilon_{V_R}^{\alpha\beta i} = \frac{1}{2V_{ci}} \delta_{\alpha\beta} [\mathcal{C}_{\phi ud}]_{2i},$$

$$\epsilon_{S_R}^{\alpha\beta i} = -\frac{1}{2V_{ci}} [\mathcal{C}_{ledq}]_{\beta\alpha i 2}^*,$$

## Definitions

$$\frac{m_D}{\lambda_D} = \int_0^1 d\xi \frac{\Phi_D(\xi)}{\xi} \quad \text{Light cone distribution =function}$$

$$\lambda_B^{\text{HQET}} > 0.172 \text{ GeV at } 90\% \text{ C.L.}$$

$$C_7^{\text{WA},\rho^0} = -\frac{2\pi^2 Q_u f_D f_{\rho^0}^{(d)} m_\rho}{T m_{D^0} m_c \lambda_D} V_{cd}^* V_{ud} \left( \frac{4}{9} C_1^{(0)} + \frac{1}{3} C_2^{(0)} \right),$$

$$C_7^{\text{WA},\omega} = \frac{2\pi^2 Q_u f_D f_\omega^{(d)} m_\omega}{T m_{D^0} m_c \lambda_D} V_{cd}^* V_{ud} \left( \frac{4}{9} C_1^{(0)} + \frac{1}{3} C_2^{(0)} \right),$$

$$C_7^{\text{WA},\rho^+} = \frac{2\pi^2 Q_d f_D f_\rho m_\rho}{T m_{D^+} m_c \lambda_D} V_{cd}^* V_{ud} C_2^{(0)},$$

$$C_7^{\text{WA},K^{*+}} = \frac{2\pi^2 Q_d f_{D_s} f_{K^*} m_{K^*}}{T m_{D_s} m_c \lambda_D} V_{cs}^* V_{us} C_2^{(0)},$$

## Scalar LQ in charm FCNC processes

(3,3,-1/3)

$$\mathcal{L}_{\bar{c}u\bar{\ell}\ell} = -\frac{4G_F}{\sqrt{2}} \left[ c_{cu}^{LL} (\bar{c}_L \gamma^\mu u_L) (\bar{\ell}_L \gamma_\mu \ell_L) \right] + \text{h.c.},$$

$$C_{cu}^{LL} = -\frac{v^2}{2m_{S_3}^2} (V_{cs}^* g_{s\mu} + V_{cb}^* b_{b\mu}) (V_{us} g_{s\mu} + V_{ub} b_{b\mu})$$

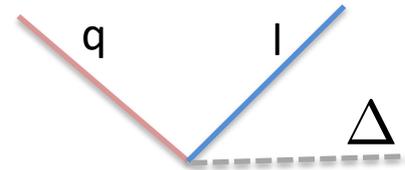
$C_{cu}^{LL}$  100 times smaller than current LHCb bound!

(3,1,-1/3)

(3,1,-1/3) introduced by Bauer and Neubert in 1511.01900 to explain both B anomalies. In 1608.07583, Becirevic et al., showed that model cannot survive flavor constraints:

$$K \rightarrow \mu\nu, B \rightarrow \tau\nu, \tau \rightarrow \mu\gamma$$

$$D_s \rightarrow \tau\nu, D \rightarrow \mu^+ \mu^-$$



## Scalar LQ (3,2,7/6)

In the case of  $\Delta C=2$  in  $D^0 - \bar{D}^0$  oscillation there is also a LQ contribution

Bound from  $\Delta C=2$  slightly stronger, but comparable to the bound coming from

$$D^0 \rightarrow \mu^+ \mu^-$$

$$\mathcal{H} = C_6 (\bar{u}_R \gamma^\mu c_R) (\bar{u}_R \gamma_\mu c_R)$$

$R_2$  (3,2,7/6) can explain  $R_{D^{(*)}}$  (Becirevic, Dorsner, SF, Faroughy, Kosnik, Sumensari, 1806.05689 and can generate c quark EDM)

## Vector LQ(3,1,5/3)

$$\mathcal{L} = Y_{ij} (\bar{\ell}_i \gamma_\mu P_R u_j) V^{(5/3)\mu} + \text{h.c.} .$$

not present in B physics at tree level!

$$D^0 - \bar{D}^0$$

(for loop effects in B Camargo-Molina, Celis, Faroughy 1805.04917 )