# Rare and forbidden decays of heavy flavor mesons at the B-factories and LHC 

Abi Soffer<br>Tel Aviv University

For the ATLAS, BABAR, Belle, CMS, LHCb

Collaborations

## Recent results covered in this talk

- LNV:
$-D^{0} \rightarrow h^{\mp} h^{\prime \mp} \ell^{ \pm} \ell^{\prime \pm} \quad$ BABAR
- LFV:
$-D^{0} \rightarrow h^{+} h^{\prime-} \ell^{+} \ell^{\prime^{-}} \quad$ BABAR
$-D^{0} \rightarrow X^{0} e^{ \pm} \mu^{\mp} \quad$ BABAR
$-B^{+} \rightarrow K^{+} \mu^{-} \tau^{+} \quad$ LHCb
PRD 101 (2020) 112003
JHEP 2020 (2020) 129
- FCNC:
$-B_{(s)} \rightarrow \mu^{+} \mu^{-} \quad$ ATLAS, CMS, LHCb
LHCb-CONF-2020-002
CMS PAS BPH-20-003
ATLAS-CONF-2020-049
$-B^{0} \rightarrow$ invisible $(+\gamma) \quad$ Belle


## Lepton-number-violating decays

- Can be mediated by a Majorana neutrino that mixes with SM neutrino [1]:

$$
\mathcal{L}=-\frac{\mathrm{g}}{\sqrt{2}} W_{\mu}^{+} \sum_{\mathrm{l}=\mathrm{e}}^{\tau} V_{\mathrm{lN}}^{*} \overline{N^{\mathrm{c}}} \gamma^{\mu} P_{\mathrm{L}} \mathrm{l}+\text { h.c. }_{\text {Mixing-matrix element }}
$$



- $\quad 2^{\text {nd }}$-order, yet somewhat enhanced if $N$ is on-shell, $m_{N}<m_{\text {hadron }}$
- $N$ can't be a SM neutrino (even if Majorana), since $m_{v}$ too small


## Lepton-flavor-violating decays

- In principle, possible due to neutrino flavor oscillations

See talk by Avelino Vicente


- But suppressed by slow neutrino oscillations \& $2^{\text {nd }}$-order interaction
- Predicted LFV branching fractions $\ll 10^{-50}$
- $\rightarrow$ Any LFV observation requires BSM mediator that's highly LFV


## The BABAR experiment





BABAR data

| Resonance | $\mathrm{L}\left(\mathrm{fb}^{-1}\right)$ | $\#\left(10^{6}\right)$ |
| :---: | :---: | :---: |
| $\Upsilon(4 S)$ | 424 | 471 |
| $\Upsilon(3 S)$ | 28 | 121 |
| $\Upsilon(2 S)$ | 14 | 99 |
| Off-resonance | 48 |  |

$40 \mathrm{fb}^{-1}$ off-resonance in shown analysis

## The BABAR Detector



## $D^{0} \rightarrow h h^{\prime} \ell \ell^{\prime}$ event selection

- Reconstruct $D^{*+} \rightarrow D^{0} \pi^{+}$to reduce combinatorial background
- Select $D^{0} \rightarrow$
- LFV:

$$
\pi^{-} \pi^{+} e^{ \pm} \mu^{\mp}, \quad K^{-} \pi^{+} e^{ \pm} \mu^{\mp}, \quad K^{-} K^{+} e^{ \pm} \mu^{\mp}
$$

- LNV:

$$
\begin{array}{ccc}
\pi^{-} \pi^{-} e^{+} e^{+}, & \pi^{-} \pi^{-} \mu^{+} \mu^{+}, & \pi^{-} \pi^{-} e^{+} \mu^{+} \\
K^{-} \pi^{-} e^{+} e^{+}, & K^{-} \pi^{-} \mu^{+} \mu^{+}, & K^{-} \pi^{-} e^{+} \mu^{+} \\
K^{-} K^{-} e^{+} e^{+}, & K^{-} K^{-} \mu^{+} \mu^{+}, & K^{-} K e^{+} \mu^{+}
\end{array}
$$

- Hadronic-decays background (e.g., Cabibbo-favored $D^{0} \rightarrow K^{-} \pi^{+} \pi^{-} \pi^{+}$) suppressed by requiring $m(K 3 \pi)$ to be inconsistent with $M_{D^{0}}$
- Backgrounds from leptons arising from semileptonic decays or charm decays with missing neutrals is suppressed with Fisher discriminant of 9 kinematic variables.


## $D^{0} \rightarrow h h^{\prime} \ell \ell^{\prime}$ yields

- Determined for each mode from fit to $\Delta m \equiv m\left(D^{*+}\right)-m\left(D^{0}\right)$
- Signal PDF $=e^{-\left(m-m_{0}\right)^{2} /\left[2 \sigma_{L, R}^{2}+\alpha_{L, R}\left(m-m_{0}\right)^{2}\right]}$ (Cruijff function)
- Bgd PDF $=m \cdot\left[1-\left(\frac{m}{m_{0}}\right)^{2}\right]^{p} \cdot \exp \left[c \cdot\left(1-\left(\frac{m}{m_{0}}\right)^{2}\right)\right]$ (ARGUS function)
- No significant signal seen
- Signal Br and upper limits determined wrt. normalization mode $\mathrm{D}^{0} \rightarrow h h^{\prime} \pi \pi$ :

| Decay mode | $N_{\text {norm }}$ <br> (candidates) | Systematic <br> $(\%)$ |
| :--- | ---: | :---: |
| $D^{0} \rightarrow K^{-} \pi^{+} \pi^{+} \pi^{-}$ | $260870 \pm 520$ | 4.7 |
| $D^{0} \rightarrow K^{-} K^{+} \pi^{+} \pi^{-}$ | $8480 \pm 110$ | 6.6 |
| $D^{0} \rightarrow \pi^{-} \pi^{+} \pi^{+} \pi^{-}$ | $28470 \pm 220$ | 6.8 |



## $D^{0} \rightarrow h h^{\prime} \ell \ell^{\prime}$ results

E791, PRL 86 (2001) 3969

| Decay mode $D^{0} \rightarrow$ | $\begin{gathered} N_{\text {sig }} \\ \text { (candidates) } \\ \hline \end{gathered}$ | $\begin{aligned} & \epsilon_{\mathrm{sig}} \\ & (\%) \end{aligned}$ | $\begin{gathered} \mathcal{B} \\ \left(\times 10^{-7}\right) \\ \hline \end{gathered}$ | $\begin{aligned} & \mathcal{B} 90 \% \text { U.L. } \\ & \left(\times 10^{-7}\right) \\ & \hline \end{aligned}$ | Previous best $\left(\times 10^{-7}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\overline{\pi^{-}} \pi^{-} e^{+} e^{+}$ | $0.22 \pm 3.15 \pm 0.54$ | 4.38 | $0.27 \pm 3.90 \pm 0.67$ | 9.1 | 1120 |
| $\pi^{-} \pi^{-} \mu^{+} \mu^{+}$ | $6.69 \pm 4.88 \pm 0.80$ | 4.91 | $7.40 \pm 5.40 \pm 0.91$ | 15.2 | 290 |
| $\pi^{-} \pi^{-} e^{+} \mu^{+}$ | $12.42 \pm 5.30 \pm 1.45$ | 4.38 | $15.4 \pm 6.59 \pm 1.85$ | 30.6 | 790 |
| $\pi^{-} \pi^{+} e^{ \pm} \mu^{\mp}$ | $1.37 \pm 6.15 \pm 1.28$ | 4.79 | $1.55 \pm 6.97 \pm 1.45$ | 17.1 | 150 |
| $K^{-} \pi^{-} e^{+} e^{+}$ | $-0.23 \pm 0.97 \pm 1.28$ | 3.19 | $-0.38 \pm 1.60 \pm 2.11$ | 5.0 | 2060 |
| $K^{-} \pi^{-} \mu^{+} \mu^{+}$ | $-0.03 \pm 2.10 \pm 0.40$ | 3.30 | $-0.05 \pm 3.34 \pm 0.64$ | 5.3 | 3900 |
| $K^{-} \pi^{-} e^{+} \mu^{+}$ | $3.87 \pm 3.96 \pm 2.36$ | 3.48 | $5.84 \pm 5.97 \pm 3.56$ | 21.0 | 2180 |
| $K^{-} \pi^{+} e^{ \pm} \mu^{\mp}$ | $2.52 \pm 4.60 \pm 1.35$ | 3.65 | $3.62 \pm 6.61 \pm 1.95$ | 19.0 | 5530 |
| $K^{-} K^{-} e^{+} e^{+}$ | $0.30 \pm 1.08 \pm 0.41$ | 3.25 | $0.43 \pm 1.54 \pm 0.58$ | 3.4 | 1520 |
| $K^{-} K^{-} \mu^{+} \mu^{+}$ | $-1.09 \pm 1.29 \pm 0.42$ | 6.21 | $-0.81 \pm 0.96 \pm 0.32$ | 1.0 | 950 |
| $K^{-} K^{-} e^{+} \mu^{+}$ | $1.93 \pm 1.92 \pm 0.83$ | 4.63 | $1.93 \pm 1.93 \pm 0.84$ | 5.8 | 570 |
| $K^{-} K^{+} e^{ \pm} \mu^{\mp}$ | $4.09 \pm 3.00 \pm 1.59$ | 4.83 | $3.93 \pm 2.89 \pm 1.45$ | 10.0 | 1800 |

## Implications for $V_{\ell N}$

- The authors of ref. [1] provide an expected limit plot for $\left|V_{N \ell}\right|^{2}$
- They comment that this is based on a MC study in an unpublished thesis, using $2.9 \mathrm{fb}^{-1}$ collected at the $\psi(3770)$, leading to an expected Br limit $\operatorname{Br}\left(D^{0} \rightarrow K^{-} \pi^{-} e^{+} e^{+}\right)<\sim 10^{-9}$, too low given the cross section of 3.7 nb .
- Later, BESIII obtained a weaker limit [2], $\operatorname{Br}\left(D^{0} \rightarrow K^{-} \pi^{-} e^{+} e^{+}\right)<2.8 \times 10^{-6}$ (cf. BABAR: $5.0 \times 10^{-7}$ )
- So this plot seems $O(300)$ too tight


Fig. 3. Upper limits on $\left|V_{\mathrm{eN}}\right|^{2}$ at $90 \%$ confidence level as a function of the Majorana neutrino mass from the $\mathrm{D}^{0} \rightarrow \mathrm{~K}^{-} \mathrm{e}^{+} \mathrm{e}^{+} \pi^{-}$estimated from the MC study at BESIII.

## Implications for $V_{\ell N}$



## $D^{0} \rightarrow X^{0} \ell \ell^{\prime}$ results




|  | $N_{\text {sig }}$ <br> (candidates) | $\epsilon_{\text {sig }}$ <br> $(\%)$ | $\mathcal{B}\left(\times 10^{-7}\right)$ | $\mathcal{B} 90 \%$ U.L. $\left(\times 10^{-7}\right)$ |  |
| :--- | ---: | :---: | ---: | ---: | ---: |
| Decay mode | $-0.3 \pm 2.0 \pm 0.9$ | $2.15 \pm 0.03$ | $-0.6 \pm 4.8 \pm 2.3$ | 8.0 | 860 |
| $D^{0} \rightarrow \pi^{0} e^{ \pm} \mu^{\mp}$ | $0.7 \pm 1.7 \pm 0.7$ | $3.01 \pm 0.04$ | $1.9 \pm 4.6 \pm 1.9$ | 8.6 | 500 |
| $D^{0} \rightarrow K_{\mathrm{S}}^{0} e^{ \pm} \mu^{\mp}$ | $0.8 \pm 1.8 \pm 0.8$ | $2.31 \pm 0.03$ | $2.8 \pm 6.1 \pm 2.6$ | 12.4 | 830 |
| $D^{0} \rightarrow \bar{K}^{* 0} e^{ \pm} \mu^{\mp}$ | $-0.7 \pm 1.7 \pm 0.4$ | $2.10 \pm 0.03$ | $-1.8 \pm 4.4 \pm 1.0$ | 5.0 | 490 |
| $D^{0} \rightarrow \rho^{0} e^{ \pm} \mu^{\mp}$ | $0.0 \pm 1.4 \pm 0.3$ | $3.43 \pm 0.04$ | $0.1 \pm 3.8 \pm 0.9$ | 5.1 | 340 |
| $D^{0} \rightarrow \phi e^{ \pm} \mu^{\mp}$ | $0.4 \pm 2.3 \pm 0.5$ | $1.46 \pm 0.03$ | $1.8 \pm 9.5 \pm 1.9$ | 17.1 | 1200 |
| $D^{0} \rightarrow \omega e^{ \pm} \mu^{\mp}$ |  |  | $6.1 \pm 9.7 \pm 2.3$ | 22.5 | 1000 |
| $D^{0} \rightarrow \eta e^{ \pm} \mu^{\mp}$ |  |  |  |  |  |
| with $\eta \rightarrow \gamma \gamma$ | $1.6 \pm 2.3 \pm 0.5$ | $2.96 \pm 0.04$ | $7.0 \pm 10.5 \pm 2.4$ | 24.0 |  |
| with $\eta \rightarrow \pi^{+} \pi^{-} \pi^{0}$ | $0.0 \pm 2.8 \pm 0.7$ | $2.46 \pm 0.04$ | $0.4 \pm 25.8 \pm 6.0$ | 42.8 |  |

CLEO,
PRL 76 (1996) 3065.
E791,
PRL 86 (2001) 3969

## Summary of charm LNV/LFV

Heavy Flavor Averaging Group https://hflav.web.cern.ch


## Summary of LNV/LFV

Heavy Flavor Averaging Group https://hflav.web.cern.ch


## Search for $B^{+} \rightarrow K^{+} \mu^{-} \tau^{+}$

$$
\text { LHCb, JHEP } 2020(2020) 129 \quad 9 \mathrm{fb}^{-1}
$$

- This charge combination is cleaner than $B^{+} \rightarrow K^{+} \mu^{+} \tau^{-}$, which has more background from $B \rightarrow \bar{D} X \mu^{+} v_{\mu}$ due to $\bar{D} \rightarrow K^{+}$
- Produce the $B^{+}$in the decay $B_{s 2}^{* 0} \rightarrow B^{+} K^{-}$
- Obtain the $\tau^{-}$4-momentum up to a quadratic ambiguity by using the $K^{+} \mu^{-}$vertex and the known masses.

- Previously used this technique for $B^{+} \rightarrow \bar{D}^{0} X \mu^{+} v_{\mu}$ [PRD 99 (2019) 092009


## Signal \& background

Signal-like


- Use the SSK sample to train a BDT to separate signal from background, e.g.,
- $\bar{B} \rightarrow D\left(\rightarrow K^{+} X\right) Y \mu^{-} \bar{v}_{\mu} \quad$ (SL $b$ decays with wrong-sign charm decay)
- $B \rightarrow \bar{D}\left(\rightarrow K^{+} \mu^{-} \bar{v}_{\mu}\right) Y \quad\left(\mu^{-}\right.$from charm decay)
- Although $M_{D} \sim M_{\tau}$, there is no SM background that peaks in $m_{\text {miss }}^{2}$, e.g.,
- $B^{+} \rightarrow K^{+} \mu^{-}\left(\bar{v}_{\mu}\right) D^{+}$not possible in the SM
- $B^{+} \rightarrow K^{+} \pi^{-} D^{+}$is $2^{\text {nd }} \operatorname{order}$ (with $\pi^{-}$misidentified as $\mu^{-}$)


## Signal extraction

Fit $m_{\text {miss }}^{2}$ distribution to signal peak + polynomial background in 4 BDT bins


No significant signal

## Normalization and results

Normalize the yield to $B^{+} \rightarrow J / \psi K^{+}$



$$
\begin{aligned}
\mathcal{B}\left(B^{+} \rightarrow K^{+} \mu^{-} \tau^{+}\right) & <3.9 \times 10^{-5} \text { at } 90 \% \mathrm{CL} \\
& <4.5 \times 10^{-5} \text { at } 95 \% \mathrm{CL}
\end{aligned}
$$

Heavy FLavor AVeraging group (HFLAV) - April 2019

## LNV \& LFV B decays summary

HFLAV https://hflav.web.cern.ch



Chuck Narris observed LFV. LNV too.

| RPP\# | Mode | PDG2017 Avg. | BABAR | BELLE | LHCb | Our Avg. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 552 | $\pi^{+} e^{ \pm} \mu^{\mp}$ | $<0.17$ | $<0.17$ |  |  | $<0.17$ |
| 553 | $\pi^{+} e^{+} \tau^{-}$ | < 74 | < 74 |  |  | < 74 |
| 554 | $\pi^{+} e^{-} \tau^{+}$ | $<20$ | $<20$ |  |  | $<20$ |
| 555 | $\pi^{+} e^{ \pm} \tau^{\mp}$ | $<75$ | $<75$ |  |  | < 75 |
| 556 | $\pi^{+} \mu^{+} \tau^{-}$ | $<62$ | $<62$ |  |  | <62 |
| 557 | $\pi^{+} \mu^{-} \tau^{+}$ | $<45$ | $<45$ |  |  | $<45$ |
| 558 | $\pi^{+} \mu^{ \pm} \tau^{\mp}$ | $<72$ | $<72$ |  |  | $<72$ |
| 559 | $K^{+} e^{+} \mu^{-}$ | $<0.091$ | $<0.091$ |  |  | $<0.091$ |
| 560 | $K^{+} e^{-} \mu^{+}$ | $<0.13$ | $<0.13$ |  |  | $<0.13$ |
| 561 | $K^{+} e^{ \pm} \mu^{\mp}$ | $<0.091$ | $<0.091$ |  |  | $<0.091$ |
| 562 | $K^{+} e^{+} \tau^{-}$ | < 43 | < 43 |  |  | < 43 |
| 563 | $K^{+} e^{-} \tau^{+}$ | $<15$ | $<15$ |  |  | $<15$ |
| 564 | $K^{+} e^{ \pm} \tau^{\mp}$ | < 30 | < 30 |  |  | <30 |
| 565 | $K^{+} \mu^{+} \tau^{-}$ | < 45 | < 45 |  |  | < 45 |
| 566 | $K^{+} \mu^{-} \tau^{+}$ | $<28$ | $<28$ |  | $<39$ | <28 |
| 567 | $K^{+} \mu^{ \pm} \tau^{\mp}$ | < 48 | < 48 |  |  | < 48 |
| 568 | $K^{*+} e^{+} \mu^{-}$ | $<1.3$ | $<1.3$ |  |  | $<1.3$ |
| 569 | $K^{*+} e^{-} \mu^{+}$ | $<0.99$ | $<0.99$ |  |  | $<0.99$ |
| 570 | $K^{*+} e^{ \pm} \mu^{\mp}$ | <1.4 | <1.4 |  |  | <1.4 |
| 571 | $\pi^{-} e^{+} e^{+}$ | $<0.023$ | $<0.023$ |  |  | $<0.023$ |
| 572 | $\pi^{-} \mu^{+} \mu^{+}$ | $<0.013$ | $<0.107$ |  | $<0.004^{\dagger}$ | $<0.004^{\dagger}$ |
| 573 | $\pi^{-} e^{+} \mu^{+}$ | < 0.15 | $<0.15$ |  |  | < 0.15 |
| 574 | $\rho^{-} e^{+} e^{+}$ | $<0.17$ | $<0.17$ |  |  | $<0.17$ |
| 575 | $\rho^{-} \mu^{+} \mu^{+}$ | $<0.42$ | $<0.42$ |  |  | $<0.42$ |
| 576 | $\rho^{-} e^{+} \mu^{+}$ | $<0.47$ | $<0.47$ |  |  | $<0.47$ |
| 577 | $K^{-} e^{+} e^{+}$ | $<0.03$ | $<0.03$ |  |  | $<0.03$ |
| 578 | $K^{-} \mu^{+} \mu^{+}$ | $<0.041$ | $<0.067$ |  | $<0.041$ | $<0.041$ |
| 579 | $K^{-} e^{+} \mu^{+}$ | < 0.16 | $<0.16$ |  |  | < 0.16 |
| 580 | $K^{*-} e^{+} e^{+}$ | $<0.40$ | $<0.40$ |  |  | < 0.40 |
| 581 | $K^{*-} \mu^{+} \mu^{+}$ | < 0.59 | < 0.59 |  |  | < 0.59 |
| 582 | $K^{*-} e^{+} \mu^{+}$ | $<0.30$ | $<0.30$ |  |  | $<0.30$ |
| 583 | $D^{-} e^{+} e^{+}$ | <2.6 | $<2.6$ | $<2.6$ |  | <2.6 |
| 584 | $D^{-} e^{+} \mu^{+}$ | < 1.8 | $<2.1$ | < 1.8 |  | < 1.8 |
| 585 | $D^{-} \mu^{+} \mu^{+}$ | $<0.69$ | $<1.7$ | $<1.1$ | < 0.69 | $<0.69$ |
| 586 | $D_{s}^{-} \mu^{+} \mu^{+}$ | < 0.58 |  |  | < 0.58 | $<0.58$ |
| 587 | $\bar{D}^{0} \pi^{-} \mu^{+} \mu^{+}$ | <1.5 |  |  | <1.5 | <1.5 |
| 589 | $\Lambda^{0} \mu^{+}$ | $<0.06$ | $<0.06$ |  |  | $<0.06$ |
| 590 | $\Lambda^{0} e^{+}$ | < 0.032 | <0.032 |  |  | $<0.032$ |
| 591 | $\bar{\Lambda}^{0} \mu^{+}$ | <0.06 | $<0.06$ |  |  | $<0.06$ |
| 592 | $\bar{\Lambda}^{0} e^{+}$ | <0.08 | <0.08 |  |  | <0.08 |

# $B_{(s)}^{0} \rightarrow \mu^{+} \mu^{-}$LHC combination 

| Same note: | LHCb-CONF-2020-002 |  | PRL 118 (2017) 191801, $1 \mathrm{fb}^{-1} @ 7 / 8 \mathrm{TeV}+1.4 \mathrm{fb}^{-1} @ 13 \mathrm{TeV}$ |
| :---: | :---: | :---: | :---: |
|  | CMS PAS BPH-20-003 | $\longleftarrow$ | JHEP 04 (2020) 188, $25 \mathrm{fb}^{-1} @ 7 / 8 \mathrm{TeV}+26.3 \mathrm{fb}^{-1} @ 13 \mathrm{TeV}$ |
|  | ATLAS-CONF-2020-049 |  | JHEP 04 (2019) 098, $25 \mathrm{fb}^{-1} @ 7 / 8 \mathrm{TeV}+36.0 \mathrm{fb}^{-1} @ 13 \mathrm{TeV}$ |

- FCNC decays, both loop- and helicity-suppressed
- Very rare in the SM and hence a good probe of NP
- Uncertainties in the SM BR calculation recently reduced thanks to advances in
- Lattice QCD [e.g., Flavour Lattice Averaging Group, EPJC 80 (2020) 113]
- EW effects at NLO [Bobeth, Gorbahn, Stamou, PRD 89 (2014) 034023]
- QCD effects at NNLO [Hermann, Misiak, Steinhauser, JHEP 12 (2013) 097]
- SM expectations for the BRs:

$$
\begin{aligned}
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right) & =(3.66 \pm 0.14) \times 10^{-9} \\
\mathcal{B}\left(B^{0} \rightarrow \mu^{+} \mu^{-}\right) & =(1.03 \pm 0.05) \times 10^{-10}
\end{aligned}
$$

## Effective lifetime for $B_{S} \rightarrow \mu^{+} \mu^{-}$

Time-dependent partial width for $B_{S}+\bar{B}_{S}$ (no flavor tag)
Width diff. b/w

$$
\begin{aligned}
& \text { mass eigenstates } \\
& \text { Average width of } \\
& \text { mass eigenstates. }
\end{aligned}
$$

$$
1 / \tau_{B_{s}}
$$

Heavy- and light-eigenstate contribution to the decay $\rightarrow \mu^{+} \mu^{-}$

$$
\mu^{+} \mu^{-} \text {is CP-odd, so } A_{\Delta \Gamma}=1 \text { in the SM, }
$$

$$
\text { expect } \tau_{B_{S} \rightarrow \mu^{+} \mu^{-}}=\tau_{B_{S}^{H}}=1.609 \pm 0.010 \mathrm{ps.} \text { This could change in NP. }
$$

$$
\begin{aligned}
& \tau_{B_{s}^{0} \rightarrow \mu^{+} \mu^{-}} \equiv \frac{\int_{0}^{\infty} t\left\langle\Gamma\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)\right\rangle d t}{\int_{0}^{\infty}\left\langle\Gamma\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)\right\rangle d t} \\
& =\frac{\tau_{B_{s}^{0}}}{1-y_{s}^{2}}\left[\frac{1+2 \mathcal{A}_{\Delta \Gamma} y_{s}+y_{s}^{2}}{1+\mathcal{A}_{\Delta \Gamma} y_{s}}\right] \\
& \mathcal{A}_{\Delta \Gamma} \equiv \frac{R_{H}^{\mu^{+} \mu^{-}}-R_{L}^{\mu^{+} \mu^{-}}}{R_{H}^{\mu_{H} \mu^{-}}+R_{L}^{\mu^{+} \mu^{-}}}
\end{aligned}
$$

## $m_{\mu^{+} \mu^{-}} \& t_{\mu^{+} \mu^{-}}$distributions





## ATLAS, CMS, LHCb results

- BR measured wrt. that of $B^{+} \rightarrow J / \psi K^{+}\left(\mathrm{LHCb}\right.$ used also $\left.B^{0} \rightarrow K^{+} \pi^{-}\right)$

$$
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)=\frac{f_{d}}{f_{s}} \frac{\varepsilon_{B^{+} \rightarrow J / \psi K^{+}}}{\varepsilon_{B_{s}^{0} \rightarrow \mu^{+} \mu^{-}}} \frac{N_{B_{s}^{0} \rightarrow \mu^{+} \mu^{-}}}{N_{B^{+} \rightarrow J / \psi K^{+}}} \mathcal{B}\left(B^{+} \rightarrow J / \psi K^{+}\right)
$$

$\frac{f_{s}}{f_{d}}=0.259 \pm 0.015$ measured by LHCb @ 7 TeV
ATLAS

$$
\begin{aligned}
& \mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)=\left(2.8_{-0.7}^{+0.8}\right) \times 10^{-9}, \\
& \mathcal{B}\left(B^{0} \rightarrow \mu^{+} \mu^{-}\right)=(-1.9 \pm 1.6) \times 10^{-10}, \\
& \\
& \mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)=\left[2.9_{-0.6}^{+0.7}(\exp ) \pm 0.2(\mathrm{frag})\right] \times 10^{-9}, \\
& \mathcal{B}\left(B^{0} \rightarrow \mu^{+} \mu^{-}\right)=\left(0.8_{-1.3}^{+1.4}\right) \times 10^{-10}, \\
& \tau_{B_{s}^{0} \rightarrow \mu^{+} \mu^{-}}=1.70_{-0.43}^{+0.60} \pm 0.09 \mathrm{ps}
\end{aligned}
$$

LHCb

$$
\begin{aligned}
& \mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)=\left(3.0 \pm 0.6_{-0.2}^{+0.3}\right) \times 10^{-9}, \\
& \mathcal{B}\left(B^{0} \rightarrow \mu^{+} \mu^{-}\right)=\left(1.5_{-1.0-0.1}^{+1.2+0.2}\right) \times 10^{-10}, \\
& \tau_{B_{s}^{0} \rightarrow \mu^{+} \mu^{-}}=2.04 \pm 0.44 \pm 0.05 \mathrm{ps}
\end{aligned}
$$

## Combination of profile likelihoods




$$
\begin{aligned}
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right) & =\left(2.69_{-0.35}^{+0.37}\right) \times 10^{-9} \\
\mathcal{B}\left(B^{0} \rightarrow \mu^{+} \mu^{-}\right) & =(0.6 \pm 0.7) \times 10^{-10}<1.9 \times 10^{-10}(95 \%) \\
\mathcal{R} & =0.021_{-0.025}^{+0.030}<0.069(95 \%)
\end{aligned}
$$

$$
\tau_{B_{s}^{0} \rightarrow \mu^{+} \mu^{-}}=1.91_{-0.35}^{+0.37} \mathrm{ps}
$$



## Search for $B^{0} \rightarrow$ invisible $(+\gamma)$

$$
\begin{array}{l|l}
\hline \text { Belle, PRD } 102(2020) 012003 & 711 \mathrm{fb}^{-1}, 772 \times 10^{6} \mathrm{~B} \overline{\mathrm{~B}}
\end{array}
$$

- FCNC, suppressed in the SM:
$-\operatorname{BR}\left(B^{0} \rightarrow\right.$ invis. $) \sim 10^{-16}($ for $4 v)$ [1]
$-\operatorname{BR}\left(B^{0} \rightarrow v \bar{v} \gamma\right) \sim 10^{-9}[2]$

- Fully reconstruct the other (tag) B in $\mathrm{O}\left(10^{3}\right)$ hadronic modes
- (The 2 B 's are not separated by direction)
- Reject events with additional good tracks, $\pi^{0}$ or $K_{L}$



## Signal and background

- Two neural networks used to suppress background
- (plots for $B^{0} \rightarrow \gamma+$ invis. Those for $B^{0} \rightarrow$ invis. are similar):


Evaluates tag-B quality $\quad \mathrm{O}_{\text {tag }}$


Evaluates event shape $\mathrm{O}_{\text {shape }}$

## Signal extraction \& results

- $B^{0} \rightarrow$ invis.: Fit the data distributions in 2 variables (uncorrelated)


Cosine of angle $\mathrm{b} / \mathrm{w}$ thrust axes of tag-B and remaining particles


$$
e^{+} e^{-} \rightarrow q \bar{q}
$$

Additional neutral energy in the EM calorimeter

- $B^{0} \rightarrow$ invis. $+\gamma$ : subtract bgd. estimated from $\mathrm{O}_{\mathrm{tag}}$ sideband, and count

$$
\begin{aligned}
& \mathcal{B}\left(B^{0} \rightarrow \text { invisible }\right)<7.8 \times 10^{-5} \\
& \mathcal{B}\left(B^{0} \rightarrow \text { invisible }+\gamma\right)<1.6 \times 10^{-5}
\end{aligned} \quad 90 \% \mathrm{CL}
$$

## Conclusions

- LFV, LNV, and rare decays are an excellent probe for NP
- Continually exploited as experiments collect more data and develop new analysis techniques
- Summary of the recent numbers:

| Decay mode <br> $D^{0} \rightarrow$ | $N_{\text {sig }}$ <br> (candidates) | $\epsilon_{\text {sig }}$ <br> $(\%)$ | $\mathcal{B}$ <br> $\left(\times 10^{-7}\right)$ | $\mathcal{B} 90 \%$ U.L. <br> $\left(\times 10^{-7}\right)$ |
| :--- | ---: | ---: | ---: | ---: |
| $\pi^{-} \pi^{-} e^{+} e^{+}$ | $0.22 \pm 3.15 \pm 0.54$ | 4.38 | $0.27 \pm 3.90 \pm 0.67$ | 9.1 |
| $\pi^{-} \pi^{-} \mu^{+} \mu^{+}$ | $6.69 \pm 4.88 \pm 0.80$ | 4.91 | $7.40 \pm 5.40 \pm 0.91$ | 15.2 |
| $\pi^{-} \pi^{-} e^{+} \mu^{+}$ | $12.42 \pm 5.30 \pm 1.45$ | 4.38 | $15.4 \pm 6.59 \pm 1.85$ | 30.6 |
| $\pi^{-} \pi^{+} e^{ \pm} \mu^{\mp}$ | $1.37 \pm 6.15 \pm 1.28$ | 4.79 | $1.55 \pm 6.97 \pm 1.45$ | 17.1 |
| $K^{-} \pi^{-} e^{+} e^{+}$ | $-0.23 \pm 0.97 \pm 1.28$ | 3.19 | $-0.38 \pm 1.60 \pm 2.11$ | 5.0 |
| $K^{-} \pi^{-} \mu^{+} \mu^{+}$ | $-0.03 \pm 2.10 \pm 0.40$ | 3.30 | $-0.05 \pm 3.34 \pm 0.64$ | 5.3 |
| $K^{-} \pi^{-} e^{+} \mu^{+}$ | $3.87 \pm 3.96 \pm 2.36$ | 3.48 | $5.84 \pm 5.97 \pm 3.56$ | 21.0 |
| $K^{-} \pi^{+} e^{ \pm} \mu^{\mp}$ | $2.52 \pm 4.60 \pm 1.35$ | 3.65 | $3.62 \pm 6.61 \pm 1.95$ | 19.0 |
| $K^{-} K^{-} e^{+} e^{+}$ | $0.30 \pm 1.08 \pm 0.41$ | 3.25 | $0.43 \pm 1.54 \pm 0.58$ | 3.4 |
| $K^{-} K^{-} \mu^{+} \mu^{+}$ | $-1.09 \pm 1.29 \pm 0.42$ | 6.21 | $-0.81 \pm 0.96 \pm 0.32$ | 1.0 |
| $K^{-} K^{-} e^{+} \mu^{+}$ | $1.93 \pm 1.92 \pm 0.83$ | 4.63 | $1.93 \pm 1.93 \pm 0.84$ | 5.8 |
| $K^{-} K^{+} e^{ \pm} \mu^{\mp}$ | $4.09 \pm 3.00 \pm 1.59$ | 4.83 | $3.93 \pm 2.89 \pm 1.45$ | 10.0 |

$$
\begin{gathered}
\mathcal{B}\left(B^{+} \rightarrow K^{+} \mu^{-} \tau^{+}\right)<3.9 \times 10^{-5} \text { at } 90 \% \mathrm{CL} \\
\\
<4.5 \times 10^{-5} \text { at } 95 \% \mathrm{CL} \\
\mathcal{B}\left(B_{s}^{0} \rightarrow \mu^{+} \mu^{-}\right)=\left(2.69_{-0.35}^{+0.37}\right) \times 10^{-9} \\
\mathcal{B}\left(B^{0} \rightarrow \mu^{+} \mu^{-}\right)=(0.6 \pm 0.7) \times 10^{-10}<1.9 \times 10^{-10}(95 \%) \\
\mathcal{R}=0.021_{-0.025}^{+0.030}<0.069(95 \%) \\
\tau_{B_{s}^{0} \rightarrow \mu^{+}} \mu^{-}=1.91_{-0.35}^{+0.37} \mathrm{PS}
\end{gathered}
$$

| Decay mode | $N_{\text {sig }}$ <br> (candidates) | $\epsilon_{\text {sig }}$ <br> $(\%)$ | $\mathcal{B}\left(\times 10^{-7}\right)$ | $\mathcal{B} 90 \% 1$ <br> $B A B A R$ |
| :--- | ---: | ---: | ---: | ---: |
| $D^{0} \rightarrow \pi^{0} e^{ \pm} \mu^{\mp}$ | $-0.3 \pm 2.0 \pm 0.9$ | $2.15 \pm 0.03$ | $-0.6 \pm 4.8 \pm 2.3$ | 8.0 |
| $D^{0} \rightarrow K_{\mathrm{S}}^{0} e^{ \pm} \mu^{\mp}$ | $0.7 \pm 1.7 \pm 0.7$ | $3.01 \pm 0.04$ | $1.9 \pm 4.6 \pm 1.9$ | 8.6 |
| $D^{0} \rightarrow \bar{K}^{* 0} e^{ \pm} \mu^{\mp}$ | $0.8 \pm 1.8 \pm 0.8$ | $2.31 \pm 0.03$ | $2.8 \pm 6.1 \pm 2.6$ | 12.4 |
| $D^{0} \rightarrow \rho^{0} e^{ \pm} \mu^{\mp}$ | $-0.7 \pm 1.7 \pm 0.4$ | $2.10 \pm 0.03$ | $-1.8 \pm 4.4 \pm 1.0$ | 5.0 |
| $D^{0} \rightarrow \phi e^{ \pm} \mu^{\mp}$ | $0.0 \pm 1.4 \pm 0.3$ | $3.43 \pm 0.04$ | $0.1 \pm 3.8 \pm 0.9$ | 5.1 |
| $D^{0} \rightarrow \omega e^{ \pm} \mu^{\mp}$ | $0.4 \pm 2.3 \pm 0.5$ | $1.46 \pm 0.03$ | $1.8 \pm 9.5 \pm 1.9$ | 17.1 |
| $D^{0} \rightarrow \eta e^{ \pm} \mu^{\mp}$ |  |  | $6.1 \pm 9.7 \pm 2.3$ | 22.5 |
| $\quad$ with $\eta \rightarrow \gamma \gamma$ | $1.6 \pm 2.3 \pm 0.5$ | $2.96 \pm 0.04$ | $7.0 \pm 10.5 \pm 2.4$ | 24.0 |
| $\quad$ with $\eta \rightarrow \pi^{+} \pi^{-} \pi^{0}$ | $0.0 \pm 2.8 \pm 0.7$ | $2.46 \pm 0.04$ | $0.4 \pm 25.8 \pm 6.0$ | 42.8 |

$$
\begin{gathered}
\mathcal{B}\left(B^{0} \rightarrow \text { invisible }\right)<7.8 \times 10^{-5} \\
\mathcal{B}\left(B^{0} \rightarrow \text { invisible }+\gamma\right)<1.6 \times 10^{-5} \\
(90 \%)
\end{gathered}
$$

