

# FDC Project

Bin Gong

Collaborated with J.X. Wang

Institute of High Energy Physics, CAS

January 28, 2021

# Outline

- 1 Brief Introduction
- 2 Model generation
- 3 Process calculation

# Brief Introduction

- FDC = Feynman Diagram Calculation
- Purpose: automatic calculation of physical processes
- First developed by Prof. J.X. Wang since 1993
- First version of FDC has been presented at AIHENP93.
- Written in REDUCE and RLISP to generate Fortran Code
- Including some additional parts for certain physical research  
e.g. FDC-PWA (Partial Wave Analysis application for  
experimental study)
- Web: available at ???

# REDUCE

- A general-purpose Computer Algebra System geared towards applications in physics.
- Written in Portable Standard LISP
- Something like Mathematica, FORM and Maple etc.
- Open-source and free now (since December 2008)
- User-level language: RLISP
- Two modes: algebraic and symbolic
- Web: <http://www.reduce-algebra.com>

# a simple example of reduce

```

twain@Twains-MacBook:~$ reduce
Loading image file: /Users/twain/reduce-algebra/scripts/../pslbuild/x86_64-mac_unknown_version-darwin1
Reduce (Free PSL version), 12-Dec-2015 ...

1: vector p1,p2,p3,p4;
2: a:=g(l,p1,p2,p3,p4);
a := p1.p2*p3.p4 - p1.p3*p2.p4 + p1.p4*p2.p3
3: share a;
4: symbolic;

nil

5* reval(a);

(plus (times (cons p1 p2) (cons p3 p4)) (minus (times (cons p1 p3) (cons p2 p4))
) (times (cons p1 p4) (cons p2 p3)))

6* bye;

Quitting
twain@Twains-MacBook:~$ █

```

$\text{Tr}(\hat{p}_1 \hat{p}_2 \hat{p}_3 \hat{p}_4)$  is calculated here, shown in both algebraic and symbolic modes

## FDC System

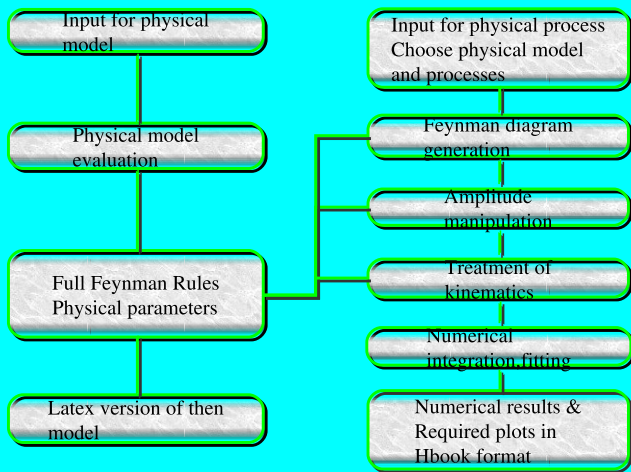


FIG.1: FDC system flow chart

## Prerequisites and Environments

- A Unix-like system
- REDUCE
  - open source
  - available at <http://reduce-algebra.com/downloading.htm>
- A Fortran Compiler
- MPI environment if you want to use MPI
- Environment variables
  - `fdc`: where you store your FDC source
  - `model`: where you store your models
  - `PATH`: you have to tell your OS where to find “reduce” and other commands provided by FDC
- `csh/tcsh`: modify `.cshrc` in your home directory and add:
  - `setenv fdc ~/fdc2.0`
  - `setenv model ~/model`
  - `set path=($path /usr/local/bin $fdc/bin ./)`

## Installation

- Install Reduce (usually psl version)
  - you will get a script called "redpsl" after installation
  - make a new script "reduce" with only two lines:  
`redhome="path of your reduce/../../pslbuild/..."`  
`exec $redhome/psl/bpsl -td 1000 -f $redhome/red/reduce.img`  
and put it in the directory you choose before  
check /usr/local/bin/reduce in the virtual machine for this step
- Copy FDC source to the directory your chosen above, and run `util/xbuild` to build fdc source in the source directory.
- Compile Fortran Libraries of FDC and BASES (confirm Fortran compiler).
- Construct/obtain a model



## Generate a new model in FDC

- No matter what tool you use in your study, a physical model is always needed, even at LO.
- A new model in FDC can be generate with following steps: (after the installation of FDC package)
  - create a new model directory from an old one with command:  
`model_cp source_dir target_dir`
  - modify the path to the directory in the file “model.tex” (% is symbol for comment in REDUCE)
  - modify the major input file “model\_input” which describes your physical model
  - run “`gmodel`”
  - a command “`glmodel`” is available to generate TeX file for your model

## a sample "model.tex" file

---

```
% Please revise the following items when a new model is created.
```

```
model_home:="/auto/homegb/gongb4/model/ex0/";
model_name:=""SM in UG and  $J/\psi$ ,  $J/\psi_8$ ,  $B_c$ "";
model_author:=""Jian-Xiong Wang"";
model_time:=""Nov 1, 2009"";
```

```
% The following three files must be prepared by USER and are placed
% in directory "model_home".
```

```
model_input='model_input$ % description of the physical model.
sybole_list='sybole_list$ % something needed for drawing diagram.
physical_parameters='physical_parameters$ % physical parameters input.
%add_counter_term_input:='one_loop_qcd_counter_term;
;end;
~
~
-
```

## a sample “model\_input” file for SM

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%----- The standard model in unitary gauge ----- %%%%%%%%%%%%%%%
%----- Gauge fields ----- %
gaugefields:=
%
  No.  Name  SU(n)  notation  coupling  breaking
  '(1  u    1    b      g1      yes   )
  (2  su   2    a      g      yes   )
  (3  su   3    gs     g3     no    )
  )$

%----- Matter fields ----- %
matterinput:={{name, 2*spin, chiral, "|g", 1, 2, 3}
, {hig, 0, rl, 1, 2, 0}
, {el, 1, l, -1, 2, 0}
, {er, 1, r, -2, 0, 0}
, {ql, 1, l, 1/3, 2, 3}
, {qldr, 1, r, -2/3, 0, 3}
, {qlur, 1, r, 4/3, 0, 3}
}$

%----- %
% name  n_group  1_componet  2_componet  ...
mdefl:={
  {hig, {2, xx2, (v0+h0-i*xx3)/2**0.5}}
  ,{el, {2, nue, ef}}
  ,{er, {2, ef, }}
  ,{ql, {2, qu, qd}}
  ,{qldr, {2, qd, }}
  ,{qlur, {2, qu, }}
  }$
vancumexpectation:='((hig v0));

fermion_generation:=(
  (q1l q2l q3l) (q1dr q2dr q3dr) (q1ur q2ur q3ur)
  (qu qc qt) (qd qs qb)
  (el mul taul) (er mur taur)
  (ef mu tau) (nue numu nut)
  );

```

## a sample “model\_input” file for IHDM

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%----- The standard model in unitary gauge ----- %%%%%%%%%%%%%%%
%----- Gauge fields -----
gaugefields:=
%   n-th Name SU(n) notation coupling breaking
%   '(1 u 1 b g1 yes )
%   (2 su 2 a g yes )
%   (3 su 3 gs g3 no )
%)$

%----- Matter fields -----
matterinput:={name, 2*spin, chiral, "lg", 1, 2, 3}
%   {hig1, 0, rl, 1, 2, 0}
%   {hig2, 0, rl, 1, 2, 0}
%   {el, 1, l, -1, 2, 0}
%   {er, 1, r, -2, 0, 0}
%   {q1l, 1, l, 1/3, 2, 3}
%   {q1dr, 1, r, -2/3, 0, 3}
%   {q1ur, 1, r, 4/3, 0, 3}
}$

%-----
mdefl:={ % name n-th group 1_componet 2_componet ...
%   {hig1, {2, xx2, (v0+h0-i*xx3)/2**0.5 }}
%   {hig2, {2, xx21, (h01-i*xx31)/2**0.5 }}
%   {el, {2, nue, ef }}
%   {er, {2, ef }}
%   {q1l, {2, qu, qd }}
%   {q1dr, {2, qd }}
%   {q1ur, {2, qu }}
}$

vacumexpectation:='((hig1 v0));

fermion_generation:='(q1l q2l q3l) (q1dr q2dr q3dr) (q1ur q2ur q3ur)
%   (qu qc qt) (qd qs qb)
%   (el mul taul) (er mur taur)
%   (ef mu tau) (nue numu nut)
);

give_up_compact:='ok;

```

## The file “matterinput”

- It is first generated by the command “gmodel”
- specify your model by change this file (choices of free parameters, masses, gauge parameters, etc)
- run “gmodel” again to apply the changes
- “matterinput” will not be changed if it already exists when you run “gmodel”

## part of "matterinputt" file for SM

```

+hig(-1)*er(-1)*el(1)*c(0,2)
+hig(-1)*hig(1)*c(0,1)
+hig(-1)*hig(1)*hig(-1)*hig(1)*c(0,5)
+hig(-1)*qldr(-1)*qll(1)*c(0,3)
+higtid(-1)*q1ur(-1)*qll(1)*c(0,4)
+qll(-1)*qldr(1)*hig(1)*c(0,3)
+qll(-1)*q1ur(1)*higtid(1)*c(0,4)$
█

gauge_boson_redefine:=(a(1,~v) => (w(1,v) + w(-1,v))/sqrt(2),
a(2,~v) => ((w(-1,v) - w(1,v))/sqrt(2))/i,
a(3,~v) => cos(theta)*z(0,v) + p(0,v)*sin(theta),
b(~v) => cos(theta)*p(0,v) - sin(theta)*z(0,v))$

% where g1 can be any one of g1,g,sin(theta)$
construles:=(g1 => g*sin(theta)/cos(theta),
zm => wm/cos(theta),
c(0,1) => (- 8*c(0,5)*wm**3 + g**3*td1)/(2*g**2*wm),
v0 => (2*wm)/g,
c(0,5) => (- g**2*h0m**2)/(8*wm**2))$

% where mass of each particle can be changed, such as just put it to 0$

phymass:='(pg 0) (gsg 0) (gs 0) (w wm) (z zm) (p 0) (qb fmb) (qs fms) (qd fmd) (qt fmt) (qc fmc) (qu fmu) (tau fmtau) (mu fmmu) (ef fmfef) (
nut 0) (numu 0) (nue 0) (h0 h0m) (xx3 xx3m) (xx2 xx2m))$

% where please take away zero mass$

phyinput:='(wm fmb fms fmd fmc fmu fmtau fmmu fmfef h0m theta g g3)$

pchalist:='((taul (tau -1) (nut 0)) (mul (mu -1) (numu 0)) (taur (tau -1)) (mur (mu -1)) (q3l (qb (quotient (minus 1) 3)) (qt (quotient 2 3)
)) (q2l (qs (quotient (minus 1) 3)) (qc (quotient 2 3))) (q3dr (qb (quotient (minus 1) 3)) (q2dr (qs (quotient (minus 1) 3))) (q3ur (qt (
quotient 2 3))) (q2ur (qc (quotient 2 3))) (gs (gs 0)) (a (w 1) (z 0) (p 0)) (b (p 0) (z 0)) (q1ur (qu (quotient 2 3))) (q1dr (qd (quotient
(minus 1) 3))) (q1l (qd (quotient (minus 1) 3)) (qu (quotient 2 3))) (er (ef -1)) (el (ef -1) (nue 0)) (hig (xx3 0) (h0 0) (xx2 1)))
$

gauge_fix_term_list:=(f(p,ksi1,ksi1p,pd(p(0,v),v) + xx3(0)*ksi1p*zm,pg(-1)),
f(z,ksi2,ksi2p,pd(z(0,v),v) + xx3(0)*ksi2p*zm,zg(-1)),
f(w,ksi3,ksi3p,pd(w(-1,v),v) + xx2(-1)*ksi3p*wm,wgm(-1)),
f(w,ksi3,ksi3p,pd(w(1,v),v) - xx2(1)*ksi3p*wm,wgp(-1)),
f(gs(1c10),ksi4,ksi4p,pd(gs(1c10,v),v),gsg(-1,1c10)))$

r_ksi_value:='((ksi1 . 1) (ksi2 . 1) (ksi3 . 1) (ksi4 . 1));

r_ksiip_value:='((ksi1p . 0) (ksi2p . ksi2) (ksi4p . 0) (ksi3p . ksi3));

```

## part of "matterinput" file for IHDM

```

coupling_comment:='(g3 " strong interaction ") (g "electro-weak interaction ")  )$
model_input_comment:="This is Standard Model in unitary gauge, include electro-weak interaction and QCD, Quark mixing terms are dropped."$

matterinteraction:=el(-1)*er(1)*hig1(1)*c(0,5)
+hig1(-1)*er(-1)*el(1)*c(0,5)
+hig1(-1)*hig1(1)*c(0,1)
+hig1(-1)*hig1(1)*hig1(-1)*hig1(1)*c(0,10)
+hig2(-1)*hig2(1)*c(0,3)
+hig1(-1)*hig1(1)*hig2(-1)*hig2(1)*c(0,9)*g**2
+hig1(-1)*hig2(1)*hig1(-1)*hig2(1)*c(0,7)*g**2
+hig1(-1)*hig2(1)*hig2(-1)*hig1(1)*c(0,8)*g**2
+hig2(-1)*hig1(1)*hig2(-1)*hig1(1)*c(0,7)*g**2
+hig2(-1)*hig2(1)*hig2(-1)*hig2(1)*c(0,6)*g**2$
%+hig1(-1)*hig1(1)*hig2(-1)*hig2(1)*c(0,9)
%+hig1(-1)*hig2(1)*hig1(-1)*hig2(1)*c(0,7)
%+hig1(-1)*hig2(1)*hig2(-1)*hig1(1)*c(0,8)
%+hig2(-1)*hig1(1)*hig2(-1)*hig1(1)*c(0,7)
%+hig2(-1)*hig2(1)*hig2(-1)*hig2(1)*c(0,6)$

gauge_boson_redefine:={a(1,~v) => (w(1,v) + w(-1,v))/sqrt(2),
a(2,~v) => ((w(-1,v) - w(1,v))/sqrt(2))/i,
a(3,~v) => cos(theta)*z(0,v) + p(0,v)*sin(theta),
b(~v) => cos(theta)*p(0,v) - sin(theta)*z(0,v)}$

% where g1 can be any one of g1,g,sin(theta)$
construles:={g1 => g*sin(theta)/cos(theta),
zm => wm/cos(theta),
c(0,1) => (- 8*c(0,10)*wm**3 + g**3*td1)/(2*g**2+wm),
v0 => (2*wm)/g,
%c(0,3) => - 2*c(0,9)*wm**2 - xx21m**2,
c(0,9) => -(c(0,3)+xx21m**2)/2/wm**2,
c(0,8) => (- h01m**2 + 2*xx21m**2 - xx31m**2)/(4*wm**2),
c(0,7) => (- h01m**2 + xx31m**2)/(8*wm**2),
c(0,3) => mu2p,
c(0,6) => lambda2a,
c(0,10) => (- g**2*h0m**2)/(8*wm**2)
}$

% where mass of each particle can be changed, such as just put it to 0$

phymass:='(pg 0) (gsg 0) (gs 0) (w wm) (z zm) (p 0) (tau fntau) (mu fmmu) (ef fme) (nut 0) (numu 0) (nue 0) (h01 h01m) (xx31 xx31m) (xx21
xx21m) (h0 h0m) (xx3 xx3m) (xx2 xx2m)}$

% where please take away zero mass$

```

part of “model.pdf” for SM

model.pdf (第 17 页, 共 23 页) ▾

model.pdf

17

### D. Three Vector Bosons Vertices

There are 3 vertices in the section

Vertex 120:  $Z_\mu^0(p_1) - W_\mu^+(p_2) - W_\mu^-(p_3)$

$$V_{120} = \cos \theta_w g i (-g_{\nu,\alpha} p_{1,\mu} + g_{\mu,\nu} p_{1,\alpha} + g_{\nu,\alpha} p_{2,\mu} - g_{\mu,\alpha} p_{2,\nu} + g_{\mu,\alpha} p_{3,\nu} - g_{\mu,\nu} p_{3,\alpha})$$

Vertex 121:  $\gamma_\nu(p_1) - W_\mu^+(p_2) - W_\mu^-(p_3)$

$$V_{121} = \sin \theta_w g i (-g_{\nu,\alpha} p_{1,\mu} + g_{\mu,\nu} p_{1,\alpha} + g_{\nu,\alpha} p_{2,\mu} - g_{\mu,\alpha} p_{2,\nu} + g_{\mu,\alpha} p_{3,\nu} - g_{\mu,\nu} p_{3,\alpha})$$

Vertex 122:  $g_{\mu,\alpha}(p_3) - g_{\alpha,\beta}(p_2) - g_{\nu,\alpha}(p_1)$

$$V_{122} = f_{a,b,c} g_\alpha (g_{\nu,\alpha} p_{1,\mu} - g_{\mu,\nu} p_{1,\alpha} - g_{\nu,\alpha} p_{2,\mu} + g_{\mu,\alpha} p_{2,\nu} - g_{\mu,\alpha} p_{3,\nu} + g_{\mu,\nu} p_{3,\alpha})$$

### E. Four Scalar Bosons Vertices

There are 6 vertices in the section

Vertex 12:  $\phi^+(p_2) - \phi^+(p_1) - \phi^-(p_4) - \phi^-(p_3)$

$$V_{12} = \frac{-g^2 m_A^2 i}{2m_W^2}$$

Vertex 11:  $\phi^0(p_2) - \phi^0(p_1) - \phi^+(p_3) - \phi^-(p_4)$

$$V_{11} = \frac{-g^2 m_A^2 i}{4m_W^2}$$

Vertex 16:  $h^0(p_2) - h^0(p_1) - \phi^+(p_3) - \phi^-(p_4)$

$$V_{16} = \frac{-g^2 m_A^2 i}{4m_W^2}$$

Vertex 15:  $\phi^0(p_4) - \phi^0(p_3) - h^0(p_2) - h^0(p_1)$

$$V_{15} = \frac{-g^2 m_A^2 i}{4m_W^2}$$

Vertex 18:  $h^0(p_4) - h^0(p_3) - h^0(p_2) - h^0(p_1)$

$$V_{18} = \frac{-3g^2 m_A^2 i}{4m_W^2}$$



## Current Models

- The Standard Model (SM) has already been constructed.
- The Minimal Supersymmetric Standard Model (MSSM) also has been constructed.
- Some other new NP models (2HDM, IHDM)
- Also compatible with phenomenological models (add\_vertices).
- Most intermediate states and effective vertices from NRQCD has been implemented in the SM.
- QCD counter terms have been manually inserted in the SM.

## Automatic Renormalization (still in process)

- In high order calculation, renormalization of the model is needed to generate counter terms which cancel the UV divergences from virtual corrections.
- The renormalization of QCD is simple ( $\overline{MS}$  for coupling,  $\overline{MS}/OS$  for fields).
- But for electroweak, you have so many choices. Things are totally different:
  - mixing between particles (more renormalization constants)
  - renormalization constants before/after SSB
  - dependence of counter terms on gauge-fixing and gauge parameters
  - different renormalization conditions ( $\overline{MS}/OS$ , zero/nonzero masses)
  - Some NP model needs special treatment (FJ tadpole scheme)

## Preset renormalization schemes in FDC

```

-----
%For scheme_switch, you can choose number 1,2,3... and what are these number represent list as follows.
% n      model      gauge-fixing      gauge-symmetrization      gauge      renormalization
%-----
% 1      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  Feynman-gauge  on-shell
% 2      Electroweak  European-scheme   gauge-asymmetric-scheme  Feynman-gauge  on-shell
% 3      Electroweak  kyoto-scheme      gauge-symmetric-scheme   Feynman-gauge  on-shell
% 4      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  unitary-gauge   on-shell
% 5      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  R_ksi-gauge     on-shell
% 6      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  nonlinear-gauge  on-shell
% 7      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  Landau-gauge    on-shell
% 8      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  unitary-gauge   MS(coupling constant) on-shell(others)
% 9      Electroweak  kyoto-scheme      gauge-asymmetric-scheme  Feynman-gauge   MS(coupling constant) on-shell(others)
% 10     QCD          kyoto-scheme      gauge-asymmetric-scheme  Feynman-gauge   MS
% 11     QCD          kyoto-scheme      gauge-asymmetric-scheme  Feynman-gauge   on-shell(all fields) MS(coupling constants)
-----

```

## Calculation (for both LO and NLO)

- create a directory for the process use `process_cp`
- modify “process.def” and “option” files in the directory to specific
  - physical model of your process
  - incoming and outgoing particles
  - order of result
  - way to obtain squared amplitude
  - some others...
- use `doall` to perform the following:
  - `gen_diag`: generate diagrams of the process (`psdraw`)
  - `amp`: manipulate square of amplitude and output in Fortran
  - `kine`: generate code for phase space integration
  - `make`: compile the Fortran code
- run the Fortran code with `int (int2, int3, int4)`
- LO only:
  - parton level event generation (SPRING inside BASES)
  - parton shower and hadronization (PYTHIA)

## a sample "process.def"

```

Please revise the following items when a new process is created.
algebraic;
model_home:="'/auto/homegb/gongb/model/smu2nloop_up_to_c/";
process_name:="'$g g-->J/psi$ Production in $e^+ e^-$ collider";
process_author:="'Jian-Xiong Wang";
process_time:="'March 1, 2006";

namel:=(ef efb jpsi etac)$
inpl:=(1 1 -1 -1)$
ncorrection:=( (g 0) (g3 2) )$
ncolor:='1$
%check_gauge_invariance:='ok;
approximation_rules:={hjpm=>2*fmc,hjpm2=>4*fmc2,hetacm=>2*fmc,hetacm2=>4*fmc2};
%special_case_option:='((1 p ec ef));
mass_drop_list:='((fme 0));
no_abs_list:='ok;
n_charge_c:='0$
%do_not_sum_ferry_partner:='ok;
input_list:=(
  (ec 10.6)
  (alpha (quotient 1 137.0))
  (acc1 0.01)
  (acc2 0.01)
  (itm1 10)
  (itm2 10)
  (ncall 2000)
  (mxdim 50)
)$
end$
histograms:={

  {1,pt(p3),50,1,5,"Pt of Jpsi"},

  {2,wcos(p3,z),50,"cos(Jpsi and beam) "}
}

```

## a sample “option”

```

%*****
% This file contains all the options which could be used in FDC system
% and all the option are set to default values. User can change them
% by set their value to other possible value explained in the comment
% line.
%*****
%***** The following is options for kinematics %*****
%  check_kin='ok$
%  physical_cut='ok$
%The list of diagram to be considered in kinematics generation
%  keep_list:='(1 2 3 4 5 6);
%***** The following is options for diagram generation %*****
%The list of diagram to be considered in amplitudes calculation
  ec_sqrts='ok;
  pan_list_drop:='((pa1 qb qt));
%  diagram_keep_list:='(1);
%  diagram_keep_list1:='(1 80 81 82 83 84);
%  diagram_keep_list1:='(1 37);
%  diagram_keep_list1:='(48);
%  ct_choose:='1;
%  ncolor:='1$
%  selfenergy:='ok$
% To add width in calculation
%  addwidth:='ok$
  amp_method:='trees$
  amp_method:='2$
%  diag_drop:='ok$

```

part of Feynman diagrams for  $e^+e^- \rightarrow J/\psi + \eta_c$

diag.pdf (第 1 页, 共 15 页)

1

Fig. 1

Fig. 2

Fig. 3

Fig. 4

## One-loop Part of FDC (EW still in process)

$$d\sigma^{(1)} = d\sigma_V(\text{Loop} + \text{CT}) + d\sigma_R$$

$$d\sigma_R = d\sigma_S(\delta_s) + d\sigma_{HC}(\delta_s, \delta_c) + d\sigma_{H\bar{C}}(\delta_s, \delta_c)$$

- The one-loop part of FDC is completed in 2007, and upgraded in 2011 to calculate processes involving P-wave particles
- The results are obtained analytically.
  - at the level of amplitude square, before the integration of phase space.
  - usually they are still in numerical form (Fortran codes), as in most cases, they are too complicated to read.
- A two-cutoff phase space slicing method (PSS) is realized in FDC to deal with IR divergences in real correction processes
- The divergences are factorized in soft/collinear limit, and added to corresponding virtual correction processes.



- Counter term diagrams are generated automatically (after the input of renormalization constant)
- Loop integrals are calculated analytically under dimensional regularization.
- All the divergence (both UV and IR) are separated during the calculation of amplitude analytically, and summed up to check if they are really cancelled with others.
- In 2007 version, Passarino-Veltman reduction method is used for tensors reduction
- In 2011, new reduction method (a kind of IBP) for loop integrals is realized.
- The cutoff independence has to be checked after summing up both real and virtual corrections.

## Fortran Codes

- all stored in the directory `fort`
- makefile
- `int.f`: main program, need parameters in `input.dat`
- `parameter(1).f`: physical parameters
- `func.f`: phase space
- `amps2.f`: squared amplitude
  - method 1:
    - `amp???.f / ampl???.f`: LO/NLO amplitude of corresponding diagram
    - `ams???.f`: square of LO amplitude
    - `amsl???.f`: square of NLO amplitude with LO amplitude
  - method 2
    - `amps20.f`: square of LO amplitude
    - `amp???.f`: square of corresponding NLO diagram with LO amplitude
- output: `convergence.dat` `fresult.dat`

## a sample “makefile”

```
# FILE makefile

# FDC1.0 Version  1.00

SHELL      = /bin/csh
f77        = ifort
fopt       =
psintlib   = basesd
fdclib     = fdcd

intlkdir   = /auto/homegb/gongb4/fdc2.0/basesv5.1/lib

cernldir   = /cern/2001/lib

fdcldir    = /auto/homegb/gongb4/fdc2.0/f77

psintlib1  = ooptools

LFLAGS=-lpdflib804 -lpacklib -lmathlib -lkernlib
.suffixes: .f .o
.f.o:
    $(f77) $(fopt) -c $*.f
#
.suffixes: .F .o
.F.o:
    $(f77) $(fopt) -c -g -I$(LT)/include $*.F
#
objs       = int.o amps2.o func.o \
            ampl83.o ampl81.o ampl80.o ampl79.o \
```

## part of "amps2.f"

```

.....
call amp158()
call amp159()
call amp160()
call amp175()
call amp176()
call amp177qd()
call amp177qs()
call amp177qu()
call amp177qc()
call amp178()
call amp179()
call amp180()
call amp181()
call amp183()
call genppp()
C The following is tree-diagram contribution
a0=amps20()

a1=c(1)
amps2=wc0**2*a0+wc0*wc1*(2*a1+b1)
amps2=wc0**2*a0
return
end

```

```

FUNCTION amps20()
IMPLICIT real*8(A-H,O-Z)
IMPLICIT integer(I-N)
include 'inclppp.f'
include 'inclcon.f'
include 'inclcon1.f'
real*8 u,t,s
COMMON / stu / u,t,s
ans=(8*s**2+16*s*t-8*s+16*t**2-8*t+1)/(8*fmc**6*s**5)
amps20=ans
return
end

```

## Some others

- combination of Fortran libraries using pre-compilation
- geometric strategy for Sector Decomposition
- numerical method for Fermion Lines
- automatic generation of R2 terms for OPP method
- reduction of coefficient (rational fraction)

Thanks for your attention!