

Tetraquark states at BESIII

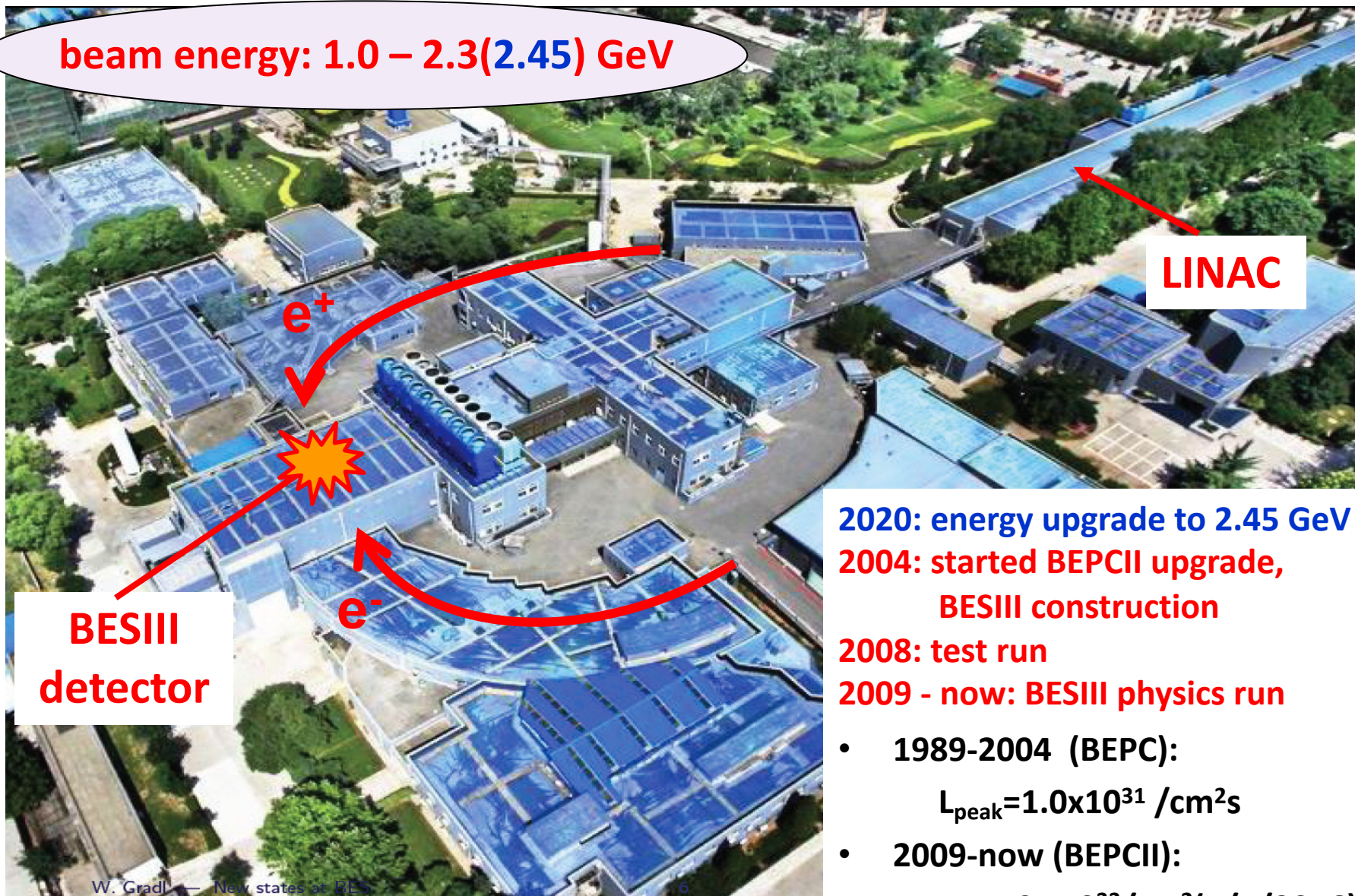
Xiao-Rui Lyu (吕晓睿)

University of Chinese Academy of Sciences (UCAS)

(On behalf of the BESIII collaboration)

- Introduction
- The tetraquark states
 - Observation of the $Z_{cs}(3985)$
 - PWA of $e^+e^- \rightarrow \pi^0\pi^0 J/\psi$ and $\pi^0 Z_c(3900)^0$ cross sections
 - Evidence of $Z_c(3900)^+ \rightarrow \rho^+ \eta_c$
 - Search for $Z_c \rightarrow \pi \chi_{cJ}, \pi \eta_c$
- Future prospects
- Summary

beam energy: 1.0 – 2.3(2.45) GeV



LINAC

BESIII
detector

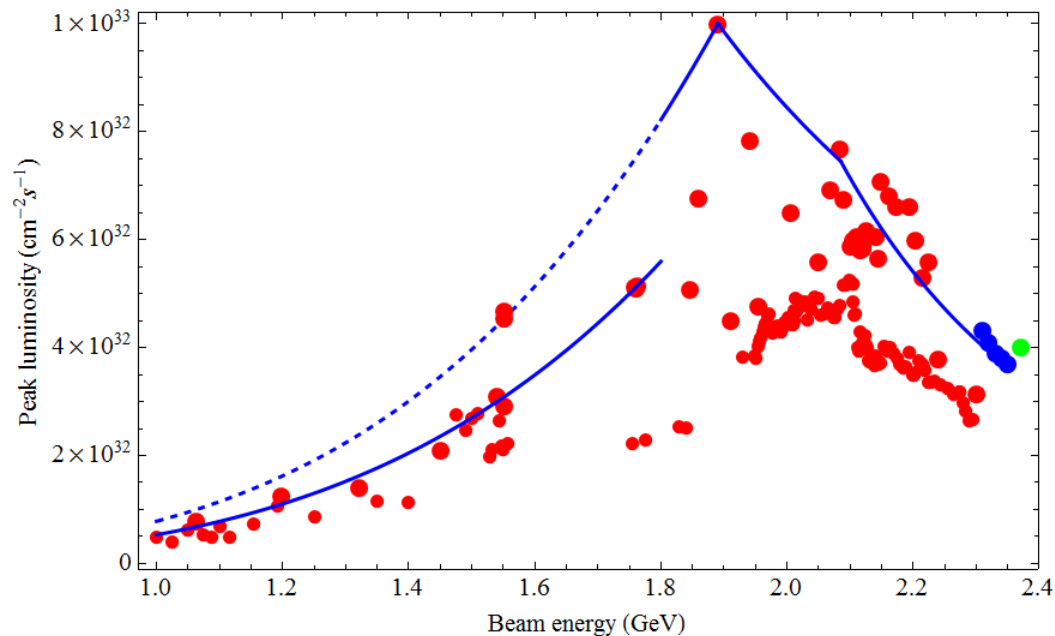
- 2020: energy upgrade to 2.45 GeV
- 2004: started BEPCII upgrade, BESIII construction
- 2008: test run
- 2009 - now: BESIII physics run

- 1989-2004 (BEPC):
 $L_{\text{peak}} = 1.0 \times 10^{31} / \text{cm}^2 \text{s}$
- 2009-now (BEPCII):

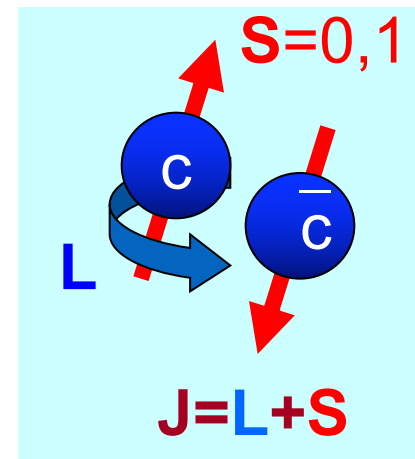
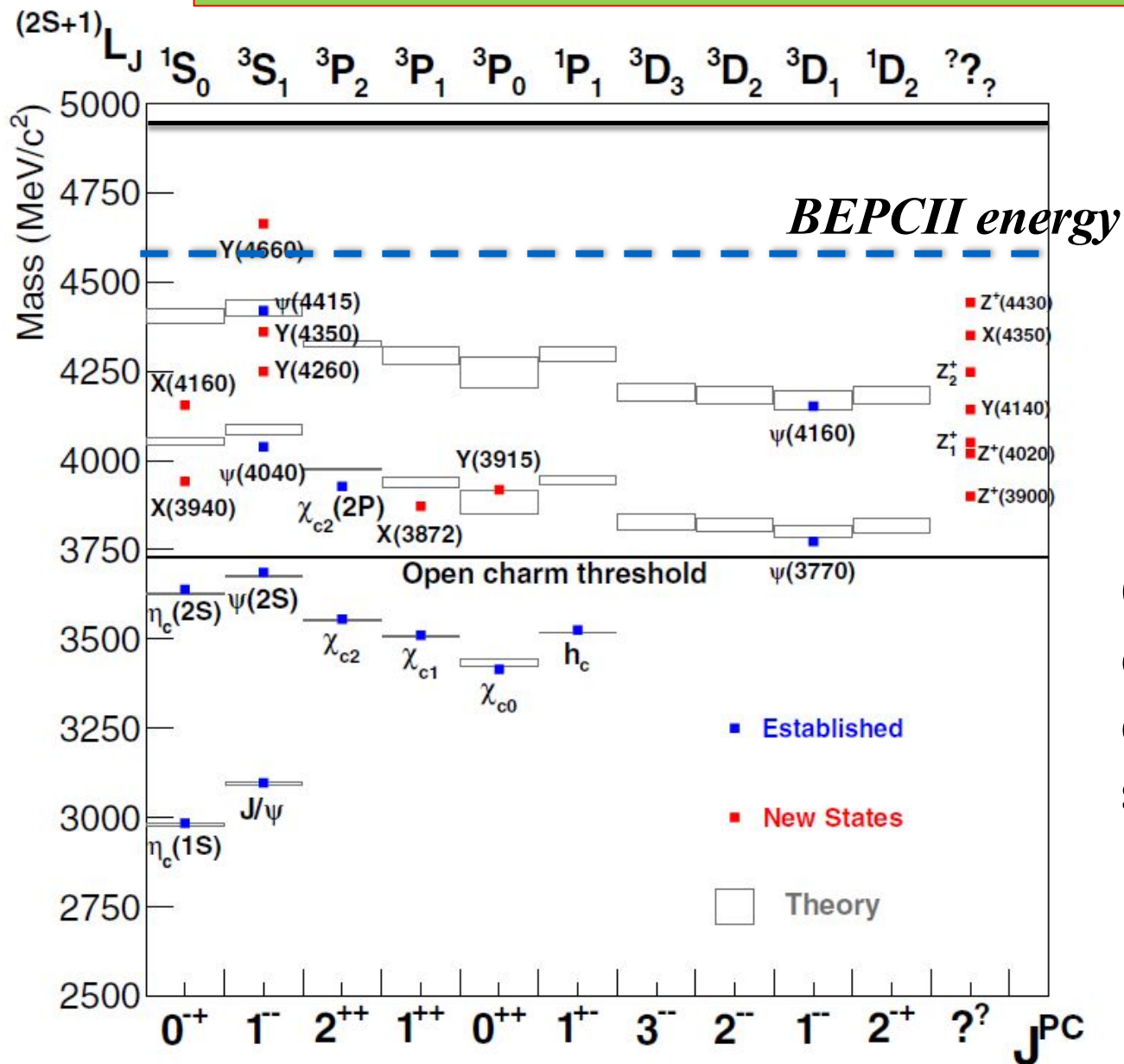
$L_{\text{peak}} = 1.0 \times 10^{33} / \text{cm}^2 (4/5/2016)$

- Increase of beam energy 2.30→2.35(2018)→2.45 GeV(2020')
 - → 2.35 GeV in 2018 summer (done)
 - → 2.45 GeV in 2020 summer (done),
change ISPB (Interaction region SePtum Bending) magnet
- Top-up injection (done)
 - Data taking efficiency increases by 20~30%

Now we are running at 2.37 GeV



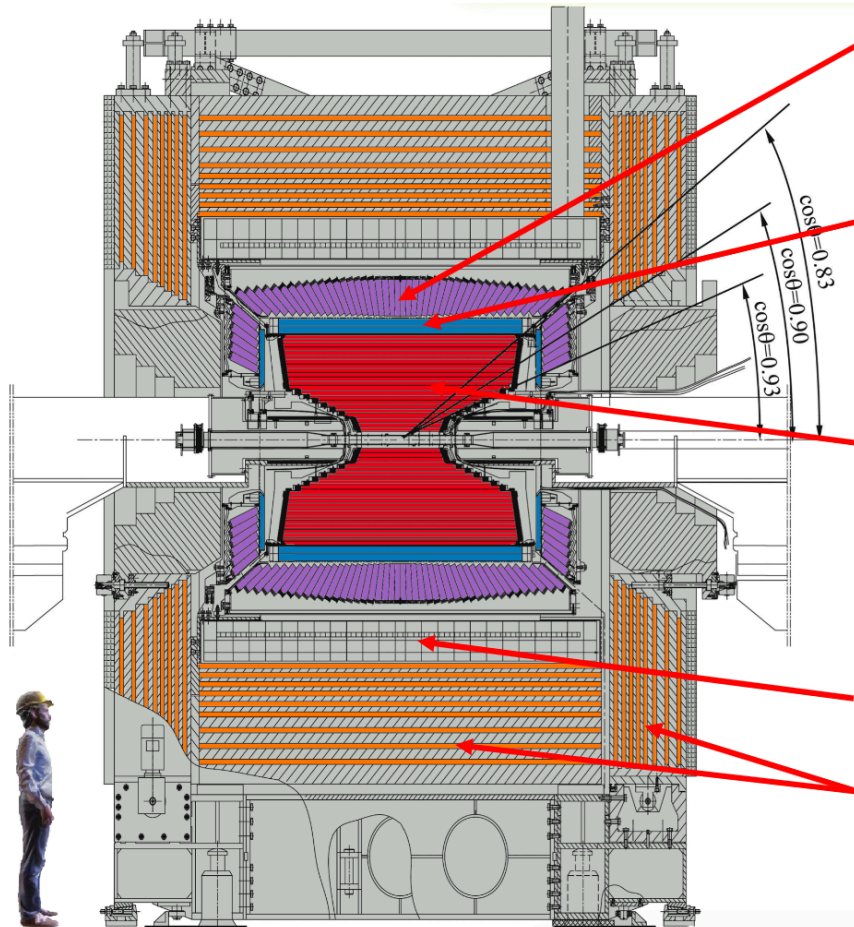
Charmonium Spectrum



Overpopulated observed **new** charmonium-like states, i.e. “XYZ”.

The BESIII detector

NIM A614, 345 (2010)



EMC: CsI crystals

$\Delta E/E = 2.5\%$ @ 1 GeV - Barrel

$\Delta E/E = 5.0\%$ @ 1 GeV - Endcaps

TOF:

$\sigma_T = 80$ ps Barrel

$\sigma_T = 110$ (60) ps Endcap

MDC: small cell & He gas

$\sigma_{xy} = 130$ μm

$\sigma_p/p = 0.5\%$ @ 1 GeV

$dE/dx = 6\%$

Magnet: 1T Super conducting

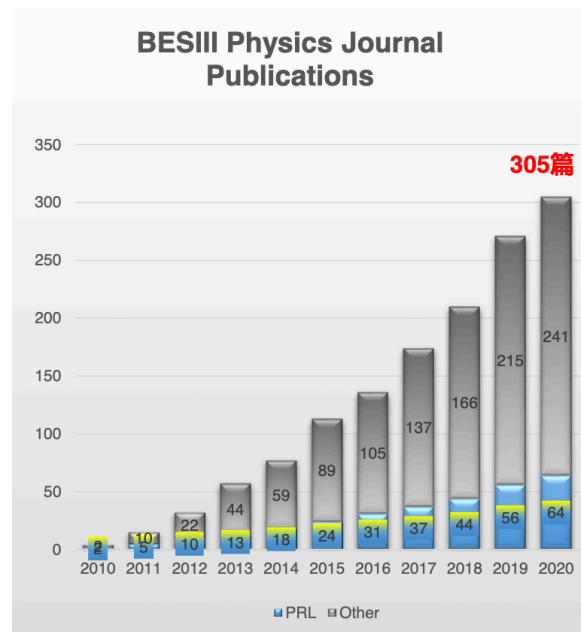
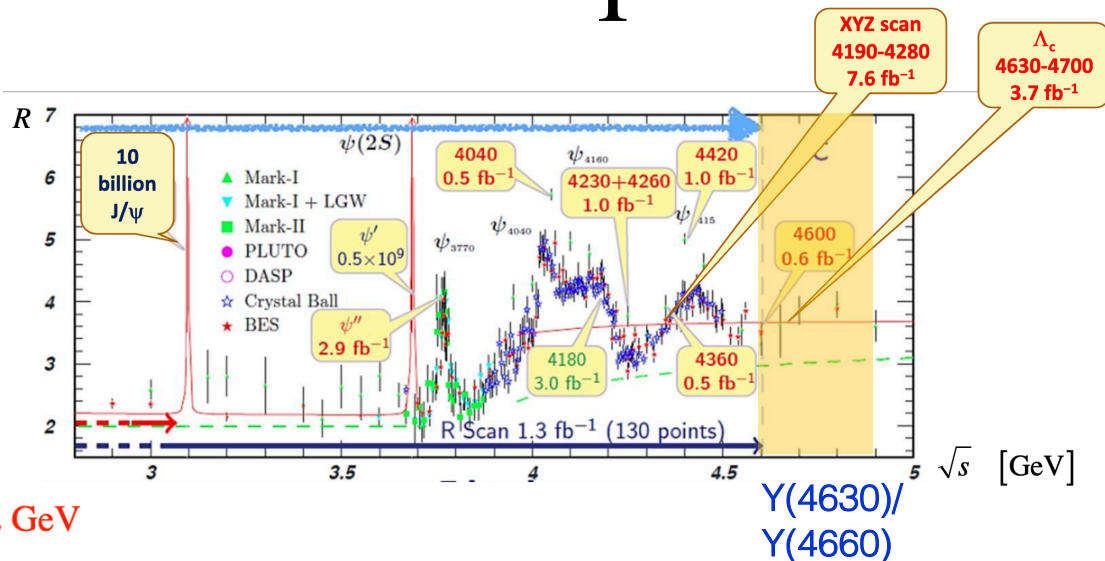
Muon ID: 9 layer RPC

Trigger: Tracks & Showers

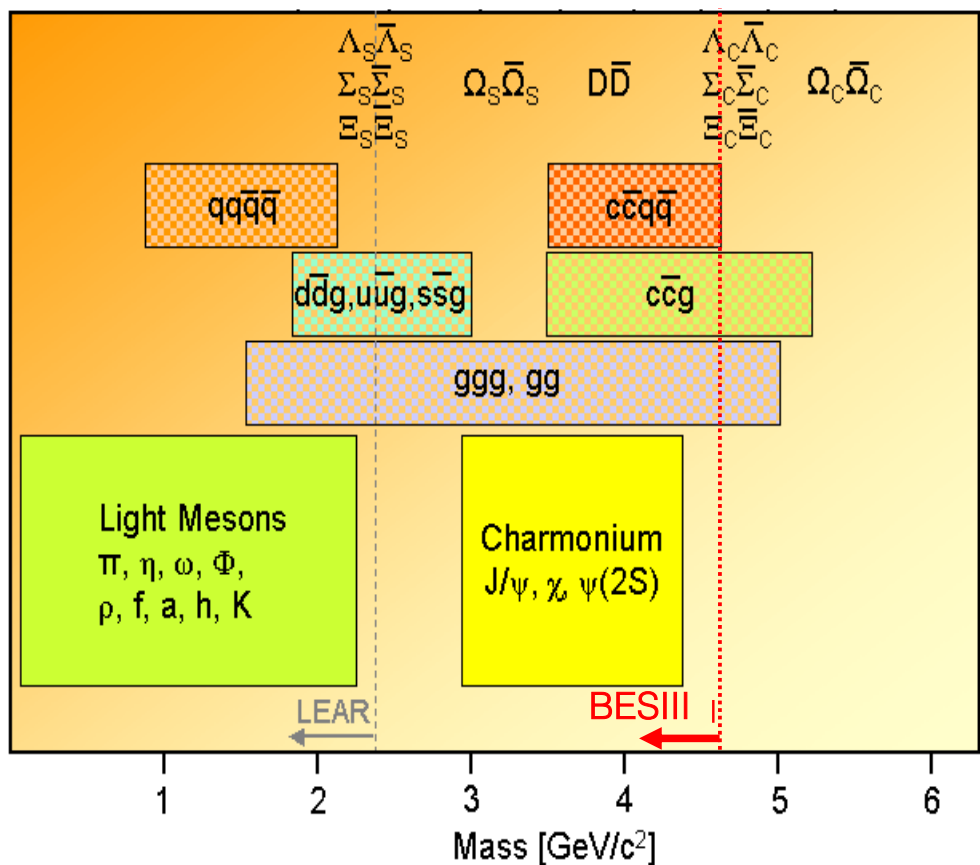
The new BESIII detector is hermetic for neutral and charged particle with excellent resolution, PID, and large coverage.

BESIII data sample

- 2009: 106M $\psi(2S)$
225M J/ψ
- 2010: 975 pb⁻¹ at $\psi(3770)$
- 2011: 2.9 fb⁻¹ (total) at $\psi(3770)$
482 pb⁻¹ at 4.01 GeV
- 2012: 0.45B (total) $\psi(2S)$
1.3B (total) J/ψ
- 2013: 1092 pb⁻¹ at 4.23 GeV
826 pb⁻¹ at 4.26 GeV
540 pb⁻¹ at 4.36 GeV
10 × 50 pb⁻¹ scan 3.81 — 4.42 GeV
- 2014: 1029 pb⁻¹ at 4.42 GeV
110 pb⁻¹ at 4.47 GeV
110 pb⁻¹ at 4.53 GeV
48 pb⁻¹ at 4.575 GeV
567 pb⁻¹ at 4.6 GeV
0.8 fb⁻¹ R-scan 3.85 — 4.59 GeV
- 2015: R-scan 2 — 3 GeV + 2.175 GeV
- 2016: ~3fb⁻¹ at 4.18 GeV (for D_s)
- 2017: 7 × 500 pb⁻¹ scan 4.19 — 4.27 GeV
- 2018: more J/ψ (and tuning new RF cavity)
- 2019: 10B (total) J/ψ
8 × 500 pb⁻¹ scan 4.13, 4.16, 4.29 — 4.44 GeV
- 2020: 5 × 500 pb⁻¹ scan 4.63 — 4.70 GeV (+ extra)



Hadron Landscape

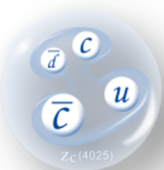


Hadron-physics challenges:

- Understanding of established states: precision spectroscopy
- Nature of exotic states: search and spectroscopy of unexpected states

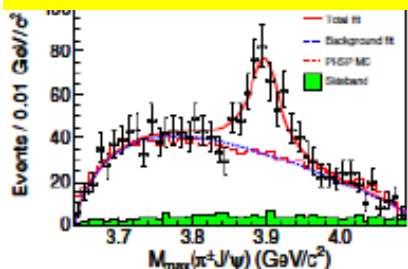
At BESIII, two golden measures to study hadron spectroscopy, *esp.*, to search for **exotics**

- Light hadrons: charmonium radiative decays (act as spin filter)
- Heavy hadrons: direct production, radiative and **hadronic transitions**



Zc(3900)⁺

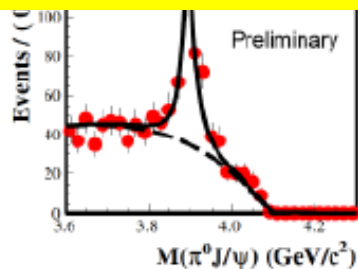
PRL 110, 252001 (2013)



$$e^+e^- \rightarrow \pi^- \pi^+ J/\psi$$

Zc(3900)⁰

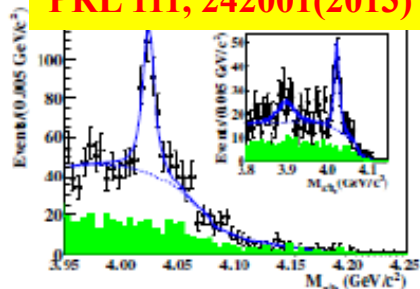
PRL 115, 112003 (2015)



$$e^+e^- \rightarrow \pi^0 \pi^0 J/\psi$$

Zc(4020)⁺

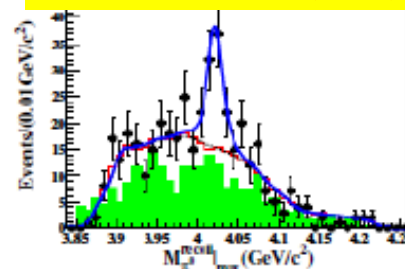
PRL 111, 242001(2013)



$$e^+e^- \rightarrow \pi^- \pi^+ h_c$$

Zc(4020)⁰

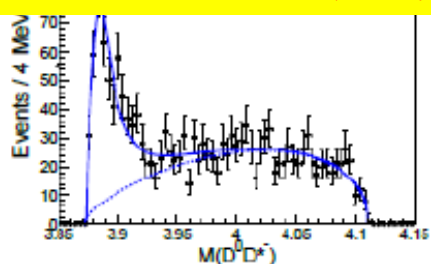
PRL 113, 212002 (2014)



$$e^+e^- \rightarrow \pi^0 \pi^0 h_c$$

Zc(3885)⁺

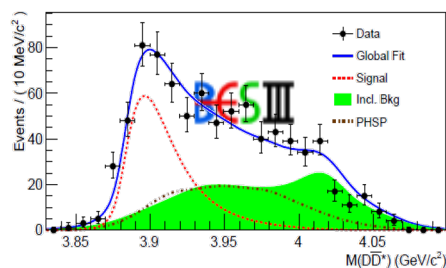
ST: PRL 112, 022001(2014)
DT: PRD92, 092006 (2015)



$$e^+e^- \rightarrow \pi^- (D \bar{D}^*)^+$$

Zc(3885)⁰

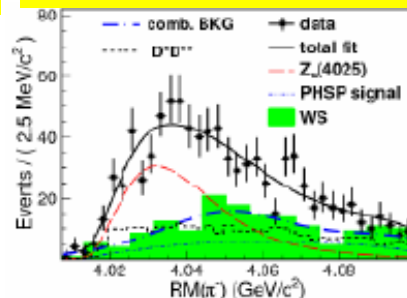
PRL 115, 222002 (2015)



$$e^+e^- \rightarrow \pi^0 (D^* \bar{D})^0$$

Zc(4025)⁺

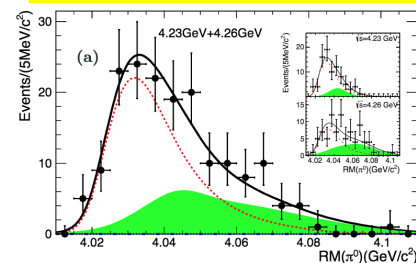
PRL 112, 132001 (2014)



$$e^+e^- \rightarrow \pi^- (D^* \bar{D}^*)^+$$

Zc(4025)⁰

PRL 115, 182002 (2015)



$$e^+e^- \rightarrow \pi^0 (D^* \bar{D}^*)^0$$

Which is the nature of these states?

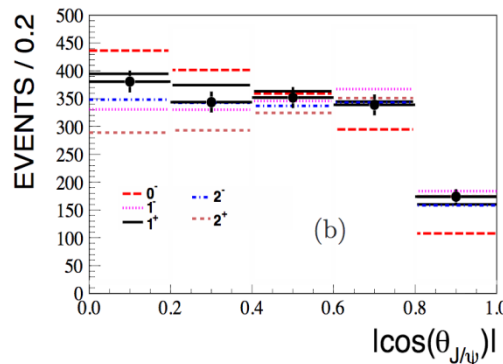
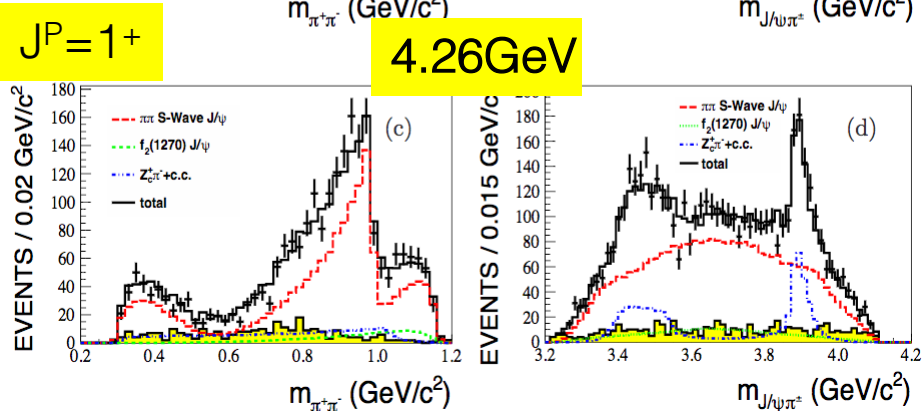
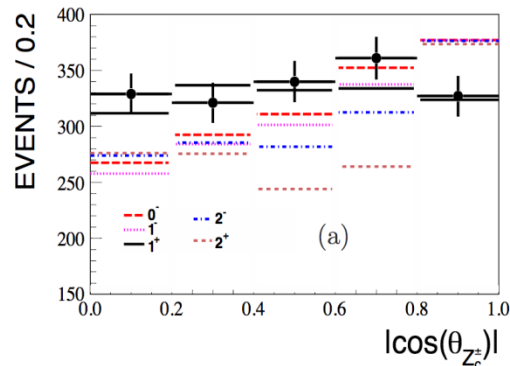
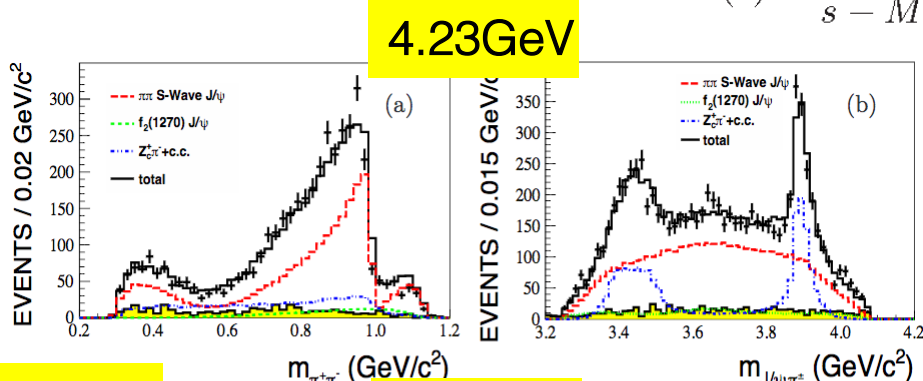
Different decay channels of the same observed states? Other decay modes?

SU(3) counter part Zcs (d → s) ?

- Z_c line shape parameterized with Flatte-like formula

PRL 119.072001 (2017)

$$BW(s) = \frac{1}{s - M^2 + i(g_1' \rho_{\pi J/\psi}(s) + g_2' \rho_{D^* D}(s))}$$

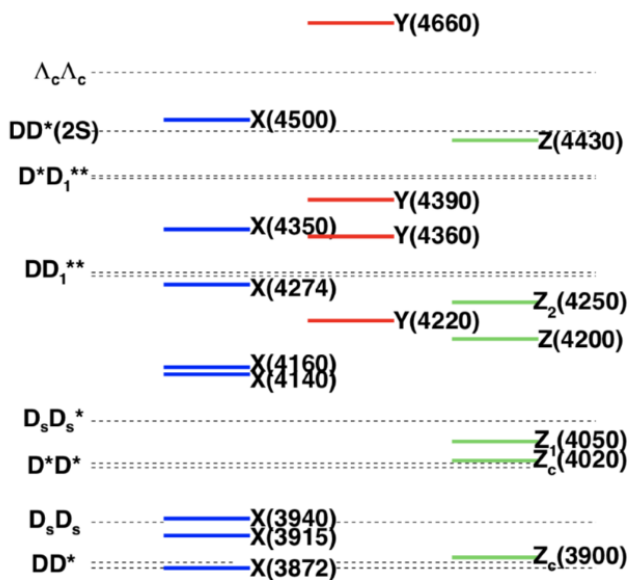


Hypothesis	$\Delta(-2 \ln L)$	$\Delta(\text{ndf})$	Significance
1^+ over 0^-	94.0	13	7.6σ
1^+ over 1^-	158.3	13	10.8σ
1^+ over 2^-	151.9	13	10.5σ
1^+ over 2^+	96.0	13	7.7σ

J^P is measured to be 1^+ with significance larger than 7.6σ

from S. L. Olsen, arXiv:1511.01589, arXiv:1812.10947

$Z_c^+(3900)$	3890 ± 3	33 ± 10	1^{+-}	$Y(4260) \rightarrow \pi^- + (J/\psi \pi^+)$ $Y(4260) \rightarrow \pi^- + (D\bar{D}^*)^+$	BESIII [49], Belle [50] BESIII [69]
$Z_c^+(4020)$	4024 ± 2	10 ± 3	$1(?)^{+(?) -}$	$Y(4260) \rightarrow \pi^- + (h_c \pi^+)$ $Y(4260) \rightarrow \pi^- + (D^* \bar{D}^*)^+$	BESIII [51] BESIII [52]
$Z_1^+(4050)$	4051_{-43}^{+24}	82_{-55}^{+51}	$?^{?+}$	$B \rightarrow K + (\chi_{c1} \pi^+)$	Belle [53], BaBar [66]
$Z^+(4200)$	4196_{-32}^{+35}	370_{-149}^{+99}	1^{+-}	$B \rightarrow K + (J/\psi \pi^+)$	Belle [62]
$Z_2^+(4250)$	4248_{-45}^{+185}	177_{-72}^{+321}	$?^{?+}$	$B \rightarrow K + (\chi_{c1} \pi^+)$	Belle [53], BaBar [66]
$Z^+(4430)$	4477 ± 20	181 ± 31	1^{+-}	$B \rightarrow K + (\psi' \pi^+)$ $B \rightarrow K + (J\psi \pi^+)$	Belle [54, 56, 57], LHCb [58] Belle [62]

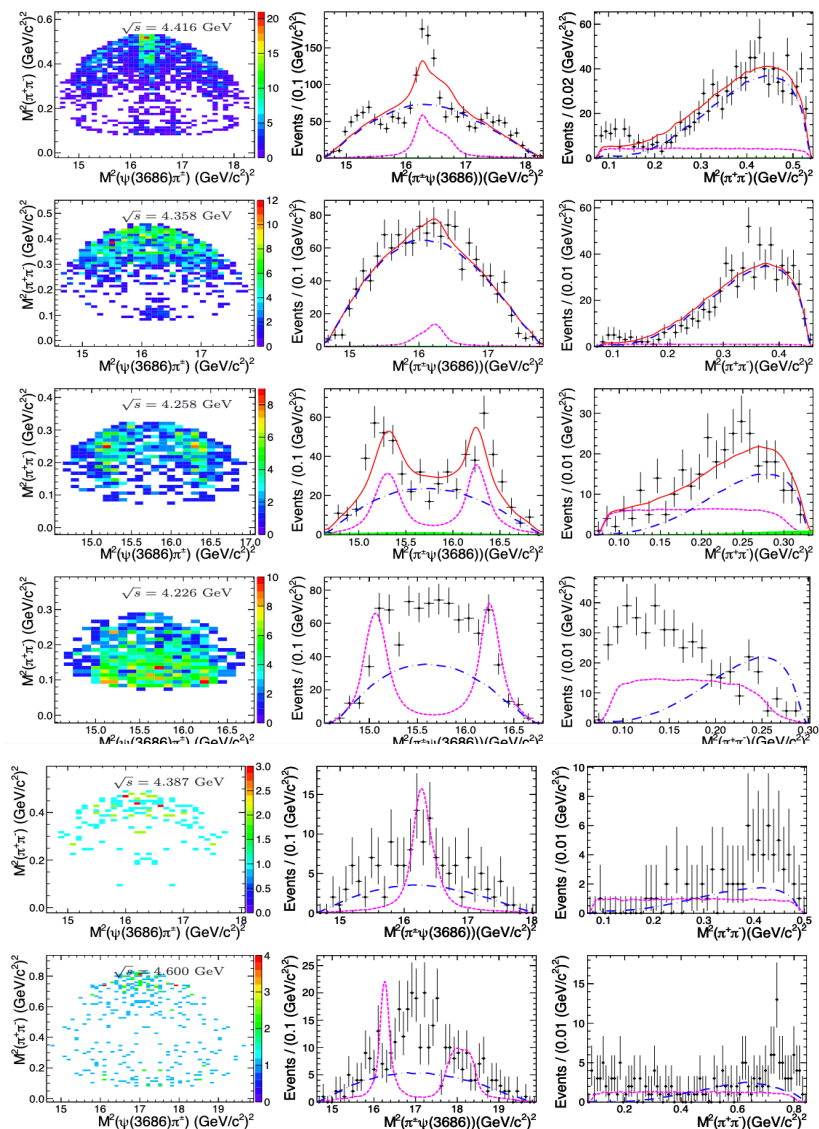


Most of them are close to the mass thresholds of charmed meson pairs
More efforts are needed to pin down their nature

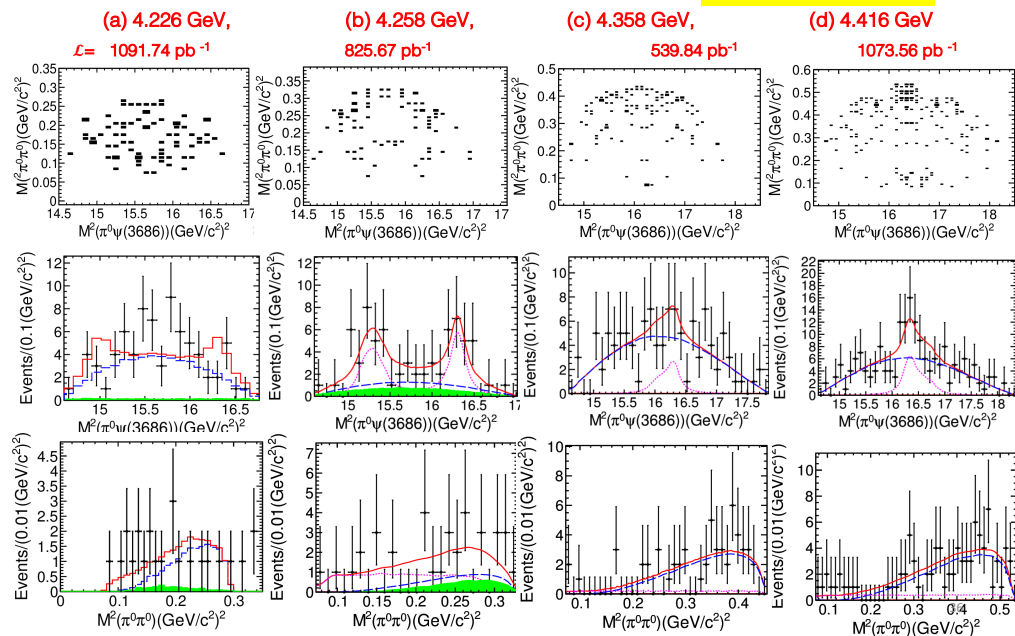
PRD 96, 032004 (2017)

$$e^+e^- \rightarrow \pi\pi\psi(3686)$$

PRD 97, 052001 (2018)

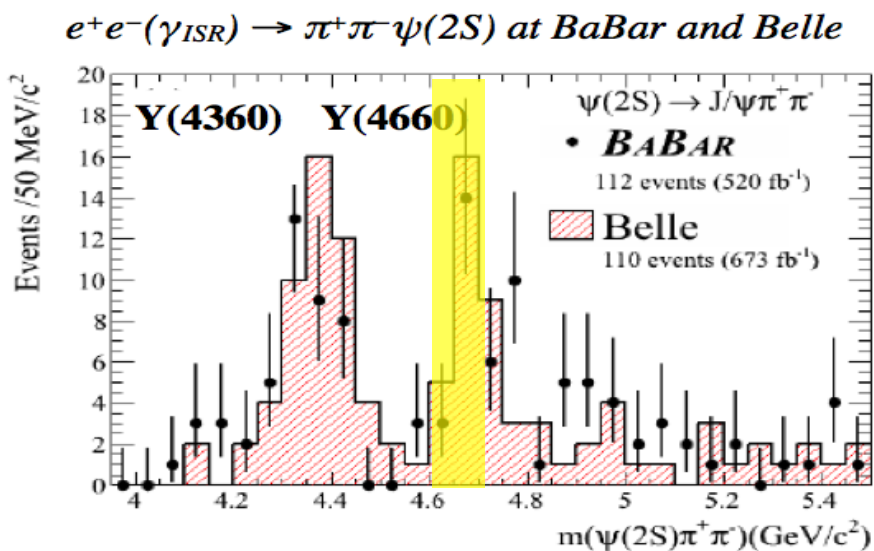
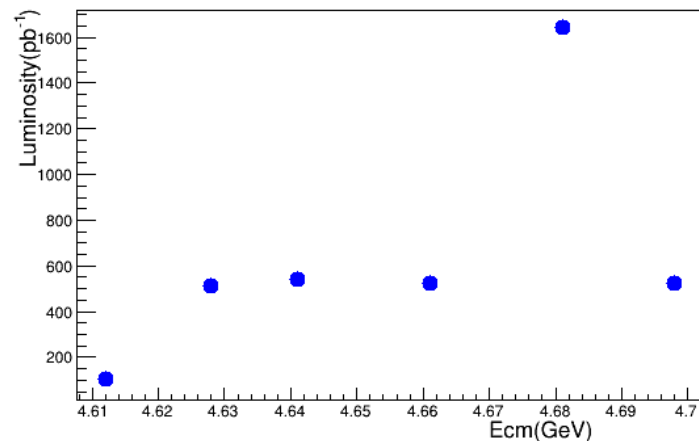


PRD 97, 052001 (2018)

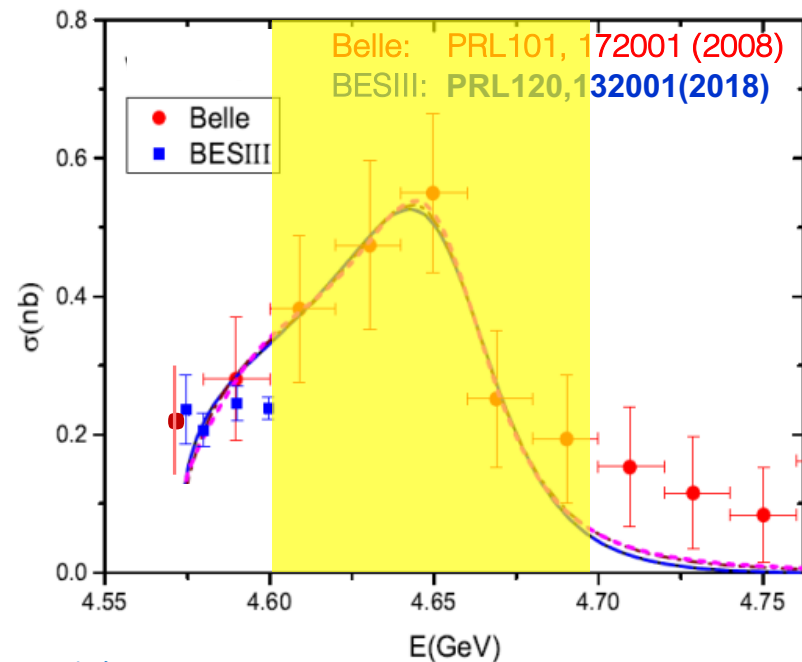


Data taking in 4.6-4.7 GeV in 2020

- 3.7fb⁻¹ data was accumulated at 4.628, 4.641, 4.661, 4.681 and 4.698GeV in 2020.
- Y(4630) & Y(4660)



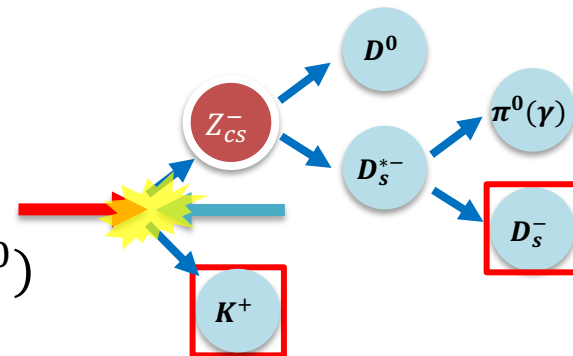
arXiv:1211.6271 and CHARM 2012



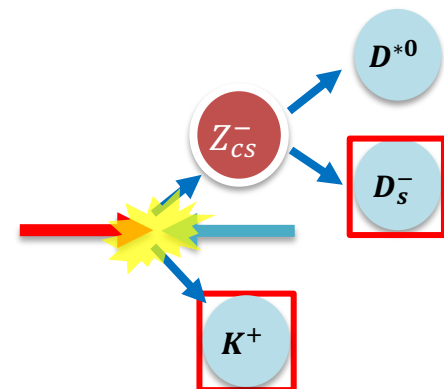
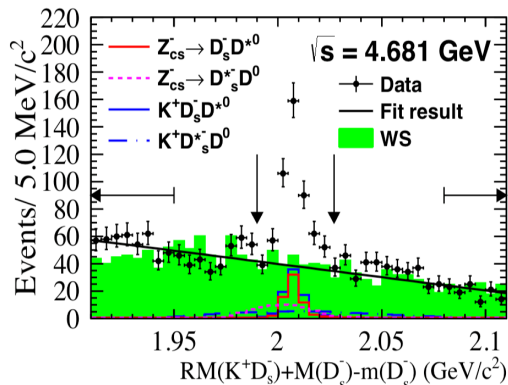
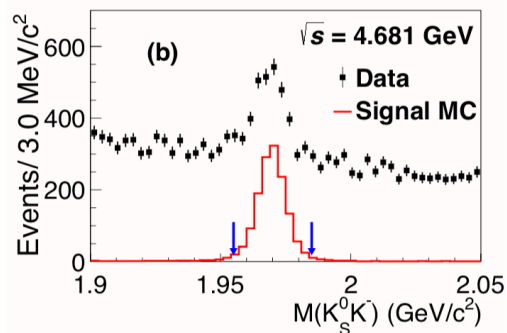
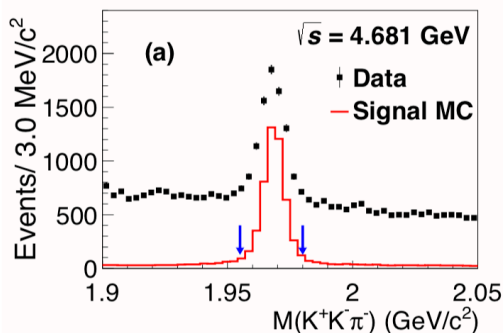
Observation of the $Z_{cs}(3985)^\pm$

arXiv: 2011.07855

- We analyze 3.7fb^{-1} data accumulated at 4.628, 4.641, 4.661, 4.681 and 4.698 GeV in 2020.
- **Partial reconstruction of K^+ and D_s^-**
- Signature in the **recoil mass spectrum of $K^+D_s^-$** to identify the process of $e^+e^- \rightarrow K^+(D_s^-D^{*0} + D_s^{*-}D^0)$



$$e^+e^- \rightarrow K^+ D_s^{*-} D^0$$

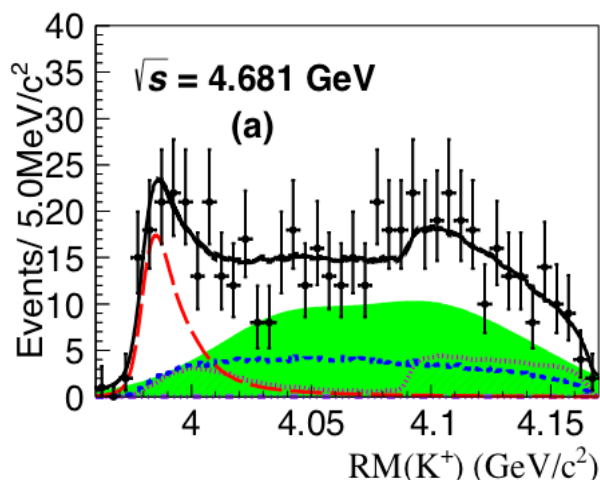
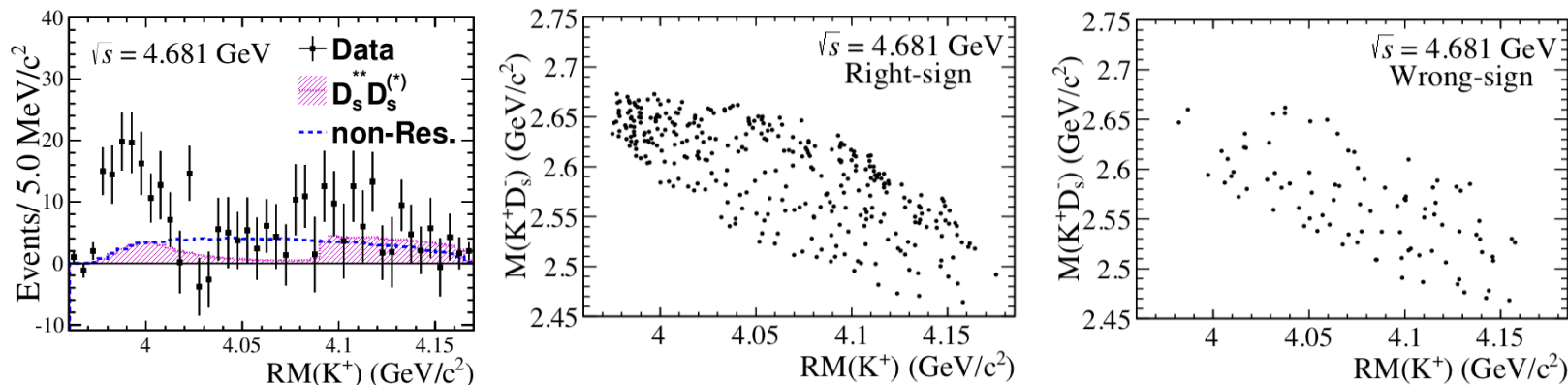


$$e^+e^- \rightarrow K^+ D_s^- D^{*0}$$

Observation of the $Z_{cs}(3985)^\pm$

arXiv: 2011.07855

- Data driven background description: wrong Sign (WS) combination of D_s^- and K^-
- Conventional charmed mesons can not describe the enhancement below 4.0 GeV/c² at 4.681 GeV



- Assume the structure as a $D_s^- D^{*0} / D_s^{*-} D^0$ resonance, denoting it as the $Z_{cs}(3985)^-$.
- A fit of $J^P=1^+$ S-wave Breit-Wigner with mass dependent width returns:

$$m = 3985.2^{+2.1}_{-2.0} \pm 1.7 \text{ MeV}/c^2$$

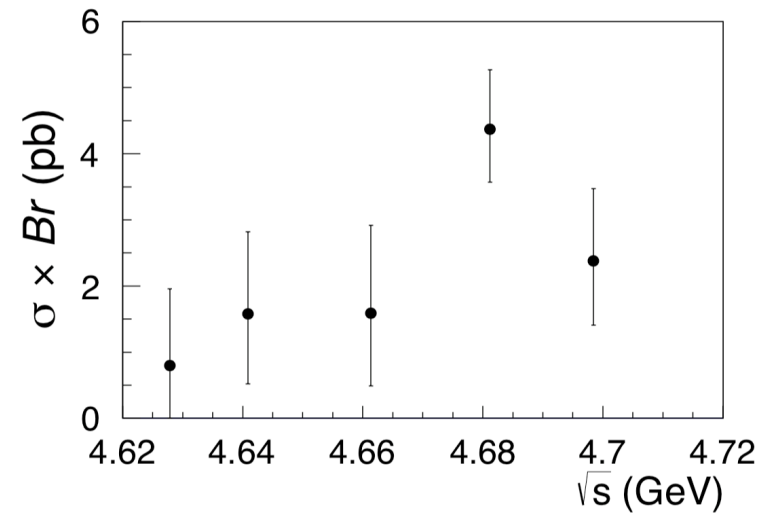
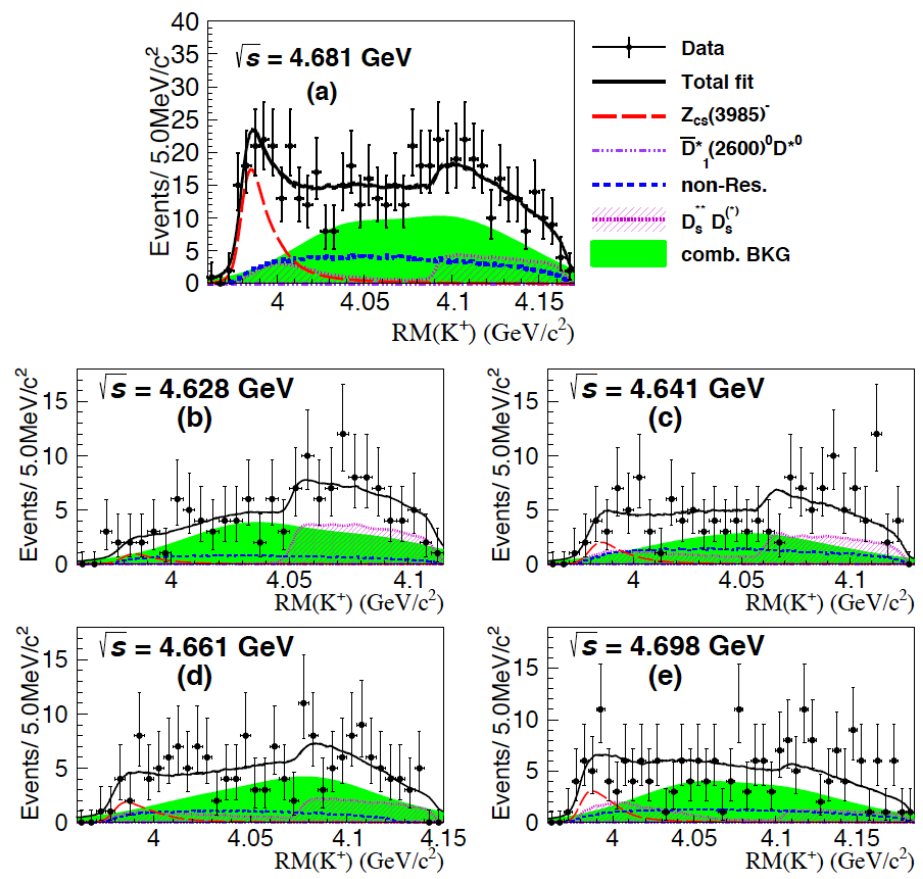
$$\Gamma = 13.8^{+8.1}_{-5.2} \pm 4.9 \text{ MeV}$$
- Global significance: $>5.3 \sigma$

First candidate of the hidden-charm tetraquark with strangeness

Cross sections of the $Z_{cs}(3985)^\pm$ production

arXiv: 2011.07855

- Simultaneous fit to the five energy points



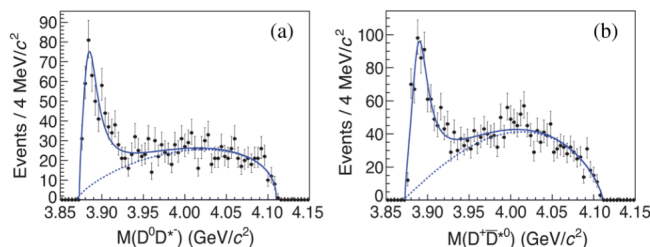
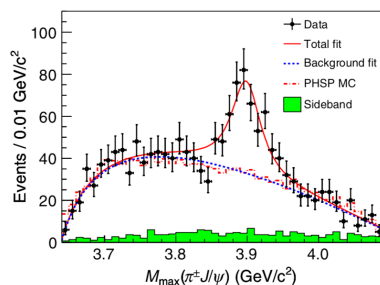
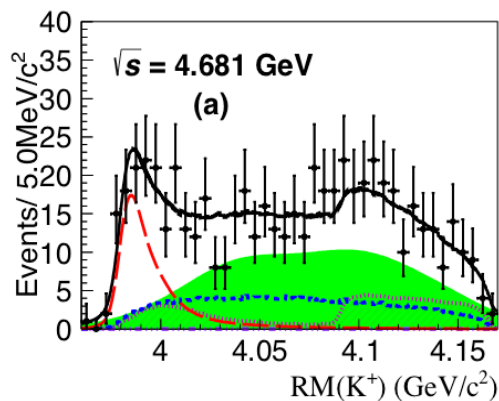
- Largest cross sections around 4.681 GeV

The $Z_{cs}(3985)^\pm$ and $Z_c(3900)^\pm$

1643/pb data @4.681 GeV

525/pb data @4.26 GeV

	$Z_{cs}(3985)^\pm$	$Z_c(3900)^\pm$	$Z_c(3885)^\pm$
Mass (MeV/c ²)	$3985.2^{+2.1}_{-2.0} \pm 1.7$	$3899.0 \pm 3.6 \pm 4.9$	$3883.9 \pm 1.5 \pm 4.2$
Width (MeV)	$13.8^{+8.1}_{-5.2} \pm 4.9$	$46 \pm 10 \pm 26$	$24.8 \pm 3.3 \pm 11.0$
$\sigma^{Born} \cdot \mathfrak{B}$ (pb)	$4.4^{+0.9}_{-0.8} \pm 1.4$	$13.5 \pm 2.1 \pm 4.8$	$83.5 \pm 6.6 \pm 22.0$



two general comments about charm-tau factory program

- $J/\psi K^\pm$ resonances:
 $Z_c(3900)$ analogue?
 $Z_c(3900)^+ = (c\bar{c}u\bar{d})$; $d \rightarrow s$: $(c\bar{c}u\bar{s}) \sim D_s \bar{D}^*$
 no natural molecular binding,
 so if discovered, would indicate
 Tq or a novel mechanism

from Marek Karliner

$Z_{cs}(3985)$

$Z_c(3900)$

$K^- Z_{cs}^+$	$\bar{K}^0 Z_{cs}^0$	$K^0 \bar{Z}_{cs}^0$	$K^+ Z_{cs}^-$
1/4	1/4	1/4	1/4

$\pi^- Z_c^+$	$\pi^0 Z_c^0$	$\pi^+ Z_c^-$
1/3	1/3	1/3

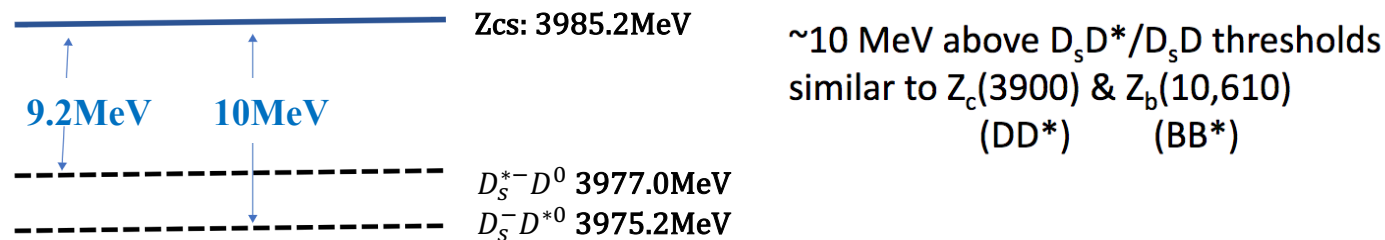
neutral/charged = 1

neutral/charged = 1/2

SU(3) partner of $Z_c(3900)$?

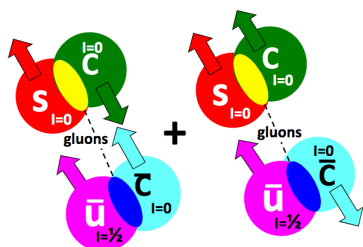
Interpretation on the nature of $Z_{cs}(3985)^\pm$

- Various interpretations are possible for the structure
 - Tetraquark state
 - Molecule
 - $D_{s2}^*(2573)^+ D_s^{*-}$ threshold kinematic effects (Re-scattering, Reflection, Triangle singularity)
 - Mixture of molecular and tetraquark

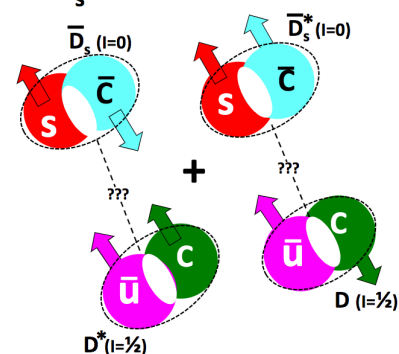


arXiv:2011.08501
 arXiv:2011.08628
 arXiv:2011.08656
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 arXiv:2011.09404
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 arXiv:2011.10959
 arXiv:2011.11488
 arXiv:2011.12230
 arXiv:2011.12326
 arXiv: 2011.13013
 arXiv: 2011.13425
 arXiv: 2011.14313
 arXiv: 2011.14517

diquark-antidiquark?



$D^* \bar{D}_s + cc$ molecule?



Search for $Z_c^{(')\dagger} \rightarrow \rho^+ \eta_c$

PRD 100, 111102(R) (2019)

- Search for new decay mode of $Z_c(3900)$ and $Z_c(4020)$
- The ratios of $Z_c^{(')\dagger} \rightarrow \rho \eta_c$ to $Z_c^{(')\dagger} \rightarrow \pi J/\psi(\pi h_c)$ may discriminate **the tetra-quark and molecule models**.

$$R_z = \frac{B(Z_c \rightarrow \rho \eta_c)}{B(Z_c \rightarrow \pi J/\psi)}$$

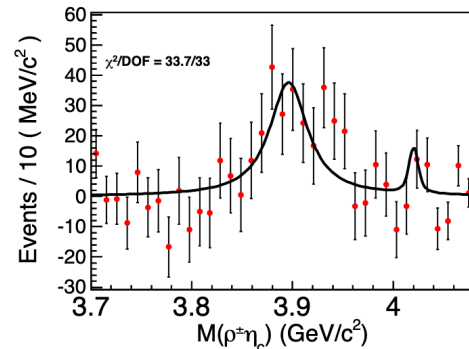
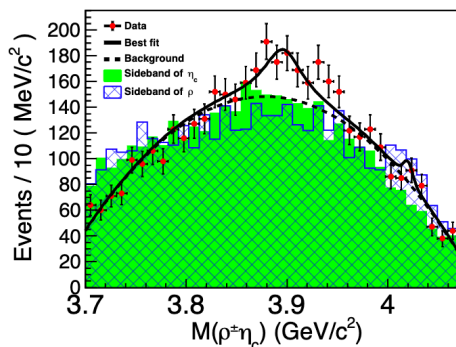
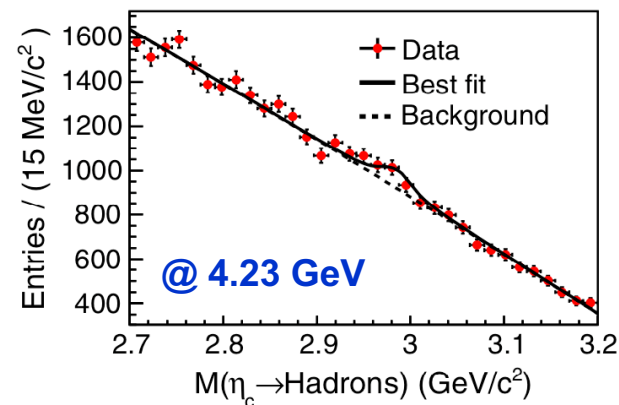
$$R_{z'} = \frac{B(Z_c' \rightarrow \rho \eta_c)}{B(Z_c' \rightarrow \pi h_c)}$$

Date sets:

- $\sim 4 \text{ fb}^{-1}$ data set distributed at $\sqrt{s} = 4.23, 4.26, 4.36, 4.40, 4.60 \text{ GeV}$

Strategy of this analysis:

- Start with looking for $e^+e^- \rightarrow \pi^+\pi^-\pi^0\eta_c, \eta_c \rightarrow 9$ hadronic decays
- Strong evidence of $e^+e^- \rightarrow \pi Z_c, Z_c \rightarrow \rho \eta_c$ is observed at $\sqrt{s} = 4.23$, statistical significance is 4.3σ . (3.9σ including systematics)
- $e^+e^- \rightarrow \pi Z_c', Z_c' \rightarrow \rho \eta_c$ is not seen in all data sets.



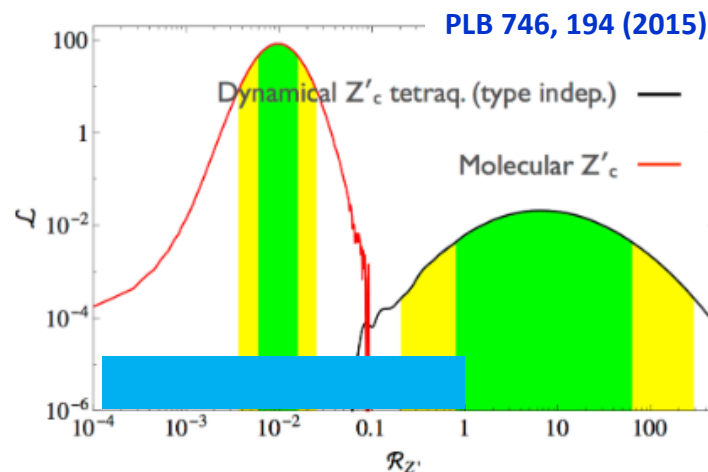
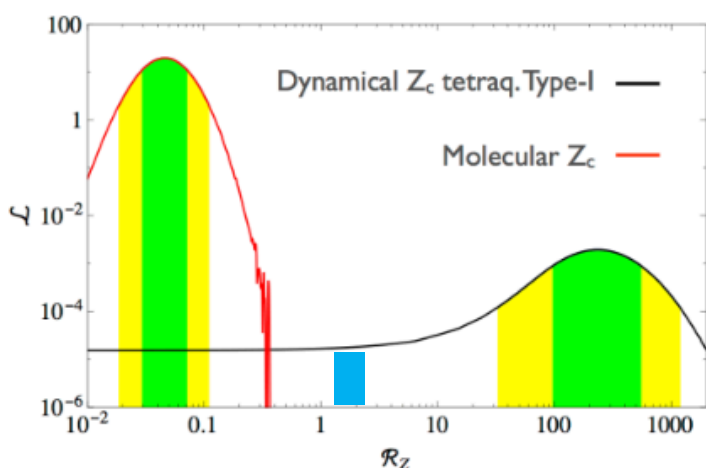
@ 4.23 GeV

Evidence for $Z_c(3900)^+ \rightarrow \rho^+ \eta_c$

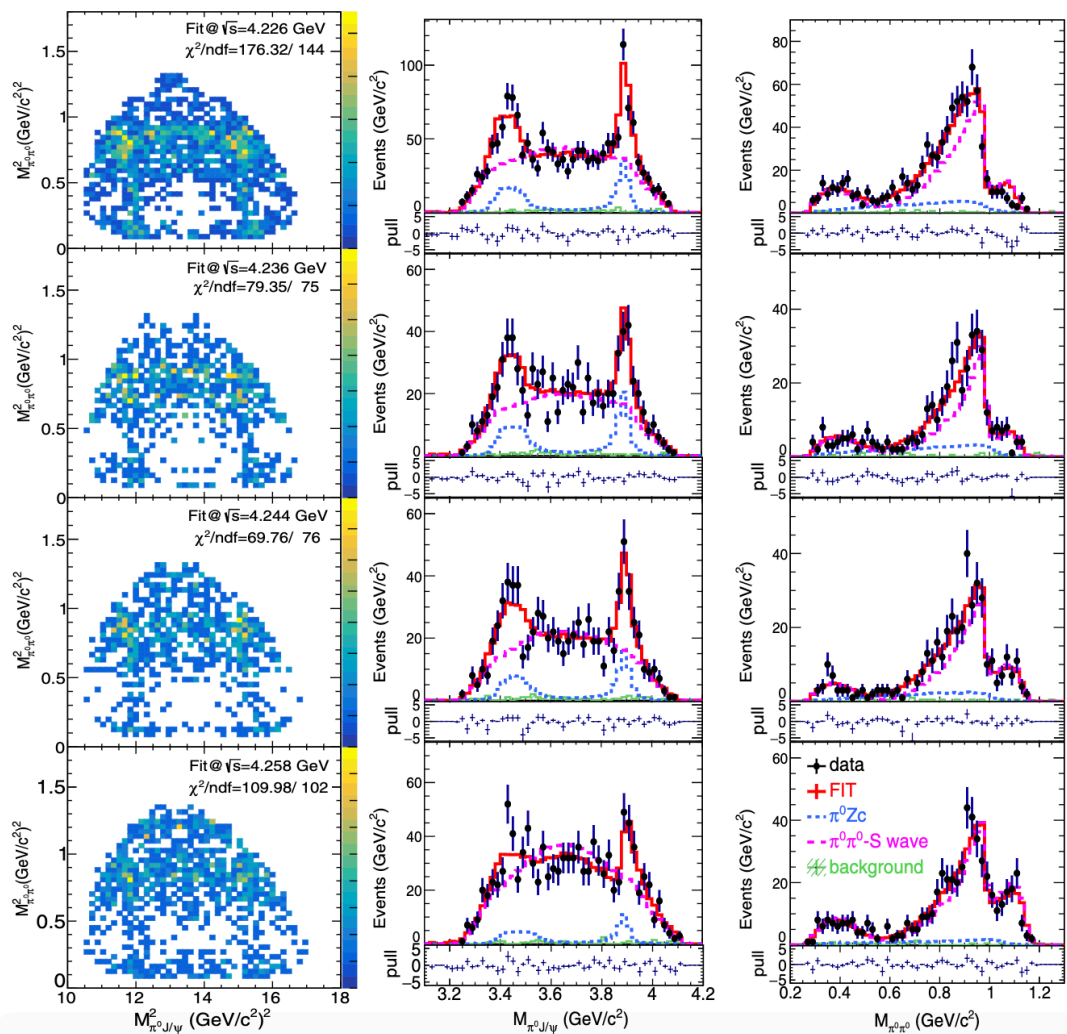


PRD 100, 111102(R) (2019)

Ratio	Measurement	Tetraquark	Molecule
$R_{Z_c(3900)}$	2.3 ± 0.8 [29]	230^{+330}_{-140} [12]	$0.046^{+0.025}_{-0.017}$ [12]
		$0.27^{+0.40}_{-0.17}$ [12]	1.78 ± 0.41 [17]
		0.66 [13]	6.84×10^{-3} [18]
		0.56 ± 0.24 [14]	0.12 [19]
		0.95 ± 0.40 [15]	
		1.08 ± 0.88 [16]	
		1.28 ± 0.37 [17]	
		1.86 ± 0.41 [17]	
$R_{Z_c(4020)}$	< 1.2 [4]	$6.6^{+56.8}_{-5.8}$ [12]	$0.010^{+0.006}_{-0.004}$ [12]



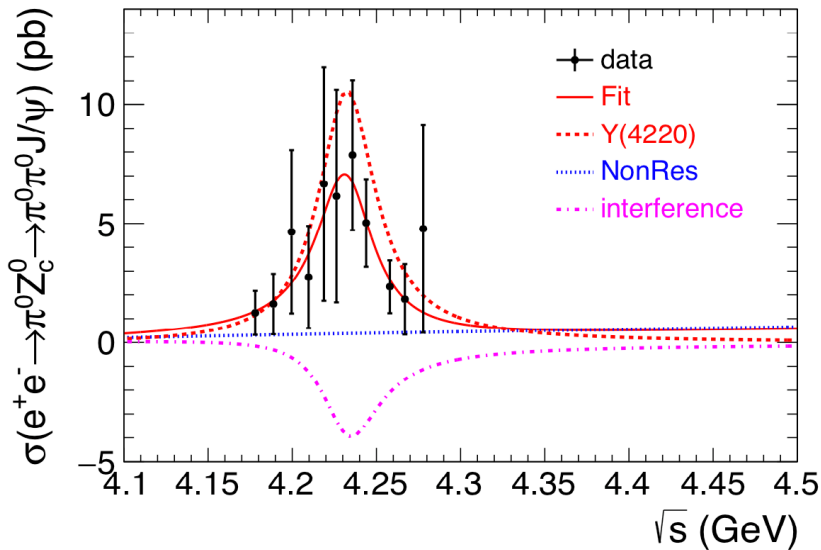
- BESIII measurement of $R_{Z_c(3900)}$ is closer to tetraquark model overall.
- Molecule calculation is highly model dependent.
- Inconsistent with hadron-charmonium model.



- Simultaneous PWA fit of $e^+e^- \rightarrow \pi^0\pi^0 J/\psi$ to the four energy points
- The spin-parity of $Z_c(3900)^0$ is determined to be 1^+
- The nominal fit includes the intermediate process $\sigma J/\psi$, $f(980)J/\psi$, $f(1370)J/\psi$ and $\pi^0 Z_c(3900)^0$.
- Mass and width of $Z_c(3900)^0$ is measured:
 - $M(Z_c(3900)^0) = (3893.0 \pm 2.3 \pm 19.9) \text{ MeV}/c^2$,
 - $\Gamma(Z_c(3900)^0) = (44.2 \pm 5.4 \pm 9.1) \text{ MeV}$.

Cross section of $e^+e^- \rightarrow \pi^0 Z_c(3900)^0$

PRD 102, 012009 (2020)



Parameters	Solution I	Solution II
$p_0 (c^2/\text{MeV})$	0.0 ± 11.3	
p_1	$(1.8 \pm 1.9) \times 10^{-2}$	
$M(R) (\text{MeV}/c^2)$	4231.9 ± 5.3	
$\Gamma_{\text{tot}}(R) (\text{MeV})$	41.2 ± 16.0	
$\Gamma_{ee} \mathcal{B}_{R \rightarrow \pi^0 Z_c(3900)^0} (\text{eV})$	0.53 ± 0.15	0.22 ± 0.25
$\phi(R)$	$(-103.9 \pm 33.9)^\circ$	$(112.7 \pm 43.0)^\circ$

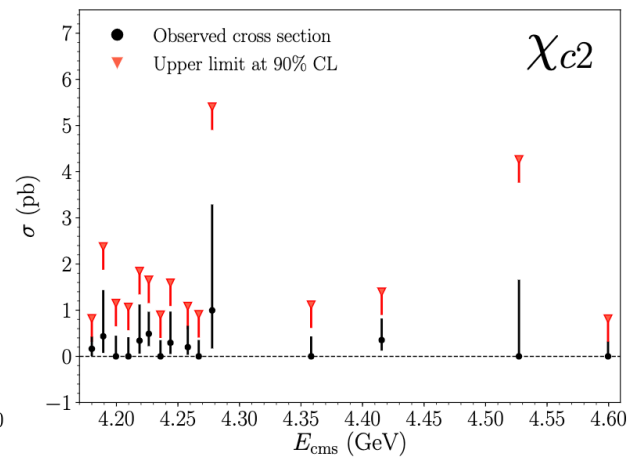
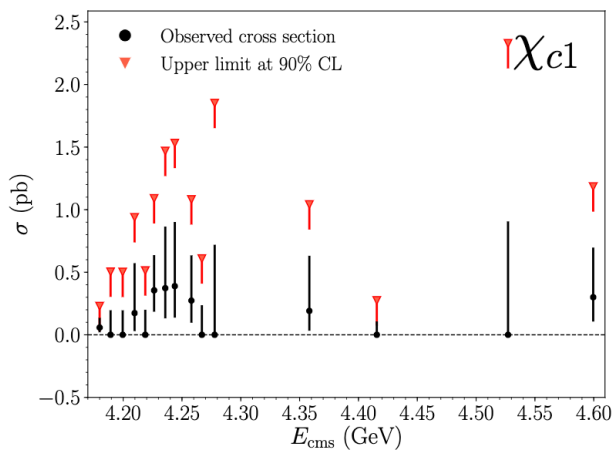
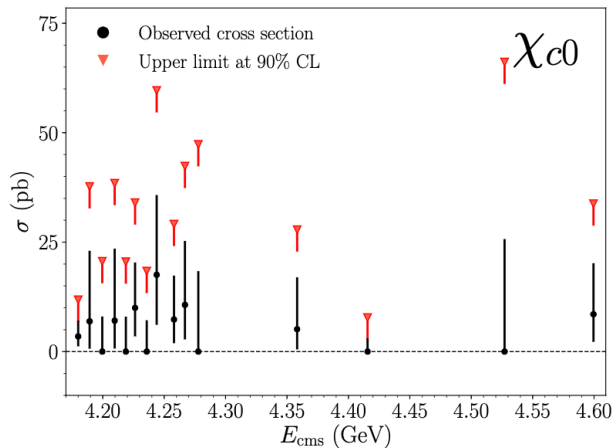
- $Z_c(3900)^0$ resonance parameters are fixed to the results of the previous four-energy-point fit
- The Born cross section of $e^+e^- \rightarrow \pi^0 Z_c(3900)^0 \rightarrow \pi^0 \pi^0 J/\psi$ is extracted.
- Clear structure around 4.2 GeV is observed
 - $M = (4231.9 \pm 5.3 \pm 4.9) \text{ MeV}/c^2$,
 - $\Gamma = (41.2 \pm 16.0 \pm 16.4) \text{ MeV}$.
- Compatible with the Y(4220) line shape
- Indication of correlation between the production of the Y(4220) and $Z_c(3900)$.

Search for $Z_c^+ \rightarrow \pi^+ \chi_{cJ}$



arXiv: 2012.02682

- Belle reported the results of $Z_c(4050)^+$ and $Z_c(4250)^+$ in $\bar{B}^0 \rightarrow K^- Z_c^+, Z_c^+ \rightarrow \pi^+ \chi_{c1}$, while BaBar did not confirm them
- BESIII studies $e^+e^- \rightarrow \pi^+\pi^-\chi_{cJ}, \chi_{cJ} \rightarrow \gamma J/\psi$ from 4.178 GeV to 4.600 GeV
- None of the processes are observed and upper limits of the production cross sections are determined
- Hence, they can be the upper limits of the product cross sections of $e^+e^- \rightarrow \pi^- Z_c(4050)^+ + c.c., Z_c(4050)^+ \rightarrow \pi^+ \chi_{cJ}$

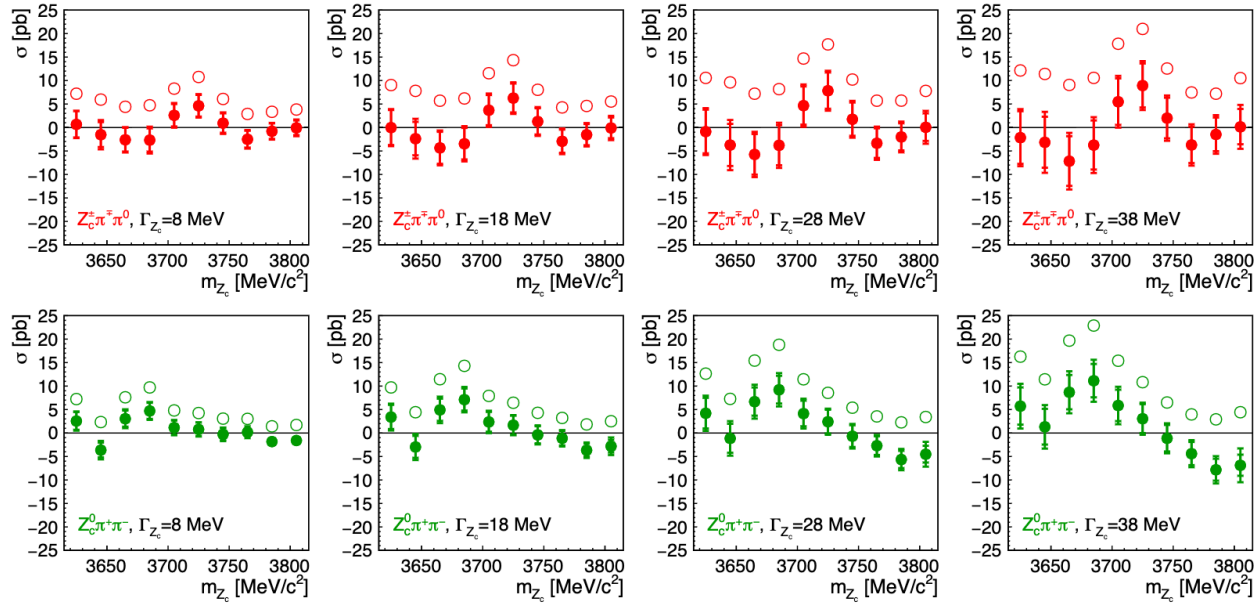
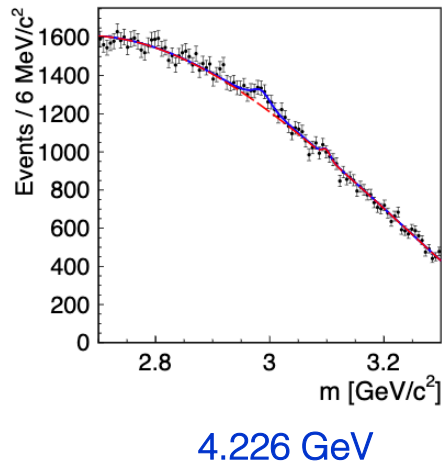


Search for $Z_c \rightarrow \pi \eta_c$

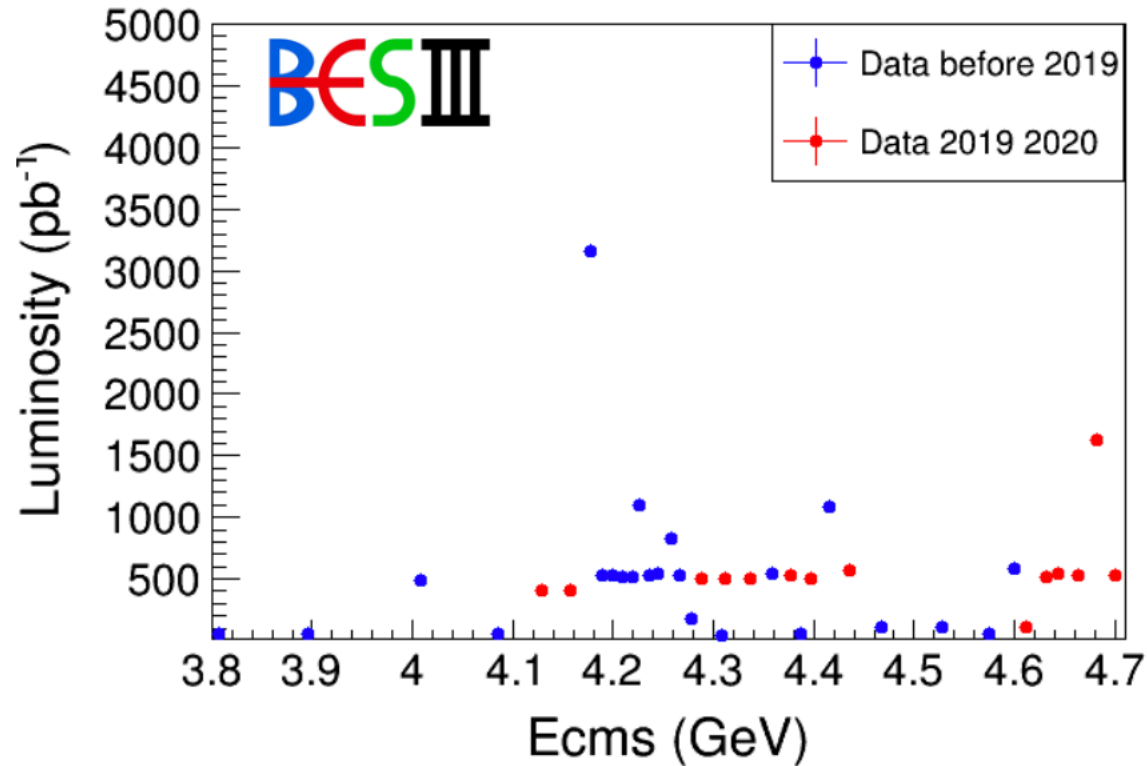
arXiv:2010.14415

- LHCb reported an evidence of $Z_c^+(4100) \rightarrow \pi^+ \eta_c$ in $\bar{B}^0 \rightarrow K^- Z_c^+(4100)$ *LHCb, EPJ C78, 1019 (2018)*
- Studies of $e^+e^- \rightarrow \pi^+ \pi^- \pi^0 \eta_c, \pi^+ \pi^- \eta_c, \gamma \pi^+ \pi^- \eta_c$ at 6 energy points from 4.178 to 4.600 GeV
- 16 hadronic η_c channels are reconstructed
- Only evidence of $e^+e^- \rightarrow \pi^+ \pi^- \pi^0 \eta_c$ @ 4.226 GeV (4.1σ)
- Different mass and width assumptions in the vicinity of $D\bar{D}$ mass are tested for $Z_c^+ \rightarrow \pi^+ \eta_c$ and $Z_c^0 \rightarrow \pi^0 \eta_c$ in $e^+e^- \rightarrow \pi^+ \pi^- \pi^0 \eta_c$ at 4.226 GeV and found to be not significant

$Z_c(4100)^-$
 $M = 4096 \pm 20_{-22}^{+18}$ MeV
 $\Gamma = 152 \pm 58_{-35}^{+60}$ MeV
 $J^P = 0^+ / 1^-$



More XYZ data set to be analyzed

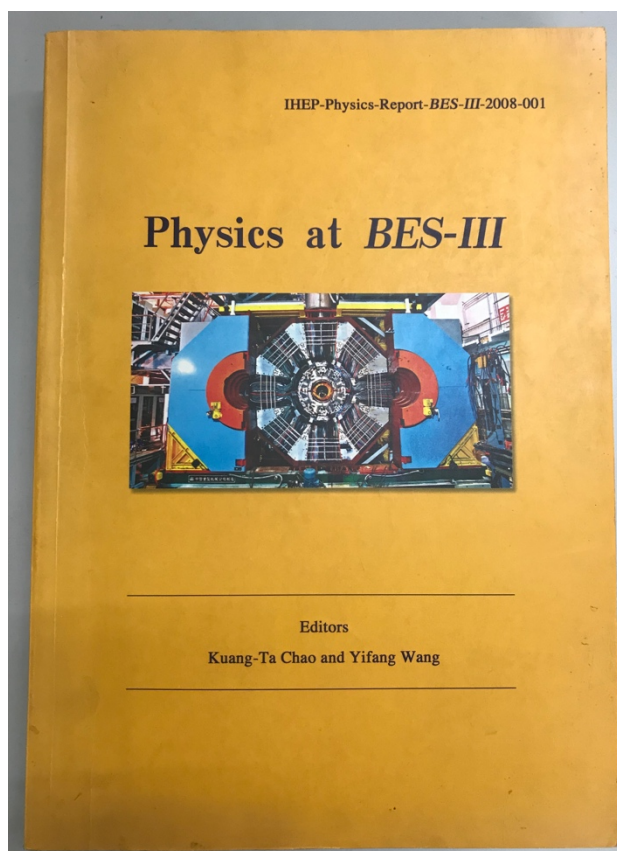


- Global descriptions of the Z_c states at different energy points in the same mode
 - ✓ $\pi J/\psi$, $\pi\psi(3686)$, πh_c , $D^*D^{(*)}$, ...
- Couple channel analyses of the above modes
- Synergies with LHCb



BESIII Physics

Chinese Physics C Vol. 44, No. 4 (2020)



Future Physics Programme of BESIII*

Abstract: There has recently been a dramatic renewal of interest in hadron spectroscopy and charm physics. This renaissance has been driven in part by the discovery of a plethora of charmonium-like XYZ states at BESIII and B factories, and the observation of an intriguing proton-antiproton threshold enhancement and the possibly related $\chi(1835)$ meson state at BESIII, as well as the threshold measurements of charm mesons and charm baryons. We present a detailed survey of the important topics in tau-charm physics and hadron physics that can be further explored at BESIII during the remaining operation period of BEPCII. This survey will help in the optimization of the data-taking plan over the coming years, and provides physics motivation for the possible upgrade of BEPCII to higher luminosity.

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Int. J. Mod. Phys. A 24, S1-794 (2009)
[arXiv:0809.1869 [hep-ex]].

Chin. Phys. C 44, 040001 (2020)
doi:10.1088/1674-1137/44/4/040001
[arXiv:1912.05983 [hep-ex]].

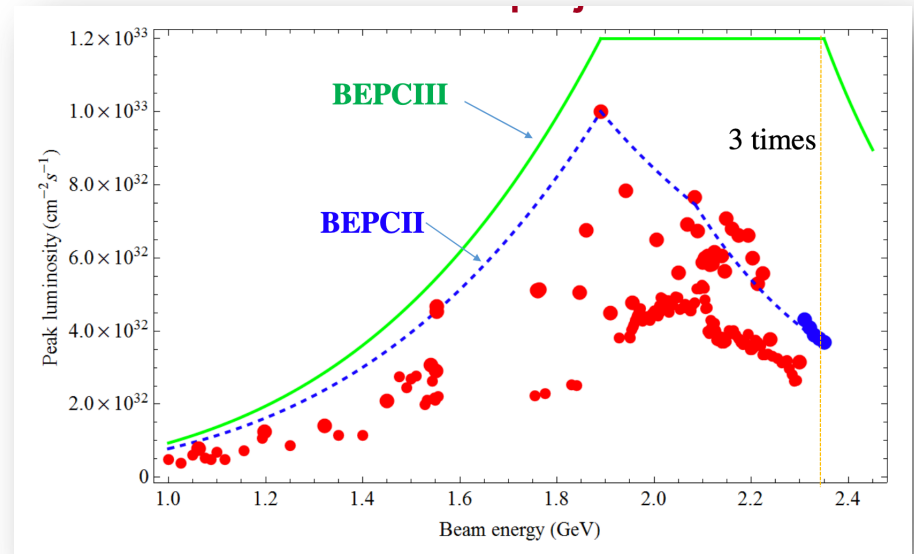
Table 7.1: List of data samples collected by BESIII/BEPCII up to 2019, and the proposed samples for the remainder of the physics program. The most right column shows the number of required data taking days in current (T_C) or upgraded (T_U) machine. The machine upgrades include top-up implementation and beam current increase.

Energy	Physics motivations	Current data	Expected final data	T_C / T_U
1.8 - 2.0 GeV	R values Nucleon cross-sections	N/A	0.1 fb^{-1} (fine scan)	60/50 days
2.0 - 3.1 GeV	R values Cross-sections	Fine scan (20 energy points)	Complete scan (additional points)	250/180 days
J/ψ peak	Light hadron & Glueball J/ψ decays	3.2 fb^{-1} (10 billion)	3.2 fb^{-1} (10 billion)	N/A
$\psi(3686)$ peak	Light hadron & Glueball Charmonium decays	0.67 fb^{-1} (0.45 billion)	4.5 fb^{-1} (3.0 billion)	150/90 days
$\psi(3770)$ peak	D^0/D^\pm decays	2.9 fb^{-1}	20.0 fb^{-1}	610/360 days
3.8 - 4.6 GeV	R values XYZ /Open charm	Fine scan (105 energy points)	No requirement	N/A
4.180 GeV	D_s decay XYZ /Open charm	3.2 fb^{-1}	6 fb^{-1}	140/50 days
4.0 - 4.6 GeV	XYZ /Open charm Higher charmonia cross-sections	16.0 fb^{-1} at different \sqrt{s}	30 fb^{-1} at different \sqrt{s}	770/310 days
4.6 - 4.9 GeV	Charmed baryon/ XYZ cross-sections	0.56 fb^{-1} at 4.6 GeV	15 fb^{-1} at different \sqrt{s}	1490/600 days
4.74 GeV	$\Sigma_c^+ \Lambda_c^-$ cross-section	N/A	1.0 fb^{-1}	100/40 days
4.91 GeV	$\Sigma_c \Sigma_c$ cross-section	N/A	1.0 fb^{-1}	120/50 days
4.95 GeV	Ξ_c decays	N/A	1.0 fb^{-1}	130/50 days

Proposal of the BEPCIII

- Following up with the beam energy and top-up upgrade, we are planning the next generation of BEPCIII (200 million CNY), to be implemented around 2022: the optimized energy is 2.35 GeV with luminosity 3 times higher than BEPCII.

	BEPCII	BEPCIII
Lum. [$10^{33} \text{cm}^{-2} \text{s}^{-1}$] @2.35GeV	0.35	1.2
β_y^* [cm]	1.5	1.35
Bunch current	7.1 mA	7.5 mA
Bunch number	56	120
SR Power [kW]	110	250
$\xi_{y,\text{lum}}$	0.029	0.039
Emittance [nmrad]	138	120
Coupling [%]	0.53	0.40
Bucket Height	0.0069	0.091
$\sigma_{z,0}$ [cm]	1.54	1.24
σ_z [cm]	1.69	1.39
RF voltage	1.6MV	3.5MV



- Major modification
- RF region
 - Vacuum chamber
 - Beam parameters

- It is crucial that different experiments, such as LHCb, BESIII and Belle II, exchange information in the efforts of amplitude analyses
 - ✓ Sharing the knowledge on analysis tools
eg, **TF-PWA** (talks given inside BESIII and LHCb) <https://github.com/jiangyi15/tf-pwa>
 - ✓ Constraints on properties of the hadronic states

A few cases:

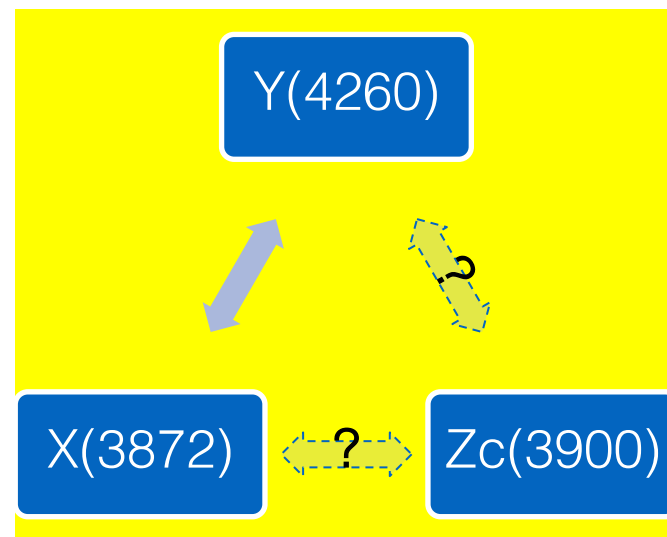
- Z_c/Z_{c_s} productions (e^+e^- annihilations or b-hadron decays) and decays (to open or hidden charm states)

State	Decay modes	Seen by
$Z_c(3900)^{\pm,0}$	$\pi^- J/\psi, (D^* \bar{D})^-$	BESIII, Belle CLEO
$Z_c(4020)^{\pm,0}$	$\pi^- h_c, (D^* \bar{D}^*)^-$	BESIII
$Z_c(4430)^\pm$	$\pi^- \psi(2S)$ $\pi^\pm J/\psi$	Belle, BaBar, LHCb

in $e^+e^- \rightarrow \pi^- Z_c$

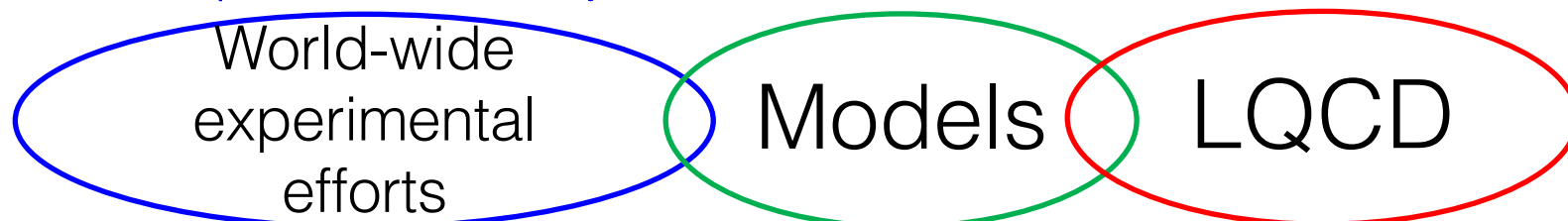
in $e^+e^- \rightarrow \pi^- Z_c$

in $B \rightarrow K Z_c$



- Energy-dependence
- Patterns in productions and decays

Pole properties

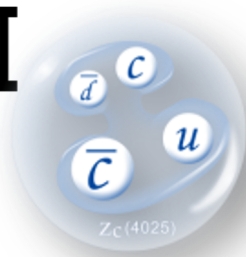


Summary

- BESIII is continuously producing many new results on tetraquark states
 - observation of $Z_{cs}(3985)$ as the first candidate of hidden-charm tetraquark with-strangeness
- Improved understanding of the previous reported Z_c states
- Continuously, more data set will be recorded and new analyses will be publicized ...
- The future BEPCIII with 3x luminosity upgrade enables BESIII to study the tetraquark states with better precisions

Thank you!

谢谢!



The Zc Family at BESIII



State	Mass (MeV/c ²)	Width (MeV)	Decay	Process
$Z_c(3900)^\pm$	$3899.0 \pm 3.6 \pm 4.9$	$46 \pm 10 \pm 20$	$\pi^\pm J/\psi$	$e^+e^- \rightarrow \pi^+\pi^- J/\psi$
$Z_c(3900)^0$	$3894.8 \pm 2.3 \pm 2.7$	$29.6 \pm 8.2 \pm 8.2$	$\pi^0 J/\psi$	$e^+e^- \rightarrow \pi^0\pi^0 J/\psi$
$Z_c(3885)^\pm$	$3883.9 \pm 1.5 \pm 4.2$ Single D tag	$24.8 \pm 3.3 \pm 11.0$ Single D tag	$(D\bar{D}^*)^\pm$	$e^+e^- \rightarrow (D\bar{D}^*)^\pm \pi^\mp$
	$3881.7 \pm 1.6 \pm 2.1$ Double D tag	$26.6 \pm 2.0 \pm 2.3$ Double D tag	$(D\bar{D}^*)^\pm$	$e^+e^- \rightarrow (D\bar{D}^*)^\pm \pi^\mp$
$Z_c(3885)^0$	$3885.7^{+4.3}_{-5.7} \pm 8.4$	$35^{+11}_{-12} \pm 15$	$(D\bar{D}^*)^0$	$e^+e^- \rightarrow (D\bar{D}^*)^0 \pi^0$
$Z_c(4020)^\pm$	$4022.9 \pm 0.8 \pm 2.7$	$7.9 \pm 2.7 \pm 2.6$	$\pi^\pm h_c$	$e^+e^- \rightarrow \pi^+\pi^- h_c$
$Z_c(4020)^0$	$4023.9 \pm 2.2 \pm 3.8$	fixed	$\pi^0 h_c$	$e^+e^- \rightarrow \pi^0\pi^0 h_c$
$Z_c(4025)^\pm$	$4026.3 \pm 2.6 \pm 3.7$	$24.8 \pm 5.6 \pm 7.7$	$D^*\bar{D}^*$	$e^+e^- \rightarrow (D^*\bar{D}^*)^\pm \pi^\mp$
$Z_c(4025)^0$	$4025.5^{+2.0}_{-4.7} \pm 3.1$	$23.0 \pm 6.0 \pm 1.0$	$D^*\bar{D}^*$	$e^+e^- \rightarrow (D^*\bar{D}^*)^0 \pi^0$

PRL 119.072001 (2017)

- If Z_c is parameterized with a Flatté-like formula

$$M_{\text{pole}} = 3881.2 \pm 4.2 \pm 52.7 \text{ MeV}, \quad \Gamma_{\text{pole}} = 51.8 \pm 4.6 \pm 36.0 \text{ MeV}$$

$$g_1' = 0.075 \pm 0.006 \pm 0.025 \text{ GeV}^2$$

$$g_2' / g_1' = 27.1 \pm 2.0 \pm 1.9$$

(consistent with the previous published results)

- Born cross section for $e^+e^- \rightarrow Z_c^+ \pi^- + c.c. \rightarrow \pi^+ \pi^- J / \psi$

$$21.8 \pm 1.0 \pm 4.4 \text{ pb at } 4.23 \text{ GeV}$$

$$11.0 \pm 1.2 \pm 5.4 \text{ pb at } 4.26 \text{ GeV}$$

- Search for $e^+e^- \rightarrow Z_c^+(4020) \pi^- + c.c. \rightarrow \pi^+ \pi^- J / \psi$ gives

upper limits at 90% C.L.:

$$<0.9 \text{ pb at } 4.23 \text{ GeV}; \quad <1.4 \text{ pb at } 4.26 \text{ GeV}$$

$$\text{then } \frac{\sigma(e^+e^- \rightarrow Z_c^+(4020) \pi^- + c.c. \rightarrow \pi^+ \pi^- J / \psi)}{\sigma(e^+e^- \rightarrow Z_c^+(3900) \pi^- + c.c. \rightarrow \pi^+ \pi^- J / \psi)} < 4\% \text{ at } 4.23 \text{ GeV}$$

$$<13\% \text{ at } 4.26 \text{ GeV}$$

Further couple channel amplitude analysis is on-going on more energy points.

PRD 96, 032004 (2017)

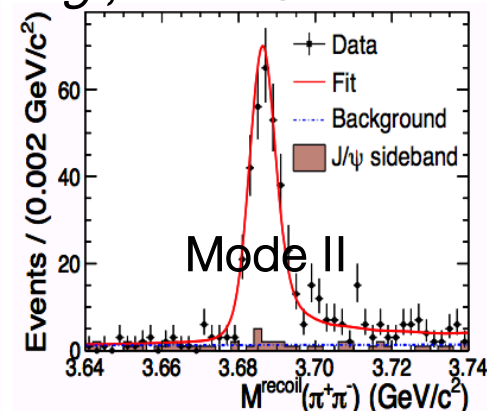
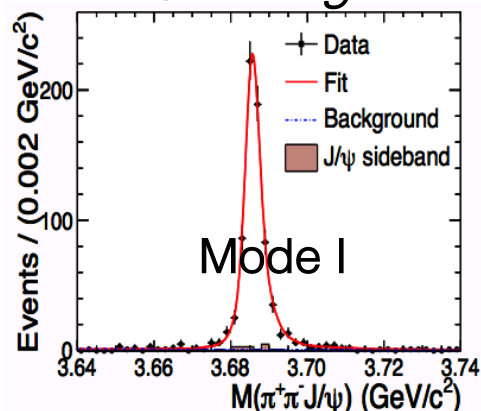
- **Data samples:**
 - 16 energy points from $\sqrt{s}=4.008$ to 4.600 GeV.
 - The total integrated luminosity (L_{int}) is 5.1 fb^{-1} .

- **Reconstructed modes:**

Mode I: $\Psi(3686) \rightarrow \pi^+\pi^-J/\psi$, $J/\psi \rightarrow l^+l^-$ ($l=e/\mu$)

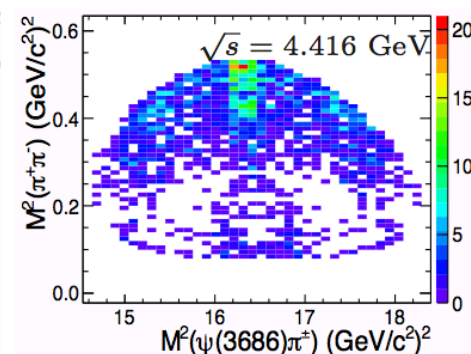
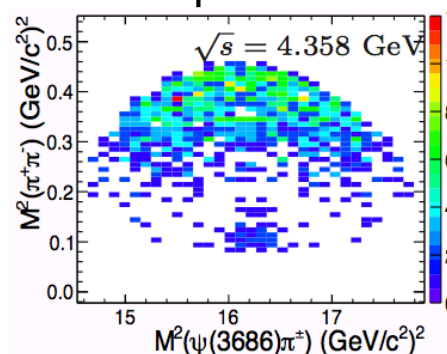
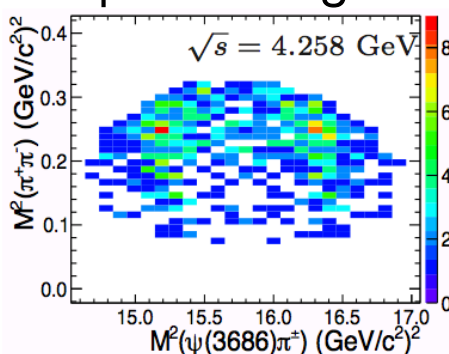
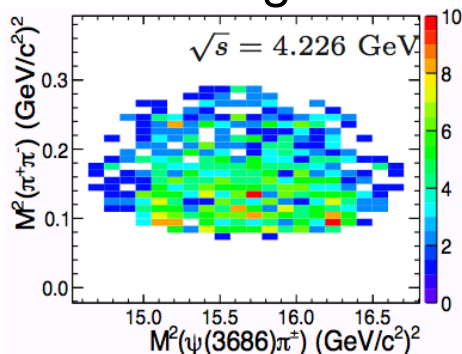
Mode II: $\Psi(3686) \rightarrow \text{neutrals}+J/\psi$,
 $\text{neutrals}=(\pi^0\pi^0, \pi^0, \eta \text{ and } \gamma\gamma)$ $J/\psi \rightarrow l^+l^-$ ($l=e/\mu$)

Clean signals at e.g., 4.416 GeV



Cross section of $e^+e^- \rightarrow \pi^+\pi^-\psi(3686)$ has been measured at 16 energy points from 4.008 to 4.600 GeV, consistent with the reported line shape. (see Zhiyong's talk)

Looking at the Dalitz plots in large data set \rightarrow quite different behaviors



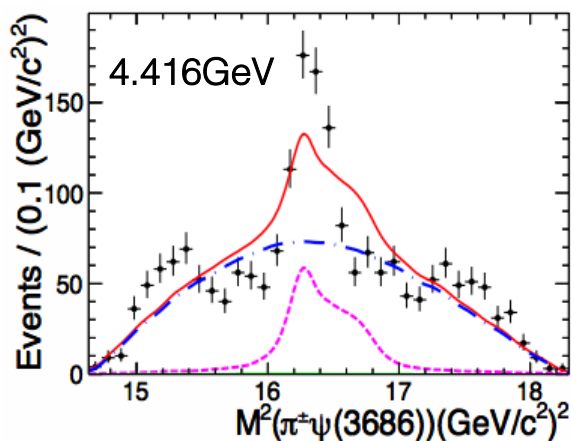
Resonant structure of $\pi^+\psi(3686)$ in $e^+e^- \rightarrow \pi^+\pi^-\psi(3686)$ at 4.416 GeV

PRD 96, 032004 (2017)

- A prominent narrow structure is observed in $\pi\psi(3686)$ mass spectrum for data at $\sqrt{s} = 4.416$ GeV.
- An S-wave Breit-Wigner fit function is performed on the Dalitz plot of $M^2(\pi^+\psi(3686))$ versus $M^2(\pi^-\psi(3686))$

$$\frac{p \cdot q/c^2}{(M_R^2 - x)^2 + M_R^2 \cdot \Gamma^2/c^4} + \frac{p \cdot q/c^2}{(M_R^2 - y)^2 + M_R^2 \cdot \Gamma^2/c^4}$$

- The fit yields a mass of $M=4032.1 \pm 2.4 \text{ MeV}/c^2$ and a width of $\Gamma=26.1 \pm 5.3 \text{ MeV}$, with a significance of 9.2σ



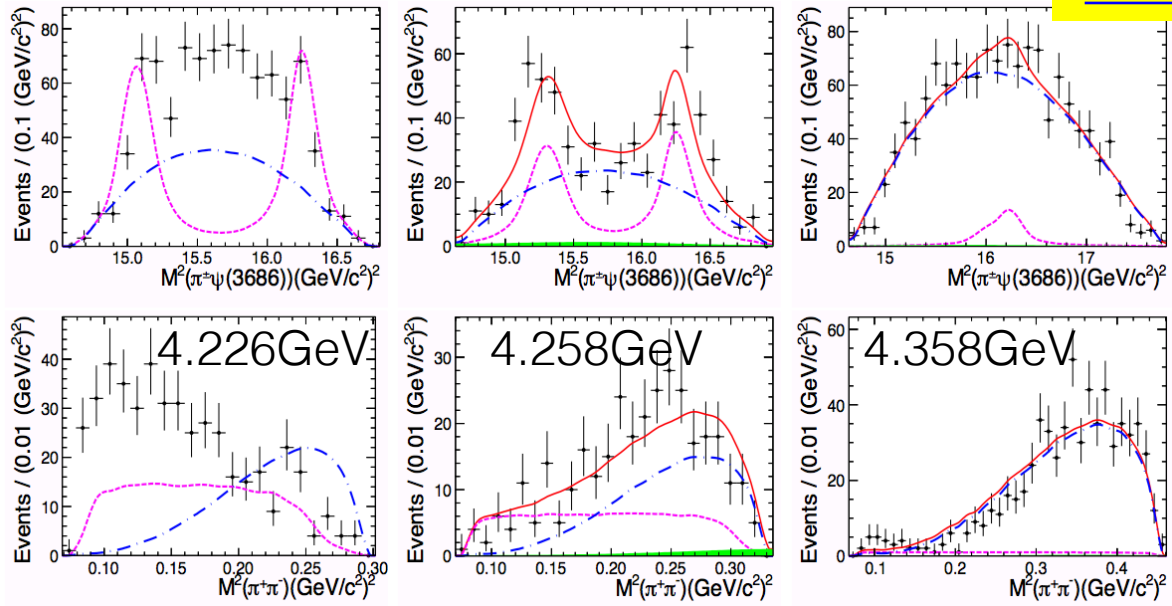
- *Quality of simple fit is not good*
- *A sophisticated amplitude analysis is carrying out*

Check on the resonance structures at other energy points



- Similar fits are carried out to data at $\sqrt{s} = 4.258$ and 4.358 GeV.
- No fit is applied at $\sqrt{s} = 4.226$ GeV due to its different behavior on the Dalitz plot and anomalous spectrum in $M^2(\pi^+\pi^-)$.

PRD 96, 032004 (2017)



- In the fits to data of 4.258 and 4.358 GeV, the $\pi^+\psi(3686)$ resonance parameters are fixed to that at 4.416 GeV. The resonances are confirmed with stat. significances of 9.6σ and 3.6σ at 4.258 and 4.358 GeV, respectively.
- At 4.226 GeV, the resonance structures are close to the kinematic boundary

Study of $e^+e^- \rightarrow \pi^0\pi^0\psi(3686)$

PRD 97, 052001 (2018)

Decay channel:

$$e^+e^- \rightarrow \pi^0\pi^0\psi(3686),$$

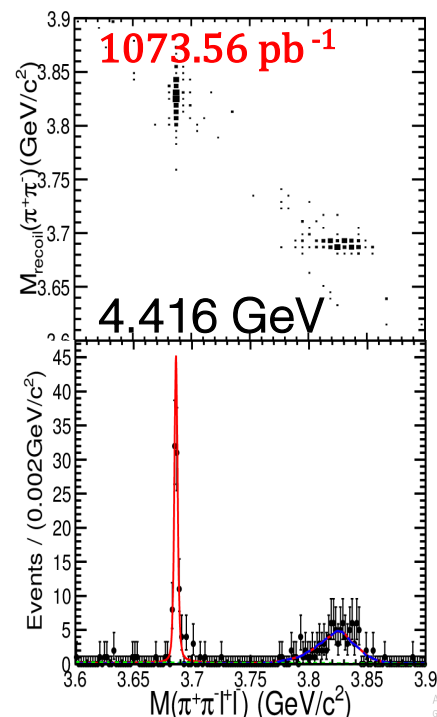
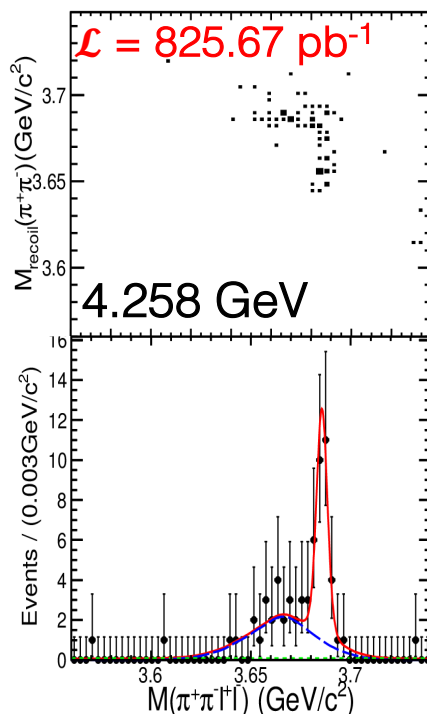
$$\psi(3686) \rightarrow \pi^+\pi^-J/\psi, \quad J/\psi \rightarrow l^+l^- (l = e/\mu).$$

Data sample

- 16 energy point from $\sqrt{s} = 4.008$ to 4.600 GeV.
- The total luminosity(\mathcal{L}): 5.2 fb⁻¹.

Clear Signals in data

Broad bumps are from backgrounds of the charged mode $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$



(a) 4.226 GeV,

$\mathcal{L} = 1091.74 \text{ pb}^{-1}$

(b) 4.258 GeV,

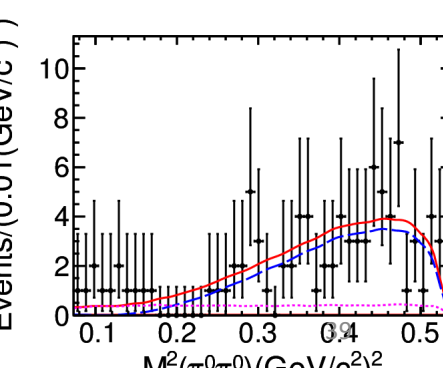
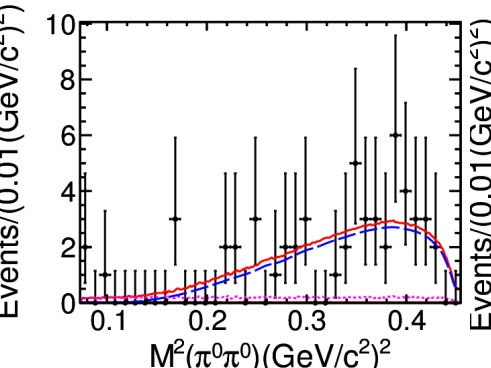
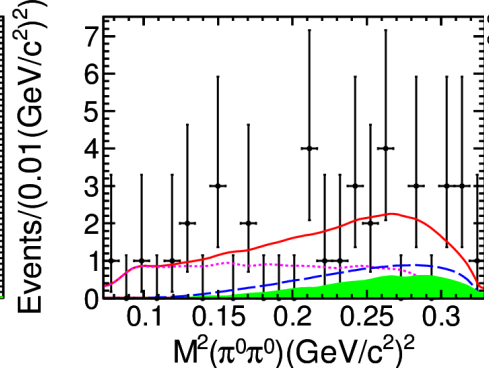
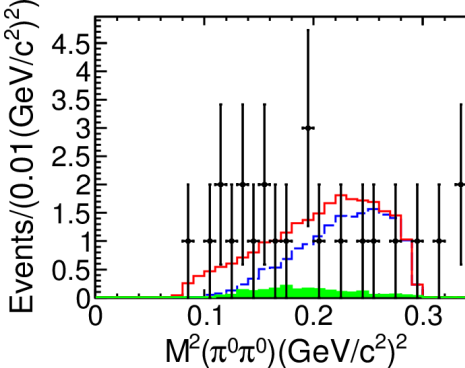
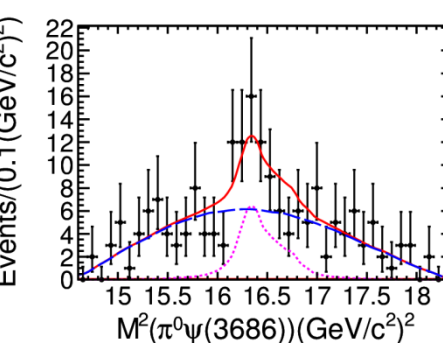
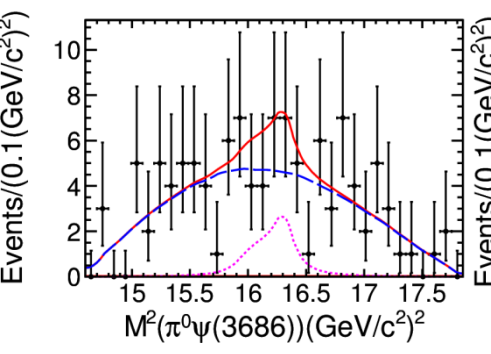
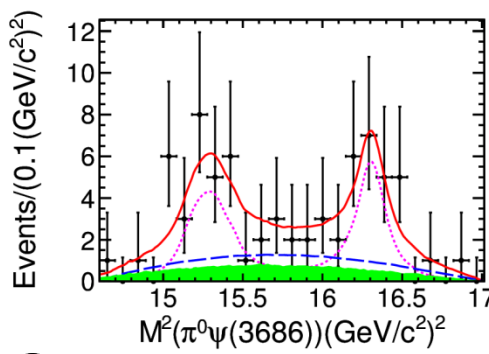
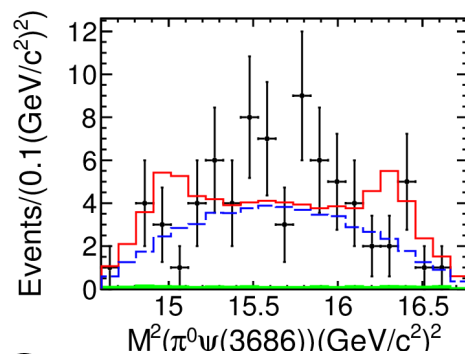
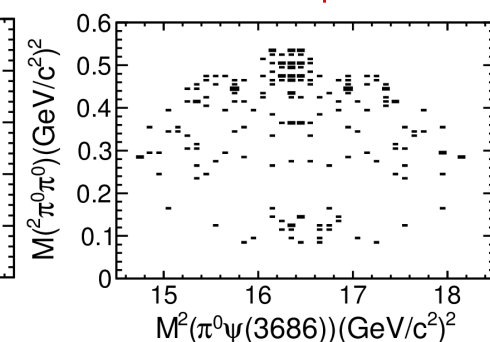
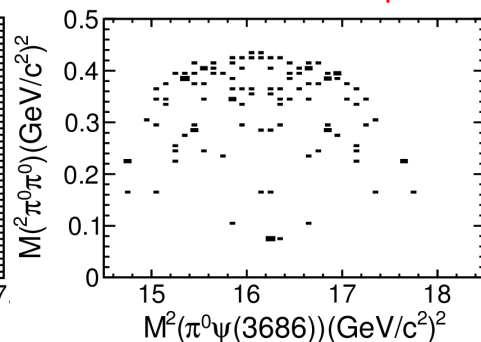
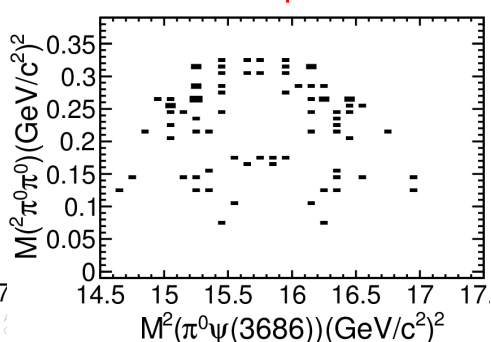
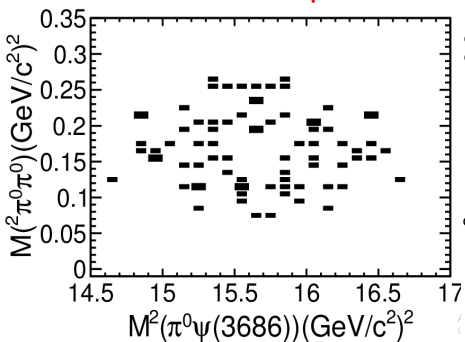
825.67 pb^{-1}

(c) 4.358 GeV,

539.84 pb^{-1}

(d) 4.416 GeV

1073.56 pb^{-1}



Simple fits to the $\pi^0\psi(3686)$ resonance

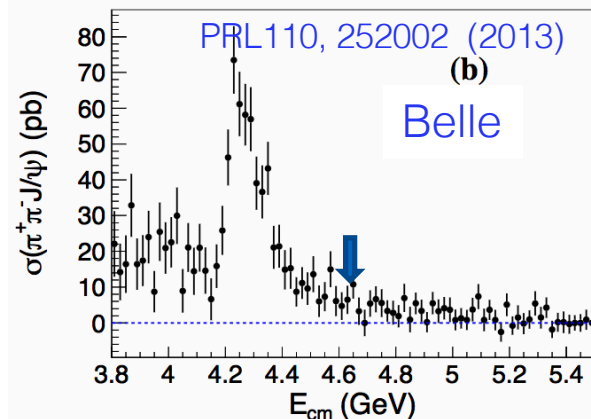
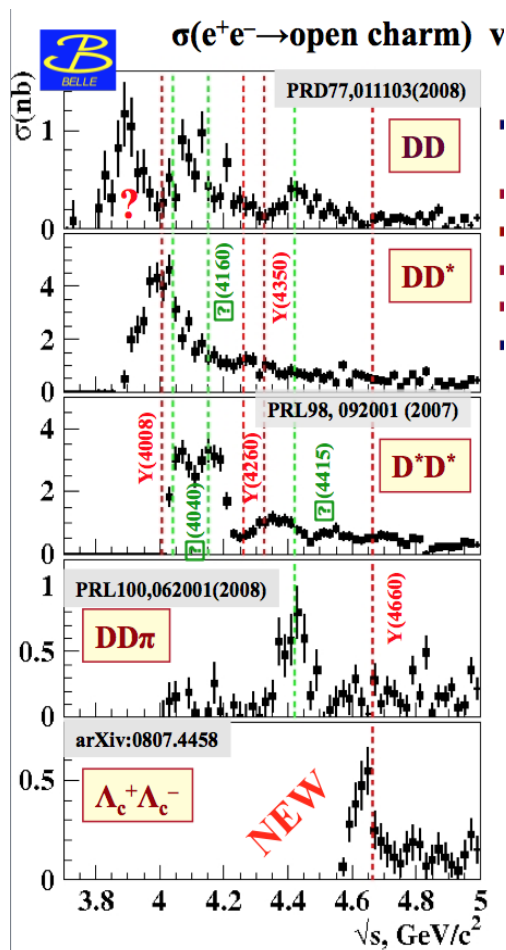
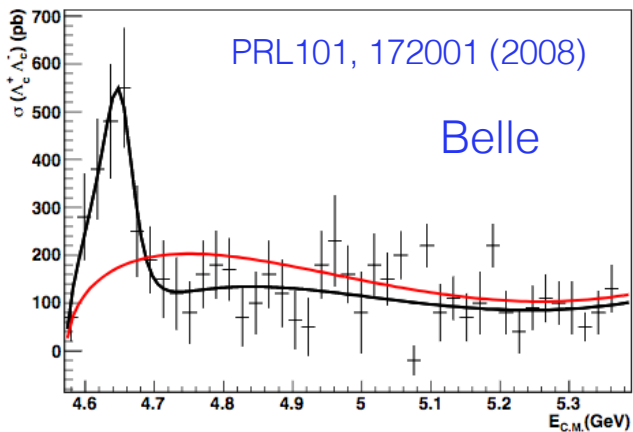
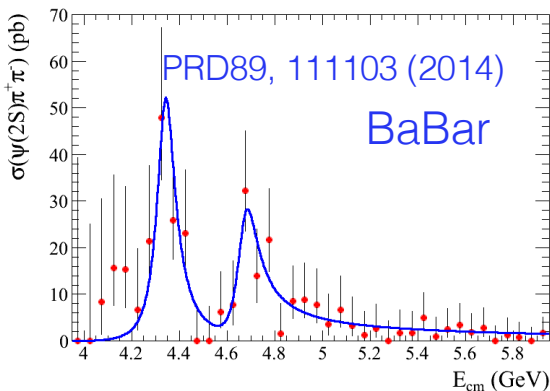
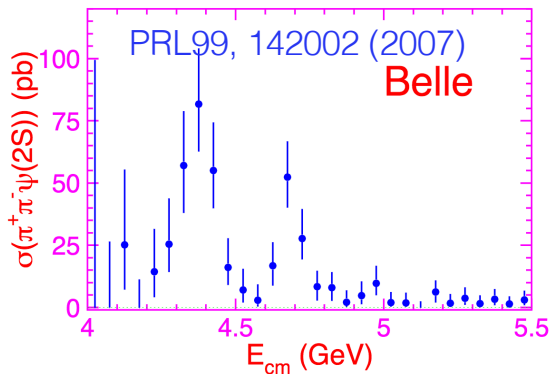
PRD 97, 052001 (2018)

- A possible intermediate state is also observed in the $\pi^0\psi(3686)$ spectrum at 4.416 GeV.
- A 2D fit with a fixed width to charged structure observed in $e^+e^- \rightarrow \pi^+\pi^-\psi(3686)$ is performed on the Dalitz distribution of $M^2(\pi_1^0\psi(3686))$ vs $M^2(\pi_2^0\psi(3686))$.

$$\frac{p_1 \cdot q_1/c^2}{(x - M_R^2)^2 + M_R^2 \cdot \Gamma^2/c^4} + \frac{p_2 \cdot q_2/c^2}{(y - M_R^2)^2 + M_R^2 \cdot \Gamma^2/c^4}$$

- The fit yields a mass (4038.7 ± 6.5) MeV/ c^2 with a significance 6.0σ .
 → consistent with the resonance in the charged mode $\pi^+\psi(3686)$
- Similar fits with fixed width and mass of the $\pi^0\psi(3686)$ resonance are carried out to the data sample at 4.258 GeV and 4.358 GeV
 - the corresponding stat. significances are 3.6σ and 4.5σ , respectively
- $Z_c(3900)$ is not significant in either energy points

The Y(4630)/Y(4660)



$$\frac{\mathcal{B}(Y_B \rightarrow \Lambda_c \bar{\Lambda}_c)}{\mathcal{B}(Y_B \rightarrow \psi(2S)\pi^+\pi^-)} = 25 \pm 7,$$

Phys.Rev.Lett. 104 (2010) 132005

$$\frac{\mathcal{B}(Y_B \rightarrow D^0 D^{*-} \pi^+)}{\mathcal{B}(Y_B \rightarrow \psi(2S)\pi^+\pi^-)} < 10$$

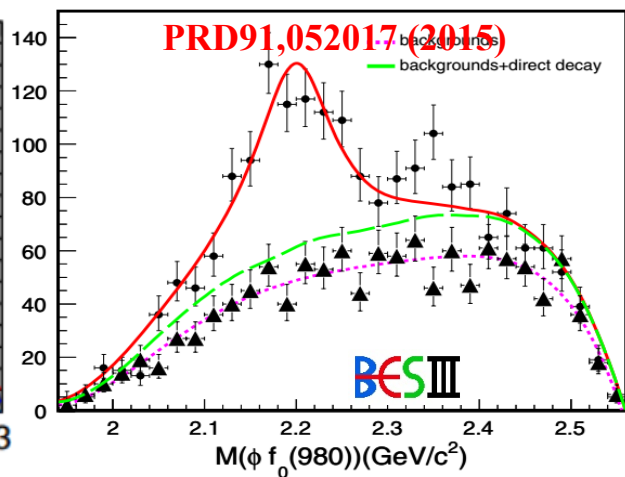
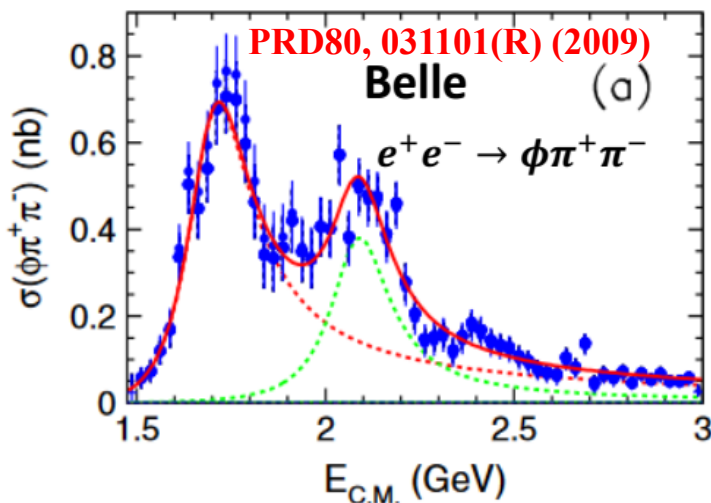
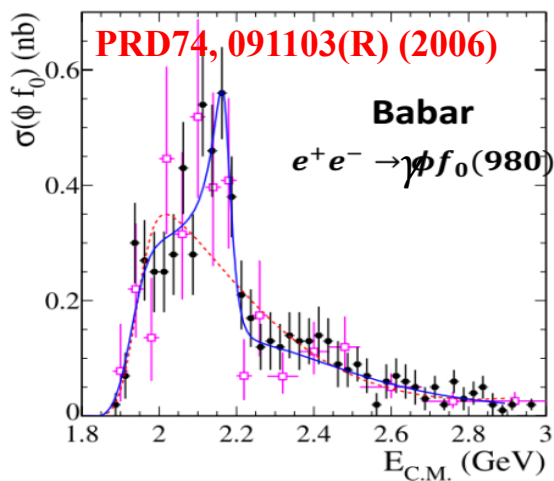
PDG

- Y(4660) baryonic coupling ≥ 10 mesonic coupling (unexpected!)
- Another missing large mesonic decay?
Or Y(4660) is a charmed baryonium?

BESIII Y(2175) and the strangeonium-like Z_S



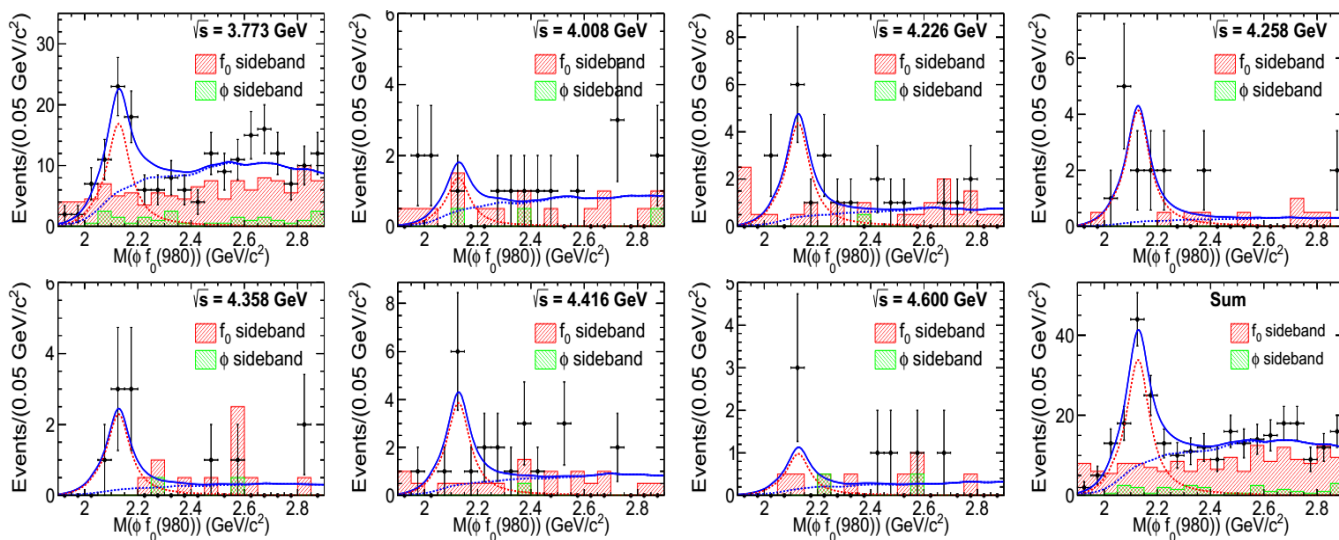
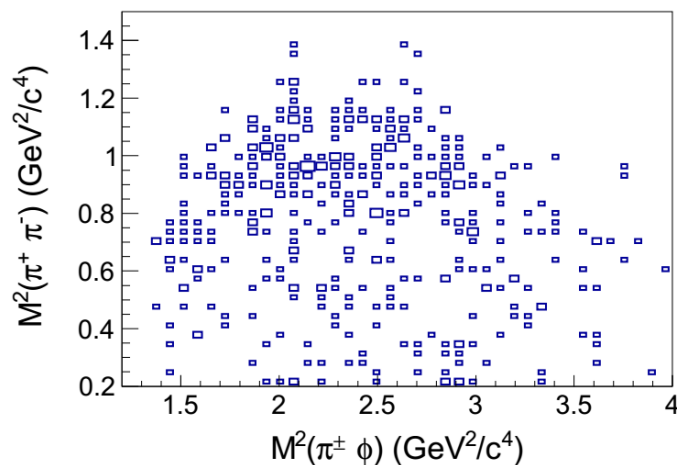
- Y(2175) (denoted as $\phi(2170)$ by PDG) was observed by BaBar, and confirmed by Belle, BESII and BESIII
 - A candidate for a tetraquark state, a strangeonium hybrid state, or a conventional $s\bar{s}$ state
- Unique place to search for the Z_S :
 - Y(2175) is regarded as strangeonium-like state analogous to Y(4260)
 - Mode: $Z_S \rightarrow \pi^\pm \phi$ (Expected mass $M_{Z_S} \approx 1.4 \text{ GeV}/c^2$)



Observation of $e^+e^- \rightarrow \eta Y(2175)$ at $\sqrt{s} > 3.7 \text{ GeV}$

PRD 99, 012014 (2019)

- Perform the search for $Y(2175)$ resonance in the process $e^+e^- \rightarrow \eta \phi f_0(980)$ at \sqrt{s} between 3.7 and 4.6 GeV.
- Combined significance for $Y(2175)$ signal is observed to be larger than 10σ .
- No significant Z_S signals in $\phi\pi^\pm$ spectrum.



Search for the Z_S at 2.125 GeV

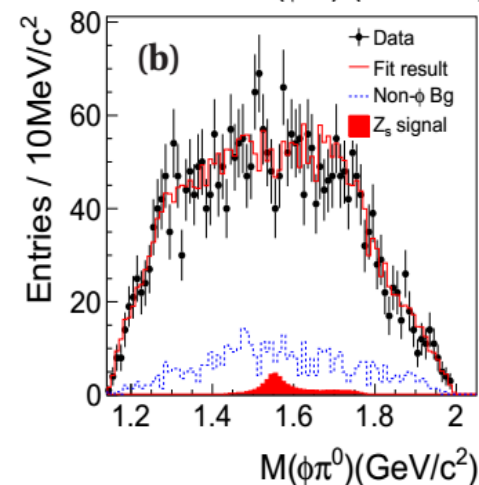
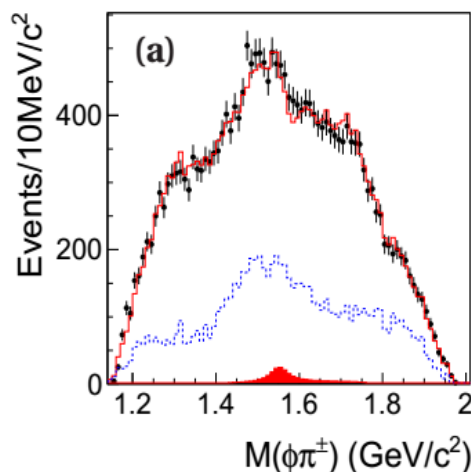
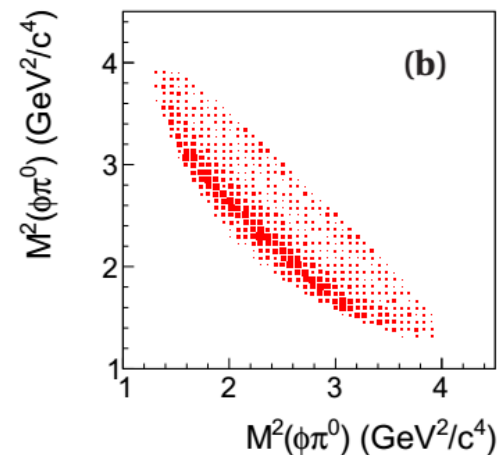
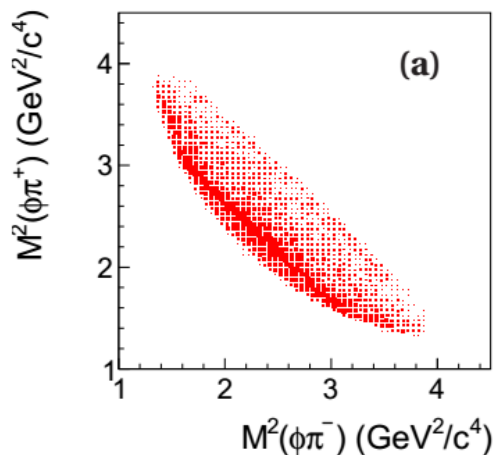
PRD99, 011101(2019)

➤ Perform the search for Z_S via $e^+e^- \rightarrow \phi\pi^+\pi^-$ ($\phi\pi^0\pi^0$) using 108 pb⁻¹ data collected at $\sqrt{s} = 2.125$ GeV.

➤ PWA is performed

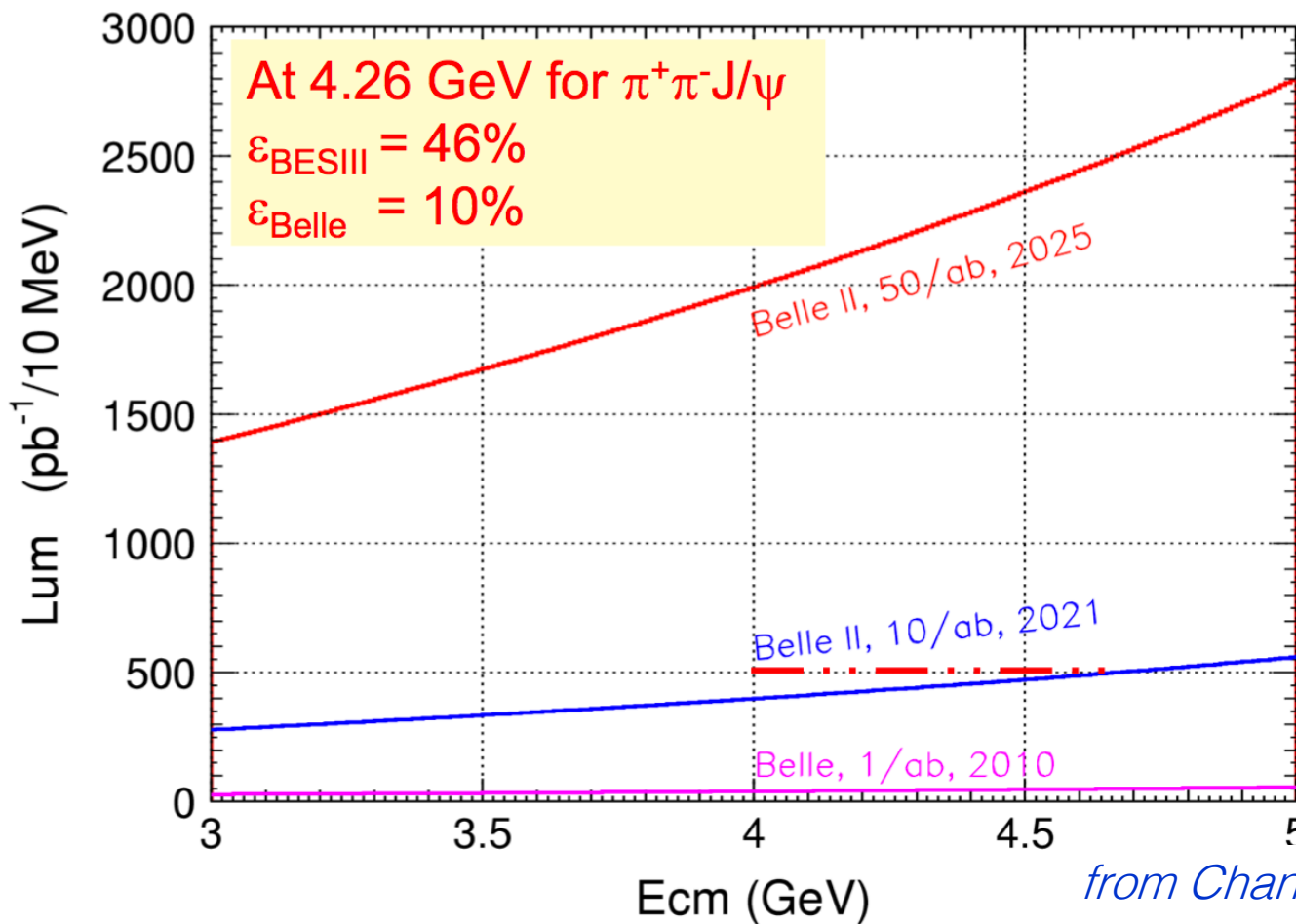
- $\phi\sigma$
- $\phi f_0(980)$
- $\phi f_0(1370)$
- $\phi f_2(1270)$
- $Z_S\pi$

➤ No clear Z_S signal is observed in the $\phi\pi$ mass spectrums around 1.5 GeV/c².



BELLE-II versus BESIII

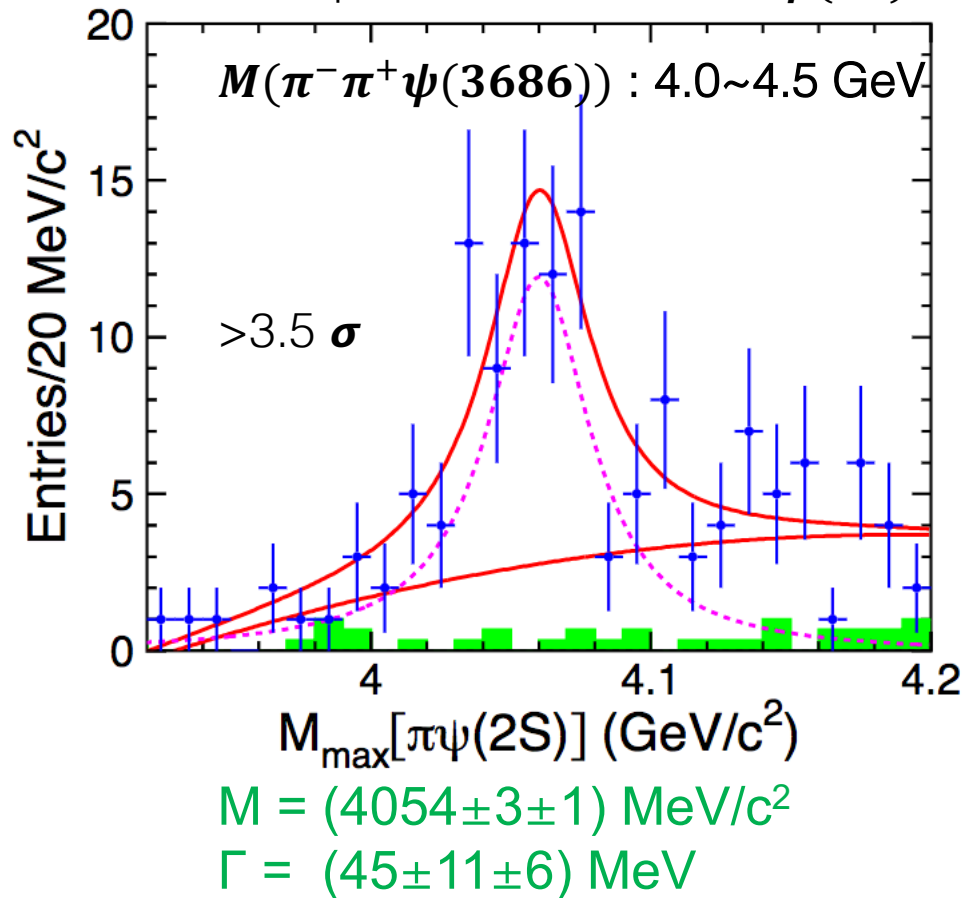
ISR produces events at all CM energies BESIII can reach



Comparison to the study of $Z' \rightarrow \pi^+ \psi(3686)$ at Belle



ISR returned productions of $\pi^- \pi^+ \psi(2S)$ at Belle



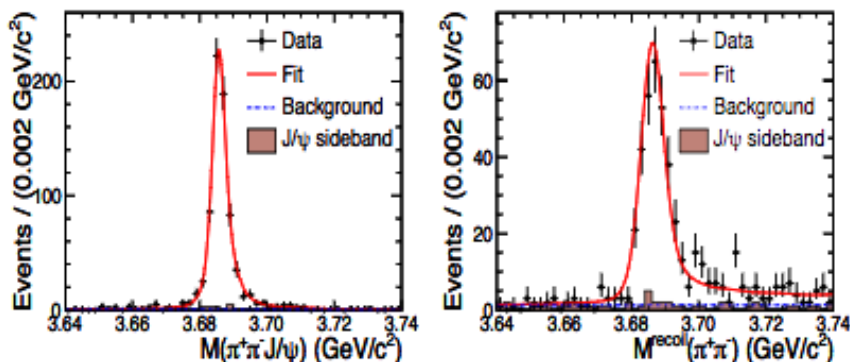
- The charged $\pi^+ \psi(3686)$ structure is about 4.030 GeV/c^2 at BESIII

$$M = 4030.3 \pm 0.1 \text{ MeV}/c^2$$

$$\Gamma = 5.1 \pm 0.2 \text{ MeV}$$

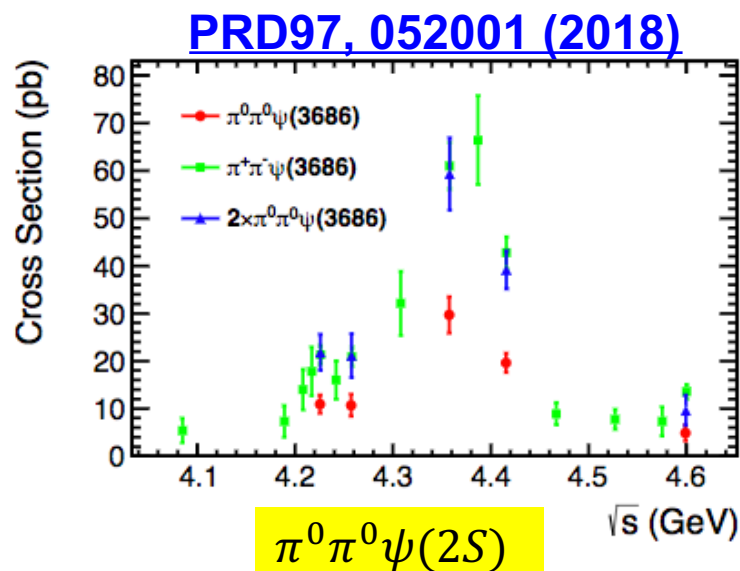
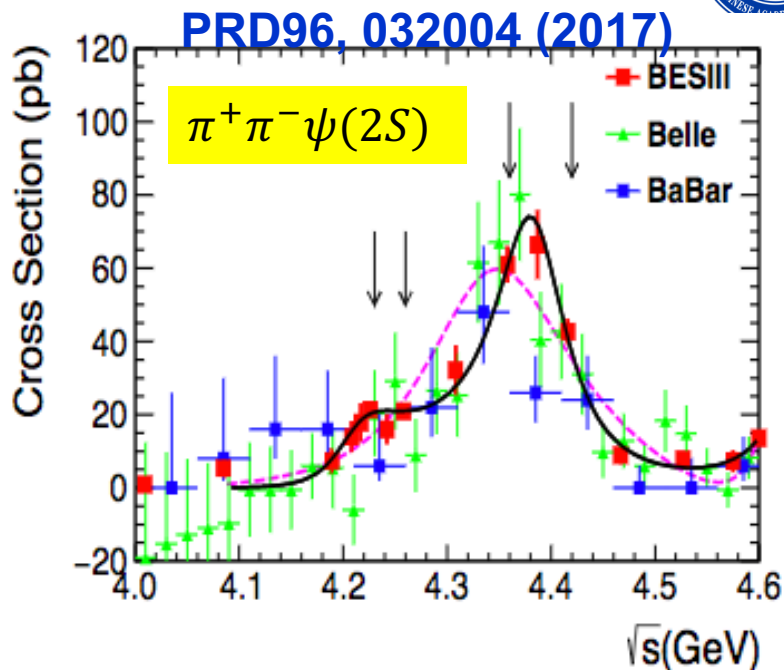
- BESIII's result deviates from that of the structure observed by Belle by over 3σ .

Belle, Phys.Rev. D91, 112007 (2015)



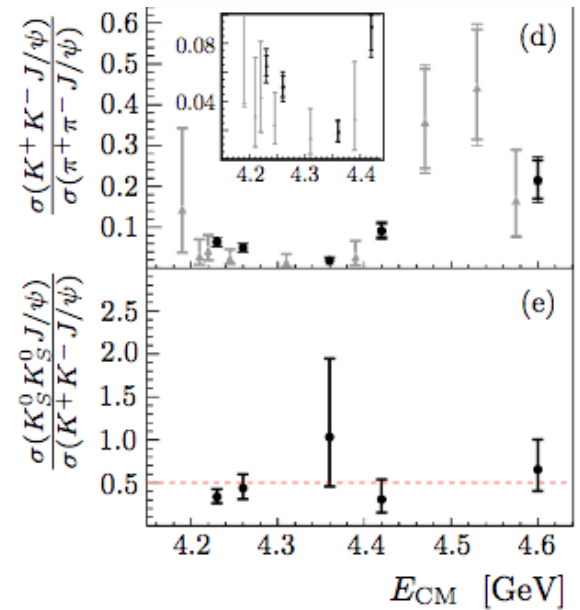
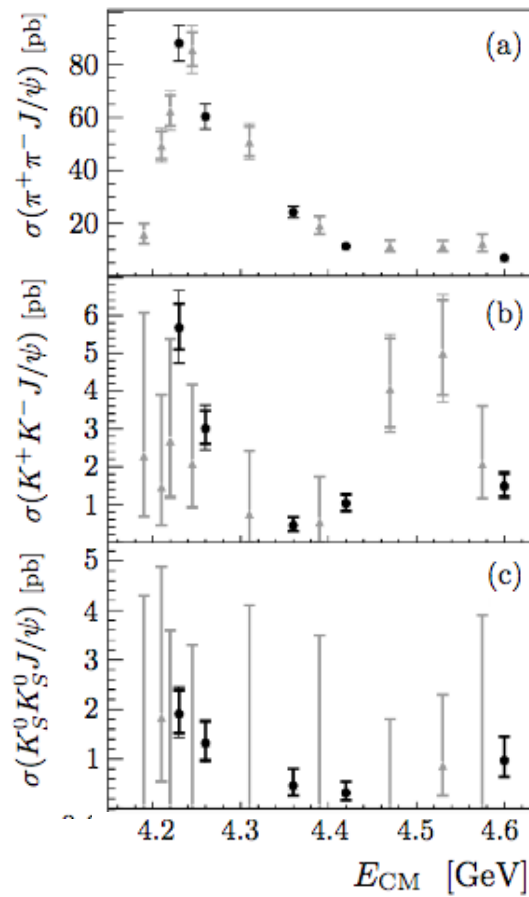
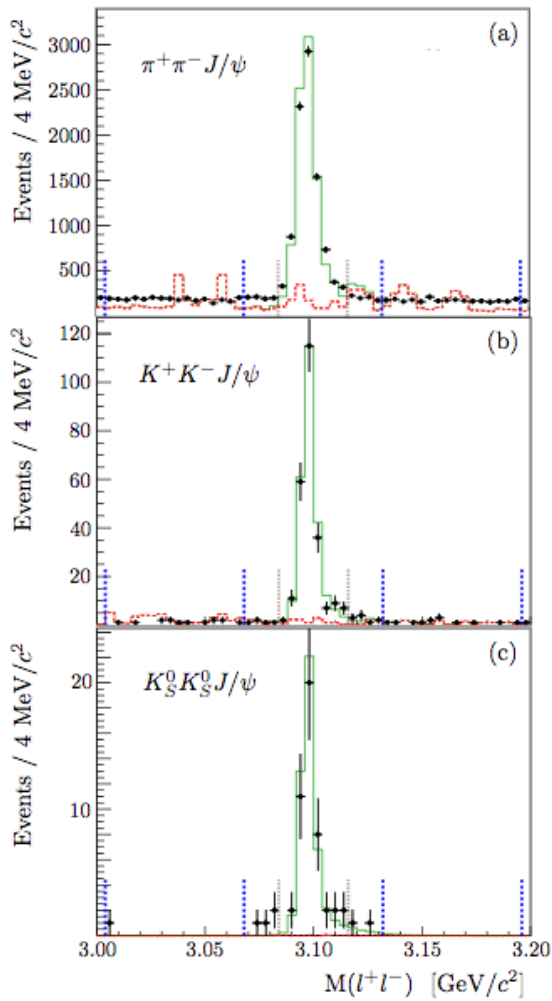
Parameters	Solution I	Solution II
$M(Y4220)$ (MeV/c ²)	4209.5 ± 7.4	
$\Gamma(Y(4220))$ (MeV)	80.1 ± 24.6	
$B\Gamma^{e^+e^-}(Y(4220))$ (eV)	0.8 ± 0.7	0.4 ± 0.3
$M(Y4390)$ (MeV/c ²)	4383.8 ± 4.2	
$\Gamma(Y(4390))$ (MeV)	84.2 ± 12.5	
$B\Gamma^{e^+e^-}(Y(4390))$ (eV)	3.6 ± 1.5	2.7 ± 1.0
ϕ_1 (rad)	3.3 ± 1.0	2.8 ± 0.4
ϕ_2 (rad)	0.8 ± 0.9	4.7 ± 0.1

- Confirm the lineshape of the Y(4360)
- Y(4220) and Y(4390) are confirmed



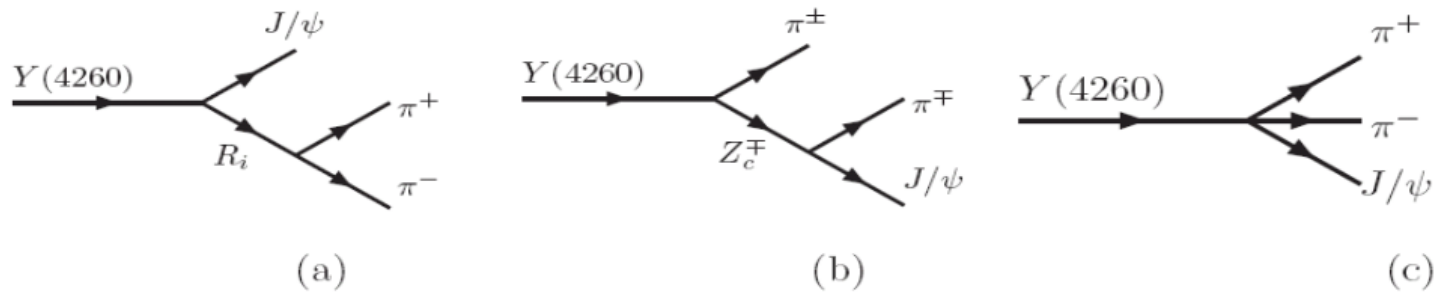
$$e^+e^- \rightarrow K^+K^-J/\psi$$

[PRD 97, 071101 \(2018\)](#)



- $\sigma(KKJ/\psi)$ lineshape is quite different from $\sigma(\pi^+\pi^-J/\psi)$ around $Y(4220)/Y(4260)$
- Higher bump around 4.5 GeV is clear and need further investigation

PRL 119.072001 (2017)



In the process $e^+e^- \rightarrow \gamma^* \rightarrow \pi^+\pi^- J/\psi$

- The helicity value of γ^* is taken as $\lambda_0 = \pm 1$ due to from e^+e^- annihilation
- $\gamma^* \rightarrow Z_c^\pm \pi^\mp, Z_c^\pm \rightarrow J/\psi \pi^\pm$, we try J^P for X : $0^-, 1^-, 1^+, 2^-, 2^+$, and 0^+ is not allowed
- Z_c^+ and Z_c^- states are assumed as isospin partner, with the same mass and coupling constant
- Six processes are included in fitting to data: $\sigma_0, f_0(980), f_2(1270), f_0(1370), Z_c^\pm$, and $\pi^+\pi^- J/\psi$