



The First LHAASO Collaboration Conference in 2021

Exploring Lorentz Invariance Violation With Sources of LHAASO

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Motivation

- Lorentz invariance is one of the founding principles of the Special Relativity theory
- Unify theory such as Quantum Gravity or String Theory, can lead to deviations from Lorentz symmetry
- Lorentz invariance violations (LIV) could lead to modifications of the dispersion relation. This will lead to some effect:
 1. speed of light changed
 2. Vacuum dispersion
 3. Vacuum birefringence
 4. vacuum Cherenkov radiation at superluminal for charge particles.
 5. Photon decay or splitting at superluminal speed
 -
- Due to long distance, astrophysical searches provide sensitive probes of LIV

LIV

Dispersion relation

$$E_\gamma^2 - p_\gamma^2 = \pm |\alpha_n| p_\gamma^{n+2},$$

$$E_{LIV}^{(n)} = \alpha_n^{-1/n} \cdot (n > 0)$$

superluminal case

Process: $\gamma \rightarrow e^+e^-$

$$E_\gamma^2 - p_\gamma^2 = |\alpha_n| p_\gamma^{n+2} = m_{\gamma,eff}^2,$$

$$E_{LIV}^{(n)} = \alpha_n^{-1/n}, (n > 0)$$

$$m_{\gamma,eff} < 2m_e.$$

$$\alpha_0 \leq \frac{4m_e^2}{E_\gamma^2 - 4m_e^2},$$

$$E_{LIV}^{(1)} \geq 9.57 \times 10^{23} \text{eV} \left(\frac{E_\gamma}{\text{TeV}} \right)^3,$$

$$E_{LIV}^{(2)} \geq 9.78 \times 10^{17} \text{eV} \left(\frac{E_\gamma}{\text{TeV}} \right)^2.$$

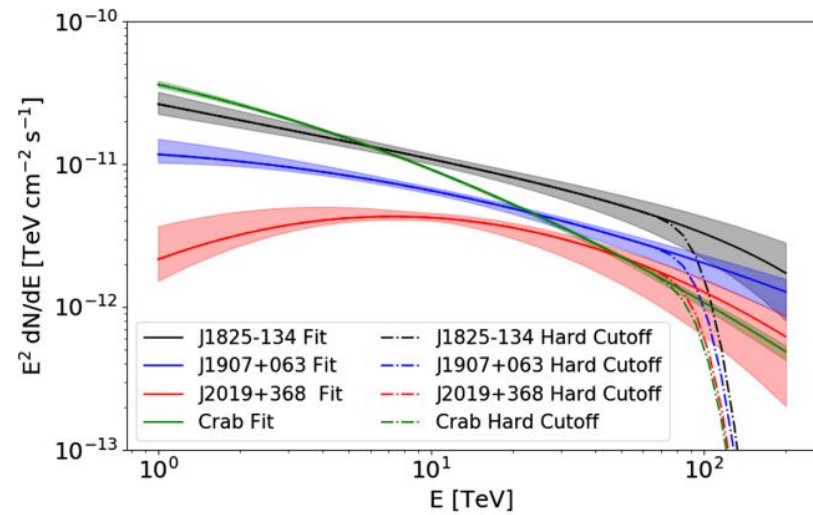
Process: $\gamma \rightarrow 3\gamma$

$$\Gamma_{\gamma \rightarrow 3\gamma} = 5 \times 10^{-14} \frac{E_\gamma^{19}}{m_e^8 E_{LIV}^{(2)10}},$$

$$E_{LIV}^{(2)} > 3.33 \times 10^{19} \text{eV} \left(\frac{L}{\text{kpc}} \right)^{0.1} \left(\frac{E_\gamma}{\text{TeV}} \right)^{1.9}.$$

1. **Hard cutoff** in SED
2. we need find is cut energy E_γ

HAWC results



Source	E_c TeV	L kpc	α_0 10^{-17}	$E_{\text{LIV}}^{(1)}$ 10^{31} eV	$E_{\text{LIV}}^{(2)}$ 10^{23} eV	$E_{\text{LIV}}^{(2)}$ 10^{23} eV (3γ)
J1825 – 134	244	1.55	1.75	1.39	0.58	12
J1907 + 063	218	2.37	2.2	0.99	0.47	10.1
J0534 + 220	152	2	4.52	0.34	0.23	4.99
J2019 + 368	120	1.8	7.25	0.17	0.14	3.15
Combined	285	...	1.29	2.22	0.8	...

95% limit cut energy is 285 TeV

Sources with high significance above 100 TeV in LHAASO-KM2A

source name	R.A. ($^{\circ}$)	dec ($^{\circ}$)	Significance (σ) above 100 TeV	E_{Max} (PeV)	Flux (\pm error) (CU) at 100 TeV
LHAASO J0534+2202	83.55	22.05	17.8	0.88 \pm 0.11	1.00(0.14)
LHAASO J1825-1326	276.45	-13.45	16.4	0.42 \pm 0.16	3.57(0.52)
LHAASO J1839-0545	279.95	-5.75	7.7	0.21 \pm 0.05	0.70(0.18)
LHAASO J1843-0338	280.75	-3.65	8.5	0.26 $^{+0.16}_{-0.10}$	0.73(0.17)
LHAASO J1849-0003	282.35	-0.05	10.4	0.35 \pm 0.07	0.74(0.15)
LHAASO J1908+0621	287.05	6.35	17.2	0.44 \pm 0.05	1.36(0.18)
LHAASO J1929+1745	292.25	17.75	7.4	0.71 $^{+0.16}_{-0.07}$	0.38(0.09)
LHAASO J1956+2845	299.05	28.75	7.4	0.42 \pm 0.03	0.41(0.09)
LHAASO J2018+3651	304.75	36.85	10.4	0.27 \pm 0.02	0.50(0.10)
LHAASO J2032+4102	308.05	41.05	10.5	1.42 \pm 0.13	0.54(0.10)
LHAASO J2108+5157	317.15	51.95	8.3	0.43 \pm 0.05	0.38(0.09)
LHAASO J2226+6057	336.75	60.95	13.6	0.57 \pm 0.19	1.05(0.16)

a

Data:

KM2A Half Array

Data: 2019.12.27-2020.11.30 V1

Live time: 312.6 days

Energy Spectrum:

Almost same as Crab (1). Main difference:

- Energy bin width: $\log E \ 0.1$
- Estimate the background with “Equal zenith angle method”

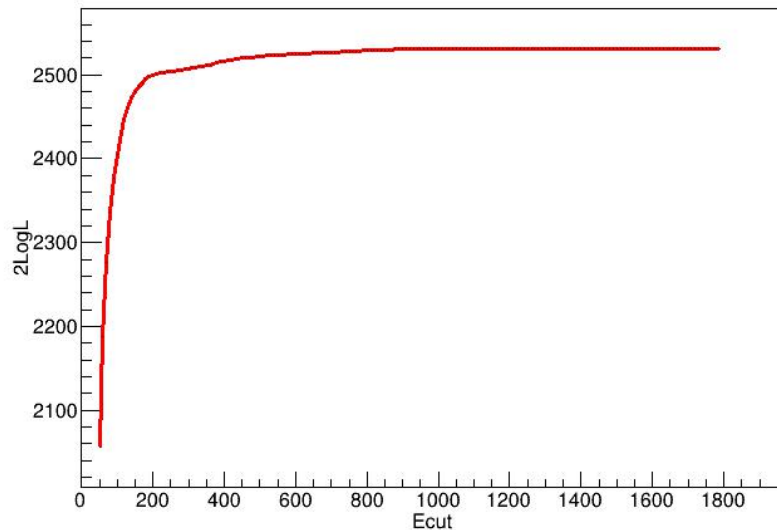
CPC crab: Chinese Physics C Vol. 45, No. 2 (2021) 025002

LHAASO J0534+2202 ($E_{\max} = 0.88$ PeV)

if cut exists?

$$f(E) = \phi_0 \left(\frac{E}{E_0} \right)^{(-\alpha - \beta \log(E/E_0))} \theta(E_{cut}, E) \quad E_0 = 20 \text{ TeV}$$

$$L(\phi_0, \alpha, \beta, E_{cut}) = \prod_{i=1}^n \text{Poisson}(N_{obs_i}, N_{sig_i}(\phi_0, \alpha, \beta, E_{cut}) + N_{bkg_i})$$



SED: Ecut->Infinity

$$\Phi_0: 1.06 \times 10^{-14} \pm 3.55 \times 10^{-16}$$

$$\alpha: -2.978 \pm 0.068$$

$$\beta: -0.018 \pm 0.046$$

2LogL: 2531.4

95% constraints on cut energy

$$TS(E_{cut}) = - \sum_{bin} 2 \log \left(\frac{L_1(\alpha_1, \beta_1, \gamma_1, E_{cut})}{L_0(\alpha_2, \beta_2, \gamma_2, E_{cut} \rightarrow \infty)} \right)$$
$$L(\phi_0, \alpha, \beta, E_{cut}) = \prod_{i=1}^n Poission(Nobs_i, Nsig_i(\phi_0, \alpha, \beta, E_{cut}) + Nbkg_i)$$

In high energy bins, the number of events is small, Wilks theorem does not apply
TS(Ecut) distribution is not a chi2(1) distribution, MC is needed

For a Ecut model

- we produce MC data
- Get distribution of pseudo data.
- Calculate exclusion limit.

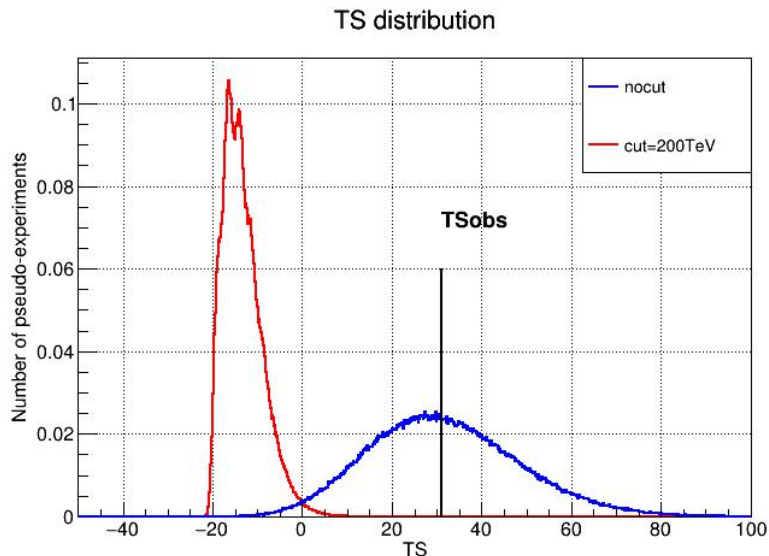
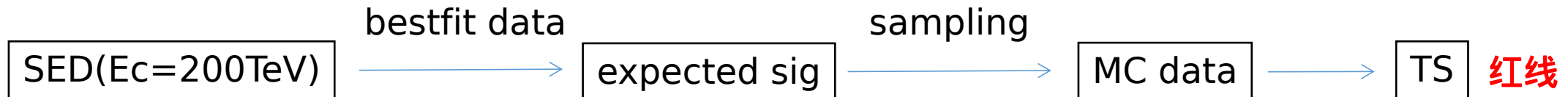
A group of Ecut are chosen, get distribution and find
Ecut corresponding to 95% exclusion.

TS distribution of pseudo data

As an example, we get exclusion for cut=200 TeV SED.

$$TS(E_{cut} = 200TeV) = - \sum_{bin} 2 \log \left(\frac{L_1(\alpha_1, \beta_1, \gamma_1, E_{cut} = 200TeV)}{L_0(\alpha_2, \beta_2, \gamma_2, E_{cut} \rightarrow \infty)} \right)$$

$$L(\phi_0, \alpha, \beta, E_{cut}) = \prod_{i=1}^n Poission(Nobs_i, Nsig_i(\phi_0, \alpha, \beta, E_{cut}) + Nbkg_i)$$



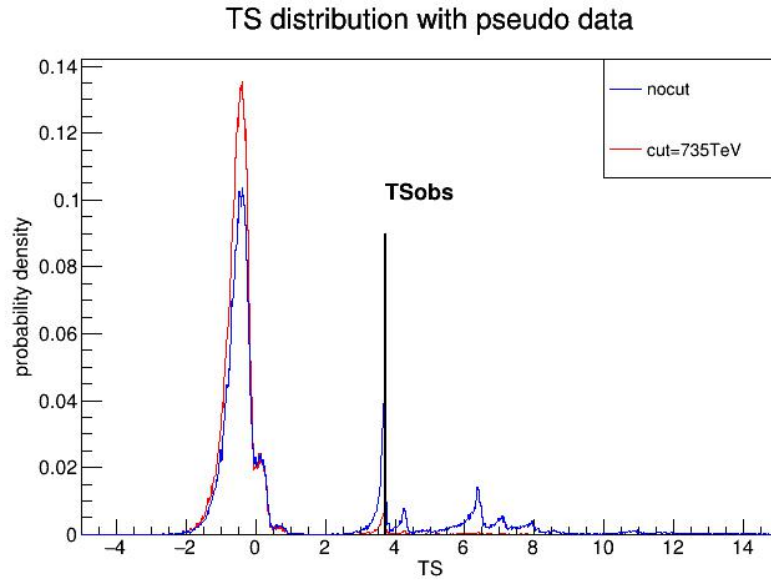
TSobs = 31

CLs+b: 0.00001%

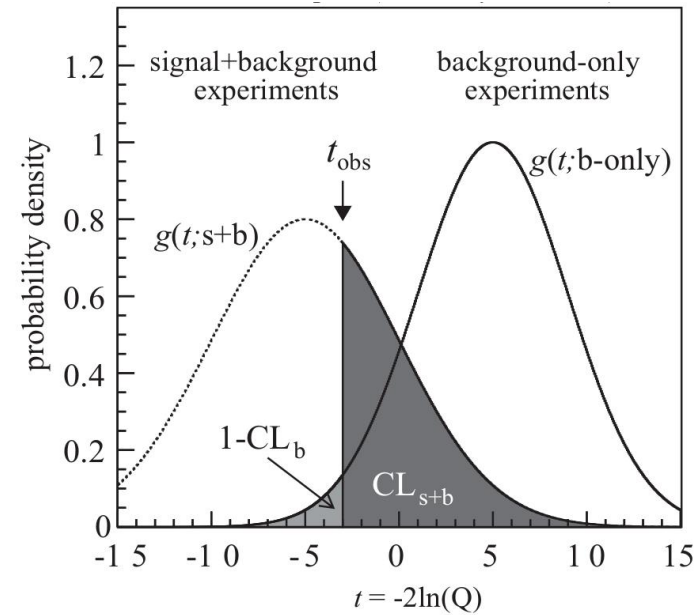
95% correspond to higher Ecut

95% exclude Ecut

Ecut=735TeV



TSobs = 3.72
CL_{s+b}: 0.8%
CL_b: 15.8%
CL_s: 5%



CLs method: $CL_s = CL_{s+b} / CL_b$

CLs method: J. Phys. G: Nucl. Part. Phys. 28
(2002) 2693-2704

LHAASO J2032+4102 & J1929+1745

LHAASO J2032+4102 (1.42 PeV)

0.3° extension

$$\Phi_0: 5.22 \times 10^{-15} \pm 3.33 \times 10^{-16}$$

$$\alpha: -3.095 \pm 0.115$$

$$\beta: -0.021 \pm 0.063$$

$$2\text{LogL}: 515.6$$

95% CLs limit:

$$E_{\text{cut}} = \mathbf{1103 \text{ TeV}}$$

J1929+1745 (0.71PeV)

0.3° extension

$$\Phi_0: 3.38 \times 10^{-15} \pm 3.37 \times 10^{-16}$$

$$\alpha: -2.941 \pm 0.185$$

$$\beta: -0.058 \pm 0.097$$

$$2\text{LogL}: 244.2$$

95% CLs limit:

$$E_{\text{cut}} = \mathbf{520 \text{ TeV}}$$

95% LIV scale constraints

$\gamma \rightarrow$

$\gamma \rightarrow 3\gamma$

Source	E_{\max} (PeV)	$E_{\text{cut}95\%}$ (PeV)	α_0 $\times 10^{-18}$	$E_{LIV}^{(1)}$ (eV) $\times 10^{32}$	$E_{LIV}^{(2)}$ (eV) $\times 10^{23}$	L kpc	$E_{LIV}^{(2)}(3\gamma)$ (eV) $\times 10^{24}$
J0534+2202	0.88	0.735	1.92	3.79	5.28	2	9.9
J2032+4102	1.42	1.1	0.86	12.7	11.8	1.4	20.7
J1929+1745	0.71	0.52	3.84	1.34	2.64	6.3	5.61
combine	-	1.1	0.86	12.7	11.8	-	-
eHWC 2020 (HAWC)	-	-	13	0.22	0.58	-	1.2
Crab 2017 (HEGRA)	-	-	-	0.0015	0.028	-	-
Crab 2013 (HEGRA)	-	-	400	-	-	-	-
Crab 2001 (CANGAROO)	-	-	400	-	-	-	-
Crab 2019 (Tibet)	-	-	-	-	-	-	0.41
GRB 090510 (Fermi-LAT)	-	-	-	0.0013	0.0009	-	-

$$E_{LIV}^{(1)} \sim 10^5 E_{Planck}$$

$$E_{LIV}^{(2)} \sim 0.0017 E_{Planck}$$

Error analysis on 95% Ecut

Simulation

flux: 7%

spectral index: 0.02

Spectrum fit

spectrum: Ecut->Infinity

$\Phi_0: 1.06 \times 10^{-14} \pm 3.55 \times 10^{-16}$

$\alpha: -2.978 \pm 0.068$

$\beta: -0.018 \pm 0.046$

2LogL: 2531.4

Check

Effect of bkg

bkg	Ecut(TeV)
bkg*10	570
bkg*2	695
bkg	735
bkg/2	757
bkg/10	773
0	775

Spectrum choice

$$f(E) = \phi_0 \left(\frac{E}{E_0} \right)^{-\alpha} e^{-\frac{E}{E\beta}}$$

Ecut: 620 TeV

Summary

- LIV superluminal case : $\gamma \rightarrow e^+e^-$, $\gamma \rightarrow 3\gamma$
- Three source
 - LHAASO J0534+2202
 - LHAASO J1929+1745
 - LHAASO J2032+4102
- 95% constraints using CLs method

$$E_{LIV}^{(1)} \sim 10^5 E_{Planck}$$

$$E_{LIV}^{(2)} \sim 0.0017 E_{Planck}$$

- One order better comparing to HAWC results

Summary

- LIV superluminal case : $\gamma \rightarrow e^+e^-$, $\gamma \rightarrow 3\gamma$
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 - LHAASO J0534+2202
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$$E_{LIV}^{(1)} \sim 10^5 E_{Planck}$$

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THANK YOU

看谱指数的影响

$\log E > 2.0$

$\phi_0 : (1.730e-14 \pm 1.481e-14)$

$\alpha : (-3.484 \pm 0.374)$

index	95% Ecut (TeV)
-3.48	735
-3.3	737
-3.6	724

$$f(E) = \phi_0 \left(\frac{E}{E_0} \right)^{(-\alpha - \beta \log(E/E_0))} \theta(E_{cut}, E) \quad E_0 = 20 \text{ TeV}$$

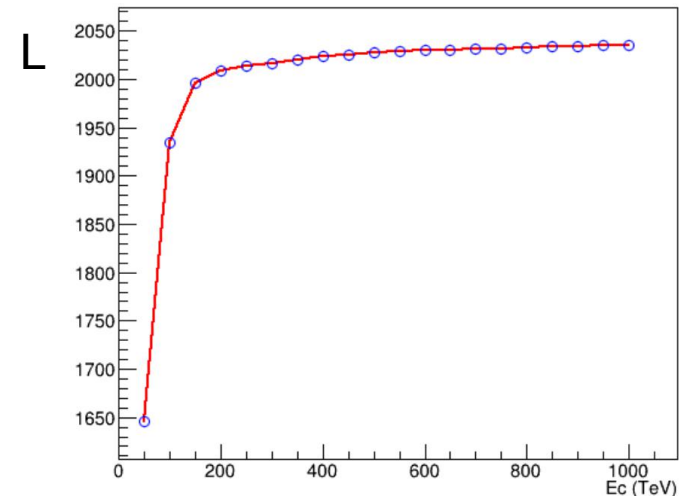
90% events around source

on: 13955, 8838, 3501, 1880, 353, 275, 127, 75, 74, 38,
23, 14, 8, 3, 1, 1, 2, 1, 0, 1, 0, 0, 0

off: 12531.7, 7745.85, 2719.33, 1307.66, 120.06, 67.7357, 14.5503, 6.89506, 6.50599, 2.94018,
0.904979, 0.524104, 0.200803, 0.193915, 0.0491451, 0.0244675, 0.0152723, 0.0308566, 0.0036518,
0.00125205, 0.00103157, 0.000687712, 0.00128946

$$L(\phi_0, \alpha, \beta, E_{cut}) = \prod_{i=1}^n \text{Poisson}(N_{obs_i}, N_{sig_i}(\phi_0, \alpha, \beta, E_{cut}) + N_{bkg_i})$$

spectrum: $E_{cut} \rightarrow \text{Infinity}$
 $\alpha: (1.059e-14 \pm 3.545e-16)$
 $\beta: (-2.978 \pm 0.068)$
 $\beta_2: (-0.118 \pm 0.046)$
 TS 2531.373



2

LHAASO J2032+4102 (1.42 PeV)

(源1.5°范围内, est<-2.36)

Energy bin (logE)	logE	E (TeV)	mjd	angle (°)	ra (°)	dec (°)	est	theta (°)	phi (°)
2.8-3.0									
2.6-2.8	2.652 96	449.7 38	58855.18810674 48	1.0016	306.73	41.1698			
3.0-3.2	3.076 39	1192. 31	58990.03228223 16	0.529082	307.45	41.329	-2.5966	36.8268	239.63
	3.169 24	1476. 52	59101.60965273 16	0.189554	307.92	40.8876	-2.4275	11.6103	182.87
	3.152 69	1421. 31	59101.62591003 42	0.113385	308.072	40.9379	-2.9745	12.7345	202.74

core_x	core_y	NfiltE	NfiltM	NuM4	NpE3
230.068	-102.153	219	6	7.4161	2929.374
-193.1925	-227.7205	284	14	23.7453	6355.3320
-205.8047	389.0966	312	6	6.6367	6258.6689

0.3°拓展

on: 18378, 11907, 4929, 2577, 387, 230, 112, 41, 57, 31, 15, 10, 2, 6, 3, 1, 0, 0, 0, 0, 1, 1, 0

off: 17631.1, 11276.7, 4546.26, 2237.79, 241.556, 142.478, 37.9953, 18.3223, 20.2199, 9.06783, 3.28855, 1.63565, 0.829864, 0.590427, 0.408925, 0.238034, 0.118758, 0.0570179, 0.0319564, 0.0140984, 0.00733407, 0.00550056, 0.00733407

alpha:(5.221e-15 +- 3.326e-16)

beta:(-3.095 +- 0.115)

beta2:(-0.021 +- 0.063)

TS 515.594

Ecut 1103.5 TS_nocut_ratio 0.027743, TS_cut_ratio 0.001347, ratio 0.0485528

Ecut 1103.6 TS_nocut_ratio 0.031008, TS_cut_ratio 0.001602, ratio 0.0516641

3

LHAASO J1929+1745 (0.71PeV)

on: 15747, 10127, 4186, 2038, 290, 212, 76, 36, 30, 19, 8, 11, 5, 2, 0, 1, 1, 1, 1, 0, 0, 0, 0

off: 15397.9, 9789.64, 3925.18, 1911.34, 214.137, 121.776, 31.6733, 15.3863, 17.8276, 6.92699,
3.16392, 1.75766, 0.941066, 0.482397, 0.224137, 0.132253, 0.141542, 0.029024, 0.0269757, 0.0142372,
0.0116941, 0.00730881, 0.00803969

alpha:(3.383e-15 +- 3.371e-16)

beta:(-2.941 +- 0.185)

beta2:(-0.058 +- 0.097)

TS 244.164

Ecut 520TeV

TS_nocut_ratio 0.135093, TS_cut_ratio 0.006777, ratio 0.0501654415846861