



# SU(3) Flavor Symmetry for Weak Hadronic Decays of $B_{bc}$ baryons

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Phys. Rev. D 102, 056005 (2020)

第二届强子与重味物理理论和实验联合研讨会, 兰州大学, 27/3/21

**1** Effective Hamiltonian

**2** Two Body Decay Modes

**3** SU(3) Invariant Amplitudes

**4** Experimental Analysis

**1** Effective Hamiltonian

**2** Two Body Decay Modes

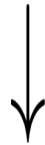
**3** SU(3) Invariant Amplitudes

**4** Experimental Analysis

# Introduction

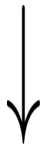


**Baryons with a heavy b(c)-quark and two c-quarks**



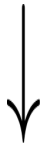
**Baryons with a heavy b-quark and c-quark**

**yet to discover**



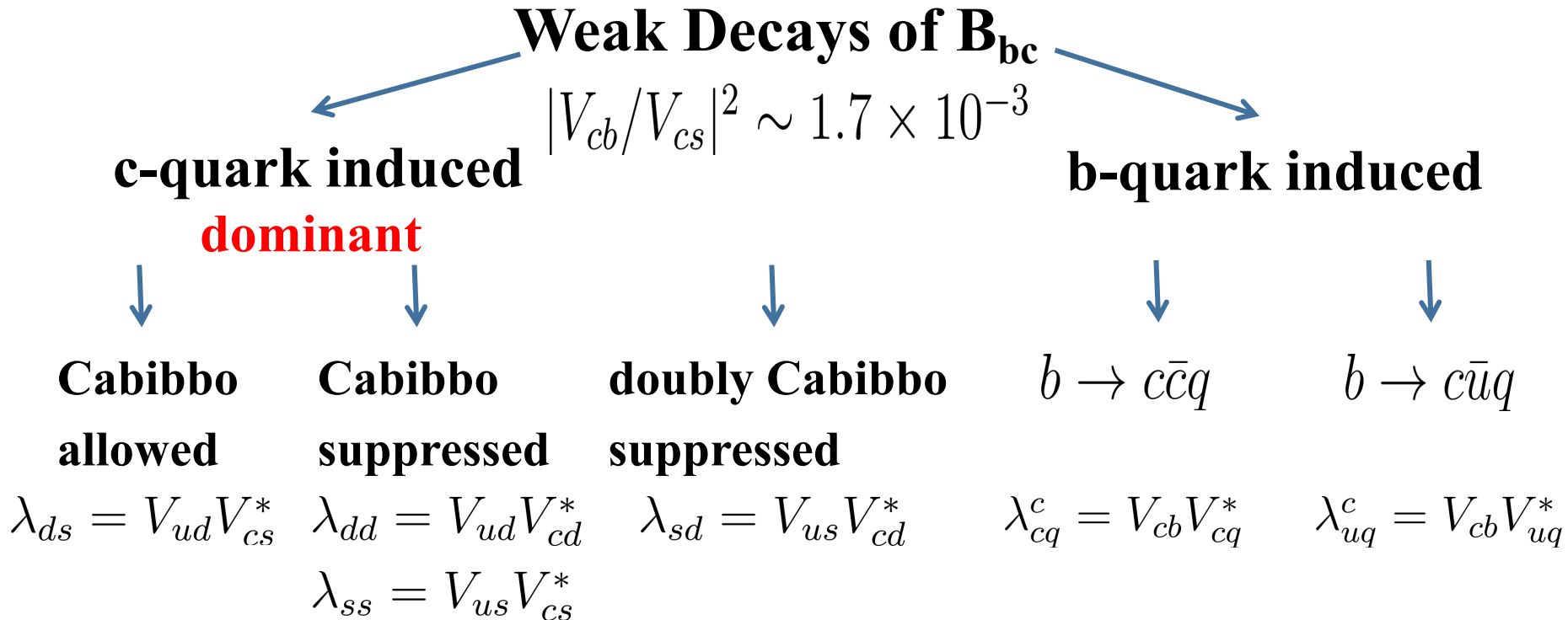
**SU(3) symmetry**

$$B_{bc} = (bcu, bcd, bcs) = (\Xi_{bc}^+, \Xi_{bc}^0, \Omega_{bc}^0)$$



**Identifying  $B_{bc}$  by dominant weak decays**

# Weak Decays



- Note: 1. Two decays to find some different favorable search strategies.**
- 2. b-decay mode has a **displaced vertex** for subsequent decays traveling  $10^3$  longer distance before decaying than c-decay ones.**

# Effective Hamiltonian



## c-quark decay

$$H_{eff}^c = \frac{G_F}{\sqrt{2}} \lambda_{q'q} [c_1(\bar{u}q')(\bar{q}c) + c_2(\bar{u}_\beta q'_\alpha)(\bar{q}_\alpha c_\beta)]$$

## b-quark decay

$$(\bar{q}_1 q_2) = \bar{q}_1 \gamma_\mu (1 - \gamma_5) q_2$$

$$H_{eff}^b = \frac{G_F}{\sqrt{2}} \lambda_{aq}^c [c_1(\bar{q}a)(\bar{c}b) + c_2(\bar{q}_\beta a_\alpha)(\bar{c}_\alpha b_\beta)]$$

## Nonzero entries

**a takes c and u**

$$H_{eff}^c : H_2^{31} = \lambda_{ds}, H_2^{21} = \lambda_{dd}, H_3^{31} = \lambda_{ss} = -\lambda_{dd}, H_3^{21} = \lambda_{sd}$$

$$H_{eff}^b(a = u) : H_1^2 = \lambda_{ud}^c, H_1^3 = \lambda_{us}^c$$

**approximation**

$$H_{eff}^b(a = c) : H^2 = \lambda_{cd}^c, H^3 = \lambda_{cs}^c$$

Eur.Phys.J.C80,59(2020),

arXiv:2006.15291

## 1 Effective Hamiltonian

## 2 Two Body Decay Modes

## 3 SU(3) Invariant Amplitudes

## 4 Experimental Analysis

# Two Body Decay Modes



**Effective Hamiltonians can induce  $B_{bc}$  to decay**

**Two body decays**  $\left\{ \begin{array}{l} \text{multi body contains unknown resonance} \\ \text{simple calculation and identified final states} \end{array} \right.$

$$H_i^{jk}$$

$$B_{bc} \rightarrow \underline{B^{(l)}} + M_b$$

**octet(decuplet)**

$$H_j^i$$

$$B_{bc} \rightarrow B_{cc} + \underline{M}$$

**octet**

$$H^i$$

$$B_{bc} \rightarrow B_{cc} + M_{\bar{c}}$$

$$B_{bc} \rightarrow \underline{B_b^{(l)}} + M$$

**anti-triplet(sextet)**

$$B_{bc} \rightarrow B_c^{(l)} + \underline{M_c}$$

**anti-triplet**

$$B_{bc} \rightarrow B_c^{(l)} + M_{c\bar{c}}$$



# Components of baryon and meson



## octet baryon

$$B_j^i : (n, p, \Sigma^{\pm,0}, \Xi^{-,0}, \Lambda)$$

## decuplet baryon

$$B'_{ijk} : (\Delta^{++,\pm,0}, \Sigma'^{\pm,0}, \Xi'^{-,0}, \Omega^-)$$

## heavy cc baryon

$$B_{cc} : (\Xi_{cc}^{++}, \Xi_{cc}^+, \Omega_{cc}^+)$$

## octet pseudoscalar meson

$$M_j^i : (\pi^{\pm,0}, K^{\pm}, K^0, \bar{K}^0, \eta)$$

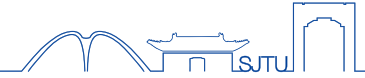
## heavy b meson

$$M_b : (B^-, \bar{B}^0, \bar{B}_s^0)$$

## heavy c meson

$$M_c : (D^0, D^+, D_s^+)$$

# Components of baryon and meson



## heavy b baryon

$$B_b = \begin{pmatrix} 0 & \Lambda_b^0 & \Xi_b^0 \\ -\Lambda_b^0 & 0 & \Xi_b^- \\ -\Xi_b^0 & -\Xi_b^- & 0 \end{pmatrix}$$

$$B'_b = \begin{pmatrix} \Sigma_b^+ & \Sigma_b^0/\sqrt{2} & \Xi_b'^0/\sqrt{2} \\ \Sigma_b^0/\sqrt{2} & \Sigma_b^- & \Xi_b'^-/\sqrt{2} \\ \Xi_b'^0/\sqrt{2} & \Xi_b'^-/\sqrt{2} & \Omega_b^- \end{pmatrix}$$

## heavy c baryon

$$B_c = \begin{pmatrix} 0 & \Lambda_c^+ & \Xi_c^+ \\ -\Lambda_c^+ & 0 & \Xi_c^0 \\ -\Xi_c^+ & -\Xi_c^0 & 0 \end{pmatrix}$$

$$B'_c = \begin{pmatrix} \Sigma_c^{++} & \Sigma_c^+/\sqrt{2} & \Xi_c'^+/\sqrt{2} \\ \Sigma_c^+/\sqrt{2} & \Sigma_c^0 & \Xi_c'^0/\sqrt{2} \\ \Xi_c'^+/\sqrt{2} & \Xi_c'^0/\sqrt{2} & \Omega_c^0 \end{pmatrix}$$

## 1 Effective Hamiltonian

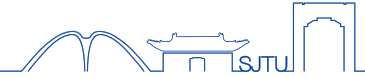
## 2 Two Body Decay Modes

## 3 SU(3) Invariant Amplitudes

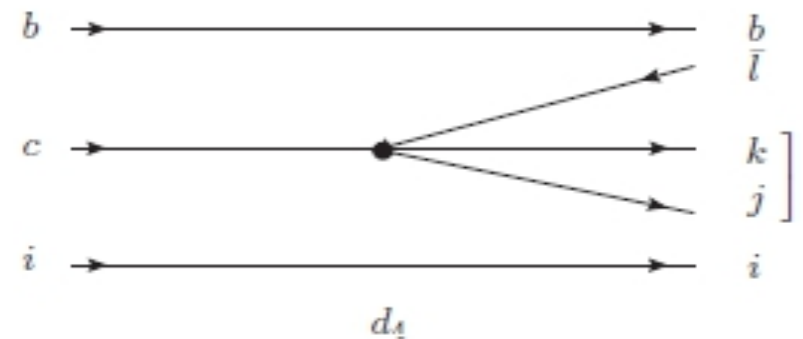
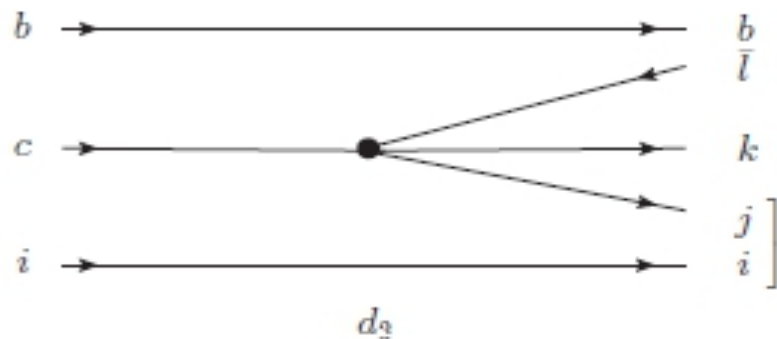
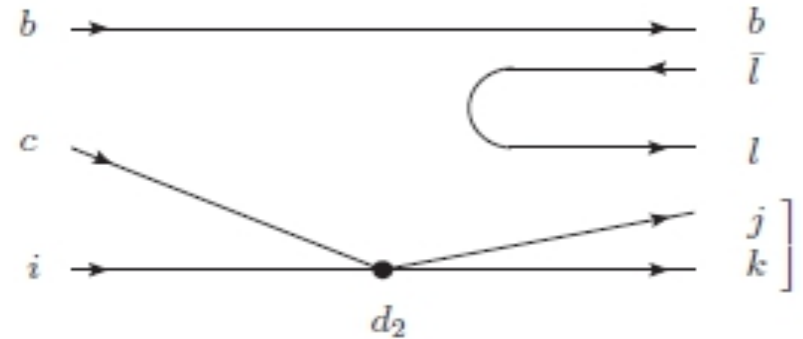
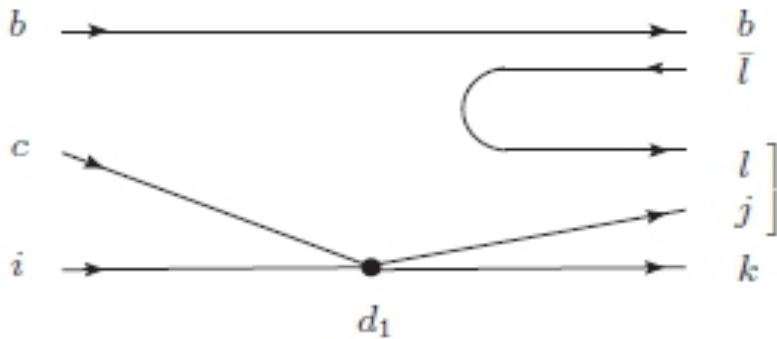
## 4 Experimental Analysis

# $H_{jk}^i$ induced decays

$$B_{bc} \rightarrow B + M_b$$



$$\begin{aligned} \mathcal{M} = & d_1 \mathbf{B}_{bc}^i H_i^{jk} \mathbf{B}_{ljk} M_b^l + d_2 \mathbf{B}_{bc}^i H_i^{jk} \mathbf{B}_{jkl} M_b^l + \underline{d' \mathbf{B}_{bc}^i H_i^{jk} \mathbf{B}_{klj} M_b^l} \\ & + d_3 \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}_{ijk} M_b^l + d_4 \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}_{jki} M_b^l + \underline{d'' \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}_{kij} M_b^l} \end{aligned}$$

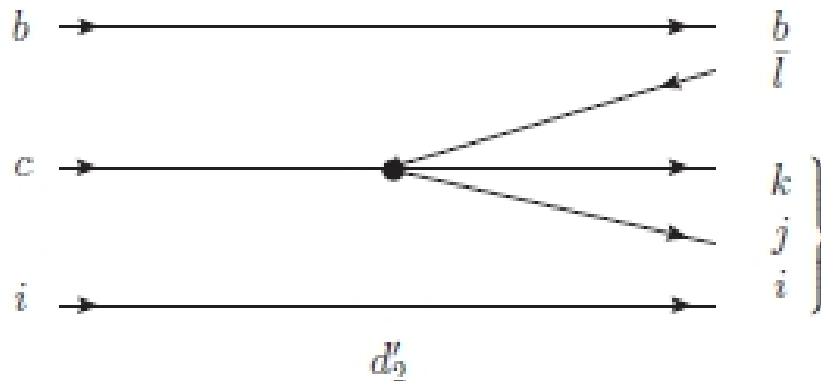
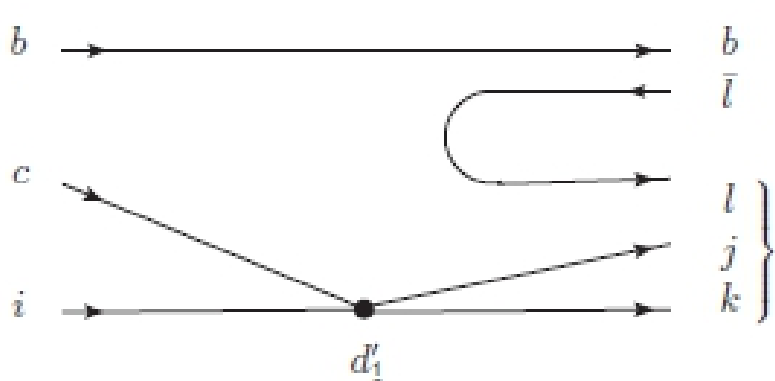


# $H_{ijk}$ induced decays



$$B_{bc} \rightarrow B' + M_b$$

$$\mathcal{M} = d'_1 \mathbf{B}_{bc}^i H_i^{jk} \mathbf{B}'_{ljk} M_b^l + d'_2 \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}'_{ijk} M_b^l$$



**Contract up-down indices in hadron and Hamiltonian**

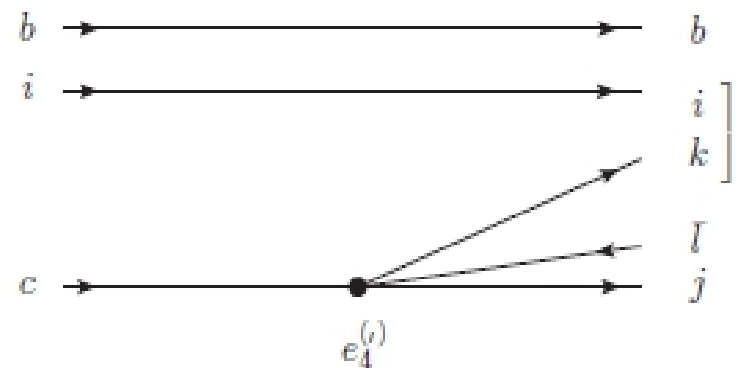
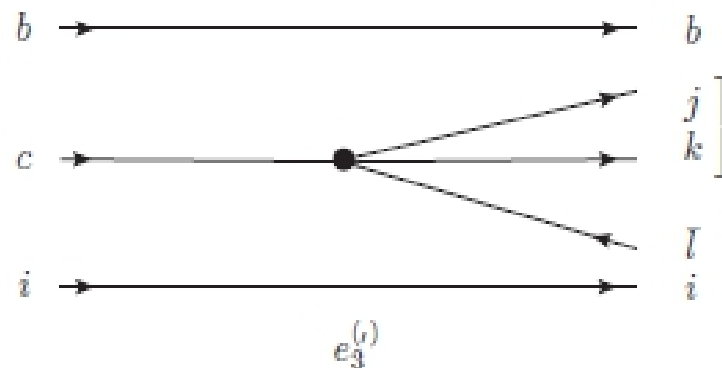
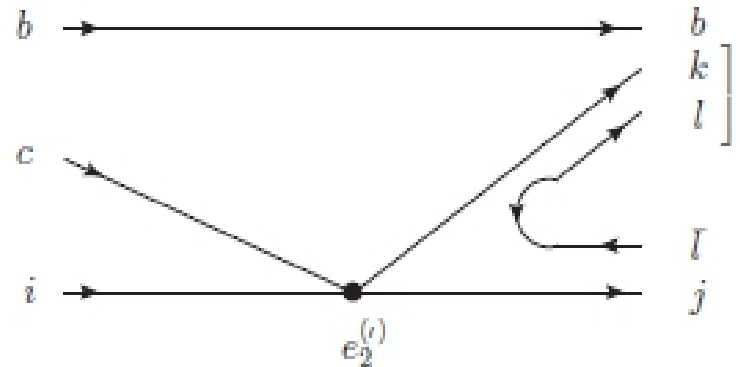
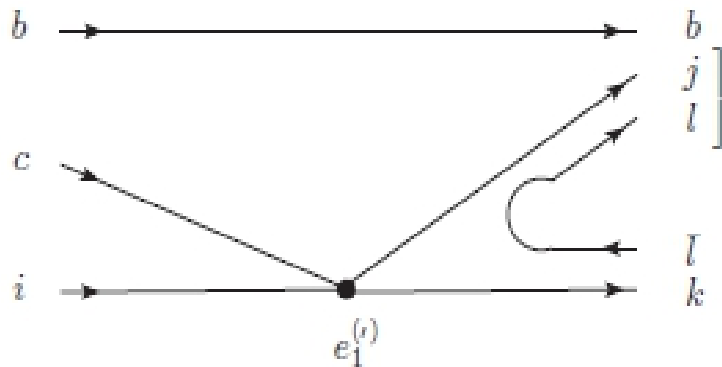


**SU(3) singlet**

# $H_{jk}^{i}$ induced decays

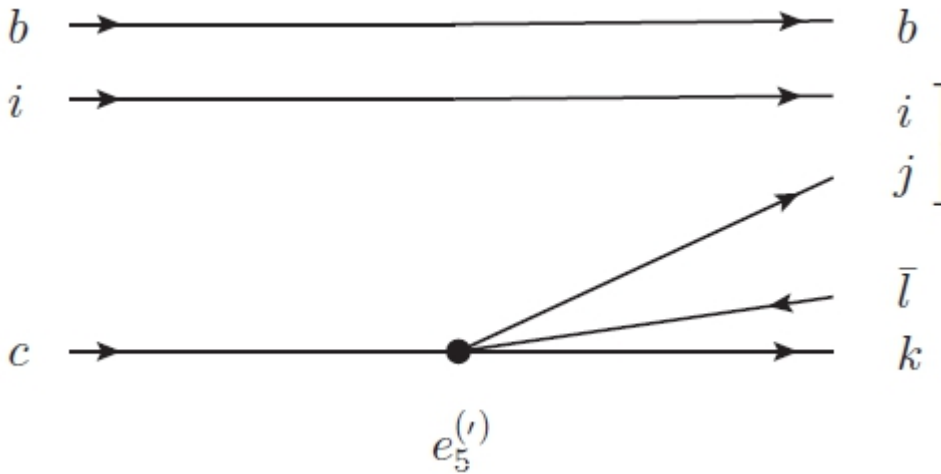


$$B_{bc} \rightarrow B_b^{(l)} + M$$



# $H_{ijk}^i$ induced decays

$$B_{bc} \rightarrow B_b^{(\prime)} + M$$



$$\left. \begin{array}{l} e_1 - e_5, e_2 + e_5 \\ e_3 - e_5, e_4 + e_5 \end{array} \right\}$$



**$e_5$  can be absorbed**

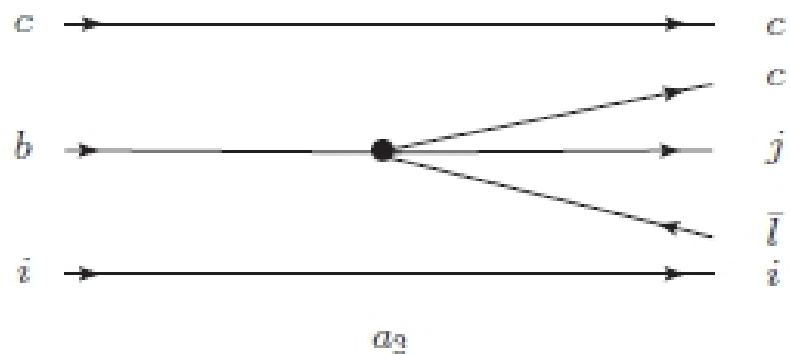
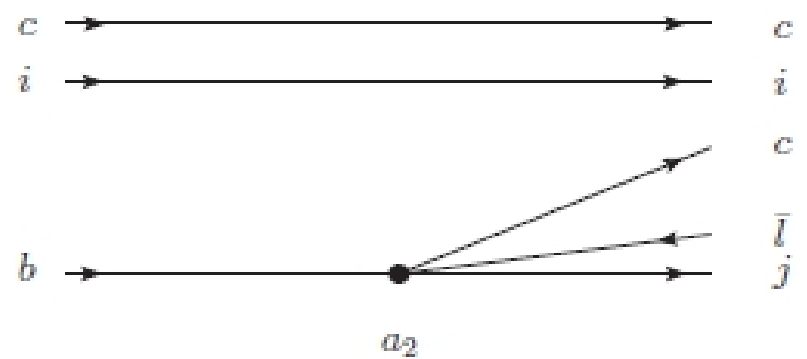
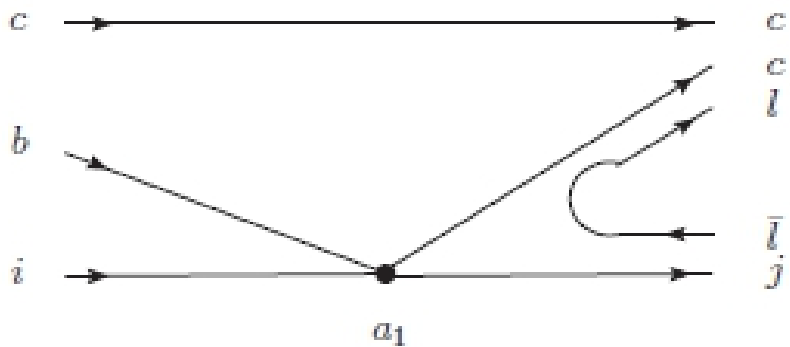
$$\begin{aligned} \mathcal{M}(\mathbf{B}_b) = & e_1 \mathbf{B}_{bc}^i H_i^{jk} \mathbf{B}_{b\ jl} M_k^l + e_2 \mathbf{B}_{bc}^i H_i^{jk} \mathbf{B}_{b\ kl} M_j^l + e_3 \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}_{b\ jk} M_i^l \\ & + e_4 \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}_{b\ ik} M_j^l + \underline{e_5 \mathbf{B}_{bc}^i H_l^{jk} \mathbf{B}_{b\ ij} M_k^l} \end{aligned}$$

$$\begin{aligned} \mathcal{M}(\mathbf{B}'_b) = & e'_1 \mathbf{B}'_{bc}^i H_i^{jk} \mathbf{B}'_{b\ jl} M_k^l + e'_2 \mathbf{B}'_{bc}^i H_i^{jk} \mathbf{B}'_{b\ kl} M_j^l + e'_3 \mathbf{B}'_{bc}^i H_l^{jk} \mathbf{B}'_{b\ jk} M_i^l \\ & + e'_4 \mathbf{B}'_{bc}^i H_l^{jk} \mathbf{B}'_{b\ ik} M_j^l + e'_5 \mathbf{B}'_{bc}^i H_l^{jk} \mathbf{B}'_{b\ ij} M_k^l \end{aligned}$$

# $H_j^i$ induced decays



$$B_{bc} \rightarrow B_{cc} + M$$



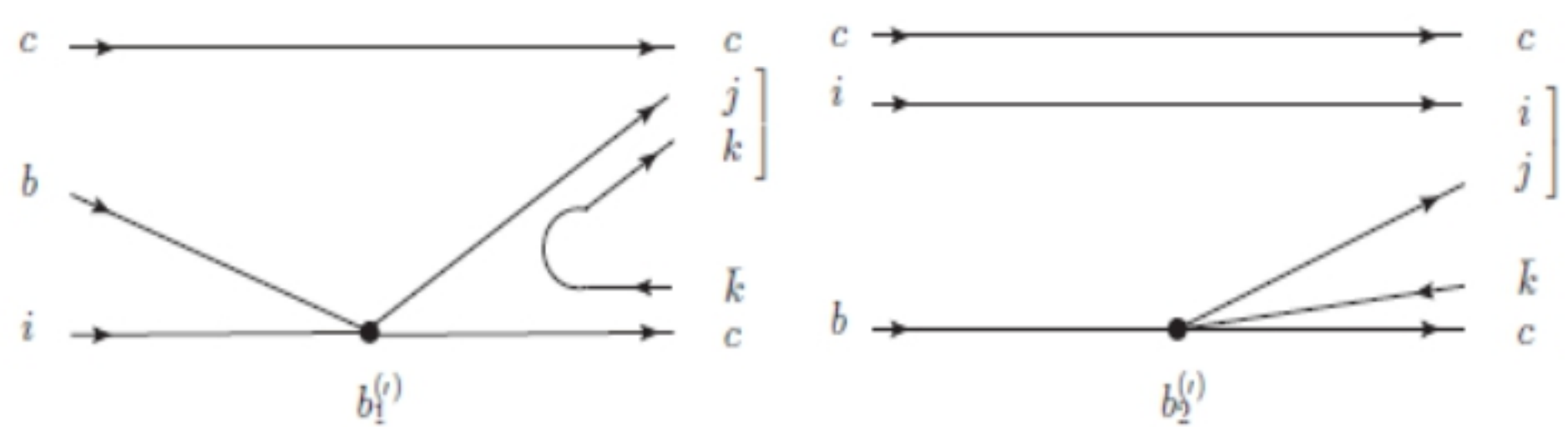
$$\mathcal{M} = a_1 \mathbf{B}_{bc}^i H_i^j \mathbf{B}_{cc l} M_j^l + a_2 \mathbf{B}_{bc}^i H_l^j \mathbf{B}_{cc i} M_j^l + a_3 \mathbf{B}_{bc}^i H_l^j \mathbf{B}_{cc j} M_i^l$$



# $H_j$ induced decays



$$B_{bc} \rightarrow B_c^{(l)} + M_c$$

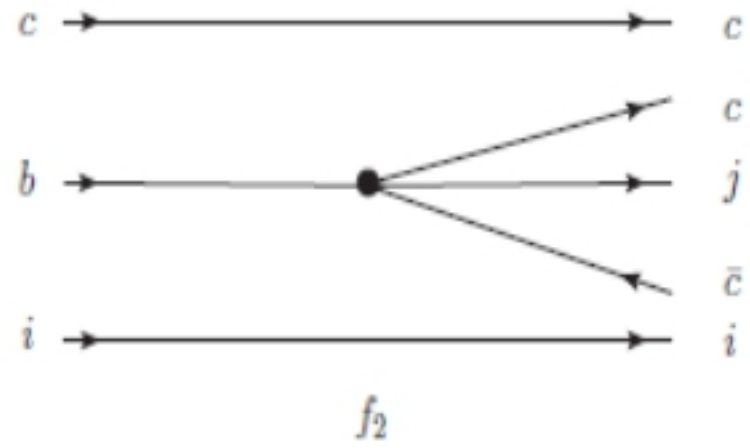
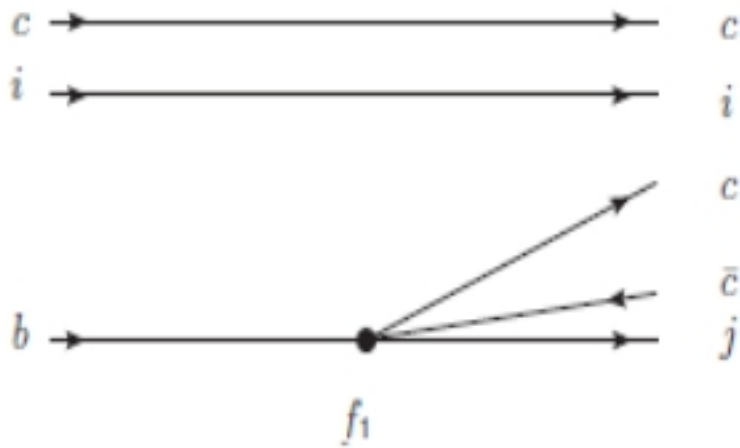


$$\mathcal{M} = b_1^{(l)} \mathbf{B}_{bc}^i H_i^j \mathbf{B}_{c jk} M_c^k + b_2^{(l)} \mathbf{B}_{bc}^i H_k^j \mathbf{B}_{c ji} M_c^k$$

# $H^i$ induced decays



$$B_{bc} \rightarrow B_{cc} + M_{\bar{c}}$$

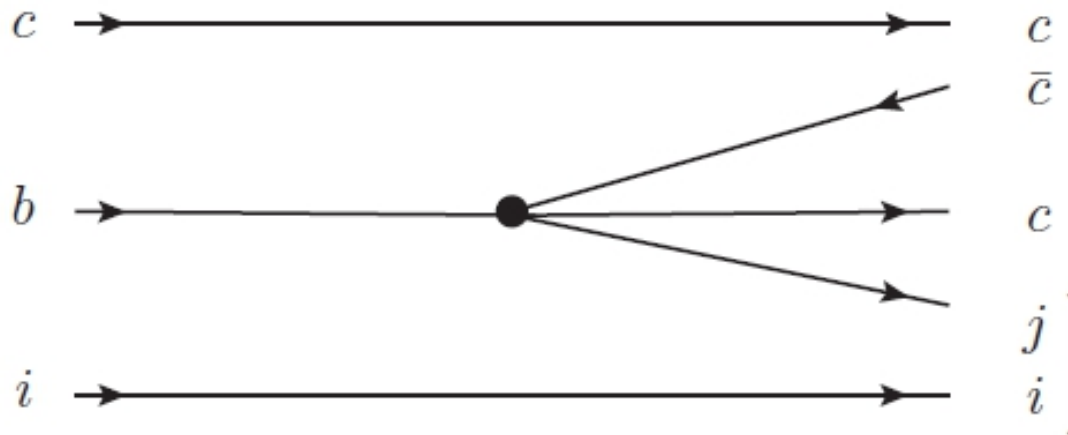


$$\mathcal{M} = f_1 \mathbf{B}_{bc}^i H^j \mathbf{B}_{cc i} M_{\bar{c} j} + f_2 \mathbf{B}_{bc}^i H^j \mathbf{B}_{cc j} M_{\bar{c} i}$$

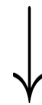
# $H^i$ induced decays



$$B_{bc} \rightarrow B_c^{(l)} + M_{c\bar{c}}$$



$$\mathcal{M} = g_{c\bar{c}}^{(l)} \mathbf{B}_{bc}^i H^j \mathbf{B}_{c ij}^{(l)} M_{c\bar{c}}$$



**Identifying dominant decay modes and relations for experiment**

## 1 **Effective Hamiltonian**

## 2 **Two Body Decay Modes**

## 3 **SU(3) Invariant Amplitudes**

## 4 **Experimental Analysis**

# Experimental Analysis



Experimental discovery {

1. Large branching ratios
2. Easily analyzed final states

Take  $c$  induced decays as example



Optimizing the identification of  $B_b^{(\prime)}$  to discover  $B_{bc}$

$b$  induced decays in backup

# Cabibbo allowed decays

$$B_{bc} \rightarrow B^{(\prime)} + M_b$$



Decay modes	Amplitudes	Decay modes	Amplitudes
$\Xi_{bc}^0 \rightarrow \Xi^0 \bar{B}_s^0$	$\lambda_{ds} d_2$	$\Xi_{bc}^0 \rightarrow \Sigma'^+ B^-$	$\lambda_{ds} \frac{1}{\sqrt{3}} d'_1$
$\Omega_{bc}^0 \rightarrow \Xi^0 \bar{B}^0$	$\lambda_{ds} d_4$	$\Xi_{bc}^0 \rightarrow \Xi'^0 \bar{B}_s^0$	$\lambda_{ds} \frac{1}{\sqrt{2}} d'_1$
$\Xi_{bc}^0 \rightarrow \Sigma^+ B^-$	$-\lambda_{ds} (d_1 - d_2)$	$\Omega_{bc}^0 \rightarrow \Xi'^0 \bar{B}^0$	$\lambda_{ds} \frac{1}{\sqrt{3}} d'_2$
$\Xi_{bc}^+ \rightarrow \Sigma^+ \bar{B}^0$	$-\lambda_{ds} (d_3 - d_4)$	$\Xi_{bc}^+ \rightarrow \Sigma'^+ \bar{B}^0$	$\lambda_{ds} \frac{1}{\sqrt{3}} d'_2$
$\Xi_{bc}^0 \rightarrow \Lambda \bar{B}^0$	$\lambda_{ds} \frac{1}{\sqrt{6}} (d_1 + d_2 + d_3 + d_4)$	$\Xi_{bc}^0 \rightarrow \Sigma'^0 \bar{B}^0$	$\lambda_{ds} \frac{1}{\sqrt{6}} (d'_1 + d'_2)$
$\Xi_{bc}^0 \rightarrow \Sigma^0 \bar{B}^0$	$\lambda_{ds} \frac{1}{\sqrt{2}} (d_1 - d_2 + d_3 - d_4)$		

## Triangle relation

$$\mathcal{M}(\Xi_{bc}^0 \rightarrow \Sigma'^+ B^-) = \mathcal{M}(\Xi_{bc}^0 \rightarrow \Xi'^0 \bar{B}_s^0) \quad \mathcal{M}(\Omega_{bc}^0 \rightarrow \Xi'^0 \bar{B}^0) = \mathcal{M}(\Xi_{bc}^+ \rightarrow \Sigma'^+ \bar{B}^0)$$

$$\mathcal{M}(\Xi_{bc}^0 \rightarrow \Sigma'^+ B^-) + \mathcal{M}(\Xi_{bc}^+ \rightarrow \Sigma'^+ \bar{B}^0) = \sqrt{2} \mathcal{M}(\Xi_{bc}^0 \rightarrow \Sigma'^0 \bar{B}^0)$$

# Cabibbo allowed decays



$$B_{bc} \rightarrow B_b^{(\prime)} + M$$

Decay modes	Amplitudes	Decay modes	Amplitudes
$\Xi_{bc}^0 \rightarrow \Xi_b^- \pi^+$	$-\lambda_{ds} e_1$	$\Xi_{bc}^0 \rightarrow \Omega_b^- K^+$	$\lambda_{ds} e'_1$
$\Xi_{bc}^+ \rightarrow \Xi_b^0 \pi^+$	$-\lambda_{ds} e_3$	$\Xi_{bc}^0 \rightarrow \Sigma_b^+ K^-$	$\lambda_{ds} e'_2$
$\Xi_{bc}^0 \rightarrow \Xi_b^0 \pi^0$	$\lambda_{ds} \frac{-1}{\sqrt{2}} (e_1 - e_3)$	$\Xi_{bc}^0 \rightarrow \Xi_b^{\prime 0} \eta$	$\lambda_{ds} \frac{1}{2\sqrt{3}} (e'_1 - 2e'_2 + e'_3)$
$\Omega_{bc}^0 \rightarrow \Xi_b^0 \bar{K}^0$	$-\lambda_{ds} (e_3 + e_4)$	$\Xi_{bc}^+ \rightarrow \Sigma_b^+ \bar{K}^0$	$\lambda_{ds} e'_4$
$\Xi_{bc}^0 \rightarrow \Xi_b^0 \eta$	$\lambda_{ds} \frac{-1}{\sqrt{6}} (e_1 + 2e_2 + e_3)$	$\Omega_{bc}^0 \rightarrow \Omega_b^- \pi^+$	$\lambda_{ds} e'_5$
$\Xi_{bc}^0 \rightarrow \Lambda_b \bar{K}^0$	$\lambda_{ds} (e_2 - e_4)$	$\Xi_{bc}^0 \rightarrow \Xi_b^{\prime 0} \pi^0$	$\lambda_{ds} \frac{1}{2} (e'_1 - e'_3)$
		$\Xi_{bc}^+ \rightarrow \Xi_b^{\prime 0} \pi^+$	$\lambda_{ds} \frac{1}{\sqrt{2}} (e'_3 + e'_5)$
		$\Xi_{bc}^0 \rightarrow \Xi_b^{\prime -} \pi^+$	$\lambda_{ds} \frac{1}{\sqrt{2}} (e'_1 + e'_5)$
		$\Xi_{bc}^0 \rightarrow \Sigma_b^0 \bar{K}^0$	$\lambda_{ds} \frac{1}{\sqrt{2}} (e'_2 + e'_4)$
		$\Omega_{bc}^0 \rightarrow \Xi_b^{\prime 0} \bar{K}^0$	$\lambda_{ds} \frac{1}{\sqrt{2}} (e'_3 + e'_4)$

$$\mathcal{M}(\Xi_{bc}^+ \rightarrow \Xi_b^0 \pi^+) - \mathcal{M}(\Xi_{bc}^0 \rightarrow \Xi_b^- \pi^+) = -\sqrt{2} \mathcal{M}(\Xi_{bc}^0 \rightarrow \Xi_b^0 \pi^0)$$

$$\mathcal{M}(\Xi_{bc}^+ \rightarrow \Sigma_b^+ \bar{K}^0) + \mathcal{M}(\Xi_{bc}^0 \rightarrow \Sigma_b^+ K^-) = \sqrt{2} \mathcal{M}(\Xi_{bc}^0 \rightarrow \Sigma_b^0 \bar{K}^0)$$

# Cabibbo allowed decays



The above give all Cabibbo allowed decay modes

Cabibbo allowed decay modes  $\left\{ \begin{array}{l} \text{dominant} \\ \text{most likely to-be-discovered} \end{array} \right.$

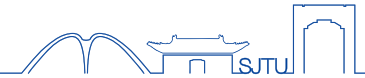
$$\Gamma(\Xi_{Qc} \rightarrow \Xi_Q \pi^+) = \frac{G_F^2}{32\pi} (\lambda_{ds} a_1 f_\pi)^2 m_{\Xi_{Qc}}^3 (1 - m_{\Xi_Q}^2 / m_{\Xi_{Qc}}^2)^3 \underline{(f_1^2 + g_1^2)}$$

$$\downarrow \quad \langle \Xi_Q | (\bar{s}c) | \Xi_{Qc} \rangle \simeq \bar{u}_{\Xi_Q} (f_1 \gamma_\mu - g_1 \gamma_\mu \gamma_5) u_{\Xi_{Qc}}$$

$$\frac{\Gamma(\Xi_{bc}^+ \rightarrow \Xi_b^0 + \pi^+)}{\Gamma(\Xi_{cc}^{++} \rightarrow \Xi_c^+ + \pi^+)} \approx 1.4 \quad \longrightarrow \quad \mathcal{B}(\Xi_{bc}^+ \rightarrow \Xi_b^0 + \pi^+) \sim 10^{-2}$$



# Analysis for discovery in LHC



**b-meson**

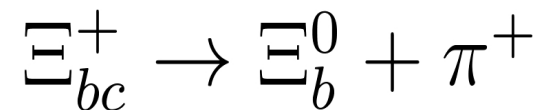
$$\mathcal{B}(\Xi_{bc}^0 \rightarrow \Lambda + \bar{B}^0) \sim 10^{-2}$$

$$\mathcal{B}(\Lambda \rightarrow p\pi^-) \simeq 64\%$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^+\pi^-) \simeq 2.5 \times 10^{-3}$$

$$\mathcal{B}(D^+ \rightarrow \pi^+\pi^0) \simeq 1.2 \times 10^{-3}$$

**10<sup>8</sup> events**



**b-baryon**

$$\mathcal{B}(\Xi_{bc}^+ \rightarrow \Xi_b^0 + \pi^+) \sim 10^{-2}$$

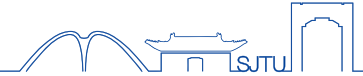
$$\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 J/\Psi) = 10^{-4} - 10^{-3}$$

$$\mathcal{B}(\Xi^0 \rightarrow \Lambda\pi^0, \Lambda \rightarrow p\pi^-) \simeq 64\%$$

$$\mathcal{B}(J/\Psi \rightarrow \mu^+\mu^- + e^+e^-) \simeq 12\%$$

**10<sup>6-7</sup> events**

# Conclusions



- 1.  $B_{bc}$  can exist and yet await to be discovered.**
- 2. We study two-body weak decays using SU(3) flavor symmetry to provide the promising modes for discovery.**
- 3. We analyze b/c induced two decay modes and get several relations among BR to test SU(3) flavor symmetry.**
- 4. We urge experimental colleagues to search for  $B_{bc}$  using two-body weak decays.**



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# Thanks!



# Backup



## Masses for heavy baryons and mesons

**bc baryon**  $m_{\Xi_{bc}} = 7.0 \text{ GeV}$ ,  $m_{\Omega_{bc}} = 7.3 \text{ GeV}$  Int.J.Mod.Phys.A23,2817(2008)

**cc baryon**  $m_{\Xi_{cc}^{++}} = m_{\Xi_{cc}^{+}} = 3.6212 \text{ GeV}$

**b baryon**  $m_{\Lambda_b^0} = 5.6196 \text{ GeV}$ ,  $m_{\Sigma_b^+} = 5.81056 \text{ GeV}$ ,  $m_{\Sigma_b^-} = 5.81564 \text{ GeV}$ ,

$m_{\Xi_b^0} = 5.7919 \text{ GeV}$ ,  $m_{\Xi_b^-} = 5.7970 \text{ GeV}$ ,  $m_{\Omega_b^-} = 6.0461 \text{ GeV}$ ,

**c baryon**  $m_{\Lambda_c^+} = 2.28246 \text{ GeV}$ ,  $m_{\Sigma_c^{++}} = 2.45397 \text{ GeV}$ ,  $m_{\Sigma_c^+} = 2.4529 \text{ GeV}$ ,  $m_{\Sigma_c^0} = 2.45375 \text{ GeV}$ ,

$m_{\Xi_c^+} = 2.46794 \text{ GeV}$ ,  $m_{\Xi_c^0} = 2.47090 \text{ GeV}$ ,  $m_{\Omega_c^0} = 2.6952 \text{ GeV}$ ,

**b meson**  $m_{B^\pm} = 5.27934 \text{ GeV}$ ,  $m_{B^0} = 5.27965 \text{ GeV}$ ,  $m_{B_s^0} = 5.36688 \text{ GeV}$ ,

**c meson**  $m_{D^\pm} = 1.86965 \text{ GeV}$ ,  $m_{D^0} = 1.86483 \text{ GeV}$ ,  $m_{D_s^\pm} = 1.96834 \text{ GeV}$ ,

# Example $\Xi_{Qc} \rightarrow \Xi_Q \pi^+$



## Momentum of CM

$$P_c = \frac{1}{2m_{B_{bc}}} \left[ m_{B_{bc}}^4 \left( 1 - \frac{(m_B + m_m)^2}{m_{B_{bc}}^2} \right) \left( 1 - \frac{(m_B - m_m)^2}{m_{B_{bc}}^2} \right) \right]^{1/2} \sim \frac{1}{2} m_{B_{bc}} \left( 1 - m_B^2/m_{B_{bc}}^2 \right)$$

**Factorize**  $A^2 \sim m_{B_{bc}}^2 \left( 1 - \frac{m_B}{m_{B_{bc}}} \right)^2 f_1^2$       $B^2 \sim m_{B_{bc}}^2 \left( 1 + \frac{m_B}{m_{B_{bc}}} \right)^2 g_1^2$       $\langle \pi^+ | (\bar{u}d) | 0 \rangle = i f_\pi q^\mu$

$$\mathcal{M}(\Xi_{Qc} \rightarrow \Xi_Q \pi^+) = i \lambda_{ds} a_1 f_\pi q^\mu \langle \Xi_Q | (\bar{s}c) | \Xi_{Qc} \rangle \simeq i \lambda_{ds} a_1 f_\pi q^\mu \bar{u}_{\Xi_Q} (f_1 \gamma_\mu - g_1 \gamma_\mu \gamma_5) u_{\Xi_{Qc}}$$

## Amplitude

$$\begin{aligned} |M|^2 &= A^2 (m_{B_{bc}} + m_B + m_m)(m_{B_{bc}} + m_B - m_m) + B^2 (m_{B_{bc}} - m_B - m_m)(m_{B_{bc}} - m_B - m_m) \\ &\sim m_{B_{bc}}^2 \left( 1 + \frac{m_B}{m_{B_{bc}}} \right)^2 A^2 + m_{B_{bc}}^2 \left( 1 - \frac{m_B}{m_{B_{bc}}} \right)^2 B^2 \sim m_{B_{bc}}^4 \left( 1 - \frac{m_B^2}{m_{B_{bc}}^2} \right)^2 (f_1^2 + g_1^2) \end{aligned}$$

## Decay width

$$\Gamma(\Xi_{Qc} \rightarrow \Xi_Q \pi^+) = \frac{G_F^2}{2} \frac{P_c}{8\pi m_{B_{bc}}^2} |M|^2 = \frac{G_F^2}{32\pi} (\lambda_{ds} a_1 f_\pi)^2 m_{\Xi_{Qc}}^3 \left( 1 - m_{\Xi_Q}^2/m_{\Xi_{Qc}}^2 \right)^3 (f_1^2 + g_1^2)$$

# b induced decay $|V_{cb}/V_{cs}| \simeq 0.04$



Decay modes	Amplitudes	Decay modes	Amplitudes
$\Xi_{bc}^+ \rightarrow \Omega_{cc}^+ K^0$	$\lambda_{ud}^c a_1$	$\Xi_{bc}^+ \rightarrow \Xi_{cc}^0 D_s^+$	$\lambda_{ud}^c b_1$
$\Xi_{bc}^+ \rightarrow \Xi_{cc}^+ \bar{K}^0$	$\lambda_{us}^c a_1$	$\Xi_{bc}^+ \rightarrow \Xi_{cc}^+ D^+$	$-\lambda_{us}^c b_1$
$\Omega_{bc}^0 \rightarrow \Omega_{cc}^+ \pi^-$	$\lambda_{ud}^c a_2$	$\Omega_{bc}^0 \rightarrow \Xi_{cc}^0 D^0$	$\lambda_{ud}^c b_2$
$\Xi_{bc}^0 \rightarrow \Xi_{cc}^+ K^-$	$\lambda_{us}^c a_2$	$\Xi_{bc}^0 \rightarrow \Xi_{cc}^0 D^0$	$-\lambda_{us}^c b_2$
$\Omega_{bc}^0 \rightarrow \Xi_{cc}^+ K^-$	$\lambda_{ud}^c a_3$	$\Xi_{bc}^+ \rightarrow \Lambda_{cc}^+ D^0$	$-\lambda_{ud}^c (b_1 + b_2)$
$\Xi_{bc}^0 \rightarrow \Omega_{cc}^+ \pi^-$	$\lambda_{us}^c a_3$	$\Xi_{bc}^+ \rightarrow \Xi_{cc}^+ D^0$	$-\lambda_{us}^c (b_1 + b_2)$
$\Xi_{bc}^+ \rightarrow \Omega_{cc}^+ \pi^0$	$\lambda_{us}^c \frac{1}{\sqrt{2}} a_3$		
<b><math>\Xi_{bc}^+ \rightarrow \Xi_{cc}^{++} \pi^-</math></b>	$\lambda_{ud}^c (a_1 + a_2)$	$\Xi_{bc}^+ \rightarrow \Sigma_{cc}^0 D^+$	$\lambda_{ud}^c b'_1$
$\Xi_{bc}^+ \rightarrow \Xi_{cc}^{++} K^-$	$\lambda_{us}^c (a_1 + a_2)$	$\Xi_{bc}^+ \rightarrow \Omega_{cc}^0 D_s^+$	$\lambda_{us}^c b'_1$
$\Xi_{bc}^0 \rightarrow \Xi_{cc}^+ \pi^-$	$\lambda_{ud}^c (a_2 + a_3)$	$\Xi_{bc}^+ \rightarrow \Xi_c^{\prime 0} D_s^+$	$\lambda_{ud}^c \frac{1}{\sqrt{2}} b'_1$
$\Omega_{bc}^0 \rightarrow \Omega_{cc}^+ K^-$	$\lambda_{us}^c (a_2 + a_3)$	$\Xi_{bc}^+ \rightarrow \Xi_c^{\prime 0} D^+$	$\lambda_{us}^c \frac{1}{\sqrt{2}} b'_1$
$\Xi_{bc}^+ \rightarrow \Xi_{cc}^+ \eta$	$\lambda_{ud}^c \frac{1}{\sqrt{6}} (a_1 + a_3)$	$\Xi_{bc}^0 \rightarrow \Sigma_{cc}^0 D^0$	$\lambda_{ud}^c b'_2$
$\Xi_{bc}^+ \rightarrow \Xi_{cc}^+ \pi^0$	$\lambda_{ud}^c \frac{-1}{\sqrt{2}} (a_1 - a_3)$	$\Omega_{bc}^0 \rightarrow \Xi_c^{\prime 0} D^0$	$\lambda_{ud}^c \frac{1}{\sqrt{2}} b'_2$
$\Xi_{bc}^+ \rightarrow \Omega_{cc}^+ \eta$	$\lambda_{us}^c \frac{-1}{\sqrt{6}} (2a_1 - a_3)$	$\Omega_{bc}^0 \rightarrow \Omega_{cc}^0 D^0$	$\lambda_{us}^c b'_2$
		$\Xi_{bc}^0 \rightarrow \Xi_c^{\prime 0} D^0$	$\lambda_{us}^c \frac{1}{\sqrt{2}} b'_2$
		<b><math>\Xi_{bc}^+ \rightarrow \Sigma_c^+ D^0</math></b>	$\lambda_{ud}^c \frac{1}{\sqrt{2}} (b'_1 + b'_2)$
		$\Xi_{bc}^+ \rightarrow \Xi_c^{\prime +} D^0$	$\lambda_{us}^c \frac{1}{\sqrt{2}} (b'_1 + b'_2)$

10<sup>-4</sup>

$$\mathcal{B}(\Xi_{bc}^+ \rightarrow \Sigma_c^+ D^0) \sim 10^{-6}$$

10<sup>-6</sup>

# b induced decay



$$B_{bc} \rightarrow B_{cc} + M_{c\bar{c}}$$

$$B_{bc} \rightarrow B_c^{(\prime)} + M_{c\bar{c}}$$

10-3

Decay modes	Amplitudes
$\Xi_{bc}^+ \rightarrow \Xi_{cc}^{++} D^-$	$\lambda_{cd}^c f_1$
$\Omega_{bc}^0 \rightarrow \Omega_{cc}^+ D^-$	$\lambda_{cd}^c f_1$
$\Xi_{bc}^+ \rightarrow \Xi_{cc}^{++} D_s^-$	$\lambda_{cs}^c f_1$
$\Xi_{bc}^0 \rightarrow \Xi_{cc}^+ D_s^-$	$\lambda_{cs}^c f_1$
$\Xi_{bc}^+ \rightarrow \Xi_c^+ \bar{D}^0$	$\lambda_{cd}^c f_2$
$\Omega_{bc}^0 \rightarrow \Xi_{cc}^+ D_s^-$	$\lambda_{cd}^c f_2$
$\Xi_{bc}^+ \rightarrow \Omega_{cc}^+ \bar{D}^0$	$\lambda_{cs}^c f_2$
$\Xi_{bc}^0 \rightarrow \Omega_{cc}^+ D^-$	$\lambda_{cs}^c f_2$
$\Xi_{bc}^0 \rightarrow \Xi_{cc}^+ D^-$	$\lambda_{cd}^c (f_1 + f_2)$
$\Omega_{bc}^0 \rightarrow \Omega_{cc}^+ D_s^-$	$\lambda_{cs}^c (f_1 + f_2)$

Decay modes	Amplitudes
$\Xi_{bc}^+ \rightarrow \Lambda_c^+ M_{c\bar{c}}$	$\lambda_{cd}^c g_{c\bar{c}}$
$\Omega_{bc}^0 \rightarrow \Xi_c^0 M_{c\bar{c}}$	$-\lambda_{cd}^c g_{c\bar{c}}$
$\Xi_{bc}^+ \rightarrow \Xi_c^+ M_{c\bar{c}}$	$\lambda_{cs}^c g_{c\bar{c}}$ <b>10-5</b>
$\Xi_{bc}^0 \rightarrow \Xi_c^0 M_{c\bar{c}}$	$\lambda_{cs}^c g_{c\bar{c}}$
$\Xi_{bc}^+ \rightarrow \Sigma_c^+ M_{c\bar{c}}$	$\lambda_{cd}^c \frac{1}{\sqrt{2}} g'_{c\bar{c}}$
$\Xi_{bc}^0 \rightarrow \Sigma_c^0 M_{c\bar{c}}$	$\lambda_{cd}^c g'_{c\bar{c}}$
$\Omega_{bc}^0 \rightarrow \Xi_c^{\prime 0} M_{c\bar{c}}$	$\lambda_{cd}^c \frac{1}{\sqrt{2}} g'_{c\bar{c}}$
$\Xi_{bc}^+ \rightarrow \Xi_c^{\prime +} M_{c\bar{c}}$	$\lambda_{cs}^c \frac{1}{\sqrt{2}} g'_{c\bar{c}}$
$\Xi_{bc}^0 \rightarrow \Xi_c^{\prime 0} M_{c\bar{c}}$	$\lambda_{cs}^c \frac{1}{\sqrt{2}} g'_{c\bar{c}}$
$\Omega_{bc}^0 \rightarrow \Omega_c^0 M_{c\bar{c}}$	$\lambda_{cs}^c g'_{c\bar{c}}$

# Analysis for discovery in LHC

$\Xi_{bc}^0 \rightarrow \Xi^0 B_s^0$	$\mathcal{B}(\Xi^0 \rightarrow \pi^0 (\Lambda \rightarrow) p \pi^-) \simeq 64\%$ , $\mathcal{B}(\bar{B}_s^0 \rightarrow \rho^- (D_s^+ \rightarrow) \pi^+ \pi^+ \pi^-) \simeq 7.5 \times 10^{-5}$	$10^7$
$\Xi_{bc}^0 \rightarrow \Sigma^+ B^-$	$\mathcal{B}(\Sigma^+ \rightarrow p \pi^0) \simeq 52\%$ , $\mathcal{B}(B^- \rightarrow \rho^- (D^0 \rightarrow) \pi^+ \pi^-) \simeq 2 \times 10^{-5}$	$10^7$
$\Xi_{bc}^+ \rightarrow \Sigma^+ \bar{B}^0$	$\mathcal{B}(\Sigma^+ \rightarrow p \pi^0) \simeq 52\%$ , $\mathcal{B}(\bar{B}^0 \rightarrow \pi^- (D^+ \rightarrow) \pi^+ \pi^0) \simeq 3 \times 10^{-6}$	$10^8$
$\Xi_{bc}^0 \rightarrow \Lambda \bar{B}^0$	$\mathcal{B}(\Lambda \rightarrow p \pi^-) \simeq 64\%$ , $\mathcal{B}(\bar{B}^0 \rightarrow \pi^- (D^+ \rightarrow) \pi^+ \pi^0) \simeq 3 \times 10^{-6}$	$10^8$
$\Xi_{bc}^0 \rightarrow \Sigma^0 \bar{B}^0$	$\mathcal{B}(\Sigma^0 \rightarrow \gamma (\Lambda \rightarrow) p \pi^-) \simeq 64\%$ , $\mathcal{B}(\bar{B}^0 \rightarrow \pi^- (D^+ \rightarrow) \pi^+ \pi^0) \simeq 3 \times 10^{-6}$	$10^8$
$\Xi_{bc}^0 \rightarrow \Xi_b^- \pi^+$	$\mathcal{B}(\Xi_b^- \rightarrow \Xi^- J/\Psi) = 10^{-4} - 10^{-3}$ , $\mathcal{B}(\Xi^- \rightarrow \pi^- (\Lambda \rightarrow) p \pi^-) \simeq 64\%$ , $\mathcal{B}(J/\Psi \rightarrow \ell^+ \ell^-) \simeq 12\%$	$10^{7-8}$
$\Xi_{bc}^+ \rightarrow \Xi_b^0 \pi^+$	$\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 J/\Psi) = 10^{-4} - 10^{-3}$ , $\mathcal{B}(\Xi^0 \rightarrow \pi^0 (\Lambda \rightarrow) p \pi^-) \simeq 64\%$ , $\mathcal{B}(J/\Psi \rightarrow \ell^+ \ell^-) \simeq 12\%$	$10^{7-8}$
$\Xi_{bc}^0 \rightarrow \Xi_b^0 \pi^0$	$\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 J/\Psi) = 10^{-4} - 10^{-3}$ , $\mathcal{B}(\Xi^0 \rightarrow \pi^0 (\Lambda \rightarrow) p \pi^-) \simeq 64\%$ , $\mathcal{B}(J/\Psi \rightarrow \ell^+ \ell^-) \simeq 12\%$	$10^{7-8}$
$\Xi_{bc}^0 \rightarrow \Xi_b^0 \eta$	$\mathcal{B}(\Xi_b^0 \rightarrow \Xi^0 J/\Psi) = 10^{-4} - 10^{-3}$ , $\mathcal{B}(\Xi^0 \rightarrow \pi^0 (\Lambda \rightarrow) p \pi^-) \simeq 64\%$ , $\mathcal{B}(J/\Psi \rightarrow \ell^+ \ell^-) \simeq 12\%$ , $\mathcal{B}(\eta \rightarrow \pi^+ \pi^- \pi^0) \simeq 23\%$	$10^{7-8}$
$\Xi_{bc}^0 \rightarrow \Lambda_b K^0$	$\mathcal{B}(\Lambda_b \rightarrow \Lambda J/\Psi) = 10^{-4} - 10^{-3}$ , $\mathcal{B}(\Lambda \rightarrow p \pi^-) \simeq 64\%$ , $\mathcal{B}(J/\Psi \rightarrow \ell^+ \ell^-) \simeq 12\%$ , $\mathcal{B}(\bar{K}_s^0 \rightarrow \pi \pi) \simeq 100\%$	$10^{7-8}$