

# Measurement of $H \rightarrow ZZ^*$ at the CEPC

Ryuta Kiuchi, Yanxi Gu, Min Zhong,  
Shih-Chieh Hsu, Xin Shi, Kaili Zhang

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# Introduction to HZZ channel

- Since the state has 3 Z bosons, there are multiple combinations of final products.
- Final states having  $(\mu^+\mu^-, jj, \nu\nu)$  are promising channels, owing to its clear signature. On the other hand, its low statistics could limit the final precision.
- This presentation summarizes the updated results from channels with the decay product combination of  $(\mu\mu, jj, \nu\nu)$

**Table : Promising decay product combinations**


Z / ZZ*				
$e^+e^-$	$\nu\nu jj$	$jj\nu\nu$		
$\mu^+\mu^-$	$\nu\nu jj$	$jj\nu\nu$		$jjjj$
$\nu\nu$	$e^+e^- jj$	$jje^+e^-$	$\mu^+\mu^- jj$	$jj\mu^+\mu^-$
$jj$	$e^+e^- \nu\nu$	$\nu\nu e^+e^-$	$\mu^+\mu^- \nu\nu$	$\nu\nu \mu^+\mu^-$

# Higgs boson width and HZZ measurement

• It is well known that the Higgs boson width and its precision can be deduced using the  $H \rightarrow ZZ^*$  precision using following relationship:

- $BR(H \rightarrow ZZ) = \Gamma(H \rightarrow ZZ) / \Gamma_H \propto g_{HZZ}^2 / \Gamma_H$

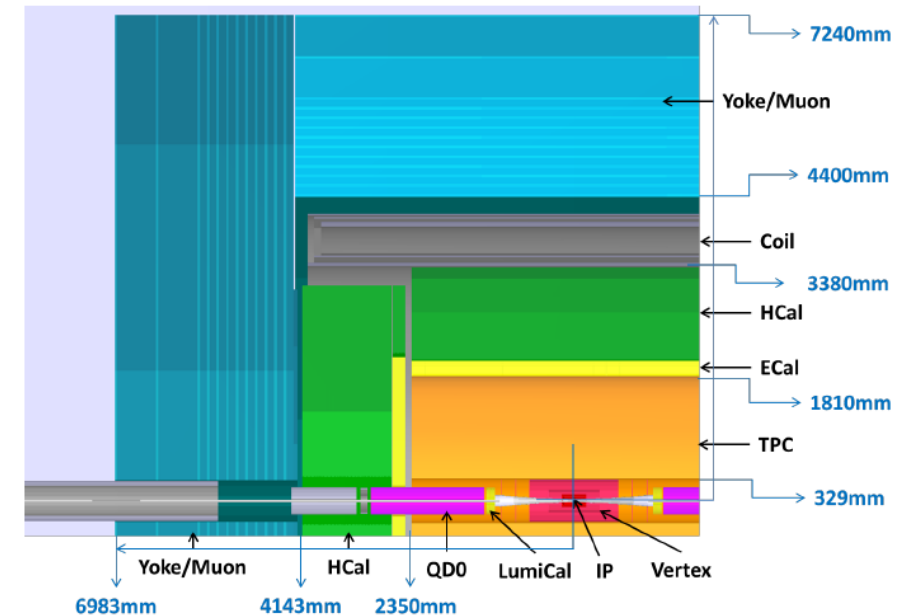
- $\sigma(ZH) \propto g_{HZZ}^2$

  $\sigma(ZH) \times BR(H \rightarrow ZZ) \propto \frac{g_{HZZ}^2 \times g_{HZZ}^2}{\Gamma_H}$

- Independent measurement of  $\sigma(ZH) \times BR(HZZ)$  and  $\sigma(ZH)$
- $H \rightarrow WW^*$  measurement can do the same calculation and current study shows that  $H \rightarrow WW^*$  precision will dominate the Higgs width precision ( please refer the CEPC white paper )

# Monte Carlo Simulation

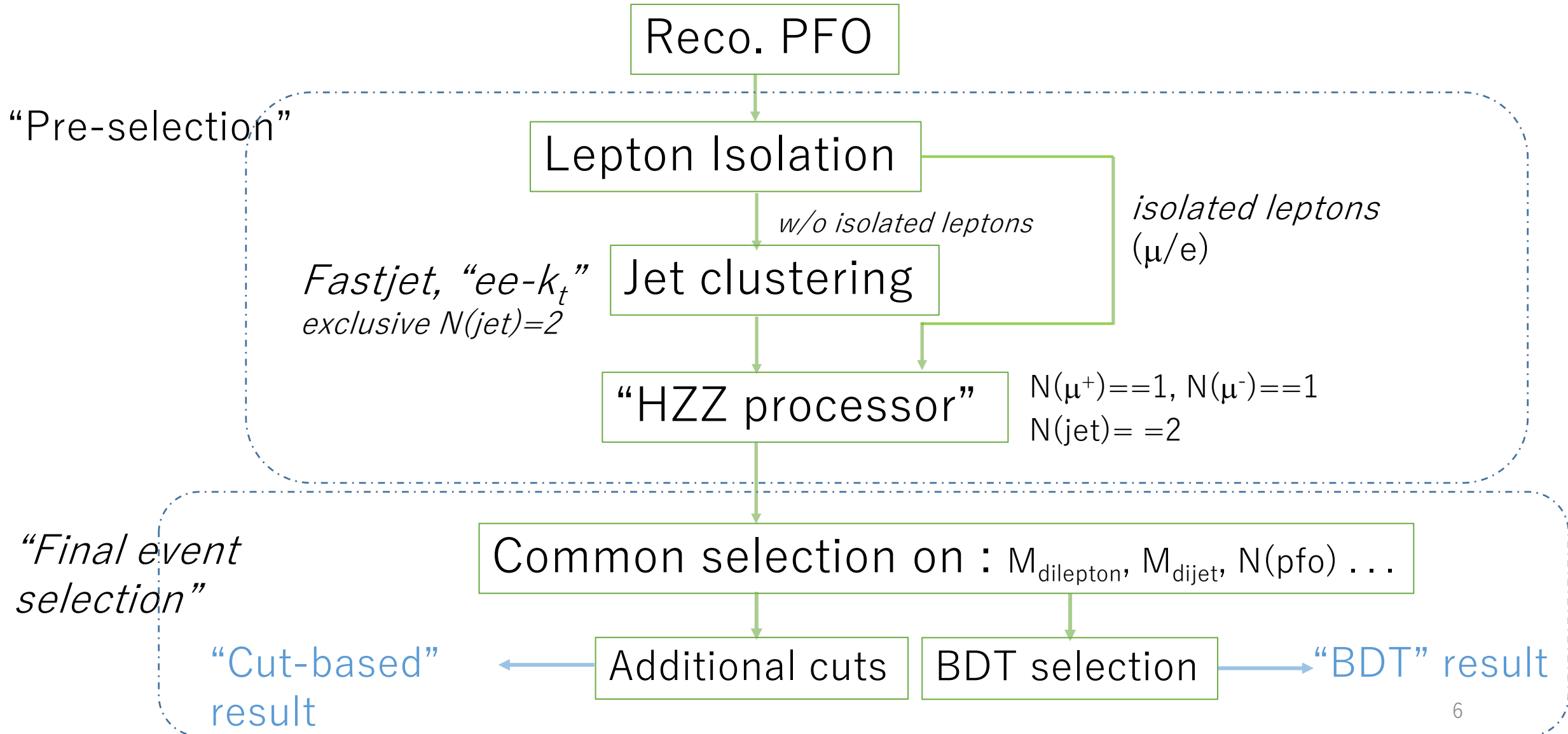
- CEPC\_v4 (240GeV, 3T) configuration
- Generator: Whizard 1.95 (with ISR,  $L=5.6 \text{ ab}^{-1}$ ,  $M_{\text{higgs}}=125 \text{ GeV}$ )
- Simulation :  
Geant4 and Mokka with ISR and bremsstrahlung effects
- Reconstruction:  
Marlin and ArborPFA



## Signal Sample

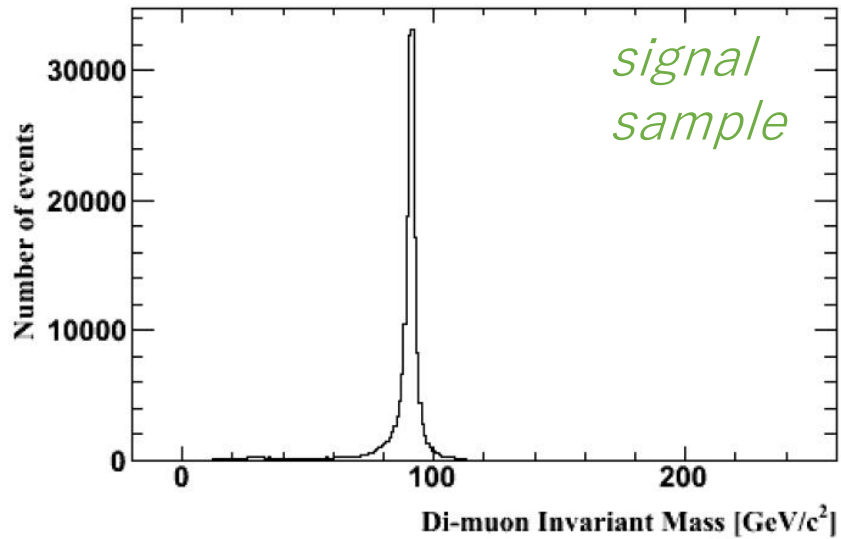
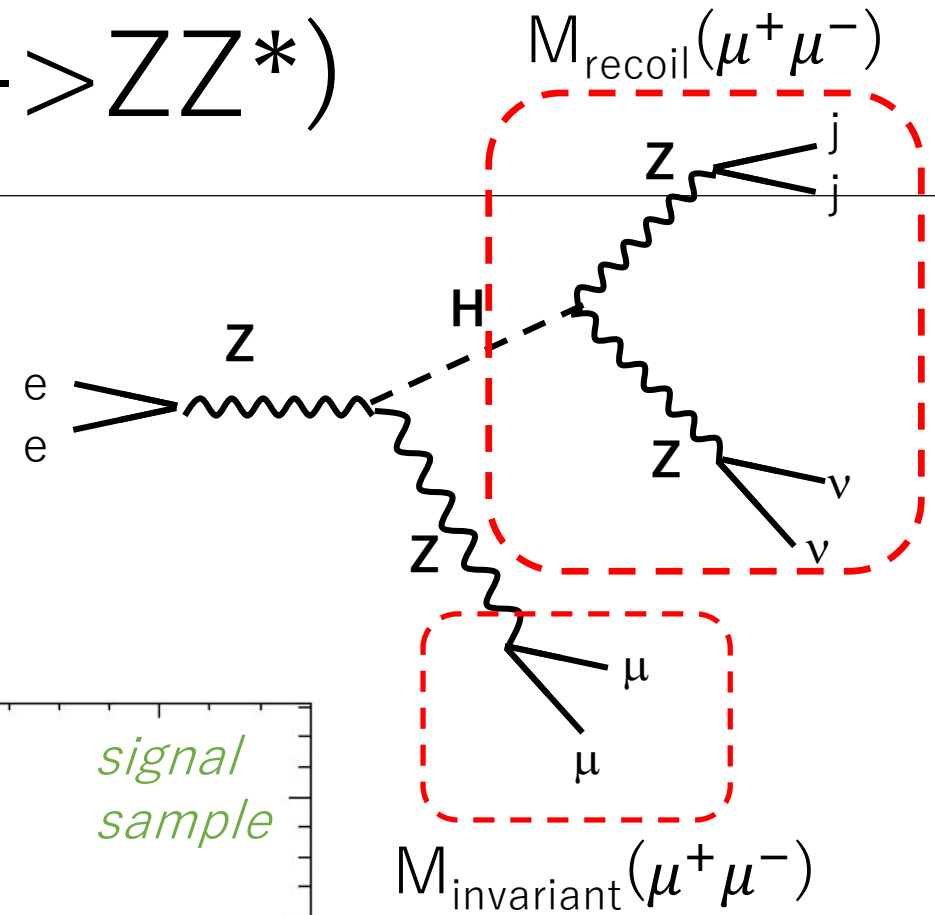
- $Z \rightarrow \mu\mu$ ,  $H \rightarrow ZZ^* \rightarrow \nu\nu q\bar{q}$
- $Z \rightarrow \nu\nu$ ,  $H \rightarrow ZZ^* \rightarrow \mu\mu q\bar{q}$
- $Z \rightarrow q\bar{q}$ ,  $H \rightarrow ZZ^* \rightarrow \nu\nu\mu\mu$

# Analysis flow chart

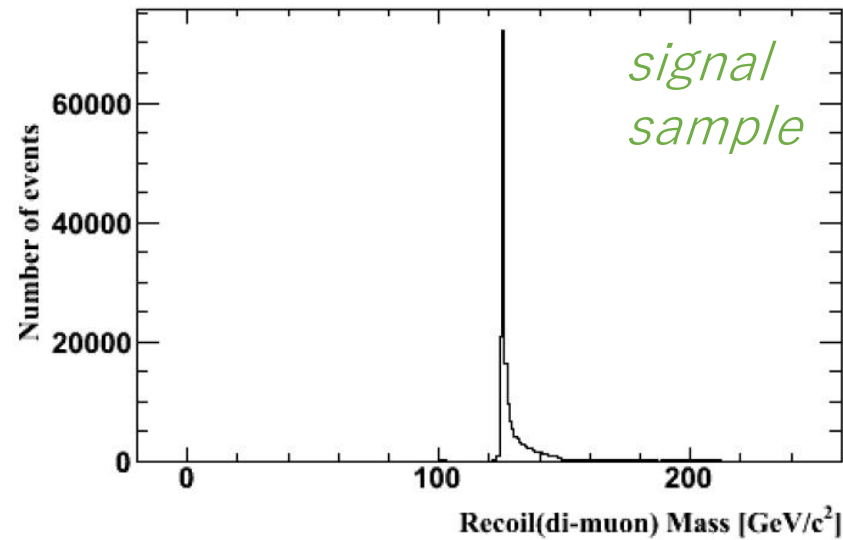


# Signature of $Z(\rightarrow \mu^+ \mu^-)H(\rightarrow ZZ^*)$

Identify two muons from initial Z boson using invariant & recoil mass as usual



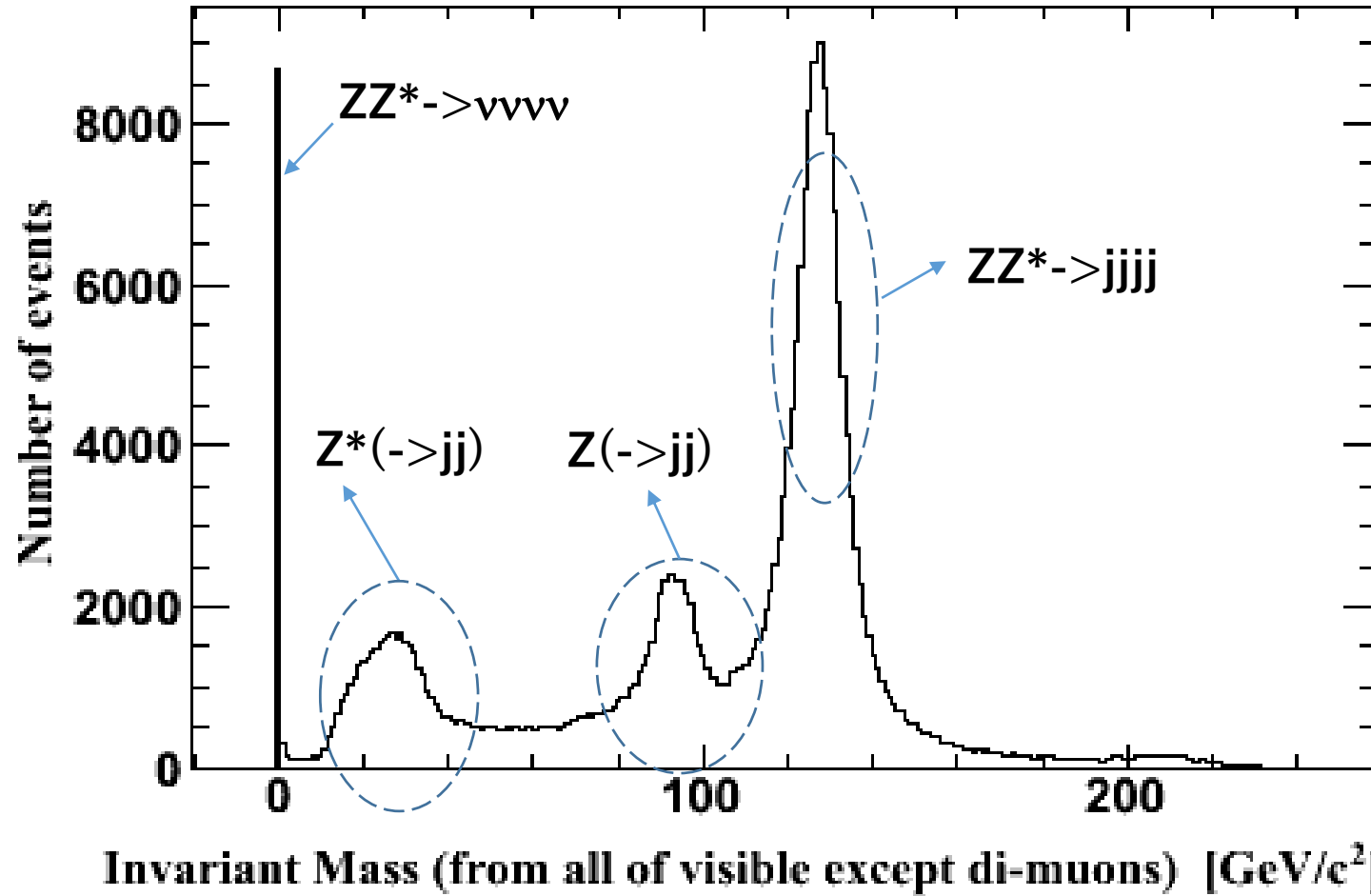
$M_{\text{Invariant}}(\mu^+\mu^-)$



$M_{\text{Recoil}}(\mu^+\mu^-)$

# Signature of $Z(->\mu^+\mu^-)H(->ZZ^*)$

# Distribution of invariant mass except two muons clearly shows each decay mode.



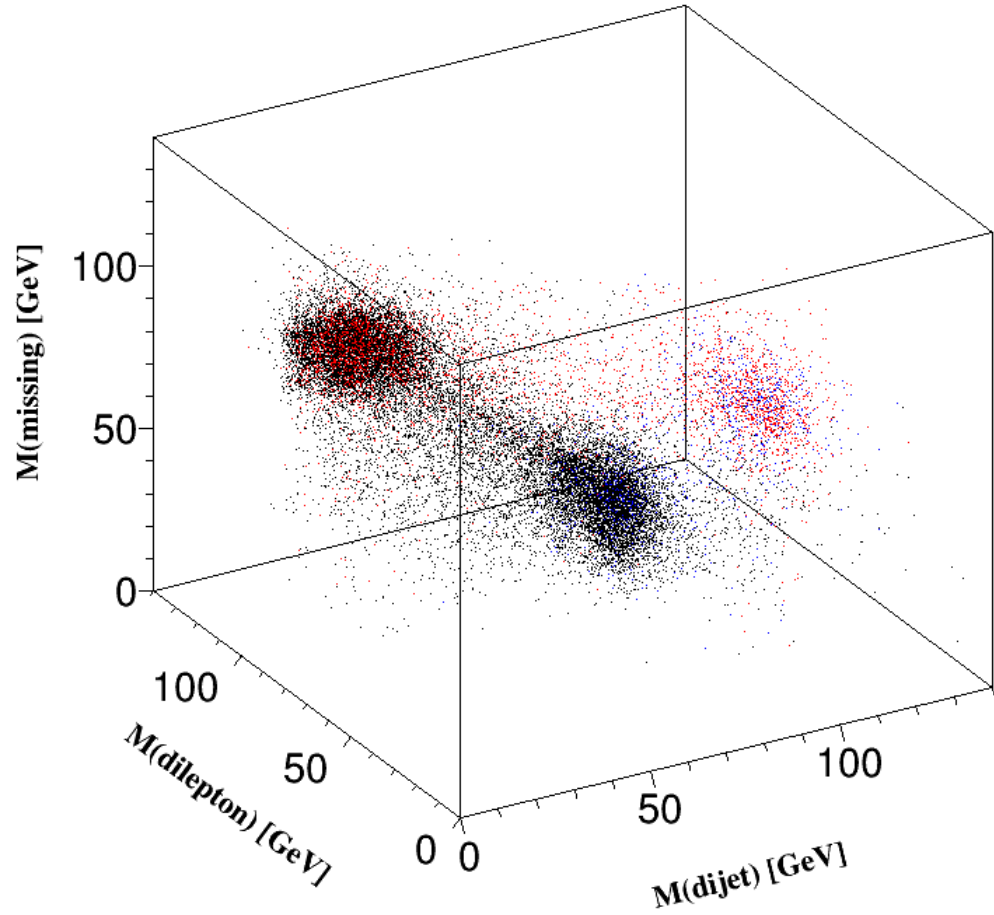
# Jet clustering  
 $N(\text{jet})=2$

# Note that above distribution is obtained by allowing  $ZZ^*(->4\nu)$  events to be saved, which are dropped normally in our analysis.



# Distribution in $M_{\mu\mu}$ - $M_{\nu\nu}$ - $M_{qq}$ space

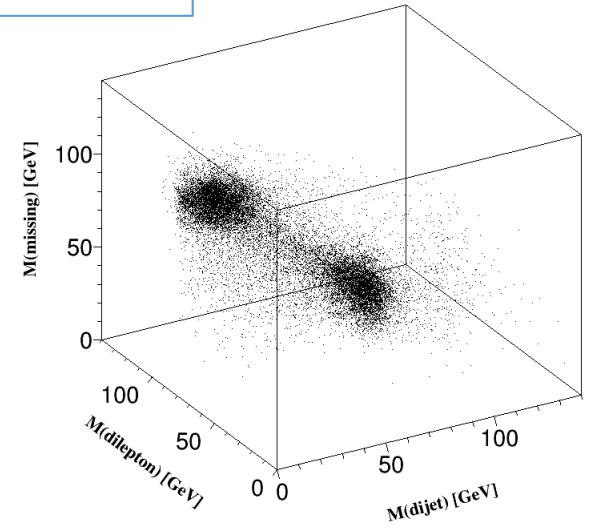
$ee \rightarrow ZH \rightarrow ZH(ZZ^*)$



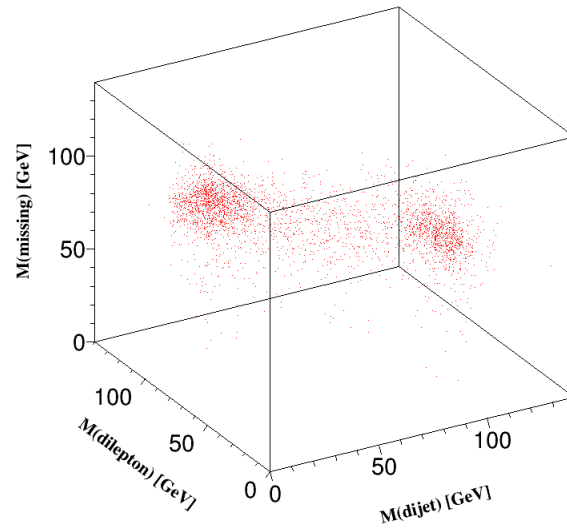
- $\mu\mu H\nu\nu qq$  ,  $\nu\nu H\mu\mu qq$
- $\nu\nu Hqq\mu\mu$  ,  $qqH\nu\nu\mu\mu$
- $qqH\mu\mu\nu\nu$  ,  $\mu\mu Hqq\nu\nu$



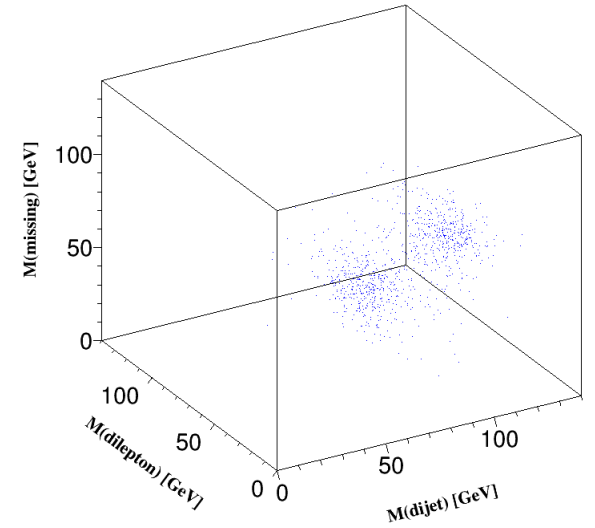
$\mu\mu HZZ$  signal



$\nu\nu HZZ$  signal

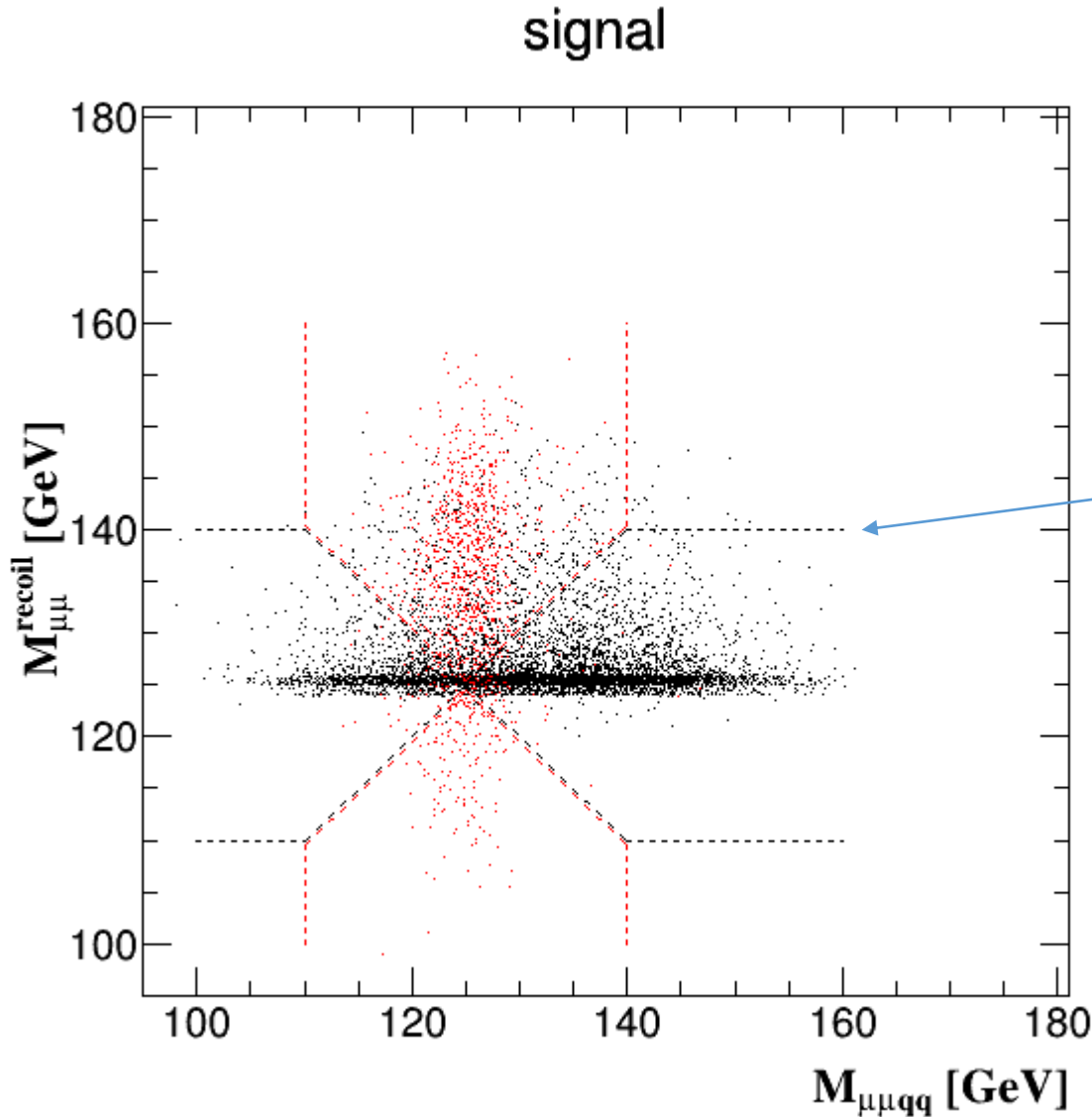


$qq HZZ$  signal



Each signal shows 2 separate distribution in this kinematic phase space.

# Separation on recoil mass distribution



- 2D Recoil mass distribution shows overlap of two signal channels

Black :  $Z \rightarrow \mu\mu, H \rightarrow ZZ^* \rightarrow \nu\nu qq$

Red :  $Z \rightarrow \nu\nu, H \rightarrow ZZ^* \rightarrow \mu\mu qq$

- To make each category exclusive, in other words, no double counting of events, “separation” has been performed on the recoil mass distribution.

# Overview table I. Cut-based analysis

**Table 1** Overview of the requirements applied when selecting events (cut-based).

Pre-selections						
$N(l) = 2$ , where leptons(l) should pass the isolation criteria						
$N(\mu^+) = 1, N(\mu^-) = 1$ with $E(\mu^\pm) > 3$ GeV						
$N(jet) = 2$						
Selection (Cut-based)	$\mu\mu H\nu\nu qq$	$\mu\mu Hqq\nu\nu$	$\nu\nu H\mu\mu qq$	$\nu\nu Hqq\mu\mu$	$qqH\nu\nu\mu\mu$	$qqH\mu\mu\nu\nu$
Mass order	$M_{\text{miss}} > M_{jj}$	$M_{\text{miss}} < M_{jj}$	$M_{\mu\mu} > M_{jj}$	$M_{\mu\mu} < M_{jj}$	$M_{\text{miss}} > M_{\mu\mu}$	$M_{\text{miss}} < M_{\mu\mu}$
$M_{\mu\mu}$ (GeV)	[80, 100]		[60, 100]	[10, 60]	[15, 55]	[75, 100]
$M_{jj}$ (GeV)	[15, 60]	[60, 105]	[10, 55]	[60, 100]		[75, 105]
$M_{\text{miss}}$ (GeV)	[75, 105]	[10, 55]		[75, 110]	[70, 110]	[10, 50]
$M_{\mu\mu}^{\text{recoil}}$ (GeV)	[110, 140]		-	-	[175, 215]	[115, 155]
$M_{\text{vis}}$ (GeV)	-	[175, 215]		[110, 140]	[115, 155]	[185, 215]
$M_{jj}^{\text{recoil}}$ (GeV)	[185, 220]	-	-	-		[110, 140]
$N_{\text{PFO}}$	[20, 90]	[30, 100]	[20, 60]	[30, 100]	[40, 95]	[40, 95]
$ \cos\theta_{\text{vis}} $				< 0.95		
$\Delta\phi_{ZZ}$ (degree)	[60, 170]	[60, 170]	< 135	< 135	-	[120, 170]
Region masking	<i>not-<math>\nu\nu HZZ</math> &amp; not-<math>qq HZZ</math></i>		<i>not-<math>\mu\mu HZZ</math> &amp; not-<math>qq HZZ</math></i>		<i>not-<math>\nu\nu HZZ</math> &amp; not-<math>\mu\mu HZZ</math></i>	

# Overview table II. BDT-based analysis

**Table 3** Overview of the requirements applied when selecting events (BDT-based).

Pre-selections						
$N(l) = 2$ , where leptons(l) should pass the isolation criteria						
$N(\mu^+) = 1, N(\mu^-) = 1$ with $E(\mu^\pm) > 3$ GeV						
$N(jet) = 2$						
Selection (MVA)	$\mu\mu H\nu\nu qq$	$\mu\mu Hqq\nu\nu$	$\nu\nu H\mu\mu qq$	$\nu\nu Hqq\mu\mu$	$qq H\nu\nu\mu\mu$	$qq H\mu\mu\nu\nu$
Mass order	$M_{\text{miss}} > M_{jj}$	$M_{\text{miss}} < M_{jj}$	$M_{\mu\mu} > M_{jj}$	$M_{\mu\mu} < M_{jj}$	$M_{\text{miss}} > M_{\mu\mu}$	$M_{\text{miss}} < M_{\mu\mu}$
$M_{\mu\mu}$ (GeV)		[80,100]	-	-	-	-
$M_{jj}$ (GeV)	-	-	-	-	[75, 105]	-
$M_{\text{miss}}$ (GeV)	-	-	[75, 110]	-	-	-
$M_{\mu\mu}^{\text{recoil}}$ (GeV)	[110, 140]	-	-	-	-	-
$M_{\text{vis}}$ (GeV)	-	-	[110, 140]	-	-	-
$M_{jj}^{\text{recoil}}$ (GeV)	-	-	-	-	[110, 140]	-
$N_{\text{PFO}}$	[20, 90]	[30, 100]	[20, 60]	[30, 100]	[40, 95]	[40, 95]
$ \cos\theta_{\text{vis}} $	< 0.95					
Region masking	<i>not-<math>\nu\nu HZZ</math> &amp; not-<math>qq HZZ</math></i>		<i>not-<math>\mu\mu HZZ</math> &amp; not-<math>qq HZZ</math></i>		<i>not-<math>\nu\nu HZZ</math> &amp; not-<math>\mu\mu HZZ</math></i>	
<i>BDT score</i>	> 0.14	> 0.01	> -0.01	> -0.01	> -0.04	> -0.01

# Number of expected events & efficiency

**Table 2** Summary of the selection efficiency  $\epsilon$  and the number of expected events  $N_{evt.}$  for each category after the final event selection in the cut-based analysis..

(Cut-based)	$\mu\mu H\nu\nu qq$		$\mu\mu Hqq\nu\nu$		$\nu\nu H\mu\mu qq$	
Process	$\epsilon$ [%]	$N_{evt.}$	$\epsilon$ [%]	$N_{evt.}$	$\epsilon$ [%]	$N_{evt.}$
Signal (“dominant”)	38	53	36	50	54	76
Signal (“sub”)	6	8	10	14	6	9
Higgs decays Bg.	$2.2 \cdot 10^{-3}$	25	$7.0 \cdot 10^{-2}$	794	$5.3 \cdot 10^{-4}$	6
SM four-fermion Bg.	$3.7 \cdot 10^{-6}$	4	$4.9 \cdot 10^{-4}$	520	$5.6 \cdot 10^{-6}$	6
SM two-fermion Bg.	0	0	0	0	0	0
	$\nu\nu Hqq\mu\mu$		$qqH\nu\nu\mu\mu$		$qqH\mu\mu\nu\nu$	
Process	$\epsilon$ [%]	$N_{evt.}$	$\epsilon$ [%]	$N_{evt.}$	$\epsilon$ [%]	$N_{evt.}$
Signal (“dominant”)	36	51	26	37	23	32
Signal (“sub”)	8	11	7	10	4	6
Higgs decays Bg.	$1.0 \cdot 10^{-2}$	114	$2.4 \cdot 10^{-2}$	275	$1.4 \cdot 10^{-2}$	160
SM four-fermion Bg.	$4.3 \cdot 10^{-5}$	46	$1.5 \cdot 10^{-4}$	157	$1.8 \cdot 10^{-4}$	190
SM two-fermion Bg.	0	0	0	0	0	0

- Signal efficiency : 27 - 60 %

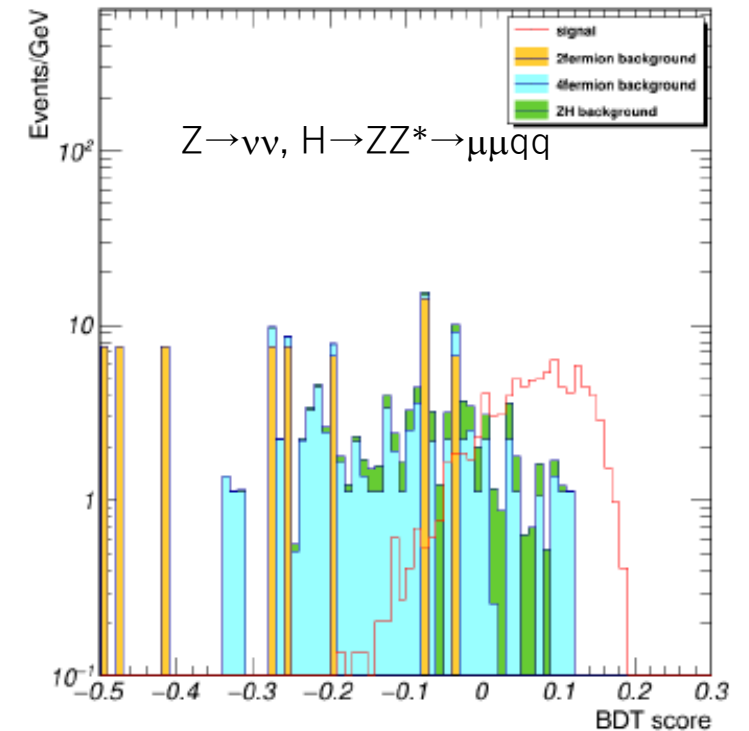
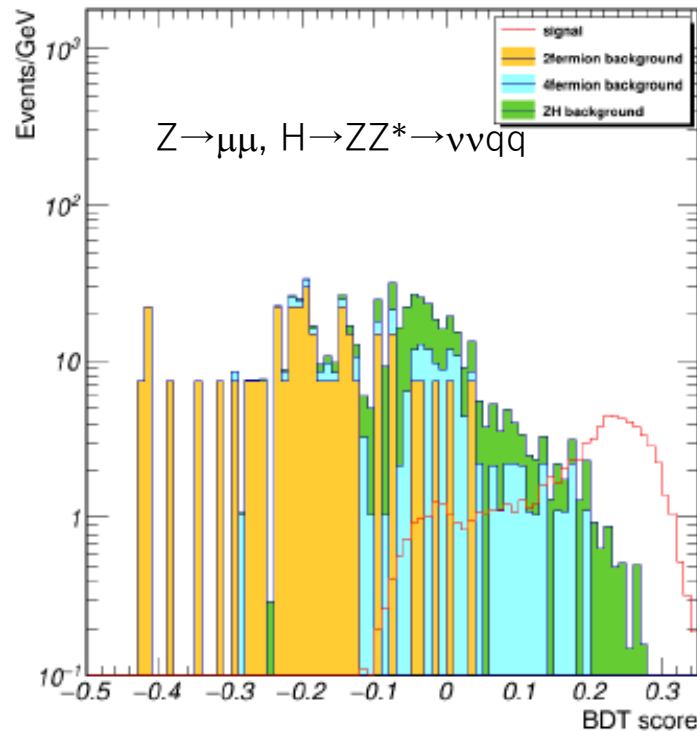
# BDT analysis

- BDT training and cuts are applied after several simple cuts :  $M_{xx}$ ,  $M^{\text{recoil}}_{xx}$ ,  $N_{\text{pfo}}$ ,  $\cos\theta$ , etc.

- BDT cut position is optimized based on the measure,  $S/\sqrt{S+B}$ , which to be maximized.

## Variables used in the BDT

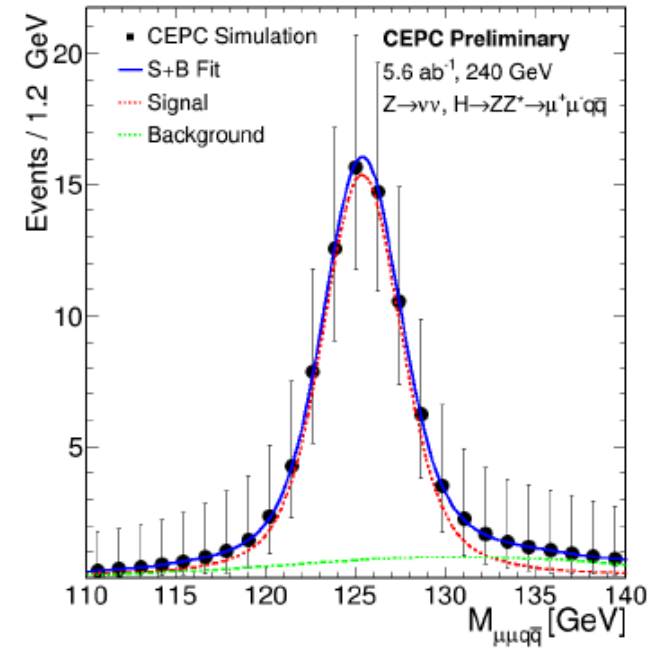
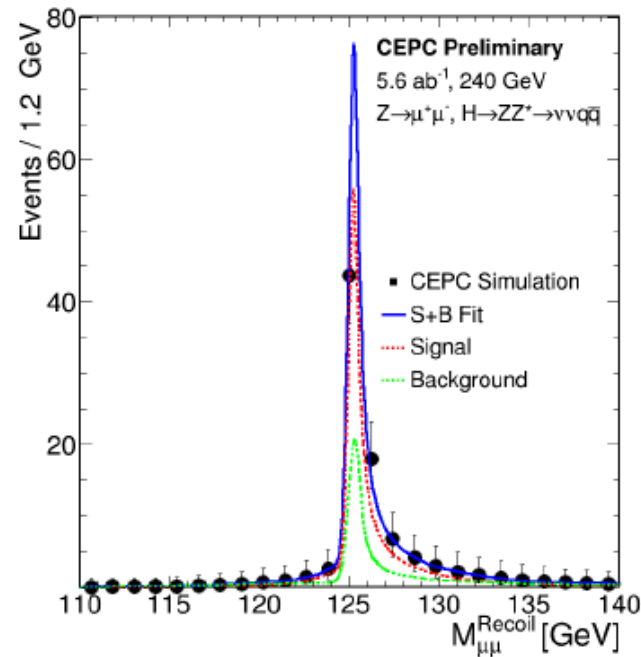
$P_{\text{all visible}}$	$E_{\text{leading-jet}}$	$\text{Cos}(\theta)$
$P_{t_{\text{all visible}}}$	$E_{\text{sub-leading-jet}}$	$(\text{Recoil}M_{\text{dimuon}})$
$M_{\text{dijet}}$	$N(\text{pfo})$	$(M_{\text{all visible}})$
$M_{\text{dimuon}}$	$\text{Angle}_{(\text{dijet-dimuon})}$	



# Obtained precision

Obtained uncertainty from each category. Both of cut-based and BDT-based results are shown together.

Category	$\frac{\Delta(\sigma \cdot BR)}{(\sigma \cdot BR)}$ [%]	
	cut-based	BDT
$\mu\mu H\nu\nu qq^{cut/mva}$	15.5	13.6
$\mu\mu Hqq\nu\nu^{cut/mva}$	48.0	42.1
$\nu\nu H\mu\mu qq^{cut/mva}$	11.9	12.5
$\nu\nu Hqq\mu\mu^{cut/mva}$	23.5	20.5
$qqH\nu\nu\mu\mu^{cut/mva}$	45.3	37.0
$qqH\mu\mu\nu\nu^{cut/mva}$	52.4	44.4
Combined	8.34	7.89

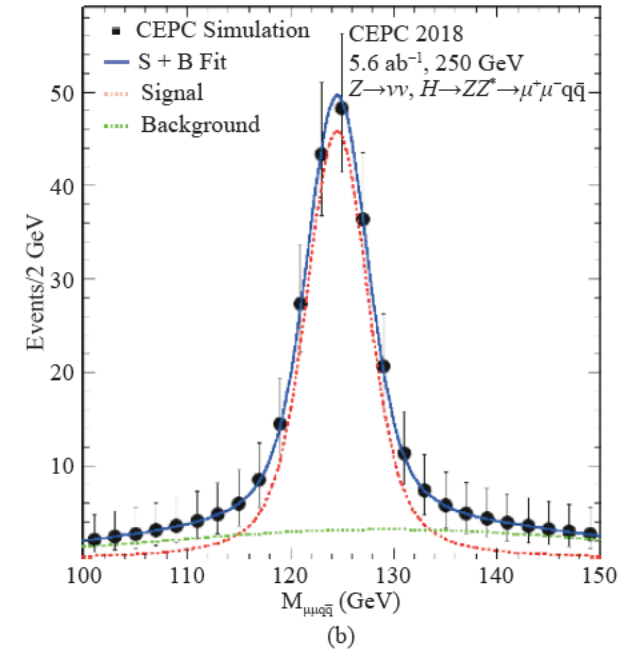
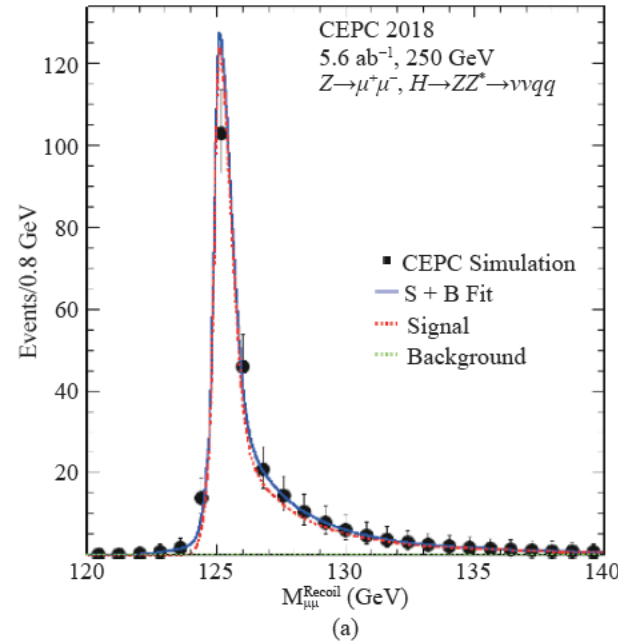


Figs. Recoil mass distribution from two best categories.

# H $\rightarrow$ ZZ\* part in the CEPC white paper

## Z $\rightarrow$ $\mu\mu$ , H $\rightarrow$ ZZ\* $\rightarrow$ $\nu\nu q\bar{q}$

- $M_{\mu\mu}$  : 80-100 GeV
- $M_{\mu\mu}^{\text{recoil}}$  : 120-160 GeV
- $M_{jj}$  : 10-38 GeV
- $P_t$  :  $> 10$  GeV



## Z $\rightarrow$ $\nu\nu$ , H $\rightarrow$ ZZ\* $\rightarrow$ $\ell^+\ell^- q\bar{q}$

- Visible Energy :  $< 180$  GeV
- $M_{\text{missing}}$  : 58-138 GeV
- Mass & pt cuts on lepton/jet pairs

Table 8. Expected relative precision for the  $\sigma(ZH) \times \text{BR}(H \rightarrow ZZ^*)$  measurement with an integrated luminosity 5.6 ab<sup>-1</sup>.

ZH final state		precision
Z $\rightarrow$ $\mu^+\mu^-$	H $\rightarrow$ ZZ* $\rightarrow$ $\nu\nu q\bar{q}$	7.2%
Z $\rightarrow$ $\nu\nu$	H $\rightarrow$ ZZ* $\rightarrow$ $\ell^+\ell^- q\bar{q}$	7.9%
combination		4.9%



# Comparison of results

	Precision from current analysis (cut-based)	Precision in the white paper <sup>#</sup>
$Z \rightarrow \mu\mu, H \rightarrow ZZ^* \rightarrow \nu\nu qq$	15.5%	7.2%
$Z \rightarrow \nu\nu, H \rightarrow ZZ^* \rightarrow \mu\mu qq$	11.9%	8.2% <sup>#</sup>
2 channels combined	9.43%	5.4%

<sup>#</sup> 7.9% in previous page is the combined results from  $Z \rightarrow \nu\nu, H \rightarrow ZZ^* \rightarrow \mu\mu qq$  &  $Z \rightarrow \nu\nu, H \rightarrow ZZ^* \rightarrow ee qq$  where the former precision of 8.2% is not separately shown in the white paper.

*there are certain discrepancy here . . .*

# Comparison of final recoil mass

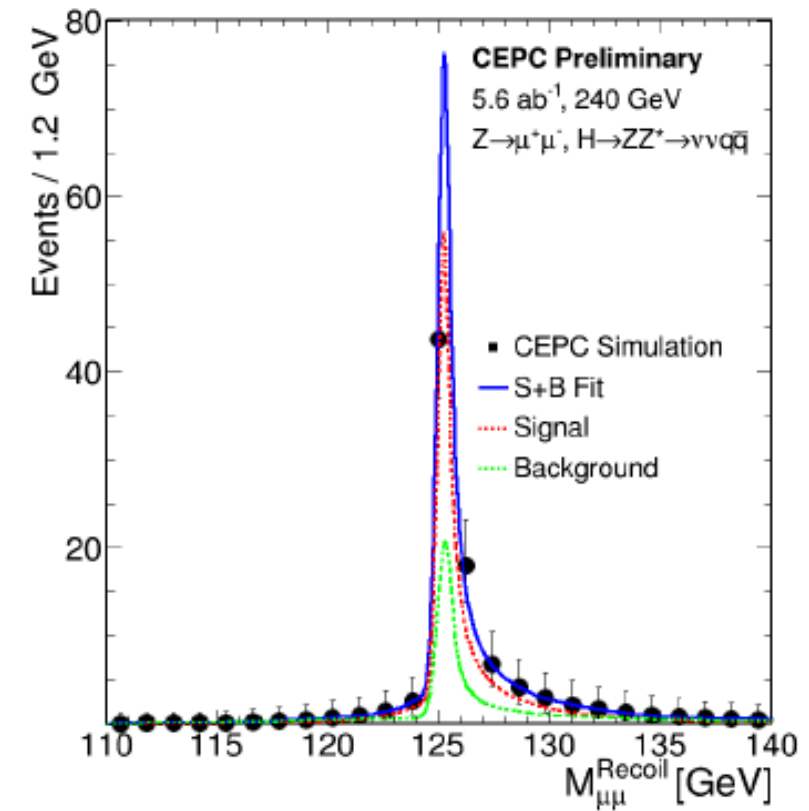
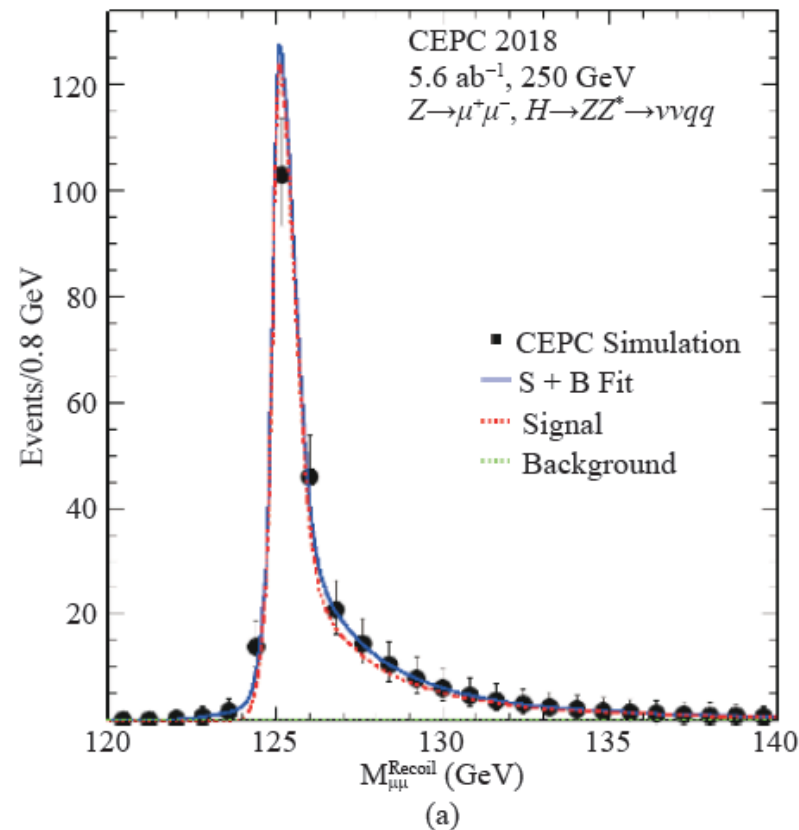
In comparison with the current analysis (left), the figure in the white paper (right) shows

Much larger signal events :

--  $N(\text{sig}) \sim 200$  (old)

--  $N(\text{sig}) \sim 60$  (current)

(smaller bg. events : )



# Number of events ?

- Using following numbers,

$$\text{-- } \sigma_{ZH}=204\text{fb, } L=5600 \text{ fb}^{-1}, \text{ BR}(H \rightarrow ZZ) = 2.64\%, \text{ BR}(Z \rightarrow qq) = 70\%, \text{ BR}(Z \rightarrow \nu\nu) = 70\%, \\ \text{BR}(Z \rightarrow \mu\mu) = 3.3\%$$

$$N( Z \rightarrow \mu\mu, H \rightarrow (Z \rightarrow \nu\nu, Z^* \rightarrow qq) ) = 139 \text{ events}$$



Number of signal of more than 200 is not what we expect, therefore, the possible scenarios would be,

1. The plot in the white paper is sum of 2 channel :  $(Z \rightarrow \nu\nu, Z^* \rightarrow qq) + (Z \rightarrow qq, Z^* \rightarrow \nu\nu)$  despite the requirement,  $M_{jj} : 10\text{-}38 \text{ GeV}$  , is described.
2. Something wrong with the scaling in the old result

# Ref: Situation of $Z \rightarrow \mu\mu$ , $H \rightarrow (Z \rightarrow qq, Z^* \rightarrow \nu\nu)$

- Background components for  $Z \rightarrow \mu\mu$ ,  $H \rightarrow (Z \rightarrow qq, Z^* \rightarrow \nu\nu)$  channel
  - $H \rightarrow bb$
  - $H \rightarrow WW$
  - $zz\text{-}sl0\mu\text{-}up/down$

There are huge background to this channel

##  $N(\text{sig}) \sim 50$  events

- Hard to bring the precision of this channel to the opposite one.

**Remaining background components (“cut-based”)**

name	scale	final
e2e2h_bb	0.21896	457
e2e2h_cc	0.011032	6
e2e2h_e3e3	0.023968	6
e2e2h_gg	0.0326888819557	2
e2e2h_ww	0.08176	312
e2e2h_zz	0.010024	7
e3e3h_zz	0.009968099681	2
qqh_e3e3	0.4844	4
qqh_zz	0.20216	14
zz_sl0mu_up	1.09032214858	125
zz_sl0mu_down	1.08025726079	386
zz_sl0tau_down	1.10887174477	4
ww_sl0muq	1.2235862395	6

# Other info. - 1

- Obtained precision in Yuqian's thesis is relatively close to current result.  
(But the thesis is published in 2017)

表 5.2 H->ZZ\*所有衰变末态中统计误差 > 20%的衰变道的统计结果

	信号事例数	信号效率	统计误差
$e^+e^- \nu\nu jj$	$65\pm 8$	50.1%	15.1%
$\mu^+\mu^- \nu\nu jj$	$88\pm 9$	67.3%	12.0%
$\nu\nu e^+e^- jj$	$43\pm 7$	27.6%	18.6%
$\nu\nu \mu^+\mu^- jj$	$90\pm 9$	57.4%	11.4%
$\nu\nu jj \mu^+\mu^-$	$77\pm 8$	49.7%	12.9%

- Root files to make the distribution in the white paper, lack the “weight” information, and weight=1 is assumed ( info. from Kaili )
- Background samples might only include the one which has large yield. ( info. from Kaili )

# Other info. - 2

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What is not in our analysis but is described in Yuqian's thesis :

- FSR correction
- LCFIPlus ( but no description of usage of tagging information in HZZ analysis is found )

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[ Short Summary ]

Although our analysis has a room to improve, not easy to reach the level in the white paper.

A possible scenario is that the old result was obtained by including very limited number of background events/components.

# H $\rightarrow$ ZZ\* precision from the other future colliders

- ILC

- $\Delta(\sigma \cdot \text{BR}(\text{HZZ}))/\sigma \cdot \text{BR}(\text{HZZ}) = 18\%$  with  $L=250 \text{ fb}^{-1}$  at 250 GeV

-  it is corresponding to  $\sim 5\%$  by scaling the number of ZH events to that of the CEPC

- Various HZZ final states are included in that estimation.

“ILC Higgs White Paper” arXiv:1310.0763

- FCC-ee

- $\Delta(\sigma \cdot \text{BR}(\text{HZZ}))/\sigma \cdot \text{BR}(\text{HZZ}) = 4.4\%$  with  $L=5 \text{ ab}^{-1}$  at 240 GeV

- No specific information about the HZZ final states analyzed is obtained yet.

Abada, A., Abbrescia, M., AbdusSalam, S.S. *et al.* FCC-ee: The Lepton Collider. *Eur. Phys. J. Spec. Top.* **228**, 261–623 (2019). <https://doi.org/10.1140/epjst/e2019-900045-4>

# Summary

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- $H \rightarrow ZZ^*$  decay is analyzed on the final state, having  $2\mu$ ,  $2\nu$ , and 2-jets.
- The final precision is obtained as 8.3% from the cut-based analysis and 7.9% from the BDT-based analysis.
- On the other hand, the past result in the white paper is  $\sim 5\%$  which shows discrepancy, and we do not have clear conditions(s) to account this difference yet.
- Any suggestions are welcome . *Thank you very much !*